

Modeling Wine Preferences via Data Mining

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Agenda



Background on Wine

- Wine was once viewed as a luxury good, but is now enjoyed by a wide range of consumers
- Portugal is a top ten wine exporting country
 - Exports of *Vinho Verde* have increased by 36% from 1997 to 2007
- Wine certifications and quality assessments are essential in the wine industry towards enhancing growth



Data Description

- Two large datasets, one for **red wine** and one for **white wine**



	Fixed Acidity	Volatle Acidity	Chloric Acid	Residual Sugar	Chlorides	Free sulfur Dioxide	Total Sulfur Dioxide	Density	pH	Sulphates	Alcohol	Quality
1	7.4	0.700	0.00	1.90	0.076	51	51	0.9978	3.51	0.58	9.4	5
2	7.8	0.880	0.00	2.60	0.098	29	87	0.9988	3.20	0.68	9.8	5
3	7.8	0.760	0.04	2.30	0.092	15	54	0.9970	3.26	0.65	9.8	5
4	11.2	0.280	0.04	1.90	0.071	17	60	0.9980	3.16	0.58	9.8	6
5	7.4	0.700	0.00	1.90	0.076	11	34	0.9978	3.51	0.58	9.4	5
6	7.4	0.680	0.00	1.40	0.075	13	40	0.9978	3.51	0.58	9.4	5
7	7.8	0.690	0.06	1.40	0.069	15	56	0.9964	3.30	0.46	9.4	6
8	7.3	0.650	0.00	1.20	0.065	15	21	0.9946	3.39	0.47	10.0	7
9	7.8	0.580	0.02	2.00	0.073	9	18	0.9968	3.36	0.57	9.5	7
10	7.3	0.590	0.36	4.10	0.071	17	102	0.9978	3.31	0.80	10.5	5
11	6.7	0.580	0.08	1.80	0.087	15	85	0.9959	3.28	0.54	9.2	5
12	7.3	0.590	0.36	4.10	0.071	17	102	0.9978	3.31	0.80	10.5	5
13	5.6	0.615	0.00	1.00	0.089	18	39	0.9943	3.19	0.52	9.9	5
14	7.8	0.610	0.29	1.00	0.114	9	39	0.9974	3.29	1.16	9.1	5
15	8.9	0.620	0.18	3.80	0.176	12	145	0.9986	3.16	0.88	9.2	5
16	8.9	0.620	0.18	1.50	0.176	11	168	0.9986	3.17	0.88	9.2	5

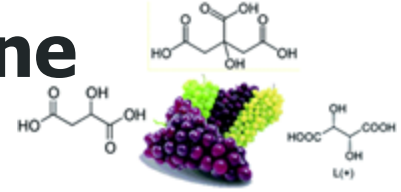
Red Wine

	Fixed Acidity	Volatle Acidity	Chloric Acid	Residual Sugar	Chlorides	Free sulfur Dioxide	Total Sulfur Dioxide	Density	pH	Sulphates	Alcohol	Quality
1	7.0	0.270	0.56	20.70	0.045	45.0	170.0	1.0010	3.00	0.43	8.8	6
2	6.3	0.300	0.34	1.60	0.049	14.0	112.0	0.9940	3.30	0.49	9.5	6
3	6.1	0.280	0.40	6.90	0.050	30.0	87.0	0.9911	3.26	0.44	10.1	6
4	7.2	0.230	0.32	6.50	0.058	47.0	186.0	0.9956	3.19	0.40	9.9	6
5	7.2	0.230	0.32	6.50	0.058	47.0	186.0	0.9956	3.19	0.40	9.9	6
6	6.1	0.280	0.40	6.90	0.050	30.0	87.0	0.9911	3.26	0.44	10.1	6
7	6.2	0.320	0.16	7.00	0.045	30.0	116.0	0.9949	3.18	0.47	9.6	6
8	7.0	0.270	0.56	20.70	0.045	45.0	170.0	1.0010	3.00	0.43	8.8	6
9	6.3	0.300	0.34	1.60	0.049	14.0	112.0	0.9940	3.30	0.49	9.5	6
10	6.1	0.220	0.43	1.50	0.044	28.0	129.0	0.9959	3.22	0.45	11.0	6
11	6.1	0.270	0.41	1.45	0.033	11.0	83.0	0.9908	3.39	0.56	12.0	5
12	6.6	0.230	0.40	4.20	0.051	17.0	109.0	0.9947	3.14	0.53	9.7	5
13	7.9	0.180	0.37	1.20	0.040	16.0	75.0	0.9920	3.18	0.63	10.8	5
14	6.6	0.180	0.40	1.50	0.044	48.0	143.0	0.9912	3.54	0.52	12.4	7
15	8.5	0.420	0.62	19.25	0.040	45.0	172.0	1.0002	2.86	0.67	9.7	5
16	8.5	0.420	0.62	1.50	0.040	45.0	172.0	1.0002	2.86	0.67	9.7	5

