

Spatial Analysis Results

2022-08-25

Models 1a-1c: 77 timepoints

- Model 1: Baseline intensity (assumed different) for each location plus two linear time components, beginning on respective intervention dates (school closure and state mandated stay-at-home-order)
 - a: Contact intensity between each pair of state borders is assumed to be different (termed distance model)
 - b: Contact intensity between each pair of state borders is assumed to be the same (CAR model)
 - c: Contact intensity between each pair of state borders is assumed to be different; the number of travelers between two locations (flow) increases with the locations' populations while decreases with the distance between them (gravity model)

Models 2a-2c: 184 timepoints

- Model 2: Baseline intensity (assumed different) for each location plus two linear time components, beginning on respective intervention dates (school closure and state mandated stay-at-home-order) and temporal basis splines of 3 degrees of freedom
 - a-c: Same as above

Models 3-4: 153 fitted timepoints, 297 missing/predicted timepoints (total: 450 timepoints)

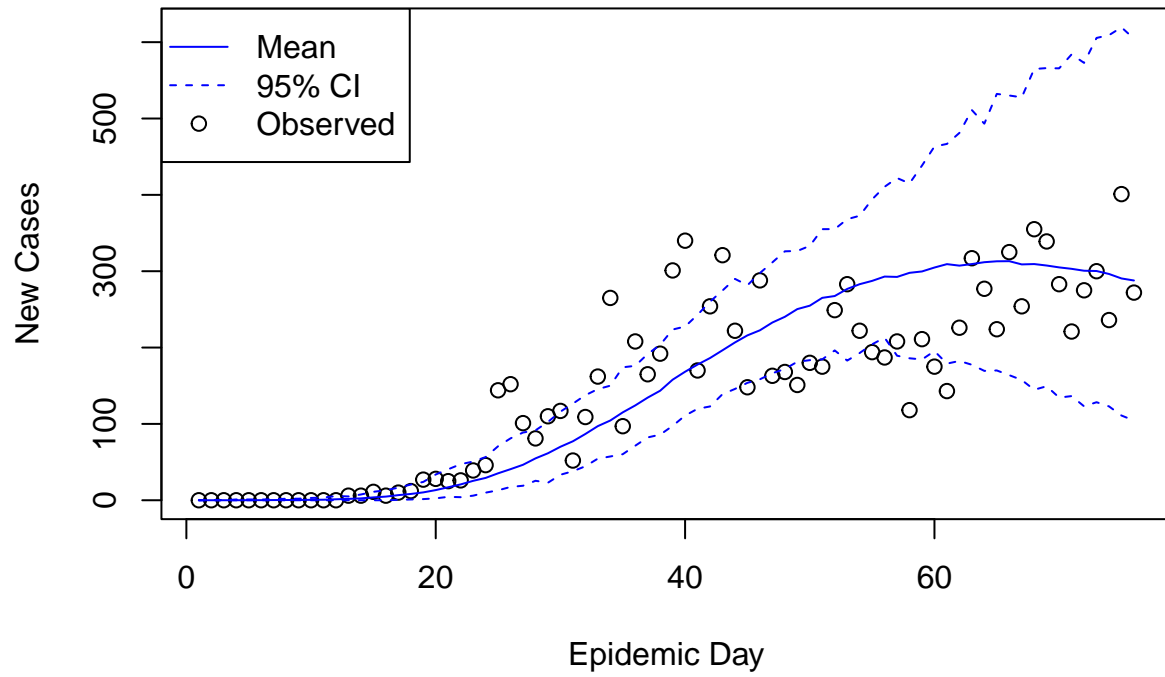
- Model 3: Baseline intensity (assumed different) for each location, a temporal basis splines of 3 degrees of freedom, the proportion of population vaccinated (at least one vaccine shot) and proportion fully vaccinated (all doses prescribed by the initial vaccination protocol) as recorded on 01/06/2021
- Model 4: Baseline intensity (assumed different) for each location, a temporal trigonometric term, the proportion of population vaccinated (at least one vaccine shot) and proportion fully vaccinated (all doses prescribed by the initial vaccination protocol) as recorded on 01/06/2021

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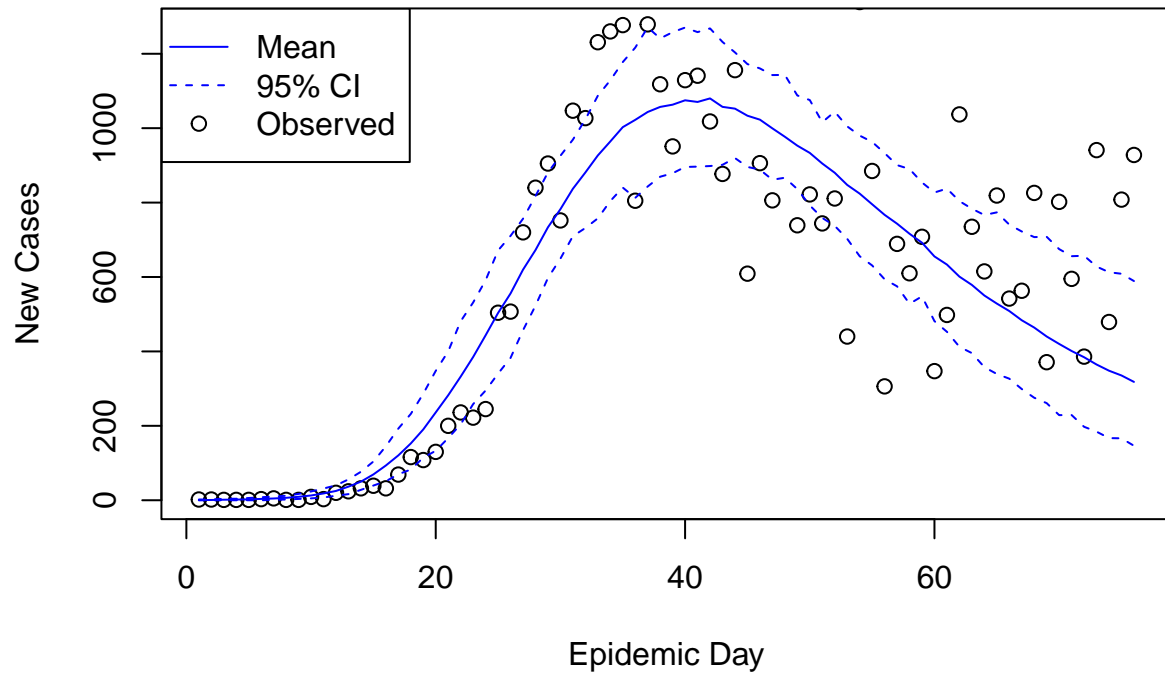
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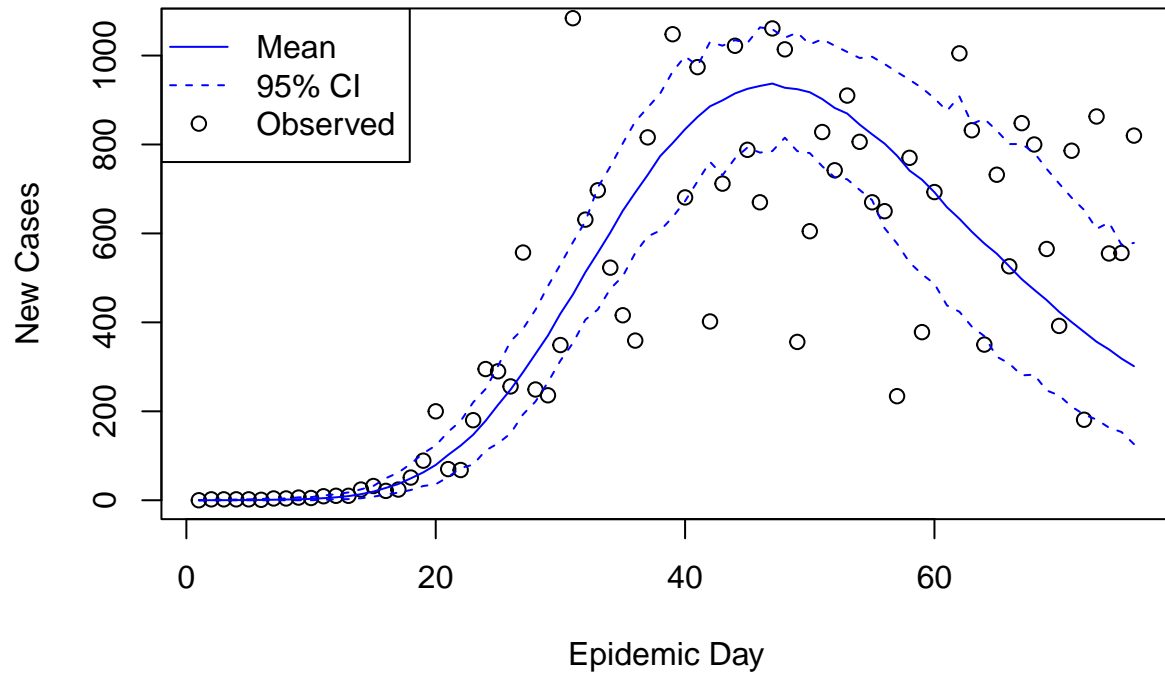
Model 1a: Posterior Distribution location ALABAMA



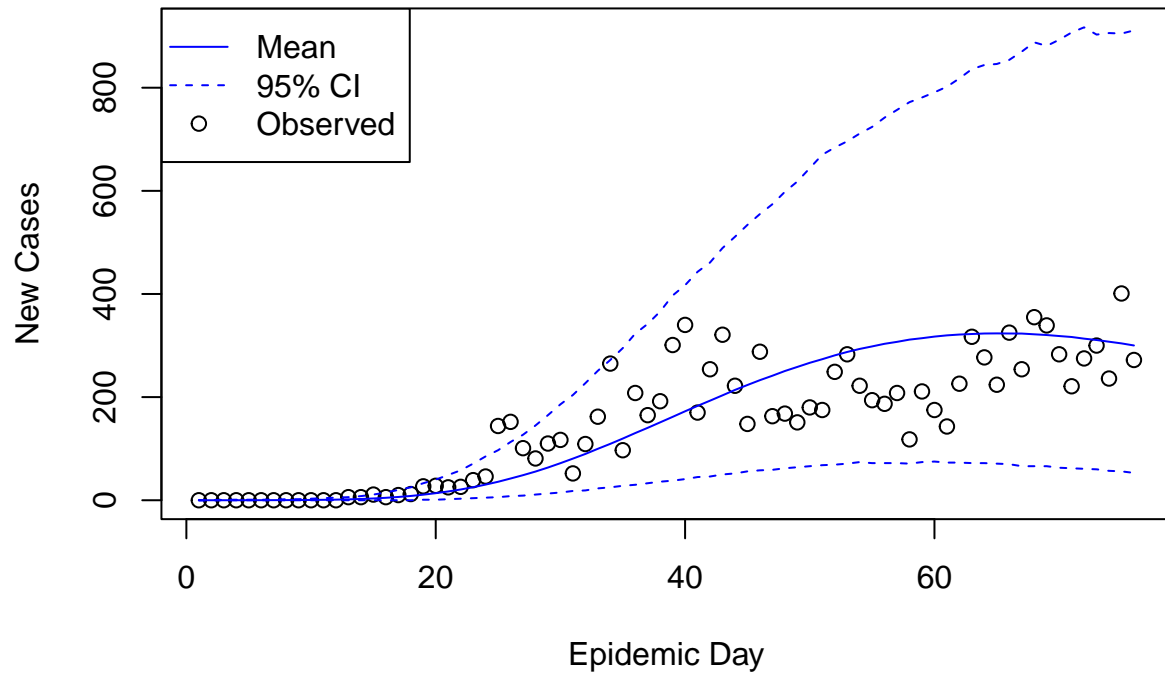
Model 1a: Posterior Distribution location FLORIDA



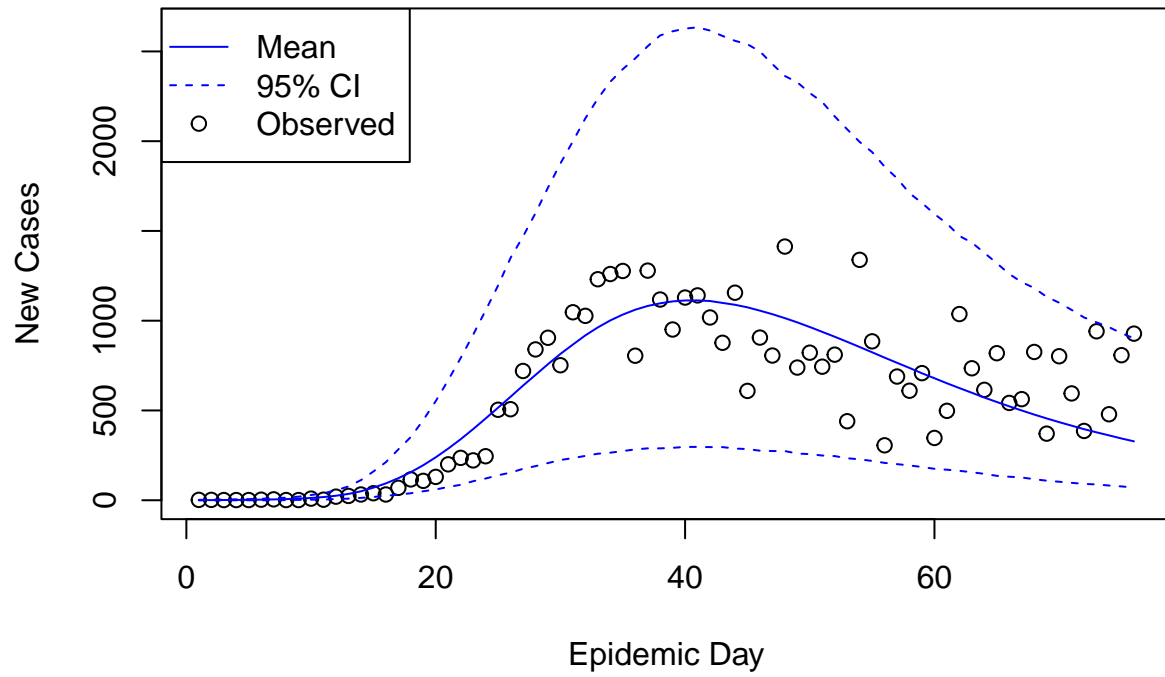
Model 1a: Posterior Distribution location GEORGIA



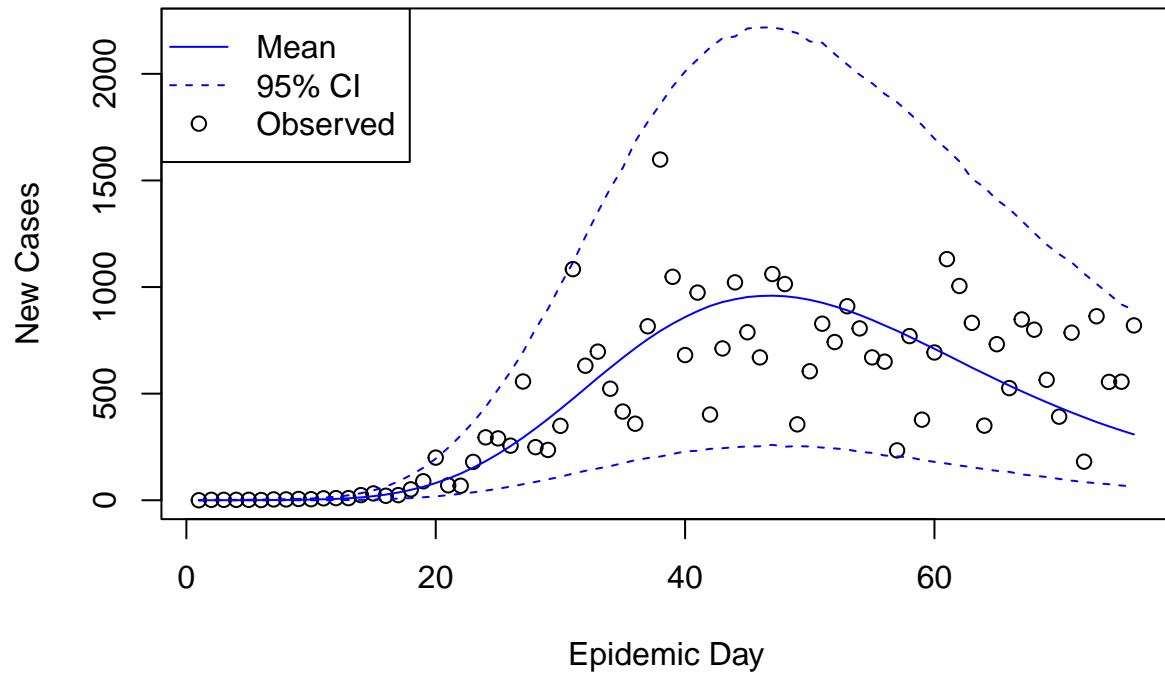
Model 1a: Posterior Predictive Distribution location ALABAMA



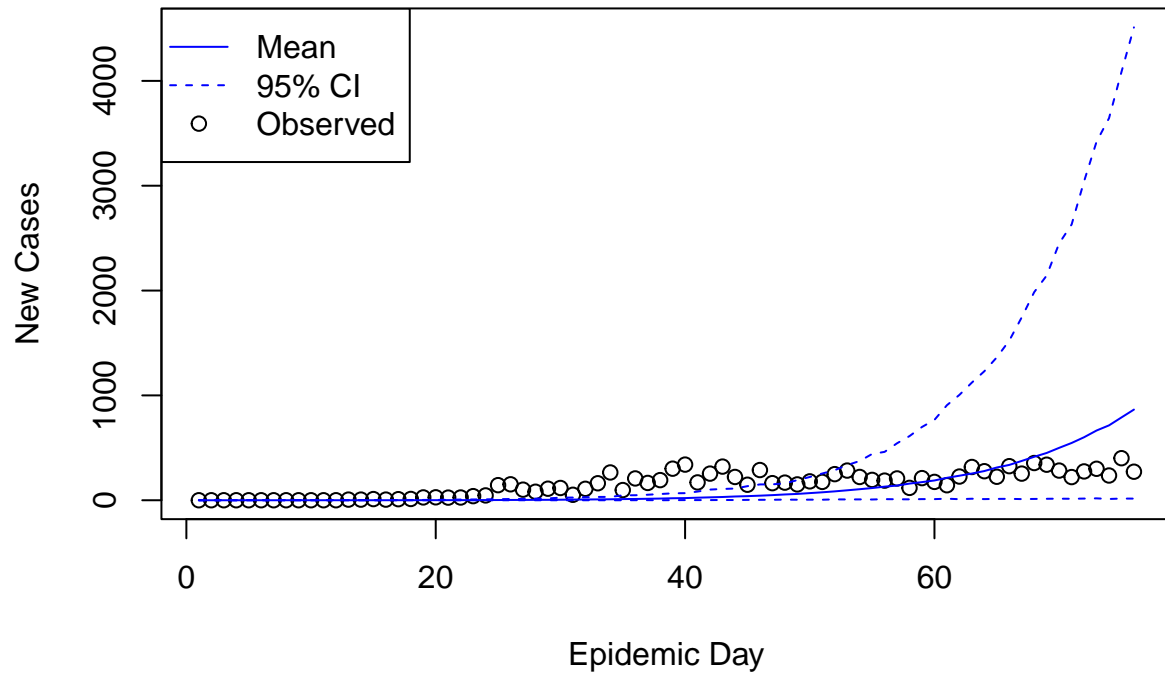
Model 1a: Posterior Predictive Distribution location FLORIDA



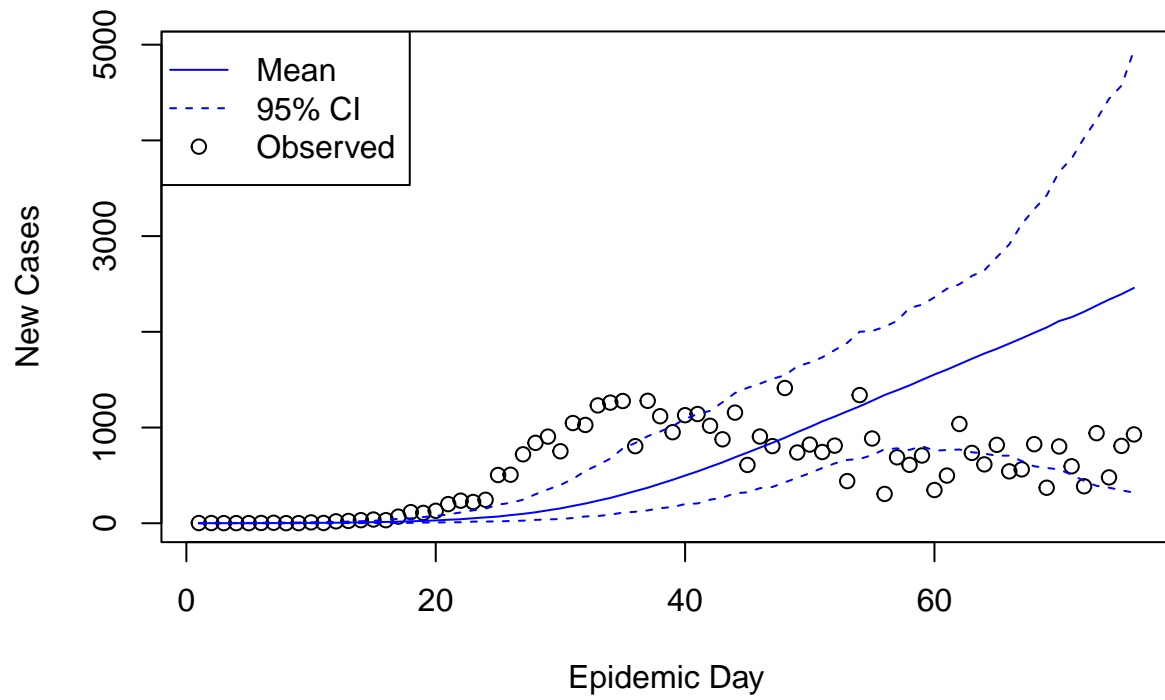
Model 1a: Posterior Predictive Distribution location GEORGIA



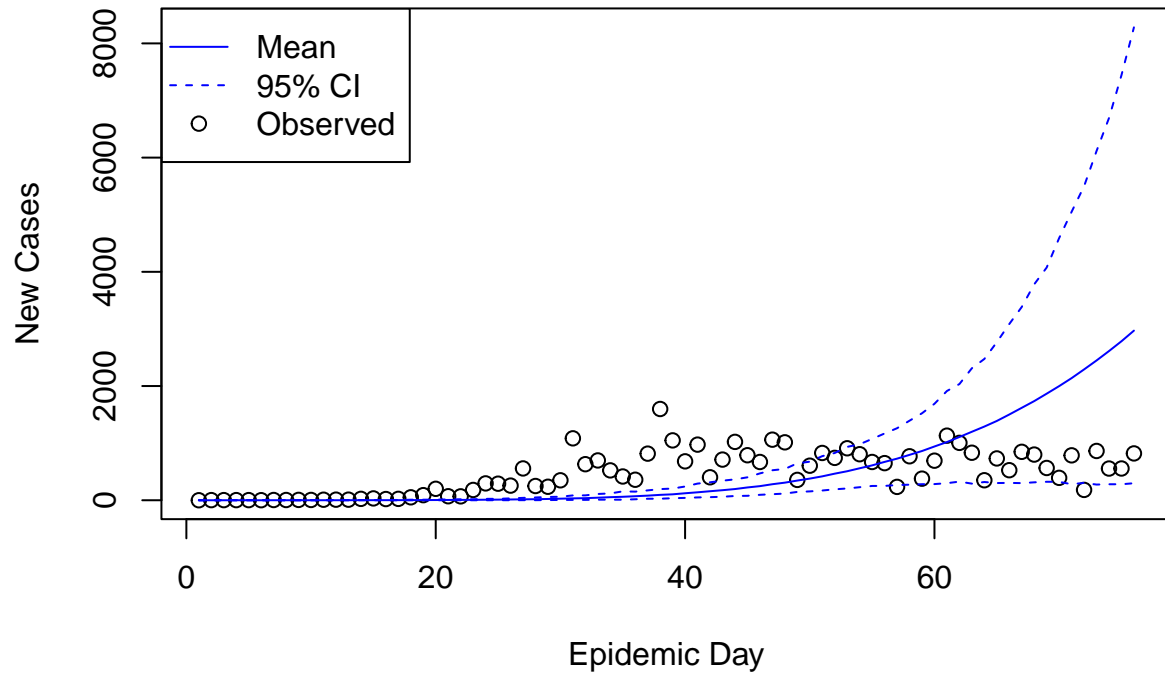
Model 1a (Basic ABC): Posterior Distribution location ALABAMA



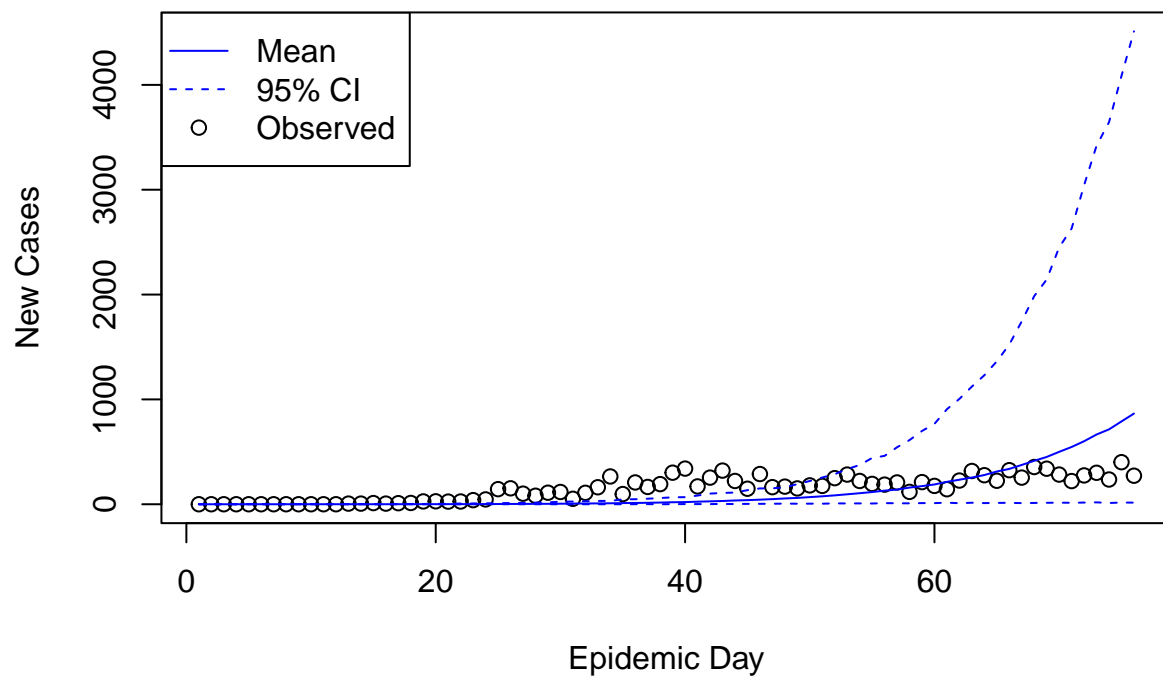
Model 1a (Basic ABC): Posterior Distribution location FLORIDA



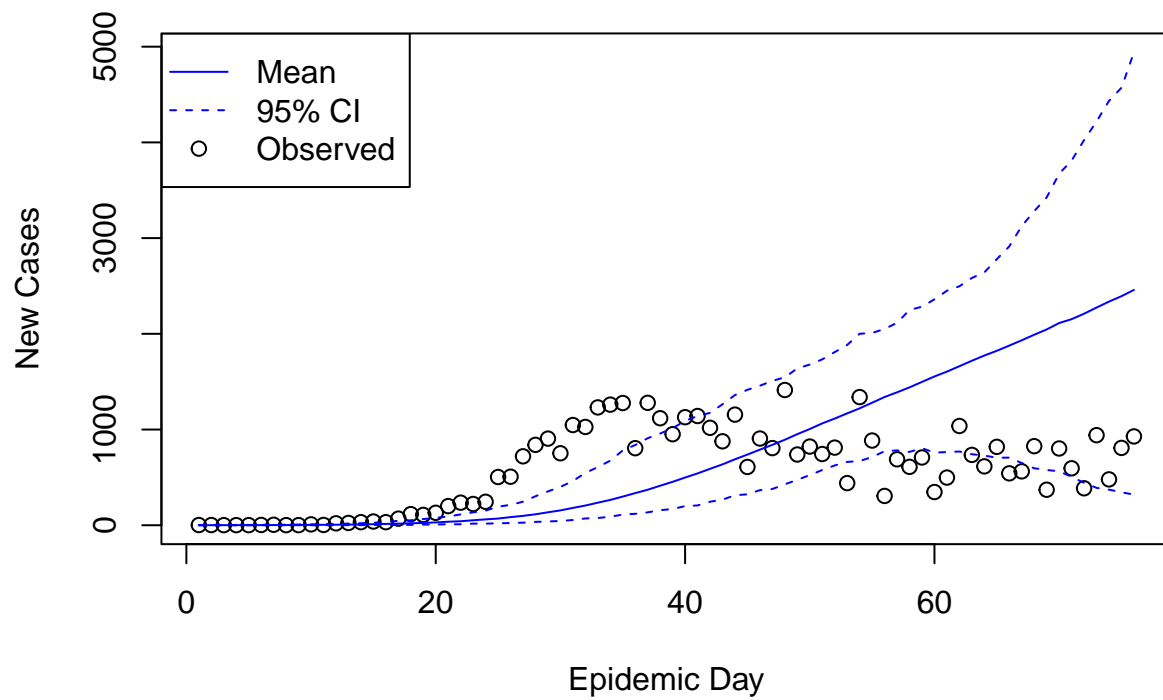
Model 1a (Basic ABC): Posterior Distribution location GEORGIA



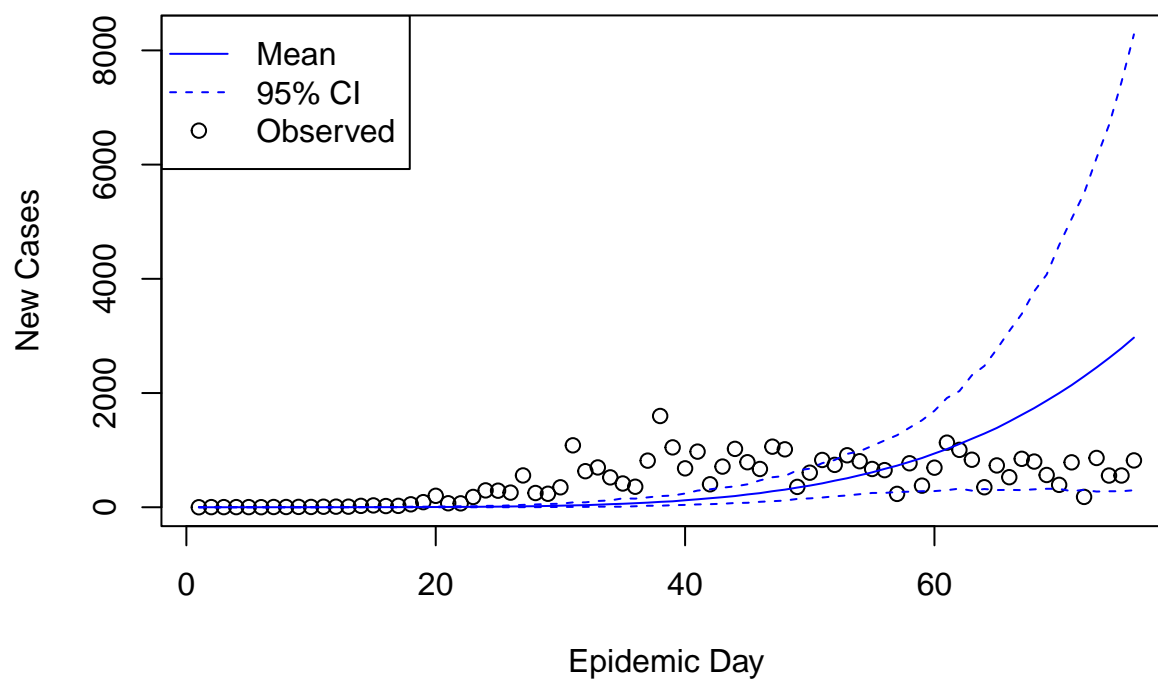
Model 1a (Basic ABC): Posterior Predictive Distribution location ALABAMA



