Heterogeneous Agent Trade

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What am I doing?

To trade economists, household heterogeneity is interesting because of the notion that some benefit from trade and others don't.

One mechanism behind this notion is heterogeneity in elasticities.

 Auer, Burstein, Lein, and Vogel (2022) is a nice example. In the context of the 2015 Swiss appreciation, they find that poor households are more price elastic.

This paper:

- A model of household heterogeneity in price elasticities at the micro level and they arise because
 of a market failure, i.e., the lack of insurance against life's circumstances.
- And I use it as a laboratory to think about aggregate trade, the gains from trade and how they are
 distributed, and the normative implications, e.g., what should the pattern of trade look like.

How I do it...

Two ingredients:

- Trade as in Armington, but households have random utility over varieties McFadden (1974)
- Standard incomplete markets model with households facing incomplete insurance against idiosyncratic productivity and taste shocks — Bewley (1979)

Qualitatively I characterize:

- How price elasticities vary at the micro-level and when micro-heterogeneity shapes aggregates.
- The welfare gains from trade at the micro and macro level.
- The efficient allocation and, thus, how market incompleteness shapes these outcomes.

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Quantitatively:

- I work at a scale typically reserved for static frameworks—I calibrate a 19 country model (the Eaton and Kortum (2002) data set) to match trade flow data using "gravity as a guide."
- Illustrate some workings of the model through gains from trade type calculations.
- Compare trade in the efficient allocation vs. the decentralized allocation.

Model: Production and Trade

M countries. Each country produces a nationally differentiated product as in Armington.

In country *i*, competitive firms' produce variety *i* with:

$$Q_i = A_i N_i$$

where A_i is TFP; N_i are efficiency units of labor supplied by households.

Cross-country trade faces obstacles:

• iceberg trade costs $d_{ii} > 1$ for one unit from supplier j to go to buyer i.

This structure leads to the following prices that households face

$$p_{ij}=\frac{d_{ij}w_j}{A_j}.$$

Continuum of households $k \in [0, L_i]$ in each country i. Household preferences:

$$\mathrm{E}\sum_{t=0}^{\infty}\beta^{t}\ \tilde{u}_{ijt}^{k},$$

where conditional direct utility for good j is

$$\tilde{u}_{ijt}^k = u(c_{ijt}^k) + \epsilon_{jt}^k, \quad j = 1, \dots, M.$$

Assumptions:

- discrete-continuous choice...so first chose one variety, then continuous choice over quantity.
- ϵ_{it}^k s are iid across hh and time; distributed Type 1 Extreme Value with dispersion parameter σ_{ϵ} .
- For now, u is well behaved.

Multiple sectors? We do this with an "infinite shopping aisle" in Mongey and Waugh (2022).

Model: Households II

Household k's efficiency units z_t evolve according to a Markov Chain. They face the wage per efficiency unit w_{it} .

Households borrow or accumulate a non-state contingent asset, a, with gross return R_i . Household's face the debt limit

$$a_{t+1} \geq -\phi_i$$
.

Conditional on a variety choice, a household's budget constraint is

$$p_{ij}c_{ijt}+a_{t+1}\leq R_ia_t+w_{it}z_t.$$

What Households Do I

Focus on a stationary setting. A hh's state are its asset holdings a and shock z.

1. Condition on variety choice their problem is:

$$v_i(a, z, j) = \max_{a', c_{ij}} \left\{ u(c_{ij}) + \epsilon_j + \beta \mathbb{E}[v_i(a', z')] \right\},$$

subject to
$$p_{ij}c_{ij} + a' \leq R_i a + w_i z$$
 and $a' \geq -\phi_i$.

2. The ex-post value function of a household in country i is

$$v_i(a,z) = \max_j \{ v_i(a,z,j) \}.$$

Two equations characterizing the commodity choice, consumption / savings...

1. The choice probability is:

$$\pi_{ij}(a,z) = \exp\left(\frac{v_i(a,z,j)}{\sigma_\epsilon}\right) / \Phi_i(a,z),$$

where
$$\Phi_i(a,z) := \sum_{j'} \exp\left(\frac{v_i(a,z,j')}{\sigma_\epsilon}\right)$$
.