White Wine

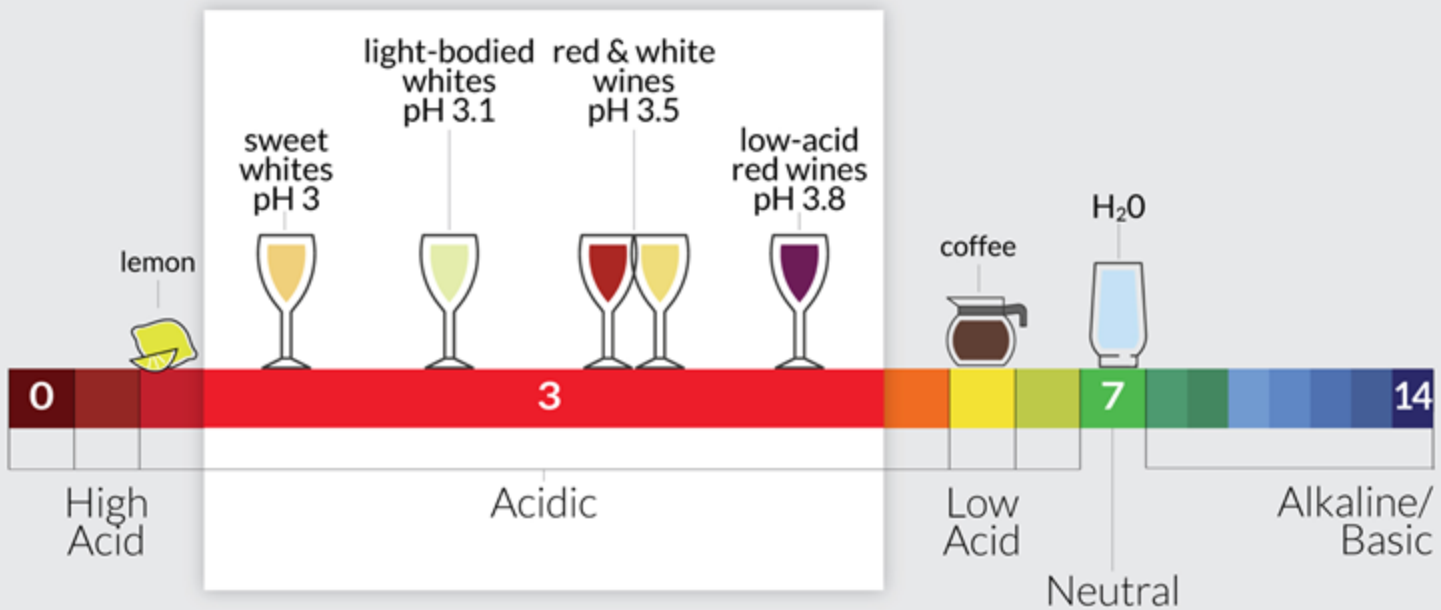
- Objective**
 - Build a **model to predict wine taste preferences** based on distinct variables

