

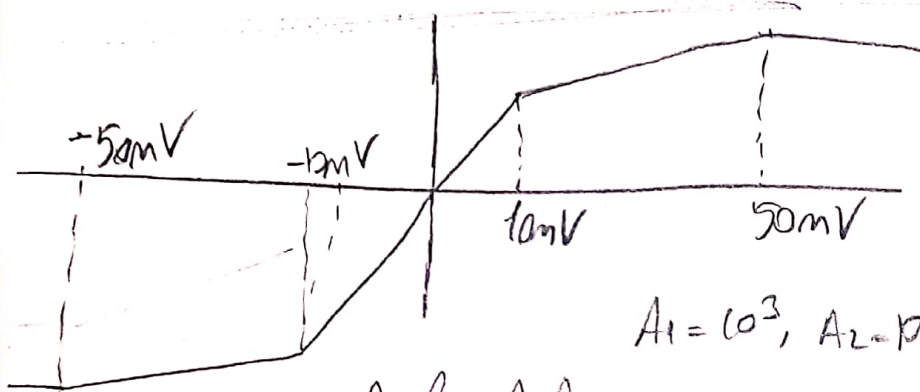
Q1. A particular amplifier has a nonlinear transfer characteristic that can be approximated as follows.

(a) For small input signals $|v_i| \leq 10 \text{ mV}$, $v_o/v_i = 10^3$

(b) For intermediate input signals, $10 \text{ mV} \leq |v_i| \leq 50 \text{ mV}$, $v_o/v_i = 10^2$

(c) For large input signals, $|v_i| \geq 50 \text{ mV}$, the output saturates.

If the amplifier is connected in a negative-feedback loop, find the feedback factor β that reduces the factor of 10 change in gain to only a 10% change. What is the transfer characteristic of the amplifier with feedback?



$$A_{1,f} = \frac{A_1}{1 + A_1\beta}$$

$$A_1 = 10^3, A_2 = 10^2 \quad A_{2,f} = \frac{A_2}{1 + \beta A_2}$$

$$A_{1,f} > A_{2,f}$$

$$A_{1,f} = A_{2,f}(1 + 10^6)$$

$$\frac{A_1}{1 + A_1\beta} = \frac{A_2}{1 + \beta A_2} \rightarrow \frac{10^3}{1 + \beta \cdot 10^3} = \frac{10^2}{1 + 10^2\beta} \quad (1.1)$$

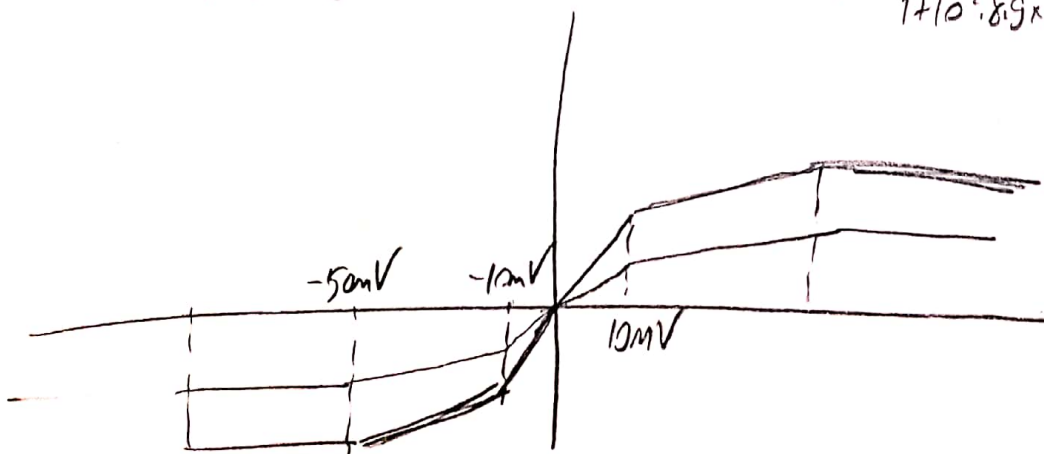
$$\frac{10 + 1000\beta}{1 + 1000\beta} = 1.1 \rightarrow 10 + 1000\beta = 1.1 + 1100\beta$$

$$100\beta = 8.9$$

$$\beta = 8.9 \times 10^{-2}$$

$$A_{1,f} = \frac{10^3}{1 + 10^3 \cdot 8.9 \times 10^{-2}} = \frac{1000}{90} = 11.1$$

$$A_{2,f} = \frac{10^2}{1 + 10^2 \cdot 8.9 \times 10^{-2}} = \frac{100}{9.9} = 10.101$$