2. Away from the constraint, consumption and asset choices must respect this Euler Equation:

$$\frac{u'(c_i(a,z,j))}{p_{ij}} = \beta R_i E_{z'} \left[\sum_{j'} \pi_{ij'}(a',z') \frac{u'(c_i(a',z',j'))}{p_{ij'}} \right].$$

Aggregates arise from explicit aggregation of hh-level actions. Two examples:

1. Aggregate, bilateral imports and exports are

$$M_{ij} = L_i \int_z \int_a p_{ij} c_i(a,z,j) \pi_{ij}(a,z) \lambda_i(a,z), \qquad X_{ji} = L_j \int_z \int_a p_{ji} c_j(a,z,i) \pi_{ji}(a,z) \lambda_j(a,z),$$

where λ_i is the *endogenous* distribution of hhs across states. Here trade flows take on a mixed-logit form similar to Berry, Levinsohn, and Pakes (1995), but everything is tied down in equilibrium.

2. The national income accounting identity (GDP = C + I + G + X - M) \dots

$$p_i Y_i = \underbrace{L_i \sum_j \int_z \int_a p_{ij} c_i(a, z, j) \pi_{ij}(a, z) \lambda_i(a, z)}_{\widetilde{P_i C_i}} + \underbrace{\left[\sum_{j \neq i} X_{ji} - \sum_{j \neq i} M_{ij} \right]}_{-R_i A_i + A_i'}.$$

Equilibrium

The Decentralized Stationary Equilibrium. A Decentralized Stationary Equilibrium are asset policy functions and commodity choice probabilities $\{g_i(a,z,j),\pi_{ij}(a,z)\}_{ij}$, probability distributions $\{\lambda_i(a,z)\}_i$ and positive real numbers $\{w_i,p_{ij},R_i\}_{ij}$ such that

- i Prices (w_i, p_{ij}) satisfy the firms problem;
- ii The policy functions and choice probabilities solve the household's optimization problem;
- iv The probability distribution $\lambda_i(a, z)$ induced by the policy functions, choice probabilities, and primitives satisfies the law of motion and is stationary;
- v Goods market clears:

$$p_i Y_i - \sum_j^M X_{ji} = 0, \quad \forall i$$

v Bond market clears with either

$$\mathrm{A_i'} = 0, \;\; \forall i \;\; \text{in the case of finacial autarky, or}$$

$$\sum_i \mathrm{A}_i' = 0,$$
 in the case of finacial globalization and $R_i = R \ orall i$

Proposition #1: The HA Trade Elasticity. The trade elasticity between country i and country j is:

$$heta_{ij} = 1 + \int_{a} \int_{z} \left\{ heta_{ij}(a,z)' + heta_{ij}(a,z)^{E}
ight\} \omega_{ij}(a,z) - \left\{ heta_{ii}^{j}(a,z)' + heta_{ii}^{j}(a,z)^{E}
ight\} \omega_{ii}(a,z),$$

which is the difference between ij and ii expenditure-weighted micro-level elasticities. The micro-level elasticities for households with states a, z are an intensive and extensive elasticity

$$\theta_{ij}(a,z)^I = \frac{\partial c_i(a,z,j)/c_i(a,z,j)}{\partial d_{ij}/d_{ij}}, \qquad \theta_{ij}(a,z)^E = \frac{\partial \pi_{ij}(a,z)/\pi_{ij}(a,z)}{\partial d_{ij}/d_{ij}},$$

and $\omega_{ij}(a,z)$ are the expenditure weights.