Importance of Specific Variables in Wine



- Total **acidity** tells us the concentration of acids present in wine
- **Potential of hydrogen (pH)** level tells us how intense these acids taste
 - Measures the degree of relative alkalinity of a liquid on a scale of 0 to 14, with 7 being neutral
- Winemakers use **pH** as a way to measure ripeness in relation to **acidity**
 - Low pH wines will taste tart and crisp
 - Higher pH wines will taste flat and lack freshness
 - Most importantly, higher pH wines are more susceptible to bacterial growth, as bacteria thrive in higher pH environments

pH Scale



Ideal Acidity for Wine

- Ideal pH range for red wine is **3.3 - 3.6**
- Ideal pH range for white wine is **3.0 - 3.4**
- Warmer climates result in higher sugar and lower acidity, whereas cooler climates result in lower sugar and higher acidity
- In a less acidic environment, a winemaker needs to compensate with higher doses of sulfur dioxide (SO₂) to keep bacteria away
 - E.g. a red wine with a pH of 3.9 would require about 60 mg/L of free SO₂ to inhibit bacteria whereas a similar wine but with a pH of 3.2 would only require about 13 mg/L

How Winemakers Control for Acidity

- Wines of **different acidity levels** can be **blended** to increase or lower the pH
- **Acid reduction** using potassium bicarbonate (KHCO_3) or agents such as ACIDEX to remove acidity and raise the pH
- **Cold stabilization** of wine can be used to increase or decrease pH
- **H₂O** can be added to wine to **dilute** its acidity and increase the pH
- **Malolactic fermentation** can raise the pH and alter the acidity of wine

Multiple Linear Regression

- Response/Dependent variable(s)
 - Wine Quality
- Regressor/Independent variable(s):
 - Fixed Acidity, Volatile Acidity, Citric Acid, Residual Sugar, Chlorides, Free Sulfur Dioxide, Total Sulfur Dioxide, Density, pH, Sulphates, Alcohol
- Training and Test sets
 - Red wine
 - Red training set: [1:800,]
 - Red test set: [801:nrow(red),]
 - White wine
 - White training set: [1:2400,]
 - White test set: [2401:nrow(white),]

```
> dim(red)
[1] 1599  12
> dim(white)
[1] 4898  12
```

Assumptions for Regression

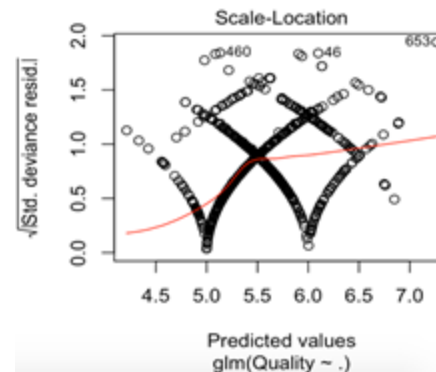
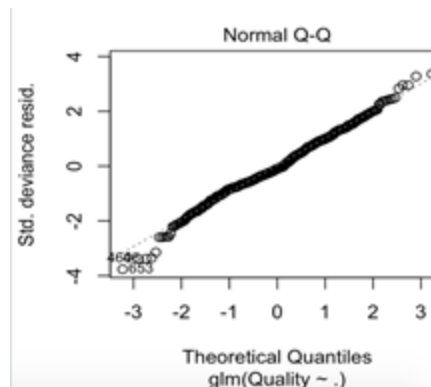
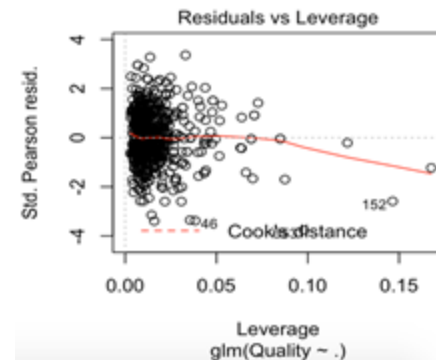
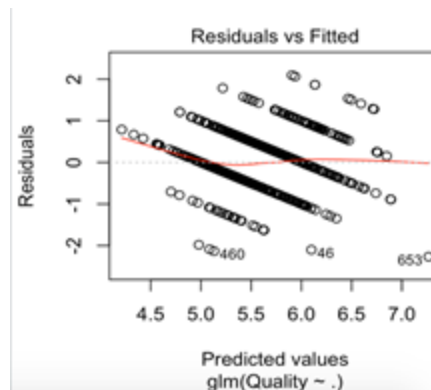
- **L.I.N.E.** assumptions/conditions must be met within both datasets to draw inferences from or make predictions from the model
 - **L**inearity
 - Relationship between dependent and independent variables is linear
 - **I**ndependence of Errors
 - No correlation between consecutive residuals
 - Each independent variable can be tested using VIF values
 - **N**ormality of Error
 - Residuals are normally distributed
 - **E**qual Variance
 - Residuals have a constant variance at every level of x

```
#assumptions for multiple linear regression - red  
Rm<-lm(Quality~., data=Rtrain)  
plot(Rm)
```

```
#assumptions for multiple linear regression - white  
Wm<-lm(Quality~., data=Wtrain)  
plot(Wm)
```

