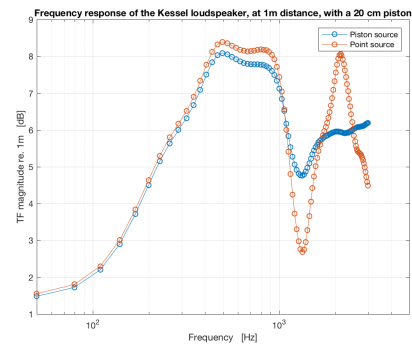
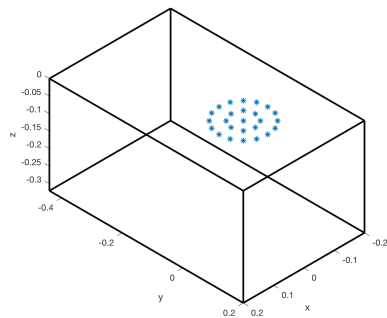


# Edge diffraction Matlab toolbox

## EDtoolbox v 0.210

### Manual



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# 1 Introduction

The edge diffraction Matlab toolbox, 'EDtoolbox', presented here computes the scattered sound pressure, for polyhedral scattering objects with rigid surfaces (Neumann boundary condition). The scattered sound pressure is modeled as a sum of geometrical acoustics components, and first- and higher-order diffraction components. In the current version, 'EDtoolbox' v 0.2xx, external scattering problems for convex bodies can be studied, with time- or frequency-domain computations. One goal for this toolbox is that compact scripts can document precisely how a computation was done, which should help to make computed results more reproducible and transparent. Furthermore, several different example scripts are supplied, so that it should be easy to get started.

The author has worked with the development of "Edge diffraction Matlab toolboxes" since around 1999. Previous versions (EDB1, EDB2, ESIE0, ESIE1, ESIE2) had evolved into quite a huge set of functions of mixed software quality. Those toolboxes tried to handle external as well as internal scattering problems with a single main program, which contributed to the complexity. So, in the late fall of 2017 quite a thorough clean-up process was started and a first version of the toolbox was focused on restricted set of problems. In addition, the toolbox was made available at [github.com](https://github.com).

This manual has an accompanying theory leaflet which describes the theory implemented in the toolbox.

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## **1.2 Acknowledgements**

Many people have contributed on a smaller and larger scale during more than twenty years of work. The last year, the collaboration with Sara Martin, Jan Slechta and Jason Summers is acknowledged in particular.

Parts of this work have been financed through Sara Martin's project "Hybrid methods" funded by the Research Council of Norway, and through Jan Slechta's stipend from the ERCIM Alain Bensoussan Fellowship Programme.

## 2 The ED toolbox

### 2.1 Installation

At [github.com](https://github.com), you can find the last version of the textttEDtoolbox at

<https://github.com/upsvensson/Edge-diffraction-Matlab-toolbox>.

On that page, you can press "Clone or download" and get the full set of Matlab files, including this manual. It is recommended that you store all the m-files in a folder called "EDtoolbox", and that you include the path to that folder in Matlab's path.

You must also download two functions from Matlab Central. These two functions are required for EDtoolbox, and they must be stored in a folder which is added to Matlab's list of paths. Those two functions are

- **DataHash**, developed by Jan Simon. This function is used to create a hash, a 32-bit character that is unique for all the calculation settings and the specific toolbox version number. That hash is stored in each intermediate file which is (optionally) stored. At a subsequent run of the program, the directory with result files is scanned for existing files with the same hash value, which makes it possible to use that existing file instead of calculating a new.
- **lgwt**, developed by Greg von Winckel. This function gives the Gauss-Legendre nodes and weights.

A number of example scripts are also available at

<https://github.com/upsvensson/EDexamples>.

### 2.2 Overview

The EDtoolbox computes the scattered, that is, reflected + diffracted, sound pressure for a scattering object according to the methods described in the accompanying theory leaflet. The sound pressure is modeled as a decomposition into several terms, illustrated in Fig. 1,

$$\begin{aligned} p_{\text{total}} &= p_{\text{direct}} + p_{\text{specular}} + p_{\text{1. order diffraction}} \\ &\quad + p_{\text{2. order diffraction}} + p_{\text{3. order diffraction}} + \dots \\ &= p_{\text{direct}} + p_{\text{specular}} + p_{\text{1. order diffraction}} + p_{\text{HOD}}. \end{aligned} \tag{1}$$

As of version 0.2xx, geometries can be external and convex only, and frequency-domain formulations have been implemented in addition to some time-domain formulations. The only supported boundary condition is the ideally rigid surface (Neumann boundary condition). It can be noted that for a convex scattering body, combinations of specular reflections and edge diffractions can not occur. Furthermore, only first-order specular reflections are possible, which simplifies greatly the identification of possible paths.

Table 1 summarizes the cases that have been implemented. The method denoted **ESIEBEM** uses the **ESIE** approach to compute the sound pressure at

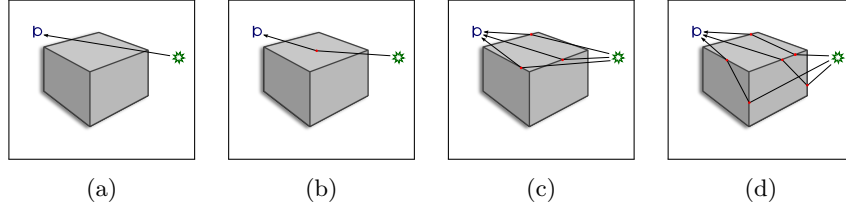


Figure 1: Illustration of the decomposition of the sound field into components: (a) Direct sound, (b) Specular reflection, (c) First-order diffraction, (d) Second-order diffraction

intermediate receiver positions at the surface of the scattering object, and then propagates this surface sound pressure to the external receiver positions using the Helmholtz integral.

Table 1: EDtoolbox - Implemented cases as of version 0.2

Problem type Method (FD/TD)	Main function	Result variables
<b>External problems, convex objects</b>		
Method: ESIE (FD)	EDmain.convexESIE	tfdirect, tfgeom, tfdiff, tfinteqdiff
Method: ESIEBEM (FD)	EDmain.convexESIEBEM	tftot
Method: separate diffraction orders (TD)	EDmain.convex.time	irdirect, irgeom, irdiff, irhod
<b>External problems, non-convex objects</b>	Not implemented yet	
<b>Internal problems</b>	Not implemented yet	

It should be pointed out that the EDtoolbox gives the value of the sound pressure at a receiver *for a normalized source amplitude of 1*; that is, the result could be viewed as a transfer function (or an impulse response), which is why the output variables have names such as `tfdirect` etc. The transfer functions (TF) are defined such that a free-field radiating monopole has the transfer function

$$\text{TF}_{\text{free-field}} = \frac{e^{-jkr}}{r}$$

and all other transfer functions are scaled accordingly. For time-domain (TD) calculations, the corresponding free-field impulse response is

$$\text{IR}_{\text{free-field}} = \frac{1}{r} \delta \left( t - \frac{r}{c} \right)$$

It could also be interpreted that the EDtoolbox gives the sound pressure at the receiver if the monopole's source signal amplitude is 1, and this source signal,

$Q_M$ , is, for frequency-domain (FD) calculations,

$$Q_M = \frac{j\omega\rho_0 U_0}{4\pi}$$

where  $U_0$  is the volume velocity of the monopole. For TD calculations the monopole source signal is

$$Q_M(t) = \frac{\rho_0}{4\pi} \frac{d}{dt} U_0(t)$$

If one prefers, it is also possible to call the output quantities "sound pressure re. 1m free-field", with the additional information that the phase reference is determined by one parameter setting, called `controlparameters.Rstart`, expecting a value in meters. The default value is zero, which would yield an `indirect`, for the case of a receiver 1 m from a source, as being a pulse of amplitude 1, at the time slot that corresponds to the propagation time for 1m.

The EDtoolbox uses only monopoles, but a plane wave can be emulated by doing those steps:

1. Place the monopole arbitrarily far away, at a distance of, say,  $10^6$  m.
2. Set `controlparameters.Rstart` to the distance to the monopole. This implies that the incident sound wave has the phase 0 at the origin. This is especially important for TD calculations with sources far away since otherwise, an impulse response with extremely many initial zeros will be generated.
3. When the result files are loaded, the `tfxxx` or `irxxx` must be multiplied by the source distance.

Sources and receivers can be placed at surfaces, but they must be positioned a tiny little distance from the surface of the scattering object;  $10^{-4}$  m suffices. The reason for this is that the functions must be able to determine which side of a plane that the sources and receivers are.

### 2.3 How to run the EDmain\_xxx functions

The `EDmain_xxx` functions are all run by assigning values to six input structs, each with a number of fields, that are further described in Section 3.2,

- `geoinputdata`
- `Sinputdata`
- `Rinputdata`
- `controlparameters`
- `filehandlingparameters`
- `envdata`

and then call the wanted main function, such as

```
EDmain_convexESIE(geoinputdata,Sinputdata,Rinputdata,envdata,...
controlparameters,filehandlingparameters)
```

Attempts have been made to give many default values to settings, such that it can be easy to get started.

### 2.3.1 A minimal working example - the frequency response of a loudspeaker

As one example, the script below defines a cuboid loudspeaker box, a point source right at the box (at a distance of  $10^{-5}$  m), and a receiver 1 m away, see Fig. 2 (a). The function `EDmain_convexESIE` is run, and after the calculations have been run, the result files are loaded and a frequency response is plotted. The example is taken from the collection of scripts in `EDexamples`. The script `EDexample_LspKessel_minimal.m` has some additional explaining text, but gives the same results as the script below. Fig. 2 (b) shows the resulting output.

