

lamin

HW5 In fig P8.19, $\beta = 200$.

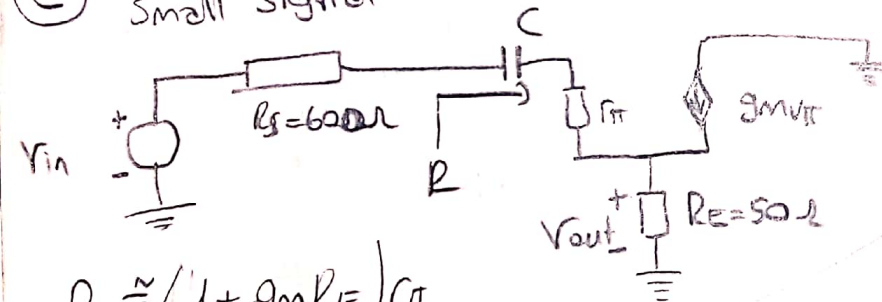
- a) Find I_B so that the transistor is biased at $I_C = 2.5 \text{ mA}$
 b) Find the numerical value of r_{π} .
 c) Write an equation for C so that the low-frequency pole is located at 100 rad/s

② $I_C = \beta \cdot I_B \rightarrow 2.5 \text{ mA} = 200 \cdot I_B \rightarrow I_B = 12.5 \mu\text{A}$

③ $g_m r_{\pi} = \beta \rightarrow r_{\pi} = \frac{\beta}{g_m} = \frac{\beta V_T}{I_C} = \frac{200 \cdot 26 \text{ mV}}{2.5 \times 10^{-3}} = 2.08 \text{ k}\Omega = r_{\pi}$

$g_m = \frac{I_C}{V_T}$

④ Small signal Model



$$R \approx (1 + g_m R_E) r_{\pi}$$

$$\frac{V_{out}}{V_{in}} = \frac{(1 + g_m R_E) \cdot r_{\pi}}{R_S + (1 + g_m R_E) r_{\pi} + \frac{1}{C_s}} \cdot \frac{R_E}{\frac{1}{g_m} + R_E} = \frac{C_s \cdot (1 + g_m R_E) r_{\pi}}{C_s R_S + C_s (1 + g_m R_E) r_{\pi} + 1} \cdot \frac{R_E}{\frac{1}{g_m} + R_E}$$

$$= \frac{C_s \cdot (1 + g_m R_E) \cdot r_{\pi}}{1 + \frac{s}{C_s \cdot (1 + g_m R_E) r_{\pi} + C_s R_S}} \cdot \frac{R_E}{\frac{1}{g_m} + R_E}$$

$$\text{Pole} \rightarrow \frac{1}{C \cdot (1 + g_m R_E) r_{\pi} + C R_S}$$

$$g_m = \frac{I_C}{V_T} = \frac{2.5 \text{ mA}}{26 \text{ mV}} =$$

$$g_m = 96.15 \text{ ms}$$

$$\text{Pole} = \frac{1}{C \cdot (1 + g_m R_E) r_{\pi} + C R_S}$$

$$\text{Pole} = \frac{1}{C \cdot (1 + g_m R_E) r_{\pi} + C \cdot R_S} \Rightarrow g_m = 96.15 \text{ mS}$$

$$R_E = 50 \Omega$$

$$r_{\pi} = 2 \text{ k}\Omega$$

$$\text{Pole} = \frac{1}{C \cdot 11.615 \text{ k}\Omega + C \cdot 600} \rightarrow \text{Pole} = \frac{1}{C \cdot 12.215 \text{ k}\Omega}$$

$\omega = 100 \text{ rad/s}$ pole value

$$100 \text{ rad/s} = \frac{1}{C \cdot 12.215 \text{ k}\Omega} \rightarrow C = \frac{1}{12.215 \times 10^3 \cdot 100} = \frac{10^{-5}}{12.215}$$

$$C = 8.188 \times 10^{-7} \text{ F} = \boxed{0.818 \mu\text{F} = C}$$

Q2. Use short-circuit time constants to estimate the lower half-power frequency for Fig. P8.20; $\beta = 99$, $r_{\pi} = 100 \Omega$

DC bias

$$I_E = (\beta + 1) I_B = 100 I_B$$

$$100 I_B \cdot 10 \Omega + 0.7 + (5.9 \text{ k}\Omega + 7 \text{ k}\Omega) I_B = 12 \text{ V}$$

$$13.9 \text{ k}\Omega \cdot I_B = 11.3 \text{ V}$$

$$\boxed{I_B = 0.812 \text{ mA}}$$

$$\boxed{I_E = 100 I_B = 81.29 \text{ mA}}$$

SC TC

C_1 short in C_2

$$\tau_2 = C_2 [R_S + R_1 \parallel [(1 + g_m R_E) r_{\pi}]]$$

C_2 short in C_1

$$\tau_1 = C_1 [R_2 \parallel [R_1 \parallel R_S + (1 + g_m R_E) r_{\pi}]]$$

(2)

