

No-Pain No-Gain: DRL Assisted Optimization in Energy-Constrained CR-NOMA Networks

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Abstract

This paper applies machine learning to optimize the transmission policy of cognitive radio inspired non-orthogonal multiple access (CR-NOMA) networks, where time-division multiple access (TDMA) is used to schedule multiple primary users and an energy-constrained secondary user is admitted to the primary users' time slots via NOMA. During each time slot, the secondary user performs the two tasks: data transmission and energy harvesting based on the signals received from the primary users. The goal of the paper is to maximize the secondary user's long-term throughput, by optimizing its transmit power and the time-sharing coefficient for its two tasks. The long-term throughput maximization problem is challenging due to the need for making decisions that yield long-term gains but might result in short-term losses. For example, when in a given time slot, a primary user with large channel gains transmits, intuition suggests that the secondary user should not carry out data transmission due to the strong interference from the primary user but perform energy harvesting only, which results in zero data rate for this time slot but yields potential long-term benefits. In this paper, a deep reinforcement learning approach is applied to emulate this intuition, where the deep deterministic policy gradient (DDPG) algorithm is employed together with convex optimization. Our simulation results demonstrate that the proposed deep reinforcement learning assisted NOMA transmission scheme can yield significant performance gains over two benchmark schemes.

I. INTRODUCTION

Machine learning has been recognized as one of the most important enabling technologies for the next generation wireless networks [1]. The key idea behind machine learning is to learn to make optimal decisions based on observed data or the environment [2]. Because of its general

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utility, machine learning has been applied to a variety of wireless communication problems. For example, supervised learning has been applied to link adaption and channel estimation in orthogonal frequency-division multiplexing (OFDM) systems [3], [4]. Unsupervised learning has been shown to be particularly beneficial for improving the accuracy of wireless positioning in [5] and reducing the complexity of beamformer design [6]. Reinforcement learning has also been shown to be applicable to various communication problems, including energy harvesting, resource allocation, data and computation offloading, and network security [7]–[9].

This paper focuses on the application of machine learning to non-orthogonal multiple access (NOMA) systems. We note that this application has already received significant attention in the literature [10]. For example, an unsupervised machine learning algorithm, K-means, has been applied to millimeter-wave NOMA networks for the joint design of beamforming and user clustering [11]. A similar K-means based approach has also been proposed for terahertz NOMA systems employing nodes equipped with multiple antennas [12]. A power minimization problem for multi-carrier NOMA facilitated by simultaneous wireless information and power transfer (SWIPT) has been solved by applying deep learning in [13]. In [14], an intelligent offloading scheme powered by deep learning was proposed for NOMA assisted mobile edge computing (NOMA-MEC). Furthermore, deep learning approaches have been developed for the design of NOMA transceivers and the codebook of sparse code multiple access (SCMA) in [15] and [16], respectively. An overview of additional related work on the application of machine learning to NOMA can be found in recent survey articles [17]–[20].

A key challenge for the application of machine learning to wireless communications is due to the following dilemma. On the one hand, if the considered wireless environments, e.g., wireless channels, are time invariant, the application of machine learning might not offer significant benefits, compared to conventional optimization tools, such as convex optimization and game theory. On the other hand, if the wireless channels are time-varying, most machine learning approaches require extensive training, which is needed to enumerate all possible situations such that the machine learning algorithm can learn how to emulate optimal decisions when these situations are encountered again in the future. Given the dynamic nature of wireless systems, extensive training can be prohibitively expensive, if not impossible. Therefore, a natural question is whether there exist communication scenarios in which the wireless environment is time-varying but this change can be effectively learned and used with a reasonable training effort. Such communication scenarios would be ideal for the application of machine learning.

The main contribution of this paper is to show that an ideal application scenario for machine learning does indeed exist in NOMA systems. In particular, this paper considers a cognitive radio (CR) inspired NOMA network, where multiple primary users and one energy-constrained secondary user communicate with the same base station, as shown in Fig. 1(a). Time-division multiple access (TDMA) is used to schedule the primary users, where the use of CR-NOMA ensures that the secondary user can be admitted to the primary users' time slots without degrading their quality of service (QoS) experience [21]. During each time slot, the secondary user performs the two tasks: Data transmission and energy harvesting from the signals sent by the primary users [22]. While it is assumed that all the users' channels are constant, for the secondary user, its communication environment is time varying and changes from one time slot to the next, since different primary users are scheduled in different time slots, as shown in Fig. 1(b). This time-varying pattern can be effectively learned by machine learning.

The objective of this paper is to maximize the secondary user's long-term throughput, by optimizing its transmit power and also the time-sharing coefficient for its two tasks. This throughput maximization problem is challenging because of the need for making a decision which might yield a long-term gain but could result in a short-term loss. For example, when a primary user with strong channels to both the base station and the secondary user transmits in a given time slot, a human would decide that the secondary user should not transmit data but carry out energy harvesting only, since the primary user would cause severe interference. Even though this decision leads to zero data rate in this particular time slot, it may yield a performance gain in the future since a significant amount of energy can be harvested due to the primary user's strong channel conditions. With conventional optimization tools, it is difficult to emulate this 'no pain no gain'-like decision, which implies that the considered NOMA scenario is ideal for the application of machine learning.

Therefore, in this paper, a deep reinforcement learning approach, termed deep deterministic policy gradient (DDPG), is applied to the considered long-term throughput maximization problem [23]. Recall that compared to supervised and unsupervised machine learning, reinforcement learning has the capability to make decisions and perform learning at the same time, which is an ideal feature for wireless communication applications [7], [24]. DDPG can be viewed as an enhanced implementation of deep reinforcement learning, where action-value functions are approximated by neural networks and the action space does not have to be discrete or finite [23], [25]. In order to facilitate the application of DDPG, the considered long-term

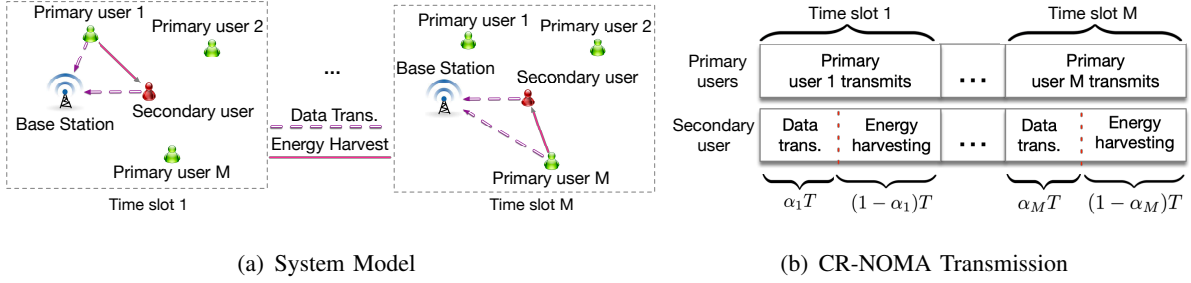


Fig. 1. A system diagram for the considered CR-NOMA uplink communication scenario, where a secondary user shares the spectrum with M primary users and harvests energy from the signals sent by the primary users.

throughput maximization problem is first decomposed into two optimization subproblems. The first subproblem focuses on a single time slot and optimizes the secondary user's transmit power and the time sharing coefficient, where the closed-form optimal solution is found by applying convex optimization. The second subproblem targets the optimization of the energy fluctuation across different time slots, and is solved by applying the adopted deep reinforcement learning tool, DDPG. Extensive simulation results are provided to demonstrate that the proposed DDPG assisted NOMA scheme effectively emulates optimal decisions and offers significant performance gains over two benchmark schemes.

II. SYSTEM MODEL

Consider a CR-NOMA uplink scenario as shown in Fig. 1(a), with one base station, M primary users, denoted by U_m , $1 \leq m \leq M$, and one energy-constrained secondary user, denoted by U_0 . Denote each user's channel gain by h_m , $0 \leq m \leq M$, and the channel between U_0 and U_i by $h_{i,0}$, $1 \leq i \leq M$, where the effects of both large scale path loss and quasi-static multi-path fading are included. We assume that all channel gains are constant during the considered CR-NOMA transmission period.

The M primary users are scheduled to transmit via TDMA based round-robin scheduling, as shown in Fig. 1(b). In particular, in the n -th time slot, denoted by t_n , user U_m , $m = (n - 1) \oplus M + 1$, is scheduled to transmit, where \oplus denotes a modulo operation. For example, for $M = 2$, the primary users scheduled at t_1 , t_2 , t_3 , and t_4 are U_1 , U_2 , U_1 , and U_2 , respectively. We note that the TDMA based round-robin scheduling is assumed to be fixed and carried out over a long period of time such that each primary user is scheduled to transmit multiple times.

The secondary user is admitted to the primary users' time slots via CR-NOMA. In particular, in time slot t_n , the secondary user uses the first $\alpha_n T$ seconds for its data transmission, where α_n is a time-sharing parameter, $0 \leq \alpha_n \leq 1$, and T denotes the duration of each time slot. The

remainder of the time slot, $(1 - \alpha_n)T$ seconds, will be used for battery charging by harvesting energy from the signals sent by the primary user U_n , as shown in Fig. 1(b). At the beginning of t_n , the scheduled primary user's channel state information (CSI), i.e., h_n and $h_{n,0}$, is assumed to be available at the secondary user¹.

Denote the remaining energy in the secondary user's battery at the beginning of the n -th time slot by E_n , which means that E_{n+1} can be expressed as follows:

$$E_{n+1} = \min \left\{ \underbrace{(1 - \alpha_n)T\eta P_n |h_{n,0}|^2}_{\text{Harvested energy}} - \underbrace{\alpha_n T P_{0,n}}_{\text{Used energy}} + E_n, E_{\max} \right\}, \quad (1)$$

where E_{\max} denotes the capacity limit of the secondary user's battery, η denotes the energy harvesting efficiency coefficient, P_n and $P_{0,n}$ denote the transmit powers of U_n and U_0 at t_n , respectively. In (1), a linear energy harvesting model is assumed, and the impact of the energy consumption for signal processing and of the radio frequency circuits has been omitted. These assumptions have been used in order to obtain insight regarding the long-term optimization of the two conflicting tasks, energy harvesting and data transmission. We note that the extension of the proposed machine learning algorithm to the case with more practical assumptions is an important direction for future research.