The response in Fig. 2 (b) demonstrates the typical "baffle-step" in the response, that is, a step-up by 6 dB from low to high frequencies, with interference ripple effects. At low frequencies (LF), the magnitude of the transfer function/frequency response should be  $1/r$  where  $r$  is the distance. For short distances, this will not be true, and we can see that the response does not quite tend towards 0 dB. For receivers at a very long distance, however, the LF response magnitude will indeed come very close to  $1/r$ .

The response is computed up to 3000 Hz. For higher frequencies (HF), a larger number of edge points (setting `controlparameters.ngauss`) would be needed. One can estimate that 3 edge points per shortest wavelength are needed. The response at HF can be computed much more efficiently with TD calculations, as demonstrated in Section 5.4.

```
mfile = mfilename('fullpath');
[infilepath,filestem] = fileparts(mfile);

%-----
% Define the scattering object = the "Kessel" loudspeaker box

corners = [ -0.20 -0.44 -0.32; 0.20 -0.44 -0.32; 0.20 0.20 -0.32; ...
            -0.20 0.20 -0.32; -0.20 -0.44 0; 0.20 -0.44 0; 0.20 0.20 0; -0.20 0.20 0];
planecorners = [ 1 4 3 2; 5 6 7 8; 1 2 6 5; 3 4 8 7; 2 3 7 6; 1 5 8 4];

%-----
% Give calculation parameter values, including S and R positions

geoinputdata = struct('corners',corners,'planecorners',planecorners);
Sinputdata = struct('coordinates',[0 0 0.00001]);
Rinputdata = struct('coordinates',[0 0 1]);
controlparameters = struct('frequencies',linspace(50,3000,100));
filehandlingparameters = struct('filestem',filestem)
filehandlingparameters.outputdirectory = [infilepath,filesep,'results'];

%-----
% Run the calculations

EDmain_convexESIE(geoinputdata,Sinputdata,Rinputdata,struct,...
controlparameters,filehandlingparameters);

%-----
```

```

% Load and present the results, and plot the geometry model

eval(['load ',filehandlingparameters.outputdirectory,filesep,...
filehandlingparameters.filestem,'_tfinteq.mat'])
eval(['load ',filehandlingparameters.outputdirectory,filesep,...
filehandlingparameters.filestem,'_tf.mat'])
tftot = tfdirect + tfgeom + tfdiff + tfinteqdiff;

figure; semilogx(controlparameters.frequencies,20*log10(abs(tftot)),'-o')
xlabel('Frequency [Hz]'); ylabel('TF magnitude re. 1m [dB]')
title('Frequency response of the Kessel loudspeaker, at 1m distance')
axis([50 5000 0 10]); grid

eddatafile = [filehandlingparameters.outputdirectory,filesep,...
filehandlingparameters.filestem,'_eddata.mat',3];
EDplotmodel(eddatafile,3)

```

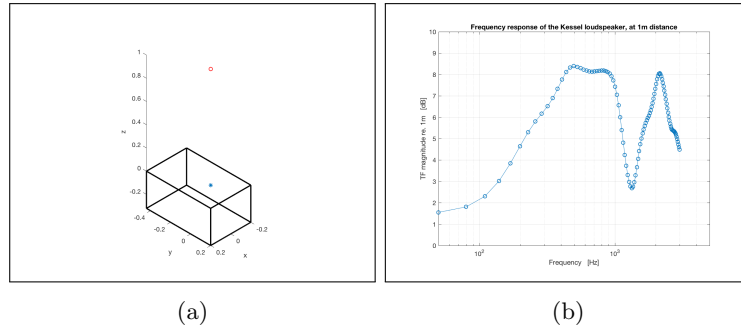


Figure 2: The "Kessel" loudspeaker example. (a) The loudspeaker model, with source and receiver positions. (b) The frequency response at 1m distance, for a point source, computed with `EDmain_convexESIE`.

## 2.4 Known bugs

A few bugs are known, as of v 0.210. Two bugs are of the same character:

- If the receiver is hidden behind the scattering object, but the direct sound path happens to pass exactly through two edges, then the path is not detected as obstructed. This failure is revealed by the test function `EDverify`, test case number 8 (see Section 4.2).
- Similarly, if the direct sound path passes exactly through two corners, the path is not detected as obstructed. This failure is revealed by the test function `EDverify`, test case number 7 (see Section 4.2).

Another bug, or unclarity of the underlying equations, is that if the direct sound passes exactly through one corner, its amplitude is presently computed as  $0.5 \times 0.5 = 0.75$  times the unobstructed sound wave amplitude. This does, however, not give a continuous sound pressure amplitude through that point.

One missing implementation, is that detailed timing data is not saved for the integral equation, when there are several sources, but `doaddsources = 0`.

Another bug is that for the `ESIEBEM` main function, the parameter `.doallSRcombinations` (see Table 3) has no effect - all source/receiver combinations are always computed.



## 3 Input and output data

### 3.1 Geometry format

The **EDtoolbox** handles only polyhedra, including polygonally shaped thin discs/plates. A polyhedron is defined here in terms of 'corners' (vertices) and 'planes' (faces/polygons). These can either be specified directly in the input struct **geoinputdata** (fields **.corners** and **.plane corners**, as in the example in section 2.3), or in a separate file of the **.cad-format**, which is a text file format exported by the CATT-Acoustic software [?], which is easy to write manually. Fig. 3 shows a simple example: a cuboid box.

#### 3.1.1 Corners

The **.corners** field is straightforward: it is a matrix of size **[ncorners,3]** where row **n** contains the x-, y- and z-coordinates of corner number **n**. For the example in Fig. 3, this matrix would have the first few lines as

```
geoinputdata.corners = [-0.2 -0.44 -0.32; ...  
0.2 -0.44 -0.32; 0.2 0.2 -0.32; ...
```

If the geometry of the scattering object is instead defined in a **.cad-file**, see section 3.1.3, the **.corners** field will be created by the function **EDreadcad**, which is called automatically. The corner numbers in the **.cad-file** will be the same in the **.corners** field. However, if the **.cad-file** had a non-contiguous numbering of the corners, a renumbering will be done for the **EDtoolbox**, starting with number 1.

#### 3.1.2 Planes

The **.plane corners** field is a matrix of size **[nplanes,nmaxcp]**, **nmaxcp** standing for "nmaxcornersperplane", where row **n** gives the corners that define plane **n**.

The example in Fig. 3 would have its planes defined as

```
geoinputdata.plane corners = [1 4 3 2; 5 6 7 8; ...
```

A few important rules must be followed:

- The corners must be defined in a counter-clockwise order, as seen from the frontal side of the plane. You can use a right-hand rule: if you place your right hand on the frontal side of the surface, with your thumb pointing in the direction of the (imagined) plane normal vector, than your curved fingers should indicate the order to specify the corners.
- Please note that for thin planes, both sides of the plane must be specified.
- If not all planes have the same number of corners, you must add zeros to the end of each row with fewer corners, so that each row gets the same number of values.

- Some geometry generating software splits up polygons into triangles, but **EDtoolbox** can not handle co-planar triangles. As large polygons as possible must be constructed for each face of the polyhedron.

### 3.1.3 The cadfile format

The cadfile format is a very simple format defined by the CATT-Acoustic software. It is a textfile with four sections, marked with textlines **%CORNERS**, **%PLANES**, **%SOURCES**, **%RECEIVERS**. For the use in the **EDtoolbox**, only the first two are used. Thus, the two sections should have the format given below, exemplifying for the same box as in Fig. 3 (the first line is optional but quite useful):

```
%LSP_Kessel.CAD

%CORNERS
1 -0.20 -0.44 -0.32
2 0.20 -0.44 -0.32
3 ...

%PLANES
1 / /RIGID
1 4 3 2

2 / /RIGID
5 6 7 8
```

### 3.1.4 Excluding some edges

There are some limited possibilities to create geometrical models with just a few edges, using the parameter **geoinputdata.firstcornertotskip**, see Table 2. By giving a corner number of the model to that parameter, all edges with at least one corner which has a number like that parameter value, or higher, will be deactivated. Another possibility is to use a cad-file and give a plane the material type **TOTABS**. Then, all edges that are connected to that plane will be deactivated. Using these techniques, it is possible to simulate, e.g., just the top edges of a noise barrier.

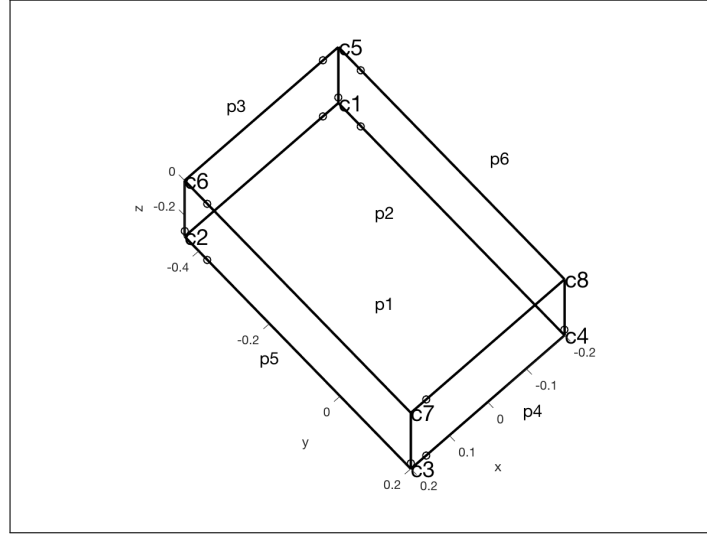


Figure 3: Illustration of a cuboid scattering object. Corner numbers and plane numbers are indicated.

### 3.2 Input parameters

The main functions, `EDmain_xxx`, are run with six structs containing all input parameters:

```
EDmain_convexESIE(geoinputdata,Sinputdata,Rinputdata,envdata,...
controlparameters,filehandlingparameters)
```

These six structs are described in Tables 2 - 7.