$$Y_1 = C_1 [R_2 \parallel (R_1 \parallel R_S + (1 + g_m R_E) r_{\pi})]$$

$$Y_2 = C_2 [R_S + R_1 \parallel [(1 + g_m R_E) r_{\pi}]]$$

$$R_1 = 5.9k\Omega$$

$$R_2 = 7k\Omega$$

$$R_E = 10\Omega$$

$$R_S = 1k\Omega$$

$$Y_1 = C_1 [7k \parallel \underbrace{[5.9k \parallel 1k]_{855} + \underbrace{(1 + 9.9) \cdot 100}_{1090}}_{1522.13}]$$

$$r_{\pi} = \frac{\beta \cdot V_T}{I_C} = \frac{V_T}{I_B} = \frac{26mV}{I_B} = 100$$

$$I_B = 0.26mA \div 0.812mA$$

$$g_m = \frac{\beta}{r_{\pi}} = 0.99 \Omega^{-1}$$

$$Y_1 = 1522.13 C_1$$

$$Y_2 = C_2 [1k + \underbrace{5.9k \parallel [1090]}_{920.02}]$$

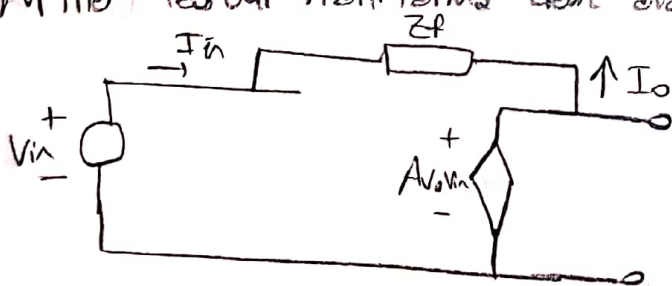
$$Y_2 = C_2 \cdot 1920.02$$

$$1920.02$$

Q3.

In a particular MOSFET amplifier for which the midband voltage gain between gate and drain is $-27V/V$, the NMOS transistor has $C_{gs} = 0.3pF$ and $C_{gd} = 0.1pF$. What input capacitance would you expect? For what range of signal-source resistances can you expect the 3dB frequency to exceed 10MHz? Neglect the effect of r_o .

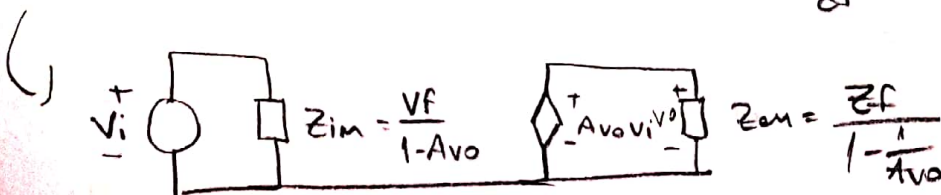
Miller Tereimi hatirlama done analiz



$$I_{in} = \frac{V_{in} - V_o}{Z_f} = \frac{V_i - A_{v0} V_i}{Z_f}$$

$$= V_i \frac{(1 - A_{v0})}{Z_f}$$

$$\frac{V_{in}}{I_{in}} = \frac{Z_f}{1 - A_{v0}}, \quad I_o = \frac{V_o - V_{in}}{Z_f} = \frac{V_o - \frac{V_o}{A_{v0}}}{Z_f} = \frac{V_o}{Z_f} \left(1 - \frac{1}{A_{v0}}\right)$$



Tipik verseyim $A_{vo} < 0$ ve $|A_{vo}| > 1$

and let $Z_f = \frac{1}{sC_f}$ then $Z_{in} = \frac{1}{sC_f(1-A_{vo})}$

capacitance
 $C_f(1-A_{vo})$

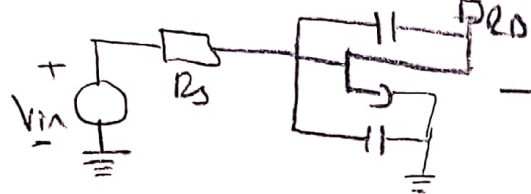
$$Z_{om} = \frac{1}{sC_f(1-\frac{1}{A_{vo}})}$$

capacitance

$$C_f(1-\frac{1}{A_{vo}}) |A_{vo}| \gg 1 \text{ ise}$$

$$\approx C_f$$

Basic CMOSFET amplifier



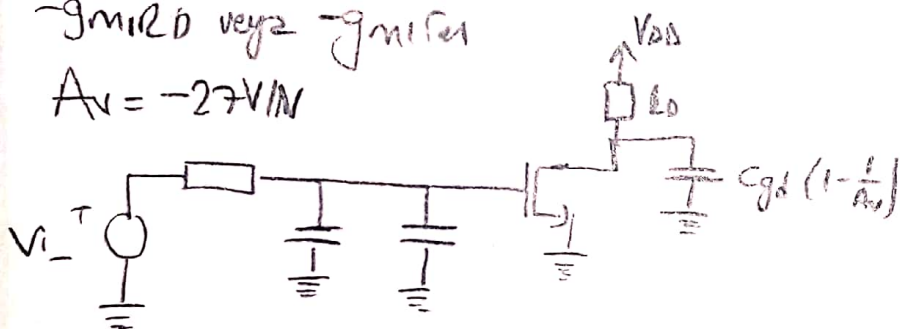
midband voltage gain

$$-g_{m1}(R_D || r_{o1}) \approx -g_{m1}R_D$$

$-g_{m1}R_D$ veya $-g_{m1}r_{o1}$

$$A_v = -27V/V$$

R_D bulunamazsa, r_{o1} değeri $-g_{m1}r_{o1}$ olur



OCTC Method ($V_i = 0$ için)

