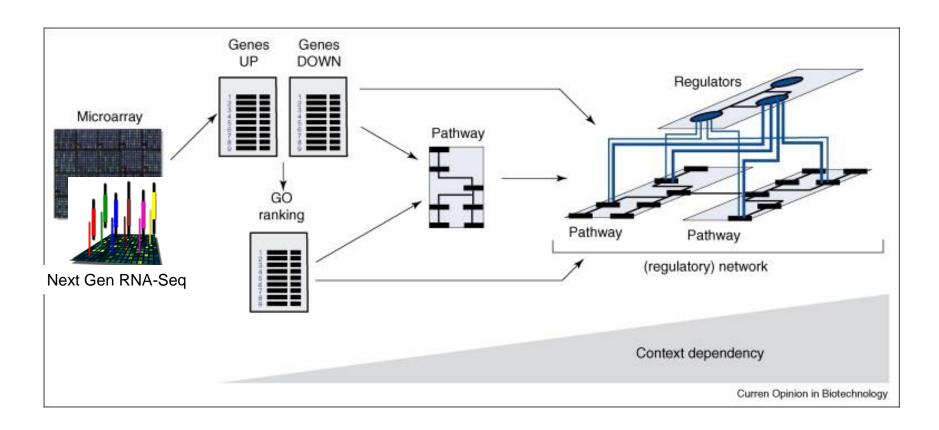


Pathway analysis

Biostat & Bioinfo short course series
7/30/2018
Jianying Li

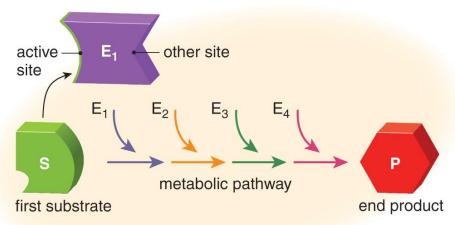
The Road to Pathway Analysis



What are biological pathways??

- Definition in Wikipedia:
 - "... a series of actions among molecules in a cell that leads to a certain product or a change in a cell."

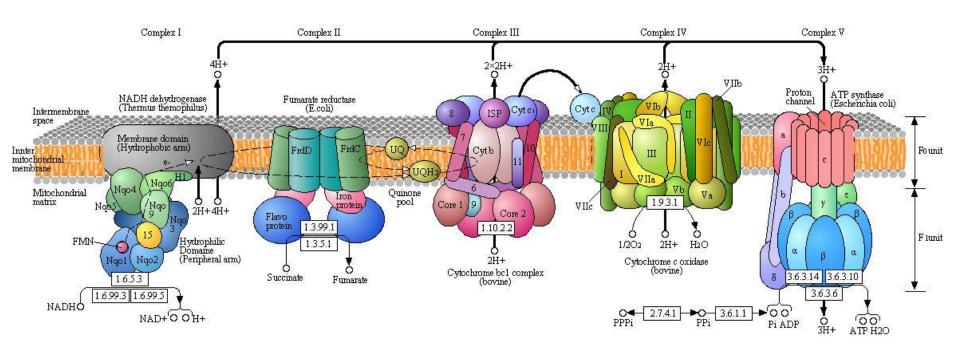
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Active enzyme and active pathway

- Pathway types:
 - Metabolic pathway
 - Ontologies
 - Gene regulation pathways
 - Signal transduction pathways

The oxidative phosphorylation



http://employees.csbsju.edu/hjakubowski/classes/ch331/oxphos/olcouplingoxphos.html

Why pathway analysis?

- Biological responses are systematic and collaborative
- Modern technologies provide high-throughput measurement
- Rich knowledge-based accumulation available
- Statistical frame works provide the analytical component

Biological responses are systematic and collaborative

- Genes are associated and respond collectively toward perturbation or condition changes
- Signal obtained from a collection of genes working together reflects a bigger picture
- PA offers apparent advantage over single-gene analysis
 - Different samples from a common condition may have different key genes that are all driving changes in the same pathway
 - Pathways may be perturbed by subtle changes in many genes
 - A small list of enriched pathways may be easier to interpret than a large list of associated genes
 - Pathways results from different studies may overlap better than single-gene results

Modern technologies provide highthroughput measurement

- Modern technologies offer large scale (landscape) measurement
 - MicroArray gene expression
 - Whole genome exome array
 - Nano-strings
- Next generation sequencing platforms
 - RNAseq
 - ChIP-seq

Rich knowledge-based accumulation available

- GeneOntology (originated since 1998)
 - Molecular function describing activities, such as catalytic or binding activities, at the molecular level
 - Biological process referring to a biological objective to which the gene product contributes
 - Cellular component referring to the place in the cell (i.e. the location) where a gene product is found
- KEGG pathway (originated since 1996)
 - Metabolism: carbohydrates, energy, lipid, nucleotides, amino acid, xenobiotics
 - Human diseases
 - Genetic information processing
- Transfac/Transpath
 - Data on transcription factors, their experimentally-proven binding sites, and regulated genes
 - Protein-protein interactions and directed modification of proteins involved in signal transduction pathways,
- It is a knowledge based/driven approach
- Pathway --- gene sets are interexchangble

Molecular Signatures Database (MSigDB v5.2)

Free database (http://www.broadinstitute.org/gsea/msigdb)

hallmark gene sets are coherently expressed signatures derived by aggregating many MSigDB gene sets to represent well-defined biological states or processes.

C1 positional gene sets for each human chromosome and cytogenetic band.

curated gene sets from online pathway databases, publications in PubMed, and knowledge of domain experts.

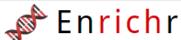
motif gene sets based on conserved cis-regulatory motifs from a comparative analysis of the human, mouse, rat, and dog genomes.

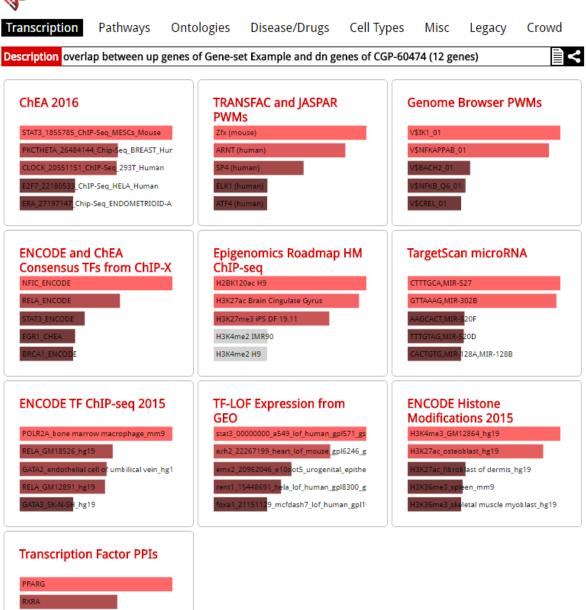
C4 computational gene sets defined by mining large collections of cancer-oriented microarray data.