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$$\theta_{ij}(\mathbf{a},\mathbf{z})^{\prime} = \frac{\partial c_i(\mathbf{a},\mathbf{z},j)/c_i(\mathbf{a},\mathbf{z},j)}{\partial d_{ij}/d_{ij}}, \qquad \theta_{ij}(\mathbf{a},\mathbf{z})^E = \frac{\partial \pi_{ij}(\mathbf{a},\mathbf{z})/\pi_{ij}(\mathbf{a},\mathbf{z})}{\partial d_{ij}/d_{ij}},$$

and $\omega_{ij}(a,z)$ are the expenditure weights.

$$\theta_{ij}(\mathbf{a},\mathbf{z})^I = \left[-\frac{\partial g_i(\mathbf{a},\mathbf{z},j)/p_{ij}c_i(\mathbf{a},\mathbf{z},j)}{\partial p_{ij}/p_{ij}} - 1 \right] \frac{\partial p_{ij}/p_{ij}}{\partial d_{ij}/d_{ij}}.$$

The idea: a Δ in trade costs relaxes the budget constraint and then the division of new resources between assets and expenditure determines the intensive margin.

In absolute value, this is larger for the poor, smaller for the rich.

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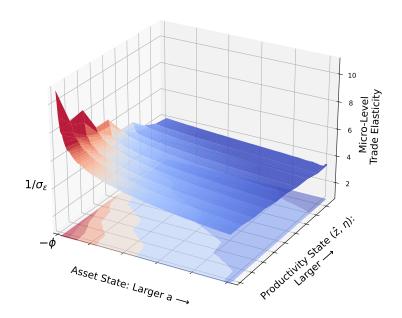
and $\omega_{ij}(a,z)$ are the expenditure weights.

$$\theta_{ij}(a,z)^{E} = -\frac{\partial \Phi_{i}(a,z)/\Phi_{i}(a,z)}{\partial d_{ij}/d_{ij}} + \frac{1}{\sigma_{\epsilon}} \frac{\partial v_{i}(a,z,j)}{\partial d_{ij}/d_{ij}}.$$

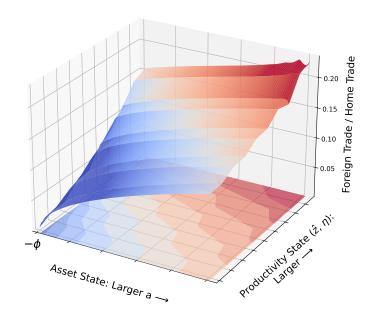
The interesting bit is $\frac{\partial v_i(a,z,j)}{\partial d_{ij}/d_{ij}}$...

In the paper, I show that if Arrow-Pratt measure of relative risk aversion > 1 than hh's with (i) high u'(c) and (ii) high MPCs are more price elastic. So poor hh's are the most price sensitive.

Trade Elasticities by HH-Level State



Trade Shares: $M_i(a, z, j)/M_i(a, z, i)$, by HH-Level State



$$\frac{\mathrm{d} W_i}{\mathrm{d} d_{ij}/d_{ij}} \approx \int_z \int_a \bigg\{ \underbrace{\frac{\mathrm{d} v_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to hh}} + \underbrace{v_i(a,z) \frac{\mathrm{d} \lambda_i(a,z)/\lambda_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to reallocation}} \bigg\} L_i \lambda_i(a,z),$$

where v_i is value function before realization of taste shocks; \approx is about abstracting from transition.

Household-level gains are

$$\frac{\mathrm{d}v_i(a,z)}{\mathrm{d}d_{ij}/d_{ij}} \approx \sigma_\epsilon \frac{\mathrm{d}\Phi_i(a,z)/\Phi_i(a,z)}{\mathrm{d}d_{ij}/d_{ij}}$$

Like standard trade models! It's all about how this price-index-like thing changes.

$$\frac{\mathrm{d} W_i}{\mathrm{d} d_{ij}/d_{ij}} \approx \int_z \int_a \bigg\{ \underbrace{\frac{\mathrm{d} v_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to hh}} + \underbrace{v_i(a,z) \frac{\mathrm{d} \lambda_i(a,z)/\lambda_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to reallocation}} \bigg\} L_i \lambda_i(a,z),$$

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Household-level gains are

$$\frac{\mathrm{d}v_i(a,z)}{\mathrm{d}d_{ij}/d_{ij}} \approx \sum_j \pi_{ij}(a,z) \frac{\mathrm{d}v_i(a,z,j)}{\mathrm{d}d_{ij}/d_{ij}}$$

The change in the $\Phi_i(a, z)$ thing (previous slide if you fell asleep) is share-weighted average of choice-specific value functions.