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Q2. A feedback amplifier is to have a closed-loop gain of $A_f = 60\text{dB}$ and a sensitivity of 10% to the open-loop gain A . Determine the open-loop gain with a unity feedback $\beta = 1$

$$A_f = 60\text{dB} \quad 20\log_{10} A_f = 60 \quad A_f = 1000$$

$$\log_{10} A_f = 3$$

$$\frac{\partial A_f}{\partial A} = \frac{\partial A_f}{\partial A} \cdot \frac{A}{A_f} = \frac{1}{\beta A + 1} \cdot \underbrace{\frac{\partial A}{\partial A}}_{100\% = 1} = \frac{1}{1 + \beta A} = 10\% = \frac{1}{10} \quad \beta A = 9$$

$$A_f = \frac{A}{1 + \beta A} = \frac{A}{10} = 1000 \quad \boxed{A = 10,000}$$

$$\beta \cdot A = 9 \quad \boxed{\beta = \frac{9}{10,000} = 9 \times 10^{-4}}$$

Q3. The feedback factor of an amplifier is $\beta = 0.8$. The open-loop gain A can be expressed in Laplace's domain of s as

$$A(s) = \frac{250s}{(1 + 0.1s)(1 + 0.001s)} \quad \text{determine (a) the closed-loop low-frequency gain } A_{of} \quad \text{(b) the closed}$$

$$A(s) = \frac{250s}{\left(1 + \frac{s}{10}\right)\left(1 + \frac{s}{1000}\right)} = A(s) \approx \frac{250s}{\left(\frac{s}{10}\right) \cdot (1)} = 2500$$

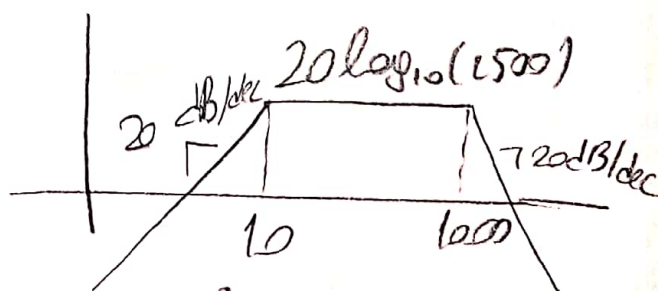
$\approx \frac{s}{10} \quad \approx 1$

$$1 + G\beta = 1 + 2500 \cdot 0.8 = 2001 = A_{of}$$

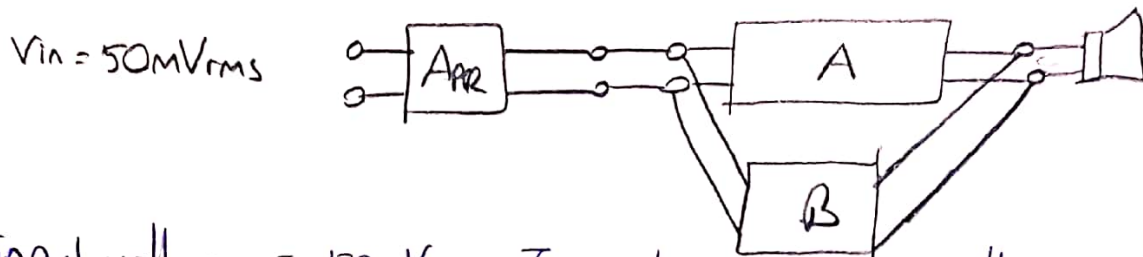
low freq $\rightarrow \frac{10}{1 + G\beta} = \frac{10}{2001} \approx \frac{50}{10000} = 5 \times 10^{-3} \text{ rad/s}$

high freq. $\rightarrow 1000(1 + G\beta) = 1000 \cdot 2001 = 2 \times 10^6 \text{ rad/s}$

$$GBW = 2500 \cdot 1000 = 2.5 \cdot 10^6 \text{ Hz}$$



Q6. Figure Pg.92 shows a nonfeedback amplifier of voltage gain A that delivers $5W$ to a 50Ω speaker when the amplifier



Input voltage is $50mV_{rms}$. The nonlinear distortion in the amplifier output is 1% of the output signal value.