Table 2: Input data struct `geoinputdata`

Field name <sup>1</sup>	Description	
<code>.geoinputfile</code>	This field should be given the file name (with path) of a <code>.cad</code> -file	
<code>.corners</code>	Format as in Section 3.1.1	
<code>.plane corners</code>	Format as in Section 3.1.2	
<code>.firstcornertoskip</code>	As described in Section 3.1.4, some edges can be deactivated by using this parameter. Default value 1e6.	

<sup>1</sup> Four alternatives exist for specifying the struct `geoinputdata`

A. An external `.cad`-file is specified in the field `.geoinputfile`

B. If the field `.geoinputfile` is not specified, then the fields `corners` and `plane corners` can give the geometry data.

C. If neither of the two alternatives above apply (e.g., if the entire struct is left empty), then a file opening window will appear, and a `.cad`-file can be selected.

D. If both alternatives A and B are given, priority will be given to the `.geoinputfile`. See section 3.1 for more information on the geometry format.

Table 3: Input data struct `Sinputdata`

Field name	Description	
<code>.coordinates</code>	Required parameter. A matrix of size <code>[nsources,3]</code> , giving the x-, y-, and z- coordinates of each source. <sup>1</sup>	
<code>.doaddsources</code>	If this value is set to 1, the contributions from all sources will be added and saved in a single transfer function, after being multiplied by the values in the matrix <code>.sourceamplitudes</code> . <sup>2</sup> Default value 0.	
<code>.sourceamplitudes</code>	A matrix of amplitudes, size <code>[nsources,nfreq]</code> , that each source is multiplied with. Using this, together with <code>.doaddsources=1</code> , a vibration pattern on a surface can be simulated. Default value <code>ones(nsources,nfreq)</code> .	
<code>.doallSRcombinations</code>	If <code>n</code> sources and <code>n</code> receivers are specified, one can choose to compute the response only for source 1 to receiver 1, source 2 to receiver 2, etc by setting this parameter to 0. This is relevant for computing monostatic backscattering. Default value 1.	

<sup>1</sup> If a source is placed at a surface, it needs to be placed a tiny distance away from the surface, say  $10^{-5}$  m.

<sup>2</sup> This is a straightforward way to simulate extended sources, or vibration patterns. See section 3.3 for a description of the scale values.

Table 4: Input data struct `Rinputdata`

Field name	Description	
<code>.coordinates</code>	Required parameter. A matrix of size [nreceivers,3], giving the x-, y-, and z- coordinates of each receiver. <sup>1</sup>	

<sup>1</sup> If a receiver is placed at a surface, it needs to be placed a tiny distance away from the surface, say  $10^{-5}$  m.

Table 5: Input data struct `envdata`

Field name	Description	
<code>.cair</code>	Should be the speed of sound in m/s. Default value 344.	
<code>.rhoair</code>	Should be the density of the medium, in kg/m <sup>3</sup> . Default value 1.21.	

Table 6: Input data struct `controlparameters`

Field name	Description	
<code>.directsound</code>	If this parameter is set to 0, the direct sound will not be computed. The result variable <code>tfdirect</code> or <code>irdirect</code> will still be generated but with values 0. Default value 1.	
<code>.skipfirstorder</code>	If this parameter is set to 1, the direct sound, specular reflection, and first-order diffraction will not be computed. Their respective output variables will be generated, with values 0. Default value 0.	
<code>.Rstart</code>	Determines the phase of the final transfer functions (or the definition of the time zero in TD calculations) <sup>1</sup> . Default value 0.	
<code>.difforder</code>	Specifies how many orders of diffraction should be included. <sup>2</sup> Default value 15.	
<code>.docalctf</code>	Determines if transfer functions will be computed. Default value 1 (for FD methods). Ignored by TD methods.	
<code>.frequencies</code>	Required for FD methods. A vector of frequency values that computations will be made for. This parameter is ignored by TD methods.	
<code>.discretizationtype</code>	Determines how the edges will be discretized: 0 $\Rightarrow$ a uniform discretization 0 $\Rightarrow$ Gauss-Legendre discretization. The value 1 is obsolete/not used. Default value 2.	
<code>.ngauss</code>	Specifies the number of quadrature points along the longest edge, for the ESIE method. It will be scaled down linearly based on the length of each edge, with a minimum of 2. Recommended value is at least 3 quadrature points per wavelength, which has to be converted manually to a number of quadrature points. Default value 16.	
<code>.surfacegaussorder</code>	For the ESIEBEM method, this parameter determines how many intermediate receivers will be placed along each plane. Default value 5.	
<code>.docalcir</code>	Determines if impulse responses will be computed. Default value 1 (for TD methods). Ignored by FD methods.	
<code>.fs</code>	Determines the sampling frequency. Default value 44100. Ignored by FD methods.	
<code>.savealldifforders</code>	If this parameter is set to 1, then results are stored for each diffraction order. Default value 0.	

<sup>1</sup> To simulate an incoming plane wave with amplitude 1, and phase zero, at the origo, then `.Rstart` should be set to the distance to the far-away point source. See also the description in Section 2.2.

<sup>2</sup> For `EDmain_convexESIE.time`, the `difforder` is actually the number of time-marching steps, which is not the same as diffraction order: one diffraction order is spread out over many time steps. For `EDmain_convex.time`, `difforder` can not be higher than 6.

Table 7: Input data struct `filehandlingparameters`

Field name	Description <sup>1</sup>	
<code>.outputdirectory</code>	Required parameter <sup>2</sup> . All result files will be saved in this directory. If not specified, a folder named "results" will be made in the folder of the <code>.cad</code> -file.	
<code>.filestem</code>	Required parameter <sup>2</sup> . All result files will start with this text string. If not specified, this field will be given the name of the <code>.cad</code> -file.	
<code>.suppressresult... recycling</code>	0 $\Rightarrow$ all result files will be inspected for possible recycling. <sup>3</sup> Default value 0.	
<code>.savecadgeo</code>	1 $\Rightarrow$ the contents of the <code>.cad</code> -file will be saved in a <code>_cadgeo.mat</code> file. Default value 0.	
<code>.saveSRdatafiles</code>	1 $\Rightarrow$ the visibility of planes and edges, as seen from sources and receivers, is stored in <code>_Sdata.mat</code> and <code>_Rdata.mat</code> files. Default value 1.	
<code>.saveeddatafile</code>	1 $\Rightarrow$ the <code>edgedata</code> struct is saved in an <code>_eddata.mat</code> file. Default value 1.	
<code>.saveed2datafile</code>	1 $\Rightarrow$ the <code>edgetoedgedata</code> struct is saved in an <code>_ed2data.mat</code> file. Default value 1.	
<code>.savesubmatrixdata</code>	1 $\Rightarrow$ the <code>submatrixdata</code> struct is saved in a <code>_submatrixdata.mat</code> file. Default value 1.	
<code>.saveinteqsousigs</code>	1 $\Rightarrow$ the edge source signals are saved in a <code>_sousigs.mat</code> file. Default value 0.	
<code>.loadinteqsousigs</code>	1 $\Rightarrow$ previously calculated, and saved, edge source signals are loaded and re-used. Default value 0.	
<code>.savepathsfile</code>	1 $\Rightarrow$ the lists of possible direct sound, specular reflections, and first-order diffractions, are saved in a <code>_paths.mat</code> file. Default value 1.	
<code>.savelogfile</code>	1 $\Rightarrow$ a log text-file is saved, see Section 3.4. Default value 1.	
<code>.savediff2result</code>	1 $\Rightarrow$ the results for second-order diffraction are saved separately, in the form of the variable <code>extraoutputdata.tfinteqdiff_nodiff2</code> . Default value 0.	

<sup>1</sup> See section 3.5 for a further description of the output files and the data stored therein.<sup>2</sup> If the geometry is given in the form of the input fields `.corners` and `.planecorners`, then the fields `.outputdirectory` and `.filestem` must be specified.<sup>3</sup> If possible, previously computed result files are reused. All the relevant input data to a function is checked, and if the settings for the current calculation match exactly the settings of a previous calculation, the results from the previous calculation will be reused. Note that the toolbox version number will be checked, so if the toolbox version has been changed, all result files will be calculated anew. All the relevant input data are encoded into a hash, which is stored together with the result variables. During the inspection, only this hash is loaded from each available result file, and checked against the hash of the current wanted settings.

### 3.3 Output data in the `_tfxxx.mat` and `_irxxx.mat` files

#### 3.3.1 The resulting sound pressure/transfer functions

The main functions, `EDmain_xxx`, can generate several types of optional output files, as indicated in table 7. The primary output is, however, the resulting sound pressure in the form of transfer functions or impulse responses. They are stored as variables in files described for each `EDmain_xxx` function in Table 8. These files are always generated.

Table 8: Primary output files and result variables

Main function	Result file	Result variables
<code>EDmain_convexESIE</code>	<code>_tf.mat</code>	<code>tfdirect</code> , <code>tfgeom</code> <code>ttfdiff</code>
	<code>_tfinteq.mat</code>	<code>tfinteqdiff</code>
<code>EDmain_convexESIEBEM</code>	<code>_tfesiebem.mat</code>	<code>tftot</code>
<code>EDmain_convex_time</code>	<code>_ir.mat</code>	<code>irdirect</code> , <code>irgeom</code> , <code>irdiff</code> , <code>irhod</code>

For several of these cases, you will have to add these terms in your own scripts, after loading the relevant files listed in Table 8, as can be seen in the example script in section 2.3:

```
tftot = tfdirect + tfgeom + tfdiff + tfinteqdiff
```

In some cases, e.g., for backscatter calculations, one might not be interested in the direct sound, and then

```
tfreflection = tfgeom + tfdiff + tfinteqdiff
```

Each of these transfer functions will have the same size:

$$\text{size}(\text{tf}) = \begin{cases} [\text{nfreq}, \text{nR}, \text{nS}], & \text{if } \text{.doaddsources} == 0 \\ [\text{nfreq}, \text{nR}], & \text{if } \text{.doaddsources} == 1 \end{cases}$$

In addition, if `doallSRcombinations` is given the value 0, then the tf-matrices will contain values only along the diagonal. Obviously, this applies only to square matrices, that is, when `nR = nS`.