Next step...one algebra trick.

$$\frac{\mathrm{d} W_i}{\mathrm{d} d_{ij}/d_{ij}} \approx \int_z \int_a \bigg\{ \underbrace{\frac{\mathrm{d} v_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to hh}} + \underbrace{v_i(a,z) \frac{\mathrm{d} \lambda_i(a,z)/\lambda_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to reallocation}} \bigg\} L_i \lambda_i(a,z),$$

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Household-level gains are

$$\frac{\mathrm{d}v_i(a,z)}{\mathrm{d}d_{ij}/d_{ij}} \approx \underbrace{\sum_j \pi_{ij}(a,z) \left\{ \frac{\mathrm{d}v_i(a,z,j)}{\mathrm{d}d_{ij}/d_{ij}} - \frac{\mathrm{d}v_i(a,z,i)}{\mathrm{d}d_{ij}/d_{ij}} \right\}}_{\text{how relative valuations change}} + \frac{\mathrm{d}v_i(a,z,i)}{\mathrm{d}d_{ij}/d_{ij}}$$

$$\frac{\mathrm{d}W_i}{\mathrm{d}d_{ij}/d_{ij}} \approx \int_z \int_a \bigg\{ \underbrace{\frac{\mathrm{d}v_i(a,z)}{\mathrm{d}d_{ij}/d_{ij}}}_{\text{gains to hh}} + \underbrace{v_i(a,z) \frac{\mathrm{d}\lambda_i(a,z)/\lambda_i(a,z)}{\mathrm{d}d_{ij}/d_{ij}}}_{\text{gains to reallocation}} \bigg\} L_i \lambda_i(a,z),$$

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Now recursively iterate forward in time given how v_{ii} connects with v_i next period.

$$\frac{\mathrm{d} W_i}{\mathrm{d} d_{ij}/d_{ij}} \approx \int_z \int_a \bigg\{ \underbrace{\frac{\mathrm{d} v_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to hh}} + \underbrace{v_i(a,z) \frac{\mathrm{d} \lambda_i(a,z)/\lambda_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}}}_{\text{gains to reallocation}} \bigg\} L_i \lambda_i(a,z),$$

where v_i is value function before realization of taste shocks; \approx is about abstracting from transition.

Household-level gains are

$$\frac{\mathrm{d}v_i(a,z)}{\mathrm{d}d_{ij}/d_{ij}} \approx \mathbb{E}_z \sum_{t=0}^{\infty} \beta^t \bigg\{ -\sigma_\epsilon \frac{\mathrm{d}\pi_{ii}(a_t,z_t)/\pi_{ii}(a_t,z_t)}{\mathrm{d}d_{ij}/d_{ij}} + u'(c_i(a_t,z_t,i)) \bigg[a_t \frac{\mathrm{d}R_i/p_{ii}}{\mathrm{d}d_{ij}/d_{ij}} \bigg] \bigg\}.$$

HH-level gains pick up two effects:

- A state contingent, ACR-like term summarizing how relative valuations across choices change.
- How hh's real wealth (+ or -) change through GE effects on prices all evaluated at the hh's
 marginal utility of home consumption.

Proposition #3: Separation of Trade and Micro-Heterogeneity. When preferences are logarithmic over the physical commodity, choice probabilities are independent of household heterogeneity

$$\pi_{ij}(a,z) = \exp\left(\frac{-\log p_{ij}}{\sigma_{\epsilon}}\right) / \sum_{j'} \exp\left(\frac{-\log p_{ij'}}{\sigma_{\epsilon}}\right) \propto M_{ij},$$

and the trade elasticity is

$$heta = -rac{1}{\sigma_\epsilon}.$$

And hh-level gains from trade

$$\frac{\mathrm{d}v_{i}(a,z)}{\mathrm{d}d_{ij}/d_{ij}} \approx \underbrace{-\frac{1}{\theta(1-\beta)} \times \frac{\mathrm{d}\pi_{ii}/\pi_{ii}}{\mathrm{d}d_{ij}/d_{ij}}}_{\mathsf{ACR}} + \underbrace{\mathbb{E}_{z} \sum_{t=0}^{\infty} \beta^{t} \left[u'(c_{i}(a_{t},z_{t},i)) \ a_{t} \ \frac{\mathrm{d}R_{i}/p_{ii}}{\mathrm{d}d_{ij}/d_{ij}} \right]}_{\mathsf{exposure to finacial market}}$$