Due to the energy causality constraint, the secondary user's transmit power is capped by the energy available at its battery, i.e.,

$$\alpha_n T P_{0,n} \leq E_n. \quad (2)$$

We note that (2) ensures that E_{n+1} shown in (1) is always non-negative.

Therefore, the data rate that the secondary user can achieve at t_n is given by²

$$R_n = \alpha_n \ln \left(1 + \frac{P_{0,n} |h_0|^2}{1 + P_n |h_n|^2} \right), \text{ [nats per channel use (NPCU)]}, \quad (3)$$

where the QoS-based successive interference cancellation (SIC) decoding order is assumed in (3) in order to guarantee that the primary users' QoS experience is not affected by admitting the secondary user into their time slots. More sophisticated SIC strategies can be used to further improve the performance of the CR-NOMA scheme, as discussed in [26].

¹During the first M time slots, h_n is simply U_n 's channel. For t_n , $n > M$, U_m is scheduled and h_n will be h_m , $m = (n - 1) \oplus M + 1$, as discussed before.

²For notational convenience, the noise power is assumed to be normalized, such that the value of the noise power is absorbed into the channel gains $|h_0|^2$ and $|h_n|^2$.

The aim of this paper is to maximize the secondary user's long-term throughput by optimizing the time-sharing parameter, α_n , and the power allocation coefficient, $P_{0,n}$. The corresponding optimization problem can be formulated as follows [8], [9], [24]:

$$\max_{P_{0,n}, \alpha_n} \sum_{n=1}^{\infty} \gamma^{n-1} R_n \quad (\text{P1a})$$

$$\text{s.t. } E_{n+1} = \min \{ (1 - \alpha_n) T \eta P_n |h_{n,0}|^2 - \alpha_n T P_{0,n} + E_n, E_{\max} \} \quad (\text{P1b})$$

$$\alpha_n T P_{0,n} \leq E_n \quad (\text{P1c})$$

$$0 \leq \alpha_n \leq 1 \quad (\text{P1d})$$

$$0 \leq P_{0,n} \leq P_{\max}, \quad (\text{P1e})$$

where P_{\max} denotes the maximal transmit power of the secondary user, and γ denotes the discount rate parameter [24].

Remark 1: One can also formulate the problem by asking the secondary user to charge its battery in each time slot before transmitting its data. Intuitively, both formulations should lead to the same problem formulation, which however is not true. In particular, if the secondary user carries out energy harvesting first, the energy available for data transmission is given by

$$\min \{ E_{\max}, E_n + \alpha_n T \eta P_n |h_{n,0}|^2 \}, \quad (4)$$

which means that the constraints in (P1c) and (P1d) need to be formulated as follows:

$$E_{n+1} = \max \{ \min \{ E_{\max}, E_n + \alpha_n T \eta P_n |h_{n,0}|^2 \} - (1 - \alpha_n) T P_{0,n}, 0 \}, \quad (5)$$

$$\alpha_n T P_{0,n} \leq \min \{ E_{\max}, E_n + \alpha_n T \eta P_n |h_{n,0}|^2 \}, \quad (6)$$

respectively. The constraints in (5) and (6) are more complicated than (P1c) and (P1d), which makes solving the rate maximization problem more difficult.

Remark 2: The following two strategies will be used as benchmark schemes in this paper. For the first scheme, termed the greedy algorithm, U_0 uses all the energy available for data transmission, and then starts energy harvesting. In particular, U_0 's transmit power is fixed at P_{\max} , and $\alpha_n = \min \left\{ 1, \frac{E_n}{T P_{\max}} \right\}$ is adopted by the greedy algorithm. For the case that $T P_{\max} \geq E_n$, this choice of α_n means that all the energy available, E_n , will be used to power data transmission, i.e., $T P_{\max} \alpha_n = E_n$. For the second benchmark scheme, termed the random algorithm, P_{\max} is used as U_0 's transmit power and α_n is uniformly generated between 0 and $\min \left\{ 1, \frac{E_n}{T P_{\max}} \right\}$.

Because $\alpha_n \leq \frac{E_n}{TP_{\max}}$, it is guaranteed that there is enough energy for U_0 to transmit during $\alpha_n T$ seconds with transmit power P_{\max} .

Remark 3: Problem P1 cannot be straightforwardly solved by applying conventional convex optimization, not only because its equality constraint in (P1b) is not affine, but also because its objective function is a long-term non-convex throughput function. However, Problem P1 is ideally suited for the application of machine learning, as discussed in the following section.

III. PROBLEM REFORMULATION FOR APPLICATION OF REINFORCEMENT LEARNING

A. Rationale Behind the Application of Reinforcement Learning

A useful criterion to evaluate whether the application of reinforcement learning is beneficial or not is whether there exists a pattern or a feature which can be effectively learned and used to increase the objective function of the considered problem. In the following, a simple example with two primary users, i.e., U_1 and U_2 , is used to illustrate the feature inherent to the considered CR-NOMA scenario.

In particular, assume that U_1 has very strong channels to both U_0 and the base station, i.e., $|h_1|^2 \rightarrow \infty$ and $|h_{1,0}|^2 \rightarrow \infty$, whereas U_2 has very weak channels to both U_0 and the base station, i.e., $|h_2|^2 \rightarrow 0$ and $|h_{2,0}|^2 \rightarrow 0$. Intuition in this situation suggests to encourage the secondary user to do the following:

- Use most of the time slot for energy harvesting when U_1 transmits. The reason is that $|h_1|^2 \rightarrow \infty$ means that U_1 is a strong interference source for U_0 's data transmission, and $|h_{1,0}|^2 \rightarrow \infty$ means an opportunity to harvest a large amount of energy from U_1 .
- Use most of the time slot for data transmission when U_2 transmits. The reason is that $|h_2|^2 \rightarrow 0$ means an interference free situation, and hence it is possible to achieve a high data rate, as indicated in (3). $|h_{1,0}|^2 \rightarrow 0$ implies that only a small amount of energy can be harvested from U_2 .

Note that the actions following this intuition might incur short-term losses compared to the benchmark schemes. For example, when U_1 transmits, a rationale action is to ask U_0 to carry out energy harvesting only, which leads to zero data rate in this particular time slot. In other words, in the time slots where U_1 transmits, the data rate achieved by the action following the intuition is smaller than the data rates achieved by the benchmark schemes. However, this temporary sacrifice yields a large amount of harvested energy and hence a potential long-term

gain. Reinforcement learning is an ideal tool for emulating this intuition by learning the feature inherent in the considered problem, as shown in the remainder of this paper.

B. Problem Reformulation

In order to facilitate the application of DDPG, problem P1 needs to be reformulated as follows. First, similar to [8], we introduce an energy fluctuation parameter, which is defined as the difference between the energy consumed and harvested at t_n :

$$\bar{E}_n = (1 - \alpha_n)T\eta P_n |h_{n,0}|^2 - \alpha_n T P_{0,n}. \quad (7)$$

\bar{E}_n can be interpreted as the energy surplus (or deficit) at t_n if $\bar{E}_n > 0$ (or $\bar{E}_n < 0$). We note that for a fixed \bar{E}_n , the data rate at t_n , R_n , depends on the power allocation coefficient and the time-sharing parameter at t_n only, where the parameters for the other time slots, i.e., α_m and $P_{0,m}$, $m \neq n$, will not have any impact on R_n . This observation can be clearly illustrated by recasting problem P1 in the following equivalent form [27, Page 133]:

$$\max_{\bar{E}_n} \sum_{n=1}^{\infty} \gamma^{n-1} \tilde{R}_n \quad (\text{P2a})$$

$$\text{s.t. } E_{n+1} = \min \{E_{\max}, E_n + \bar{E}_n\}, \quad (\text{P2b})$$

where \tilde{R}_n is defined as follows:

$$\tilde{R}_n = \sup \{R_n | (1 - \alpha_n)T\eta P_n |h_{n,0}|^2 - \alpha_n T P_{0,n} = \bar{E}_n, (\text{P1c}), (\text{P1d}), (\text{P1e})\}.$$

Therefore, problem P1 can be solved by first solving the following optimization problem:

$$\max_{P_{0,n}, \alpha_n} R_n \quad (\text{P3a})$$

$$\text{s.t. } (1 - \alpha_n)T\eta P_n |h_{n,0}|^2 - \alpha_n T P_{0,n} = \bar{E}_n \quad (\text{P3b})$$

$$(\text{P1c}), (\text{P1d}), (\text{P1e}).$$

Denote the optimal solutions of problem P3 by $\alpha_n^*(\bar{E}_n)$ and $P_{0,n}^*(\bar{E}_n)$, where $\alpha_n^*(\bar{E}_n)$ and $P_{0,n}^*(\bar{E}_n)$ are expressed as functions of \bar{E}_n in order to highlight the fact that the optimal solutions, α_n and $P_{0,n}$, are obtained for a given \bar{E}_n . The closed-form expressions for $\alpha_n^*(\bar{E}_n)$ and $P_{0,n}^*(\bar{E}_n)$ are then substituted in problem P2, which yields the following optimization problem:

$$\max_{\bar{E}_n} \sum_{n=1}^{\infty} \gamma^{n-1} R_n (\alpha_n^*(\bar{E}_n), P_{0,n}^*(\bar{E}_n)) \quad (\text{P4a})$$

$$\text{s.t. } E_{n+1} = \min \{E_{\max}, E_n + \bar{E}_n\}. \quad (\text{P4b})$$

where $R_n(\alpha_n^*(\bar{E}_n), P_{0,n}^*(\bar{E}_n))$ is a function of \bar{E}_n only, i.e., $R_n(\alpha_n^*(\bar{E}_n), P_{0,n}^*(\bar{E}_n)) = \alpha_n^*(\bar{E}_n) \ln \left(1 + \frac{P_{0,n}^*(\bar{E}_n)|h_0|^2}{1+P_n|h_n|^2} \right)$.