The impulse responses have the sizes:

$$\text{size}(\text{ir}) = \begin{cases} [\text{nirsamples}, \text{nR}, \text{nS}], & \text{if } \text{.doaddsources} == 0 \\ [\text{nirsamples}, \text{nR}], & \text{if } \text{.doaddsources} == 1 \end{cases}$$

where the value of `nirsamples` depends on the geometry of the scattering object, the sampling frequency, and the value of `.Rstart`.



The variable `irhod` contains the higher-order diffraction. This is a cell variable, which has a structure which is determined by the parameter `.savealldifforders`:

$$\text{irhod} = \begin{cases} \text{single cell, irhod}\{1\} , & \text{if } .\text{savealldifforders} = 0 \\ \text{one cell for each diffraction order } n, \text{irhod}\{n\} , & \text{if } .\text{savealldifforders} = 1 \end{cases}$$

Each `irhod{n}` has the size:

$$\text{size}(\text{irhod}\{n\}) = \begin{cases} [\text{nirsamples}, nR, nS], & \text{if } \text{doaddsources} == 0 \\ [\text{nirsamples}, nR], & \text{if } \text{doaddsources} == 1 \end{cases}$$

### 3.3.2 Timing data in the `_tfinteq.mat` file

The file named `<filestem>_tfinteq.mat` will contain a variable called `timingstruct`. This struct contains timing data for the different parts of `EDmain_convexESIE` as shown in Table 9.

One example of values is given below for the example `EDexample_LspKessel_minimal` in Section 2.3.

```
timingstruct =
struct with fields:
geoinput: 0.0092
edgedata: 0.0248
Sdata: 0.0099
Rdata: 0.0050
findpaths: 0.0264
maketfs: [0.4092 0.0046 0.0014 0.4026]
edgetoedgedata: 0.0246
submatrixdata: 0.0137
integralequation: [53.6891 0.0904 0.0158 0.4994 0.0140]
```

Table 9: The `timingstruct` in the `_tfinteq.mat` file

Field name	Function which is timed
<code>.geoinput</code>	<code>EDreadcad</code> , or <code>EDreadgeomatrices</code>
<code>.edgedata</code>	<code>EDedgeo</code>
<code>.Sdata</code>	<code>EDSorRgeo</code>
<code>.Rdata</code>	<code>EDSorRgeo</code>
<code>.findpaths</code>	<code>EDfindconvexGApats</code>
<code>.maketfs</code> <sup>1</sup>	<code>EDmakefirstordertfs</code>
<code>.edgetoedgedata</code>	<code>EDed2geo</code>
<code>.submatrixdata</code>	<code>EDinteg_submatrixstructure</code>
<code>.integralequation</code> <sup>2</sup>	<code>EDintegralequation_convex_tf</code>

<sup>1</sup> Four values, which are times for:

- (1) the entire function call,
- (2) generating direct sound component(s),
- (3) generating specular reflection(s),
- (4) generating first-order diffraction

<sup>2</sup> Five values are times for:

- (1) the entire function call (all frequencies),
- (2) generating the **H**-matrix for one frequency (done only if `difforder > 2`),
- (3) compute the source term **q**<sub>0</sub> for one frequency,
- (4) compute **q** via iterations, for one frequency,
- (5) propagate the edge source signals **q** to the receiver point, for one frequency

### 3.3.3 Other output data in the `_tfinteq.mat` file

The `_tf` and `_tfinteq` files will also contain three more variables:

- **EDsettings**, which is a cell variable that contains all 6 input structs, and the EDtoolbox version number:
  - `EDsettings{1}` = `geoinputdata`
  - `EDsettings{2}` = `Sinputdata`
  - `EDsettings{3}` = `Rinputdata`
  - `EDsettings{4}` = `envdata`
  - `EDsettings{5}` = `controlparameters`
  - `EDsettings{6}` = `filehandlingparameters`
  - `EDsettings{7}` = `EDversionnumber`
- **EDdatainpuhash**, which is a 32-bit hex character string which uniquely describes all the settings of the relevant input parameters, and EDtoolbox version. It is like a compact fingerprint of the contents in **EDsettings** described above. The settings can, however, not be extracted from this hash; it is just used to check if an existing file can be recycled for a subsequent calculation.

- `recycledresultsfile`, which is either empty, if the calculations have been run, or contains a file-name, where the results have been copied from.

### 3.4 Log file

If the parameter `filehandlingparameters.savelogfile` is set to 1, a log file will be generated as a plain text file. Its contents will be as below.

```
#####
# EDmain.convexESIE, v. 0.108 (2Feb2018)
# filestem for results: EDexample.LspKessel_minimal

EDreadgeomatrices (8 corners and 6 planes), time: 0.009236 s
EDedgeo, (12 edges), time: 0.024809 s
EDSorRgeo(S), (1 source(s)), time: 0.009944 s
EDSorRgeo(R), (1 receiver(s)), time: 0.005021 s
EDfindconvexGpaths (100 frequencies)
    Total time: 0.02637 s
EDmakefirstordertfs (100 frequencies)
    Total time: 0.40925 s. Parts, for all frequencies, as below
    Generate the direct sound: 0.004572 s
    Generate the specular reflections: 0.001432 s
    Generate the first-order diffraction: 0.40264 s
EDed2geo, time: 0.024557 s
EDinteg_submatrixstructure, (252 submatrices, out of 432, to compute), time: 0.013727 s
    (Edges discretized with: 8 to 16 discretization points)
    (Avg. "edge element" size: 0.04 m.
    OK up to 2867 Hz (3 discret. points per wavelength))
    (9248 edge source signals to compute)
    (628864 non-zero elements in the IE matrix)
EDintegralequation.convex_tf (100 frequencies. Diffraction order: 15)
    Total time: 53.6891 s. Parts, for one freq, as below
    Compute the H-matrix: 0.090421 s
    Compute Qfirstterm: 0.015794 s
    Compute Qfinal: 0.49939 s
    Compute the result at the receiver(s): 0.014038 s
```

### 3.5 Other output files

The contents in the optional output files are described in table 10, and some of the structs are further detailed in tables 11 - 16 below. Whether or not these files are generated is set by the various fields of `filehandlingparameters`, as specified in the last column in Table 10 and further in Table 7.

Table 10: Contents of the optional output files

Output file <sup>1</sup>	Contents <sup>2</sup>	filehandling-parameters
<code>_cadgeo</code>	planedata, extraCATTdata	<code>.savecadgeo</code>
<code>_eddata</code>	planedata, edgedata, EDinputdatahash <sup>3</sup>	<code>.saveeddata</code>
<code>_Sdata, _Rdata</code>	Sdata or Rdata, EDinputdatahash <sup>3</sup>	<code>.saveSRdata</code>
<code>_ed2data</code>	planedata, edgedata, edgetoedgedata, EDinputdatahash <sup>3</sup>	<code>.saveed2data</code>
<code>_paths</code>	firstorderpathdata, EDinputdatahash <sup>3</sup>	<code>.savepaths</code>
<code>_submatrixdata</code>	Hsubmatrixdata, EDinputdatahash <sup>3</sup>	<code>.save_submatrix</code>

<sup>1</sup> The output files will all start with the text label in `filestem`, followed by an underscore and a label, as given in this table.

<sup>2</sup> The contents will all be structs unless marked.

<sup>3</sup> The text string in EDinputdatahash will be determined from different subsets of all input parameter settings for each output file.

As one example of an extra result file, the `edgedata` struct can be mentioned. Internally in the calculations, edges are generated as illustrated in Fig. 4, by the function `EDedgeo`. The edge numbers, and other edge-related parameters, are not immediately relevant for the end results, but can be found in the optional output file `xxx.eddata.mat`.

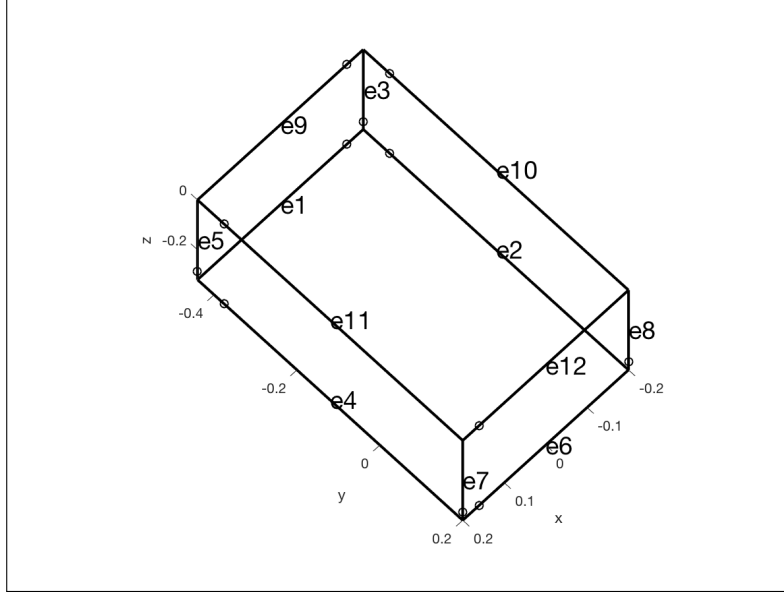


Figure 4: Illustration of a cuboid scattering object, with the derived edge numbers indicated. For each edge, the little circle indicates the starting end.