$$C_1 = C_{gs} + C_{gd}(1-A_v) \quad R_1 = R_S \quad C_2 = (1-\frac{1}{A_v})C_{gd}$$

$$T_1 = C_1 R_1 = [C_{gs} + C_{gd}(1-A_v)] R_S$$

$$C_2 = C_{gd}(1-\frac{1}{A_v}) \quad C_2 \text{ } R_2 \text{ 'yi görüyor} \quad R_2 = R_D || r_{o1}$$

$$T_2 = C_2 R_2 = [C_{gd}(1-\frac{1}{A_v})] [R_D || r_{o1}]$$

$$W_{3dB} \approx \frac{1}{T_1 + T_2} = \frac{1}{C_1 R_1 + C_2 R_2} = \frac{1}{(C_{gs} + C_{gd}(1-A_v)) R_S + [C_{gd}(1-\frac{1}{A_v})] [R_D || r_{o1}]}$$

$$T_1 \gg T_2 \rightarrow W_{3dB} \approx \frac{1}{T_1}$$

$$\forall W_{3dB} = 2\pi f_{3dB} = \frac{1}{R_s [C_{gs} + C_{gd}(1-A_v)]}$$

$$2\pi \times 10 \times 10^6 = \frac{1}{R_s [0.3 \times 10^{-12} + 0.1 \times 10^{-12}(2.8)]}$$

$$C_{gs} = 0.3 \text{ pF}$$

$$C_{gd} = 0.1 \text{ pF}$$

$$A_v = -2.8 \text{ V/V}$$

$$R_s = \frac{1}{2\pi \times 10^7 \times 3.1 \times 10^{-12}} = \frac{10^5}{2\pi \times 3.1} = \boxed{5.134 \text{ k}\Omega = R_s}$$

$W_{3dB} > 2\pi \cdot 10 \text{ MHz}$ calculate use $R_s < 5.134 \text{ k}\Omega$ small

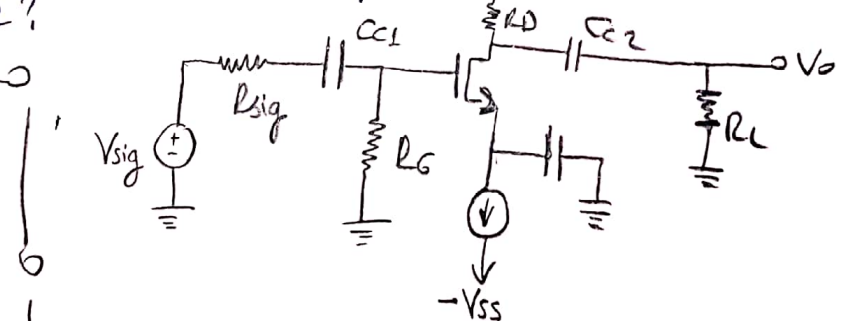
In a fet amplifier, such as that in Fig. 4.49 (a). the resistance of the source $R_{sig} = 100 \text{ k}\Omega$, amplifier input resistance (which is due to the biasing network) $R_{in} = 100 \text{ k}\Omega$, $C_{gs} = 1 \text{ pF}$, $C_{gd} = 0.2 \text{ pF}$, $g_m = 3 \text{ mA/V}$, $r_o = 50 \text{ k}\Omega$, $R_D = 8 \text{ k}\Omega$ and $R_L = 10 \text{ k}\Omega$. Determine the expected 3-dB cut-off frequency f_H and the midband gain. In evaluating ways to double f_H , a designer considers the alternatives of changing either R_{out} or R_{in} . To raise f_H as described what separate change in each would be required? What midband voltage gain results in each case?

SCTC Method

$$V_{sg} = 0 \text{ i.e. in}$$

$$V_{DD} - V_{SS} \rightarrow \text{gnd}$$

I is open circuit.



$$\tau_{e1} = C_{c1} R_{c1} \rightarrow R_{c1} (C_{c1} \text{ in } \text{forward direction}) \Rightarrow R_{sig} R_G \rightarrow C_{c1} \text{ is } \text{dominant}$$