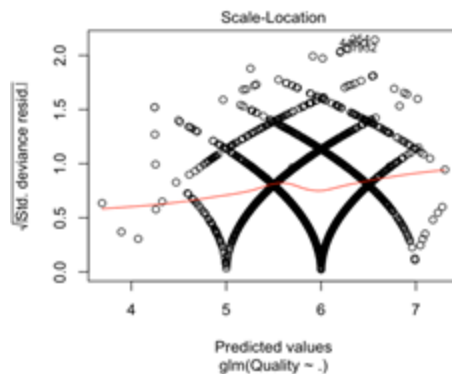
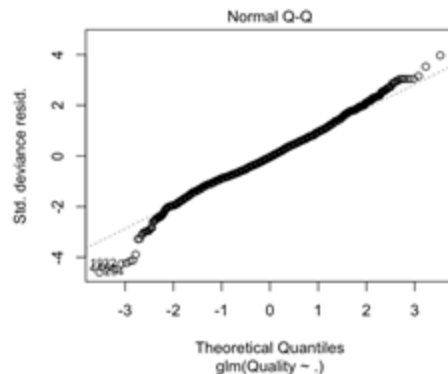
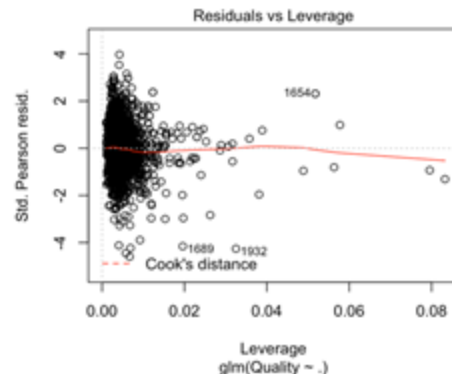
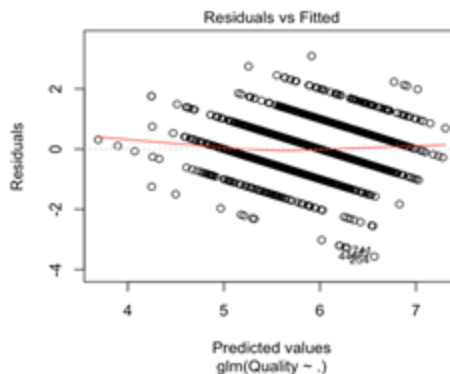
Red Wine Assumptions

- Linearity
 - No significant U-shape in "Residuals vs Fitted"
- Independence of Errors
 - No cyclical patterns in "Residuals vs Leverage"
- Normality of Error
 - Residuals are normally distributed in "Normal Q-Q"
- Equal Variance
 - Inconsistent variance in "Scale-Location"



White Wine Assumptions

- Linearity
 - No significant U-shape in "Residuals vs Fitted"
- Independence of Errors
 - No cyclical patterns in "Residuals vs Leverage"
- Normality of Error
 - Residuals are normally distributed in "Normal Q-Q"
- Equal Variance
 - Inconsistent variance in "Scale-Location"



Model Fitness – Red Wine

- Adjusted R-Squared: 0.3098
 - A low adjusted R-squared indicates that the additional input variables are not adding value to the model
 - Currently, the red wine model is a bad fit
- Significance at $\alpha = 0.05$
 - The model is not statistically significant at $\alpha = 0.05$, as the p-value from the model is 0.6358, which is greater than 0.05

```
> summary(Rm)
```

```
Call:
```

```
lm(formula = Quality ~ ., data = Rtrain)
```

```
Residuals:
```

```
      Min       1Q   Median       3Q      Max
-2.26520 -0.39961 -0.06639  0.44318  2.09402
```