This mimics the results of Anderson, De Palma, and Thisse (1987). This was not obvious to me given the environment ...risk, market incompleteness, borrowing constraints, etc.

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$$\frac{\mathrm{d} v_i(a,z)}{\mathrm{d} d_{ij}/d_{ij}} \approx \underbrace{-\frac{1}{\theta(1-\beta)} \times \frac{\mathrm{d} \pi_{ii}/\pi_{ii}}{\mathrm{d} d_{ij}/d_{ij}}}_{\mathsf{ACR}} + \underbrace{\mathbb{E}_z \sum_{t=0}^{\infty} \beta^t \bigg[u'(c_i(a_t,z_t,i)) \ a_t \ \frac{\mathrm{d} R_i/p_{ii}}{\mathrm{d} d_{ij}/d_{ij}} \bigg]}_{\mathsf{exposure to finacial market}}.$$

And we are back to Arkolakis et al. (2012) + what's going on with the financial market.

Proposition #4: The Centralized (Efficient) Allocation. The allocation satisfying the Centralized Planning Problem (with a utilitarian SWF and country-specific Pareto weights ψ_i) is:

1. An allocation of consumption satisfying:

$$\psi_i u'(c_i(z,j,t)) = \chi_j(t) d_{ij}$$

where $\chi_j(t)$ is the multiplier on j resource constraint for variety j,

2. And variety choice probabilities:

$$\pi_{ij}(t) = \exp\left(\frac{u(c_i(j,t)) - u'(c_i(j,t))c_i(j,t)}{\sigma_{\epsilon}}\right) \bigg/ \sum_{j'} \exp\left(\frac{u(c_i(j',t)) - u'(c_i(j',t))c_i(j',t)}{\sigma_{\epsilon}}\right).$$

- 1. is a Backus and Smith (1993)-like condition.
- 2. is new trade should reflect the net social benefit of buying that commodity.

Proposition #5: Trade Elasticities and Welfare Gains in the Efficient Allocation The trade elasticity between i, j in the efficient allocation is:

$$heta_{ij} = -rac{1}{\sigma_{\epsilon}}igg[u'(c_{ij})c_{ij}igg].$$

And the welfare gains from a reduction in trade costs between i, j are

$$\frac{\mathrm{d}W}{\mathrm{d}d_{ij}/d_{ij}} = \frac{\partial W}{\partial d_{ij}/d_{ij}} = \frac{\psi_i}{1-\beta} \times u'(c_{ij})c_{ij}\pi_{ij}L_i,$$

which is the discounted, weighted, direct effect from relaxing the resource constraint.

Two comments:

- Mimics the results of Atkeson and Burstein (2010) but with household (not firm) heterogeneity.
- With log preferences the direct effect is equivalent to Arkolakis et al. (2012).

Quantitative Analysis

This is what I'll do today...

- 1. Calibrate my model using my "gravity as a guide" approach on the 19 country data set of Eaton and Kortum (2002).
- **2.** Some gains from trade type calculations.
- 3. Trade in the efficient allocation vs. the decentralized allocation.

Household Parameters

Parameters common across countries:

- CRRA for u with relative risk aversion $\gamma = 1.5$.
- Earnings process is a mixture of a persistent and transitory component and calibrated as in Krueger, Mitman, and Perri (2016).
- Discount factor β jiggled to target a world interest rate of 1.5% in financial globalization case.

Parameters scaled across countries to deliver balanced-growth-like properties.