Table 11: The `planedata` struct, generated by `EDreadcad` or `EDreadgeomatrices`

Field name	Size	Description
<code>.corners</code>	<code>[ncorners,3]</code>	x, y and z for each corner, taken from input data.
<code>.plane corners</code>	<code>[nplanes,nmax]</code>	For each plane, the corner numbers that define the plane, taken from input data. Zeros fill each row to give <code>nmax</code> columns, where <code>nmax</code> is the max number of corners per plane.
<code>.plane abtypes</code>	<code>sparse([nplanes,nn])</code>	For each plane, its absorber type. The values are either taken from the cad-file (in <code>EDreadcad</code> ), or given the value 'RIGID' for each plane (in <code>EDreadgeomatrices</code> ).
<code>.plane eqs</code>	<code>[nplanes,4]</code>	For each plane, the $A, B, C, D$ parameters of its plane equation on the form $Ax + By + Cz = D$ where $A, B, C$ are normalized to give the plane normal vector.
<code>.ncorners per plane vec</code>	<code>[nplanes,1]</code>	The number of corners per plane.
<code>.minvals</code> <code>.maxvals</code>	<code>[nplanes,3]</code> <code>[nplanes,3]</code>	<code>[min(<math>x_i</math>), min(<math>y_i</math>), min(<math>z_i</math>)]</code> <code>[max(<math>x_i</math>), max(<math>y_i</math>), max(<math>z_i</math>)]</code> These min- and max-values give each plane's "axis-aligned bounding box (AABB)".
<code>.plane has indents</code>	<code>[nplanes,1]</code>	For each plane, 0 or 1, telling if the plane has any indents.
<code>.indenting corners</code>	<code>[nplanes,nmax]</code>	For each plane, the number to the first corner in a corner triplet which identifies an indenting corner. The number of the corner is the order given in <code>plane corners</code> for that plane.
<code>.corner in front of plane</code>	<code>[nplanes,ncorners]</code>	-1, 0 or 1. These values specify: 1 means that a corner is in front of the plane 0 means that a corner is aligned with the plane, including belonging to the plane -1 means that a corner is behind the plane
<code>.model type</code>	—	'convex_ext' or 'convex_int' or 'singleplate' or 'thinplates' or 'other'

Table 12: The fields added to the `planedata` struct by `EDedgeo`

Field name	Size	Description
<code>.plane is thin</code>	<code>[nplanes,1]</code>	For each plane, 0 or 1, telling if the plane is thin
<code>.plane sees plane</code>	<code>[nplanes,nplanes]</code>	For each plane-plane pair, -2,-1,0,1: 1 means that a plane is in front of the other plane, but obstruction has not been checked 0 means that a plane is completely behind the other plane -1 means that a plane is aligned with the other plane -2 means that a (thin) plane is back-to-back with the other (thin) plane
<code>.rear side plane</code>	<code>[nplanes,1]</code>	For each plane, the number of the plane on the other side. Only relevant for thin planes.
<code>can plane obstruct</code>	<code>[nplanes,1]</code>	States whether or not a plane has the potential to obstruct (in a plane-to-plane path; which is irrelevant for external convex problems)
<code>.refl factors</code>	<code>[nplanes,1]</code>	-1 (SOFT), 0 (TOTABS), 1 (RIGID)

Table 13: The `edgedata` struct, generated by `EDedgeo`

Field name	Size	Description
<code>.edgecorners</code>	<code>[nedges,2]</code>	For each edge, a starting corner (column 1) and an ending corner (column 2). This direction is maintained through all calculations.
<code>.closedangvec</code>	<code>[nedges,1]</code>	For each edge, the "closed wedge angle" is given, in radians. For a 90-degree external corner of a scattering box, the value would be $\pi/2$ .
<code>.edgestartcoords</code>	<code>[nedges,3]</code>	For each edge, the x,y,z of the starting corner. Redundant; could have been found from <code>planedata.corners(edgecorners(:,1),:)</code>
<code>.edgeendcoords</code>	<code>[nedges,3]</code>	For each edge, the x,y,z of the starting corner. Redundant; could have been found from <code>planedata.corners(edgecorners(:,2),:)</code>
<code>.edgelengthvec</code>	<code>[nedges,1]</code>	For each edge, the edge length. Redundant, could have been computed from the starting and ending coordinates for each edge.
<code>.offedges</code>	<code>[noffedges,1]</code>	A list with all the edges that are not active; either because they have an open angle of 90 degrees (or 60 or 45 or ...), or because <code>firstskipcorner</code> has been given a value which turns off some corners, and therefore edges.
<code>.edgenvecs</code>	<code>[nedges,3]</code>	For each edge, the normal vector of its reference plane/face. The ref. plane is defined by a right-hand rule: if the right-hand thumb is aligned with the direction of the edge (as defined by the two corners in <code>.edgecorners</code> ), then the right-hand fingers will come out of the reference plane, and thereby point in the direction of the normal of the reference plane.
<code>.edgenormvecs</code>	<code>[nedges,3]</code>	For each, a normalized vector in the direction of the edge.
<code>.edgestartcoordsnudge</code>	<code>[nedges,3]</code>	Same as <code>.edgestartcoords</code> , but moved a short distance away from the edge start point.
<code>.edgeendcoordsnudge</code>	<code>[nedges,3]</code>	Same as <code>.edgeendcoords</code> , but moved a short distance away from the edge endpoint.
<code>.edgerelatedcoord... sysmatrices</code>	<code>[nedges,9]</code>	For each edge, 9 values that form a matrix which can be used to compute the coordinates of points in the edge-related coordinate system. Each row has to be reshaped: <code>Bmatrix = reshape(edgerelatedcoordsys... matrices(edgenumber,:),3,3);</code>
<code>.indentingedgepairs</code>	<code>[nn,2]</code>	A list of edge pairs that form an indent.
<code>.planesatedge</code>	<code>[nedges,2]</code>	For each edge, the two connected planes.
<code>.edgesatplane</code>	<code>[nplanes,nmaxcp]</code>	For each plane, the connected edges. The value <code>nmaxcp</code> is the largest number of edges for one plane.
<code>.edgeseesplane</code>	<code>[nplanes,nedges]</code>	-2,-1,0 or 1 For each plane-edge pair: -2 means that the edge belongs to the plane -1 means that the edge is aligned with the plane, but does not belong to it 0 means that the edge is completely behind the plane 1 means that the edge has at least some point in front of the plane, but obstruction has not been checked

Table 14: Output data struct **Sdata**, generated by **EDSorRgeo**

Field name <sup>1</sup>	Size	Description <sup>1</sup>
<b>.sources</b>	[nsources,3]	For each source, the x-, y-, z-coordinates <sup>2</sup>
<b>.visplanesfroms</b>	[nplanes,nsources]	For each plane-source pair: 0: S is behind a plane which is RIGID or TOTABS, 1: S is aligned with a plane, but outside the polygon that defines the plane, 2: S is in front of a plane which is reflective (which means that a specular reflection is possible), 3: S is in front of a plane which is TOTABS (which means that a specular reflection is not possible), 4: S is inside a plane which is RIGID, 5: S is inside a plane which is TOTABS
<b>.vispartedgesfroms</b>	[nedges,nsources]	For each edge-source pair, a value $0-2^n - 1$ . The value $n$ is an integer for checking part-visibility of an edge. This visibility check is irrelevant for convex-shaped objects, but has been used in previous toolbox versions. 0: S can not see any part of the edge $2^n - 1$ : S can see the entire edge other: S can see parts of an edge
<b>.soutsidemodel</b>	[1,nsources]	For each source, 0 or 1, specifying if the source is outside the entire model. This is used in cases where a huge grid of sources, or receivers, is generated with some of them being outside the domain of interest.
<b>.vispartedgesfroms_start</b>	[nedges,nsources]	For each edge-source pair: 0: S can not see the start-point of the edge 1: S can see the start-point of the edge
<b>.vispartedgesfroms_end</b>	[nedges,nsources]	For each edge-source pair: 0: S can not see the end-point of the edge 1: S can see the end-point of the edge
<b>.reftoshortlistS</b>	[nedges,nsources]	For each edge-source pair, a pointer to the 3 following short lists <sup>3</sup>
<b>.rSsho</b>	[nshortlist,3]	A list of unique values of $rS$ <sup>3</sup>
<b>.thetaSsho</b>	[nshortlist,3]	A list of unique values of $\theta S$ <sup>3</sup>
<b>.zSsho</b>	[nshortlist,3]	A list of unique values of $zS$ <sup>3</sup>

<sup>1</sup> An equivalent version exists for receivers, with field names **.receivers**, **.visplanesfromr** etc.

<sup>2</sup> Direct copy from **Sinputdata.coordinates**

<sup>3</sup> Instead of storing all  $nedges*nsources$  values of  $rS, \theta S, zS$ , three more compact "short lists" are stored, with unique values, and  $nedges*nsources$  pointers to these short lists. Thus, the  $r$ -value of source 2, rel. to edge 7, is found as **rSsho(reftoshortlistS(7,2))**.