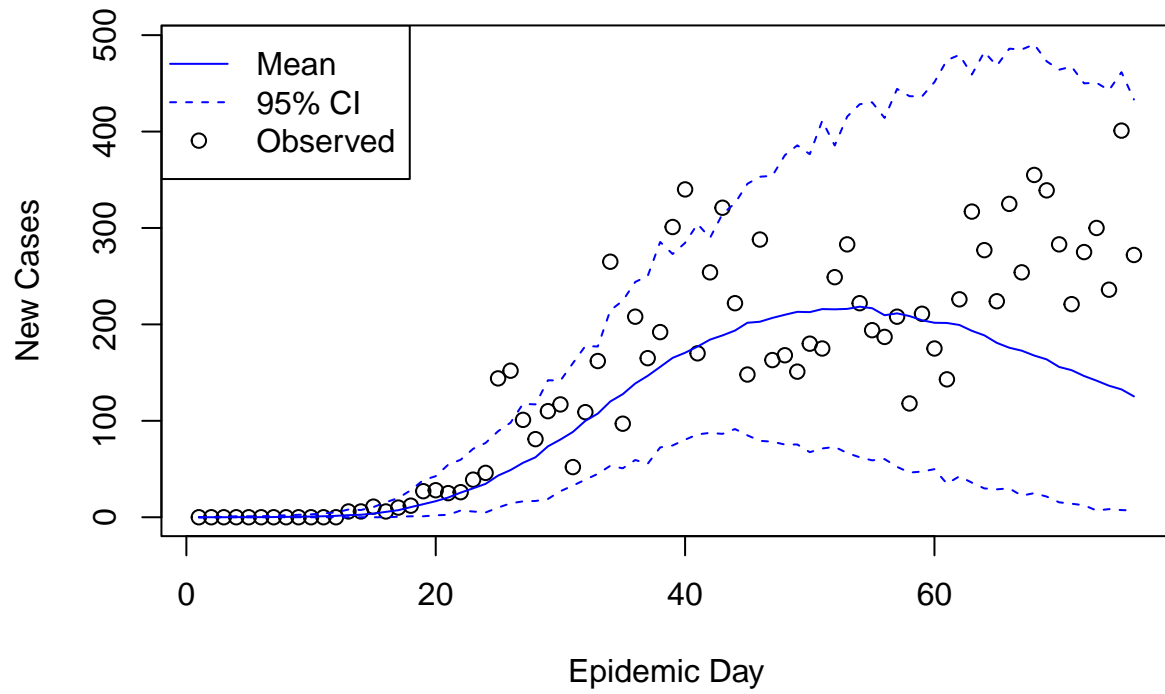
Model 1a (Basic ABC): Posterior Predictive Distribution location FLORIDA



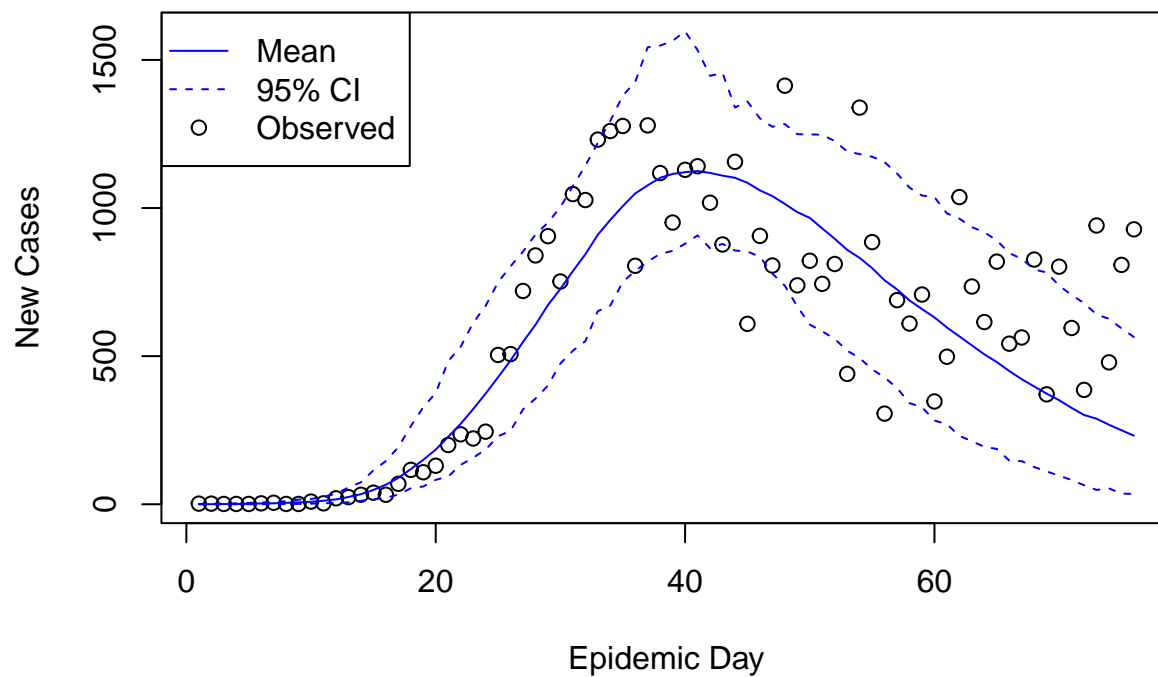
Model 1a (Basic ABC): Posterior Predictive Distribution location GEORGIA



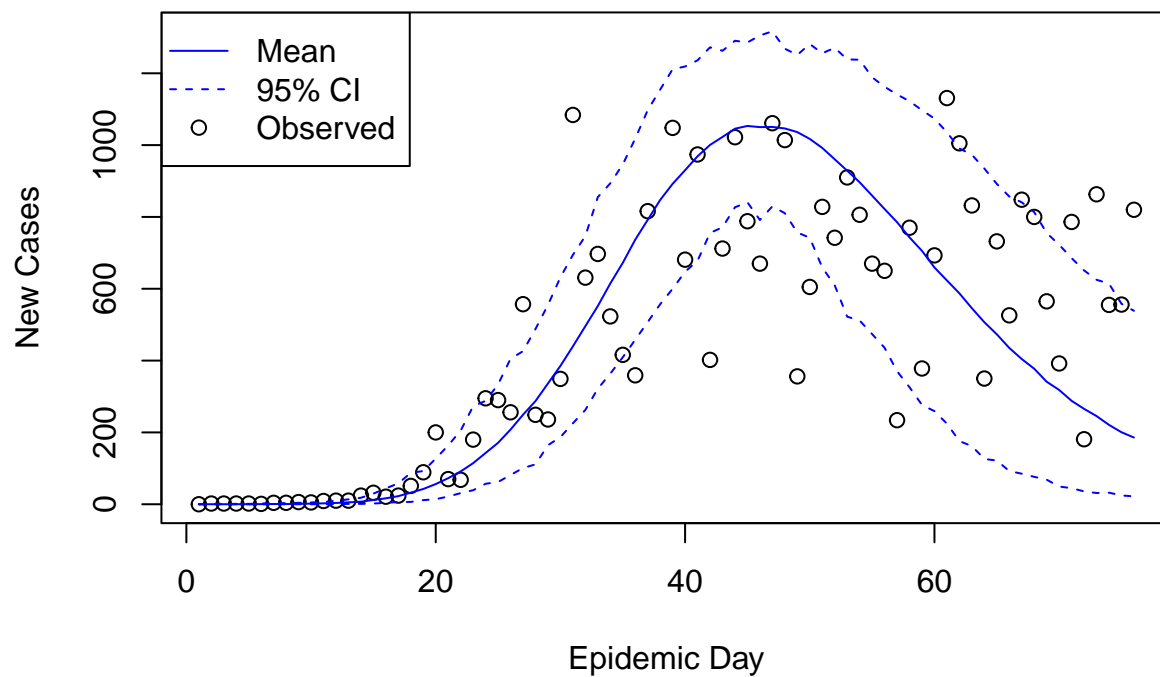
Model 1a (Weibull Distribution): Posterior Distribution location ALABAMA



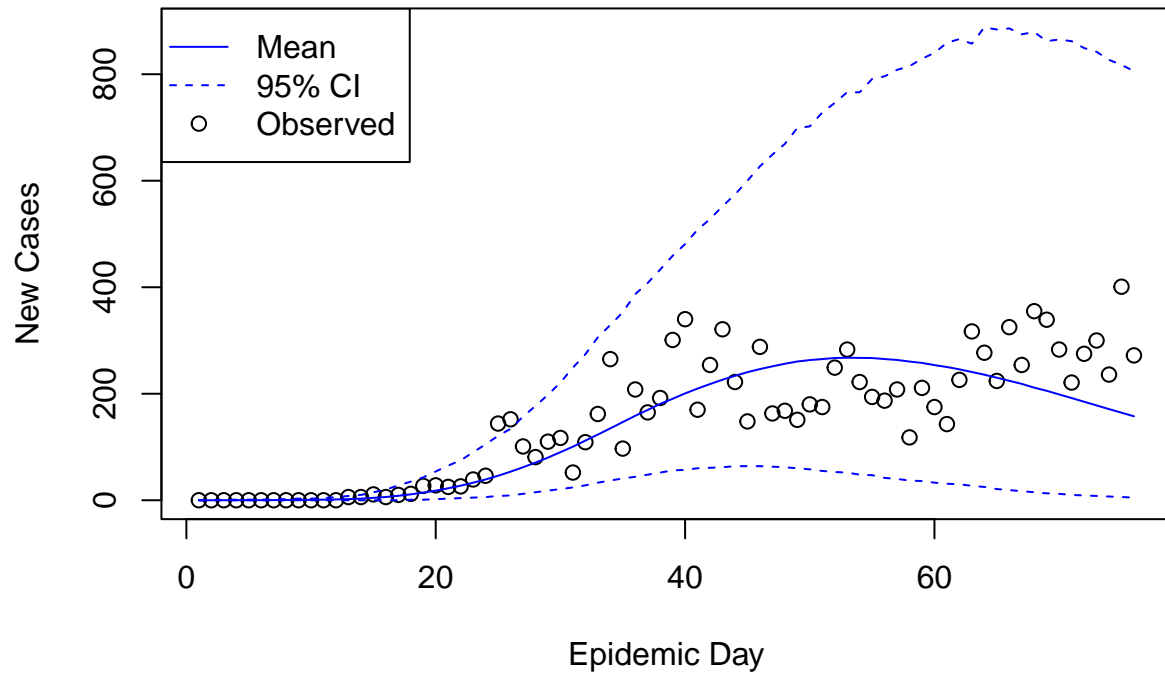
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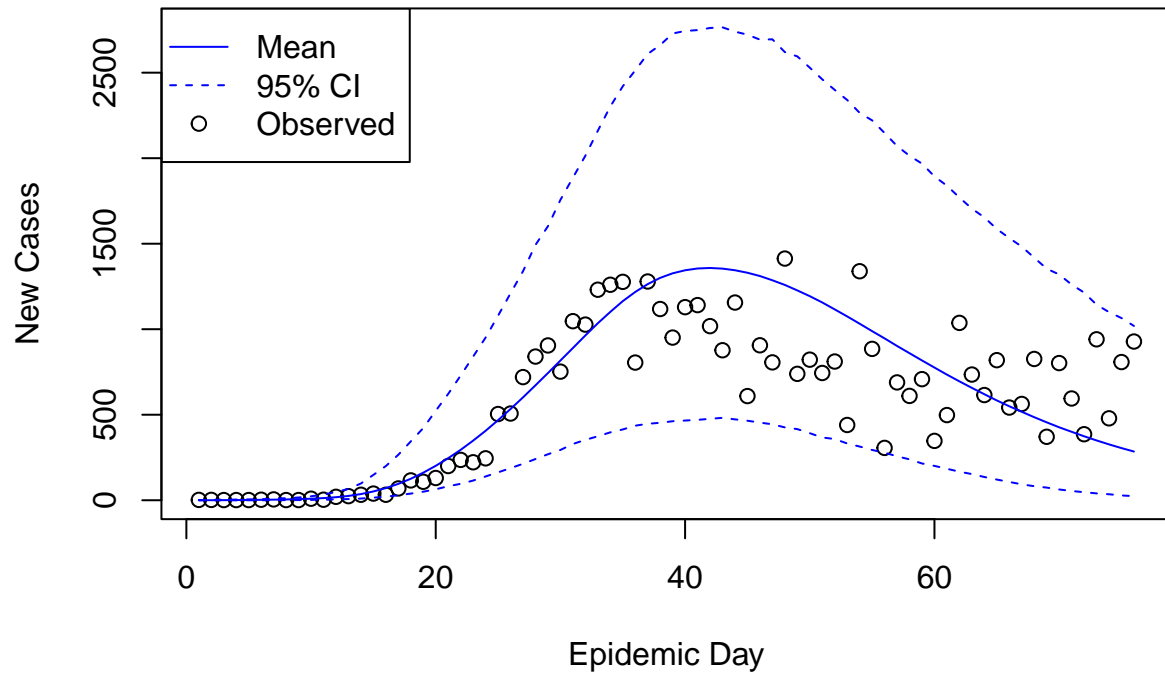
Model 1a (Weibull Distribution): Posterior Distribution location GEORGIA



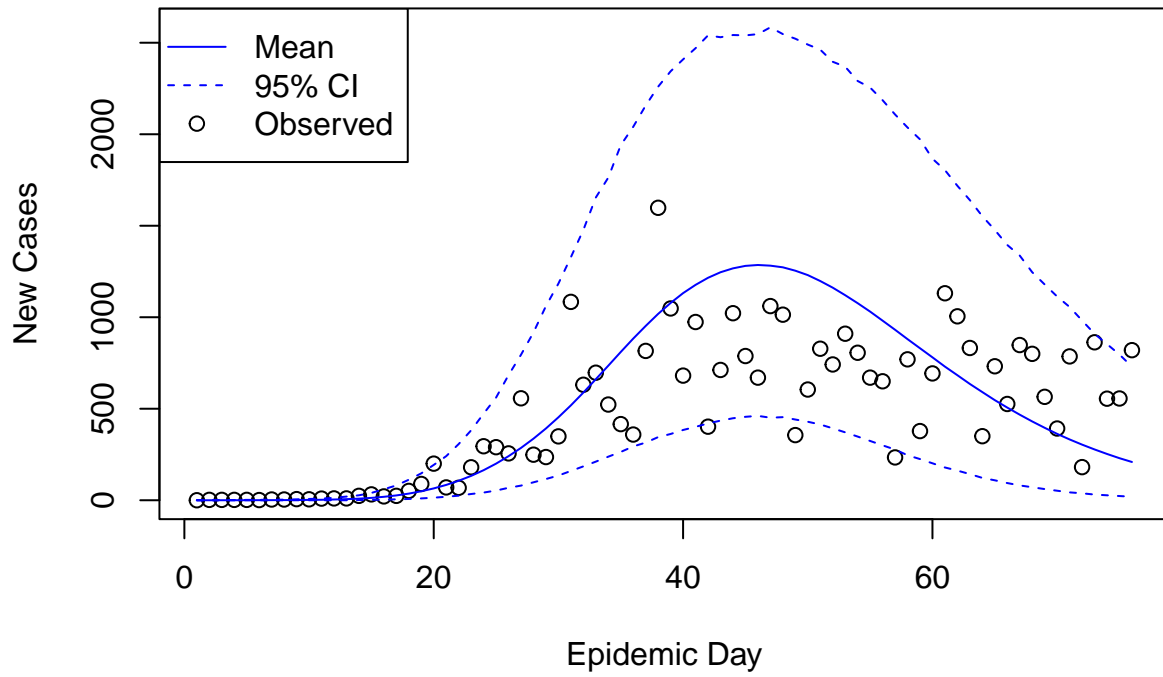
Model 1a (Weibull Distribution): Posterior Predictive Distribution location ALABAMA



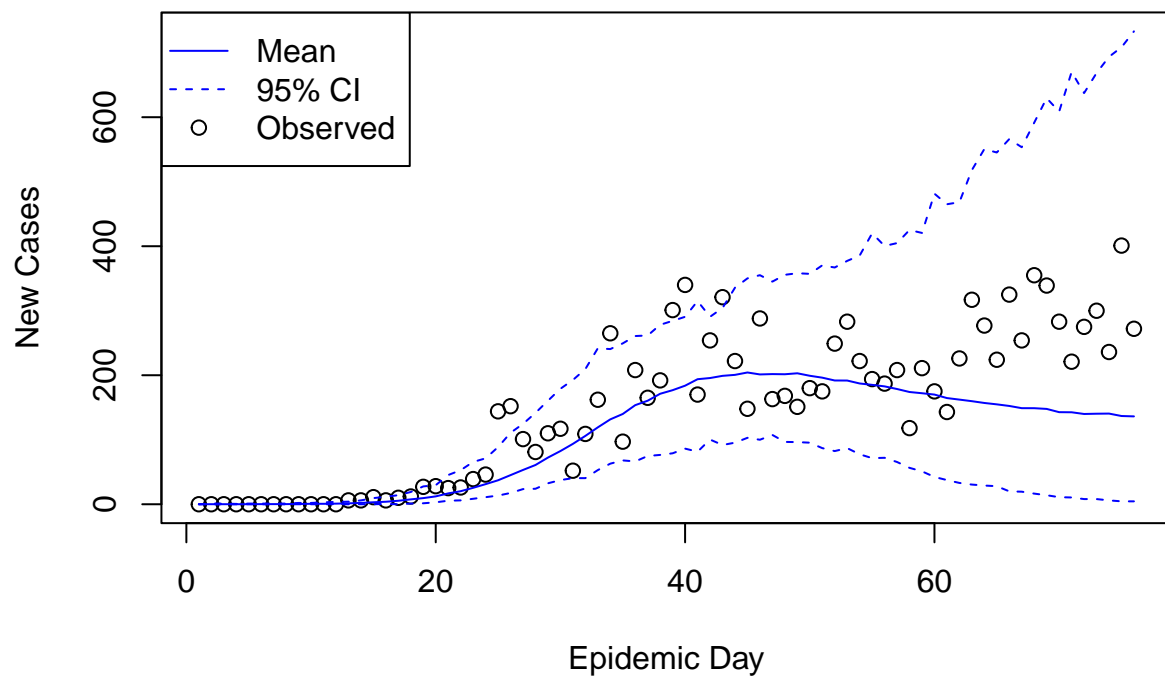
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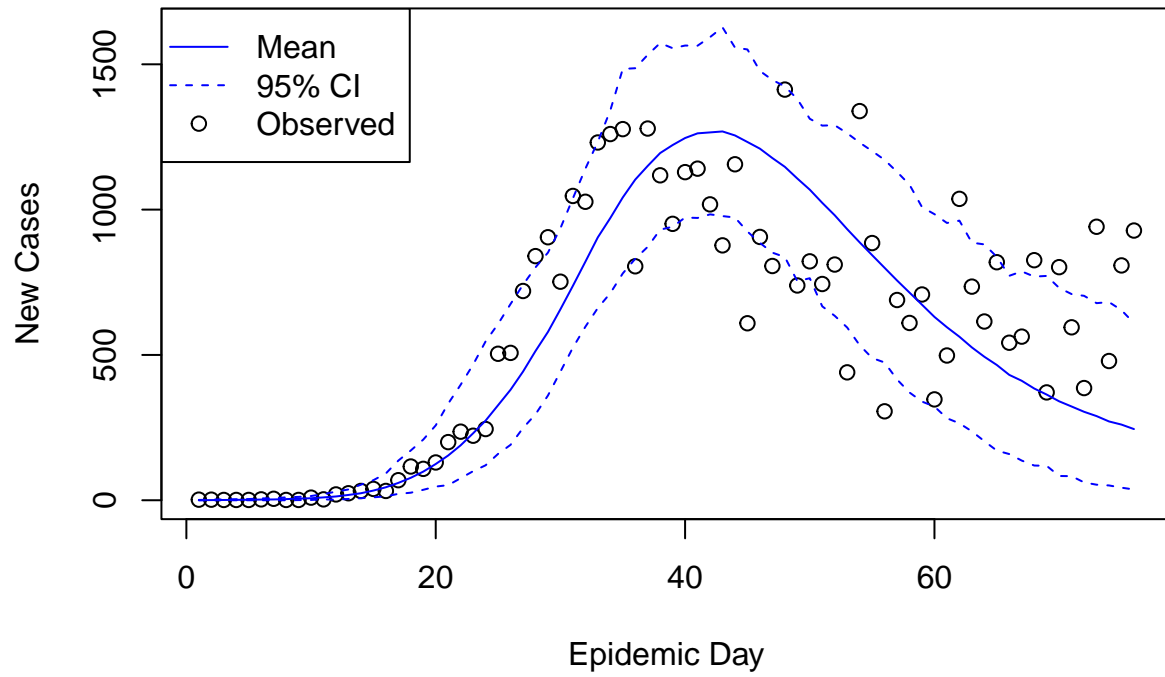
Model 1a (Weibull Distribution): Posterior Predictive Distribution location GEORGIA



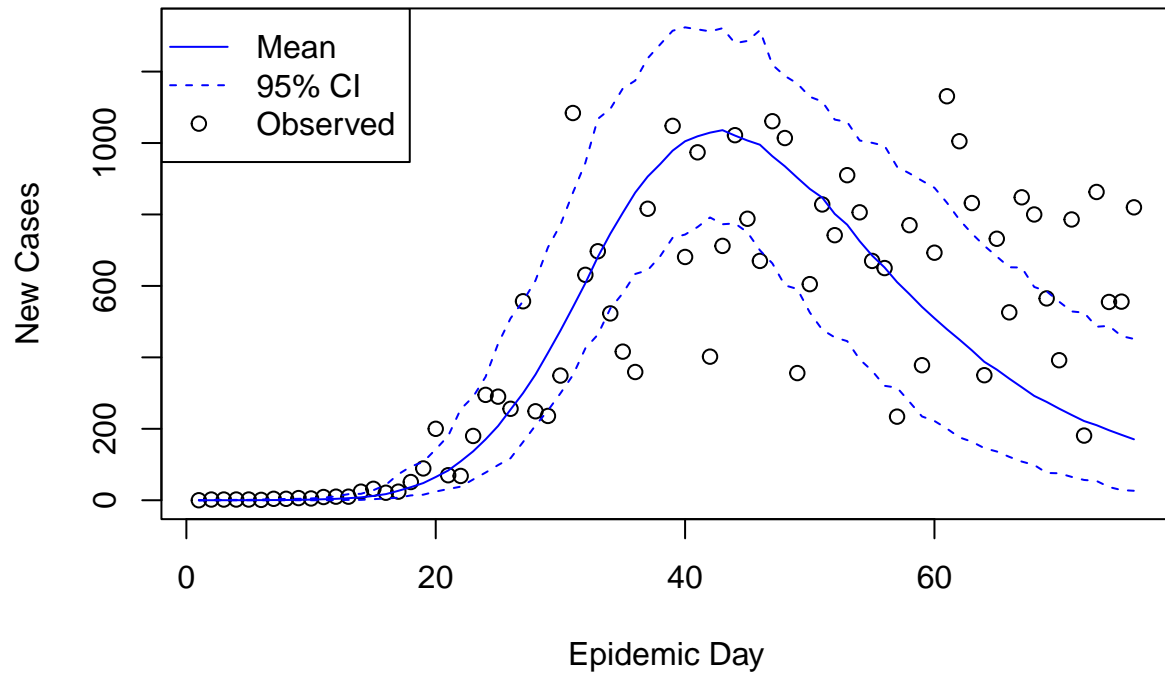
Model 1b: Posterior Distribution location ALABAMA



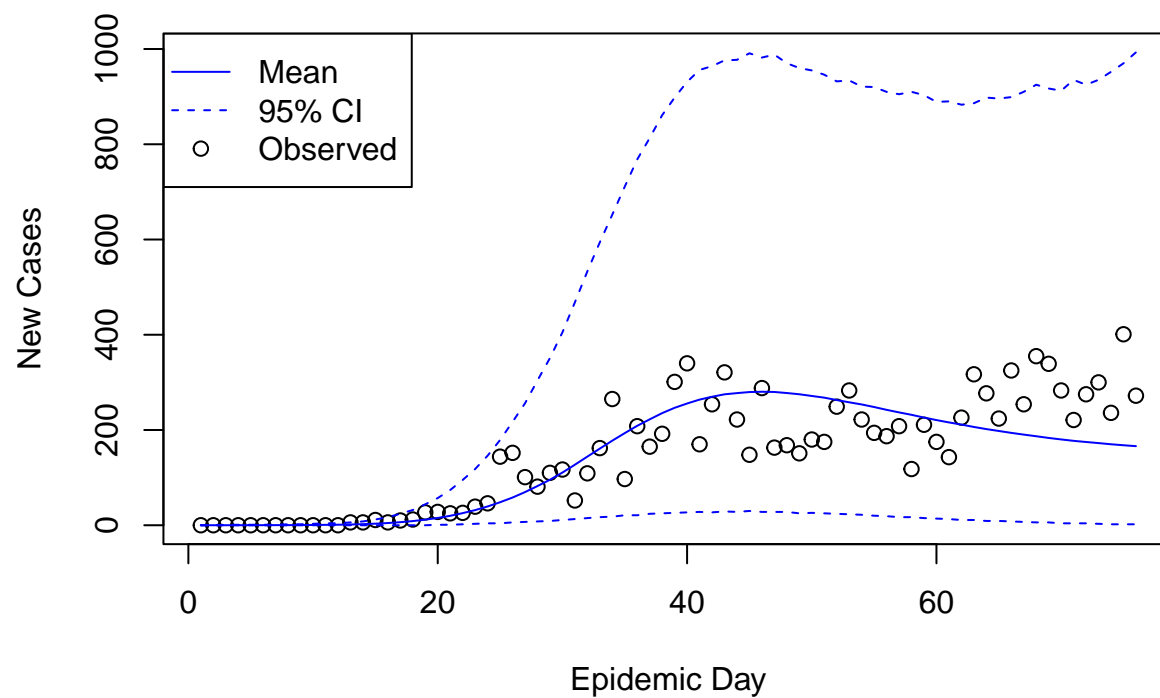
Model 1b: Posterior Distribution location FLORIDA



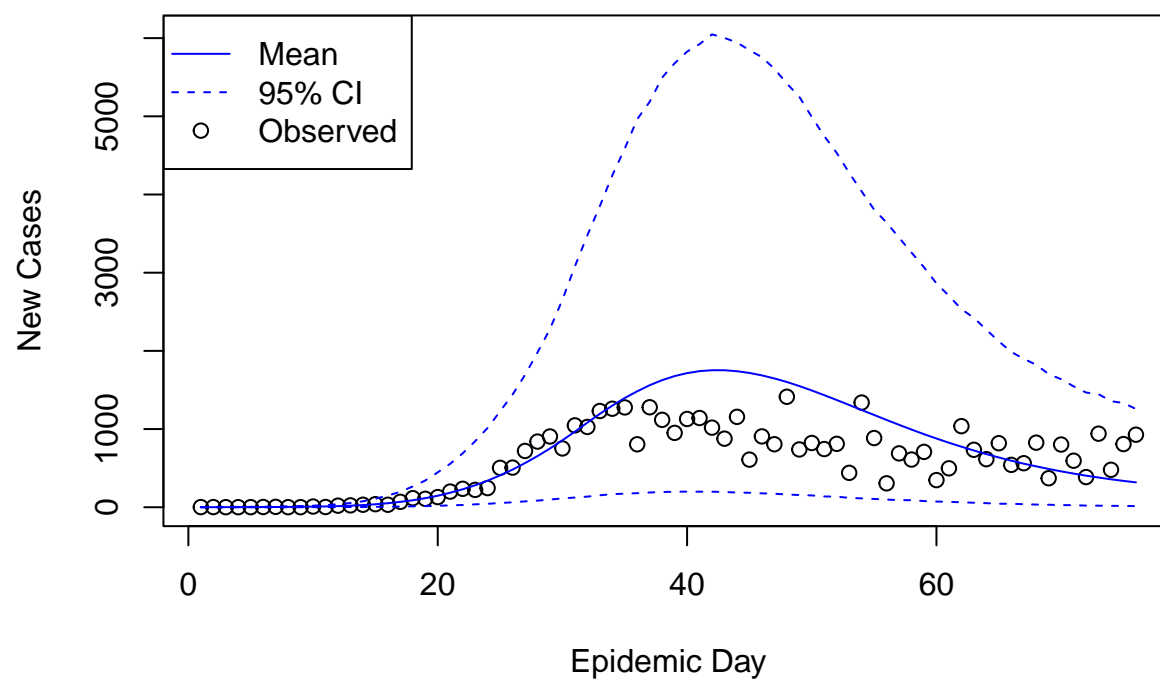
Model 1b: Posterior Distribution location GEORGIA



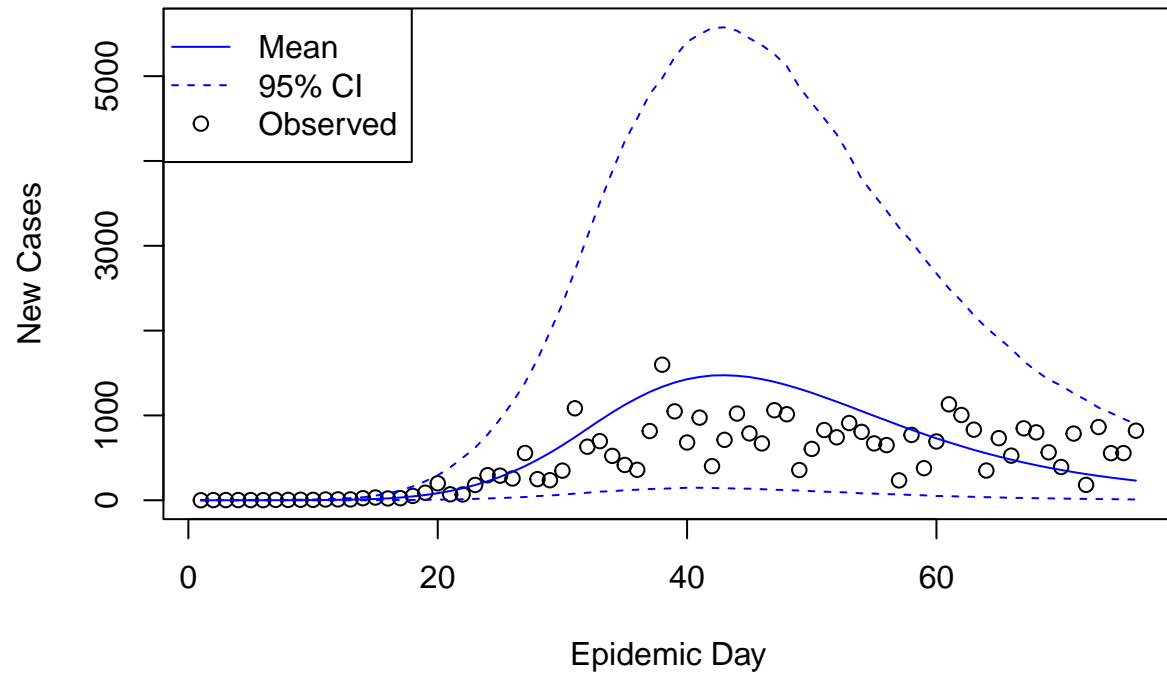
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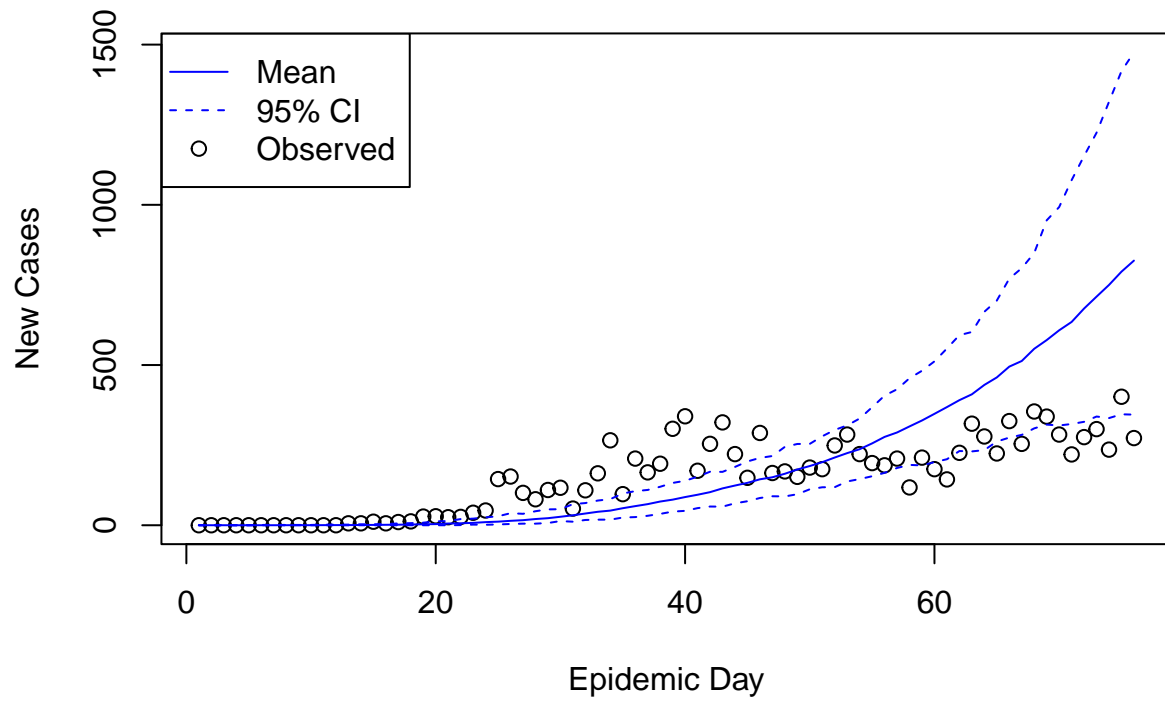
Model 1b: Posterior Predictive Distribution location FLORIDA



