

### AIAP Question 3

#### A. Gradient Descent

1.  $h_{\theta}(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2$
2. MSE Cost function:  $\frac{1}{n} \sum_{i=1}^n (h_{\theta}(x^{(i)}) - y^{(i)})^2$
3. We have 3 simultaneous equations:  
 $30 = \theta_0 + 3\theta_1 + \theta_2$  ----- (1)  
 $55 = \theta_0 + 6\theta_1 + \theta_2$  ----- (2)  
 $70 = \theta_0 + 3\theta_1 + 3\theta_2$  ----- (3)  
 $(3) - (2) = 3\theta_1 = 25$   
Thus  $\theta_1 = 25/3$  ----- (4)  
Sub (4) into (3), we have  $45 = 3\theta_2 + \theta_0$  ----- (5)  
 $(1) \times 3 - (5)$ , we get  $\theta_0 = -15$   
Thus  $\theta_2 = 10$

#### B. Regularization

1. Regularization refers to the process where we try to prevent overfitting the model by reducing the coefficient values towards 0. This fitting procedure includes a loss function that is known as residual sum of squares. Coefficients are chosen to minimize the loss function. Unregularized cost functions may not generalize well with future data. For example, a simple regression formula is  $y = a_1 x_1 + a_2 x_2 + b$ . In this case if coefficient  $a_1$  is of a much higher value than  $a_2$ , then variations in  $a_2$  may not be reflected accurately as the predictions will rely on changes in  $a_1$ .  $\lambda$  as a parameter with which we decide on the how much we want to penalize the flexibility of the model. With  $\lambda = 0$ , there is no penalty and this gives a least squares estimate. But as  $\lambda \rightarrow \infty$ , the penalty grows and the coefficient values approach 0.
2. L1 and L2 regularisation refer to Lasso and Ridge regression respectively. The difference is that Lasso penalizes only the high coefficients. Lasso can eliminate all the coefficients in comparison to Ridge.