C5 GO gene sets consist of genes annotated by the same GO terms.

oncogenic signatures defined directly from microarray gene expression data from cancer gene perturbations.

immunologic signatures defined directly from microarray gene expression data from immunologic studies.





http://amp.pharm.mssm.edu/Enrichr/enrich

Statistical frame works

- Well-established statistical and computation algorithms
- Parametric method
 - Hypergeometric test
 - Fisher's exact test
- Non-parametric approaches
 - GSEA
 - GSA
 - Etc.
- Other algorithms
 - Auto expand: Draws sub-networks around the selected objects
 - Shortest paths: Uses Dijkstra's shortest paths algorithm to find the shortest directed paths between the selected objects.
 - Self regulation: Finds the shortest directed paths containing transcription factors between the selected objects
 - Etc.

Hypergeometric Test

- A simple example:
 - 5 patients with the disease D and 5 healthy control subjects
 - Checked for elevated levels of the blood constituent C.
 - 4 of the patients, but only 2 of the healthy subjects show an elevated level of *C*.
- May we infer that the concentration of C is elevated inpatients with disease D more often than in healthy subjects?
- Or could our result have been mere coincidence?

2x2 contingency table

	Patient with disease D	Healthy control subject	Total
Elevated level of compound C	4	2	6
Normal level of compound C	1	3	4
Total	5	5	10

$$E_{r,c} = \frac{(\text{Sum of row } r) \times (\text{Sum of column } c)}{\text{Sample size}}$$

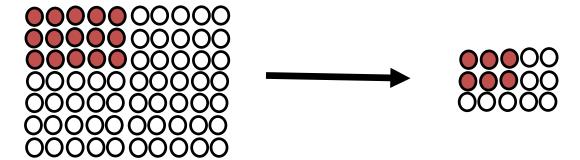
Expected value for top left corner from null model (no association): 5×6 / 10 = 3

Probability to get this 2×2 table without an association between *D* and *C*:

```
Number of ways to Number of ways to
choose 4 out of 5 \times choose 2 out of 5
    patiens to
                           controls to
 \frac{have\ elevated\ C}{nuber\ of\ ways\ to} = \frac{4/2}{10}
            choose 6 our of 10
             persons to have
                elevated C
                   in R:
                   > dhyper( 4, 5, 5, 6 )
```

[1] 0.2380952

Hypergeometric Test (Right-tailed)

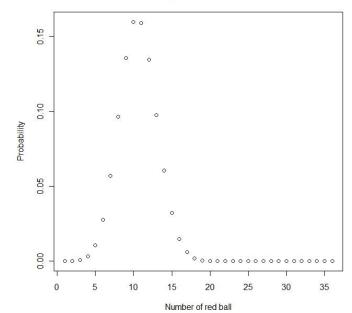


- An urn with two types of marbles:
 - N total # of marbles
 - Of which, m # of red marbles
 - Drawing a red marble is a success!
 - Drawing a white marble is a failure!
- n is the # of marbles randomly drawn
- k is the # of successes (red marbles) in the sample
- Hypergeometric distribution gives the probability

$$P(X = k) = \frac{\binom{m}{k} \binom{N-m}{n-k}}{\binom{N}{n}}. \quad \text{for } k = 0,1,2,...,n \\ k < = m, n-k < = N-m$$

- Number of red ball: 50
 Number of white ball: 120
- Number of ball drawn (without replacement): 36 ← n
- Possible number of success ??
 - (0,1, 2,36),
- Probability to get $\frac{20}{10}$ red balls is: 0.0001494571 p(k=20, 36, 50, 170)

Probablity getting # of success!



Under the null hypothesis, i.e., the assumption that there is no association between elevated levels of compound *C* and presence of disease *D*, the probability that 4 or even more of the patients have elevated levels of *C*,

	Patient with disease D	Healthy control subject	Total
Elevated level of compound C	5	1	6
Normal level of compound C	0	4	4
Total	5	5	10

in R: > dhyper(5, 5, 5, 6) [1] 0.02380952

Under the null hypothesis, i.e., the assumption that there is no association between elevated levels of compound *C* and presence of disease *D*, the probability that 4 or even more of the patients have elevated levels of C,

$$p = \frac{\binom{5}{4}\binom{5}{2}}{\binom{10}{6}} + \frac{\binom{5}{5}\binom{5}{2}}{\binom{10}{6}} = 0.26$$

This is insignificant

```
in R: > 1 - phyper(3, 5, 5, 6) [1] 0.2619048
```

Fisher's Exact Test (FET)

--right-tailed test

	Patient with disease D	Healthy control subject	Total
Elevated level of compound C	X	m-x	m
Normal level of compound C	k-x	n-k + x	n
Total	k	m+n - k	m+n

So, now you are probably given something like the following:

```
x < -4 #patients with elevated level of compound C m < -6 #all with elevated level of compound C n < -4 #all with normal level of compound C k < -5 #total number of patient volunteers
```

Hypergeometric test vs. FET, we shall get same result

phyper((x-1), m, n, k, lower.tail=FALSE)

(fisher.test(matrix(c(x,(k-x), (m-x), (n-k+x)),2,2), alternative='greater'))\$p.value

Pathway analysis (behind the scene)

Contingency table

```
DEG Not DEGs totals

In a GO category x m-x m

Not in GO category k-x n-k+x n

totals k m+n-k m+n (genes on array)
```

So, now you are probably given something like the following:

```
x <- 5 #num_of_DEG in GO

m <- 20 #num_of_gene on chip in GO

n <- 500 #num_of_gene on chip NOT in GO

k <- 40 #num_of_DEG
```

Hypergeometric test vs. FET, we shall get same result

- phyper((x-1), m, n, k, lower.tail=FALSE)
- (fisher.test(matrix(c(x,(k-x), (m-x), (n-k+x)),2,2), alternative='greater'))\$p.value

Ingenuity Pathway Analysis (IPA)

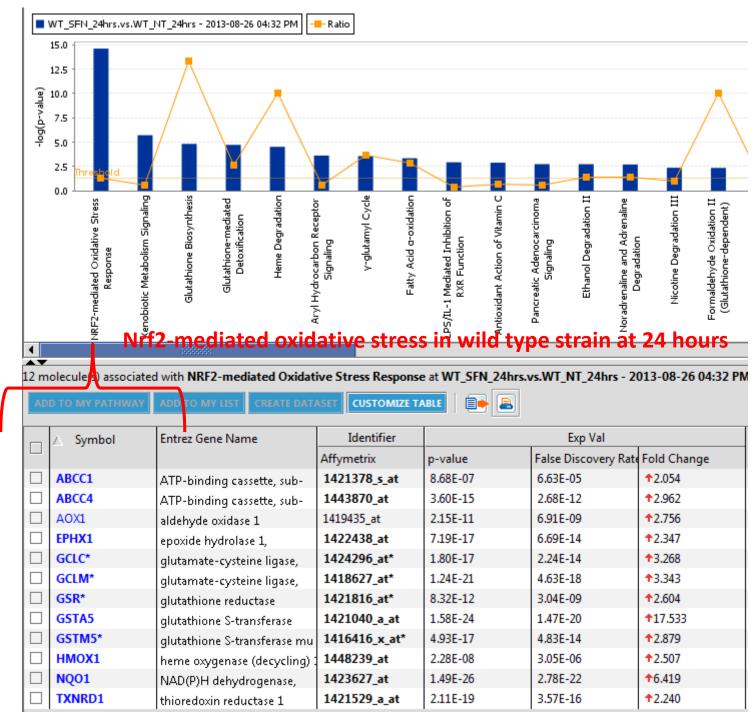
--Knowledgebase

- Desktop Java application utilizing a remote server for data, analysis and file management
- IPA Ontology: Curation of the scientific literature and content extraction of the IPA repository of molecular interactions, regulatory events, biological processes, gene-to-phenotype associations, and chemical knowledge