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	13.814270	29.160616	0.474	0.6358
`Fixed Acidity`	0.037628	0.035297	1.066	0.2867
`Volatile Acidity`	-1.023671	0.158995	-6.438	2.10e-10 ***
`Citric Acid`	-0.264088	0.193707	-1.363	0.1732
`Residual Sugar`	0.002101	0.022651	0.093	0.9261
Chlorides	-1.194417	0.508944	-2.347	0.0192 *
`Free sulfur Dioxide`	0.005029	0.003468	1.450	0.1474
`Total Sulfur Dioxide`	-0.004895	0.001044	-4.690	3.22e-06 ***
Density	-10.588858	29.763640	-0.356	0.7221
pH	-0.086864	0.261459	-0.332	0.7398
Sulphates	0.680155	0.138437	4.913	1.09e-06 ***
Alcohol	0.267089	0.033492	7.975	5.36e-15 ***

```
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

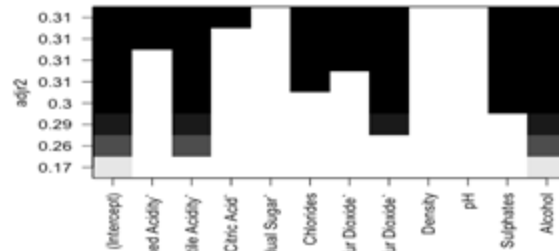
```
Residual standard error: 0.6335 on 788 degrees of freedom
```

```
Multiple R-squared:  0.3193,    Adjusted R-squared:  0.3098
```

```
F-statistic: 33.61 on 11 and 788 DF,  p-value: < 2.2e-16
```

Improved Red Wine Model

- Best regressor(s) to incorporate into model:
 - Used *regsubsets* {leaps}
 - Fixed Acidity, Volatile Acidity, Citric Acid, Chlorides, Free Sulfur Dioxide, Total Sulfur Dioxide, Sulphates, and Alcohol
- Adjusted R-Squared: 0.312
 - Compared to the original values, the relatively higher Adjusted R-Squared indicates the regressors can add more value to the model
- Significance at $\alpha = 0.05$
 - The model is statistically significant at $\alpha = 0.05$, as the p-value from the model is $2e-16$, which is less than 0.05



```
> summary(fitR)
```

Call:

```
lm(formula = Quality ~ `Fixed Acidity` + `Volatile Acidity` +  
  `Citric Acid` + Chlorides + `Free sulfur Dioxide` + `Total Sulfur Dioxide` +  
  Sulphates + Alcohol, data = Rtrain)
```

Residuals:

Min	1Q	Median	3Q	Max
-2.22837	-0.40410	-0.06757	0.44475	2.10794

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	2.962163	0.303470	9.761	< 2e-16	***
`Fixed Acidity`	0.035104	0.017966	1.954	0.0511	.
`Volatile Acidity`	-1.033679	0.157581	-6.560	9.74e-11	***
`Citric Acid`	-0.257201	0.193081	-1.332	0.1832	
Chlorides	-1.160423	0.490300	-2.367	0.0182	*
`Free sulfur Dioxide`	0.004677	0.003417	1.369	0.1715	
`Total Sulfur Dioxide`	-0.004787	0.001016	-4.713	2.88e-06	***
Sulphates	0.682293	0.134398	5.077	4.79e-07	***
Alcohol	0.269975	0.024477	11.030	< 2e-16	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.6325 on 791 degrees of freedom
Multiple R-squared: 0.3189, Adjusted R-squared: 0.312
F-statistic: 46.29 on 8 and 791 DF, p-value: < 2.2e-16

Model Fitness – White Wine

- Adjusted R-Squared: 0.2787
 - A low adjusted R-squared indicates that the additional input variables are not adding value to the model
 - Currently, the white wine model is a bad fit
- Significance at $\alpha = 0.05$
 - The model is statistically significant at $\alpha = 0.05$, as the p-value from the model is 2.54×10^{-15} , which is less than 0.05