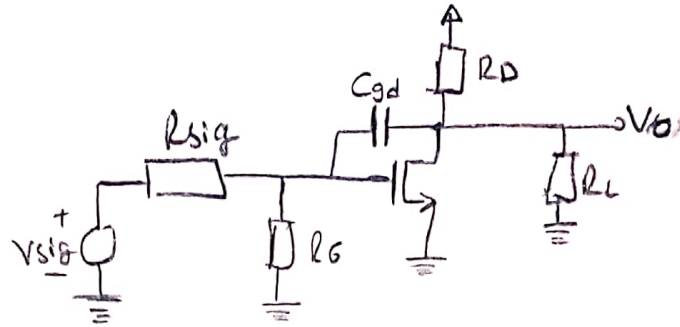
$$\tau_{e2} = C_{c2} R_{c2} \rightarrow R_{c2} (C_{c2} \text{ in } \text{reverse direction}) \Rightarrow (R_D || r_o + R_L) \rightarrow C_{c2} \text{ is } \text{dominant}$$

$$\tau_{e3} = C_s R_{cs} \rightarrow R_{cs} (C_s \text{ in } \text{reverse direction}) \Rightarrow \frac{1}{g_m} \rightarrow C_{c1} \text{ is } \text{dominant}$$

$$W_L = \frac{1}{T_{e1}} + \frac{1}{T_{e2}} + \frac{1}{T_{e3}} = \frac{1}{C_{c1} \cdot (R_{sig} + R_G)} + \frac{1}{C_{c2} \cdot (R_D \parallel R_L \parallel R_O + R_L)} + \frac{1}{C_S \cdot \frac{1}{g_m}}$$

High freq. cutoff

C_{c1}, C_{c2} ve C_S



Midband gain = $A_v = \frac{R_G}{R_{sig} + R_G} (-g_m) [R_D \parallel R_L \parallel R_O]$ Bu ortaki paralel kapasitör çiftlik görünüyor değil

$T_{H1} = [C_{gs} + C_{gd}(1 - A_v)] \cdot [R_{sig} \parallel R_G]$

$C_{gd}(1 - \frac{1}{A_v})$ oper. current

$T_{H2} = [C_{gd}(1 - \frac{1}{A_v})] [R_D \parallel R_L \parallel R_O]$

$W_H = \frac{1}{T_{H1} + T_{H2}}$ $T_{H1} \gg T_{H2}$ ise $W_H \approx \frac{1}{T_{H1}}$

$= W_H = \frac{1}{[C_{gs} + C_{gd}(1 - A_v)] \cdot [R_{sig} \parallel R_G]}$

$C_{gs} = 1 \text{ pF}$

$C_{gd} = 0.2 \text{ pF}$

A_v bulunacak

$R_{sig} = 100 \text{ k}\Omega$

$R_G \rightarrow$ bilinmiyor

$g_m = 3 \text{ mS}$

$R_D = 8 \text{ k}\Omega$

$R_L = 10 \text{ k}\Omega$

$R_O = 50 \text{ k}\Omega$

$A_v = \frac{R_G}{100 \text{ k}\Omega + R_G} (-3) \cdot \left[\frac{80 \text{ k}\Omega}{18} \parallel 10 \text{ k}\Omega \parallel 50 \text{ k}\Omega \right]$

$R_G = 100 \text{ k}\Omega$ olsun

$A_v = \frac{1}{1} \cdot -3 \cdot 408.16$

$A_v = -612.24$

★ Hesaplamız $R_G = 100 \text{ k}\Omega$ için yapılmıştır.

(6)

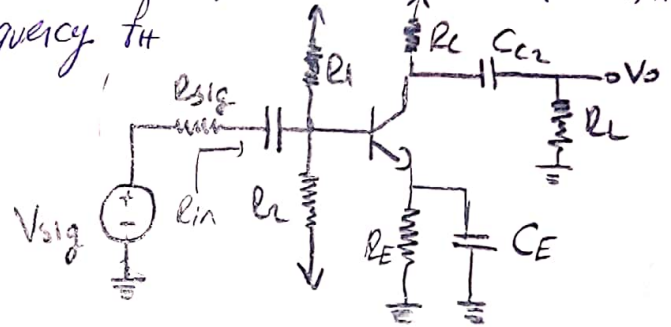
$$W_H = \frac{1}{[10^{-12} + 0.2 \cdot 10^{-12} \cdot (1 - (-611.24))]} \cdot [100k \parallel 100k]$$

$$W_H = 161749.48$$

Solu

$$\rightarrow R_G = 100k \text{ için}$$

Consider the common-emitter amplifier of Fig. P5.159 under the following conditions: $R_{sig} = 5k\Omega$, $R_1 = 33k\Omega$, $R_2 = 22k\Omega$, $R_G = 39k\Omega$, $R_C = 4.7k\Omega$, $R_E = 5.6k\Omega$, $V_{CC} = 5V$. The dc emitter current can be shown to be $I_E = 0.3mA$ at which $\beta_0 = 120$, $r_o = 300k\Omega$, and $r_x = 50\Omega$. Find the input resistance R_{in} and the midband gain A_{m_i} . If the transistor is specified to have $f_T = 700MHz$ and $C_{\mu} = 1pF$ find the upper 3-dB frequency f_H .