Table 15: Output data struct `firstorderpathdata`

Field name	Size	Description
<code>.specreflIScoords</code>	<code>[nIS,3]</code>	A list of all valid image sources (IS). For each IS, its x-, y- z-coordinates
<code>.specreflIlist</code>	<code>[nIS,3]</code>	For each IS, three values: S,R,amp. S is the generating source, R is the receiver number, and amp is an amplitude factor.
<code>.diffpaths</code>	<code>[nreceivers,nsources,... nedges]</code>	For each receiver-source-edge triplet: 0 or 1, specifying whether or not that edge is visible
<code>.edgeisactive</code>	<code>[nedges,1]</code>	For each edge: 0 or 1, specifying whether or not that edge is at all active
<code>.directsoundlist</code>	<code>[ndircombs,3]</code>	A list of valid direct sound components. For each such component, three values: S,R,amp. S is the generating source, R is the receiver number, and amp is an amplitude factor.
<code>.ncomponents</code>	<code>[1,3]</code>	A list of number of components: <code>[ndircombs,nIS,ndiffrcombs]</code>

Table 16: Output data struct `Hsubmatrixdata`

Field name	Size	Description
<code>.nedgeelems</code>	<code>[nedges,1]</code>	For each edge, the number of edge elements = quadrature order.
<code>.edgepairlist</code>	<code>[nedgepairs,2]</code>	A list of all edge-sees-edge pairs of the polyhedron. Column 1 has the "to-edge" numbers and column 2 has the "from-edge" numbers. The edge source signals are stored in the edge source signal vector following this order.
<code>.bigmatrixstartnums</code>	<code>[nedgepairs,1]</code>	For each edgepair in <code>.edgepairlist</code> , this vector gives the start index in the edge source signal vector. Each edgepair occupies a number of elements, corresponding to the product of the values of <code>ngauss</code> for the two involved edges.
<code>.bigmatrixendnums</code>	<code>[nedgepairs,1]</code>	For each edgepair in <code>.edgepairlist</code> , this vector gives the end index in the edge source signal vector.
<code>.isthinplaneedgepair</code>	<code>[nedgepairs,1]</code>	For each edgepair in <code>.edgepairlist</code> , 0 or 1, indicating if the path from the "from-edge" to the "to-edge".
<code>.Hsubmatrix</code>	<code>[nedgepairs,nedgepairs]</code>	A matrix with pointers, which for row m, column n, gives the number of the separately stored Hsub matrix which has the transfer matrix elements for the transfer from edgepair number n, to edgepair number m. Scattering objects with symmetries will have a number of identical pointer values, indicating that not all submatrices need to be computed. There are <code>nsub</code> unique submatrices.
<code>.listofsubmatrices</code>	<code>[nsub,3]</code>	
<code>.edgetriplelist</code>	<code>[nsub,3]</code>	edgenumbers
<code>.submatrixcounter</code>		nsub
<code>.nuniqueubmatrices</code>		nuniquesub
<code>.reftoshortlist</code>	<code>[nsub,1]</code>	
<code>.isthinplanetriplet</code>	<code>[nsub,1]</code>	0 or 1
<code>.quadraturematrix_pos</code>	<code>[ngauss,ngauss]</code>	sparse matrix
<code>.quadraturematrix.... weights</code>	<code>[ngauss,ngauss]</code>	sparse matrix



## 4 Some auxiliary functions

### 4.1 EDplotmodel

EDplotmodel - Plots a model which is given in an eddatafile.

Input parameters:

eddatafile (optional) If an input file is not specified, a file opening window will be presented.  
plotoptions (optional) The text-string 'plotoptions', with an integer can give extra options:

```
if bit0 = 1 (= 1) => plot sources
if bit1 = 1 (= 2) => plot Rdata.receivers
if bit2 = 1 (= 4) => plot plane normal vectors
if bit3 = 1 (= 8) => print plane numbers
if bit4 = 1 (=16) => print edge numbers (and indicate start end of each edge
                    with a little circle)
if bit5 = 1 (=32) => print corner numbers
if bit6 = 1 (=64) => print plane numbers using the CAD file numbering
if bit7 = 1 (=128)=> print corner numbers using the CAD file numbering
Example: the integer 11 = 1011 binary, so bits 0,1, and 3 are set.
```

'sounumbers', vector of source numbers (optional)

If the text-string 'sounumbers' is given, followed by a vector of integers, only those source numbers are plotted.

'recnumbers', vector of source numbers (optional)

If the text-string 'recnumbers' is given, followed by a vector of integers, only those source numbers are plotted.

'edgenumbers', vector of edge numbers (optional)

If the text-string 'edgenumbers' is given, followed by a vector of integers, only those edge numbers are plotted with a solid line. The others are plotted with dashed lines.

Sources and Rdata.receivers are taken from an sdatafile and an rdatafile, the file name of which is assumed to be similar to the eddatafile.

### 4.2 EDverify

EDverify runs EDtoolbox for one or several defined tests, and compares the results to expected results. A logfile is written.

Input parameters:

outputdirectory (optional) The directory where the logfile will be stored. If this parameter is not given any value, no logfile will be written, but the user will get a window to specify a directory where the temporary calculation results will be stored.

runtest (optional) A vector of 0 or 1, which for each position n tells if test n should be run. Default value: all 1.

showtext (optional) 0 or 1; determines if the results should be printed on the screen. The results are always written to the logfile. Default value: 0.

plotdiagrams (optional) 0 or 1: determines if result plots will be generated. Default value: 0.

Output parameter:

passtest A vector with -1 (fail), 0 (not run), or 1 (pass) for all the tests.

Tests:

1. Response at cuboid surface, plane wave incidence, 0 Hz, no singularity problem. HOD test.
2. Field continuity across zone boundaries, single edge, 100 Hz. Perpendicular edge hit. Diff1 test.
3. Field continuity across zone boundaries, single edge, 100 Hz. Skewed edge hit. Diff1 test.
4. Field continuity across corner zone boundaries, single edge, 100 Hz. Diff1 test.
5. Field continuity for receivers close to a single edge, 100 Hz. Diff1 test.
6. Replicate a non-centered internal monopole, at 0.1 Hz.
7. Direct sound obscuring for a corner-on hit of an octahedron.
8. Direct sound obscuring for an edge-on hit of a cube.

```
passtest = EDverify(outputdirectory,runtest,showtext,plotdiagrams);
```

### 4.3 EDcirclepoints

EDcirclepoints distributes point coordinates across a circular surface.

Input parameters:

radius           The piston radius, in meters  
numberofcircles   The number of circles of point sources. The value 1 will lead to  
                  9 point sources. The value 2 gives 25 point sources etc

```
coordinates = EDcirclepoints(radius,numberofcircles)
```

### 4.4 EDmakegeo\_cylinder

EDmakegeo\_cylinder generates the geometry for a polyhedral cylinder. The end caps of the cylinder will be parallel to the z=0 plane, symmetrically placed. Optionally, the whole cylinder can be translated in the z-direction.

The polygonal shape will be scaled so that regardless of numbers of edges, the volume of the polygonal cylinder will be the same as a truly circular cylinder with the radius given as input parameter.

Input parameters:

radius           The radius of the equivalent circular cylinder  
width            The length of the cylinder  
numberofcorners   The number of corners approximating the circular cross-section  
intextgeom       'int' or 'ext' defining if an interior or exterior geometry should be constructed  
fullcirclefract   1 or 0.5, indicating whether a full or half cylinder should be created.  
angleoffset (optional) 1 or 0, indicating whether or not the first corner  
                  should be placed in y = 0 (angleoffset = 0) or shifted  
                  half an angle step (angleoffset = 1).  
ztranslation (optional) A value which will be added to all the z-coordinates.

Output parameters:

corners           Matrix, [2\*numberofcorners,3], with the corner coordinates  
plane corners     Matrix, [numberofcorners+2,numberofcorners], with the plane corners.  
                  The first numberofcorners rows have the planes of the cylindrical surface,  
                  and the two last rows have the flat circular endsurfaces.  
ncornersperplanevec A vector which gives the number of corners per plane  
radius            The actual radius of the corners; this will be different from the (desired)  
                  input parameter 'radius', since the polygonal approximation of the circle  
                  is scaled so that it gets the same cross-section area as the real circle.

```
[corners,plane corners,ncornersperplanevec,radius] = EDmakegeo_cylinder...  
(radius,width,numberofcorners,intextgeom,fullcirclefract,angleoffset,ztranslation);
```

## 5 Example scripts

In the folder `EDexamples`, a number of examples of different types are given. These scripts are hopefully easy to modify to individual needs. In Section 2.3, a loudspeaker simulation was demonstrated, with a single point source representing the loudspeaker element.

### 5.1 `EDexample_LspKessel_piston.m`

This example demonstrates how to simulate a circular piston, with the script `EDexample_LspKessel_piston.m`. Below, the parts of this script that differ from `EDexample_LspKessel_minimal.m` are given, and Fig. 5 shows the results, and the model (without the receiver position), respectively. In Fig. 5, also the frequency response from Fig. 2 is shown for comparison.

The auxilliary function `EDcirclepoints` distributes points equally in  $n$  concentric circles, and positions them around the origin in the  $z = 0$  plane, see Section 4.

```
controlparameters = struct('frequencies', linspace(50,3000,100));
nfreq = length(controlparameters.frequencies);
sources = EDcirclepoints(0.1,2);
sources(:,3) = 0.00001;
nsources = size(sources,1);
Sinputdata = struct('coordinates',sources);
Sinputdata.doaddsources = 1;
Sinputdata.sourceamplitudes = ones(nsources,nfreq)*1/nsources;
```

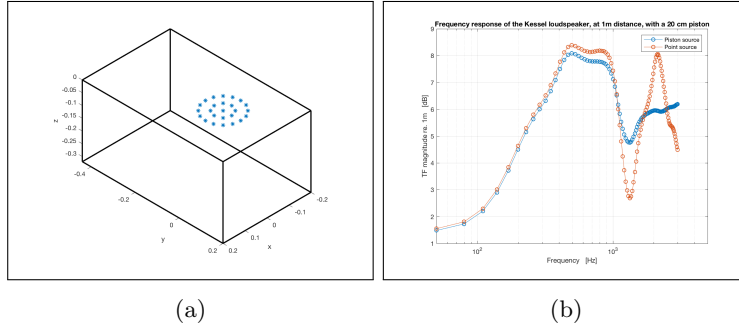


Figure 5: The "Kessel\_piston" loudspeaker example with a 20 cm piston source. (a) The loudspeaker model, with the piston represented by 25 point sources. (b) The frequency response at 1m distance, for the piston and point source.