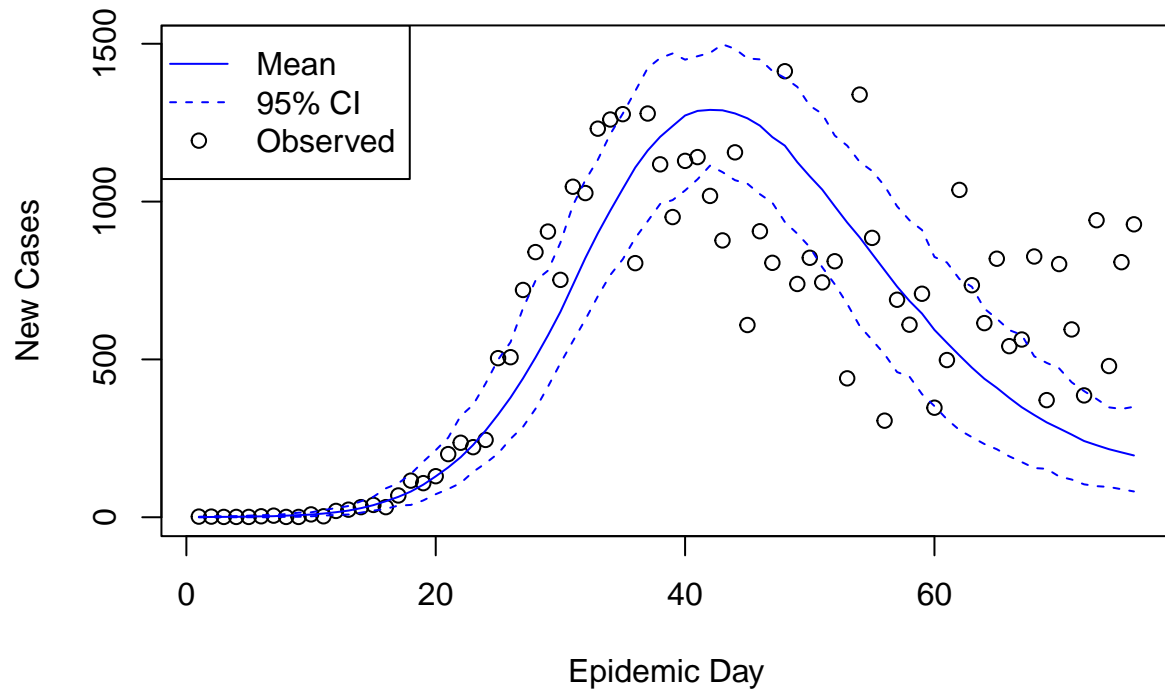
Model 1b: Posterior Predictive Distribution location GEORGIA



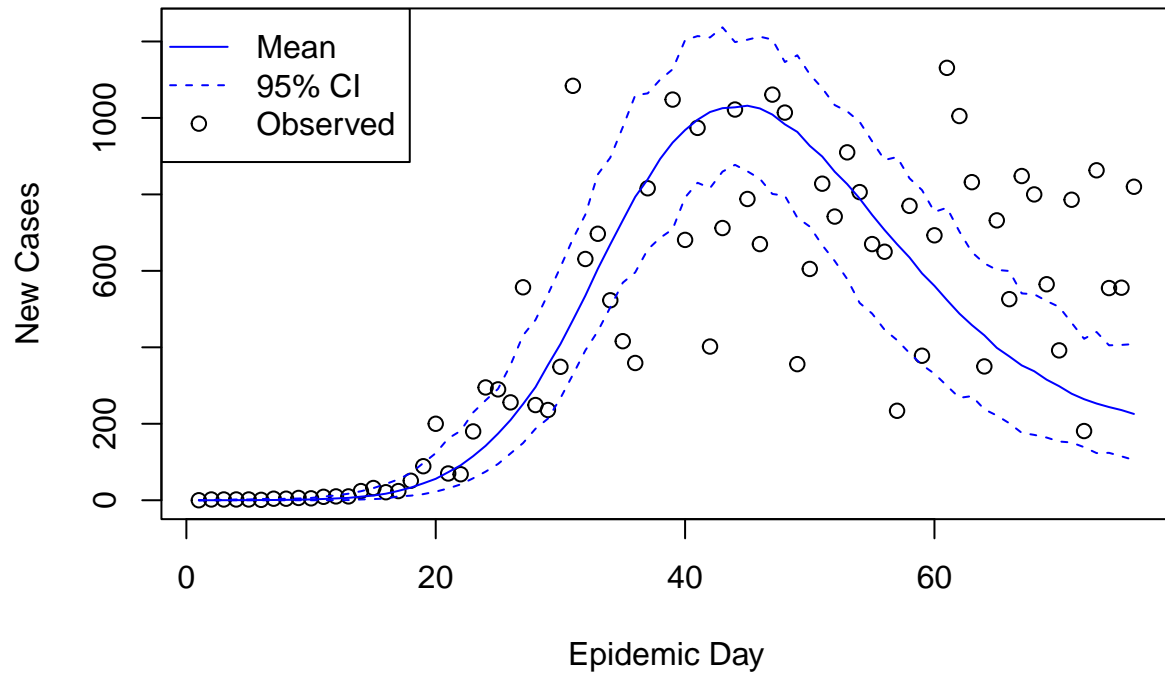
Model 1c: Posterior Distribution location ALABAMA



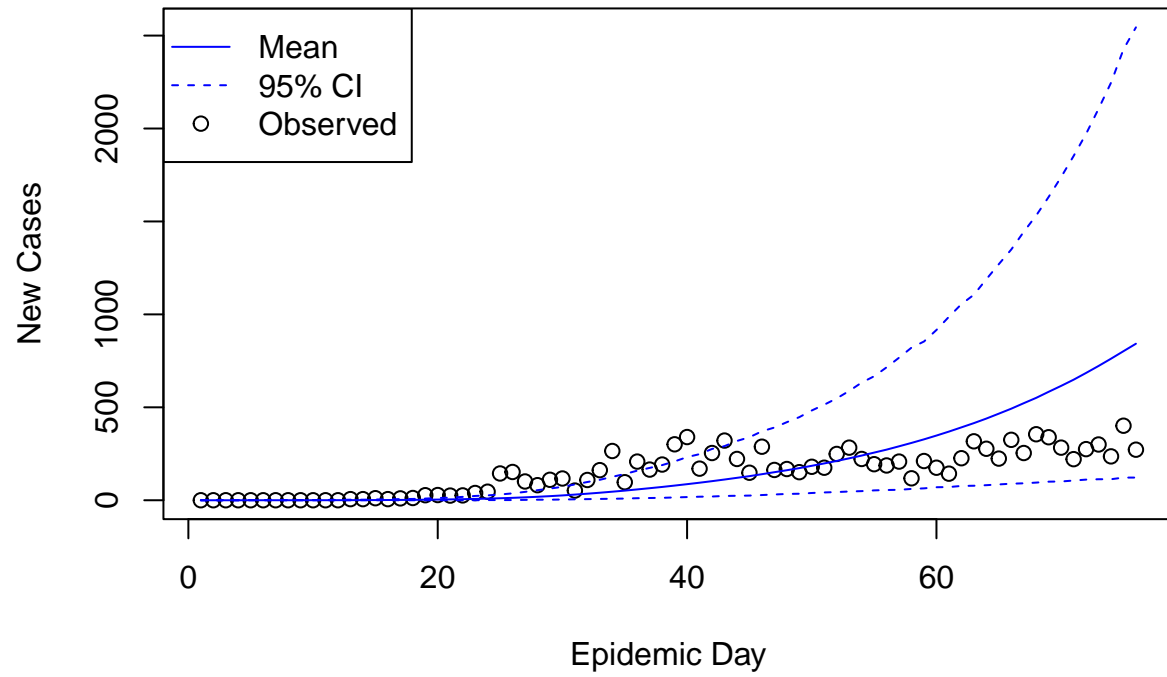
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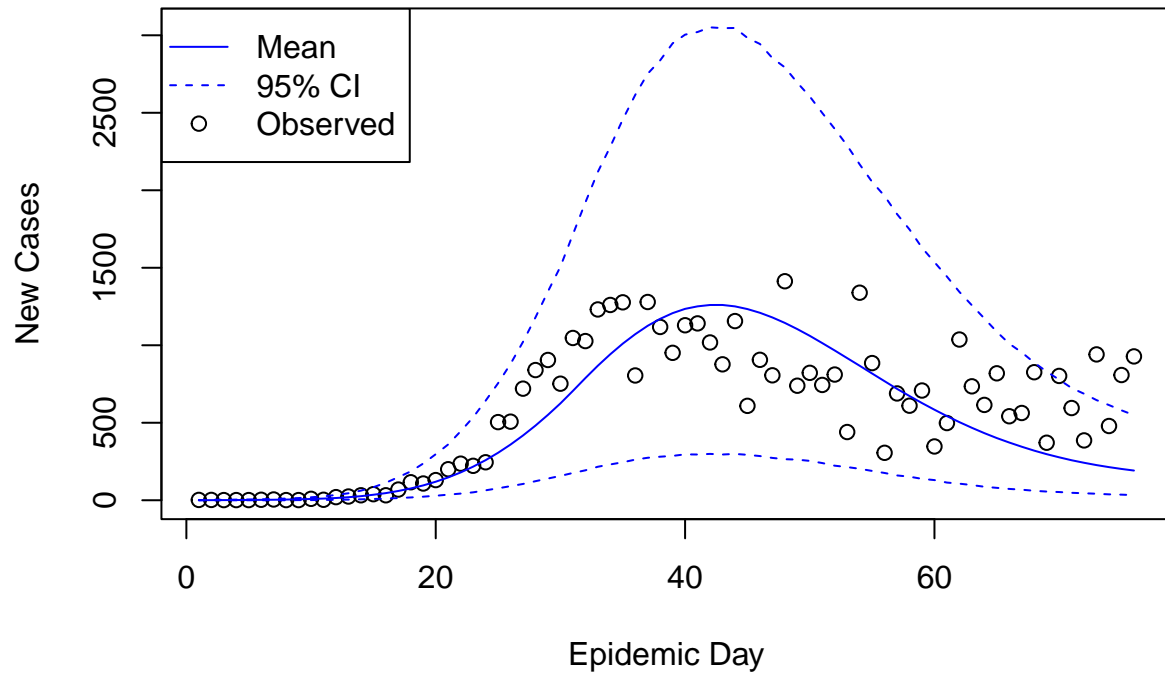
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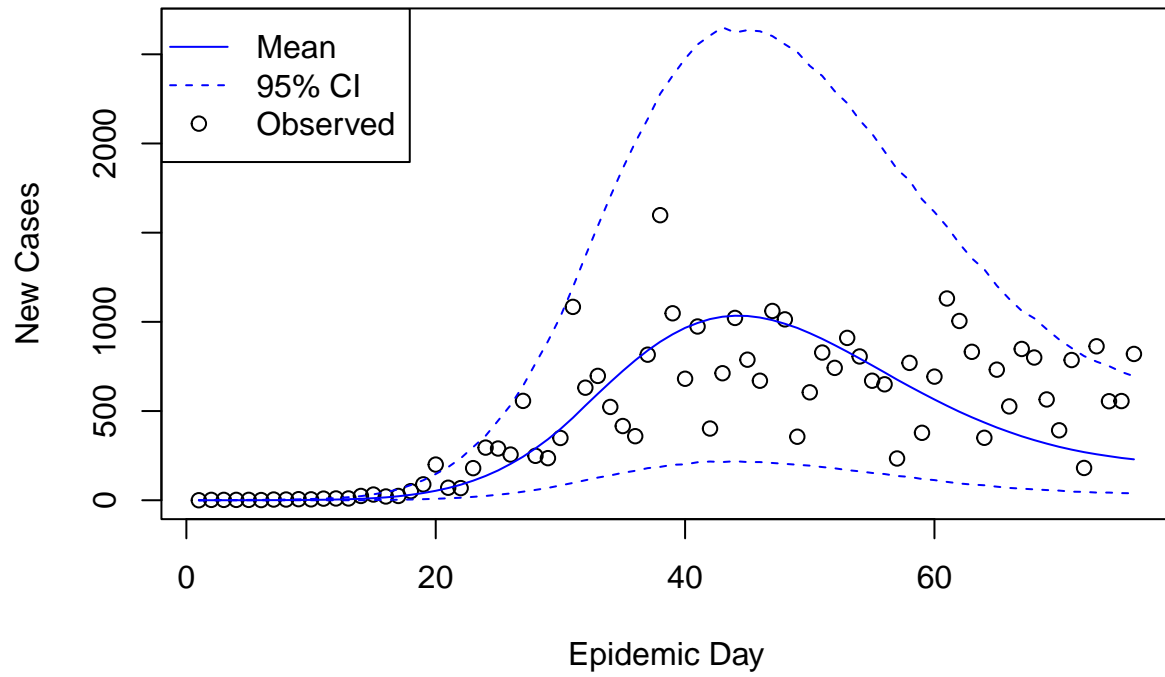
Model 1c: Posterior Predictive Distribution location ALABAMA



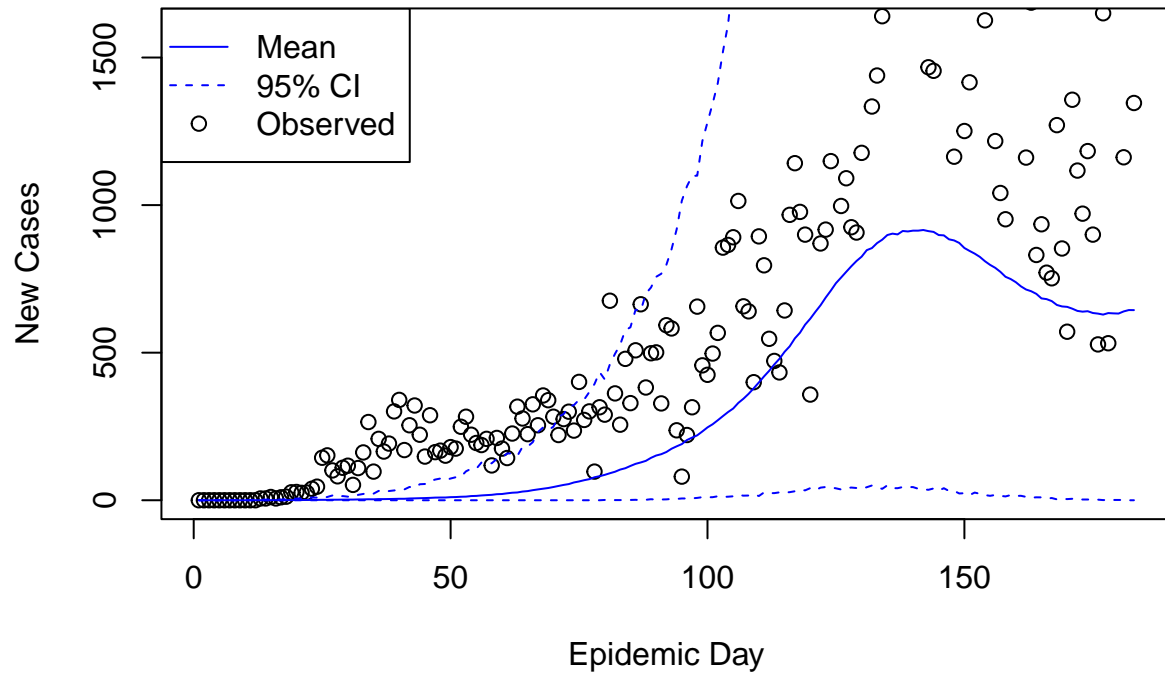
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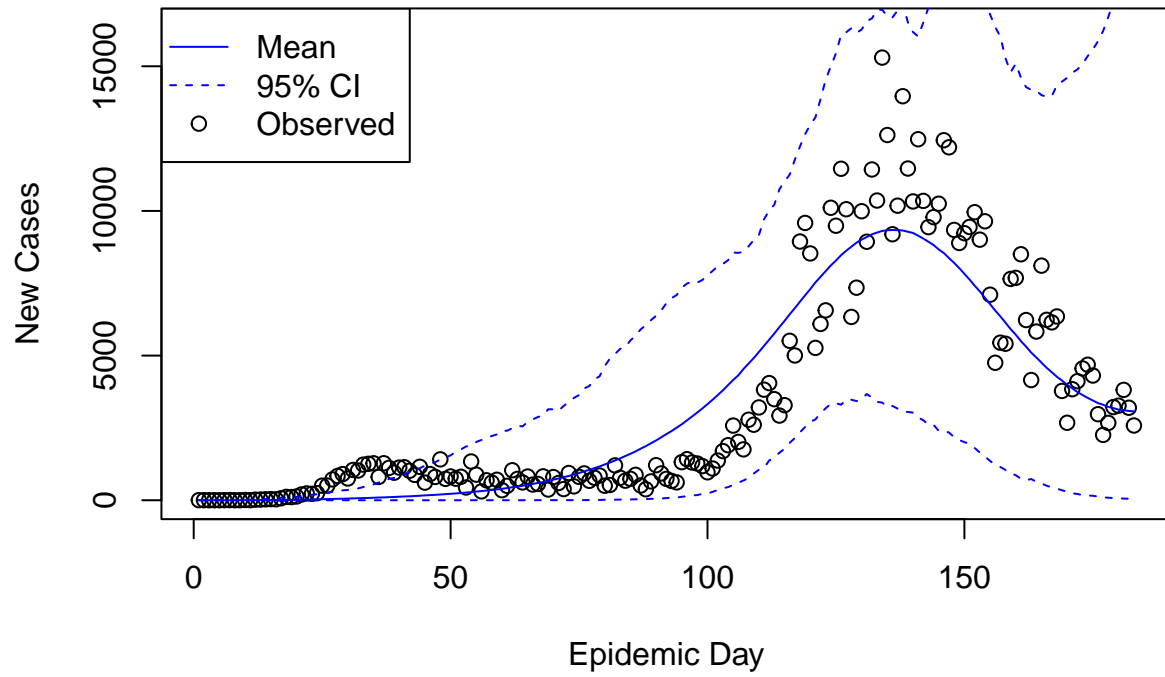
Model 1c: Posterior Predictive Distribution location GEORGIA



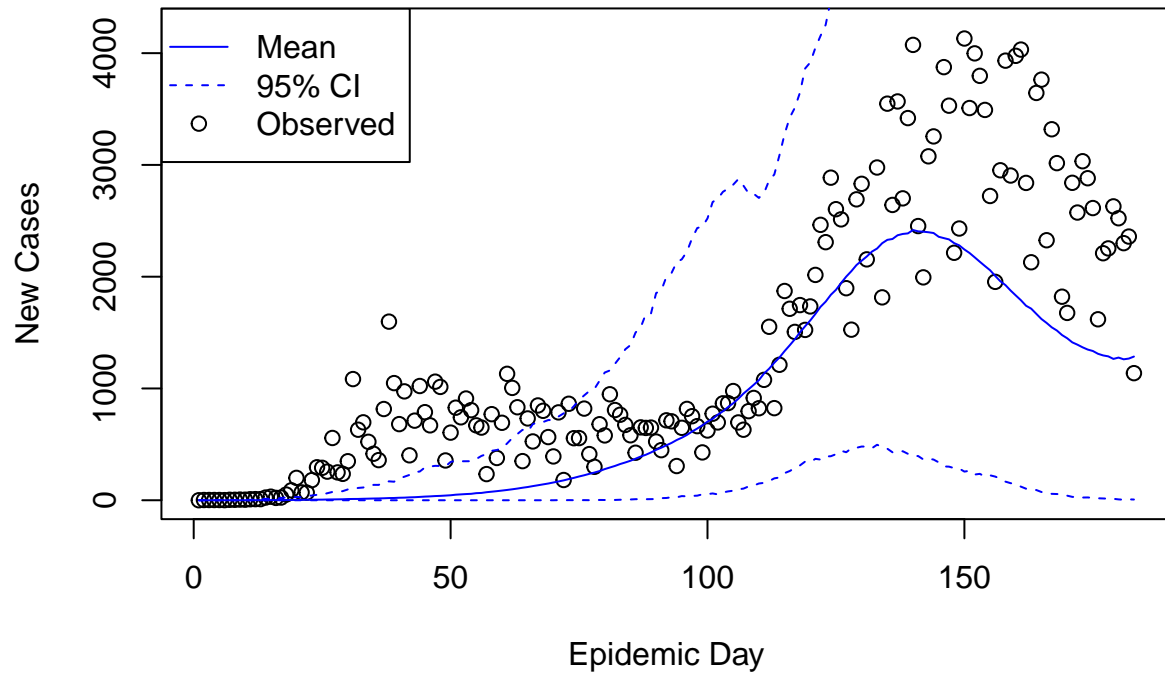
Model 2a: Posterior Distribution location ALABAMA



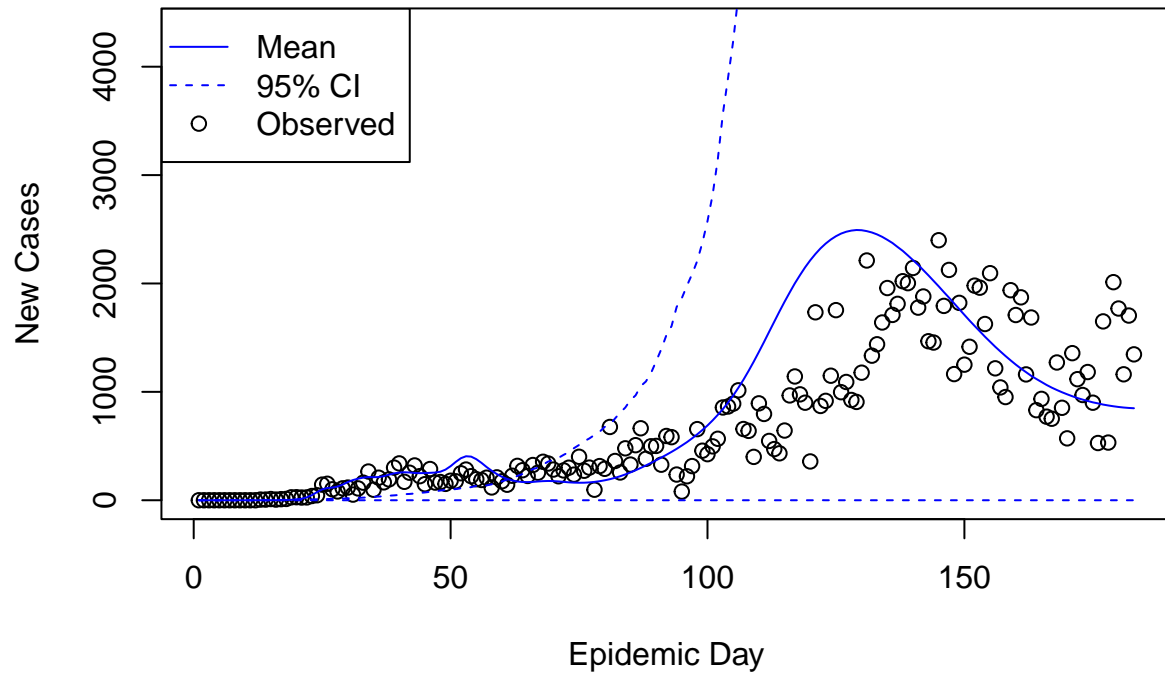
Model 2a: Posterior Distribution location FLORIDA



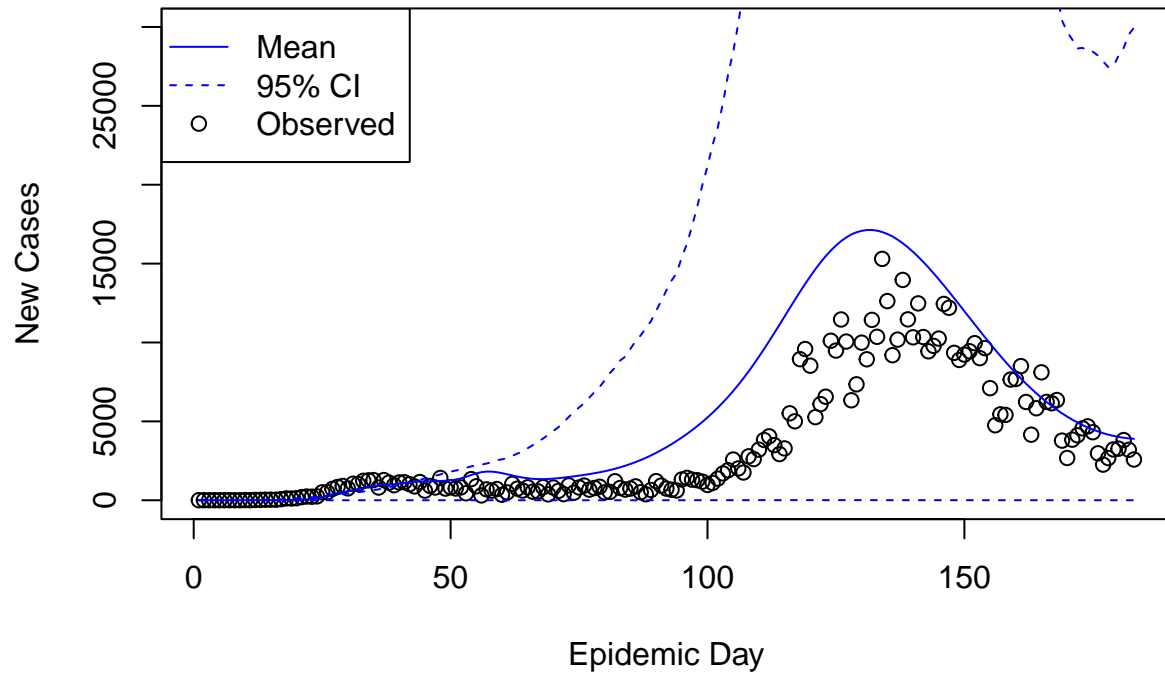
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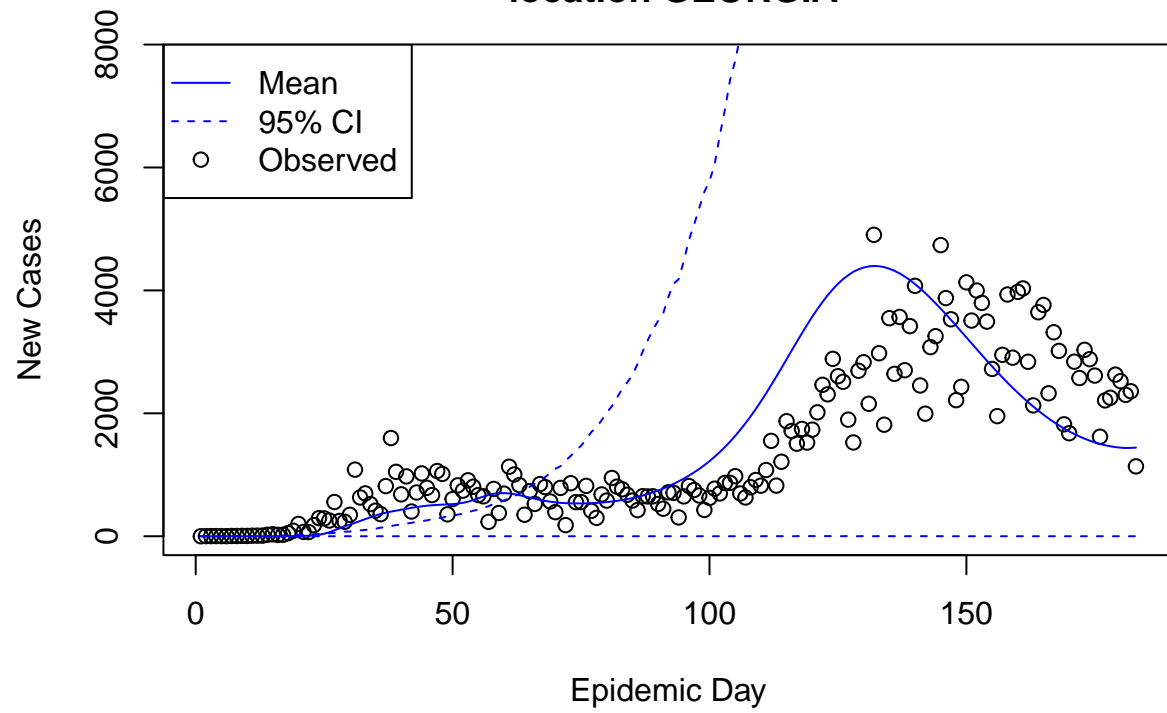
Model 2a: Posterior Predictive Distribution location ALABAMA



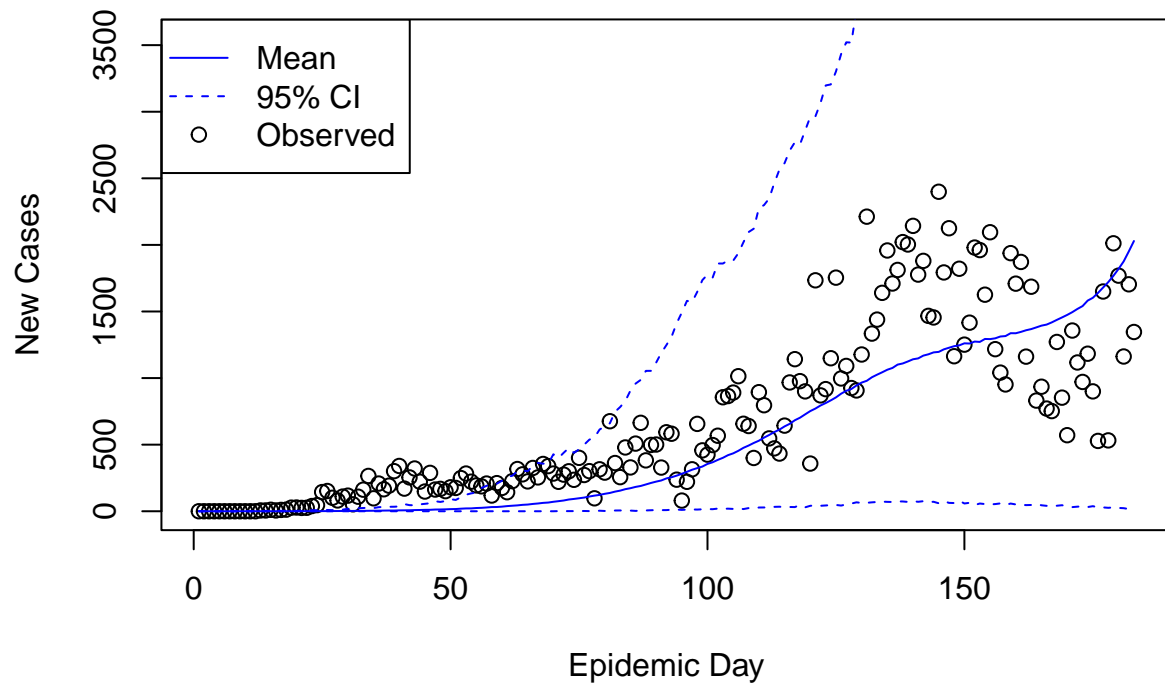
Model 2a: Posterior Predictive Distribution location FLORIDA