In Section IV, problem P3 will be solved via convex optimization, where closed-form expressions for $\alpha_n^*(\bar{E}_n)$ and $P_{0,n}^*(\bar{E}_n)$ will be presented. In Section V, problem P5 will be reformulated as a reinforcement learning problem and the DDPG algorithm will be applied to find the solution.

IV. FINDING CLOSED-FORM EXPRESSIONS FOR $\alpha_n^*(\bar{E}_n)$ AND $P_{0,n}^*(\bar{E}_n)$

In order to find closed-form expressions for $\alpha_n^*(\bar{E}_n)$ and $P_{0,n}^*(\bar{E}_n)$, we first recast (P3) as follows:

$$\max_{P_{0,n}, \alpha_n} f_0(P_{0,n}, \alpha_n) \triangleq \alpha_n \ln \left(1 + \frac{P_{0,n}|h_0|^2}{1+P_n|h_n|^2} \right) \quad (\text{P5a})$$

$$\text{s.t.} \quad f_1(P_{0,n}, \alpha_n) = 0, \quad (\text{P5b})$$

$$f_2(P_{0,n}, \alpha_n) \leq 0, \quad (\text{P5c})$$

$$(\text{P1d}), (\text{P1e}). \quad (\text{P5d})$$

where $f_1(P_{0,n}, \alpha_n) = (1 - \alpha_n)T\eta P_n|h_{n,0}|^2 - \alpha_n T P_{0,n} - \bar{E}_n$ and $f_2(P_{0,n}, \alpha_n) = \alpha_n T P_{0,n} - E_n$.

Remark 4: Note that problem P5 is not jointly convex in $P_{0,n}$ and α_n . For example, its equality constraint, (P5b), is not an affine function. A similar optimization problem was considered in [8], where the equality constraint was relaxed to an inequality constraint. However, in the expression for the relaxed inequality constraint shown in [8, Eq. (13)], there is still a term which involves the multiplication of two optimization variables, which means that the inequality function is not convex and hence the relaxed problem is not in a convex form.

According [27, Page 133], an equivalent form of problem (P5) can be found as follows:

$$\max_{\alpha_n} \tilde{f}_0(\alpha_n) \quad (\text{P6a})$$

$$\text{s.t.} \quad 0 \leq \alpha_n \leq 1, \quad (\text{P6b})$$

where $\tilde{f}_0(\alpha_n)$ is defined as follows:

$$\tilde{f}_0(\alpha_n) = \sup \{f_0(P_{0,n}, \alpha_n) | f_1(P_{0,n}, \alpha_n) = 0, f_2(P_{0,n}, \alpha_n) \leq 0, P_{0,n} \geq 0\}. \quad (8)$$

Finding $\tilde{f}_0(\alpha_n)$ is equivalent to solving the following optimization problem:

$$\max_{P_{0,n}} \quad \alpha_n \ln \left(1 + \frac{P_{0,n}|h_0|^2}{1 + P_n|h_n|^2} \right) \quad (\text{P7a})$$

$$\text{s.t.} \quad P_{0,n} = \frac{(1 - \alpha_n)\eta P_n|h_{n,0}|^2}{\alpha_n} - \frac{\bar{E}_n}{\alpha_n T} \quad (\text{P7b})$$

$$P_{0,n} \leq \frac{E_n}{\alpha_n T} \quad (\text{P7c})$$

$$0 \leq P_{0,n} \leq P_{\max}. \quad (\text{P7d})$$

Note that problem P7 is a function of $P_{0,n}$ only, where α_n is fixed. By using the equality constraint in (P7b), the optimal value of $\tilde{f}_0(\alpha_n)$ can be found as follows:

$$\tilde{f}_0^*(\alpha_n) = \alpha_n \ln \left(1 + \frac{\frac{(1-\alpha_n)\eta P_n|h_{n,0}|^2|h_0|^2}{\alpha_n} - \frac{\bar{E}_n|h_0|^2}{\alpha_n T}}{1 + P_n|h_n|^2} \right), \quad (9)$$

where the constraints in (P7c) and (P7d) can be guaranteed by expressing the domain of $\tilde{f}_0(\alpha_n)$ as follows:

$$\mathcal{D} = \left\{ \alpha_n | 0 \leq \frac{(1 - \alpha_n)\eta P_n|h_{n,0}|^2}{\alpha_n} - \frac{\bar{E}_n}{\alpha_n T} \leq \min \left\{ P_{\max}, \frac{E_n}{\alpha_n T} \right\} \right\}. \quad (10)$$

By using $\tilde{f}_0^*(\alpha_n)$ and showing the constraints on the domain of the function explicitly, problem (P6) can be equivalently recast as follows:

$$\max_{\alpha_n} \quad \alpha_n \ln \left(1 + \frac{\frac{(1-\alpha_n)\eta P_n|h_{n,0}|^2|h_0|^2}{\alpha_n} - \frac{\bar{E}_n|h_0|^2}{\alpha_n T}}{1 + P_n|h_n|^2} \right) \quad (\text{P8a})$$

$$\text{s.t.} \quad \alpha_n \leq 1 - \frac{\bar{E}_n}{T\eta P_n|h_{n,0}|^2} \quad (\text{P8b})$$

$$\alpha_n \geq 1 - \frac{E_n + \bar{E}_n}{T\eta P_n|h_{n,0}|^2} \quad (\text{P8c})$$

$$\alpha_n \geq \frac{T\eta P_n|h_{n,0}|^2 - \bar{E}_n}{T\eta P_n|h_{n,0}|^2 + TP_{\max}} \quad (\text{P8d})$$

$$0 \leq \alpha_n \leq 1. \quad (\text{P8e})$$

Note that for problem P8, there are three lower bounds and two upper bounds on α_n . In addition, the domain of the objective function in (P8a) also imposes a constraint on the choice of α_n . Therefore, the problem might be infeasible if one of the lower bounds is larger than one of the upper bounds, and hence it is important to carry out a feasibility study for problem P8, as is done in the following proposition.

Proposition 1. *Problem P8 is always feasible.*

Proof. See Appendix A. □

Remark 5: For the case $\bar{E}_n = T\eta P_n |h_{n,0}|^2$, the upper bound in (P8b) becomes 0, which means that the only feasible solution for this case is $\alpha_n^*(\bar{E}_n) = 0$. Therefore, no data transmission happens and $R_n = 0$ for this case. We note that the case with $\bar{E}_n = T\eta P_n |h_{n,0}|^2$ can cause a singularity issue when analyzing the convexity of the objective function. Therefore, unless otherwise stated, it is assumed that $\bar{E}_n \neq T\eta P_n |h_{n,0}|^2$ for the remainder of this section.

Another important step in finding the optimal solution of problem P8 is to study the convexity of its objective function, which is done in the following proposition.

Proposition 2. *The objective function of problem P8 is a concave function of α_n , for $\alpha_n \geq 0$.*

Proof. See Appendix B. □

Given the two useful properties provided in Propositions 1 and 2, it can be easily verified that problem P8 is a concave problem; however, finding a closed-form solution for problem P8 is challenging, due to the multiple constraints on the choices of α_n as shown in (P8b), (P8c), (P8d), and (P8e). It is important to point out that these constraints cannot be merged. For example, the constraint in (P8c) is not always stricter than $\alpha_n \geq 0$ shown in (P8e) since

$$1 - \frac{E_n + \bar{E}_n}{T\eta P_n |h_{n,0}|^2} = \frac{T\eta P_n |h_{n,0}|^2 - E_n - \bar{E}_n}{T\eta P_n |h_{n,0}|^2} \quad (11)$$

which can be either negative or positive. As a result, finding the optimal solution by directly applying the Karush-Kuhn-Tucker (KKT) conditions to problem P8 is difficult, since five dual variables are required due to the large number of inequality constraints. Furthermore, the fact that the root of the first-order derivative of the objective function is in the form of the Lambert W function with two branches makes it more challenging to find a closed-form expression for the optimal solution.

Nevertheless, by using the properties of the inequality constraints of problem P8, a closed-form optimal solution can be found, as shown in the following lemma.

Lemma 1. *The optimal solution for problem P8 can be expressed as follows:*

$$\alpha_n^*(\bar{E}_n) = \min \{1, \max \{x^*, \theta_0\}\}, \quad (12)$$

if $\bar{E}_n \neq T\eta P_n |h_{n,0}|^2$, otherwise $\alpha_n^*(\bar{E}_n) = 0$. where $x^* = \frac{\kappa_1 - \kappa_2}{e^{W_0(e^{-1}(\kappa_1 - 1)) + 1} - 1 + \kappa_1}$, $\theta_0 = \max \left\{ 1 - \frac{E_n + \bar{E}_n}{T\eta P_n |h_{n,0}|^2}, \frac{T\eta P_n |h_{n,0}|^2 - \bar{E}_n}{T\eta P_n |h_{n,0}|^2 + TP_{\max}} \right\}$, $\kappa_1 = \frac{\eta P_n |h_{n,0}|^2 |h_0|^2}{1 + P_n |h_n|^2}$, $\kappa_2 = \frac{\bar{E}_n |h_0|^2}{T(1 + P_n |h_n|^2)}$ and $W_0(\cdot)$ denotes the principle branch of the Lambert W function [28].

Proof. See Appendix C. □

Remark 6: Given the closed-form expression for $\alpha_n^*(\bar{E}_n)$, the optimal power allocation coefficient is given by

$$P_{0,n}^*(\bar{E}_n) = \frac{(1 - \alpha_n^*)\eta P_n |h_{n,0}|^2}{\alpha_n^*} - \frac{\bar{E}_n}{\alpha_n^* T}, \quad (13)$$

if $\bar{E}_n \neq T\eta P_n |h_{n,0}|^2$. We note that the case of $\bar{E}_n = T\eta P_n |h_{n,0}|^2$ is not discussed in the proof of Lemma 1. As discussed in Remark 5, if $\bar{E}_n = T\eta P_n |h_{n,0}|^2$, the entire time available will be used for energy harvesting, and there is no data transmission, i.e., $\alpha_n^*(\bar{E}_n) = 0$. For this special case, there is no need to specify the value of $P_{0,n}^*(\bar{E}_n)$.