- Set $\sigma_{\epsilon,i} = \sigma_{\epsilon} \times A_i^{1-\gamma}$ and $\sigma_{\epsilon} = 0.25$. In a log model corresponds with a trade elasticity of 4.
- Set the borrowing constraint so $\phi_i = \phi \times A_i$ where $\phi = 0.50$. Interpretation: the constraint = 50 % of average, autarky labor income.

County Specific Parameters — Using Gravity as a Guide

The problem: no closed form map from trade flows to parameters as in standard trade models. But I want the model to replicate the geographic pattern of activity seen in the data.

• Step 0. Impose a trade cost function to reduce the parameter space

$$\log d_{ij} = d_k + b + l + e_h + m_i$$

Step 1. Run this gravity regression on the data

$$og\left(\frac{M_{ij}}{M_{ii}}\right) = Im_i + Ex_j + d_k + b + l + e_h + \delta_{ij}$$

- Step 2. Guess TFP terms and coefficients on the trade cost function, compute an equilibrium, run the same regression from above on model generated data.
- Step 3. Evaluate difference between model and data and update parameters until convergence.

County Specific Parameters — Using Gravity as a Guide

The solution: use the gravity regression "as a guide" where I estimate parameters of the model so that the regression coefficients run on my model's data match that seen in the data.

• Step 0. Impose a trade cost function to reduce the parameter space

$$\log d_{ij} = d_k + b + l + e_h + m_i.$$

Step 1. Run this gravity regression on the data

$$\log\left(\frac{M_{ij}}{M_{ii}}\right) = Im_i + Ex_j + d_k + b + I + e_h + \delta_{ij}.$$

- Step 2. Guess TFP terms and coefficients on the trade cost function, compute an equilibrium, run the same regression from above on model generated data.
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Bilateral Trade: Model vs. Data

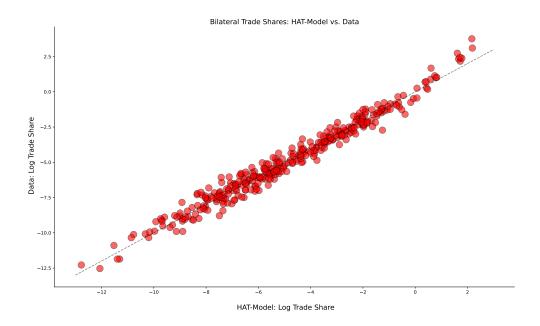


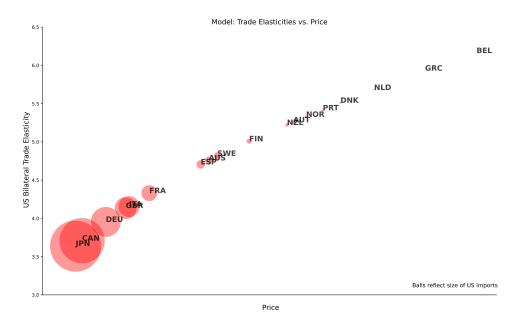
Table 1: Estimation Results

Barrier	Moment	HAT-Model	
		Model Fit	Parameter
[0, 375)	-3.10	-3.10	2.35
[375, 750)	-3.67	-3.67	2.81
[750, 1500)	-4.03	-4.03	3.09
[1500, 3000)	-4.22	-4.22	3.23
[3000, 6000)	-6.06	-6.06	4.88
[6000, maximum]	-6.56	-6.56	5.69
Shared border	0.30	0.30	0.91
Language	0.51	0.51	0.87
EFTA	0.04	0.04	0.98
European Community	0.54	0.54	0.89

Note: The first column reports data moments the HAT-model targets. The second reports the model moments. The third column reports the estimated parameter values.

Far distances ≈ 10 percent less expensive than standard models would predict.

US Trade Elasticities: $-\theta_{us,j}$



Gains from Trade

Two ideas I want to illustrate:

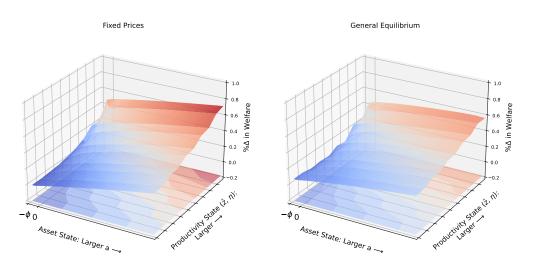
- 1. You pick the market, you pick a person.
- 2. GE effects have distributional consequences.