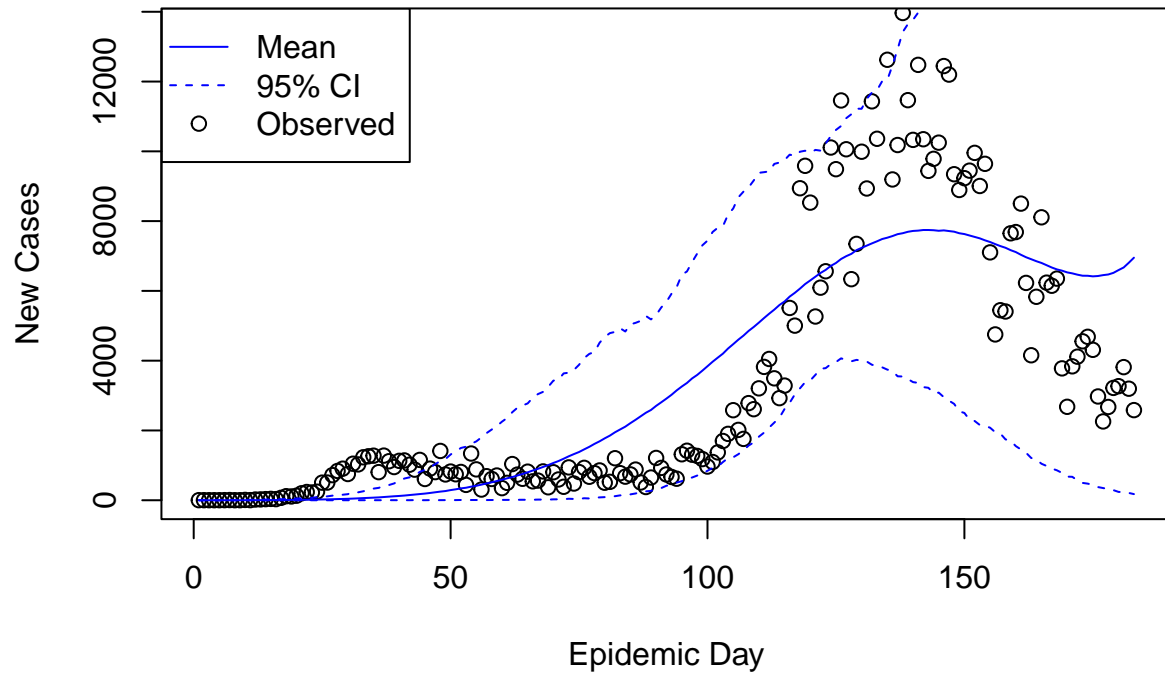
Model 2a: Posterior Predictive Distribution location GEORGIA



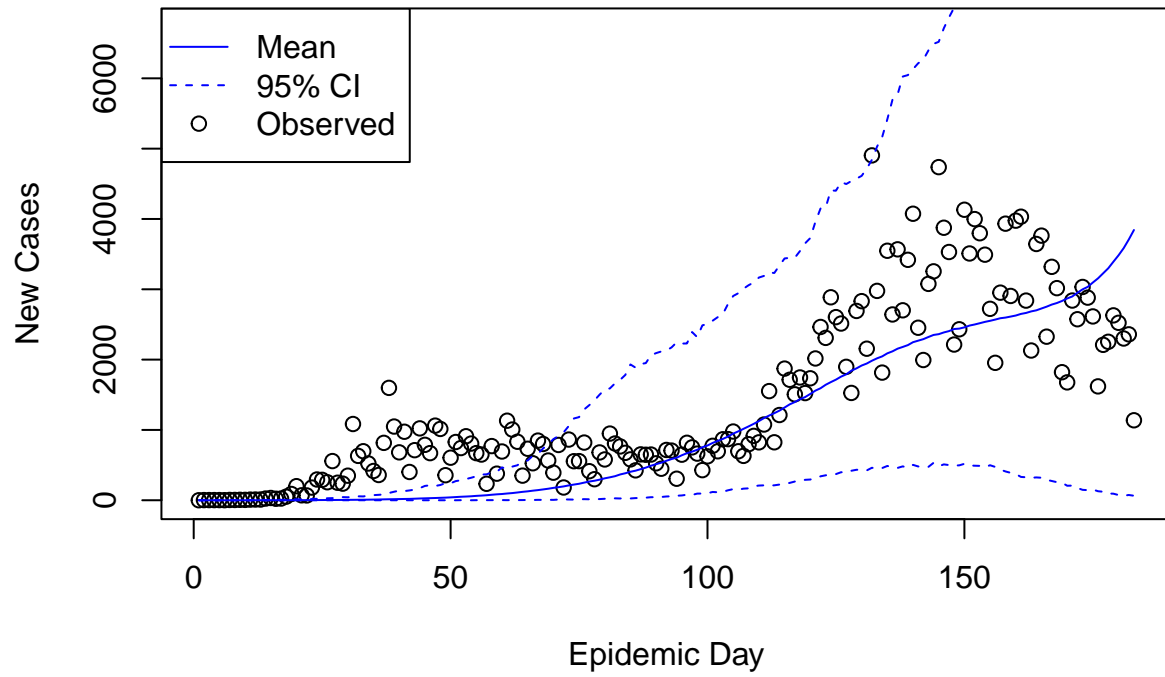
Model 2a (Basic ABC): Posterior Distribution location ALABAMA



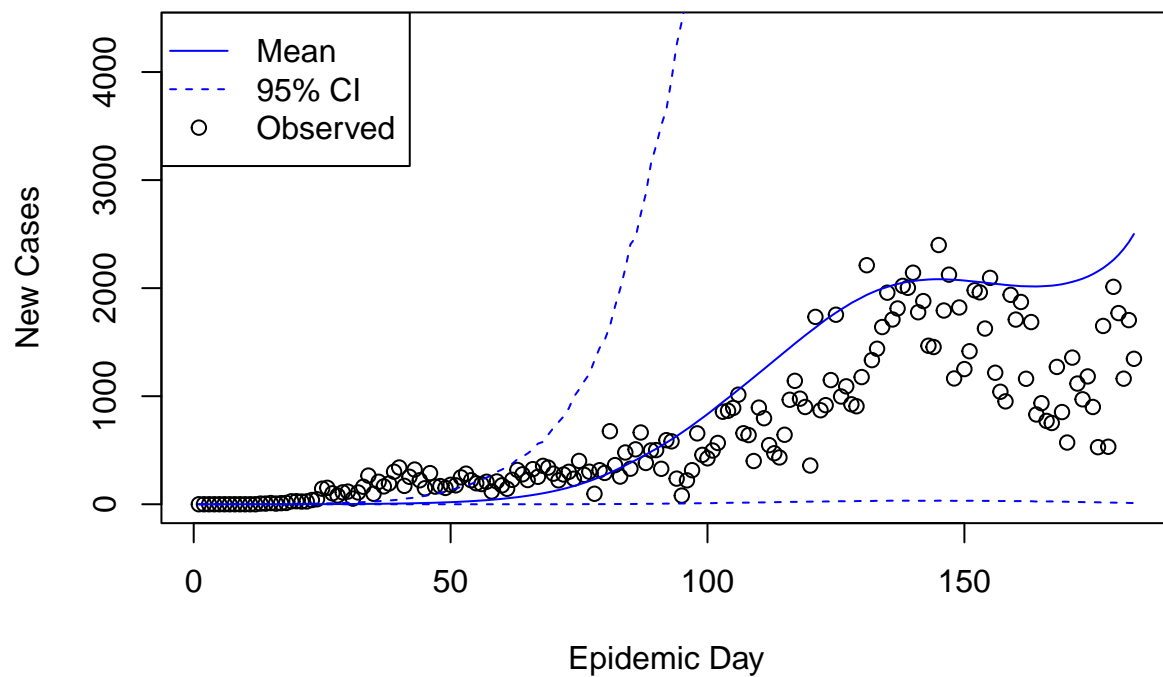
Model 2a (Basic ABC): Posterior Distribution location FLORIDA



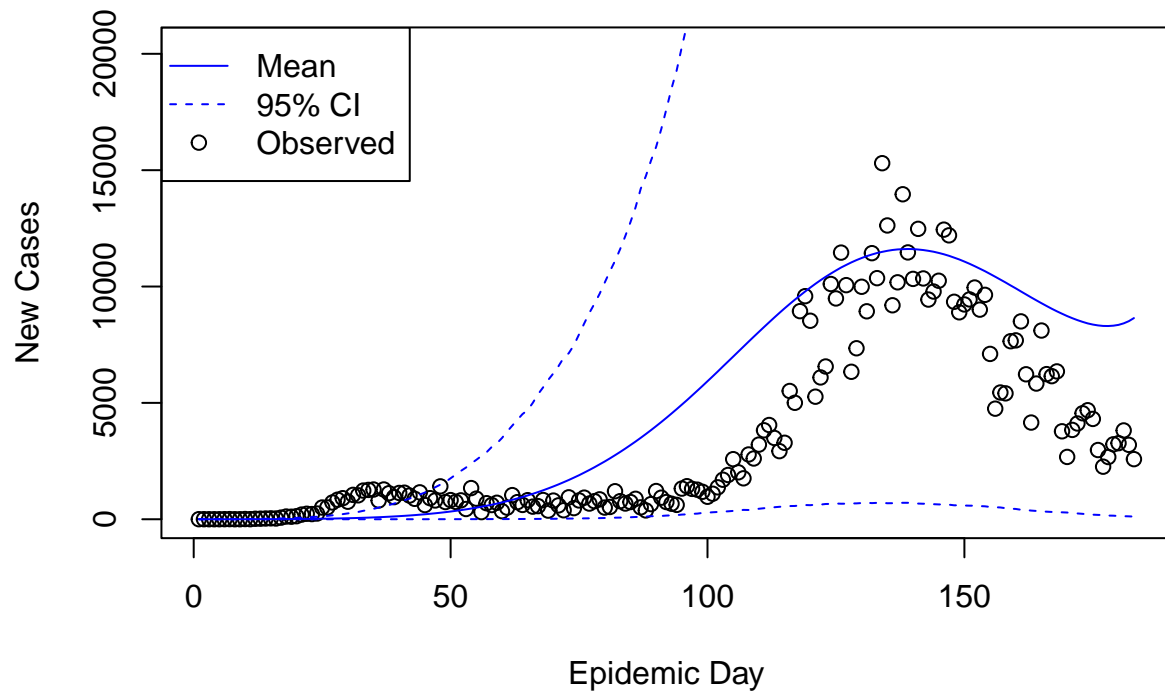
Model 2a (Basic ABC): Posterior Distribution location GEORGIA



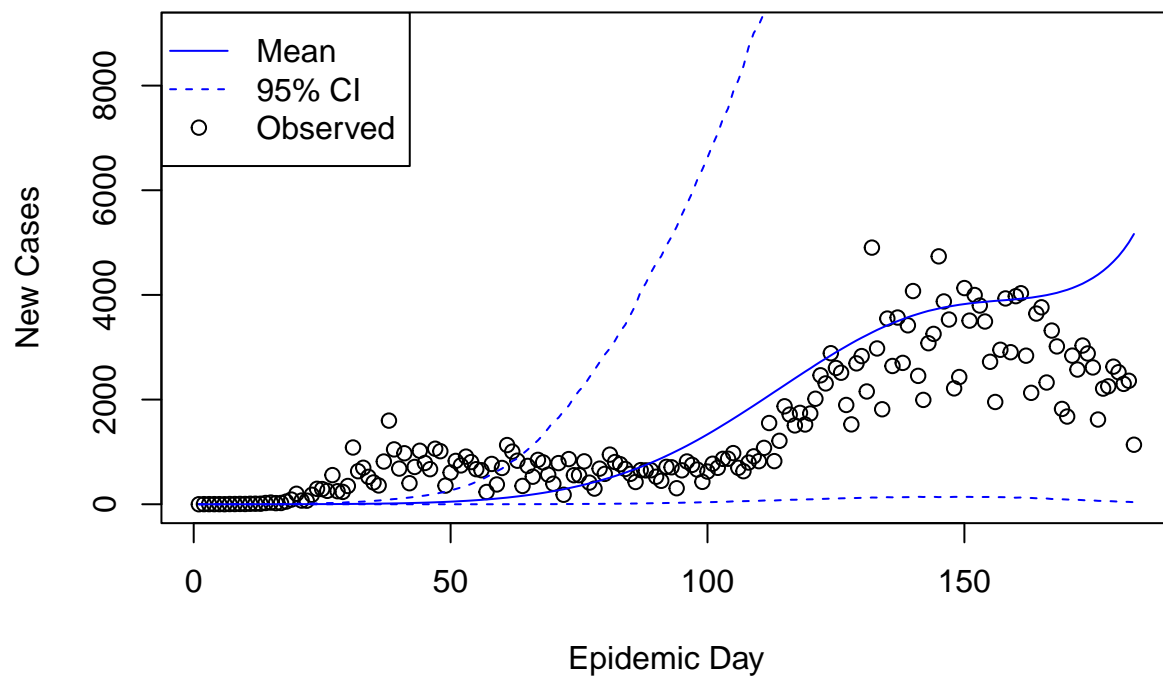
Model 2a (Basic ABC): Posterior Predictive Distribution location ALABAMA



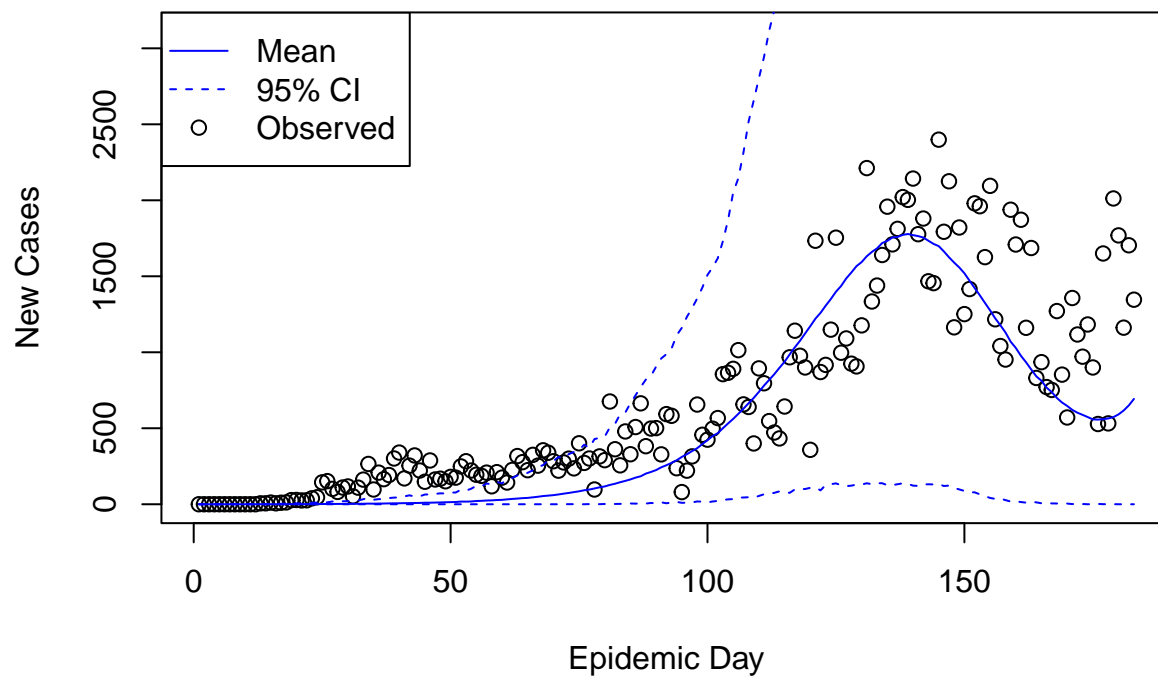
Model 2a (Basic ABC): Posterior Predictive Distribution location FLORIDA



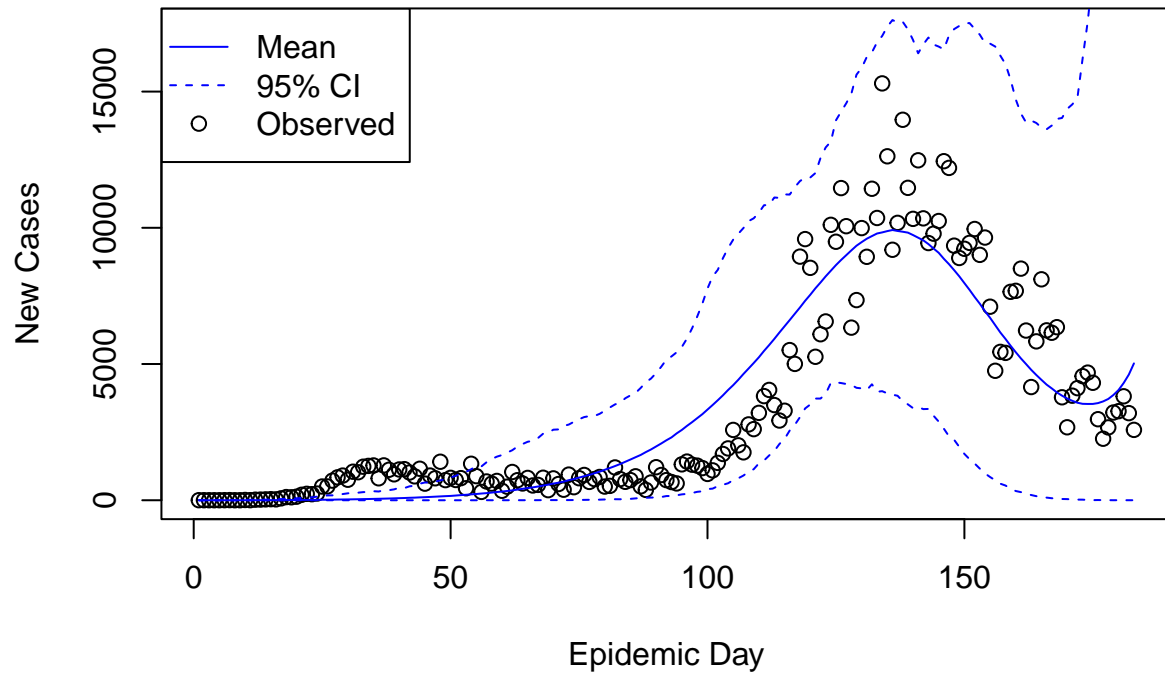
Model 2a (Basic ABC): Posterior Predictive Distribution location GEORGIA



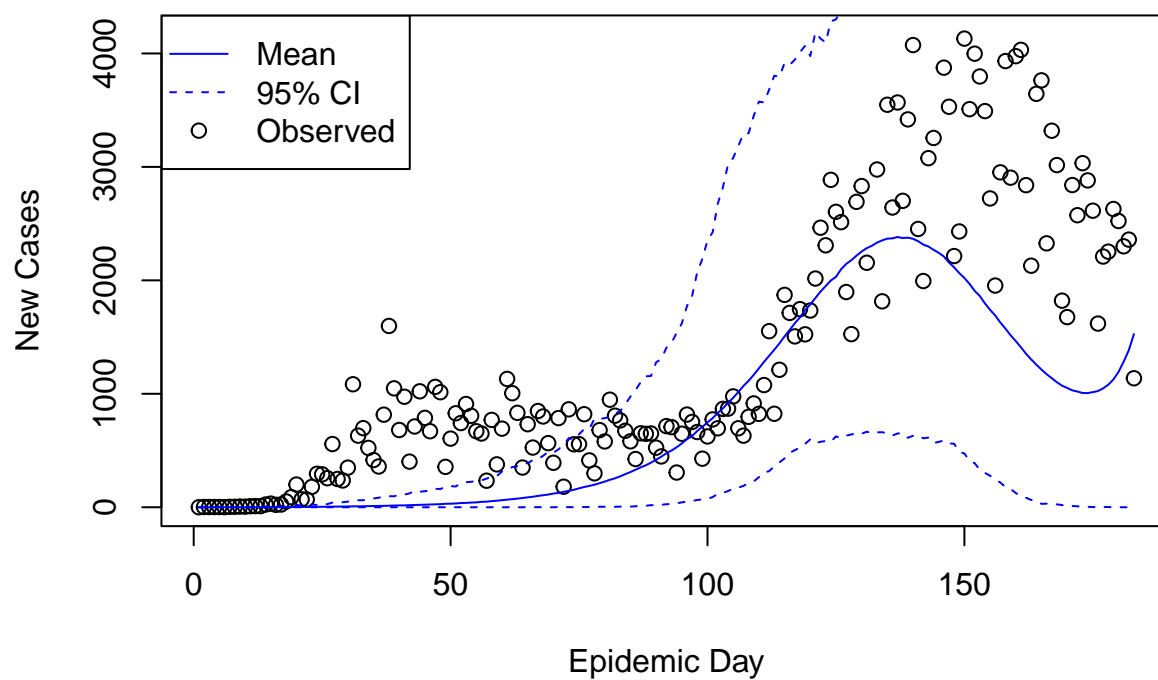
Model 2a (Weibull Distribution): Posterior Distribution location ALABAMA



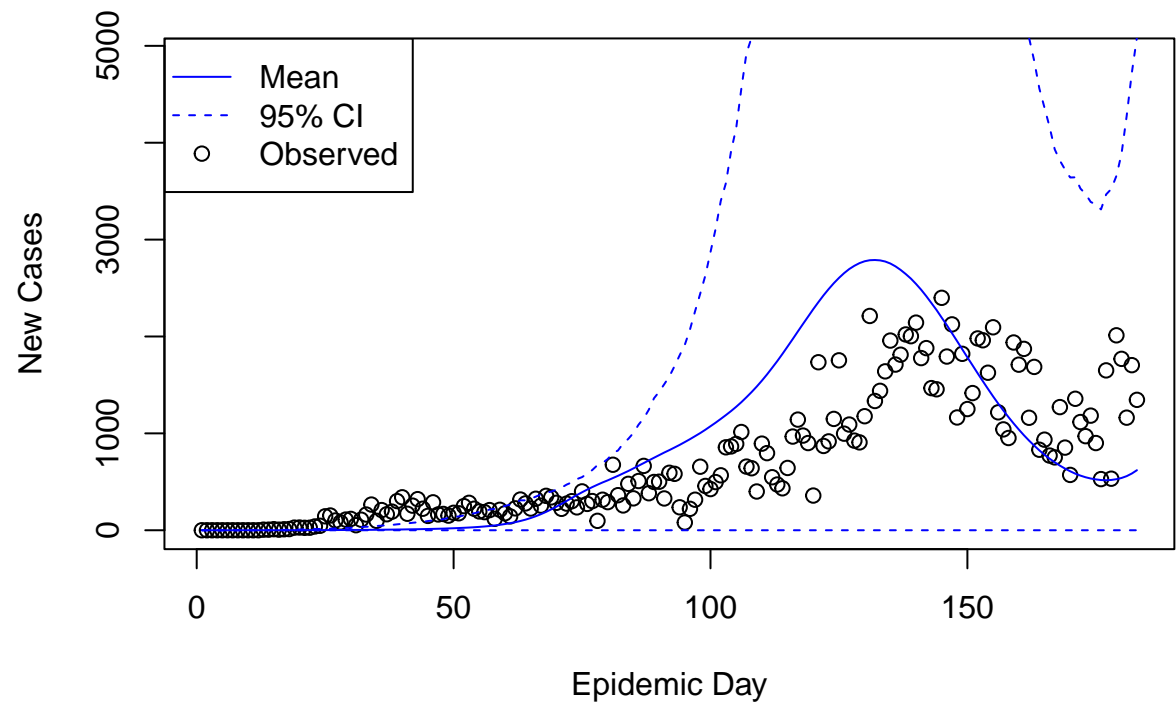
Model 2a (Weibull Distribution): Posterior Distribution location FLORIDA



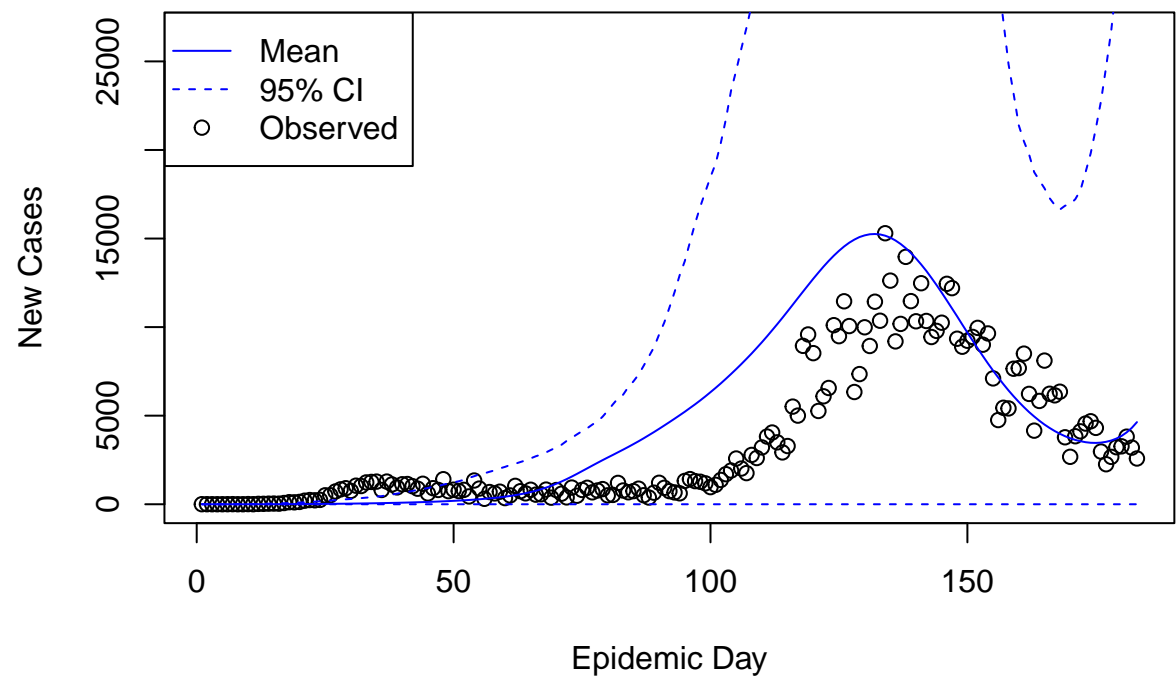
Model 2a (Weibull Distribution): Posterior Distribution location GEORGIA



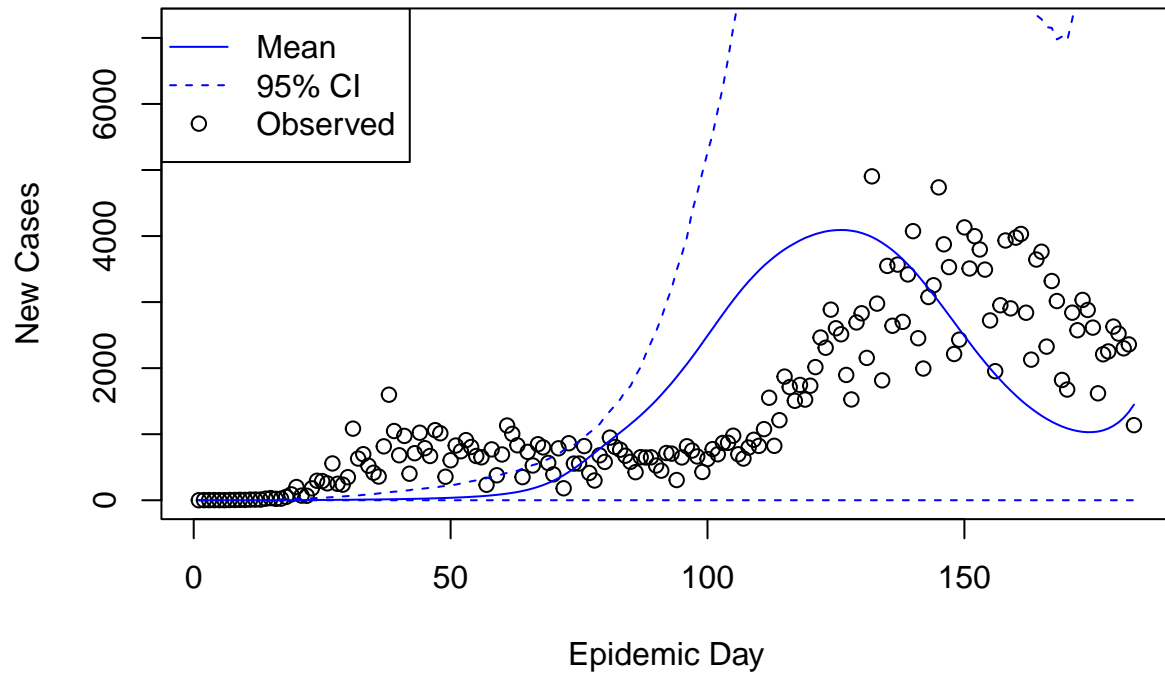
**Model 2a (Weibull Distribution): Posterior Predictive Distribution
location ALABAMA**



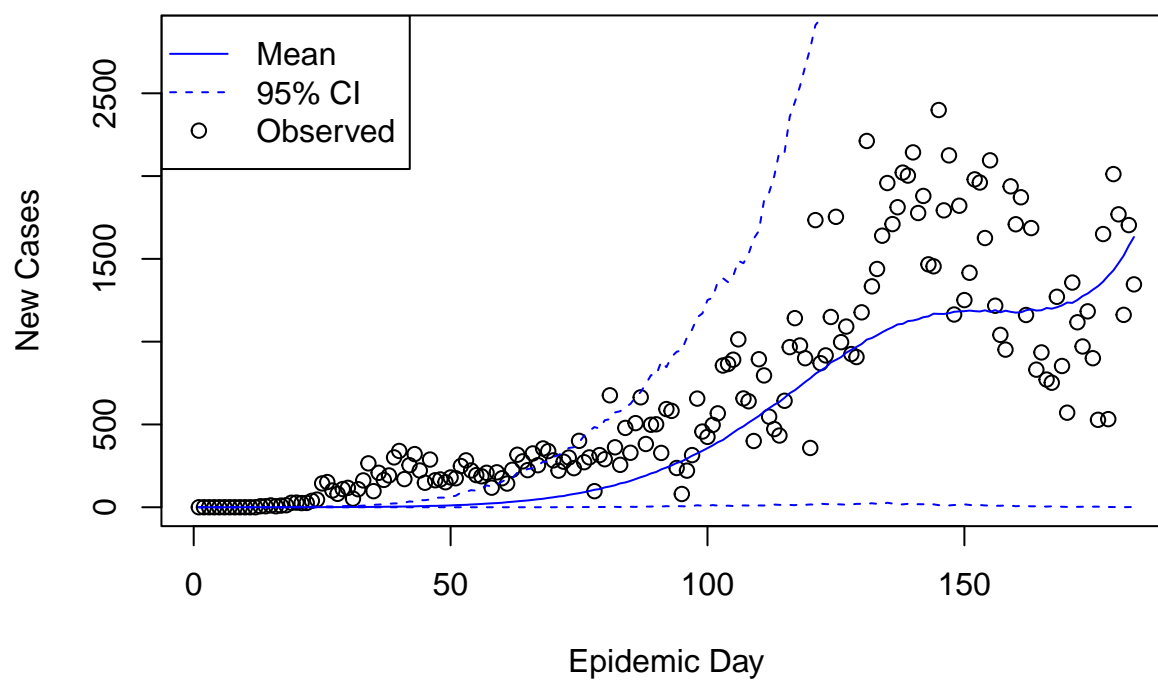
**Model 2a (Weibull Distribution): Posterior Predictive Distribution
location FLORIDA**



