

Ques 5, problem 2

$$y = \arcsin(\sin x)$$

$$\frac{d}{dx}(\sin^{-1}(\sin x)) \rightarrow \frac{d(\sin^{-1}a)}{da} \cdot \frac{da}{dx}, \quad a = \sin x$$
$$\frac{d(\sin^{-1}a)}{da} = \frac{1}{\sqrt{1-a^2}}$$

$$\rightarrow \frac{\frac{d}{dx}(\sin x)}{\sqrt{1-\sin^2 x}} \rightarrow \frac{\frac{d}{dx} \sin x}{\sqrt{1-\sin^2 x}} = \frac{\frac{d \sin a}{da} \cdot \frac{da}{dx}}{\sqrt{1-\sin^2 x}}, \quad a = x$$
$$\frac{d \sin a}{da} = \cos a$$

$$\rightarrow \cos x \left(\frac{\frac{d}{dx}(x)}{\sqrt{1-\sin^2 x}} \right) \rightarrow 1 \cdot \frac{\cos x}{\sqrt{1-\sin^2 x}} \rightarrow$$

$$\rightarrow \sqrt{\cos^2 x} \cdot \sec x$$

(secant function)