V. A DDPG APPROACH TO OPTIMIZE \bar{E}_n

A. A Brief Introduction to DDPG

The ultimate goal of DDPG is to determine an action, denoted by a , which can maximize the action-value function, denoted by $Q(s, a)$, for a given state, denoted by s , via the following maximization problem [24]:

$$a^*(s) = \arg \max_a Q(s, a), \quad (14)$$

which is similar to tabular reinforcement learning algorithms, such as Q-learning and state-action-reward-state-action (SARSA) [29]. But unlike Q-learning and SARSA, for DDPG, there is no need to build a table to store the values of $Q(s, a)$. Instead, the action-value function is approximated by using neural networks, which is similar to deep Q networks (DQN). Furthermore, unlike Q-learning, SARSA, and DQN, DDPG is designed for the case when actions are continuous variables.

In particular, the four neural networks used for DDPG are listed in the following [23]:

- An actor network (also termed a policy network), parameterized by ω_μ , takes s as its input and outputs an action which is denoted by $\mu(s|\omega_\mu)$.
- A target actor network, parameterized by ω_{μ_t} , outputs $\mu_t(s|\omega_{\mu_t})$.
- A critic network (also termed a Q network), parameterized by ω_c , takes s and a as its inputs, and outputs the corresponding state-value function, denoted by $Q(s, a|\omega_c)$.

- A target critic network, parameterized by ω_{c_t} , outputs $Q_t(s, a | \omega_{c_t})$.

The key features of DDPG are described in the following.

1) *Exploration*: From the user's perspective, the actor network is the most important component since it provides the desired solution. In order to encourage the algorithm to explore the environment, noise is added to the output of the actor network, which means that the action to be taken for state s is given by [23]

$$a(s) = \mu(s | \omega_\mu) + n, \quad (15)$$

where n denotes the exploration noise.

2) *Updating the networks*: While only the actor network is used to generate the needed action, the other three networks are crucial to make sure that the actor network is properly trained. Assume that there exists a tuple (s, a, r, s_-) , where r is the reward if action a is taken for the current state s and s_- denotes the next state. Based on this tuple, the networks are updated as follows [23]:

- The actor network is trained by maximizing the state-value function, as shown in (14). By using the parameters of the actor and critic networks, the objective function for the maximization problem can be rewritten as $J(\omega_\mu) = Q(s, a = \mu(s | \omega_\mu) | \omega_c)$. Given the fact that the action space is continuous and also assuming that the state-value function is differentiable, the parameters of the actor network, ω_μ , can be updated by carrying out gradient ascent. Note that gradient search requires the derivative of the objective function with respect to ω_μ , where the following chain rule can be used:

$$\nabla_{\omega_\mu} J(\omega_\mu) = \nabla_a Q(s, a | \omega_c) \nabla_{\omega_\mu} \mu(s | \omega_\mu). \quad (16)$$

Therefore, the output of the actor network can be used as the input of the critic network, and the parameters of the actor network (ω_μ) are updated by maximizing the output of the critic network and fixing the parameters of the critic network.

- The critic network plays a crucial role in updating the actor network, as can be seen from (16). The update of the critic network relies on the two target networks. On the one hand, by using the output of the target actor network as an input of the target critic network, a target value for the state-value function is obtained as follows:

$$y = r + \gamma Q_t(s_-, \mu_t(s_- | \omega_{\mu_t}) | \omega_{c_t}), \quad (17)$$

where γ denotes the discount parameter. On the other hand, another estimate for the state-value function can be generated by using the critic network, i.e., $Q(s, a|\omega_c)$. The critic network can be updated by minimizing the loss defined as follows:

$$L = (y - Q(s, a|\omega_c))^2. \quad (18)$$

- The two target networks have the same structure as their counterparts and their parameters are updated as follows:

$$\omega_{c_t} \rightarrow \tau\omega_c + (1 - \tau)\omega_{c_t}, \quad \omega_{\mu_t} \rightarrow \tau\omega_\mu + (1 - \tau)\omega_{\mu_t}, \quad (19)$$

where τ is the soft updating parameter. We note that the two target networks are updated with a much lower frequency than their counterparts.

3) *Replay Buffer*: Similar to DQN, for DDPG, the past experience, i.e., multiple tuples from the past, $(s_i, a_i, r_i, s_{i,-})$, are stored in a pool, termed the replay buffer. When the networks are updated, a fixed number of the tuples are randomly selected from the buffer and used for network updating, which means that both (16) and (18) are carried out in a batch mode.

B. Application of DDPG to CR-NOMA

By using the closed-form expression for $\alpha^*(\bar{E}_n)$ developed in Lemma 1 and $P_{0,n}^*(\bar{E}_n)$ shown in (13), the long-term throughput maximization problem can be rewritten as follows:

$$\max_{\bar{E}_n} \sum_{n=1}^{\infty} \gamma^{n-1} \alpha^*(\bar{E}_n) \ln \left(1 + \frac{P_{0,n}^*(\bar{E}_n)|h_0|^2}{1 + P_n|h_n|^2} \right) \quad (\text{P9a})$$

$$\text{s.t.} \quad E_{n+1} = \min \{E_{\max}, E_n + \bar{E}_n\}. \quad (\text{P9b})$$

Because problem P9 is a function of a single continuous variable, \bar{E}_n , it is ideally suited for the application of DDPG. The key step for the application of reinforcement learning is to define the state space, the action space, and the reward, as discussed in the following.

1) *State space*: For the considered long-term system throughput maximization problem, we define the state as the following tuple:

$$s_n = \begin{bmatrix} |h_n|^2 & |h_{n,0}|^2 & E_n \end{bmatrix}^T, \quad (20)$$

where $[\cdot]^T$ denotes a transpose operation. We note that s_n includes the channel gains associated with the primary user served at t_n , the secondary user's channel to the base station, and the energy available at the beginning of t_n .

2) *Action Space*: It is natural to use \bar{E}_n as the action. For example, if both $|h_n|^2$ and $|h_{n,0}|^2$ are extremely strong, a good choice for the action is $\bar{E}_n \geq 0$, such that data transmission is avoided due to the strong interference caused by U_n , and to spend more time for energy harvesting due to the strong connection between U_n and U_0 .

However, it is important to point out that the range of \bar{E}_n can be quite large. In particular, as shown in the proof of Proposition 1, the value of \bar{E}_n is bounded by the two following extreme situations:

$$\underbrace{-\min\{E_n, TP_{\max}\}}_{\text{No energy harvesting}} \leq \bar{E}_n \leq \underbrace{\min\{E_{\max} - E_n, T\eta P_n |h_{n,0}|^2\}}_{\text{No data transmission}}, \quad (21)$$

which can be a very large negative number and a very large positive number, respectively. Note that, compared to the existing work in [8], where only $-E_n$ is used as the lower bound on \bar{E}_n , we also include $-TP_{\max}$ in the lower bound. This is due to the transmit power constraint $P_{0,n} \leq P_{\max}$, which means that the maximal energy consumed within T seconds is TP_{\max} , if there is sufficient energy available at the beginning of t_n , i.e., $E_n > TP_{\max}$.

In order to improve the stability of the used neural networks, it is preferable to constrain the possible choices of the action within a small and fixed range, ideally between 0 and 1. By using the upper and lower bounds on \bar{E}_n and introducing an auxiliary variable β_n , $0 \leq \beta_n \leq 1$, \bar{E}_n can be expressed as follows:

$$\bar{E}_n = \beta_n \min\{E_{\max} - E_n, T\eta P_n |h_{n,0}|^2\} - (1 - \beta_n) \min\{E_n, TP_{\max}\}. \quad (22)$$

It is straightforward to verify that the lower bound in (21) is used if $\beta_n = 0$, and the upper bound can be realized by letting $\beta_n = 1$. Therefore, β is a suitable action variable for DDPG networks.

3) *Reward*: Because the objective function of the optimization problem in P9 is based on the secondary user's long-term data rate, it is natural to use R_n as the reward at t_n .

By using the defined state space, action space, and reward, DDPG can be applied straightforwardly. In particular, each episode consists of multiple steps/iterations. During each step, the DDPG algorithm first generates an action according to the current state, finds the next state according to the chosen action, and then the DDPG agent starts learning by updating the four neural networks as discussed in the previous subsection. The details for the DDPG implementation of DDPG can be found in [30].

VI. SIMULATION RESULTS

In this section, we study the performance of the proposed DDPG assisted NOMA transmission strategy by using computer simulation results. In our simulations, the learning rates for the actor and critic networks are set as 0.002 and 0.004, respectively. The reward discount parameter is $\gamma = 0.9$, the network updating parameter is $\tau = 0.01$, and the batch size for the replay experience is 32. The base station is located at the origin of the x-y plane, and the secondary user is located at (1 m, 1 m). The primary users' transmit power is set as $P_n = 30$ dBm, the initial energy in the battery is $E_{\max} = 0.1$ J, $T = 1$ s, $P_{\max} = 0.1$ W, and the energy harvesting efficiency coefficient is set as $\eta = 0.7$. The additive white Gaussian noise power spectral density is -170 dBm/Hz, the total bandwidth is 1 MHz, the carrier frequency is 914 MHz, the path loss model in [31] is used, and the path loss exponent is 3.

Regarding the neural networks, a simple neural network which consists of 2 hidden layers with 64 nodes each is used for the actor network, where the rectified linear activation function (ReLU) is used in the first hidden layer, and the hyperbolic tangent function is used for the second hidden layer and the output layer. Since the critic network takes two inputs, s and a , both s and a are fed to two individual hidden layers with 64 nodes each before they are concatenated and connected to another hidden layer with 64 nodes. ReLU is used in all the layers of the critic network. The two target networks are built in the same manner as their counterparts. The detailed setups for the four employed neural networks can be found in [30].