Ingenuity® Expert Findings	Experimentally demonstrated Findings that are manually curated for accuracy and contextual details from the full-text of articles in top journals.
Ingenuity® ExpertAssist Findings	Manually reviewed, automatically extracted Findings from the abstracts of a broad range of recently published journal articles.
Ingenuity® Expert Knowledge	Knowledge modeled by Ingenuity experts such as pathways, toxicity lists, and more.
Ingenuity® Supported Third Party Information	Manually reviewed content from selected sources and databases such as BIND, Argonaute 2, etc.

IPA Enrichment Analysis

- Uses the Fisher's exact test to determine the significance of a functional group or pathway
 - # molecules in a list that are associated with a function/pathway (k)
 - total # of molecules that are associated with a function/pathway (m)
 - # of molecules in all possible functions/pathways (N)
 - # of molecules in a list (n)



All the DEGs in the pathway are up-regulated

A non-parametric approach

- Compare a sample empirical distribution function to the reference distribution
- Or, compare two sample empirical distribution functions
- Required data:
 - Ranked list of genes sorted by differential expression (includes all genes)
 - A gene set
- If the genes in the gene set tend to fall near either end of the ranked list, the gene set is considered significantly enriched
- The test significance is obtained from empirical distribution
 - Permutation based
 - Bootstrapping
 - Etc.

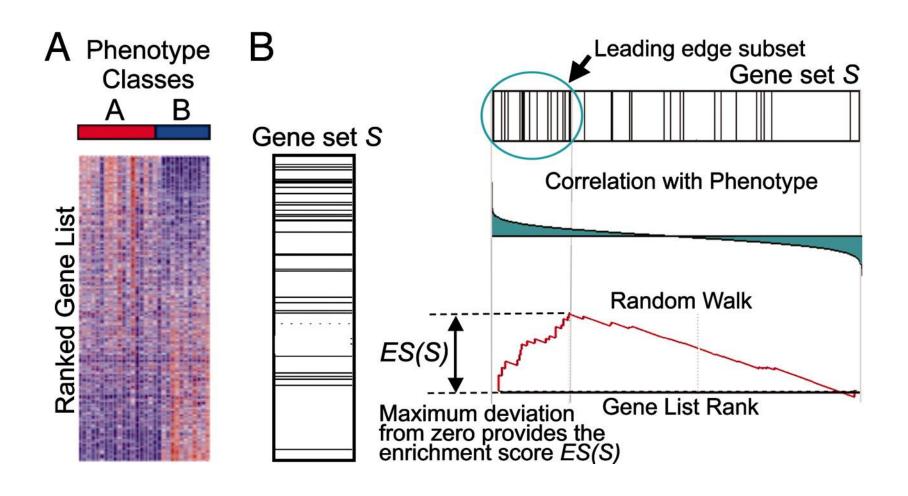
A non-parametric approach (GSEA)

- Mootha et al. [2003] suggest to use Kolmogorov-Smirnov (K-S) test
 - Sort all genes by LFC.
 - Go through the list, increasing a running sum for each gene in the gene set by (N-n), and decreasing it for each gene not in the gene set by n.
 - [N: number of genes, n: size of gene set]
 - The maximum value of the running sum is the enrichment score (ES).

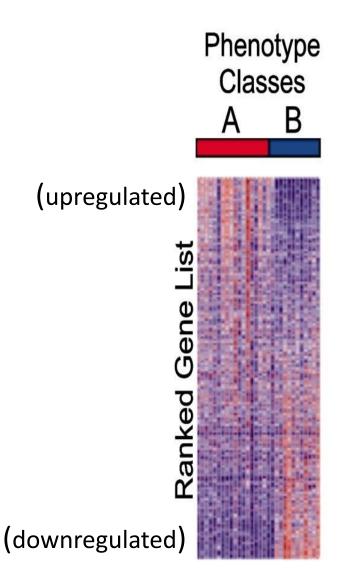
A non-parametric approach

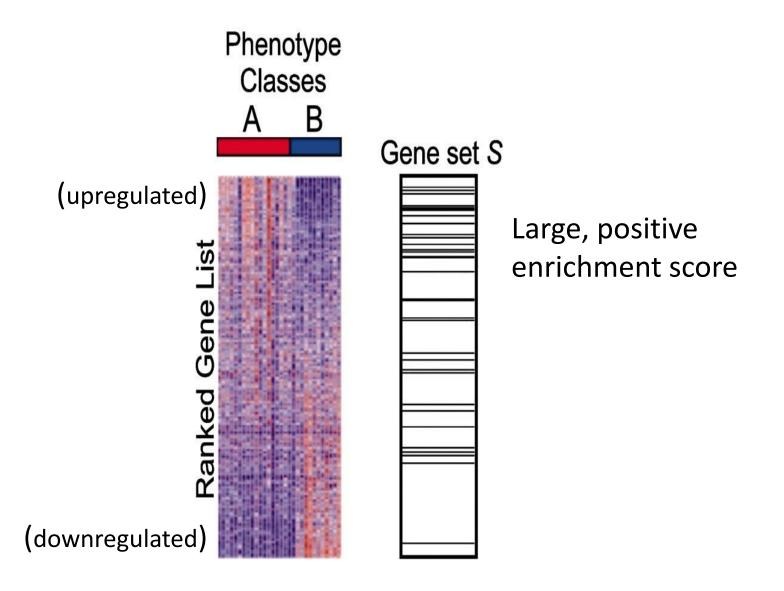
- Assessing significance
 - To get p values, we do not use the KS distribution but rather estimate the null by subject permutation
- Improved enrichment score
 - The KS statistic tests whether distributions are different, but this difference may not have a clear direction, making biological interpretation difficult
 - The updated GSEA algorithm [Subramanian et al., PNAS 102 (2005) 15545] weights the in-/decrements of the running sum by the LFC.