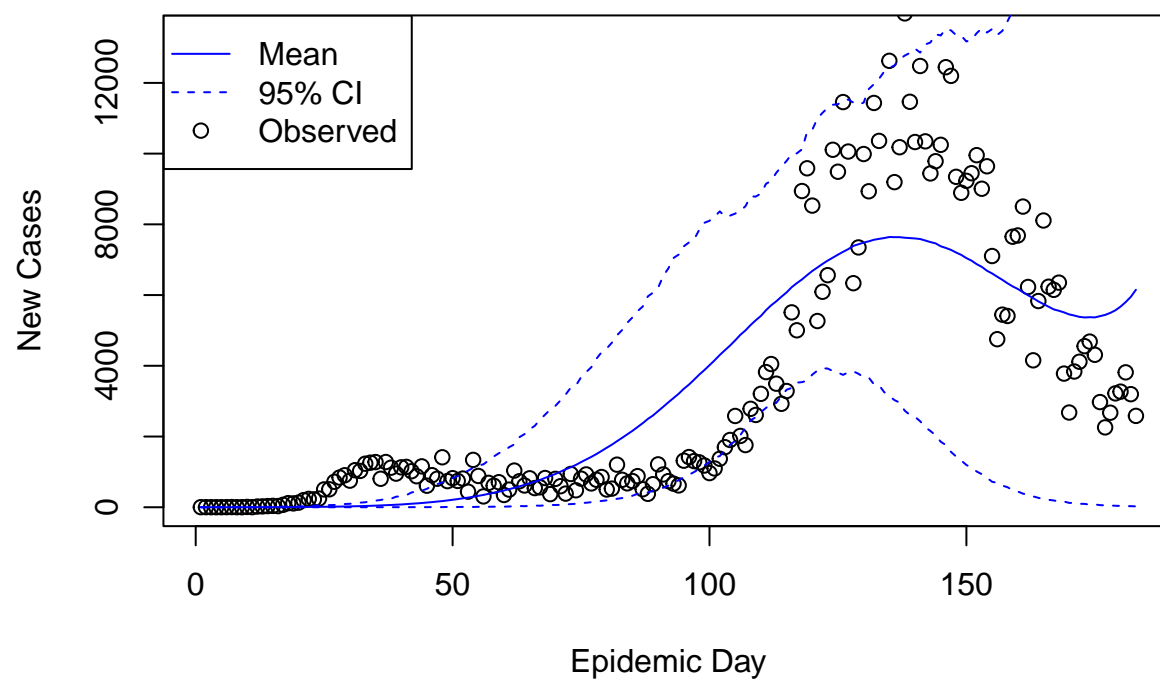
Model 2a (Weibull Distribution): Posterior Predictive Distribution location GEORGIA



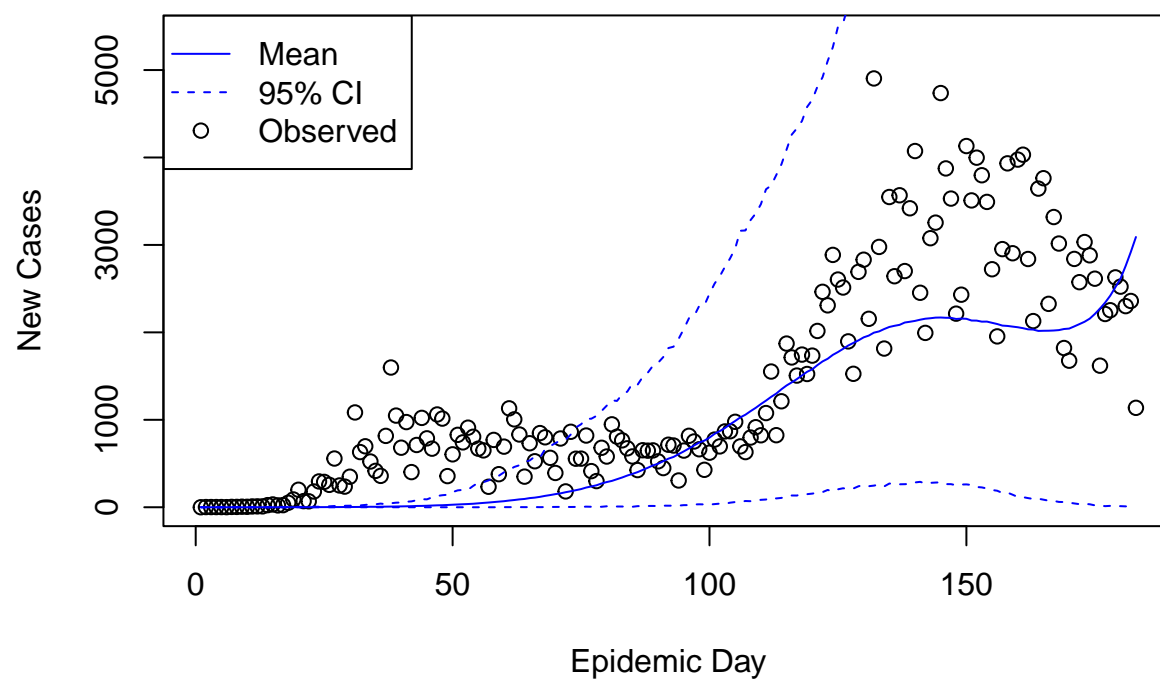
Model 2a (Basic ABC, Weibull): Posterior Distribution location ALABAMA



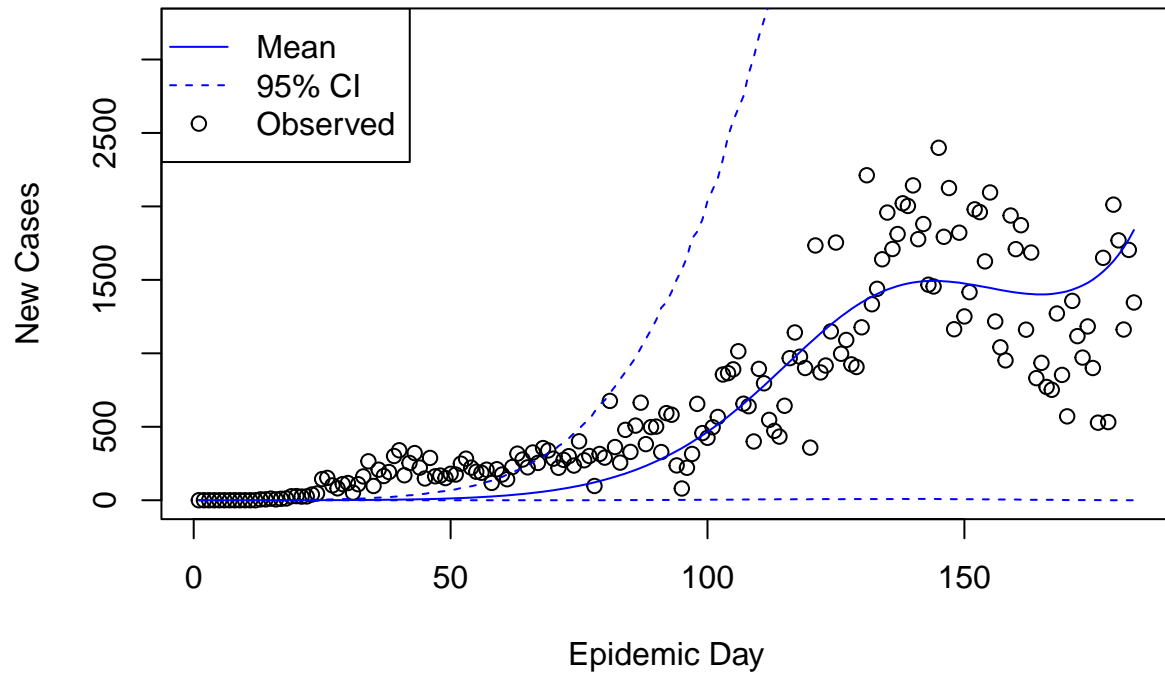
Model 2a (Basic ABC, Weibull): Posterior Distribution location FLORIDA



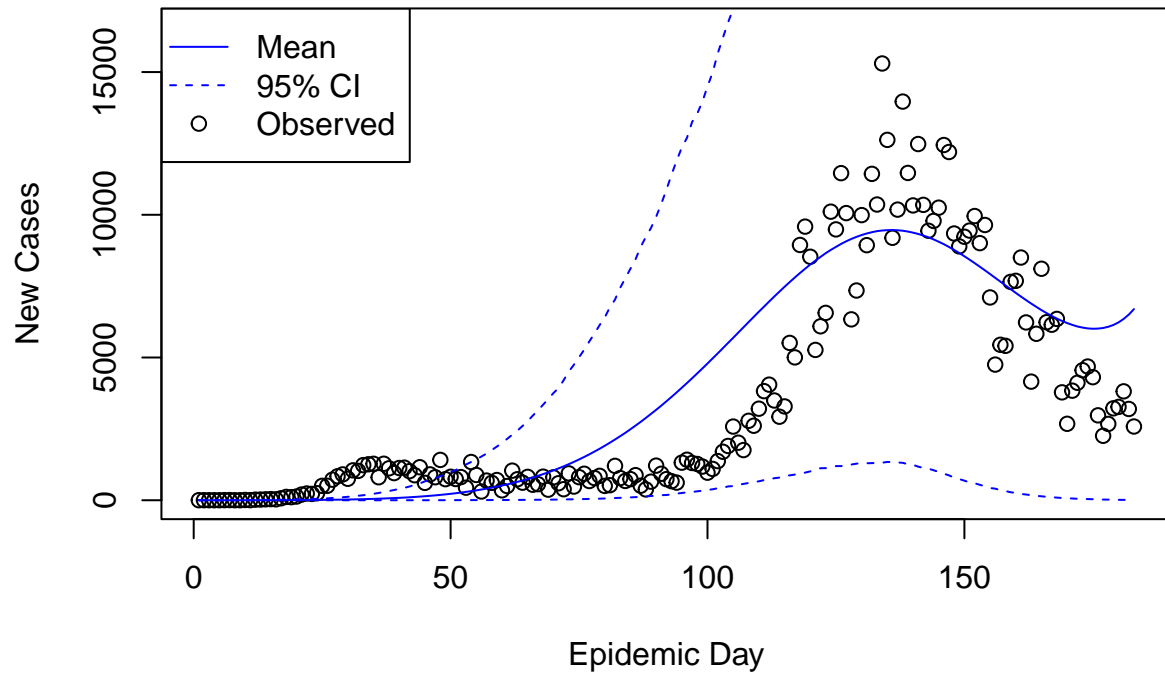
Model 2a (Basic ABC, Weibull): Posterior Distribution location GEORGIA



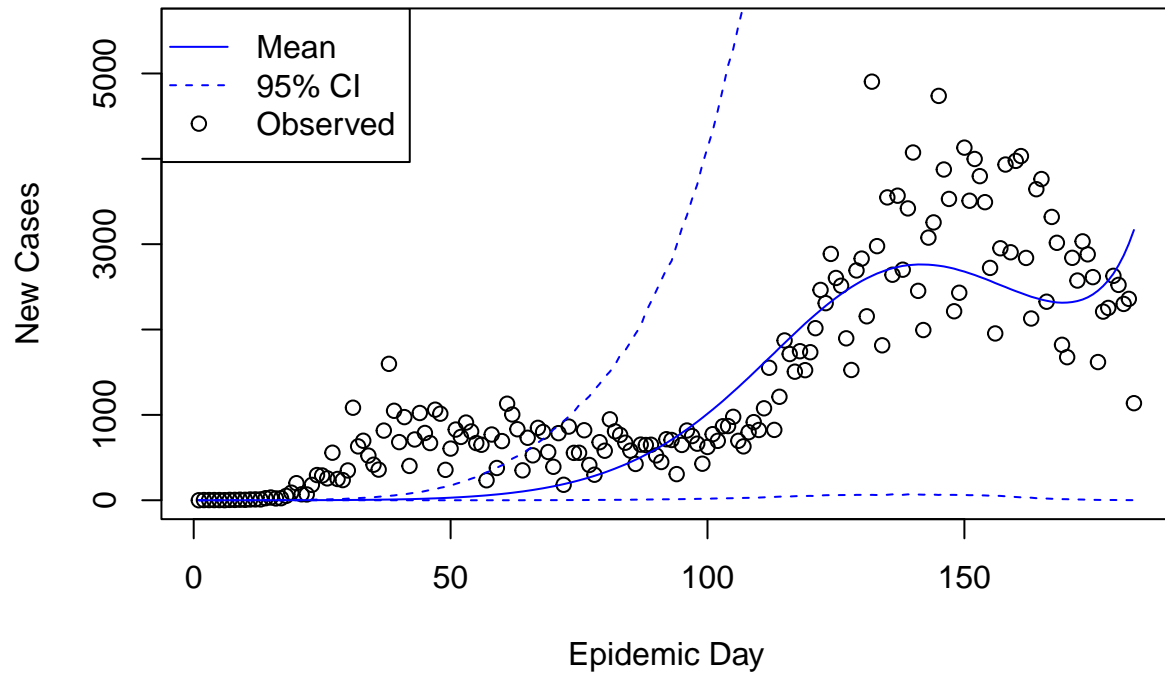
Model 2a (Basic ABC, Weibull): Posterior Predictive Distribution location ALABAMA



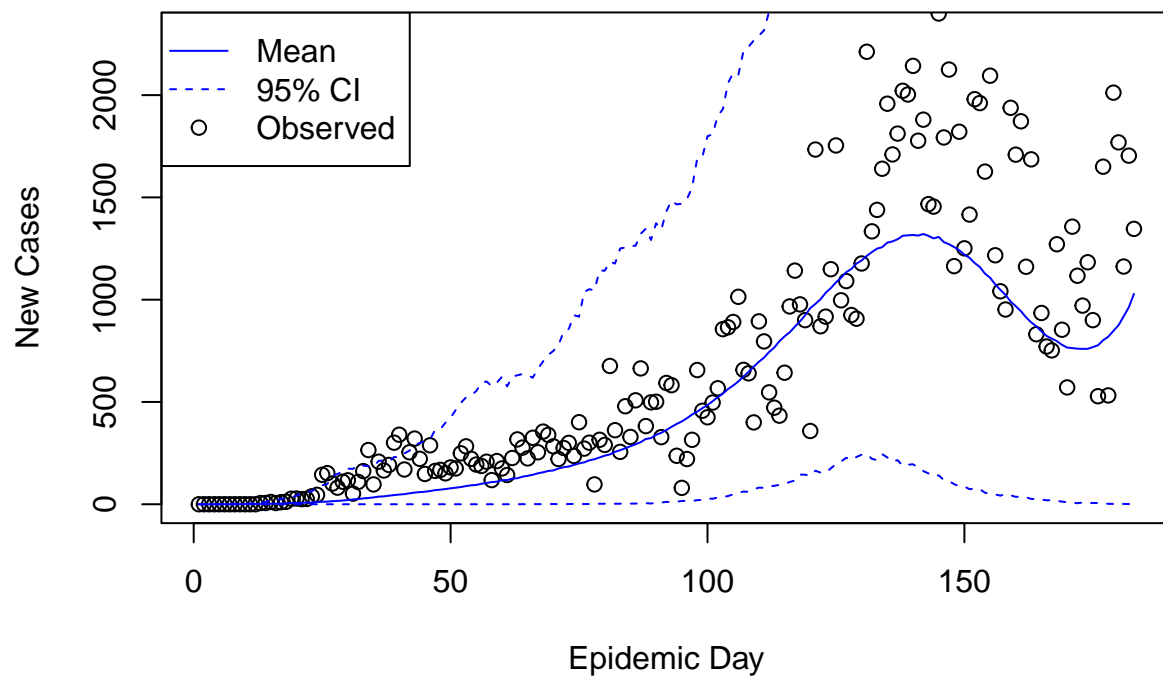
Model 2a (Basic ABC, Weibull): Posterior Predictive Distribution location FLORIDA



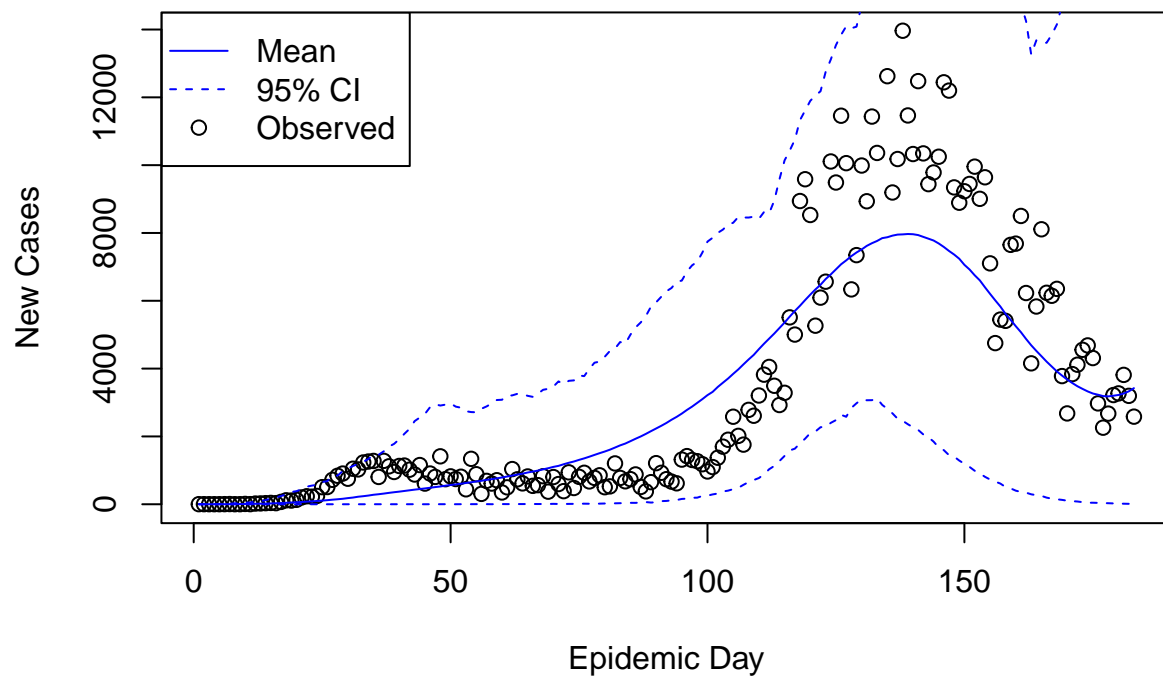
Model 2a (Basic ABC, Weibull): Posterior Predictive Distribution location GEORGIA



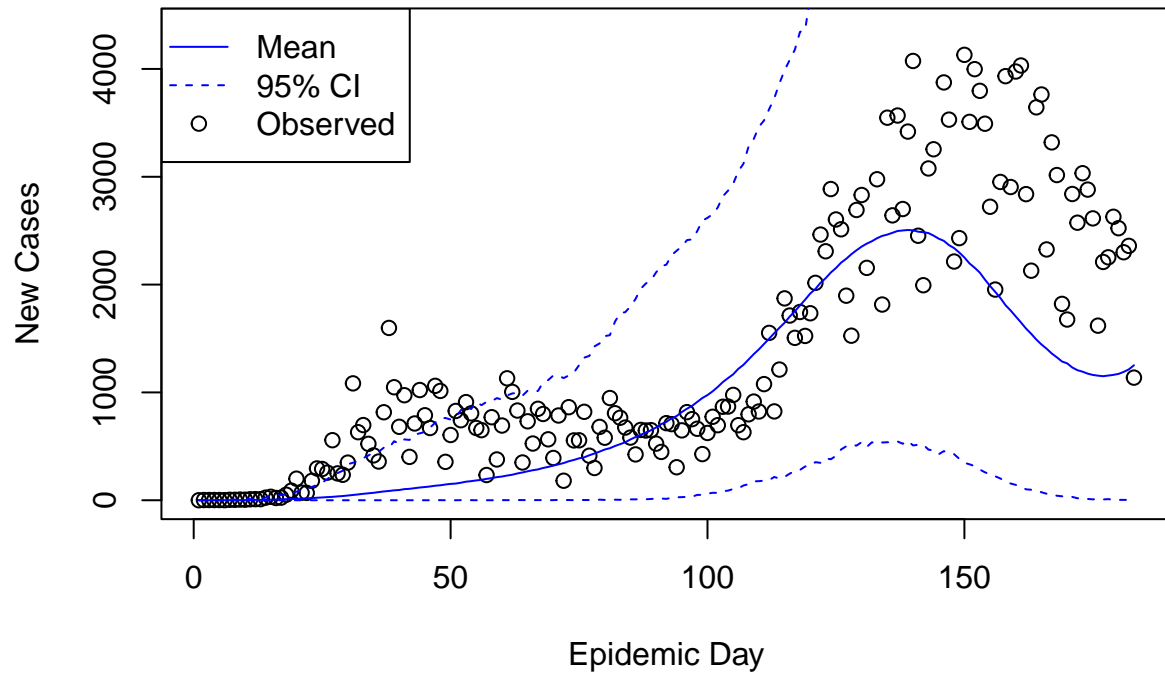
Model 2b: Posterior Distribution location ALABAMA



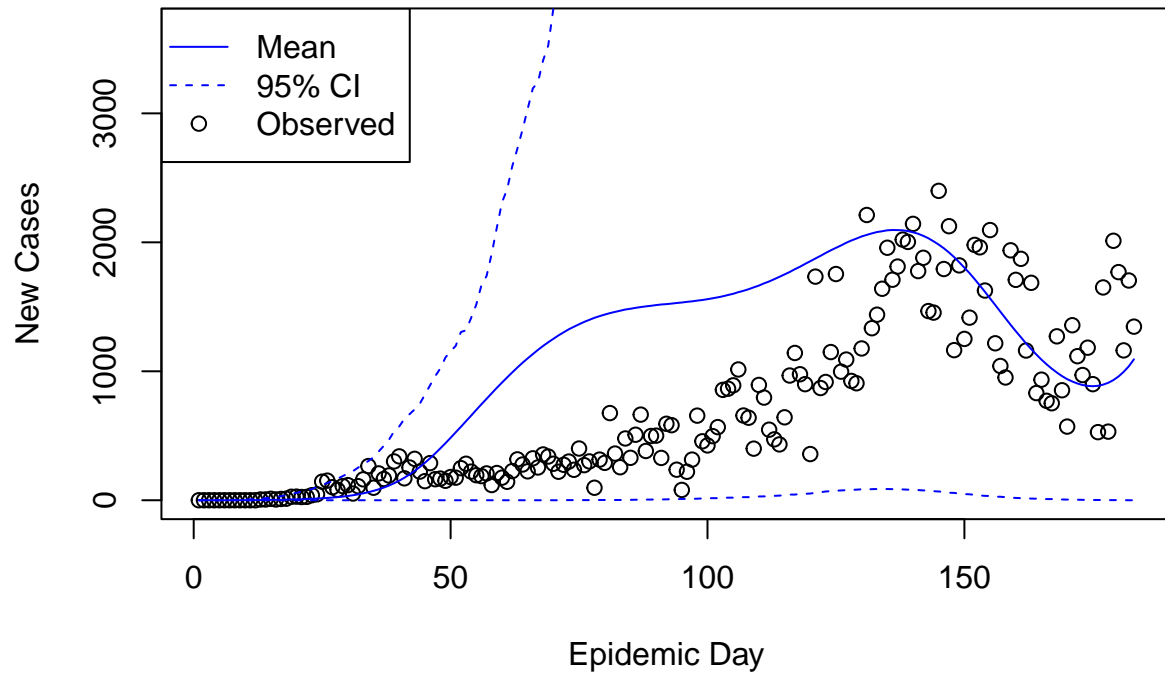
Model 2b: Posterior Distribution location FLORIDA



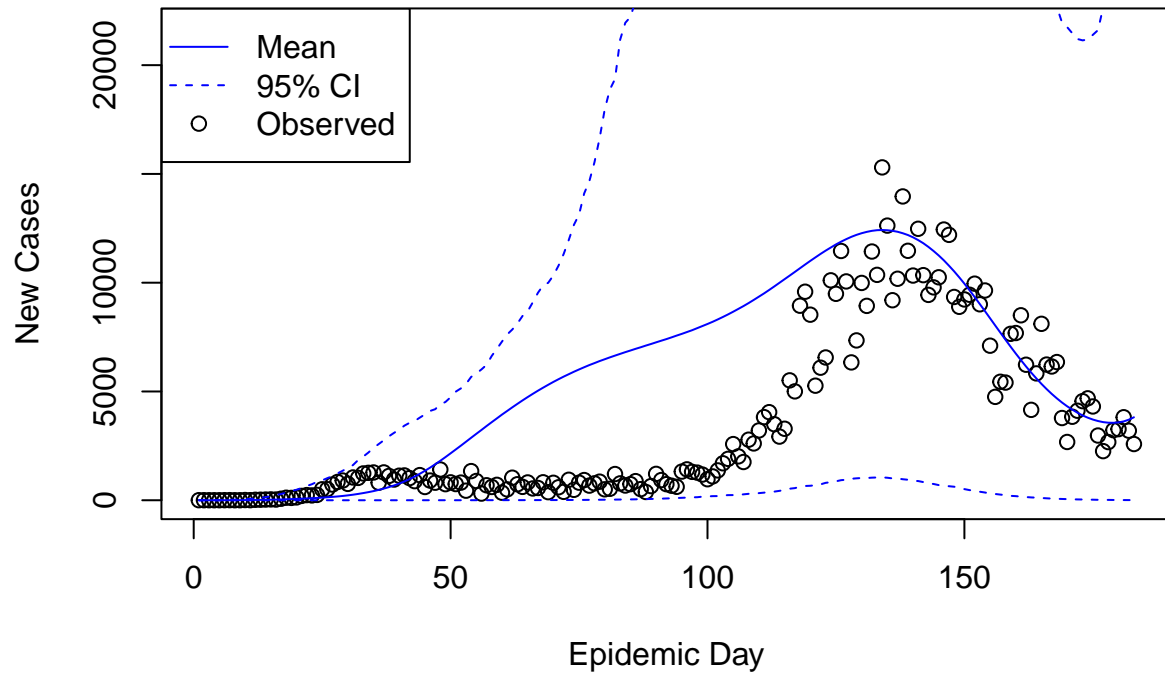
Model 2b: Posterior Distribution location GEORGIA



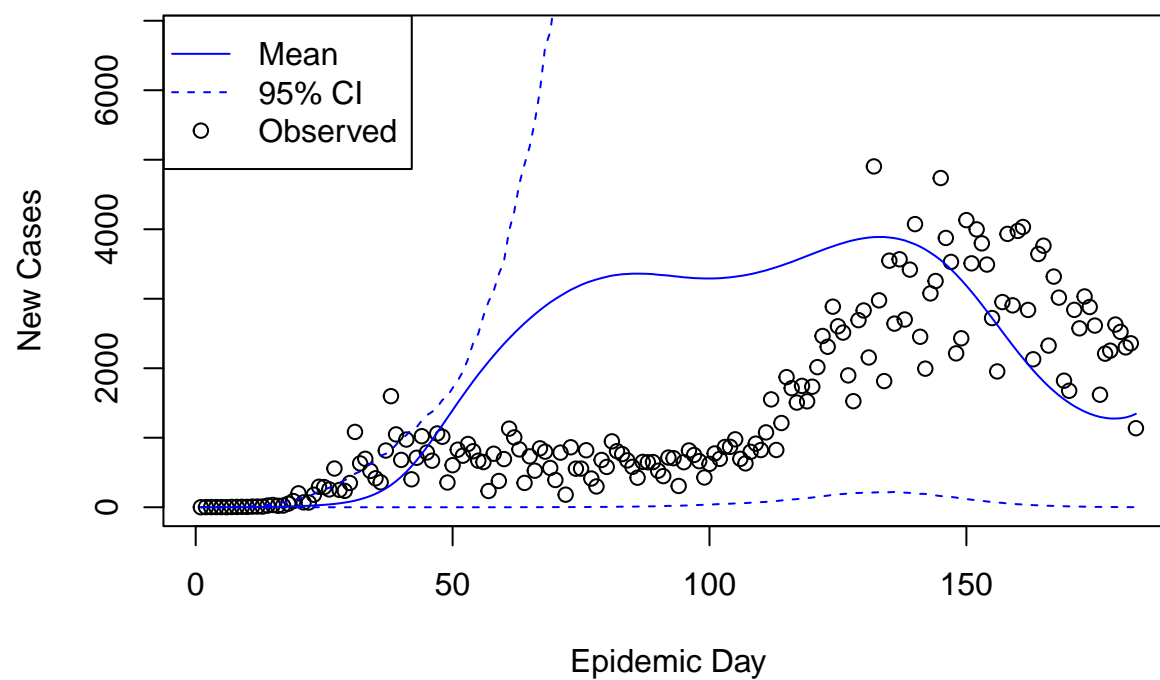
Model 2b: Posterior Predictive Distribution location ALABAMA



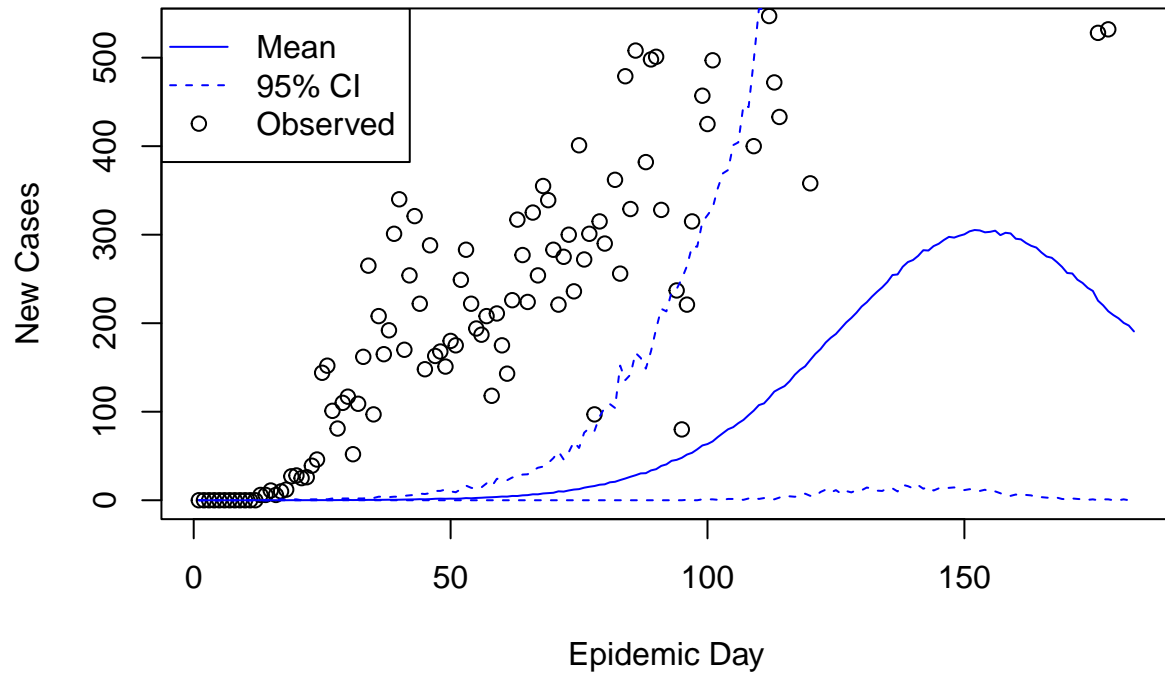
Model 2b: Posterior Predictive Distribution location FLORIDA



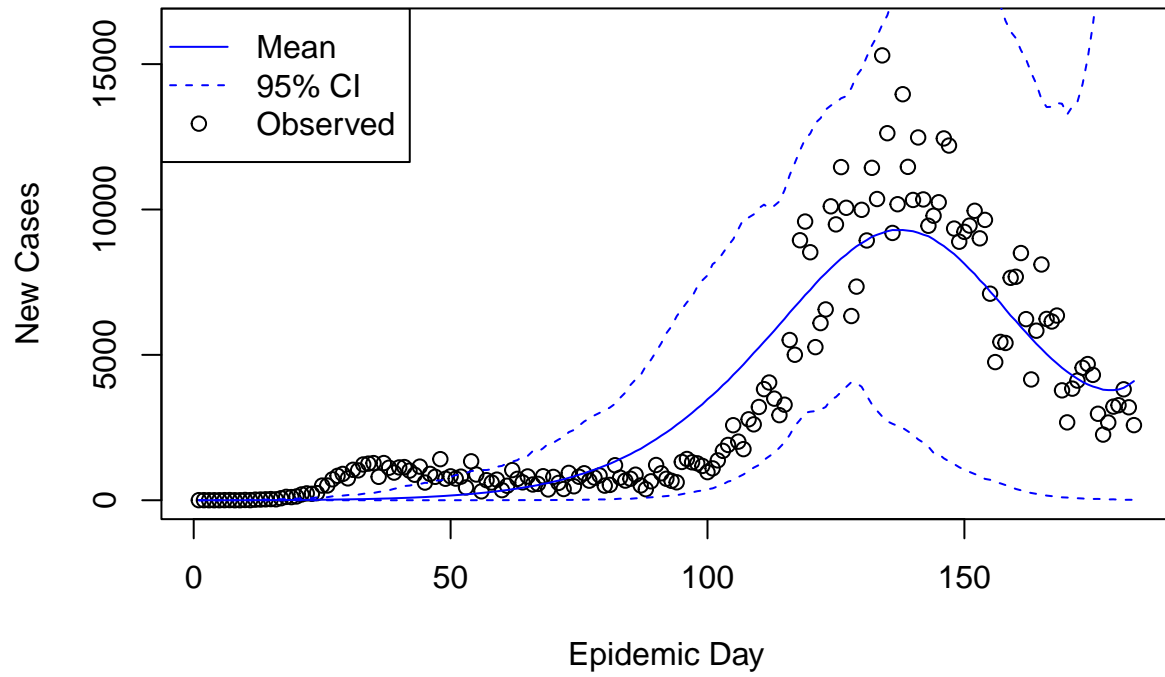
Model 2b: Posterior Predictive Distribution location GEORGIA