The concepts of steps, episodes, and experiments for DDPG can be interpreted in the considered CR-NOMA context as follows. Each step represents a time slot, each episode consists of 100 time slots (or steps), and each experiment consists of multiple episodes. During each experiment, the users' channels are kept constant, and at the beginning of each experiment, the neural networks are randomly initialized. At the beginning of each episode, the secondary user's battery is reset to E_{\max} .

A. A Two-User Deterministic Case

In order to gain insight into the performance of DDPG, we first focus on a deterministic case with two primary users, where the two primary users are located at (0 m, 1 m) and (0 m, 1000 m), only large scale path loss is considered, and random fading is omitted. The rationale behind this setting is the study of an extreme scenario, in which U_1 has a strong channel to both the base station and U_0 , but U_2 's channels to both nodes are extremely weak. An intuitive decision

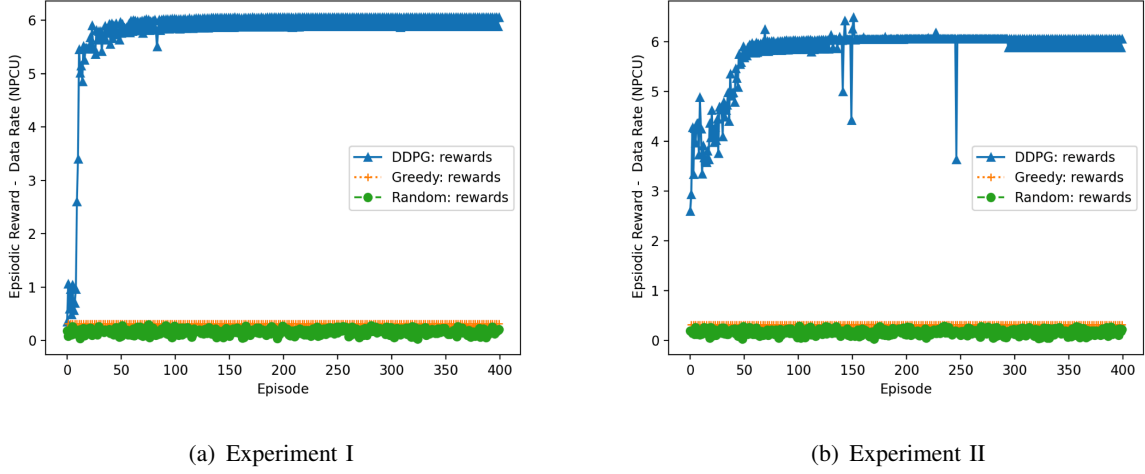


Fig. 2. A deterministic extreme case with $M = 2$ primary users. The two primary users are located at (0 m, 1 m) and (0 m, 1000 m). Only large scale path loss is considered and random fading is omitted. The difference between two experiments is caused by the fact that the neural networks are randomly initialized at the begging of each experiment.

for this case is to ask U_0 to carry out energy harvesting only, when U_1 transmits, which has the following two benefits: severe interference from U_1 is avoided and a large amount of energy from U_1 is harvested. When U_2 transmits, an intuitive decision is to avoid energy harvesting at U_0 since only a small amount of energy can be harvested due to the severe path loss between U_0 and U_2 . Instead, U_0 should carry out data transmission only, since U_2 will not cause much interference. With this intuitive decision, the amount of energy harvested when U_1 transmits is given by [31]

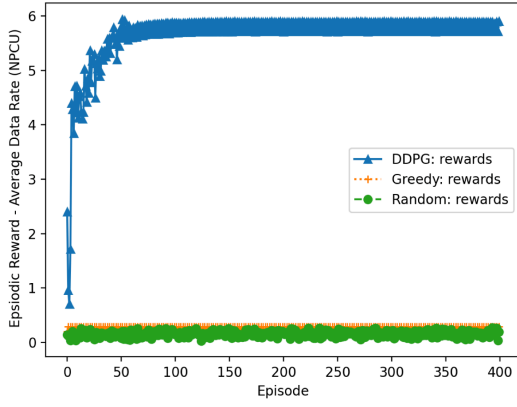
$$E = (1 - \alpha_n) T \eta P_n |h_{n,0}|^2 = 0.7/10^{3.17} \text{ J} = 7 * 10^{-4.17} \text{ J} \approx 4.7 * 10^{-4} \text{ J}. \quad (23)$$

When U_2 transmits, the entire time slot is used for data transmission using the harvested energy shown in (23). Therefore, the available transmit power is $\frac{E}{T} = 4.7 * 10^{-4} \text{ W}$, which means that the following average data rate, denoted by \bar{R}_n , is achievable by the secondary user:

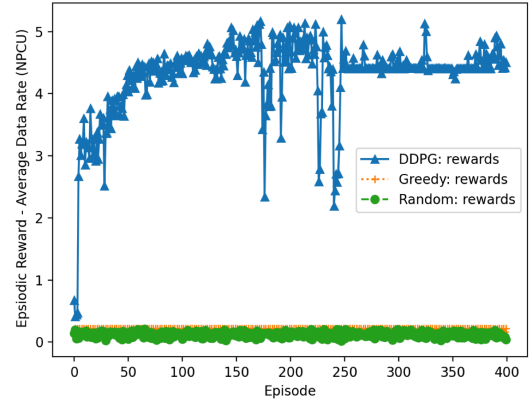
$$\bar{R}_n = \frac{1}{2} \alpha_n \ln \left(1 + \frac{P_{0,n} |h_0|^2}{1 + P_n |h_n|^2} \right) \quad (24)$$

$$= \frac{1}{2} \ln \left(1 + \frac{4.7 * 10^{-4} \times \frac{1}{10^{3.17} * 2^{\frac{3}{2}}}}{10^{-14} + 10^{-3.17} \times 1000^{-3}} \right) \approx 6.01 \text{ NPCU}, \quad (25)$$

where the factor $\frac{1}{2}$ is used since U_0 transmits only when U_2 transmits. Comparing the result in (25) with Fig. 2, one can observe that the proposed reinforcement learning scheme realizes this intuitive decision. We note that DDPG might perform slightly differently for different random initializations, as shown in Figs. 2(a) and 2(b). On the other hand, the benchmark schemes yields much worse performances than the proposed scheme, since the decisions they make are



(a) Experiment I



(b) Experiment II

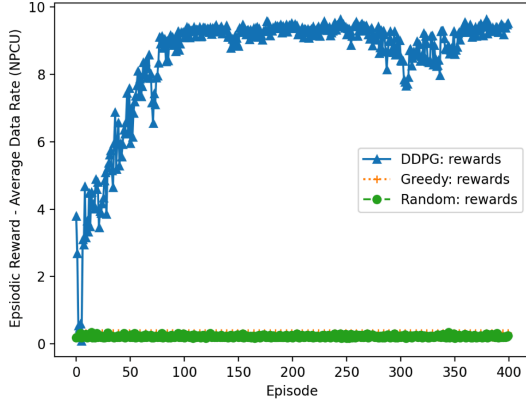
Fig. 3. The performance of the proposed DDPG scheme with $M = 2$ primary users. Both large scale path loss and small-scale multi-path fading are considered. The two experiments are based on different small-scale fading realizations.

not based on a long-term objective. For example, when U_1 transmits, the greedy algorithm will still try to facilitate data transmission, which results in an inefficient energy use due to the strong interference caused by U_1 .

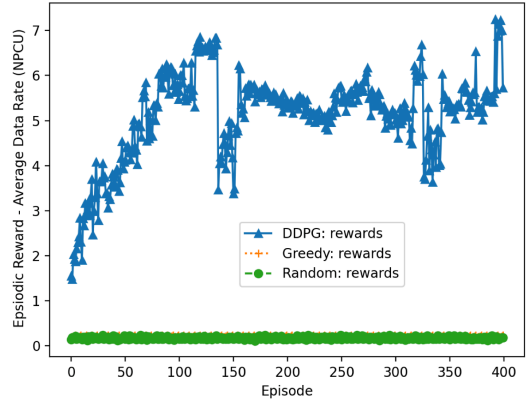
B. General Multi-User Cases with Random Fading

In this subsection, the performance of the proposed reinforcement learning scheme is studied for a more general case with multiple users and random small-scale fading. In particular, the M users are equally spaced on a segment between (1 m, 0 m) and (1000 m, 0 m). Independent identically distributed (i.i.d.) complex Gaussian random variables with zero mean and unit variance are used to simulate the small-scale channel fading.

In Figs. 3, 4, and 5, $M = 2$, $M = 5$, and $M = 10$ primary users are considered, respectively. On the one hand, comparing Fig. 3 to Fig. 2, a data rate reduction can be observed, which is due to the consideration of channel fading. On the other hand, comparing Figs. 4(a) and 5(a) to Fig. 3, it is interesting to observe that the cases with $M = 5$ and $M = 10$ can yield larger data rates than the case with $M = 2$. This is due to the fact that for $M > 2$, it is possible for the secondary user to use more than half of the time for data transmission. As can be observed by comparing the respective subfigures of Fig. 3, 4, and 5, different data rates are realized for a given M , which is due to the fact that the subfigures employ different realizations of the small-scale fading. However, regardless of the realizations of the random fading, the proposed DDPG scheme can always achieve a considerably larger data rate than the two benchmark schemes, as is evident from the figures.