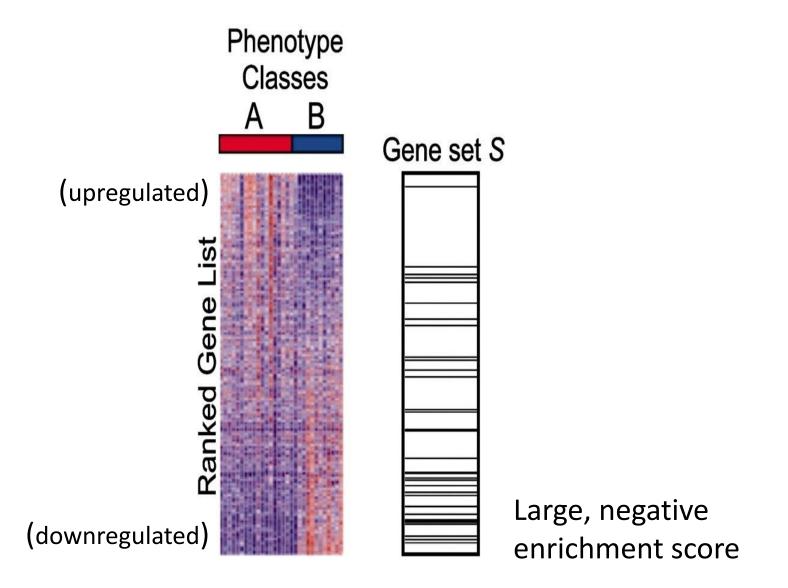
A GSEA overview illustrating the method.

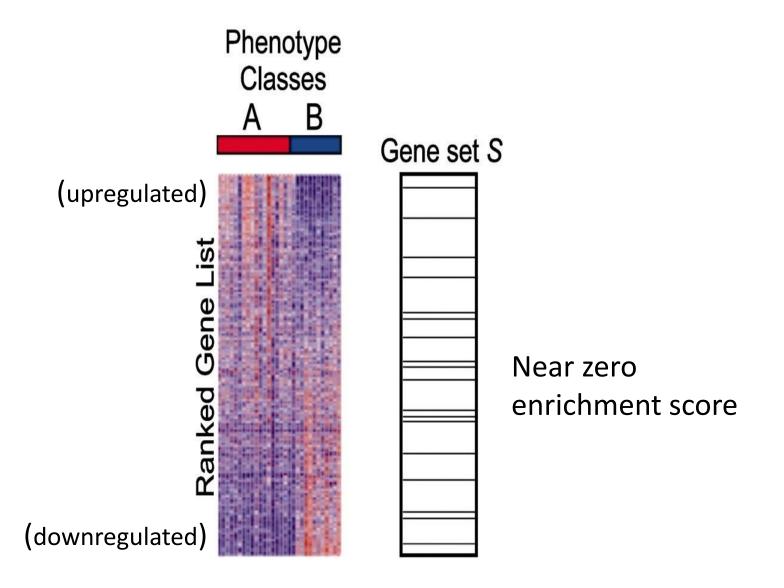


Subramanian A et al. PNAS 2005;102:15545-15550

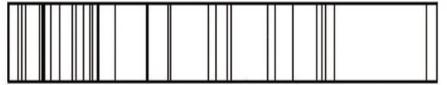




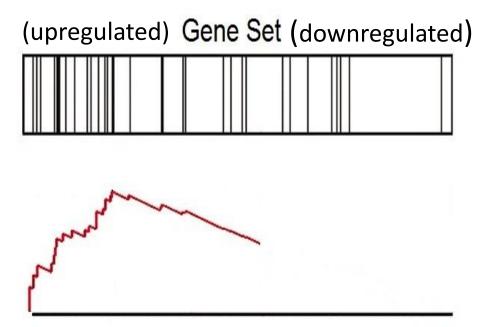


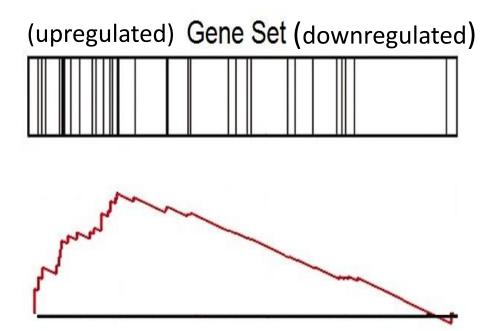


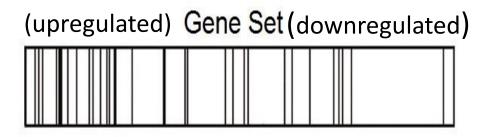
(upregulated) Gene Set (downregulated)

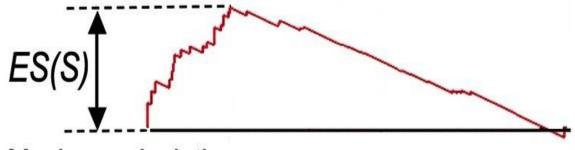


(upregulated) Gene Set (downregulated)