## 5.2 EDexample\_LspCylinder16.m

The shape of a loudspeaker enclosure has much influence on the frequency response, as shown in [H. Olson, "Direct radiator loudspeaker enclosures," J. Audio Eng. Soc. 17, pp. 22-29, 1969]. The enclosure shape with the strongest diffraction effect is the cylinder, with a source centrally placed, and that is demonstrated by the example `EDexample_LspCylinder16.m`. The result diagram in Fig. 6 tries to mimic the results in the paper by Olson. It was not stated in that paper what the distance to the microphone, so it was chosen to generate the same dip frequencies as in the published frequency response. Parts of the script contents are given below. The auxiliary function `EDmakegeo_cylinder` is used to generate the polygonal cylinder shape, see Section 4.

```
radius = 0.3048;
length = 2*radius;
[corners,plane_corners,ncorners,radius] = EDmakegeo_cylinder...
(radius,length,16,'e',1,0,-radius);
geoinputdata = struct('corners',corners,'plane_corners',plane_corners);

Sinputdata = struct('coordinates',[0 0 0.00001]);
Rinputdata = struct('coordinates',[0 0 6.6]);
controlparameters = struct('frequencies',linspace(50,4000,100));
controlparameters.ngauss = 24;
controlparameters.difforder = 30;
```

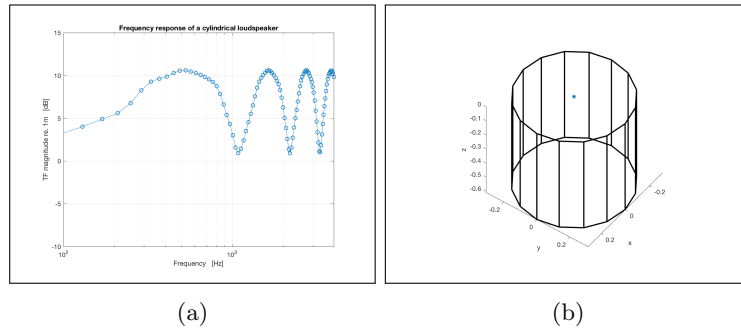


Figure 6: A cylindrical loudspeaker modeled as a 16-sided polygonal cylinder, with a point source. (a) The frequency response at 6.6 m distance. (b) The loudspeaker model, with the point source marked.

### 5.3 EDexample\_LspKessel\_ir.m

This example demonstrates how low-order diffraction impulse responses can be computed, with the script `EDexample_LspKessel_ir.m`. The result diagrams in Fig. 7 show the impulse responses of the individual diffraction orders, and the corresponding frequency responses (transfer functions), including different numbers of diffraction orders. In Fig. 7 (d), a low-pass filtering effect can be observed for the direct sound and specular reflection, which coincide. The cause of this is the simple conversion of the direct sound Dirac pulse to a two-sample impulse response. Such an approach is the simplest possible "fractional delay" version, which gives a very small phase error for the direct sound but a substantial magnitude error. A simple remedy is to double or quadruple the sampling frequency. These impulse responses correspond to the results in [J. Vanderkooy, "A simple theory of cabinet edge diffraction," J. Audio Eng. Soc. 39, pp. 923-933, 1991], which used an edge diffraction model with a substantial low-frequency error, but with identical results to the method here for higher frequencies.

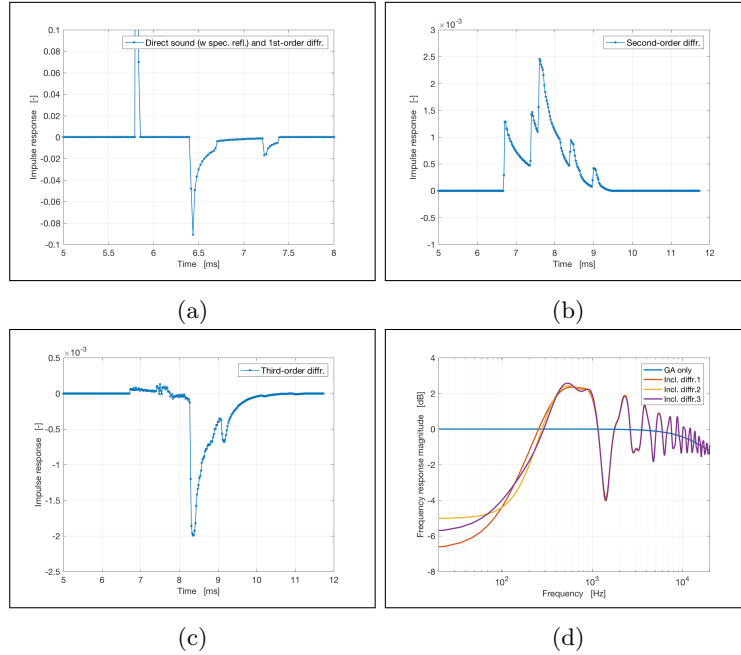


Figure 7: Diffraction impulse responses and frequency responses for the Kessel loudspeaker case, computed with `EDmain_convex_time`. (a) Direct sound and first-order diffraction components. The direct sound, around 5.8 ms, has an amplitude which is not shown, in order to see the weaker first-order diffraction components. (b) Second-order diffraction components. (c) Third-order diffraction components. (d) The corresponding frequency responses.

#### 5.4 EDexample\_LspKessel\_ir\_and\_tf.m

This example expands on the previous one by showing that the impulse response, with low-order diffraction, can be quite accurate for mid to high frequencies, whereas the higher-order diffraction calculation, in the frequency domain, can be employed for the LF range. The script `EDexample_LspKessel_ir_and_tf.m` runs both `EDmain_convex_time` and `EDmain_convexESIE`. The result diagrams in Fig. 8 show the impulse responses of the individual diffraction orders, as in the previous example, and the corresponding frequency responses (transfer functions), including different numbers of diffraction orders. Apparently, the difference between the results with diffraction orders up to 3 and up to 15, is getting very small above approximately 1 kHz.

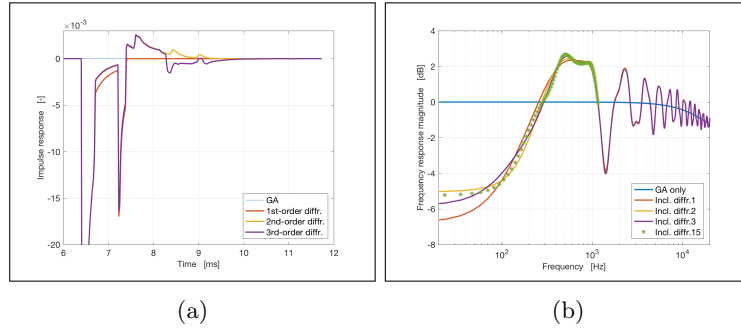


Figure 8: Diffraction impulse responses and frequency responses for the Kessel loudspeaker case. (a) Direct sound and first-order diffraction components, computed with `EDmain_convex_time`. The direct sound, around 5.8 ms, is not shown. (b) The corresponding frequency responses, and the frequency response computed with `EDmain_convexESIE`.

## 6 Appendix - Program structure for EDmain\_convexESIE

The main functions `EDmain_xxx` run through a sequence of processing blocks that are partly identical for the different main functions. Tables 17-18 show this sequence for three of those functions, and they are described briefly below.

Table 17: The processing block sequence of two `EDmain_xxx` functions

<b>EDmain_convexESIE</b>	<b>EDmain_convex_time</b>
<code>EDcheckinputstructs</code>	←
<code>EDreadcad/EDreadgeomatrices</code>	←
<code>EDedgeo</code>	←
<code>EDSorRgeo(.Sdata)</code>	←
<code>EDSorRgeo(.Rdata)</code>	←
<code>EDfindconvexGApats</code>	←
<code>EDmakefirstordertfs</code>	<code>EDmakefirstorderirs</code>
<code>EDed2geo</code>	←
<code>EDinteg_submatrixstructure</code>	----
<code>EDintegralequation_convex_tf</code>	----
----	<code>EDfindHODpaths</code>
----	<code>EDmakeHODirs</code>

Table 18: The processing block sequence of the `EDmain_convexESIEBEM` function

<b>EDmain_convexESIEBEM</b>	
<code>EDcheckinputstructs</code>	
<code>EDreadcad/EDreadgeomatrices</code>	
<code>EDgensurfreceivers</code>	
<code>EDmain_convexESIE</code>	Run with intermediate surface receivers Propagate intermediate surface pressure to original receivers ("fieldpoints")

### 6.1 EDcheckinputstructs

This function checks the input data and assigns default values to input parameters that have not been specified.

Input: `geoinputdata, Sinputdata, Rinputdata, envdata, controlparameters, filehandlingparameters`  
Output: `geoinputdata, Sinputdata, Rinputdata, envdata, controlparameters, filehandlingparameters`

### 6.2 EDreadcad or EDreadgeomatrices

The geometry can either be specified in a separate `.cad` file, or given as input data matrices. See more on this topic in Section 3.1. The data is stored in a struct called `planedata`, see Table 11 for details.

For EDreadcad:

Input: `geoinputdata.geoinputfile`

Output: `planedata, extraCATTdata`

For EDreadgeomatrices:

Input: `geoinputdata.corners, geoinputdata.planecorners`

Output: `planedata`

### 6.3 EDedgeo

This function identifies all the edges of the polyhedron, and stores data about them in a separate struct called `edgedata`, see Table 13 for details.

Input: `planedata, geoinputdata.firstcornertotskip`

Output: `planedata, edgedata`

### 6.4 EDSorRgeo

This function is run twice, once to find the visibility data for the source, and the second time to find the visibility data for the receiver. The visibility data tells what edges and planes each source and receiver can see. The structs `Sdata` and `Rdata` are described in Table 14.