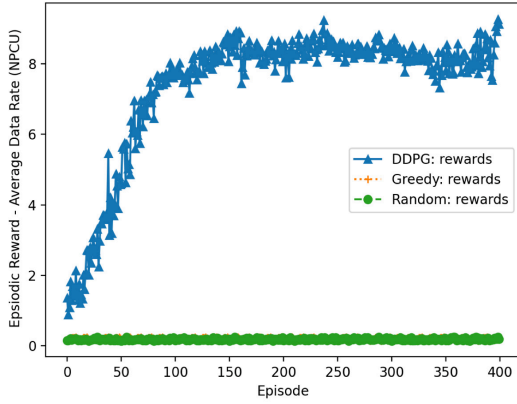


(a) Experiment I

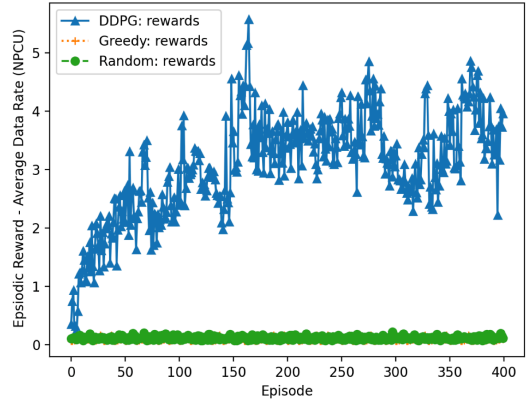


(b) Experiment II

Fig. 4. The performance of the proposed DDPG scheme with $M = 5$ primary users. Both large scale path loss and small-scale multi-path fading are considered. The two experiments are based on different small-scale fading realizations.



(a) Experiment I



(b) Experiment II

Fig. 5. The performance of the proposed DDPG scheme with $M = 10$ primary users. Both large scale path loss and small-scale multi-path fading are considered. The two experiments are based on different small-scale fading realizations.

Recall that for the deterministic case with $M = 2$ considered in Fig. 2, the decision generated by the proposed DDPG scheme converges quickly, e.g., after 50 episodes, the DDPG curves shown in Fig. 2 become almost flat. This property disappears in general for the cases with random fading. In particular, depending on the random fading realization, the DDPG agent might lead to a constant decision policy after a sufficiently large number of episodes, as shown in Figs. 3(a), 4(a), and 5(a). However, Figs. 3(b), 4(b), and 5(b) also show that for certain random fading realizations, the DDPG algorithm may converge very slowly. One possible reason for this observation is that for the two-user deterministic case considered in Fig. 2, the underlying pattern is simple, e.g., one user has strong channels but the other user does not. This simple pattern can be quickly and efficiently learned by DDPG. When there are more users packed in the same area

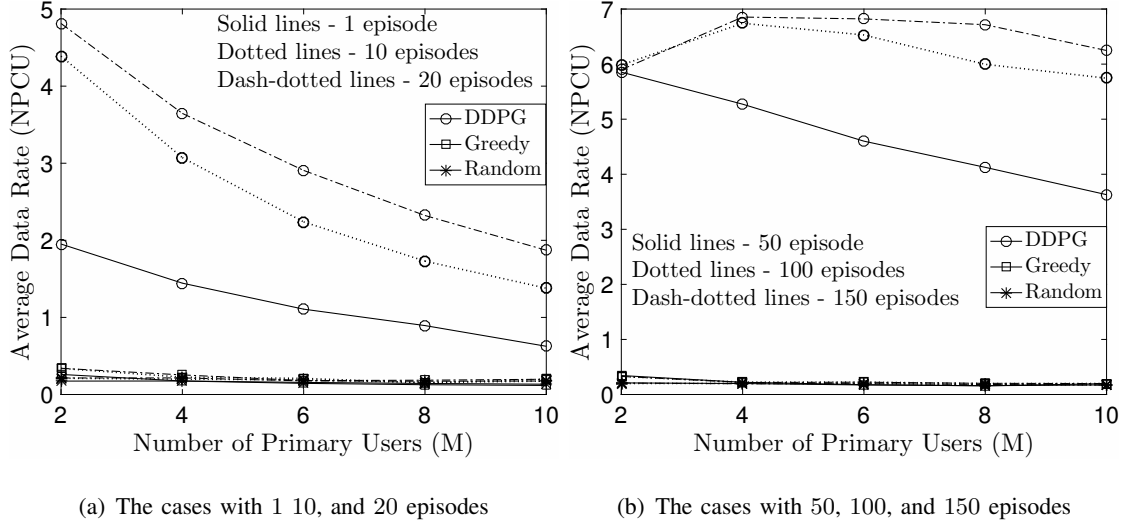


Fig. 6. Impact of M and the number of the used episodes on the performance of the proposed DDPG scheme.

and/or the fading is random, it is possible that such a clear pattern does not exist, i.e., multiple users' channel conditions are similar to each other. As a result, there is no clear strategy for energy harvesting and data transmission.

Finally, in Fig. 6, the performances of the considered three schemes are compared by using the average data rate as the metric, where Monte Carlo simulations are carried out to average out the randomness caused by random fading. In Fig. 6(a), three choices for the number of employed episodes are used, in order to illustrate how the performance of the DDPG scheme is affected by the number of episodes. As can be observed from Fig. 6(a), even for a single episode, the proposed DDPG algorithm can already realize a larger data rate than the greedy and random schemes. By increasing the number of episodes from 1 to 10 or 20, the performance gain of the proposed DDPG algorithm over the benchmark schemes can be further improved, as shown in Fig. 6(a). Recall that we observe from Figs. 3 - 5 that the proposed DDPG algorithm starts to converge after 100 episodes. This is the reason why increasing the number of episodes in Fig. 6(b) from 100 to 150 improves the performance of the proposed DDPG scheme only slightly. Another important observation from Fig. 6 is that, with a small number of episodes, inviting more primary users to participate in the NOMA transmission decreases the performance gain of DDPG compared to the two benchmark schemes; however, this performance loss can be mitigated by using more episodes, as can be observed from Fig. 6.

VII. CONCLUSIONS

In this paper, machine learning was applied in CR-NOMA networks to facilitate spectrum and energy cooperation between multiple primary users and an energy-constrained secondary

user. The goal of the machine learning algorithm is to maximize the secondary user's long-term throughput, which is challenging due to the need for making decisions which yield long-term gains but might result in short-term losses. For example, when, in a given time slot, a primary user with large channel gains transmits, an intuitive approach is that the secondary user should not carry out data transmission but perform energy harvesting only, which results in zero data rate for this time slot but yields benefits in the long-term. Here, the considered long-term throughput maximization problem was first reformulated, and then a deep reinforcement learning approach, termed DDPG, was applied to emulate the intuitive solution. The provided simulation results demonstrate that the proposed deep reinforcement learning assisted NOMA transmission scheme can yield significant performance gains over two benchmark schemes.

APPENDIX A

PROOF FOR PROPOSITION 1

In order to analyze the feasibility of problem P8, the range of \bar{E}_n needs to be studied first. Recall that \bar{E}_n is the difference between the energy harvested and consumed at t_n , i.e., $(1 - \alpha_n)T\eta P_n|h_{n,0}|^2 - \alpha_n TP_{0,n}$. The smallest value achievable by \bar{E}_n is caused by the case with no energy harvesting, i.e., all the time is used for data transmission and $\alpha_n = 1$, which means that

$$\bar{E}_n \geq -TP_{0,n}. \quad (26)$$

Furthermore, the energy available at the beginning of t_n is E_n , which means that the energy available for data transmission is capped by E_n , which results in another lower bound on \bar{E}_n , i.e., $\bar{E}_n \geq -E_n$. As a result, \bar{E}_n can be lower bounded as follows:

$$\bar{E}_n \geq -\min\{E_n, TP_{\max}\}, \quad (27)$$

where we replaced $P_{0,n}$ by P_{\max} in (26). On the other hand, the largest value achievable by \bar{E}_n is caused by the decision not to carry out any data transmission but perform energy harvesting only, i.e., $\alpha_n = 0$. In this case, an upper bound on \bar{E}_n can be obtained as follows:

$$\bar{E}_n \leq T\eta P_n|h_{n,0}|^2. \quad (28)$$

Moreover, there is an upper bound on the amount of energy stored at t_n because of the finite battery capacity. In particular, given the capacity of the battery, E_{\max} , and the energy available

in the battery at the beginning of t_n , E_n , the maximal amount of new energy that can be stored at t_n is capped by $E_{\max} - E_n$. As a result, \bar{E}_n is upper bounded as follows:

$$\bar{E}_n \leq \min \{E_{\max} - E_n, T\eta P_n |h_{n,0}|^2\}. \quad (29)$$

By combining (27) and (29), \bar{E}_n can be bounded as follows:

$$-\min\{E_n, TP_{\max}\} \leq \bar{E}_n \leq \min \{E_{\max} - E_n, T\eta P_n |h_{n,0}|^2\}. \quad (30)$$

The feasibility of problem P8 is illustrated in the following two steps. The first step is to show that the lower bounds on α_n for problem P8 do not conflict with the upper bounds. The second step is to show that the intersection of the set defined by the constraints of problem P8 and the domain of its objective function is non-empty.

Note that there are three lower bounds defined by (P8c), (P8d), and (P8e), respectively. Firstly, we focus on the lower bound $\alpha_n \geq 0$ in (P8e). Apparently, it does not conflict with the upper bound in (P8e), i.e., $\alpha_n \leq 1$. In order to compare this lower bound to the upper bound in (P8b), $\alpha_n \leq 1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}$, we first rewrite the upper bound in (30) as follows:

$$\bar{E}_n \leq \min \{E_{\max} - E_n, T\eta P_n |h_{n,0}|^2\} \leq T\eta P_n |h_{n,0}|^2. \quad (31)$$

Therefore, $1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2} \geq 0$, and hence one can conclude that the lower bound $\alpha_n \geq 0$ does not conflict with the upper bound in (P8b).

Secondly, we focus on the lower bound in (P8c), $\alpha_n \geq 1 - \frac{E_n + \bar{E}_n}{T\eta P_n |h_{n,0}|^2}$. To prove that it does not conflict with the upper bound in (P8e), $\alpha_n \leq 1$, it is sufficient to show the following

$$1 - \frac{E_n + \bar{E}_n}{T\eta P_n |h_{n,0}|^2} \leq 1, \quad (32)$$

which requires $\bar{E}_n \geq -E_n$. This always holds because the use of the lower bound in (30) yields $\bar{E}_n \geq -\min\{E_n, TP_{\max}\}$ or equivalently $\bar{E}_n \geq \max\{-E_n, -TP_{\max}\} \geq -E_n$. In addition, it is straightforward to show that the lower bound in (P8c) is always smaller than the upper bound in (P8b) by using the fact that $E_n \geq 0$.