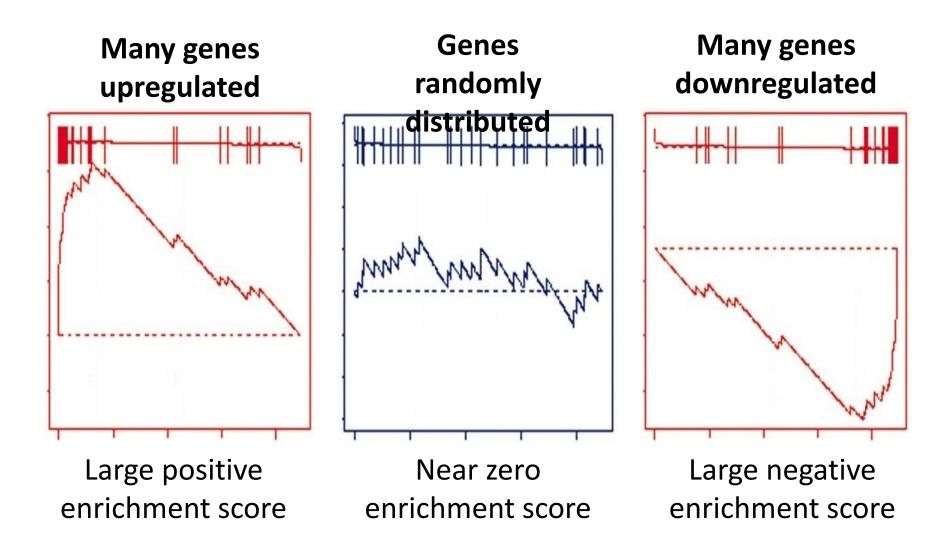


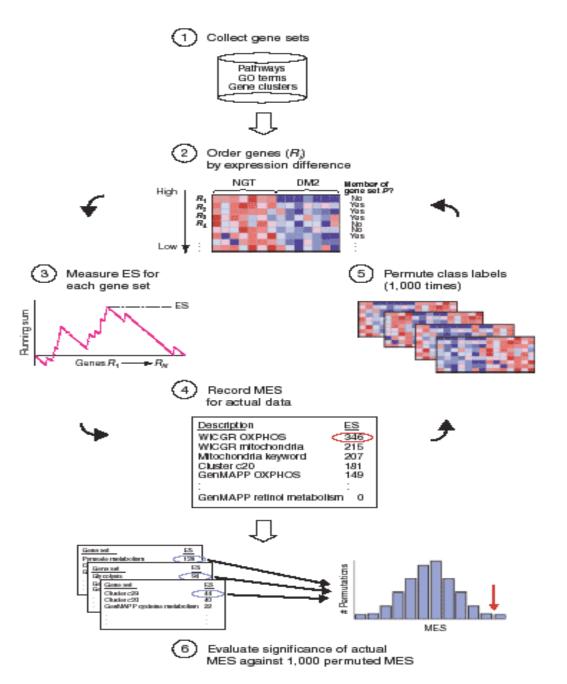




Maximum deviation from zero provides the enrichment score *ES(S)*

Kolmogorov–Smirnov (KS) Test





Mootha et al., Nature Genetics, 2003, 34(3):267-273

Kolmogorov–Smirnov (KS) Test

- Used in Gene Set Enrichment Analysis (GSEA)
 - Free software (http://www.broadinstitute.org/gsea)
 - Pros:
 - Large collection of gene sets
 - Uses more information than methods that only use DEG list
 - Enrichment plot improves interpretability
 - Cons:
 - Permutation-based p-values

Sampling over genes

- Hypergeometric testing for gene sets has been criticized on the ground of it sampling over genes (observation) instead of over microarrays (subjects)
- Hence, the meaning of the p values is quite unclear.
- Especially: Correlations between genes inflate the apparent sample size, causing potentially severe over-estimation of significance.
- Increasing the number of replicates influences significance only indirectly.

Sampling over subjects

- Instead of using the hypergeometric distribution to get a p value from out statistic, we should better use subject permutation:
 - Let L_0 be the list of differential expressed genes and $m=|L_0|$ its size.
 - For **N** permutations σ_i (i=1,...,N) of the subject labels, calculate the DE statistic and let Li be the list of the m top ranking genes.
 - Let k_i be the number of differentially expressed genes in the gene set, i.e. the size of the intersection $L_i \cap S$.
 - The p value for gene set S is now the fraction of permutation that had a larger gene set than the correct sample assignment, i.e.,

$$p = \frac{|\{i | k_i > k_0\}|}{N}$$

Challenge with sampling over subject

- Enough replicates are required to have something to permute.
- The calculation is time consuming.

 Hence, it may still make sense to use hypergeometric testing and live with the disagreement on whether it is statistically sound.

The universe matters

It is important to choose the universe correctly

Case 1: universe is all genes in the genome

	DEGs	Non-DEGs	Total
In GO	10	30	40
Not in GO	390	3570	3960
Total	400	3600	4000

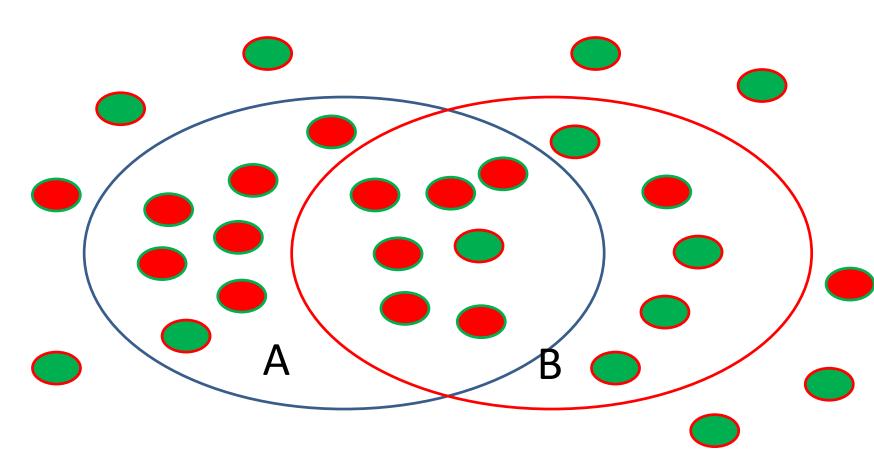
p = 0.049

Case 2: universe is only expressed genes

	DEGs	Non-DEGs	Total
In GO	10	30	40
Not in GO	390	570	960
Total	400	600	1000

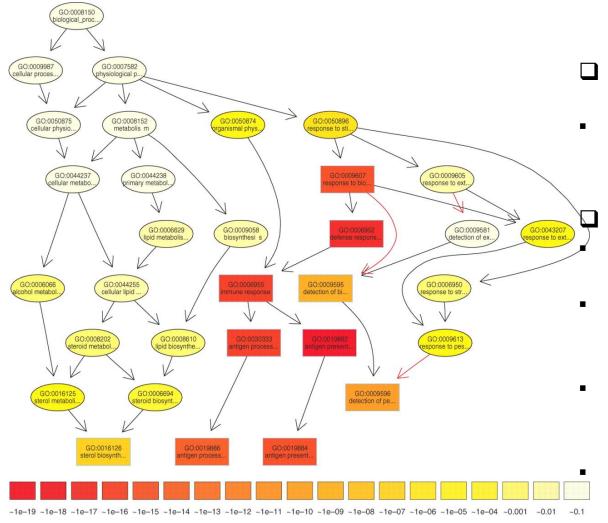
p=0.0048

Sets are overlapped



Set B is enriched only because of it overlap with set A

The subgraph induced by the 10 most significant GO terms identified by a current state-ofthe-art method for scoring GO terms for enrichment.



Alexa A et al. Bioinformatics 2006;22:1600-1607

☐ TopGO's elimination algorithm

Test the leaf sets first. If significant, remove its "genes" before testing its ancestor sets

TopGO's weight algorithm

The genes are weighted by their relevance in the significant nodes.

- The enrichment score of a parent (gene node u) is compared with the scores of its children.
 - Children with a better score than u represent the interesting genes better.

 Therefore, their significance is increased Children with a lower score than u have their significance reduced.



Hands on practice on both parametric and non-parametric

NOW, IT IS YOUR TURN

Click to download



GSEA Home

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Molecular Signatures Database

Documentation

Contact

Overview

Gene Set Enrichment Analysis (GSEA) is a computational method that determines whether an a priori defined set of genes shows statistically significant, concordant differences between two biological states (e.g. phenotypes).

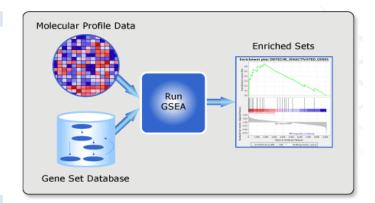
From this web site, you can:

- Download the GSEA software and additional resources to analyze, annotate and interpret enrichment results.
- Explore the Molecular Signatures Database (MSigDB), a collection of annotated gene sets for use with GSEA software.
- View documentation describing GSEA and MSigDB.

What's New

05-Jun-2013: Version 4.0 of the Molecular Signatures Database (MSigDB) is now available, which includes a new gene set collection (C7) of 1,910 immunologic signatures generated as part of the Human Immunology Project Consortium. We also released a newer version (2.0.13) of the GSEA desktop application. There were no changes to the GSEA algorithm.