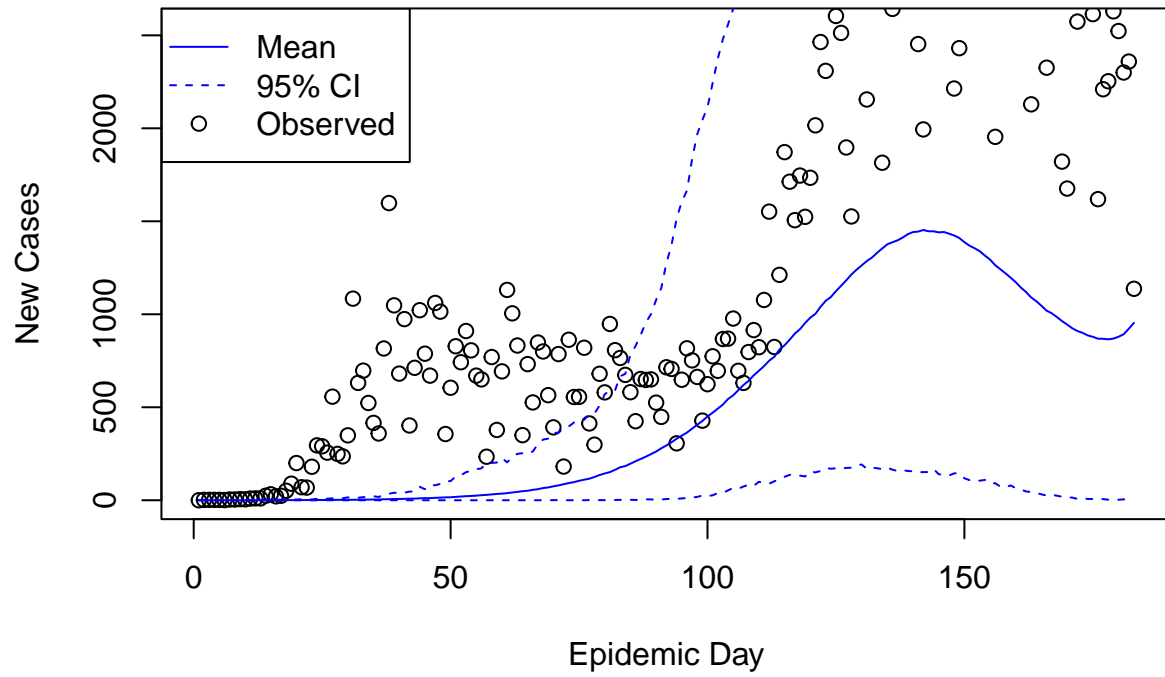
Model 2c: Posterior Distribution location ALABAMA



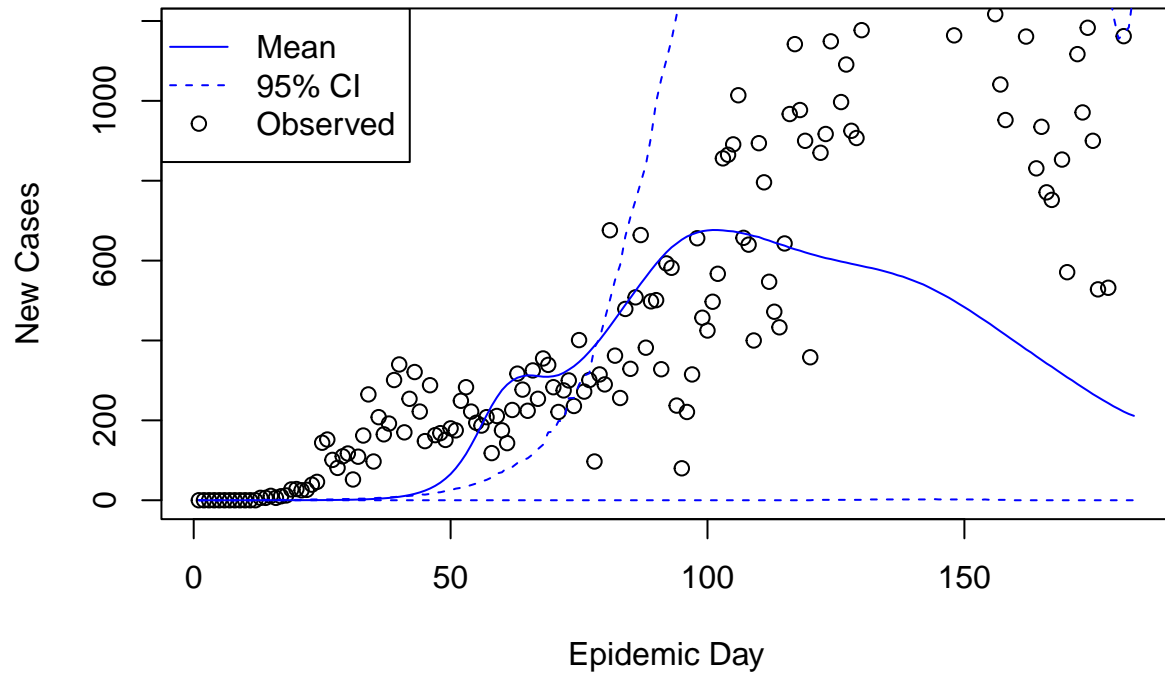
Model 2c: Posterior Distribution location FLORIDA



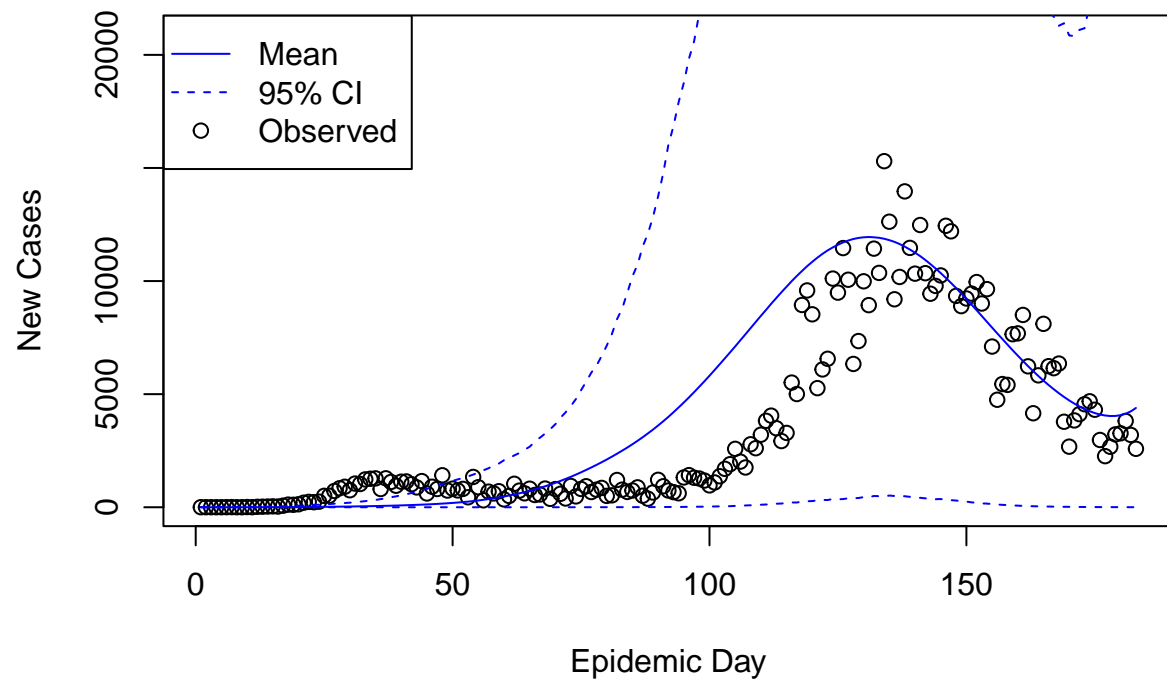
Model 2c: Posterior Distribution location GEORGIA



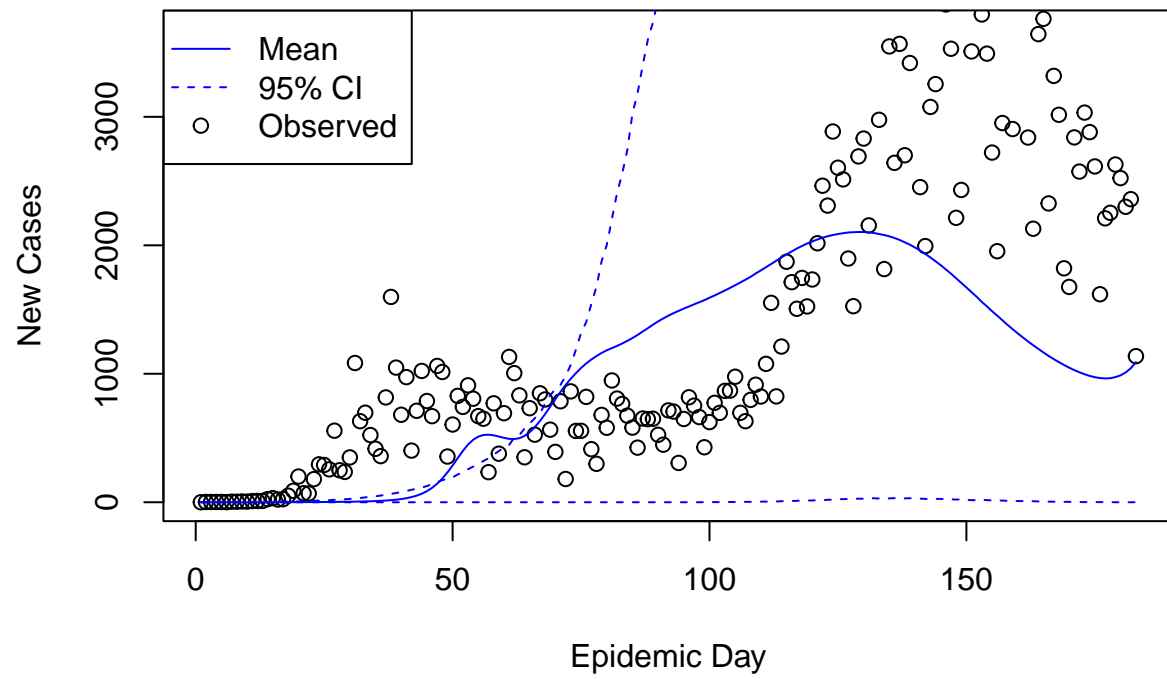
Model 2c: Posterior Predictive Distribution location ALABAMA



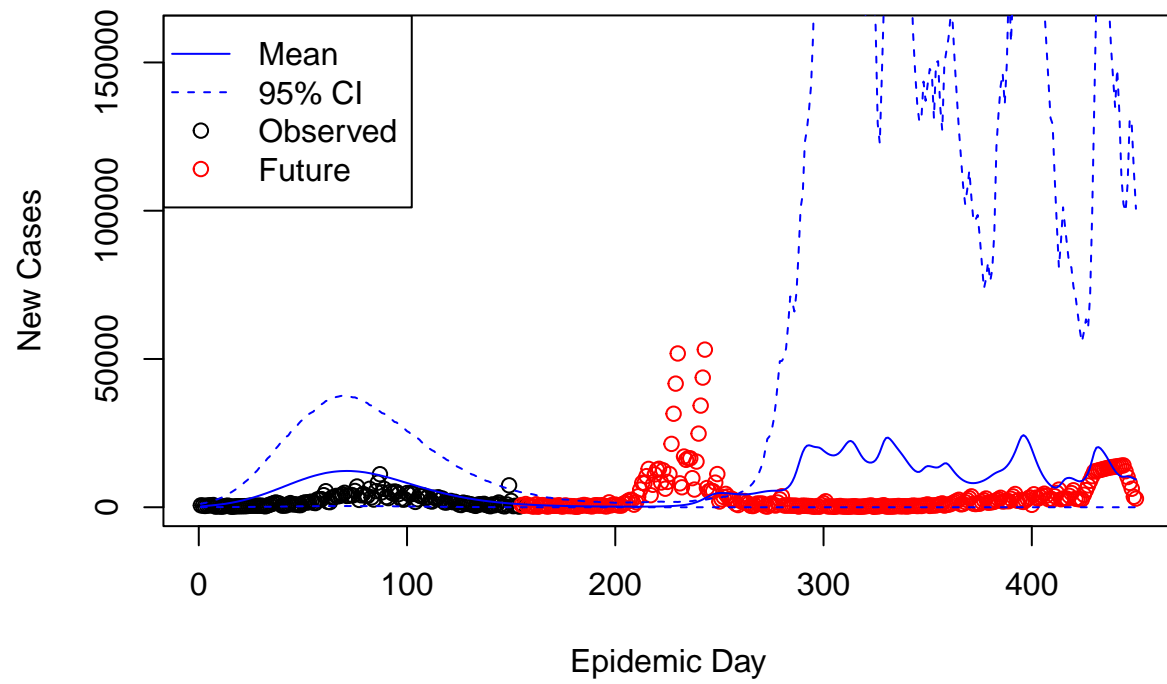
Model 2c: Posterior Predictive Distribution location FLORIDA



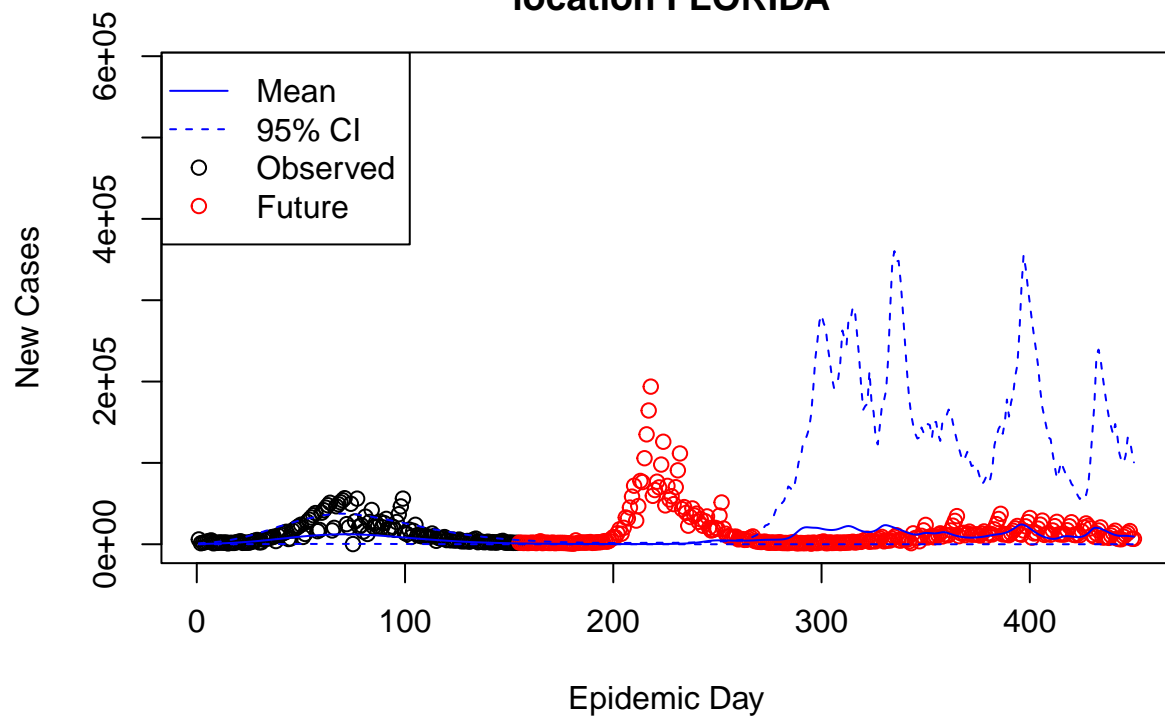
Model 2c: Posterior Predictive Distribution location GEORGIA



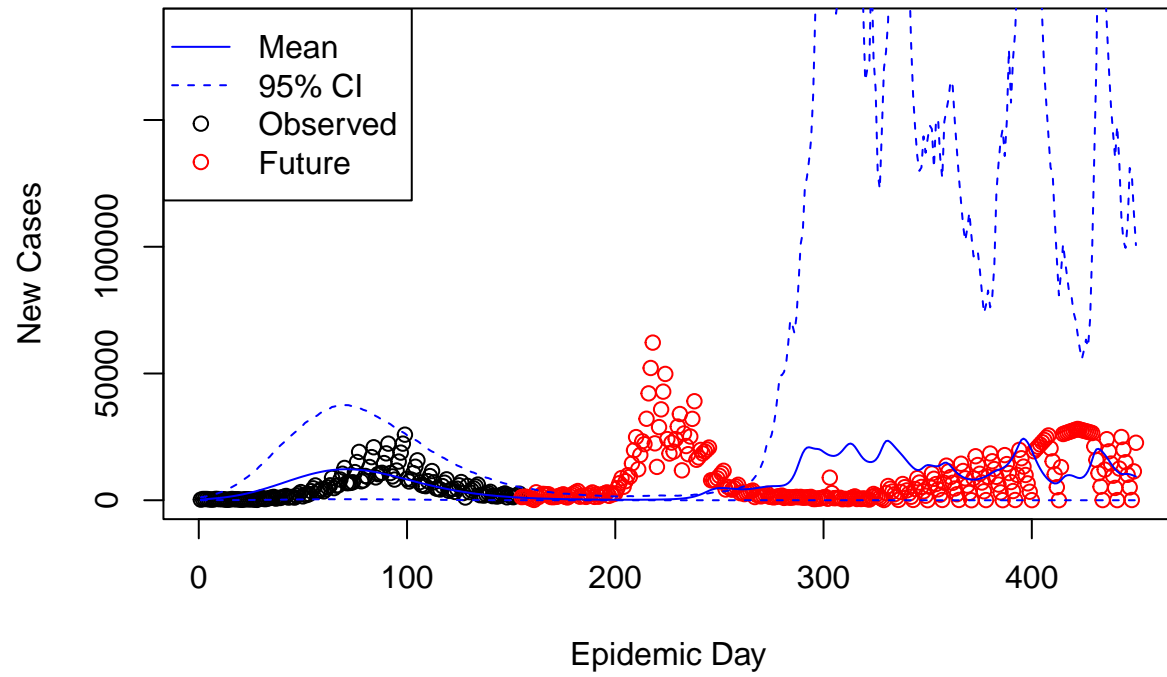
Model 3: Posterior Distribution location ALABAMA



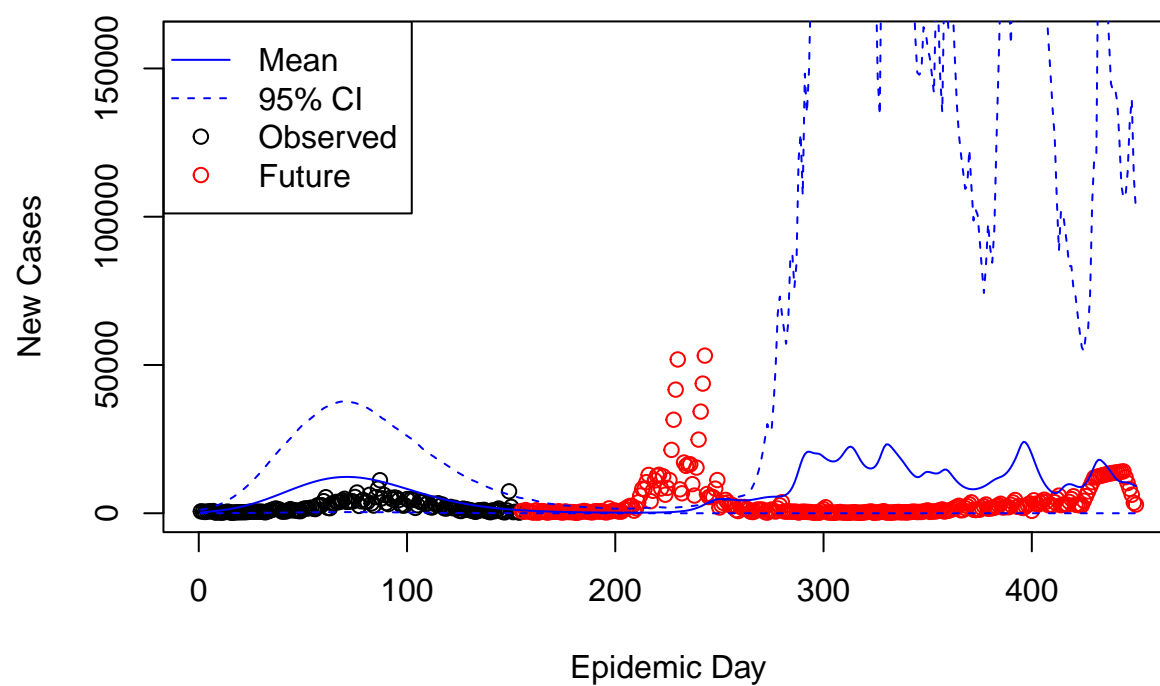
Model 3: Posterior Distribution location FLORIDA



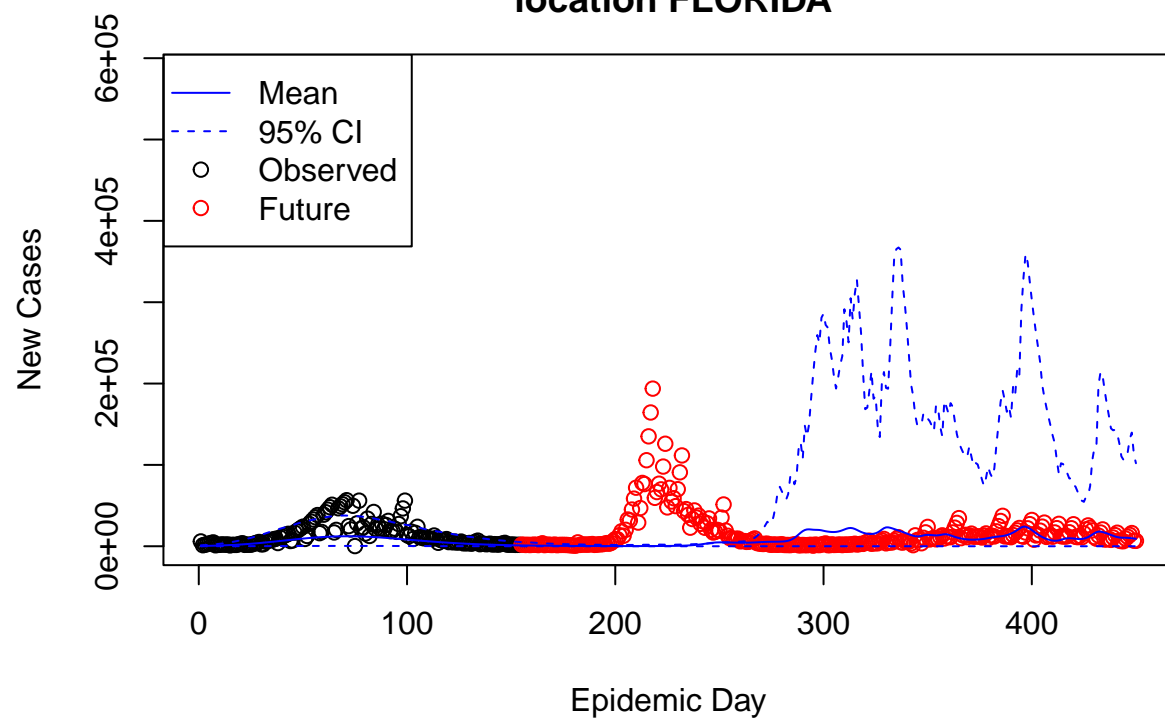
Model 3: Posterior Distribution location GEORGIA



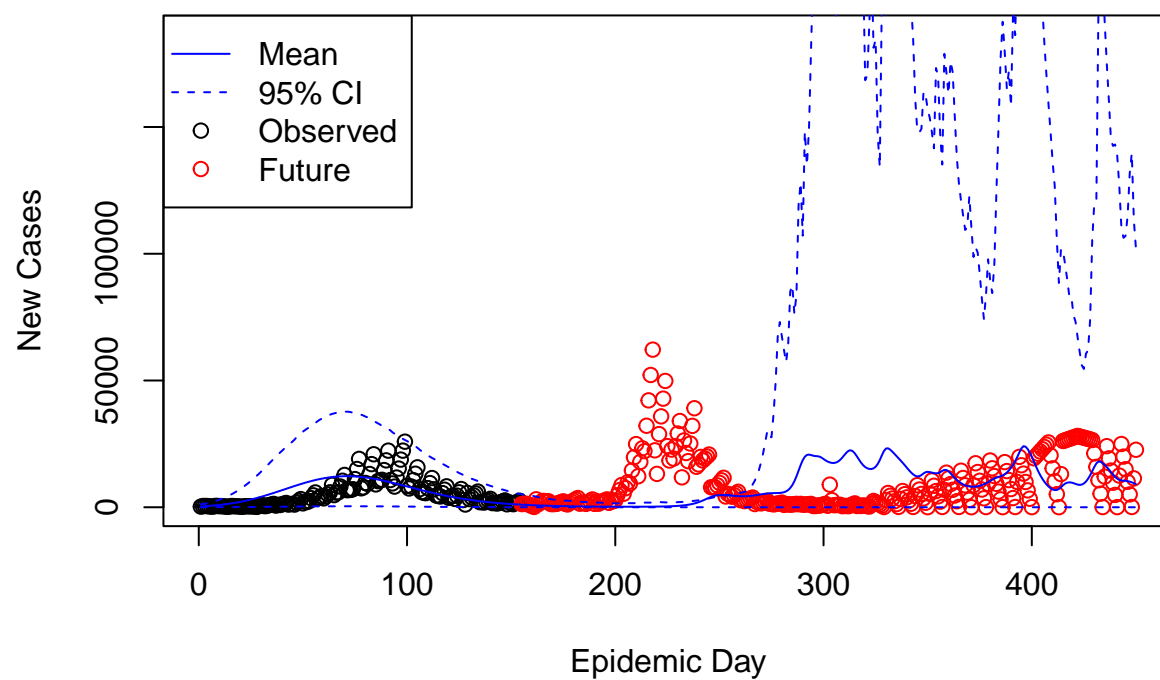
Model 3: Posterior Predictive Distribution location ALABAMA



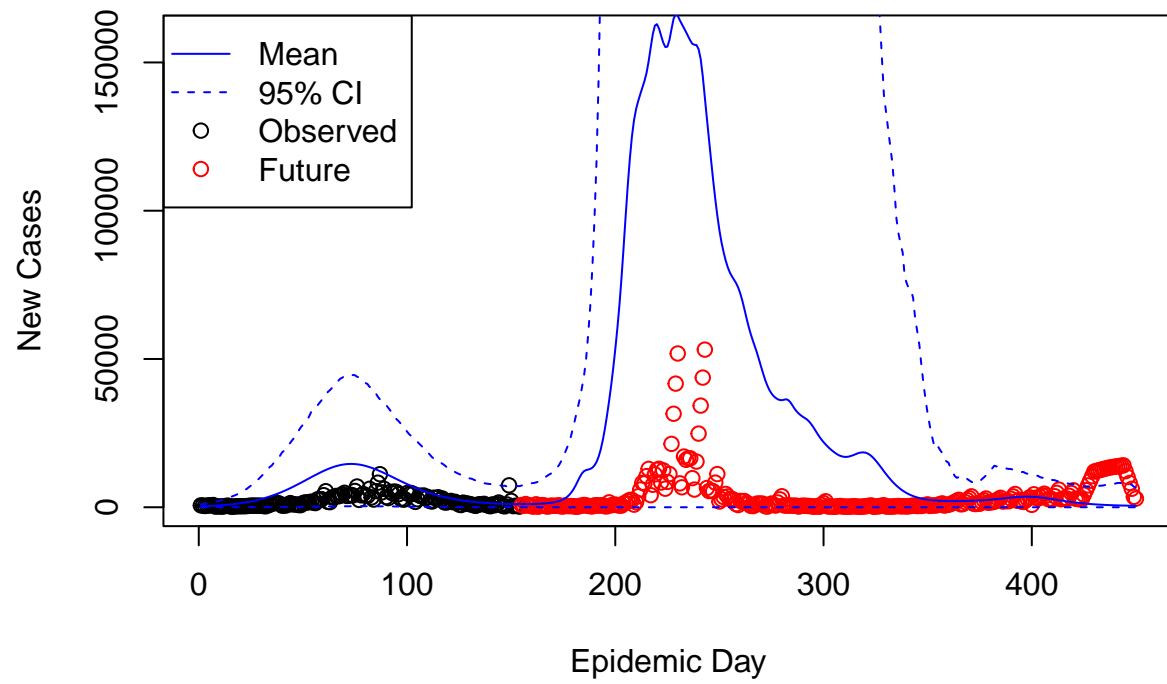
Model 3: Posterior Predictive Distribution location FLORIDA



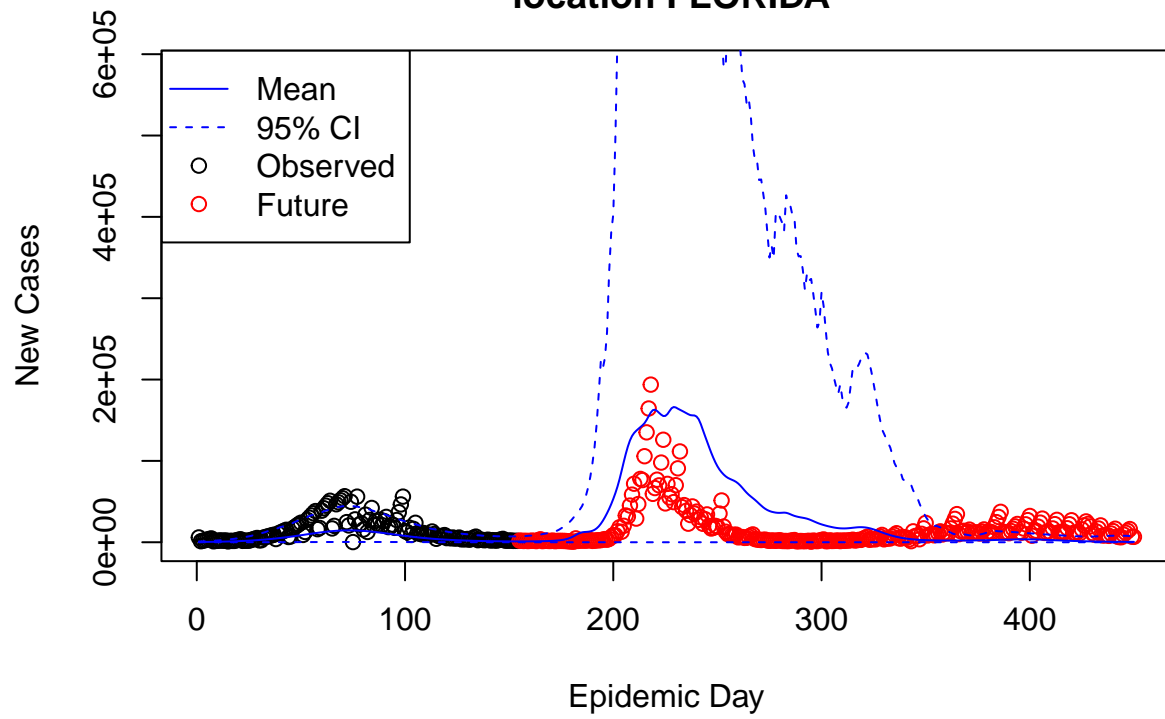
Model 3: Posterior Predictive Distribution location GEORGIA