Next slides:

10% reduction to US import trade cost on different source markets: Japan (big), France (medium). Focus on US welfare and break it down by. . .

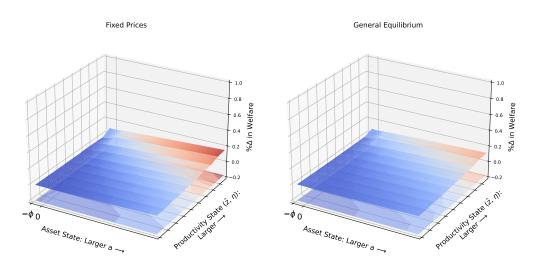
- A. Fix R & w, so what is direct effect of change in trade cost,
- B. R & w adjust to clear goods and asset markets.

U.S. Welfare: 10% Reduction to Japan



1. Most gain — but trade is very pro-rich. 2. R fell \Rightarrow the poor who don't benefit directly from trade with Japan gain (left vs. right panel).

U.S. Welfare: 10% Reduction to France



Relative to Japan: Gains from trade smaller, very concentrated on the rich.

Efficient Trade

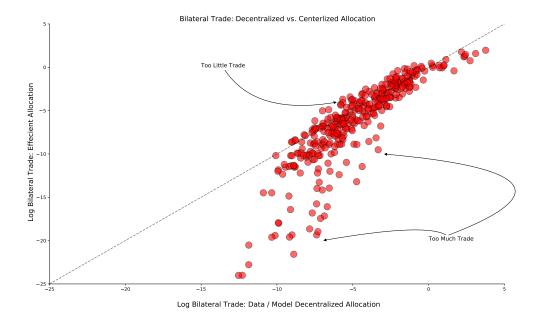
The previous slides suggest that being exposed / liberalizing with some markets is better than others.

What is the first-best pattern of trade?

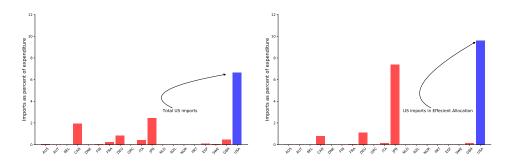
How I answer this question:

- Take a stand on country-specific Pareto weights I set them proportional to a country's TFP.
 Why? P2C2E in a slide.
- Then given calibrated parameter values, compute the efficient allocation in Proposition #4.

Efficient Trade



US Imports: Decentralized vs. Efficient Allocation



For the US, the Planner reallocates trade and expands it...

- Squashes trade with uncompetitive sources these varieties are like luxuries in that they only
 cater to the rich like France.
- Expands trade with sources that can "serve the masses" like Japan (productive and large).
- On net, US trade expands...but this does not happen everywhere.

Where I'm headed next...

On my todo list:

- Can trade policy improve outcomes? Put in tariffs and redistribute.
- Quality or "residual demand shifters" and calibration to line up with the micro-evidence of papers like Auer et al. (2022).

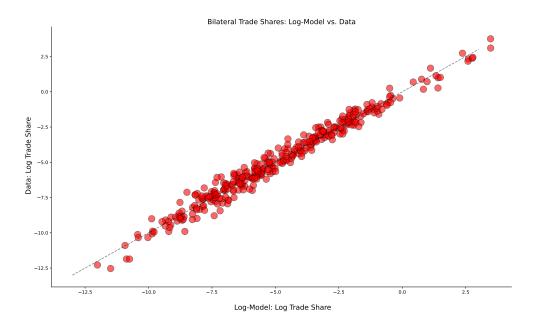
Any thing else? Email me!

One more thing: My github repository provides the code and supplementary work behind this paper at https://github.com/mwaugh0328/heterogeneous-agent-trade.