29-May-2013: GSEA and MSigDB may experience intermittent connectivity issues on Monday, June 3rd between the hours of 6AM and 9AM (Eastern



Registration

Please register to download the GSEA software and view the MSigDB gene sets. After registering, you can log in at any time using your email address. Registration is free. Its only purpose is to help us track usage for reports to our funding agencies.

Contributors



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Login to GSEA/MSigDB

Login

Click here to register to view the MSigDB gene sets and/or download the GSEA software. This helps us track and better serve our user community.

If you have already registered for GSEA or MSigDB please enter your registration email address below.

Items marked with * are required.





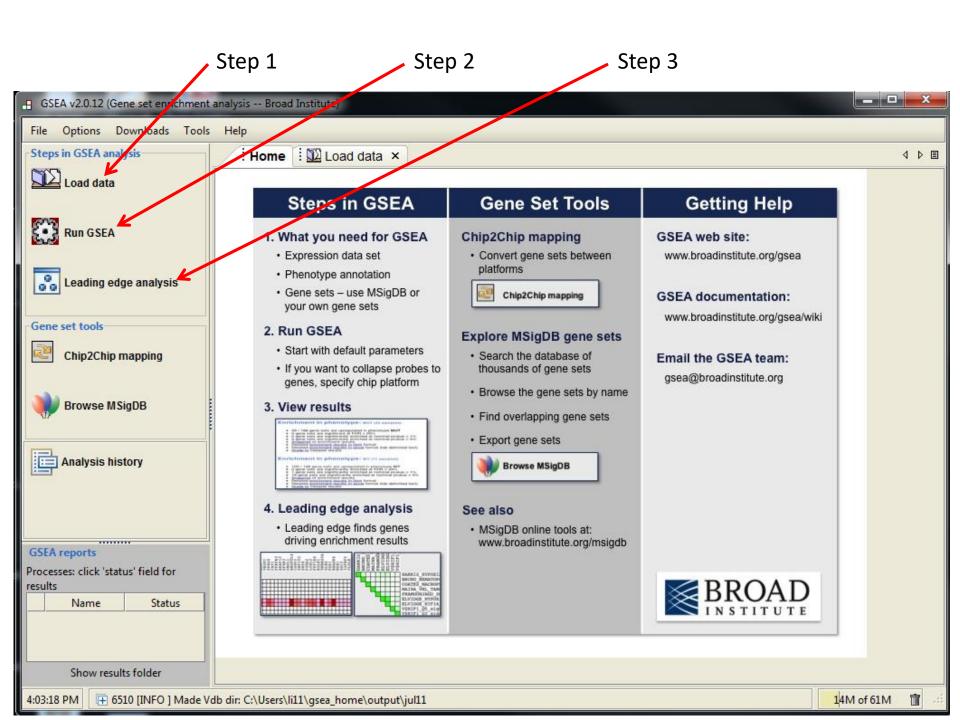
Downloads

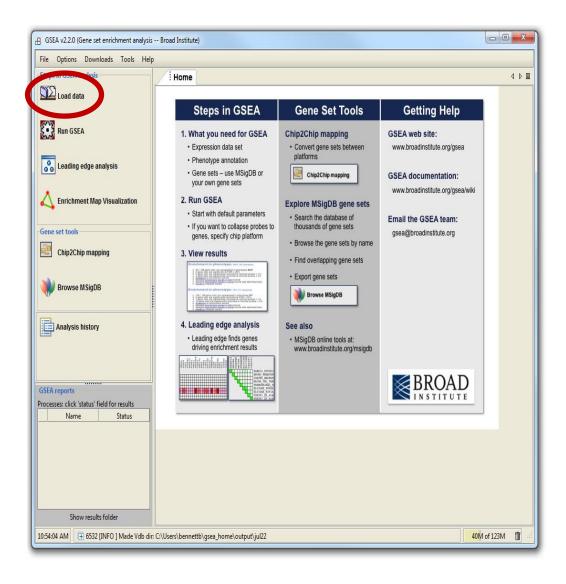
The GSEA software and source code and the Molecular Signatures Database (MSigDB) are freely available to individuals in both academia and industry for internal research purposes. Please see the GSEA/MSigDB license for more details.

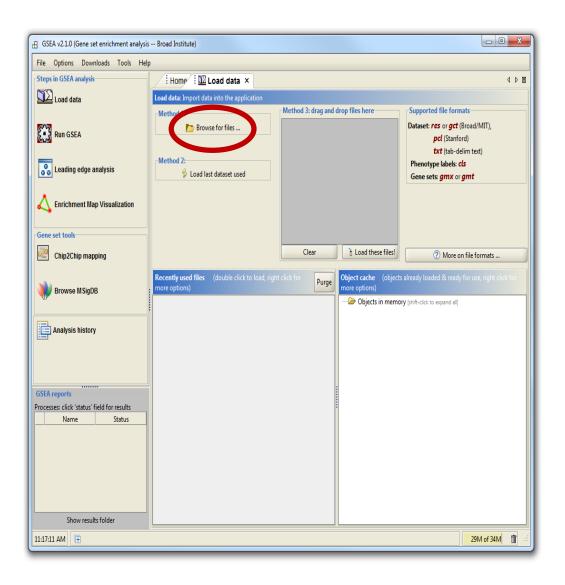
Software

There are several options for GSEA software. All options implement exactly the same algorithm. Usage recommendations and installation instructions are listed below. Current Java implementations of GSEA require Java 6 or 7.

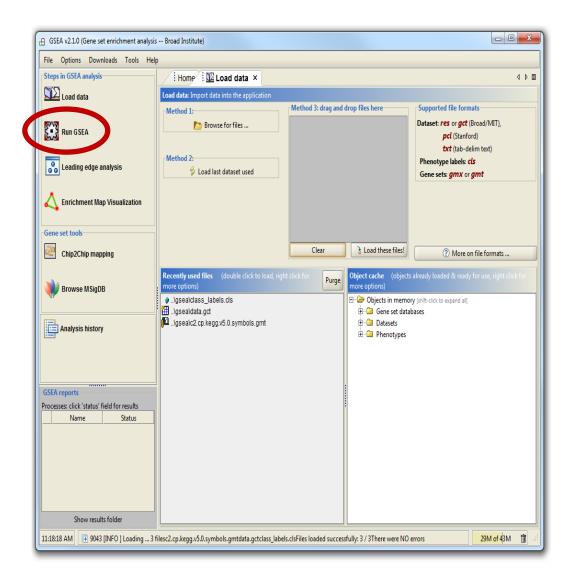
javaGSEA Desktop Application	 Easy-to-use graphical user interface Runs on any desktop computer (Windows, Mac OS X, Linux etc.) that supports Java 6 or 7 Produces richly annotated reports of enrichment results Integrated gene sets browser to view gene set annotations, search for gene sets and magene sets between platforms 	Launch with 1GB (for 32 or 64-bit Java) • memory: Launch
javaGSEA Java Jar file	 Command line usage Runs on any platform that supports Java 6 or 7 We recommend using the 'Launch' buttons above instead of this mode for most users 	download gsea2-2.2.0.jar
R-GSFA	► Usage from within the R programming environment	download

