

[Ex 3, page 33]

$$2) A_1(x_1, y_1) \rightarrow A'_1(x'_1; y'_1)$$

$$A_2(x_2, y_2) \rightarrow A'_2(x'_2; y'_2)$$

$$\begin{aligned} |A_1 A_2|^2 &= [x'_2 - x'_1]^2 + [y'_2 - y'_1]^2 + [a_{11}(x_2 - x_1) + \\ &+ a_{12}(y_2 - y_1)]^2 + [a_{21}(x_2 - x_1) + a_{22}(y_2 - y_1)]^2 = \\ &= (a_{11}^2 + a_{21}^2)(x_2 - x_1)^2 + (a_{12}^2 + a_{22}^2)(y_2 - y_1)^2 + \\ &+ 2(a_{11}a_{12} + a_{21}a_{22})(x_2 - x_1)(y_2 - y_1) = \\ &= (x_2 - x_1)^2 + (y_2 - y_1)^2 = |A_1 A_2|^2 \\ \Rightarrow |A_1 A_2| &= |A'_1 A'_2| \end{aligned}$$