Input: `planedata, edgedata, Sinputdata.coordinates` or

`planedata, edgedata, Rinputdata.coordinates`

Output: `Sdata` or

`Rdata`

### 6.5 EDfindconvexGApaths

This functions finds all the valid direct sound paths, specular reflection paths, and first-order diffraction paths. This function is specialized for the case of external, convex scattering objects, and for such objects, each source-receiver combination can have maximum one specular reflection. The results are stored in a struct called `firstorderpathdata`, see Table 15.

Input: `planedata, edgedata, Sdata, Sinputdata.doallSRcombinations,`  
`Rdata, controlparameters.difforder,`

`controlparameters.directsound`

Output: `firstorderpathdata`

#### Notes

The specular reflections are found with the image source method: all potentially visible image sources are constructed, using the `Sdata.visplanesfroms` matrix. Then, the visibility for each receiver is determined by checking if the line from the image source to the receiver passes through the intended finite reflection plane. This visibility test employs the same test as the direct sound obscuration test: point-in-polygon. The ray-shooting algorithm in the 2D-flattened polygon version is used for this test. When a hit is very close to an edge, or a corner, the amplitude is reduced from 1 to 0.5, for both the direct sound and the specular reflection.

The first-order diffraction components are found by combining the matrices `Sdata.vispartedgesfroms` and `Rdata.vispartedgesfromr`. Edges that are visible from both the source and the receiver should generate first-order edge diffraction.



## 6.6 EDmakefirstordertfs

Based on the paths specified in the struct `firstorderpathdata`, the function `EDmakefirstordertfs` generates the transfer functions `tfdirect`, `tfgeom`, and `tfdiff`.

Input: `firstorderpathdata, controlparameters, envdata, Sinputdata, Rdata.receivers, edgedata`  
Output: `tfdirect, tfgeom, tfdiff, timingdata`

### Notes

The direct sound and specular reflection components are straightforward to compute as

$$\begin{cases} \text{tfdirect} \\ \text{tfgeom} \end{cases} = A \frac{e^{-jkr}}{r}$$

where  $A$  is 0.5 if an edge or corner hit occurred, and 1 otherwise.

First-order edge diffraction is computed with numerical solution of the integrals presented in [Svensson et al, AAA, 2009]. Matlab's built-in `quadgk` is used for this, yielding high accuracy. For certain source-receiver positions, this integral gets a strong singularity, and then, an analytical integration is carried out for a very small part of the edge, around the apex point. A simplified version of the formulation in [Svensson, Calamia, AAA, 2006] is applied for that analytical integration.

## 6.7 EDed2geo

This function is run only if `difforder > 1`. It identifies which edges see which other edges, and stores this information in a struct `edgetoedgedata`.

Input: `edgedata, planedata, Sdata, Rdata`  
Output: `edgetoedgedata`

## 6.8 EDinteg\_submatrix

This function is run only if `difforder > 1`. It identifies and sets up the submatrix structure for the subsequent integral equation solving, by the function `EDintegral_convex_tf`.

Input: `edgedata.edgelenhvec, edgedata.closwedangvec, edgedata.planesatedge, edgetoedgedata, controlparameters.ngauss, controlparameters.discretizationtype,`  
Output: `Hsubmatrixdata`

See notes in Section 6.9

## 6.9 EDintegral\_convex\_tf

This function is run only if `difforder > 1`. It computes the accumulation of higher-order diffraction, from order 2 up to a specified diffraction order. The result is stored in the transfer function `tfinteqdiff`.

The higher-order edge diffraction is computed with the numerical solution of the edge source integral equation (ESIE) presented in [Asheim, JASA, 2013].

The solution involves two stages. In a first stage, so-called edge source amplitudes are computed. In a second stage the diffracted sound pressure at receiver points is computed by "propagating the edge source signal to the external field points" by computing a double integral.

**Input:** `envdata, planedata, edgedata, edgetoedgedata, Hsubmatrixdata, Sdata, Sinputdata.doaddsources, Sinputdata.sourceamplitudes, Sinputdata.doallSRcombinations, Rdata, controlparameters, filehandlingparameters`  
**Output:** `tfinteqdiff, timingdata`

#### Notes

The edge-source amplitudes are found by solving the ESIE. The straightforward Nystrom method is used, implying that the integral equation is sampled in discretization points along the edges, here called "edge points" or "gauss points". A Gauss-Legendre quadrature scheme is very efficient for this computation, which gets formulated as a matrix equation:

$$\mathbf{q} = \mathbf{q}_0 + \mathbf{H}\mathbf{q} \quad (2)$$

where  $\mathbf{q}$  is a vertical vector of all the edge source amplitudes to compute. The term  $\mathbf{q}_0$  gives the contribution from the external monopole source(s), and is computed explicitly without any integration.  $\mathbf{H}$  is a huge matrix containing the edge-point-to-edge-point interaction terms, or integral Kernel values. This matrix is computed only if `difforder > 2`, since the  $\mathbf{q}_0$  is the exact solution for `difforder = 2`. The matrix equation is solved by iteration, and each iteration step corresponds to one diffraction order. Thus, if one iteration step is computed, then the resulting  $\mathbf{q}$  will give diffracted sound of maximum diffraction orders 3, etc.

The vector of unknowns to compute,  $\mathbf{q}$ , consists of sections, where each segment contains all combinations, from all edge points on one edge (the "from-edge"), to all edge points on another edge (the "to-edge"). The locations, and identities, of those sections are described in the matrices `Hsubmatrixdata.edgepairlist`, `Hsubmatrixdata.bigmatrixstartnums`, and `Hsubmatrixdata.bigmatrixendnums`. Each of these matrices has `nedgepairs` rows, see Table 16. Each row in `.edgepairlist` gives the "to-edge" number in column 1 and the "from-edge" number in column 2. The same row in `.bigmatrixstartnums` gives the starting position in the  $\mathbf{q}$ -vector. Since edges might have different numbers of edge points, each section of  $\mathbf{q}$  might have a different length.

This subdivision of the  $\mathbf{q}$ -vector into sections leads to that the large  $\mathbf{H}$ -matrix is composed of blocks, or submatrices, and consequently a very sparse structure. These submatrices are stored as individual matrices, `Hsub` (being sparse, they are actually stored as two lists: one of locations, and one of values, see below). The submatrices have different sizes since each submatrix connects one section of the  $\mathbf{q}$ -vector to another. The matrix `Hsubmatrixdata.Hsubmatrix`, of size `[nedgepairs, nedgepairs]`, gives a zero, or an integer. The zero implies that that part of the  $\mathbf{H}$ -matrix is zero, whereas an integer refers to the individual `Hsub`-matrix. There will be a total of `nsub` submatrices, and the matrices `Hsubmatrixdata.listofsubmatrices`, `Hsubmatrixdata.edgetripletlist`, `Hsubmatrixdata.reftoshortlist`, `Hsubmatrixdata.isthinplanetriplet` all have `nsub` rows. Each row in `.edgetripletlist` gives the "to-edge" in pos. 1, the "via-edge" in pos. 2, and the "from-edge" in pos. 3, for the submatrix. The matrix `.listofsubmatrices` contains a re-ordered list of submatrix numbers in column 1. By going through the submatrices in this re-ordered order, the sizes of the submatrix are going through as few changes as possible. This is advantageous for the processing speed, since large matrices don't have to change size more often than necessary. Furthermore, for scattering objects with symmetries, many submatrices will be identical. Therefore, the list `.reftoshortlist` contains the "stand-in" submatrices that can be used: if `.reftoshortlist(72) == 12`, then submatrix 72 can use the contents of submatrix 12, and consequently, no new matrix entries need to be computed for submatrix 72.

Finally, each submatrix is sparse as well, and its contents are stored as two lists: `Hsubdatalistsnn` and `ivuselistsnn`, rather than being stored as a matrices. So, `ivuselistsnn` is a long list of the locations in the submatrix number `nn`, and `Hsubdatalistsnn` contains the corresponding data values. The actual solution of Eq. (2) is done iteratively, that is, with the Neumann approach:

$$\mathbf{q}_N = \sum_{i=0}^N \mathbf{q}_i, \quad \mathbf{q}_i = \mathbf{H}\mathbf{q}_{i-1}, \quad i \geq 1$$

The value for  $N$  has to be set manually through the parameter `controlparameters.difforder`, and  $N = \text{difforder} - 2$ .

As the last step, the sound pressure at the receiver point is computed as a discretized version of a double integral. This is efficiently computed as a dot product

$$p = \mathbf{f} \bullet \mathbf{q}_N$$

where  $\mathbf{f}$  is a vertical vector containing sampled kernel values for the propagation double integral.

## 6.10 EDfindHODpaths

This function is run only if `difforder > 1`, and for the TD implementation in `EDmain_convex_time`. It identifies which higher-order diffraction paths are possible, up to a certain diffraction order, and stores this information in a struct `hodpaths`.

Input: `edgetoedgedata.edgeseesedge, Sdata.visedgesfroms,`  
`Rdata.visedgesfromr, controlparameters.difforder`  
Output: `hodpaths`

## 6.11 EDmakeHODirs

This function is run only if `difforder > 1`, and for the TD implementation in `EDmain_convex_time`. It computes higher-order diffraction irs, and stores them information in a cell variable `irhod`, that might optionally contain each diffraction order separately.

Input: `hodpaths, controlparameters.difforder, elemsize, edgedata,`  
`edgetoedgedata, Sdata, Sinputdata.doaddsources, Sinputdata.sourceamplitudes,`  
`Rdata, envdata.cair, controlparameters.fs, controlparameters.Rstart,`  
`controlparameters.savealldifforders`  
Output: `irhod`