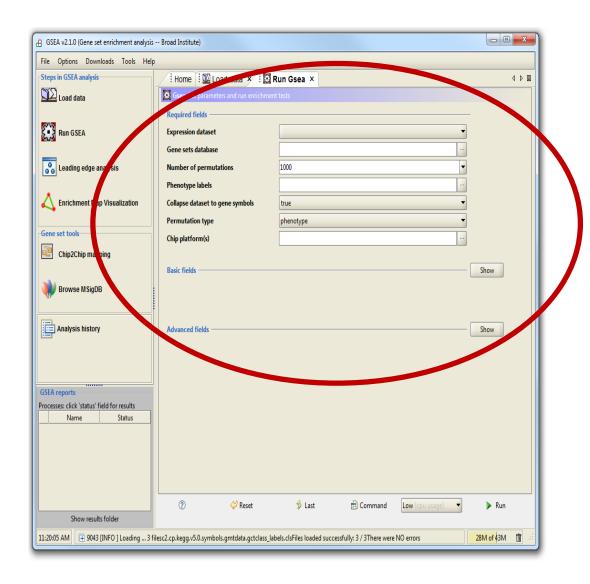


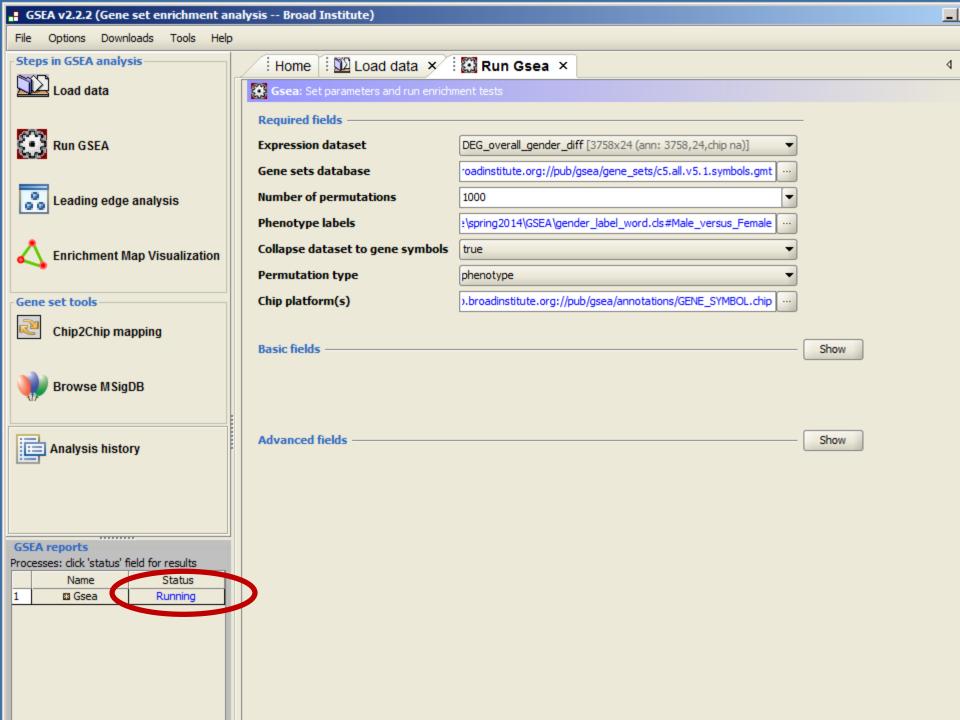


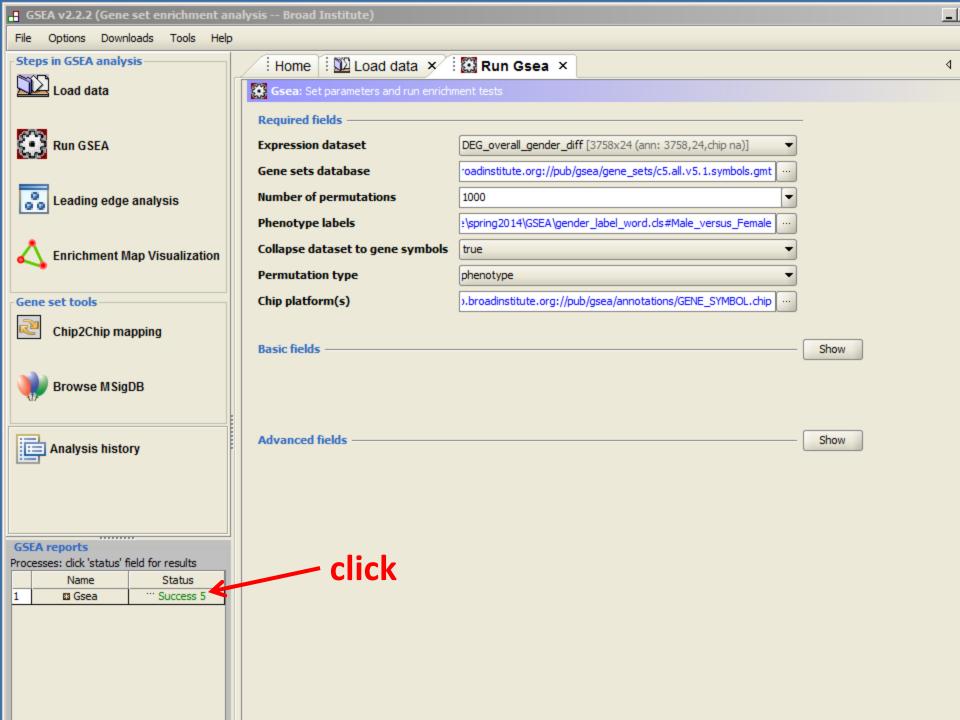


- Supported file types:
 - http://www.broadinstitute.org/cancer/software/gsea/wiki/index.php/
 Data formats
- Required:
 - Expression data file
 - Class label file
- Optional:
 - Gene set file









Enrichment in phenotype: Male (12 samples)

- · 31 / 378 gene sets are upregulated in phenotype Male
- 0 gene sets are significant at FDR < 25%
- 0 gene sets are significantly enriched at nominal pvalue < 1%
- 1 gene sets are significantly enriched at nominal pvalue < 5%
 Snapshot of enrichment results
- Detailed enrichment results in html format
- Detailed enrichment results in excel format (tab delimited text)
- Guide to interpret results

Enrichment in phenotype: Female (12 samples)

- · 347 / 378 gene sets are upregulated in phenotype Female
- 4 gene sets are significantly enriched at FDR < 25%
- 4 gene sets are significantly enriched at nominal pvalue < 1%
- 5 gene sets are significantly enriched at nominal pvalue < 5%
- Snapshot of enrichment results
 Detailed enrichment results in html format
- Detailed enrichment results in excel format (tab delimited text)
- Detailed enrichment results in excel format (tab delimited text)
 Guide to interpret results