Thirdly, we focus on the lower bound in (P8d), $\alpha_n \geq \frac{T\eta P_n |h_{n,0}|^2 - \bar{E}_n}{T\eta P_n |h_{n,0}|^2 + TP_{\max}}$. To prove that it does not conflict with the upper bound in (P8e), it is sufficient to show the following

$$\frac{T\eta P_n |h_{n,0}|^2 - \bar{E}_n}{T\eta P_n |h_{n,0}|^2 + TP_{\max}} \leq 1, \quad (33)$$

which requires $\bar{E}_n \geq -TP_{\max}$. This also always holds because the use of the bound in (30) yields $\bar{E}_n \geq \max\{-E_n, -TP_{\max}\} \geq -TP_{\max}$. In order to show that the lower bound in (P8d) is always smaller than the upper bound in (P8b), we need to prove the following inequality

$$\frac{T\eta P_n |h_{n,0}|^2 - \bar{E}_n}{T\eta P_n |h_{n,0}|^2 + TP_{\max}} \leq 1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}, \quad (34)$$

which can be simplified as follows:

$$\bar{E}_n \leq T\eta P_n |h_{n,0}|^2. \quad (35)$$

This inequality always holds since $\bar{E}_n \leq \min\{E_{\max} - E_n, T\eta P_n |h_{n,0}|^2\} \leq T\eta P_n |h_{n,0}|^2$ based on (30). In summary, the constraints of problem (P8) do not conflict with each other, and the set defined by these constraints is not empty.

The last step to analyse the feasibility of problem P8 is to show that the intersection of the domain of the objective function of problem P8 and the set defined by the constraints is not empty. Recall that the domain of the objective function (P8a) imposes the following constraint on α_n :

$$1 + \frac{(1 - \alpha_n) \eta P_n |h_{n,0}|^2 |h_0|^2}{\alpha_n (1 + P_n |h_n|^2)} - \frac{1}{\alpha_n} \frac{\bar{E}_n |h_0|^2}{T(1 + P_n |h_n|^2)} \geq 0. \quad (36)$$

As can be shown, the constraint imposed on α_n by problem P8 is stricter than (36). In particular, one can convert the following inequality

$$\frac{(1 - \alpha_n) \eta P_n |h_{n,0}|^2 |h_0|^2}{\alpha_n (1 + P_n |h_n|^2)} - \frac{1}{\alpha_n} \frac{\bar{E}_n |h_0|^2}{T(1 + P_n |h_n|^2)} \geq 0, \quad (37)$$

into the following equivalent form:

$$(1 - \alpha_n) T \eta P_n |h_{n,0}|^2 - \bar{E}_n \geq 0. \quad (38)$$

With some algebraic manipulations, one can find that the inequality constraint in (38) is equivalent to constraint (P8b). In other words, the intersection of the set defined by the constraints of problem P8 and the domain of its objective function is non-empty. As a result, problem (P8) is always feasible, and the proposition is proved.

APPENDIX B

PROOF FOR PROPOSITION 2

Recall that the objective function of problem P8 can be expressed as follows:

$$\tilde{f}_0^*(\alpha_n) = \alpha_n \ln \left(1 + \frac{(1 - \alpha_n) \eta P_n |h_{n,0}|^2 |h_0|^2}{\alpha_n (1 + P_n |h_n|^2)} - \frac{1}{\alpha_n} \frac{\bar{E}_n |h_0|^2}{T(1 + P_n |h_n|^2)} \right). \quad (39)$$

By using (38) and the fact that $T\eta P_n|h_{n,0}|^2 \geq \bar{E}_n$, it can be shown that $\alpha_n = 0$ is in the domain of $\tilde{f}_0^*(\alpha_n)$.

To simplify notations, we define $\kappa_1 = \frac{\eta P_n|h_{n,0}|^2|h_0|^2}{1+P_n|h_n|^2}$, $\kappa_2 = \frac{\bar{E}_n|h_0|^2}{T(1+P_n|h_n|^2)}$, and $x = \alpha_n$. Therefore, the objective function $\tilde{f}_0^*(x)$ can be expressed as follows:

$$\begin{aligned}\tilde{f}_0^*(x) &= x \ln \left(1 + \frac{1-x}{x} \kappa_1 - \frac{1}{x} \kappa_2 \right) \\ &= x \ln \left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x} \right).\end{aligned}\quad (40)$$

As discussed in the proof of Proposition 1, the term $1 + \frac{1-x}{x} \kappa_1 - \frac{1}{x} \kappa_2$ is strictly positive once all the constraints in problem P8 are satisfied. Furthermore, as discussed in Remark 5, it is assumed that $\bar{E}_n \neq T\eta P_n|h_{n,0}|^2$. Therefore, the first order derivative of $\tilde{f}_0^*(x)$ is given by

$$\begin{aligned}\frac{d\tilde{f}_0^*(x)}{dx} &= \ln \left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x} \right) - \frac{\frac{\kappa_1 - \kappa_2}{x}}{1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x}} \\ &= \ln \left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x} \right) - \frac{(\kappa_1 - \kappa_2)}{x(1 - \kappa_1) + \kappa_1 - \kappa_2}.\end{aligned}\quad (41)$$

The second order derivative of $\tilde{f}_0^*(x)$ is given by

$$\frac{d^2\tilde{f}_0^*(x)}{dx^2} = -\frac{(\kappa_1 - \kappa_2)}{x(x(1 - \kappa_1) + \kappa_1 - \kappa_2)} + \frac{(1 - \kappa_1)(\kappa_1 - \kappa_2)}{(x(1 - \kappa_1) + \kappa_1 - \kappa_2)^2}.\quad (42)$$

With some algebraic manipulations, the second order derivative can be expressed as follows:

$$\frac{d^2\tilde{f}_0^*(x)}{dx^2} = \frac{-(\kappa_1 - \kappa_2)^2}{(x(1 - \kappa_1) + \kappa_1 - \kappa_2)^2 x} \leq 0,\quad (43)$$

for $x \geq 0$. Therefore, the objective function is a concave function for $\alpha_n \geq 0$ and the proof is complete.

APPENDIX C

PROOF FOR LEMMA 1

Problem P8 can be expressed in the following compact form

$$\max_{\alpha_n} \quad \alpha_n \ln \left(1 + \frac{(1 - \alpha_n)}{\alpha_n} \kappa_1 - \frac{1}{\alpha_n} \kappa_2 \right) \quad (\text{P10a})$$

$$\text{s.t.} \quad \alpha_n \leq \min \left\{ 1, 1 - \frac{\bar{E}_n}{T\eta P_n|h_{n,0}|^2} \right\} \quad (\text{P10b})$$

$$\alpha_n \geq \max \left\{ 0, 1 - \frac{E_n + \bar{E}_n}{T\eta P_n|h_{n,0}|^2}, \frac{T\eta P_n|h_{n,0}|^2 - \bar{E}_n}{T\eta P_n|h_{n,0}|^2 + TP_{\max}} \right\}. \quad (\text{P10c})$$

Denote x^* as the optimal solution of the maximization problem $\max_{x \geq 0} \tilde{f}_0^*(x)$. As indicated by Proposition 2, $\tilde{f}_0^*(x)$ is a concave function of x for $x \geq 0$, and hence there exists a single maximum, i.e., x^* . However, because x^* is obtained by discarding the constraints, (P10b) and (P10c), it is possible that x^* is not a feasible solution of problem P10.

Therefore, the lemma is proved in the following three steps. In the first step, we analyze the properties of $\tilde{f}_0^*(x)$ at the boundary values given by (P10b) and (P10c). In the second step, a closed-form expression for x^* is developed, where the conclusion about the comparison between x^* and one of the boundary values, $1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}$, is crucial to avoid the ambiguity caused by the two branches of the Lambert W function. In the third step, a closed-form solution for problem P10 is obtained by using the obtained closed-form x^* .

1) Analysis of the properties of $\tilde{f}_0^(x)$:* The aim of this subsection is to show that $\tilde{f}_0^*(x)$ is non-decreasing at $x = 0$ and non-increasing at $1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}$, the boundary values shown in (P10b) and (P10c), which can be proved by showing the following

$$f'(0) \geq 0 \quad \& \quad f'\left(1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}\right) \leq 0, \quad (44)$$

where $f'(x) \triangleq \frac{d\tilde{f}_0^*(x)}{dx}$ denotes the first order derivative of $\tilde{f}_0^*(x)$. We note that (44) requires the implicit assumption that both 0 and $1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}$ are in the domain of the objective function, which can be easily shown by using (38).