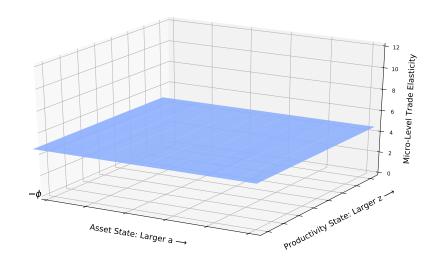
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Log Model — Fit of Trade Data



Log Model — Micro Elasticities



How do households respond on the intensive margin to a change in trade costs?

$$egin{aligned} heta_{ij}(\mathsf{a},\mathsf{z})' &:= rac{\partial c_{ij}(\mathsf{a},\mathsf{z})/c_{ij}(\mathsf{a},\mathsf{z})}{\partial d_{ij}/d_{ij}}, \ &= \left[-rac{\partial g_{ij}(\mathsf{a},\mathsf{z})/p_{ij}c_{ij}(\mathsf{a},\mathsf{z})}{\partial p_{ij}/p_{ij}} - 1
ight] rac{\partial p_{ij}/p_{ij}}{\partial d_{ij}/d_{ij}}. \end{aligned}$$

The idea: A reduction in trade costs relaxes the hh's budget constraint, so the intensive margin elasticity depends on the division of new resources between assets and expenditure.

How do households respond on the extensive margin?

$$\theta_{ij}(a,z)^E := \frac{\partial \pi_{ij}(a,z)/\pi_{ij}(a,z)}{\partial d_{ij}/d_{ij}},$$

$$=-\frac{\partial \Phi_i(a,z)/\Phi_i(a,z)}{\partial d_{ij}/d_{ij}}-\frac{1}{\sigma_\epsilon}\bigg[u'(c_{ij}(a,z))c_{ij}(a,z)\bigg]+\beta\mathbb{E}\frac{1}{\sigma_\epsilon}\frac{\partial v_i(a',z')}{\partial d_{ij}/d_{ij}}.$$

To get a sense of things, vary the second term by wealth...

$$\frac{\partial (u'(c_{ij}(a,z))c_{ij}(a,z))}{\partial a} = u'(c_{ij}(a,z)) \times \mathsf{MPC}_{ij}(a,z) \times \left[-\rho_{ij}(a,z) + 1 \right]$$

where $\rho_{ij}(a,z)$ is the Arrow-Pratt measure of relative risk aversion.

With CRRA, if risk aversion > 1, then poor, high marginal utility households (who are also high MPC households) are more elastic relative to rich households on the extensive margin.

How do households respond on the extensive margin?

$$egin{aligned} heta_{ij}(\mathsf{a},\mathsf{z})^{\mathsf{E}} &:= rac{\partial \pi_{ij}(\mathsf{a},\mathsf{z})/\pi_{ij}(\mathsf{a},\mathsf{z})}{\partial d_{ij}/d_{ij}}, \ &= -rac{\partial \Phi_i(\mathsf{a},\mathsf{z})/\Phi_i(\mathsf{a},\mathsf{z})}{\partial d_{ii}/d_{ii}} - rac{1}{\sigma_{\epsilon}} igg[u'(c_{ij}(\mathsf{a},\mathsf{z}))c_{ij}(\mathsf{a},\mathsf{z}) igg] + eta \mathbb{E} rac{1}{\sigma_{\epsilon}} rac{\partial v_i(\mathsf{a}',\mathsf{z}')}{\partial d_{ii}/d_{ii}}. \end{aligned}$$

To get a sense of things, vary the second term by wealth...

$$\frac{\partial (u'(c_{ij}(\textbf{a},\textbf{z}))c_{ij}(\textbf{a},\textbf{z}))}{\partial \textbf{a}} = u'(c_{ij}(\textbf{a},\textbf{z})) \times \mathsf{MPC}_{ij}(\textbf{a},\textbf{z}) \times \bigg[-\rho_{ij}(\textbf{a},\textbf{z}) + 1 \bigg],$$

where $\rho_{ij}(a, z)$ is the Arrow-Pratt measure of relative risk aversion.

With CRRA, if risk aversion > 1, then poor, high marginal utility households (who are also high MPC households) are *more elastic relative* to rich households on the extensive margin.