

We then have: Y= bsing X= a((054- E) = a sing アカニメネナリネ! rd = a2 ((1-22) sindy + cosdy -2 22000 + 62) SiNA 4=1-cos24! 12 = 03 [1-62-cos24+620524+cos24-d(cus4+62) = a3[1+62(0524-24(074) = 22(1-20054), and so (4)= a (1-2 cusy) Thus for, our derivation has been purely geometrical. Now, we can use our shape on equation (A) to relate & and 4. For a body under the un inverse square force,  $\theta(r)$  is;  $\theta(r) = \int \frac{(1/ra) dr}{\left[2\mu(E + \frac{\kappa}{r} - \frac{e^2}{2\mu r})\right]}$ 

$$\frac{1}{2\pi} \int \frac{(1/h) dr}{|E+K-\frac{2}{2nr^2}|} \int \frac{1}{|E+K-\frac{2}{2nr^2}|} \int \frac{1}{|E+K-\frac{2}{2nr^2}|} \int \frac{1}{|E+K-\frac{2}{2nr^2}|} \int \frac{1}{|E+K-\frac{2}{2nr^2}|} \int \frac{1}{|E+K-\frac{2}{2nr^2}|} \int \frac{1}{|E+\frac{2}{2nr^2}|} \int \frac{1}{|E+\frac{2}{2nr^2}|}$$

Which is all equivilent to b, so:  $cos(\theta) = \frac{\ell^2}{2nr}$ , where  $\epsilon = \sqrt{\frac{\epsilon \ell^2}{2k_{2n}^2 + 1}}$ ,  $\chi = \frac{\ell^2}{2k_{2n}^2 + 1}$ ,  $\chi = \frac{\ell^2}{2k_{2n}^2 + 1}$ (= 1+4 cost) (which describes a somie section with eccentricity 4) P+ 4 r cost = 2, 1/2) ( a = a ( ( = 4))! because the orbit is an ellipse, we require that X= 2(1-2), 10: - (E) r+ 2 - coso + all (-22) ) = al (2) ho cost = a(1-42)-1, nolding he to beth sides! 4+41(0x8=4+0)(1-22)-r 4161+(050) = ((4-1)) + a(4-4)(1+4) 61(1+6058)=(1-4)[a(1+4)-r]

Now, we recall that  $r = a(1 - 2\cos\psi)$ ; making this substitution, it follows that: をか(11+2000日)=(1-2)[K(1+ん)-K(1-4cosp)] Kr((1+ (05θ) = 2(1- ε) [ K+ 56 (65 φ)]  $\Gamma(1+\cos\theta)=\alpha(1-\epsilon)(1+\cos\psi)$ Boing back to the relation +4×cost=4(1.43) we instead subtract he, giving: 486068+610= 0,(1-62)-1-41 2r(cose-1)= a(1-a)(1+a)-r(1+a) ٤+(cosq-1)=(1+4)[x(1-4)-r] us r= a(1-4 cos ψ)1 21(1058-1) = (1+4)[4(1-4)-4(1-4(0)4)] 2 r ( cost -1) = a (1+a) [1-2-1+2 cost] Xv((056-1)=4(1+4)[-5/+ \$/(054)]

r (cosq-1) = x(1+x)(cosq-1) Dividing the result from sultragting he by that from sallting they he sives: (050+1 = 1+2, 1-cosp (050+1 = 1-2, 1-cosp and as tand = (050-1. ナムのター 1-2+との少 2 aveten (1+8) 10 - Vereten (ta) Differentiating + in 2 = [ 1+2 ] +un & sives; Ysecre do= Ysecry 1th 2中 do = (052 \$ ) 1+5 1 14 as r(1+(050)= L(1-4)(1+(054), r= L(1-4) 1+(054) however, い しょるき=ま(1+しのの日); r=4(1-4) (052(4)

Reppleis second low states that equal went are swept out by the wold in equal times. Buy that the period of orbit is T; the war of the ellipse is A = 12 h b. Because area is swept out at a constant rate, this rate must be the area swept out in un orbit in a time T, At - A = Rub; we can equale this will the area integral, SdA=15, rado (analogous to 40 st for a circle), That is; Tabte & Srada As do = Cos2# 11-2 dp ( r=a[1-2] cos2# rab == = = (1+4) rd4 Saking V= 4(1- 20054); 125 + = = = 1 (4 - 25 in4)

les b= </1-62'; RESTERT + = \$ [4- 25 in4)  $\frac{dn}{t} + = \psi - 4 \sin \psi$ Which must sometrow be approximated,