SCTC method for W_L

$$Y_{C1} = C_{C1} \cdot R_{CC1}$$

$R_{CC1} = C_{C1}$ 'in görüldüğü direnç

$$R_{CC1} = R_{sig} + (R_1 \parallel R_2 \parallel r_{\pi})$$

$$Y_1 = C_{C1} \cdot (R_{sig} + (R_1 \parallel R_2 \parallel r_{\pi})) = C_{C1} \cdot (5k\Omega + (33k\Omega \parallel 22k\Omega \parallel 10.4k\Omega))$$

$$Y_1 = C_{C1} \cdot (5k\Omega + 5.816k\Omega)$$

$$Y_1 = C_{C1} \cdot 10.816k\Omega$$

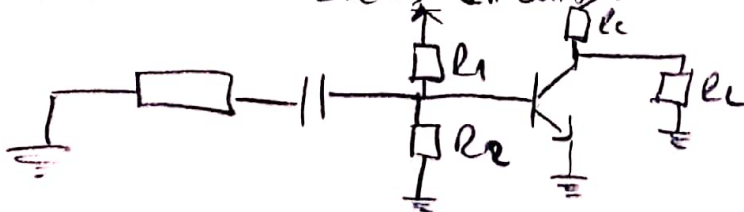
C_{C1} 'in solda görüldüğü direnç R_{sig}
" " sağda " " $R_1 \parallel R_2 \parallel r_{\pi}$

$$r_{\pi} = \frac{\beta \cdot V_T}{I_C} = \frac{120 \cdot 26 \times 10^{-3}}{0.3 \times 10^{-3}}$$

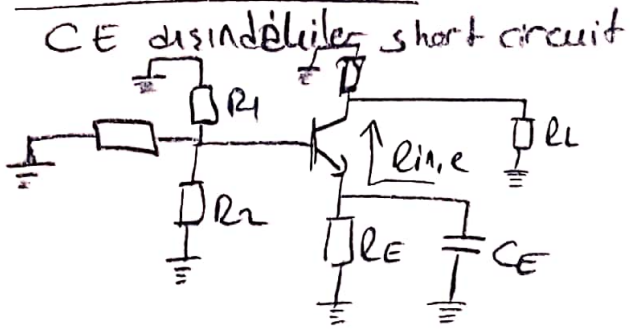
$$I_C \approx I_E$$

$$r_{\pi} = 10.4k\Omega$$

Bu methodda sadece C_{C1} birlendi
diğer kapasitörler short circuit



SCTC for C_E



$$Y_{CE} = C_E \cdot R_{CE}$$

R_{CE} : C_E 'in gördüğü direnç.

$$R_{in,e} \parallel R_E = R_{CE}$$

$$R_{in,e} = \frac{r_{\pi} + R_B}{1 + \beta}$$

$$Y_{CE} = C_E \cdot \left(\frac{r_{\pi} + R_B}{1 + \beta} \parallel R_E \right)$$

$$Y_{CE} = C_E \cdot \left(\frac{10.4k\Omega + 3.626k\Omega}{121} \parallel 39k\Omega \right)$$

$$115.92 \parallel 39k\Omega \approx 115.92$$

$$Y_{CE} = C_E \cdot 115.92$$

$$r_{\pi} = 10.4k\Omega$$

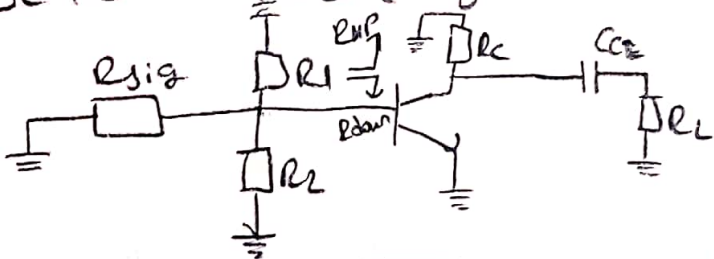
$$R_B = R_{sig} \parallel R_1 \parallel R_2$$

$$R_B = 5k\Omega \parallel 33k\Omega \parallel 22k\Omega$$

$$R_B = 3.626k\Omega$$

$$R_E = 39k\Omega$$

SCTC for C_{C2} (kaynakları çıkar C_{C2} disindeli kapasitörler kısaltırsak)



$$Y_{CC2} = R_{CC2} \cdot C_{C2}$$

R_{CC2} : C_{C2} 'nin gördüğü direnç

R_{CC2} : sağında R_L görür

R_{CC2} : solunda gördüğüne R_{left} diyelim.

$R_{down} = r_{in}$ test kaynağı ekleyelim

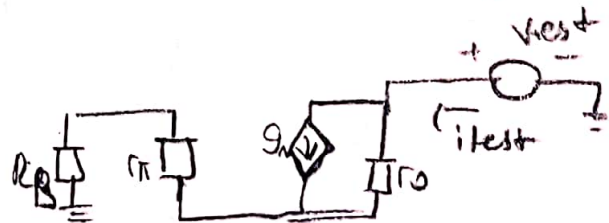
$$R_{left} = R_{up} \parallel R_{down}$$