In order to show $f'(0) \geq 0$, assume $x = \epsilon \rightarrow 0$. Thus, by using (41), $f'(\epsilon)$ can be expressed as follows:

$$\begin{aligned} f'(\epsilon) &= \ln\left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{\epsilon}\right) - \frac{(\kappa_1 - \kappa_2)}{\epsilon(1 - \kappa_1) + \kappa_1 - \kappa_2} \\ &\xrightarrow{\epsilon \rightarrow 0} \ln\left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{\epsilon}\right) - 1. \end{aligned} \quad (45)$$

Note that $\kappa_1 - \kappa_2 \geq 0$, which can be proved as follows:

$$\begin{aligned} \kappa_1 - \kappa_2 &= \frac{\eta P_n |h_{n,0}|^2 |h_0|^2}{1 + P_n |h_n|^2} - \frac{\bar{E}_n |h_0|^2}{T(1 + P_n |h_n|^2)} \\ &= \frac{(T\eta P_n |h_{n,0}|^2 - \bar{E}_n) |h_0|^2}{T(1 + P_n |h_n|^2)} \geq 0, \end{aligned} \quad (46)$$

which is due to the fact that $\bar{E}_n \leq T\eta P_n |h_{n,0}|^2$ as shown in (30). As a result, $\frac{\kappa_1 - \kappa_2}{\epsilon}$ approaches positive infinity for $\epsilon \rightarrow 0$, where the trivial case $\bar{E}_n = T\eta P_n |h_{n,0}|^2$ is not considered as discussed in Remark 5. Therefore, for $\epsilon \rightarrow 0$, $f'(\epsilon)$ can be approximated as follows:

$$f'(\epsilon) \xrightarrow{\epsilon \rightarrow 0} \ln\left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{\epsilon}\right) - 1 \geq 0. \quad (47)$$

In order to show $f' \left(1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2} \right) \leq 0$, define $\theta_1 = 1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}$ for simplicity of notation. The first order derivative $f'(\theta_1)$ is given by:

$$f'(\theta_1) = \ln \left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{\theta_1} \right) - \frac{(\kappa_1 - \kappa_2)}{\theta_1(1 - \kappa_1) + \kappa_1 - \kappa_2}. \quad (48)$$

The following identity holds:

$$\frac{\kappa_1 - \kappa_2}{\theta_1} = \frac{(T\eta P_n |h_{n,0}|^2 - \bar{E}_n) |h_0|^2}{T(1 + P_n |h_n|^2)} \frac{T\eta P_n |h_{n,0}|^2}{T\eta P_n |h_{n,0}|^2 - \bar{E}_n} = \frac{\eta P_n |h_{n,0}|^2 |h_0|^2}{(1 + P_n |h_n|^2)} = \kappa_1,$$

which means

$$f'(\theta_1) = -\frac{(\kappa_1 - \kappa_2)}{\theta_1(1 - \kappa_1) + \kappa_1 - \kappa_2}. \quad (49)$$

$f'(\theta_1)$ can be further rewritten as follows:

$$f'(\theta_1) = -\frac{\frac{(\kappa_1 - \kappa_2)}{\theta_1}}{(1 - \kappa_1) + \frac{\kappa_1 - \kappa_2}{\theta_1}} = -\frac{\kappa_1}{(1 - \kappa_1) + \kappa_1} = -\kappa_1 \leq 0, \quad (50)$$

since κ_1 is non-negative. Therefore, the inequality in (44) is proved.

By using the concavity of the objective function and also (44), it is straightforward to show that x^* is bounded as follows:

$$0 \leq x^* \leq \theta_1. \quad (51)$$

The bounds in (51) will be useful to solve an ambiguity issue caused by the Lambert W function, as shown in the following subsection.

2) *Finding a closed-form expression for x^** : The fact that the objective function $\tilde{f}_0^*(x)$ is concave means that x^* is the root of the following equation:

$$\ln \left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x^*} \right) - \frac{(\kappa_1 - \kappa_2)}{x^*(1 - \kappa_1) + \kappa_1 - \kappa_2} = 0, \quad (52)$$

which can be rewritten as follows:

$$\ln \left(1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x^*} \right) - \frac{\frac{(\kappa_1 - \kappa_2)}{x^*}}{(1 - \kappa_1) + \frac{\kappa_1 - \kappa_2}{x^*}} = 0. \quad (53)$$

Define $y^* = 1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x^*}$, which leads to:

$$\ln(y^*) - \frac{(y^* - 1 + \kappa_1)}{y^*} = 0, \quad (54)$$

or equivalently

$$y^* \ln(y^*) - y^* = \kappa_1 - 1. \quad (55)$$

In order to apply the the Lambert W function, define $y^* = e^{z^*}$, which results in the following equation:

$$z^* e^{z^*} - e^{z^*} = \kappa_1 - 1 \quad (56)$$

or equivalently

$$(z^* - 1)e^{z^*-1} = e^{-1}(\kappa_1 - 1). \quad (57)$$

The form of (57) makes the application of the Lambert W function possible. Recall that there is a single real-valued solution for the equation $we^w = z$, if $z \geq 0$, which is given by $w = W_0(z)$, i.e., the principal branch of the Lambert W function. However, if z is negative, there are two real-valued solutions, denoted by $w = W_0(z)$ and $w = W_{-1}(z)$, respectively.

For the considered problem, $\kappa_1 - 1$ is not always positive since

$$\kappa_1 - 1 = \frac{\eta P_n |h_{n,0}|^2 |h_0|^2}{1 + P_n |h_n|^2} - 1 \quad (58)$$

can be negative if $|h_n|^2$ is much larger than $|h_{n,0}|^2$. As a result, for the case $\kappa_1 - 1 < 0$, there are two real-valued solutions corresponding to the two branches of the Lambert W function as follows:

$$z^* - 1 = W_0(e^{-1}(\kappa_1 - 1)), \quad (59)$$

$$z^* - 1 = W_{-1}(e^{-1}(\kappa_1 - 1)). \quad (60)$$

With the two possible choices for z^* , there will be also two choices for x^* , which makes the final expression of $\alpha^*(\bar{E})_n$ very complicated. Fortunately, the solution corresponding to $z^* - 1 = W_{-1}(e^{-1}(\kappa_1 - 1))$ can be discarded, as proved in the following.

In the following, assume $\kappa_1 - 1 < 0$, and proof by contradiction will be used to show that $z^* - 1 = W_{-1}(e^{-1}(\kappa_1 - 1))$ is not a feasible solution. Note that, according to (58), $\frac{\eta P_n |h_{n,0}|^2 |h_0|^2}{1 + P_n |h_n|^2}$ is strictly positive, and hence $\kappa_1 - 1$ is strictly larger than -1 , i.e. $-1 < \kappa_1 - 1 < 0$. According to the property of the Lambert W function, $w = W_{-1}(z) < -1$, for $-1 < z < 0$. Therefore, $z^* - 1 = W_{-1}(e^{-1}(\kappa_1 - 1)) < -1$, which means

$$z^* < 0 \implies y^* = e^{z^*} < 1. \quad (61)$$

By using the relationship between y^* and x^* , x^* needs to satisfy the following inequality:

$$1 - \kappa_1 + \frac{\kappa_1 - \kappa_2}{x^*} < 1 \implies \kappa_1(1 - x^*) < \kappa_2, \quad (62)$$

where the fact that $x^* \geq 0$ is used. By substituting the expressions of κ_1 and κ_2 into the above inequality, x^* needs to satisfy the following inequality:

$$\frac{\eta P_n |h_{n,0}|^2 |h_0|^2}{1 + P_n |h_n|^2} (1 - x^*) < \frac{\bar{E}_n |h_0|^2}{T(1 + P_n |h_n|^2)}, \quad (63)$$

which can be further rewritten as follows:

$$T\eta P_n |h_{n,0}|^2 (1 - x^*) < \bar{E}_n. \quad (64)$$

In the following, we show that the condition in (64) cannot be met. According to our previous analysis, $f'(\theta_1) \leq 0$, which implies the following:

$$x^* \leq \theta_1 \triangleq 1 - \frac{\bar{E}_n}{T\eta P_n |h_{n,0}|^2}. \quad (65)$$

With some algebraic manipulations, the inequality that x^* needs to satisfy can be expressed as follows:

$$(1 - x^*) T\eta P_n |h_{n,0}|^2 \geq \bar{E}_n, \quad (66)$$

which contradicts the condition in (64). Therefore, the solution $z^* - 1 = W_{-1}(e^{-1}(\kappa_1 - 1))$ can be discarded, and $z^* - 1 = W_0(e^{-1}(\kappa_1 - 1))$ is the solution which should be used.

Therefore, with $z^* - 1 = W_0(e^{-1}(\kappa_1 - 1))$, y^* can be written as follows:

$$y^* = e^{z^*} = e^{W_0(e^{-1}(\kappa_1 - 1)) + 1}, \quad (67)$$

which means that a closed-form expression for x^* is obtained as follows:

$$x^* = \frac{\kappa_1 - \kappa_2}{e^{W_0(e^{-1}(\kappa_1 - 1)) + 1} - 1 + \kappa_1}. \quad (68)$$

3) *Finding the optimal solution for problem P10:* Although x^* yields the maximal value for the objective function, x^* is not necessarily the optimal solution of problem P10, since x^* might violate one of the constraints of problem P10. To facilitate the discussions, the constraints of problem P10 are rewritten as follows:

$$\max\{0, \theta_0\} \leq \alpha_n \leq \min\{1, \theta_1\}, \quad (69)$$

which defines the feasible set of α_n , where θ_0 is defined in Lemma 1. While the relationship between 0 , θ_1 and x^* is fixed as shown in (51), the relationship between x^* , 1 , and θ_0 is not fixed, and there are three possible cases which yield three different solutions:

- Case 1: When $\max\{0, \theta_0\} \leq x^*$ and $x^* \leq \min\{1, \theta_1\}$, x^* is inside of the feasible set of problem P10 as shown in Fig. 7. Hence, x^* is the optimal solution of the problem.

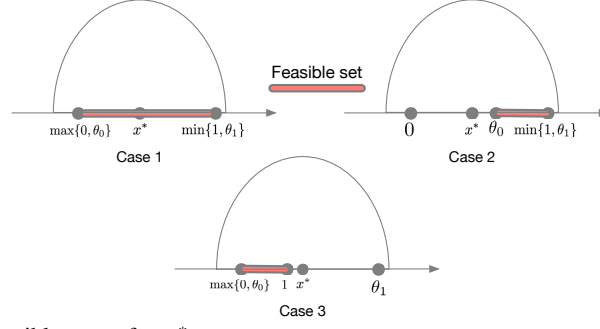


Fig. 7. Illustration for three possible cases for x^*

- Case 2: When $x^* < \theta_0$, the feasible set of α_n is $[\theta_0, \min\{1, \theta_1\}]$ and x^* is at the left-hand side of the feasible set as shown in Fig. 7. The function is monotonically decreasing over the feasible set, and hence θ_0 is the optimal solution of the problem.
- Case 3: When $x^* > 1$, the feasible set of α_n becomes $[\max\{0, \theta_0\}, 1]$ and x^* is at the right-hand side of the feasible set as shown in the figure. The function is monotonically increasing over the feasible set, and hence 1 is the optimal solution of the problem.

In summary, the optimal solution for problem P10 is given by

$$\alpha_n^*(\bar{E}_n) = \min \{1, \max \{x^*, \theta_0\}\}, \quad (70)$$

and the lemma is proved.

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