```
> summary(Wm)
```

```
Call:
```

```
lm(formula = Quality ~ ., data = Wtrain)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-3.5669	-0.5154	-0.0374	0.4796	3.0864

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	2.529e+02	3.176e+01	7.964	2.54×10^{-15} ***
`Fixed Acidity`	1.348e-01	3.295e-02	4.090	4.45×10^{-5} ***
`Volatile Acidity`	-1.743e+00	1.652e-01	-10.547	$< 2 \times 10^{-16}$ ***
`Citric Acid`	7.870e-02	1.305e-01	0.603	0.5464
`Residual Sugar`	1.072e-01	1.206e-02	8.886	$< 2 \times 10^{-16}$ ***
Chlorides	-2.367e-01	7.427e-01	-0.319	0.7500
`Free sulfur Dioxide`	6.113e-03	1.336e-03	4.575	5.01×10^{-6} ***
`Total Sulfur Dioxide`	1.077e-04	5.467e-04	0.197	0.8439
Density	-2.551e+02	3.220e+01	-7.923	3.51×10^{-15} ***
pH	1.187e+00	1.624e-01	7.312	3.58×10^{-13} ***
Sulphates	8.936e-01	1.530e-01	5.839	5.95×10^{-9} ***
Alcohol	9.932e-02	4.013e-02	2.475	0.0134 *

```
---  
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

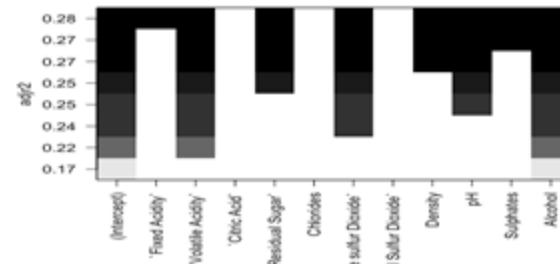
```
Residual standard error: 0.7791 on 2388 degrees of freedom
```

```
Multiple R-squared:  0.282,    Adjusted R-squared:  0.2787
```

```
F-statistic: 85.27 on 11 and 2388 DF,  p-value: < 2.2e-16
```

Improved White Wine Model

- Best regressor(s) to incorporate into model:
 - Used *regsubsets* {leaps}
 - Fixed Acidity, Volatile Acidity, Residual Sugar, Free Sulfur Dioxide, Density, pH, Sulphates, and Alcohol
- Adjusted R-Squared: 0.2795
 - Compared to the original values, the relatively higher Adjusted R-Squared indicates the regressors can add more value to the model
- Significance at $\alpha = 0.05$
 - The model is statistically significant at $\alpha = 0.05$, as the p-value from the model is $2e-16$, which is less than 0.05



```
> summary(fitW)
```

```
Call:
lm(formula = Quality ~ 'Fixed Acidity' + 'Volatile Acidity' +
    'Residual Sugar' + 'Free sulfur Dioxide' + Density + pH +
    Sulphates + Alcohol, data = Wtrain)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-3.5485 -0.5163 -0.0338  0.4800  3.0869
```

```
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  2.519e+02  3.005e+01   8.383  < 2e-16 ***
'Fixed Acidity'  1.375e-01  3.180e-02   4.324  1.59e-05 ***
'Volatile Acidity' -1.758e+00  1.607e-01 -10.934 < 2e-16 ***
'Residual Sugar'  1.073e-01  1.153e-02   9.310 < 2e-16 ***
'Free sulfur Dioxide' 6.282e-03  1.077e-03   5.834  6.16e-09 ***
Density      -2.541e+02  3.043e+01  -8.350 < 2e-16 ***
pH           1.179e+00  1.561e-01   7.551  6.12e-14 ***
Sulphates     9.008e-01  1.519e-01   5.931  3.46e-09 ***
Alcohol       1.021e-01  3.950e-02   2.584  0.00982 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.7787 on 2391 degrees of freedom
Multiple R-squared:  0.2819,    Adjusted R-squared:  0.2795
F-statistic: 117.3 on 8 and 2391 DF,    p-value: < 2.2e-16
```


Model Evaluation

- Mean Absolute Percentage Error (MAPE) is used to determine the prediction error of the models
- MAPE of red wine model = 9.5976%
- MAPE of white wine model = 10.3711%
- Both models have a MAPE of $< 10.5\%$, indicating that the average unsigned percentage error for each model is very low (models are good fits)