R_{up} , R_{down} belirtilen bölge dirençleri

$$R_{up} = R_C$$

$$R_{left} = R_{up} \parallel R_{down} = R_C \parallel r_o$$

$$R_{CC2} = R_L + R_C \parallel r_o$$



$$\frac{V_{test}}{i_{test}} = R_{down} = r_o$$

$$T_{C2} = C_2 R_{C2} = C_2 \cdot (R_L + R_C \parallel r_o)$$

$$T_{C2} = C_2 \cdot (5.6k\Omega + \underbrace{4.7k\Omega \parallel 300k\Omega}_{\approx 4.7k\Omega})$$

$$R_L = 5.6k\Omega$$

$$r_o = 300k\Omega$$

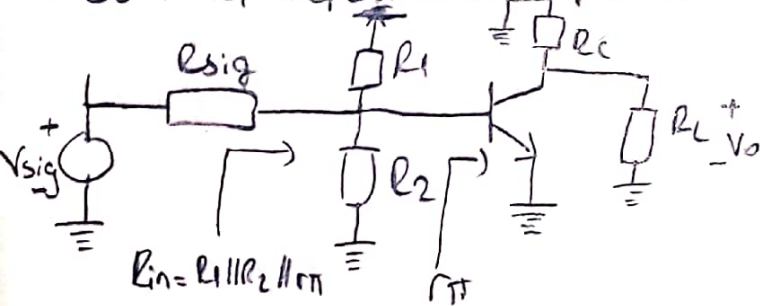
$$R_C = 4.7k\Omega$$

$$T_{C2} = C_2 (10.3k\Omega)$$

$$W_L = \frac{1}{T_{C1}} + \frac{1}{T_{C2}} + \frac{1}{T_{C3}} = \frac{1}{C_1 \cdot 10.816k\Omega} + \frac{1}{C_2 \cdot 10.3k\Omega} + \frac{1}{C_3 \cdot 115.9}$$

Midband ile R_{in} elde etme

midband'de tüm kapasitörler ~~short~~ short circuit } Bu iki değeri bulmaya
 \rightarrow BJT iç kapasitörleri open circuit } göre devre çizilebilir



$$\frac{V_o}{V_{sig}} = A_m = (-g_m) \cdot \underbrace{\left[R_C \parallel r_o \parallel R_L \right]}_{\frac{V_o}{I_{out}}}$$

$$= \underbrace{\left(-11.53 \times 10^{-3} \right)}_{\frac{I_{out}}{V_{sig}}} \cdot \underbrace{(2.55k\Omega)}_{\frac{V_o}{I_{out}}}$$

$$g_m = \frac{I_E}{r_{\pi}} = \frac{120}{10.4k\Omega}$$

$$g_m = 11.53mS$$

$$R_{in} = R_1 \parallel R_2 \parallel r_{\pi} = 33k\Omega \parallel 22k\Omega \parallel 10.4k\Omega = 5.816k\Omega$$

$$A_m = -29.40$$

$$R_C = 4.7k\Omega$$

$$r_o = 300k\Omega$$

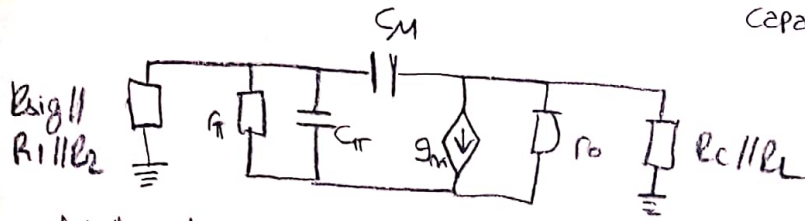
$$R_L = 5.6k\Omega$$

$$R_C \parallel r_o \parallel R_L$$

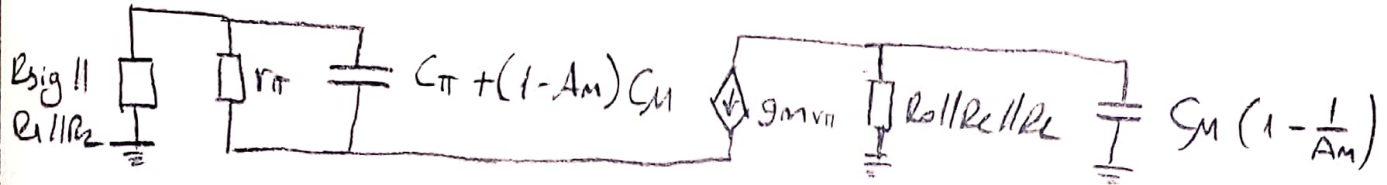
$$R_C \parallel R_L$$

$$R_{sig} = 5k\Omega$$

$W_4 \rightarrow$ OCTC kullanarak \rightarrow bağımsız kaynakları diğer
capacitörler short circuit



Miller theorem



$$1 - A_m \gg 1 \quad 1 < 1 - \frac{1}{A_m} < 2$$

$$A_m < 0$$

$$C_1 = C_\pi + (1 - A_m) C_M$$

$$C_2 = C_M \left(1 - \frac{1}{A_m}\right)$$

= open circuit C_2 , C_1 'in görüldüğü direnç R_{C1}

$$R_{C1} = R_{sig} \parallel R_1 \parallel R_2 \parallel r_\pi \quad \text{and} \quad T_{C1} = C_1 R_{C1} = C_1 (R_{sig} \parallel R_1 \parallel R_2 \parallel r_\pi)$$

$$T_{C1} = C_1 (5k \parallel 33k \parallel 10.4k)$$

$$T_{C1} = C_1 (3.06k)$$

open circuit C_1 , R_{C2} : C_2 'nin görüldüğü direnç.