Dataset details

- · The dataset has 3750 native features
- After collapsing features into gene symbols, there are: 2736 genes

Gene set details

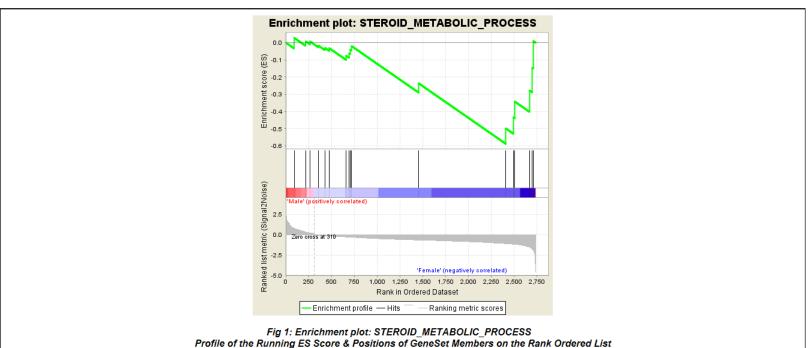
- Gene set size filters (min=15, max=500) resulted in filtering out 1076 / 1454 gene sets
- The remaining 378 gene sets were used in the analysis
- List of gene sets used and their sizes (restricted to features in the specified dataset)

Gene markers for the Male versus Female comparison

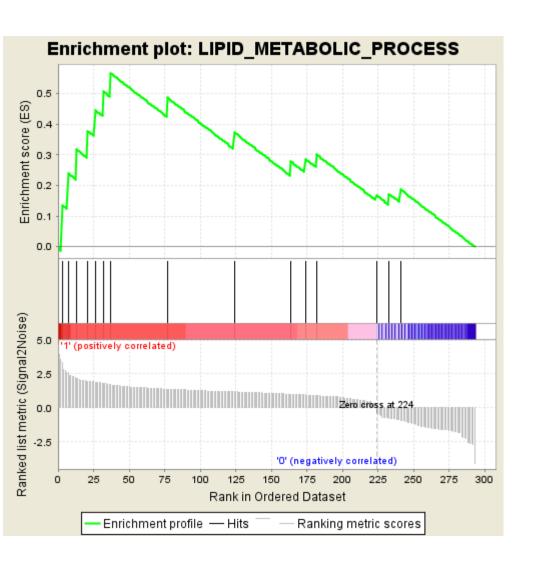
- · The dataset has 2736 features (genes)
- # of markers for phenotype Male: 310 (11.3%) with correlation area 10.8%
- # of markers for phenotype Female: 2426 (88.7%) with correlation area 89.2%
- . Detailed rank ordered gene list for all features in the dataset
- Heat map and gene list correlation profile for all features in the dataset
- <u>Buttefly plot</u> of significant genes

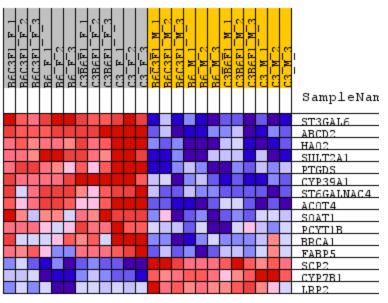
	GS follow link to MSigDB	GS DETAILS	SIZE	ES	NES	NOM p-val	FDR q-val	FWER p-val	RANK AT MAX	LEADING EDGE
1	STEROID_METABOLIC_PROCESS	Details	1	-0.59	-1.86	0.000	0.247	0.093	326	tags=35%, list=12%, signal=40%
2	MONOCARBOXYLIC_ACID_METABOLIC_PROCESS	Details	27	-0.47	-1.84	0.004	0.146	0.107	644	tags=37%, list=24%, signal=48%
3	CELLULAR_LIPID_METABOLIC_PROCESS	Details	64	-0.45	-1.81	0.000	0.136	0.138	575	tags=31%, list=21%, signal=39%
4	FATTY_ACID_METABOLIC_PROCESS	Details	19	-0.59	-1.76	0.008	0.184	0.217	644	tags=47%, list=24%, signal=62%
5	LIPID_METABOLIC_PROCESS	Details	78	-0.39	-1.65	0.014	0.410	0.415	675	tags=29%, list=25%, signal=38%
6	CARBOXYLIC_ACID_METABOLIC_PROCESS	Details	51	-0.32	-1.45	0.090	1.000	0.696	696	tags=24%, list=25%, signal=31%
7	ORGANIC_ACID_METABOLIC_PROCESS	Details	51	-0.32	-1.45	0.090	1.000	0.696	696	tags=24%, list=25%, signal=31%
8	LIPID_BIOSYNTHETIC_PROCESS	Details	22	-0.46	-1.40	0.150	1.000	0.747	575	tags=36%, list=21%, signal=46%
9	GOLGI_APPARATUS	Details	30	-0.43	-1.39	0.076	1.000	0.753	379	tags=37%, list=14%, signal=42%
10	GTPASE_ACTIVITY	Details	15	-0.50	-1.38	0.092	1.000	0.761	195	tags=33%, list=7%, signal=36%
11	CELL_MIGRATION	Details	22	-0.48	-1.35	0.121	1.000	0.781	969	tags=64%, list=35%, signal=98%
12	OXIDOREDUCTASE_ACTIVITY	Details	66	-0.27	-1.34	0.119	1.000	0.783	284	tags=12%, list=10%, signal=13%
13	TRANSMEMBRANE_RECEPTOR_PROTEIN_KINASE_ACTIVITY	Details	15	-0.53	-1.34	0.105	1.000	0.794	795	tags=67%, list=29%, signal=93%

Table: GSEA Results Summary	
Dataset	DEG_overall_gender_diff_overall_gender_diff_collapsed_to_symbols.gender_label_word.cls #Male_versus_Female.gender_label_word.cls #Male_versus_Female_repos
Phenotype	gender_label_word.cls#Male_versus_Female_repos
Upregulated in class	Female
GeneSet	STEROID_METABOLIC_PROCESS
Enrichment Score (ES)	-0.5875557
Normalized Enrichment Score (NES)	-1.8563647
Nominal p-value	0.0
FDR q-value	0.24662763
FWER p-Value	0.093



Lipid metabolism enriched -- GSEA





- http://www-stat.stanford.edu/~tibs/GSA/
- http://www.netsci.org/Resources/Software/Bioinform/pathwayan alysis.html
- http://www.broadinstitute.org/gsea/index.jsp
- http://david.abcc.ncifcrf.gov/
- http://www.biocarta.com/
- http://web.expasy.org/pathways/
- http://www.genmapp.org/
- http://www.genome.jp/kegg/
- http://www.ingenuity.com/
- http://www.genego.com/metacore.php
- http://www.geneontology.org/
- http://omicslab.genetics.ac.cn/GOEAST/tutorial.php
- http://expressome.kobic.re.kr/GAzer/document.jsp
- <u>http://www.biobase-international.com/products</u>
- http://jaspar.genereg.net/