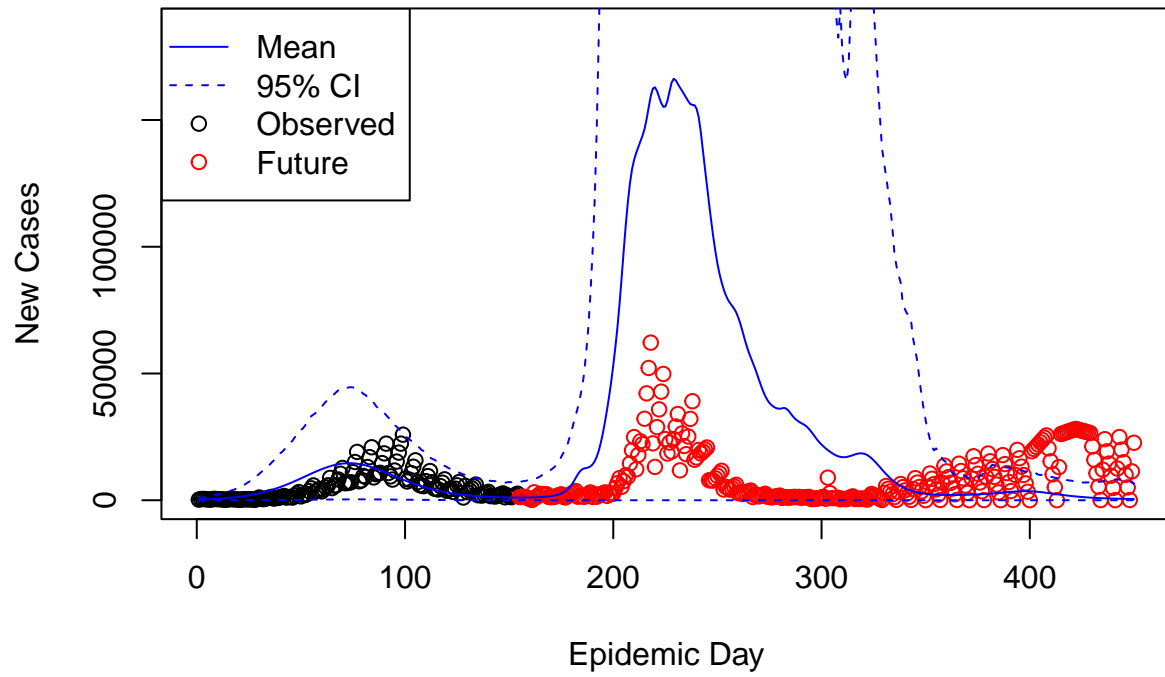
Model 4: Posterior Distribution location ALABAMA



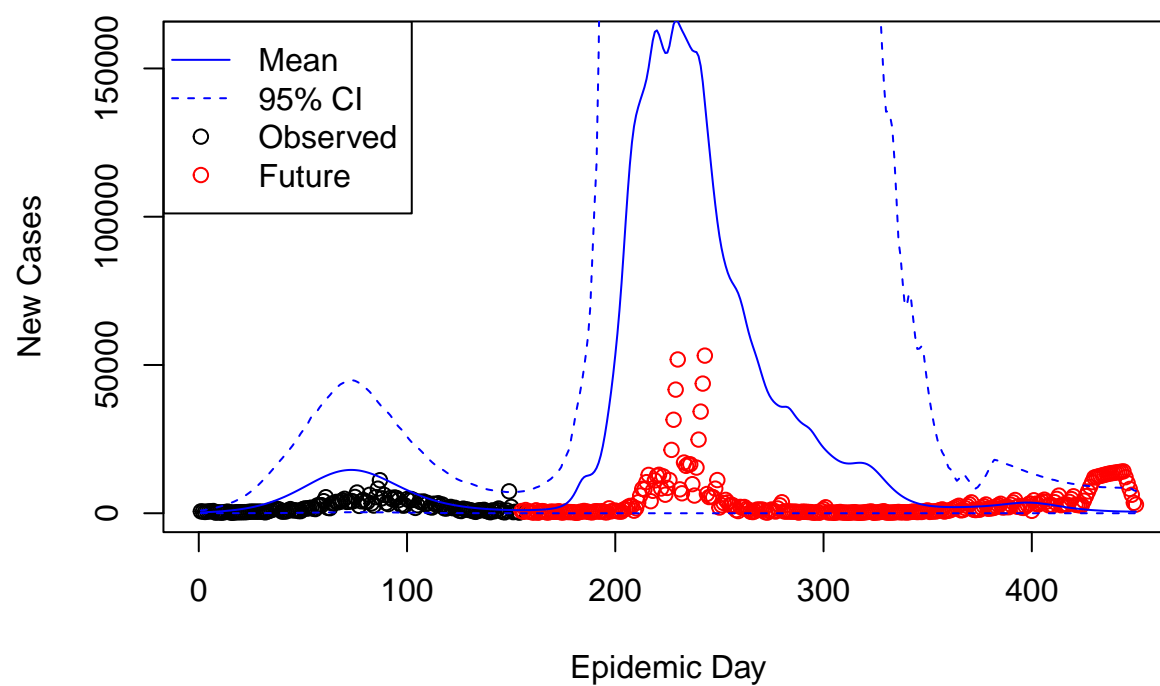
Model 4: Posterior Distribution location FLORIDA



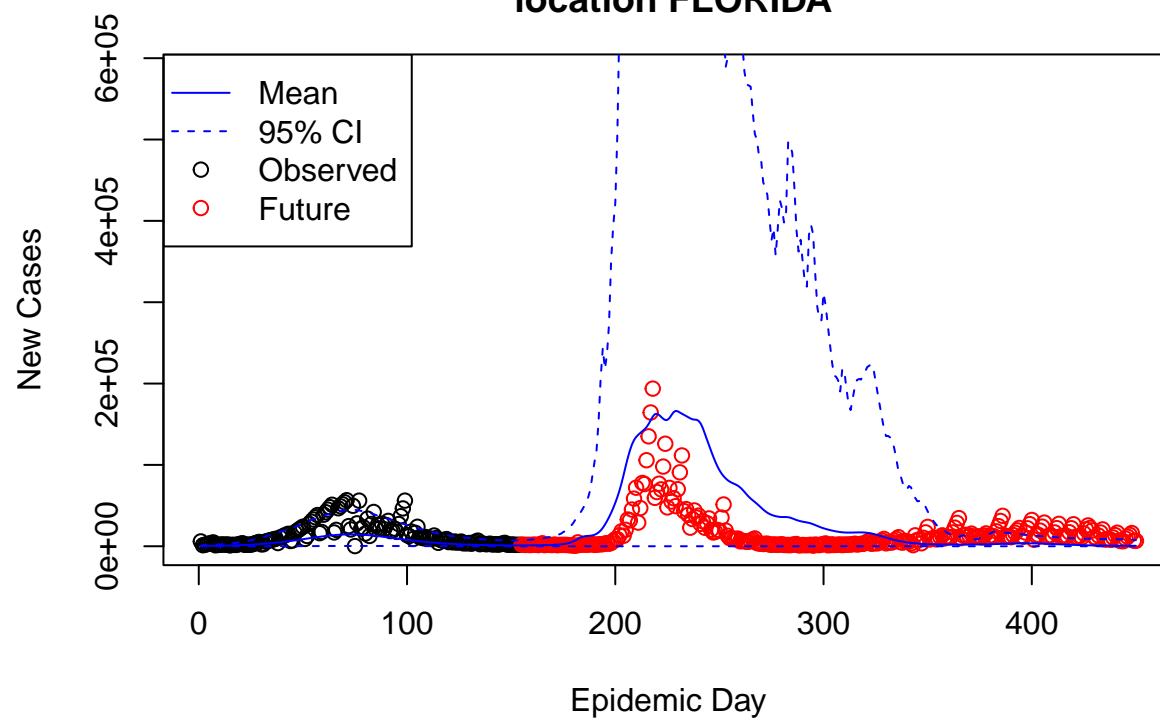
Model 4: Posterior Distribution location GEORGIA



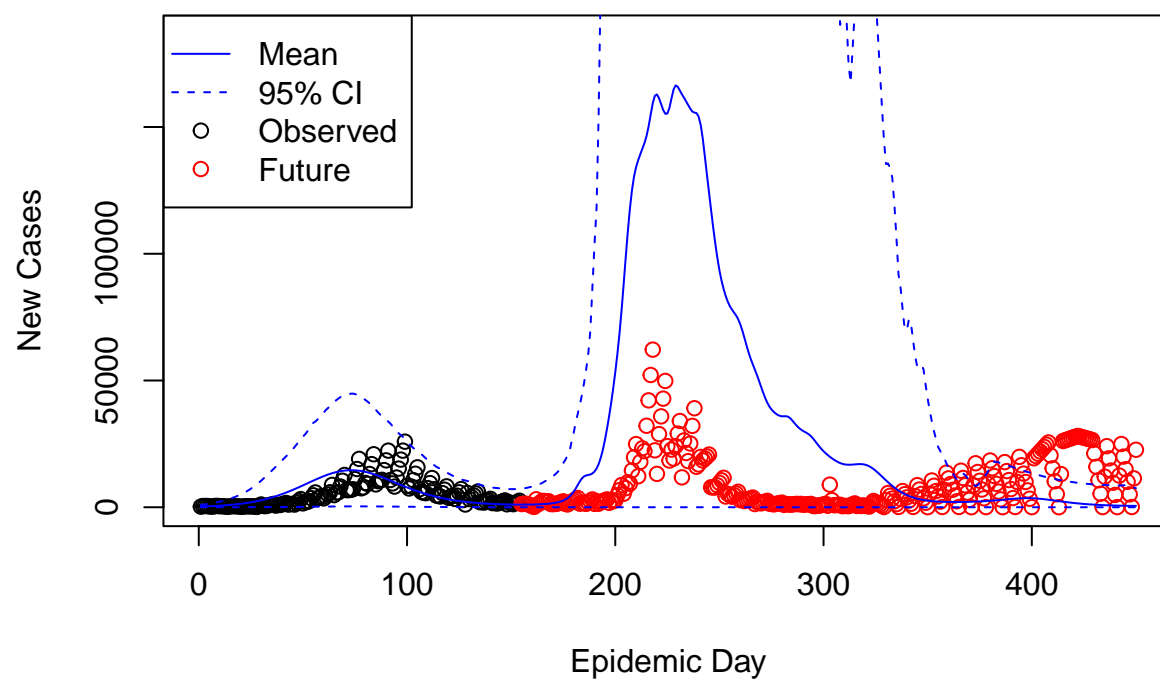
Model 4: Posterior Predictive Distribution location ALABAMA



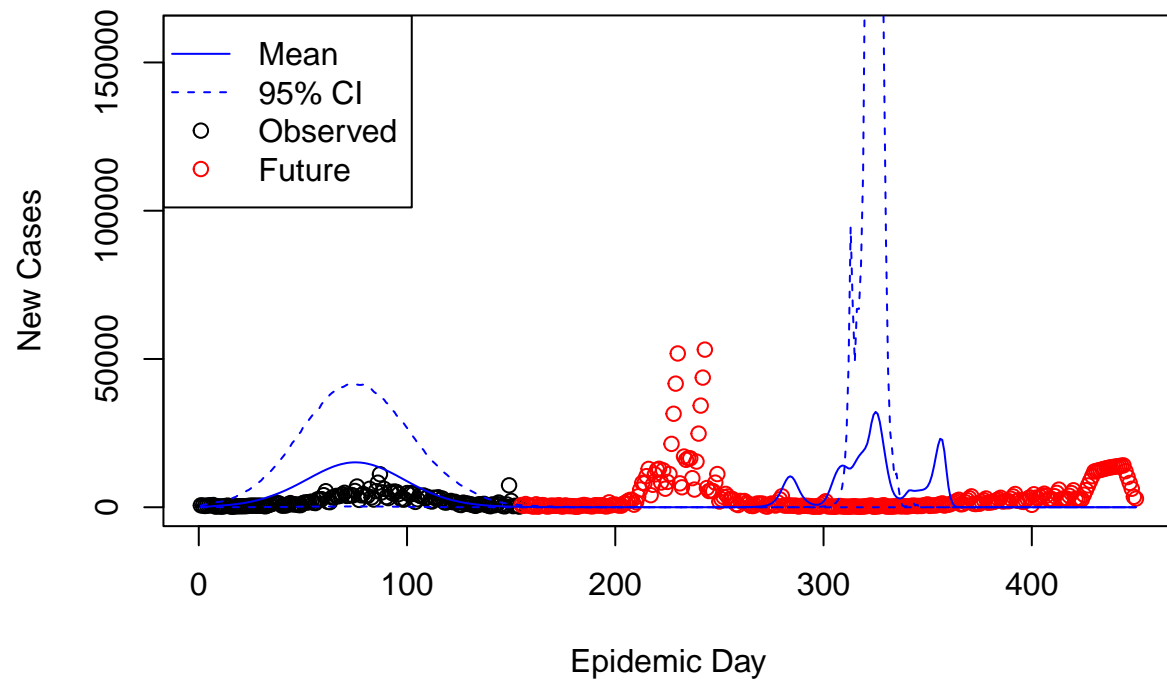
Model 4: Posterior Predictive Distribution location FLORIDA



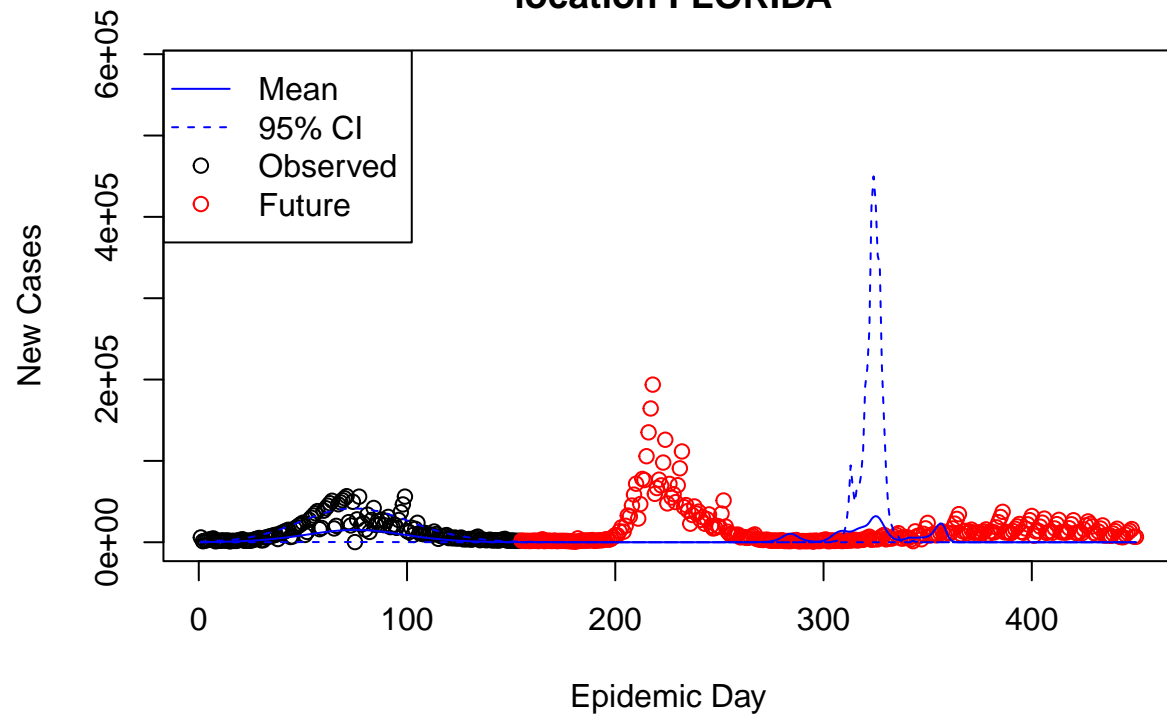
Model 4: Posterior Predictive Distribution location GEORGIA



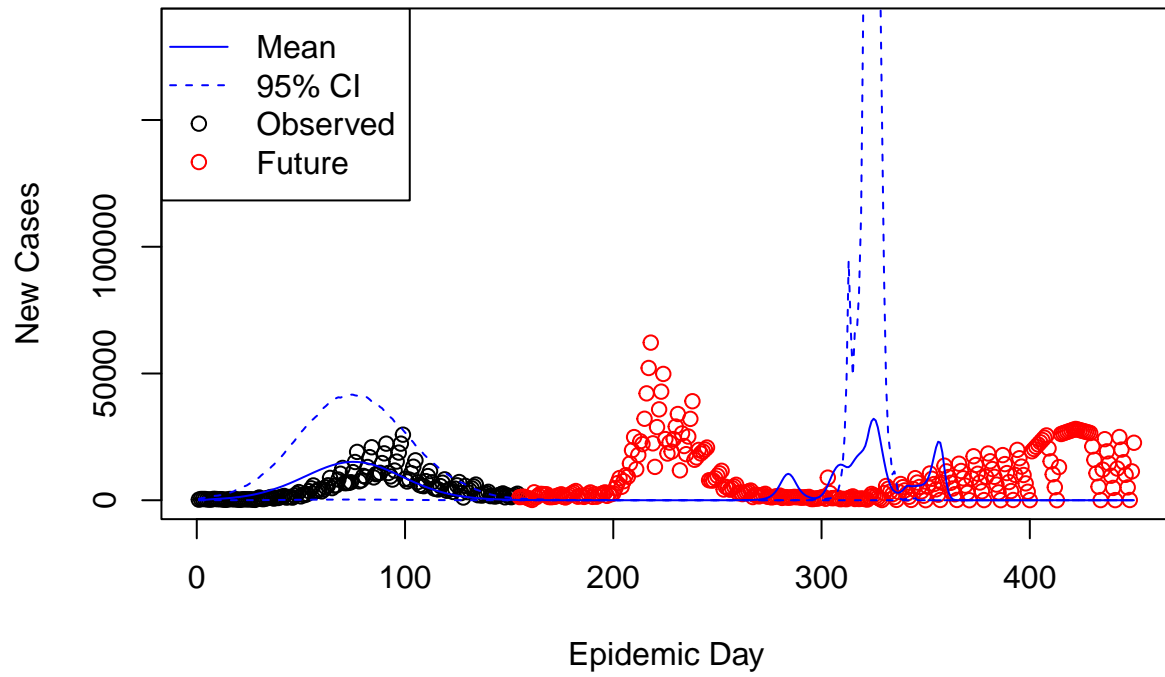
Model 3 (Weibull Distribution): Posterior Distribution location ALABAMA



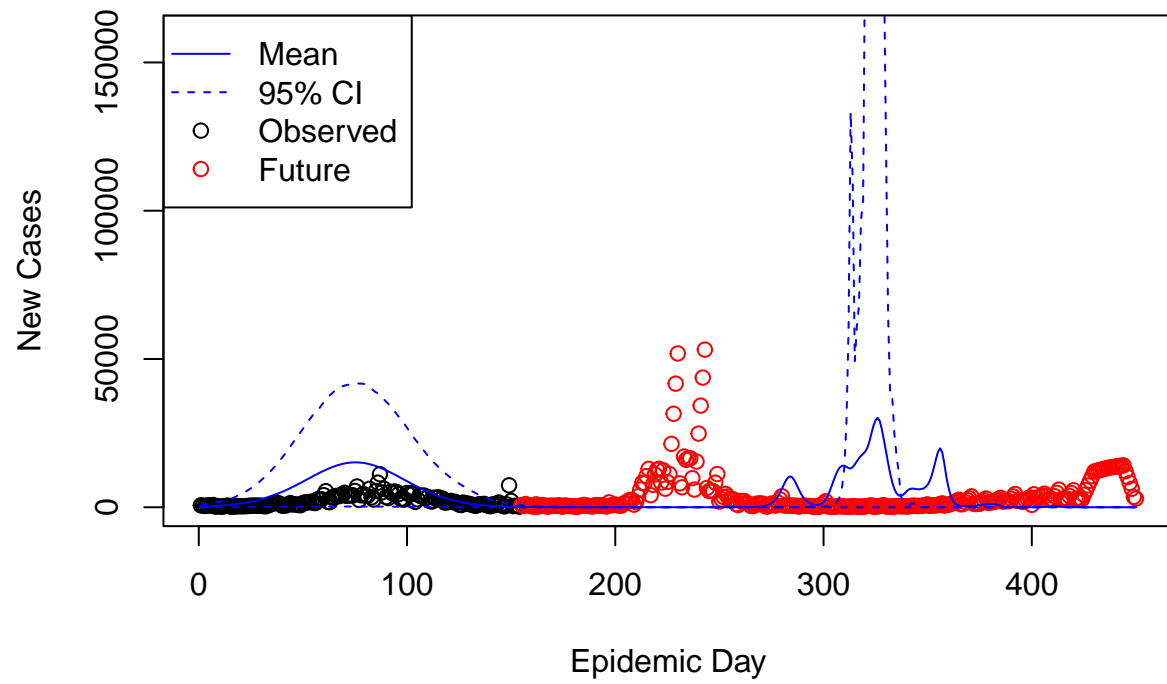
Model 3 (Weibull Distribution): Posterior Distribution location FLORIDA



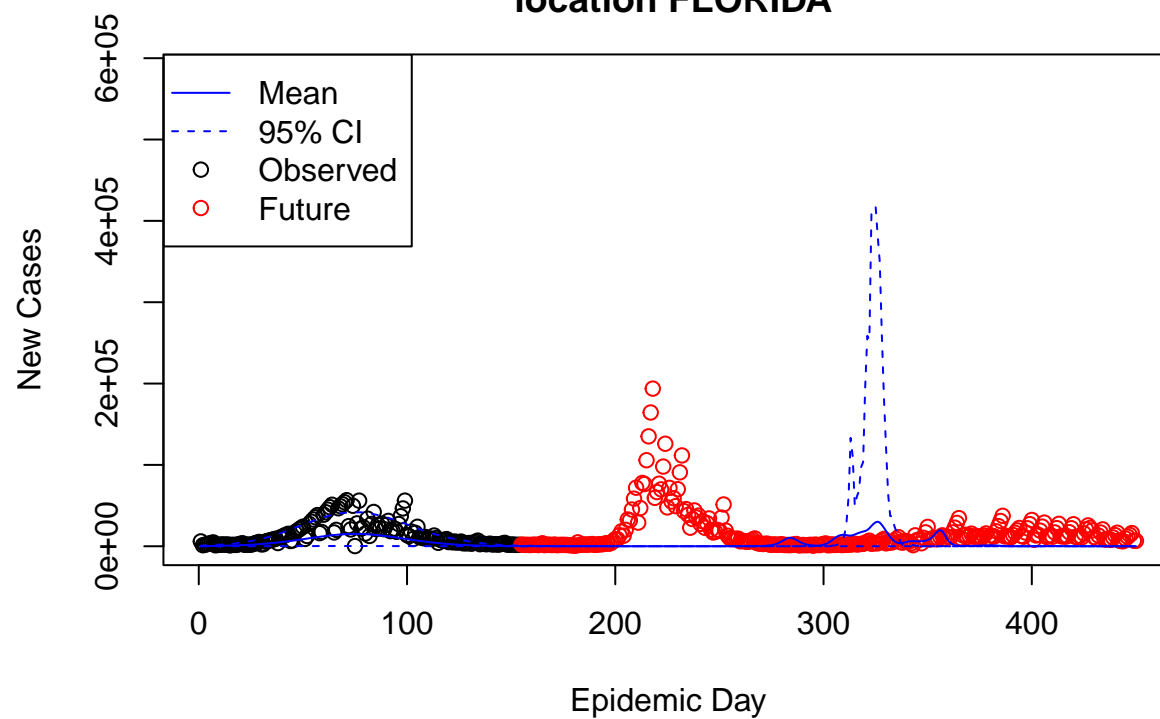
Model 3 (Weibull Distribution): Posterior Distribution location GEORGIA



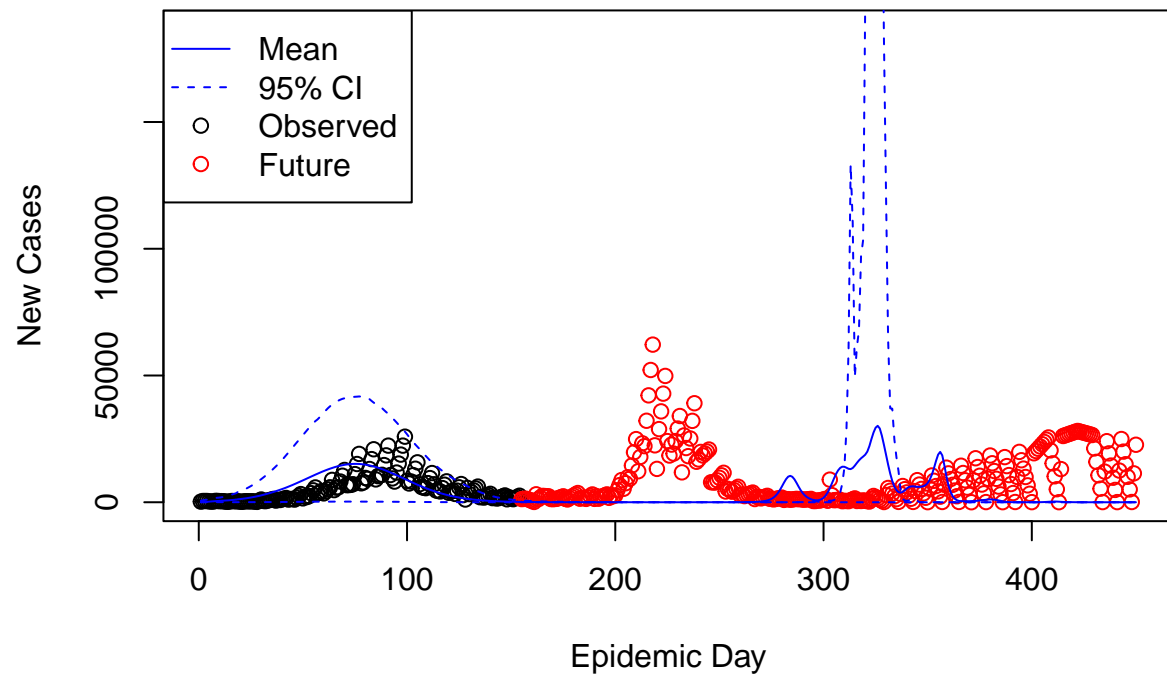
Model 3 (Weibull Distribution): Posterior Predictive Distribution location ALABAMA



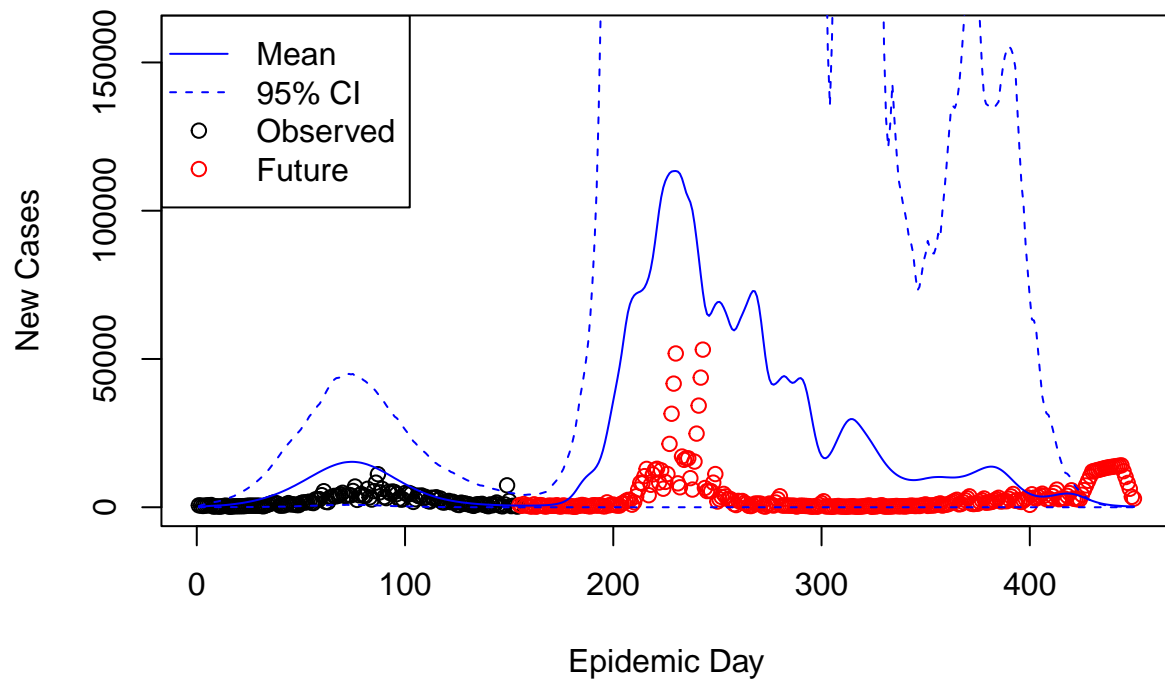
Model 3 (Weibull Distribution): Posterior Predictive Distribution location FLORIDA



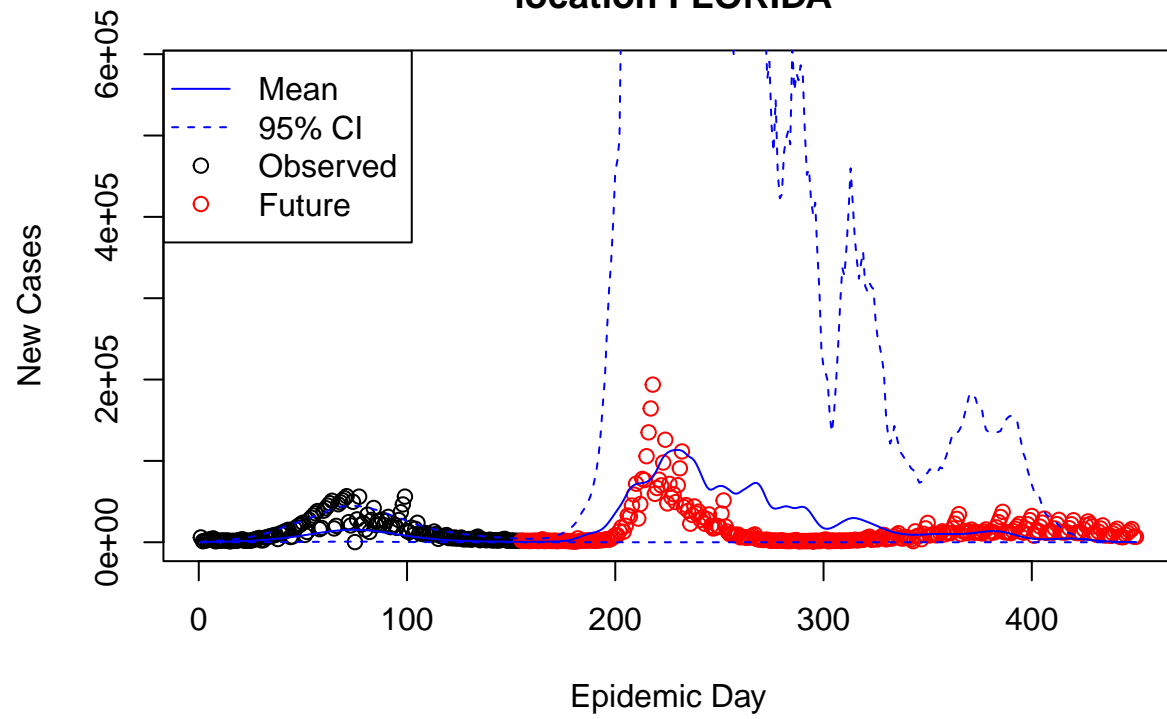
Model 3 (Weibull Distribution): Posterior Predictive Distribution location GEORGIA



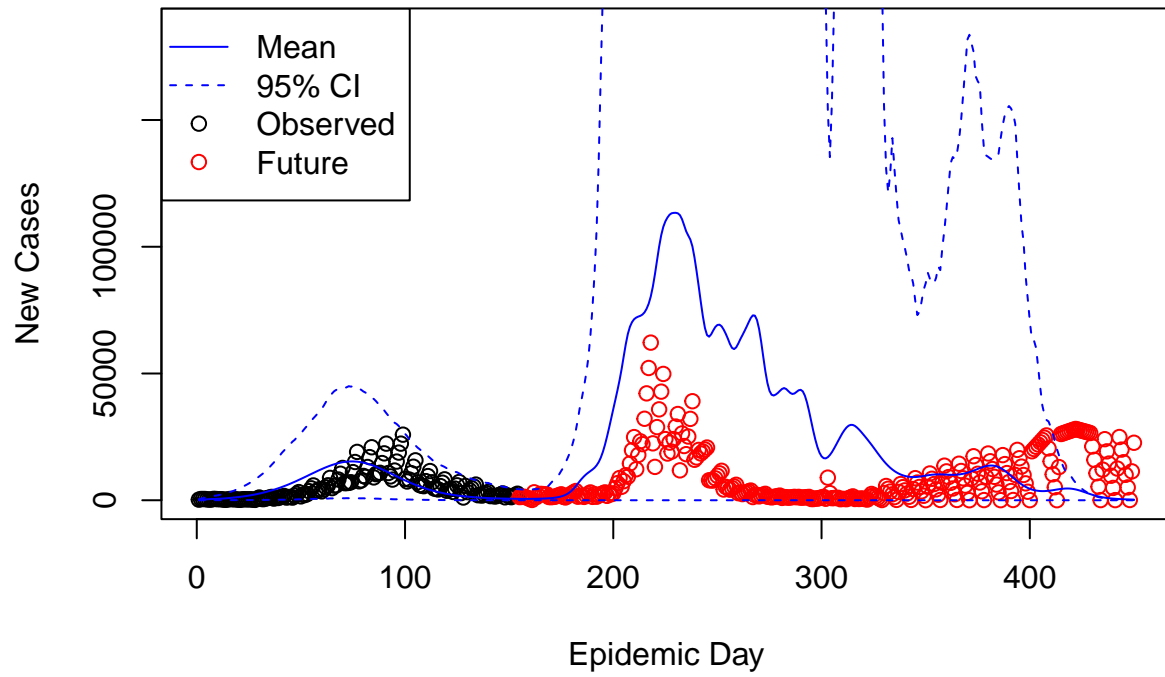
Model 4 (Weibull Distribution): Posterior Distribution location ALABAMA