$$R_{C2} = r_o \parallel R_c \parallel R_L$$

$$T_{C2} = R_{C2} C_2 = C_2 (r_o \parallel R_c \parallel R_L)$$

$$= C_2 (300k \parallel 4.7k \parallel 5.6k)$$

$$T_{C2} = C_2 \cdot 2.55k$$

$$r_\pi = 10.4k$$

$$R_{sig} = 5k$$

$$R_1 = 33k$$

$$R_2 = 22k$$

$$R_E = 3.9k$$

$$R_C = 4.7k$$

$$R_L = 5.6k$$

$$V_{CC} = 5V$$

$$I_C = 0.3mA$$

$$\beta_0 = 120$$

$$\beta_0 = 300k$$

$$r_\pi = 50k$$

$$C_M = 1pF$$

$$f_T = 700MHz$$

$$W_H = \frac{1}{\tau_{C1} + \tau_{C2}} = \frac{1}{C_{C1} \cdot 306 \mu s + C_{C2} \cdot 2.55 \mu s}$$

$$2\pi f_T = \frac{g_m}{(C_\pi + g_m)}$$

$$g_m = \frac{I_E}{V_T} = \frac{\beta}{\beta+1} I_E \cdot \frac{1}{V_T}$$

$$C_\pi + 10^{-12} = \frac{11.90 \times 10^{-3}}{2\pi \cdot 700 \cdot 10^6}$$

$$\beta = 120$$

$$\frac{120}{121} \cdot \frac{0.3 \cdot 1}{25 \times 10^{-3}} =$$

$$g_m = 11.90 \text{ mS}$$

$$C_\pi + 10^{-12} = 2.705 \times 10^{-12}$$

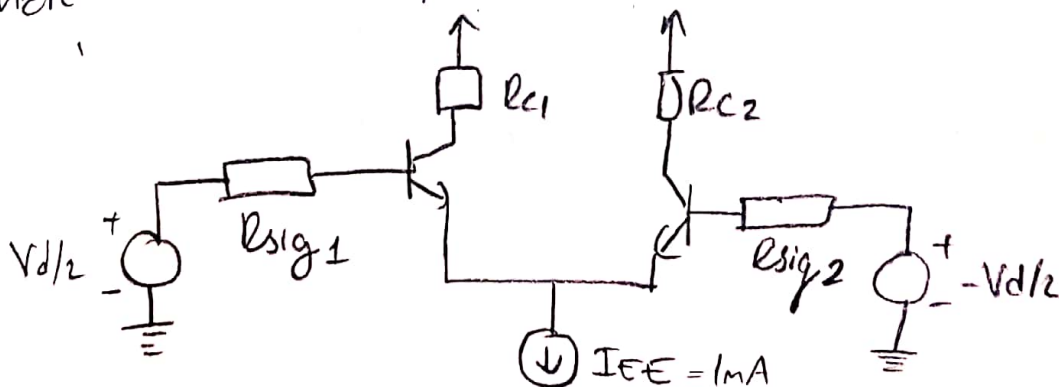
$$f_T = 700 \text{ MHz}$$

$$C_M = 1 \text{ pF}$$

$$C_\pi = 1.705 \times 10^{-12} \text{ F} = 1.705 \text{ pF} \quad \star$$

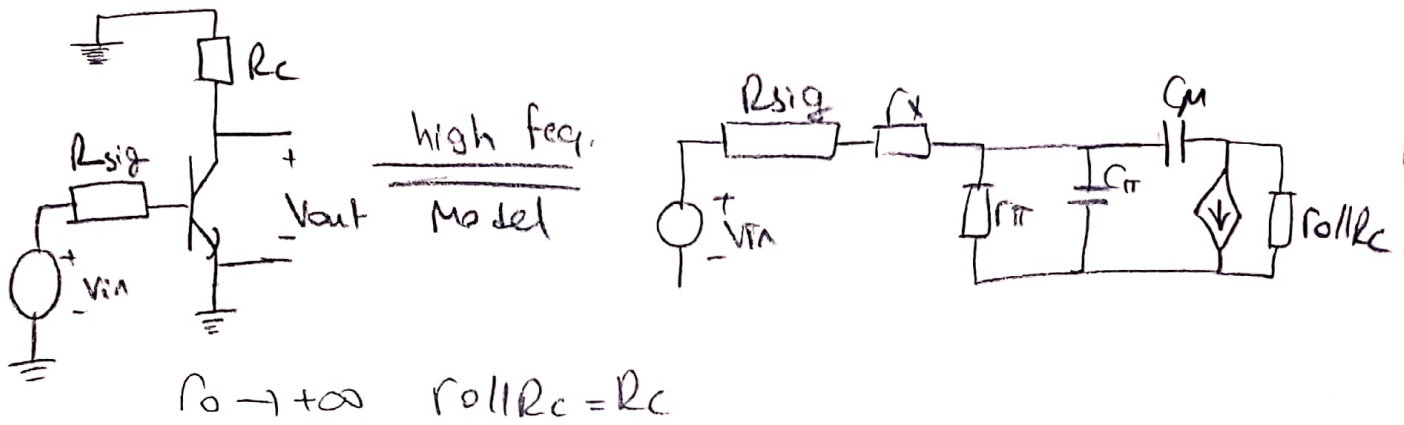
Q6. A BJT differential amplifier operating with a 1-mA current source uses transistors for which $\beta = 100$, $f_T = 600 \text{ MHz}$, $C_M = 0.5 \text{ pF}$, and $r_x = 100 \Omega$. Each of the collector resistances is $10 \text{ k}\Omega$, and R_o is very large. The amplifier is fed in a symmetrical fashion with a source resistance of $10 \text{ k}\Omega$ in series with each of the two input terminals.