```
MAPE<-function(pred, true)
{
  return(100*mean(abs((pred-true)/true), na.rm=T))
}
```

```
MAPE(Rpred, Rtest$Quality)
MAPE(Wpred, Wtest$Quality)
```

```
> MAPE(Rpred, Rtest$Quality)
[1] 9.597551
> MAPE(Wpred, Wtest$Quality)
[1] 10.37114
```

Variance Inflation Factor – Red Wine

```
> RVIF
```

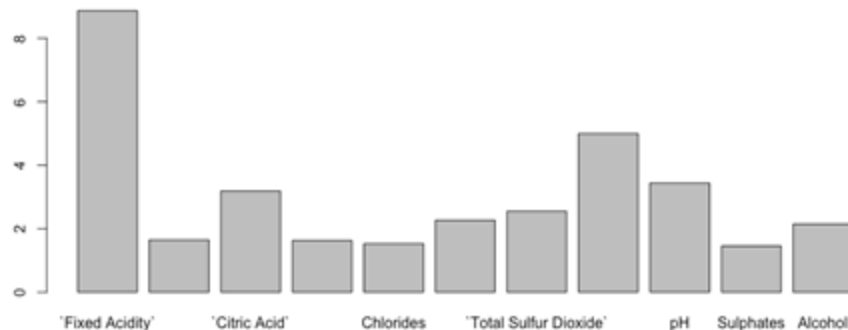
Fixed Acidity	8.866974	Volatile Acidity	1.645710	Citric Acid	3.184926
Residual Sugar	1.627857	Chlorides	1.528297	Free sulfur Dioxide	2.265589
Total Sulfur Dioxide	2.551407	Density	4.996512	pH	3.438727
Sulphates	1.455214	Alcohol	2.144835		

```
> which(RVIF>5)
```

```
Fixed Acidity`  
1
```

- `which(RVIF>5)` highlights regressors that exhibit multicollinearity
 - ∴ Fixed Acidity is highly collinear with the other regressors in the model

- Threshold for VIF: 5
- A variable with a higher VIF contributes more to the standard error of a regression



Variance Inflation Factor – White Wine

```
> WVIF
```

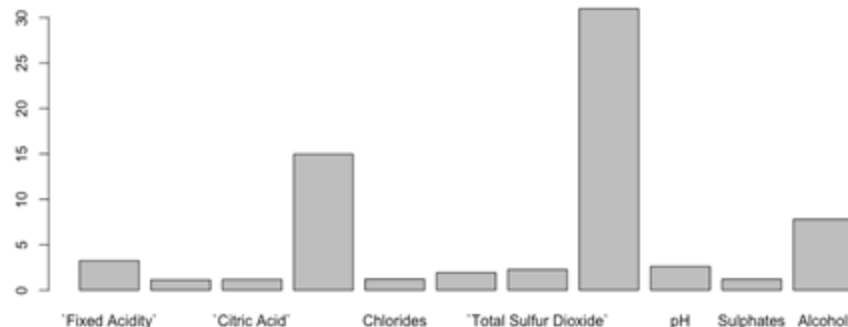
'Fixed Acidity'	3.241740	'Volatile Acidity'	1.128829	'Citric Acid'	1.182005
'Residual Sugar'	14.969678	Chlorides	1.213800	'Free sulfur Dioxide'	1.928162
'Total Sulfur Dioxide'	2.271571	Density	30.975080	pH	2.611740
Sulphates	1.204943	Alcohol	7.799363		