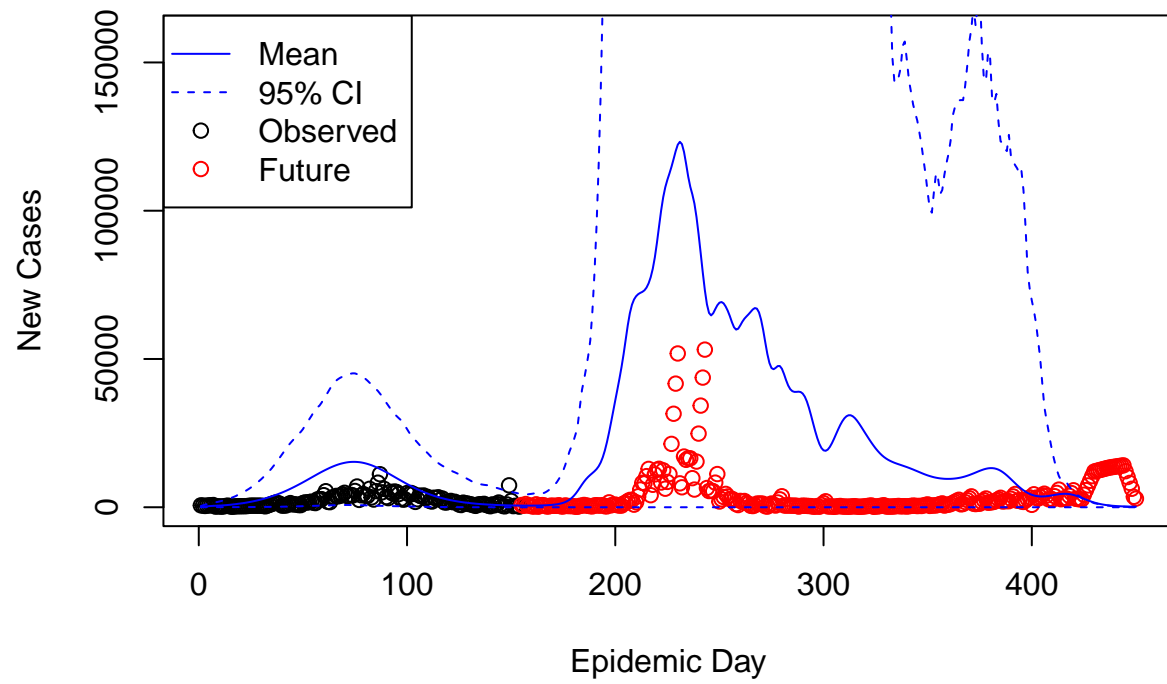
Model 4 (Weibull Distribution): Posterior Distribution location FLORIDA



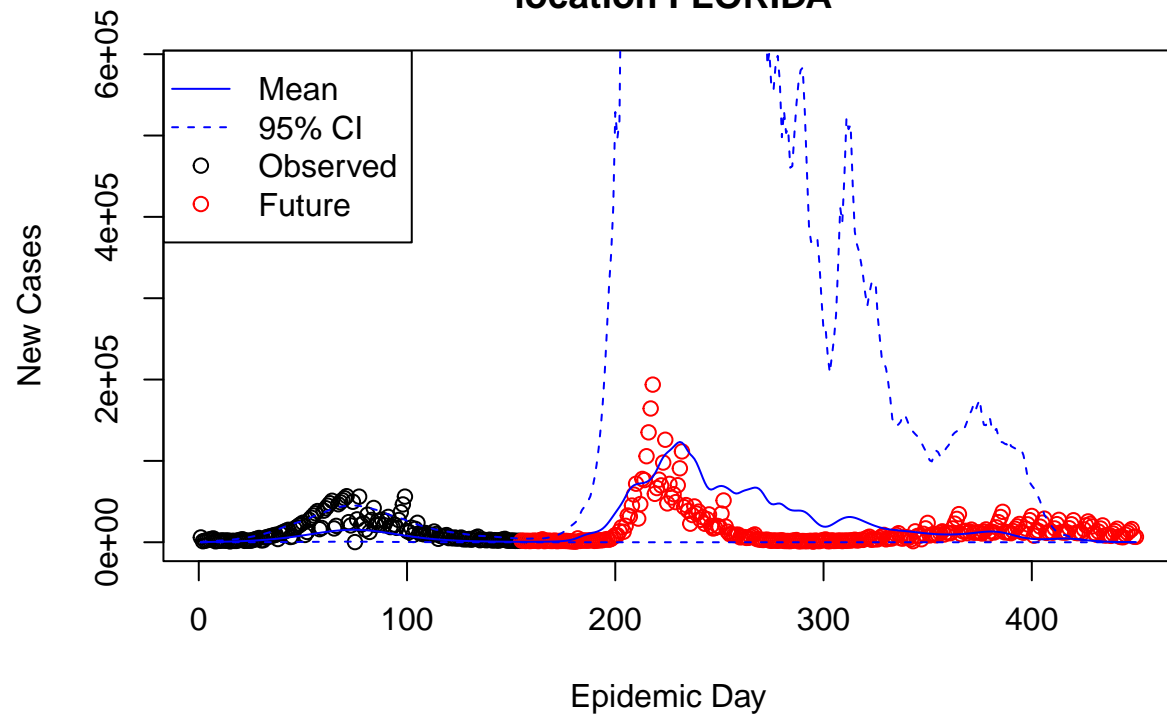
Model 4 (Weibull Distribution): Posterior Distribution location GEORGIA



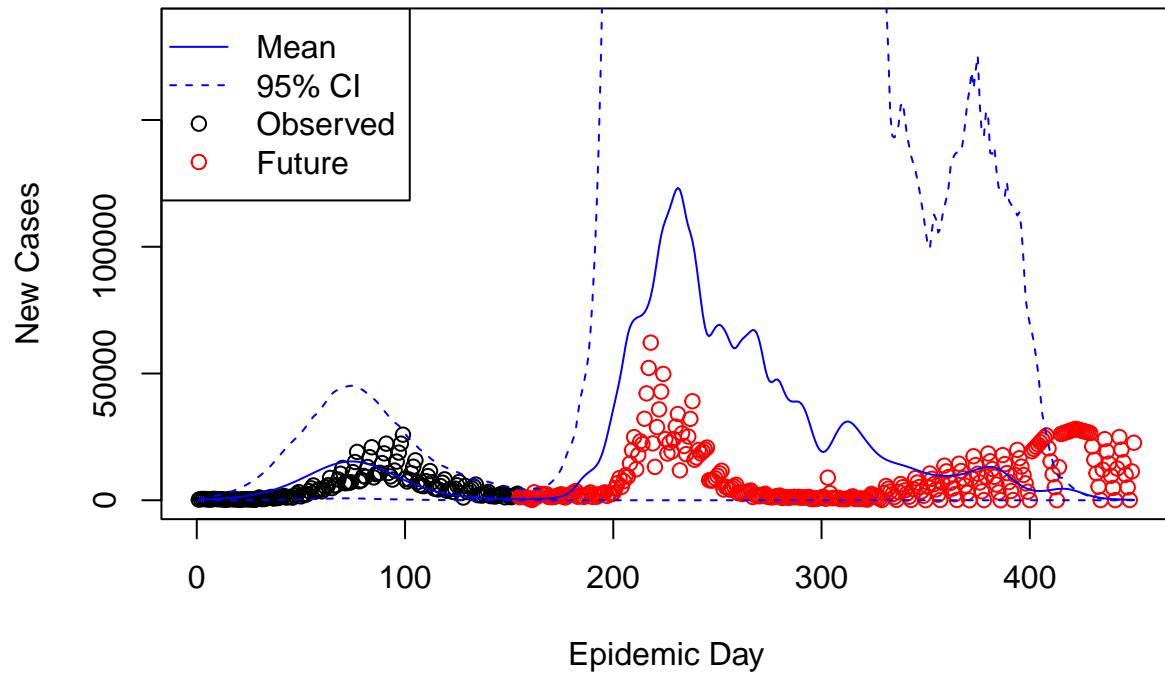
Model 4 (Weibull Distribution): Posterior Predictive Distribution location ALABAMA



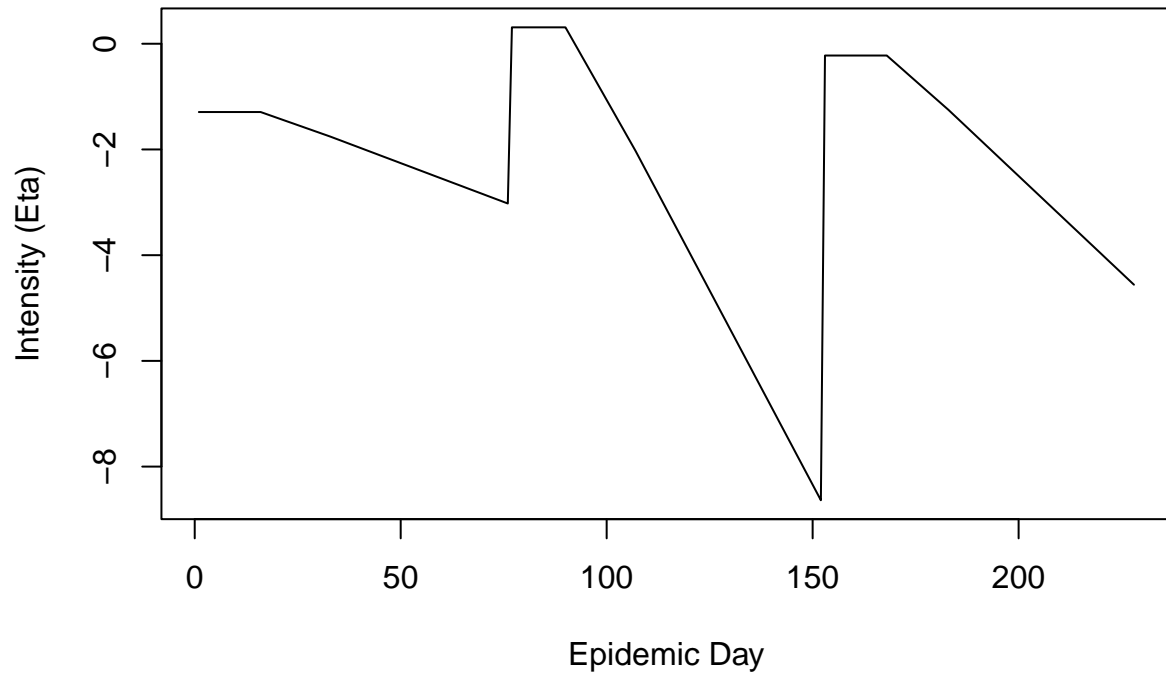
Model 4 (Weibull Distribution): Posterior Predictive Distribution location FLORIDA



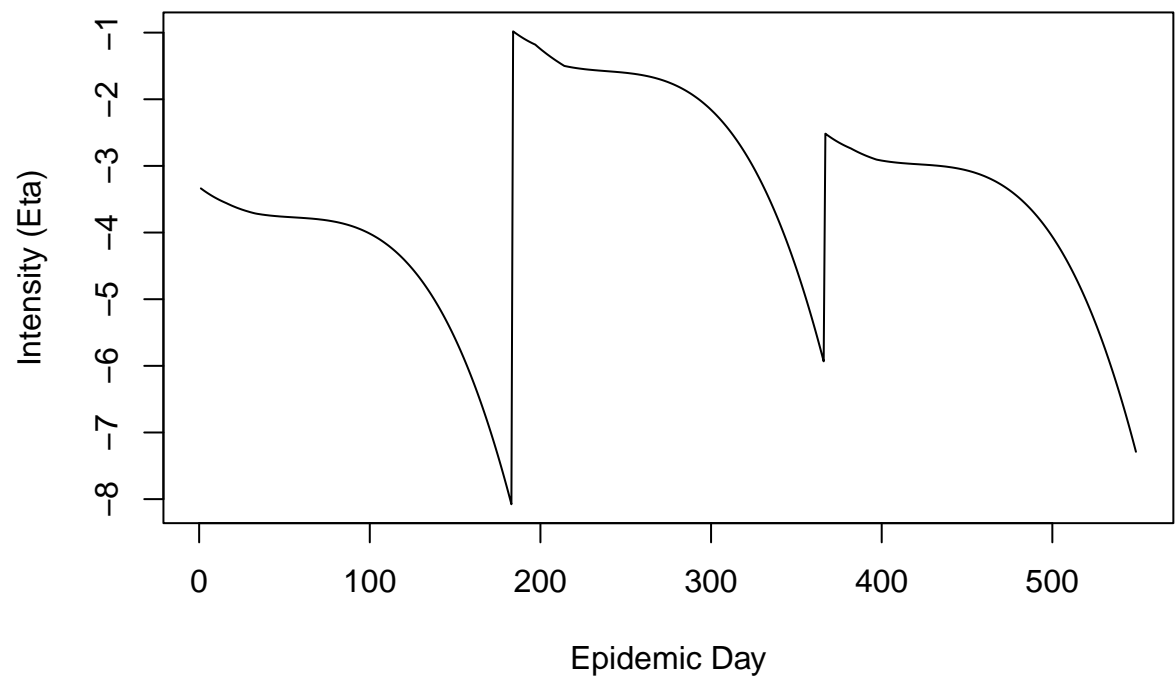
Model 4 (Weibull Distribution): Posterior Predictive Distribution location GEORGIA



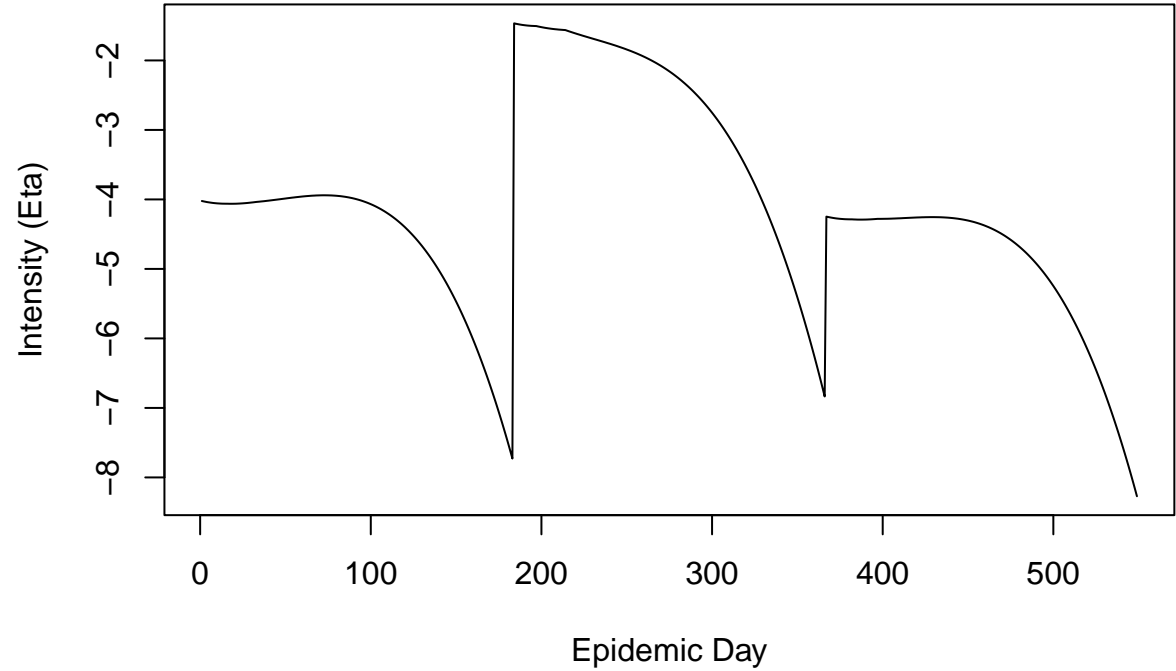
Model 1a Intensity Prediction



Model 2a Intensity Prediction



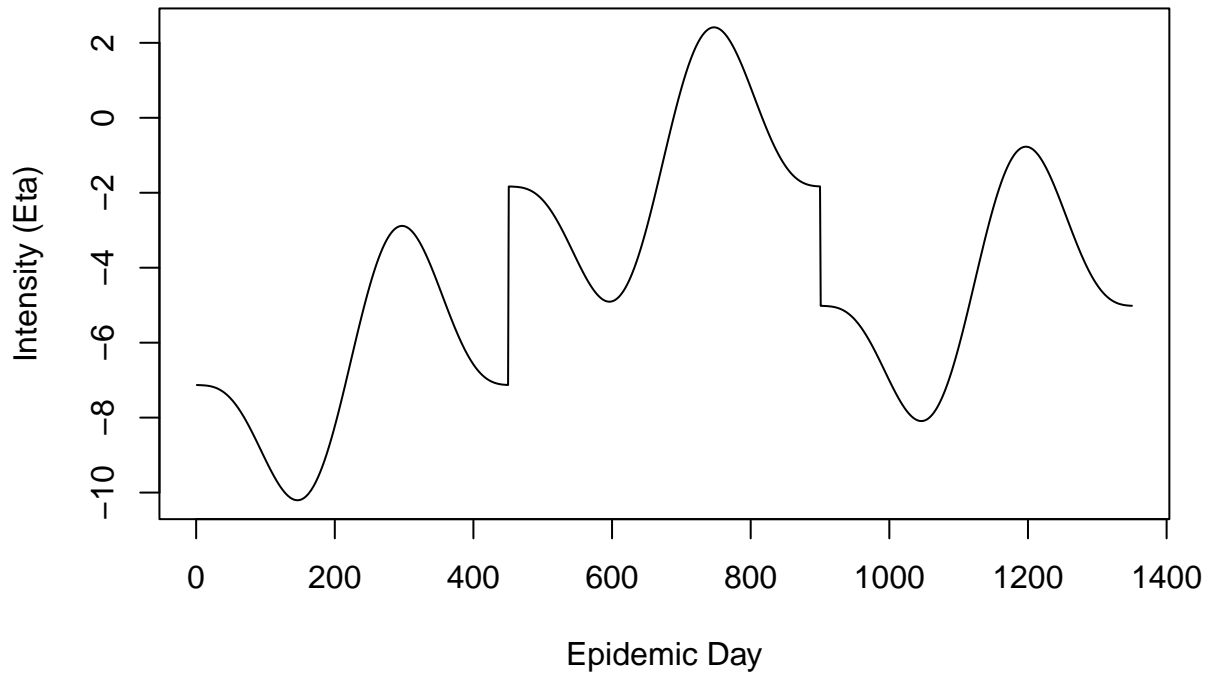
Model 2a (Weibull) Intensity Prediction



Model 4 (Exponential Distribution) Intensity Prediction



Model 4 (Weibull Distribution) Intensity Prediction



Model 1a

```
## Summary: SEIR Model
##
## Locations: 3
## Time Points: 76
## Data Model Parameters: 0
## Exposure Process Parameters: 5
## Reinfection Model Parameters: 0
## Spatial Parameters: 3
## Transition Parameters: 2
##
##
## Parameter Estimates:
```

	Mean	SD	95% LB	95% UB
Beta_SE_1	-1.292	0.300	-1.971	-0.743
Beta_SE_2	0.310	0.169	-0.001	0.667
Beta_SE_3	-0.223	0.165	-0.539	0.135
Beta_SE_4	-13.740	2.247	-17.908	-9.854
Beta_SE_5	-0.951	4.690	-9.492	8.177
rho_1	0.158	0.098	0.022	0.388
rho_2	0.164	0.090	0.019	0.321
rho_3	0.340	0.067	0.209	0.463
gamma_EI	0.199	0.048	0.125	0.289

## gamma_IR	0.062	0.032	0.010	0.120
## S0_1	4903185.000	0.000	4903185.000	4903185.000
## S0_2	21477733.000	0.000	21477733.000	21477733.000
## S0_3	10617423.000	0.000	10617423.000	10617423.000
## E0_1	0.000	0.000	0.000	0.000
## E0_2	2.000	0.000	2.000	2.000
## E0_3	0.000	0.000	0.000	0.000
## I0_1	0.000	0.000	0.000	0.000
## I0_2	2.000	0.000	2.000	2.000
## I0_3	0.000	0.000	0.000	0.000
## R0_1	0.000	0.000	0.000	0.000
## R0_2	0.000	0.000	0.000	0.000
## R0_3	0.000	0.000	0.000	0.000

Model 2a

```
## Summary: SEIR Model
##
## Locations: 3
## Time Points: 183
## Data Model Parameters: 0
## Exposure Process Parameters: 8
## Reinfection Model Parameters: 0
## Spatial Parameters: 1
## Transition Parameters: 2
##
##
## Parameter Estimates:
```

##	Mean	SD	95% LB	95% UB
## Beta_SE_1	-5.313	4.276	-14.944	0.849
## Beta_SE_2	-0.119	0.918	-1.950	1.364
## Beta_SE_3	-3.385	2.716	-8.989	1.654
## Beta_SE_4	-0.674	4.692	-8.543	8.983
## Beta_SE_5	-2.159	5.635	-13.585	6.947
## Beta_SE_6	-4.187	3.319	-11.032	2.379
## Beta_SE_7	2.482	4.783	-5.428	11.867
## Beta_SE_8	-5.316	4.567	-14.254	2.648
## rho_1	0.386	0.160	0.098	0.725
## gamma_EI	0.163	0.040	0.092	0.237
## gamma_IR	0.056	0.039	0.005	0.152
## S0_1	4903185.000	0.000	4903185.000	4903185.000
## S0_2	21477733.000	0.000	21477733.000	21477733.000
## S0_3	10617423.000	0.000	10617423.000	10617423.000
## E0_1	0.000	0.000	0.000	0.000
## E0_2	2.000	0.000	2.000	2.000
## E0_3	0.000	0.000	0.000	0.000
## I0_1	0.000	0.000	0.000	0.000
## I0_2	2.000	0.000	2.000	2.000
## I0_3	0.000	0.000	0.000	0.000
## R0_1	0.000	0.000	0.000	0.000
## R0_2	0.000	0.000	0.000	0.000
## R0_3	0.000	0.000	0.000	0.000

Model 2a (Weibull Distribution)

```
## Summary: SEIR Model
##
## Locations: 3
## Time Points: 183
## Data Model Parameters: 0
## Exposure Process Parameters: 8
## Reinfection Model Parameters: 0
## Spatial Parameters: 3
## Transition Parameters: 4
##
##
## Parameter Estimates:
##           Mean      SD      95% LB      95% UB
## Beta_SE_1    -4.022  2.746    -10.427     0.587
## Beta_SE_2    -1.466  1.463     -4.396     1.220
## Beta_SE_3    -4.247  2.844    -10.404     1.077
## Beta_SE_4    -0.526  3.184     -7.067     4.965
## Beta_SE_5    -0.714  3.122     -5.919     4.863
## Beta_SE_6    -0.350  3.739     -8.562     5.366
## Beta_SE_7     1.894  3.883     -6.094     9.465
## Beta_SE_8    -3.394  3.608    -10.085     3.446
## rho_1         0.334  0.163      0.023     0.614
## rho_2         0.150  0.103      0.005     0.365
## rho_3         0.263  0.142      0.033     0.547
## latent_shape  2.139  0.252      1.627     2.595
## latent_scale  6.829  0.751      5.396     8.167
## infectious_shape  4.959  1.826      1.298     8.169
## infectious_scale 16.933  4.818      9.094    25.779
## S0_1        4903185.000  0.000  4903185.000  4903185.000
## S0_2       21477733.000  0.000  21477733.000  21477733.000
## S0_3       10617423.000  0.000  10617423.000  10617423.000
## E0_1         0.000  0.000      0.000     0.000
## E0_2         2.000  0.000      2.000     2.000
## E0_3         0.000  0.000      0.000     0.000
## I0_1         0.000  0.000      0.000     0.000
## I0_2         2.000  0.000      2.000     2.000
## I0_3         0.000  0.000      0.000     0.000
## R0_1         0.000  0.000      0.000     0.000
## R0_2         0.000  0.000      0.000     0.000
## R0_3         0.000  0.000      0.000     0.000
```

Model 4 (Exponential)

```
## Summary: SEIR Model
##
## Locations: 3
## Time Points: 450
## Data Model Parameters: 0
## Exposure Process Parameters: 8
## Reinfection Model Parameters: 0
```

```

## Spatial Parameters: 3
## Transition Parameters: 2
##
##
## Parameter Estimates:
##           Mean      SD      95% LB      95% UB
## Beta_SE_1    -4.207  3.603    -11.699     1.945
## Beta_SE_2     0.758  2.809     -5.076     5.404
## Beta_SE_3    -3.810  3.900    -12.162     3.151
## Beta_SE_4    -1.848  5.594    -11.806     9.716
## Beta_SE_5    -1.472  7.962    -15.557    12.792
## Beta_SE_6    -3.400  1.387     -6.064    -0.504
## Beta_SE_7    -0.872  1.276     -3.247     1.752
## Beta_SE_8     3.378  1.430     0.958     5.839
## rho_1         0.215  0.142     0.016     0.511
## rho_2         0.145  0.098     0.005     0.360
## rho_3         0.297  0.146     0.092     0.604
## gamma_EI      0.151  0.041     0.080     0.225
## gamma_IR      0.065  0.031     0.008     0.116
## S0_1        4870968.000  0.000  4870968.000  4870968.000
## S0_2        21348159.000  0.000  21348159.000  21348159.000
## S0_3        10543493.000  0.000  10543493.000  10543493.000
## E0_1           500.000  0.000     500.000     500.000
## E0_2          5000.000  0.000     5000.000     5000.000
## E0_3           200.000  0.000     200.000     200.000
## I0_1           640.000  0.000     640.000     640.000
## I0_2          5937.000  0.000     5937.000     5937.000
## I0_3           241.000  0.000     241.000     241.000
## R0_1          20048.000  0.000     20048.000     20048.000
## R0_2          79782.000  0.000     79782.000     79782.000
## R0_3          38080.000  0.000     38080.000     38080.000

```

Model 4 (Weibull)

```

## Summary: SEIR Model
##
## Locations: 3
## Time Points: 450
## Data Model Parameters: 0
## Exposure Process Parameters: 8
## Reinfection Model Parameters: 0
## Spatial Parameters: 3
## Transition Parameters: 4
##
##
## Parameter Estimates:
##           Mean      SD      95% LB      95% UB
## Beta_SE_1    -4.896  3.832    -11.993     1.497
## Beta_SE_2     1.049  2.709     -5.030     5.546
## Beta_SE_3    -2.596  3.560    -11.222     2.383
## Beta_SE_4    -2.059  5.204    -12.425     6.616
## Beta_SE_5    -3.763  6.784    -16.596     8.209
## Beta_SE_6    -2.832  1.514     -5.746     0.418

```

## Beta_SE_7	-0.391	1.514	-3.196	2.670
## Beta_SE_8	2.770	1.672	-0.579	5.980
## rho_1	0.306	0.160	0.048	0.629
## rho_2	0.190	0.121	0.015	0.433
## rho_3	0.231	0.148	0.017	0.511
## latent_shape	2.043	0.478	1.153	2.839
## latent_scale	6.819	1.149	4.622	9.081
## infectious_shape	4.891	2.319	0.710	9.211
## infectious_scale	22.714	8.218	6.585	36.181
## S0_1	4870968.000	0.000	4870968.000	4870968.000
## S0_2	21348159.000	0.000	21348159.000	21348159.000
## S0_3	10543493.000	0.000	10543493.000	10543493.000
## E0_1	500.000	0.000	500.000	500.000
## E0_2	5000.000	0.000	5000.000	5000.000
## E0_3	200.000	0.000	200.000	200.000
## I0_1	640.000	0.000	640.000	640.000
## I0_2	5937.000	0.000	5937.000	5937.000
## I0_3	241.000	0.000	241.000	241.000
## R0_1	20048.000	0.000	20048.000	20048.000
## R0_2	79782.000	0.000	79782.000	79782.000
## R0_3	38080.000	0.000	38080.000	38080.000

Bayes Factor (Model 1a vs Model 1b vs Model 1c)

##	Distance	CAR	Gravity
## Distance	1.00000000	16.462687	9.3474576
## CAR	0.06074343	1.000000	0.5677966
## Gravity	0.10698096	1.761194	1.0000000

Bayes Factor (Model 2a vs Model 2b vs Model 2c)

##	Distance	CAR	Gravity
## Distance	1.00000000	1.3561116	1.383407
## CAR	0.7374024	1.0000000	1.020128
## Gravity	0.7228531	0.9802695	1.0000000

Bayes Factor (Exponential vs Weibull under Model 1a)

##	[,1]	[,2]
## [1,]	1.0000000	3.022843
## [2,]	0.3308144	1.000000

Bayes Factor (Exponential vs Weibull under Model 2a)

##	[,1]	[,2]
## [1,]	1.0000000	0.622276
## [2,]	1.607004	1.000000

Coverage, width and bias for model 1a with exponential distribution, SMC-ABC (latent and infectious period estimates)

```
## $coverage
## [1] 1
##
## $width
## [1] 0.136887
##
## $bias
## [1] -16.94345
```

```
## $coverage
## [1] 1
##
## $width
## [1] 0.1037973
##
## $bias
## [1] 1.051762
```

Coverage, width and bias for model 2a with exponential distribution, SMC-ABC (latent and infectious period estimates)

```
## $coverage
## [1] 1
##
## $width
## [1] 0.08563094
##
## $bias
## [1] 4.058638
```

```
## $coverage
## [1] 1
##
## $width
## [1] 0.08526893
##
## $bias
## [1] 3.261002
```

Coverage, width and bias for model 2a with Weibull distribution, SMC-ABC (latent and infectious period estimates (shape and scale))

```
## $coverage
## [1] 1
```

```
##
## $width
## [1] 0.9968238
##
## $bias
## [1] 2.732983
```

```
## $coverage
## [1] 1
##
## $width
## [1] 2.849094
##
## $bias
## [1] 0.3229856
```

```
## $coverage
## [1] 1
##
## $width
## [1] 7.156211
##
## $bias
## [1] 30.53288
```

```
## $coverage
## [1] 1
##
## $width
## [1] 16.76137
##
## $bias
## [1] -5.720726
```

Coverage, width and bias for model 4 with exponential distribution, SMC-ABC (latent and infectious period estimates)

```
## $coverage
## [1] 1
##
## $width
## [1] 0.1339373
##
## $bias
## [1] 9.422127
```

```
## $coverage
## [1] 1
##
## $width
## [1] 0.1050449
```

```
##
## $bias
## [1] -2.732824
```

Coverage, width and bias for model 4 with Weibull distribution, SMC-ABC (latent and infectious period estimates (shape and scale))

```
## $coverage
## [1] 1
##
## $width
## [1] 1.755215
##
## $bias
## [1] -1.880829
```

```
## $coverage
## [1] 1
##
## $width
## [1] 4.488851
##
## $bias
## [1] 0.1787558
```

```
## $coverage
## [1] 1
##
## $width
## [1] 8.812926
##
## $bias
## [1] 28.75374
```

```
## $coverage
## [1] 1
##
## $width
## [1] 32.62747
##
## $bias
## [1] 26.46842
```

Runtimes

```
##          user.self sys.self elapsed
## model 1   9013.290   75.045 1427.865
## model 2    360.886   13.259  57.756
```

## model 3	21764.164	189.012	3310.206
## model 4	4839.358	63.619	830.120
## model 5	9035.048	91.580	1469.613
## model 6	3444.724	22.469	468.603
## model 7	761.381	26.397	115.032
## model 8	3020.588	39.741	427.094
## model 9	14090.237	104.257	2056.698
## model 10	4069.530	31.586	544.678
## model 11	3289.843	26.394	441.865
## model 12	5720.690	35.189	793.683
## model 13	6594.632	47.456	919.279
## model 14	25686.391	169.012	3726.878
## model 15	18691.818	83.698	2506.355