- Sketch the differential half-circuit and its high-frequency equivalent circuit.
- Determine the low-frequency value of the overall differential gain.
- Use Miller's theorem to determine the input capacitance and hence estimate the 3-dB frequency and the gain-bandwidth product.



②

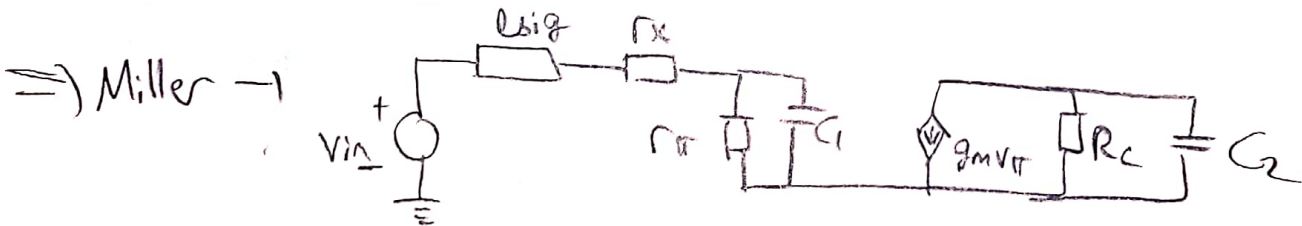
Half Circuit



$$A = \text{midband gain} = \frac{V_c}{V_b} = -g_m R_c$$

$$\text{midband gain } A_m = \frac{r_{\pi}}{r_{\pi} + R_{sig} + r_x} \cdot (-g_m R_c)$$

Miller's theorem - OCTC



$$C_1 = C_{\pi} + C_{\mu}(1 - A) \quad C_2 = C_{\mu}\left(1 - \frac{1}{A}\right) = C_{\mu}\left(1 + \frac{1}{g_m R_c}\right)$$

OCTC C_2 open circuit R_{c1} : C_1 'in görülgü direnc.

$$R_{c1} = r_{\pi} || (R_{sig} + r_x) \quad Y_{c1} = C_1 R_{c1} = C_1 (r_{\pi} || (R_{sig} + r_x))$$

OCTC C_1 open R_{c2} : C_2 'in görülgü direnc.

$$R_{c2} = R_c$$

$$W_H = \frac{1}{Y_{c1} + Y_{c2}} \approx \frac{1}{Y_{c1}} = \frac{1}{C_1 (r_{\pi} || (R_{sig} + r_x))}$$

$$Y_{c1} \gg Y_{c2}$$

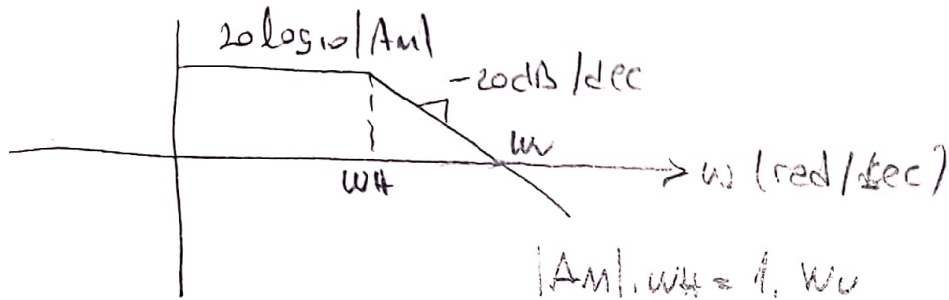
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①

Gain-Bandwidth Product

$$GBW = |A_m| \frac{\omega_H}{2\pi} = |A_m| \cdot f_H$$

$$= \left| \frac{r_{\pi}}{r_{\pi} + r_x + R_{sig}} (-g_m R_c) \right| \cdot \frac{1}{2\pi C_{c1}}$$



$$\frac{GBW}{2\pi} = \frac{\omega_u}{2\pi} = f_u$$

$$f_T = \frac{g_m}{2\pi(C_{\mu} + C_{\pi})} \rightarrow \underbrace{C_{\mu} + C_{\pi}}_{0.5 \text{ pF}} = \frac{g_m}{2\pi f_T} = \frac{0.02}{2\pi \cdot 600 \times 10^6}$$

$$C_{\mu} + C_{\pi} = 5.305 \times 10^{-12}$$

$$C_{\pi} = 5.305 \times 10^{-12} - 0.5 \times 10^{-12} = 4.805 \times 10^{-12} = \boxed{4.80 \text{ pF} = C_{\pi}}$$

⑬