```
> which(WVIF>5)
```

'Residual Sugar'	Density	Alcohol
4	8	11

- `which(RVIF>5)` highlights regressors that exhibit multicollinearity
 - ∴ Residual Sugar, Density, and Alcohol are highly collinear with the other regressors in the model

- Threshold for VIF: 5
- A variable with a higher VIF contributes more to the standard error of a regression



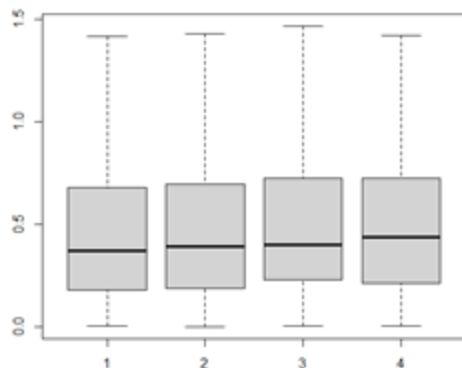
Red Wine Model Robustness (K-fold CV Test)

- K-fold cross validation is a procedure used to estimate the skill of the model on new data
- Four fold Cross Validation
 - Because the performance metrics across all four folds are similar, the red wine model can be described as robust
 - In other words, the model performance stays stable when the data (in both the training and test sets) changes, thus, it is robust

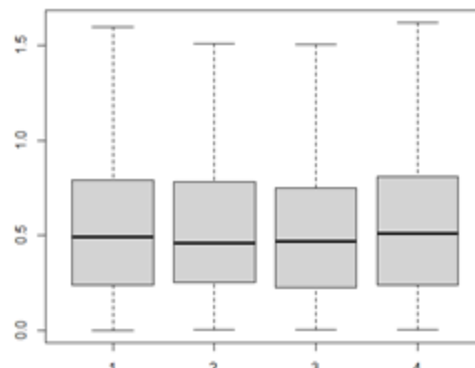
```
23 K<-4
24 dt1<-red[sample(1:nrow(red), nrow(red)), ]
25 len<-floor(nrow(dt1)/K) # number of obs. in testing set
26 pred<-matrix(, len, K)
27 test.all<-matrix(, len, K)
28 pred.err<-matrix(, len, K)
29
30
31 for(k in 1:K)
32 {
33   index <- ((k-1)*len+1):(k*len)
34
35   te<-dt1[index, ]
36   tr<-dt1[-index, ]
37
38   fit <- lm(quality~., data=red)
39
40   pre<- predict(fit, newdata=te)
41   test.all[1:len, k]<-te$quality
42   pred[1:len, k]<- pre
43   pred.err[1:len, k]<- abs(pre-te$quality)
44 }
45
46
47 boxplot(pred.err, outline = FALSE)
```

White Wine Model Robustness (K-fold CV Test)

- Because the performance metrics across all four folds are similar, the white wine model can be described as robust
- In other words, the model performance stays stable when the data (in both the training and test sets) changes, thus, it is robust



Red Wine



White Wine

Red Wine Model Conclusion

- Best model (eight regressors):

```
> summary(fitR)
```

Call:

```
lm(formula = Quality ~ `Fixed Acidity` + `Volatile Acidity` +  
  `Citric Acid` + Chlorides + `Free sulfur Dioxide` + `Total Sulfur Dioxide` +  
  Sulphates + Alcohol, data = Rtrain)
```

- (RVIF>5):

```
> which(RVIF>5)  
`Fixed Acidity`  
1
```

- Variable(s) most important towards determining the quality of red wine:
 - Volatile Acidity, Citric Acid, Chlorides, Free Sulfur Dioxide, Total Sulfur Dioxide, Sulphates, and Alcohol

White Wine Model Conclusion

- Best model (eight regressors):

```
> summary(fitW)
```

Call:

```
lm(formula = Quality ~ `Fixed Acidity` + `Volatile Acidity` +  
  `Residual Sugar` + `Free sulfur Dioxide` + Density + pH +  
  Sulphates + Alcohol, data = Wtrain)
```

- (RVIF>5):

<pre>> which(WVIF>5)</pre>		
<pre>`Residual Sugar`</pre>	<pre>Density</pre>	<pre>Alcohol</pre>
4	8	11
- Variable(s) most important towards determining the quality of white wine:
 - Fixed Acidity, Volatile Acidity, Free Sulfur Dioxide, pH, and Sulphates

References

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**THANK
YOU**