- Find the numerical value of the gain A .
- Find the value of β required in fig P.9.9b to reduce the distortion to 0.1% with the same output signal amplitude.
- Find the value of gain A_{pr} required in preamp

$$\frac{V_{rms,out}^2}{R_L} = P_{rms,out} \quad V_{rms,out} = \sqrt{5W \cdot 50\Omega} = 5V_{rms}$$

$$\text{GAIN} \rightarrow A = \frac{V_{rms,out}}{V_{rms,in}} = \frac{5V_{rms}}{50mV_{rms}} = 100$$

$$A = A_{pr} \cdot \frac{A}{1+A\beta} \quad A_{pr} = 1+A\beta$$

First config. gain preamp. gain amp. feedback

$$\text{Distortion}_2 = \frac{\text{Distortion}_1}{1+A\beta} \Rightarrow 0.1\% = \frac{1\%}{1+A\beta}$$

$$A_{pr} = 1+A\beta = 10 \quad \frac{A}{1+A\beta} = 10$$

$$A\beta = 10 \quad \beta = \frac{10}{A} = \frac{10}{100} = 0.1$$

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Q5. For an amplifier with shunt feedback. $R_{if} = 140\Omega$, $R_o = 2k\Omega$, $R_{of} = 26k\Omega$, $A_f = 20$, $\omega_H = 10^4 \text{ rad/s}$, $\omega_{Lf} = 10 \text{ rad/s}$

find R_i , A , β , ω_H , and ω_L

Changing a resistor in amplifier A from $10k\Omega$ to $11k\Omega$ changes A_f from 20 to 21. Use sensitivity to find the new value of A.

$$\text{shunt feedback} \Rightarrow \frac{R_i}{1+\beta A} = R_{if} \quad R_o = 2k\Omega$$

$$R_{of} = 26k\Omega$$

$$(1+\beta A)R_o = R_{of} \quad 26k\Omega = 2k\Omega(1+\beta A) \quad 1+\beta A = 13 \quad \beta A = 12$$

$$A_f = \frac{A}{1+\beta A} = 20 \Rightarrow A = \underbrace{(1+\beta A)}_{13} \underbrace{A_f}_{20} \quad \boxed{A = 260}$$

$$\beta = \frac{12}{A} = \frac{12}{260} =$$

$$\omega_{H,f} = \omega_H(1+\beta A) = (10^4 \text{ rad/s})(13) = 1.3 \times 10^5 \text{ rad/s}$$

$$\omega_{L,f} = \frac{\omega_L}{(1+\beta A)} \Rightarrow 10 = \frac{\omega_L}{13} \quad \boxed{\omega_L = 130 \text{ rad/s}}$$

$$\boxed{\beta = 0.0461}$$

$$\text{GBW} = A \cdot \omega_H = 260 \cdot 10^4 \text{ rad/s}$$

$$\int_P^{A_f} = \frac{\int_P^A}{1+\beta A}, \quad \int_P^A = \frac{\Delta A_f}{\Delta P} \cdot \frac{P}{A_f} = \frac{1}{1+\beta A} \cdot \frac{\Delta A}{\frac{\Delta P}{P}} = \int_P^A \cdot \frac{1}{1+\beta A}$$

$$\frac{\Delta A_f}{A_f} = \frac{1}{1+\beta A} \cdot \frac{\Delta A}{A} = \frac{21-20}{20} = \frac{1}{13} \cdot \frac{\Delta A}{260}$$

$$A_{\text{sen}} = A + \Delta A = 260 + 169 = 429$$

$$\Delta A = \frac{260 \cdot 13}{20} = 169$$

$$A: \rightarrow \frac{429-260}{260} \cdot 100 = 65\%$$

$$A_f: \rightarrow \frac{21-20}{20} \cdot 100 = 5\%$$

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