

Exercice 6, page 2

$$\begin{cases} y = \frac{t^2}{t-1} \\ x = \frac{t}{t^2-1} \end{cases}$$

$$y' = \frac{y't}{x't}$$

$$y'_t \text{ as quotient } \frac{d}{dx} \left(\frac{y}{x} \right) = \frac{v \frac{dy}{dt} - y \frac{dv}{dt}}{v^2}; \quad y = \frac{t^2}{t-1}, \quad v = t-1$$

$$\Rightarrow \frac{(t-1) \left(\frac{d}{dt} \left(\frac{t^2}{t-1} \right) \right) - t^2 \left(\frac{d}{dt} (t-1) \right)}{(t-1)^2} \rightarrow \frac{2t(t-1) - t^2}{(t-1)^2} \rightarrow$$

$$\rightarrow \frac{t(t-2)}{(t-1)^2}$$

$$x'_t \text{ as quotient (ou borne)}, \quad v = t, \quad v = t^2-1$$

$$\Rightarrow \frac{(t^2-1) \left(\frac{d}{dt} (t) \right) - t \left(\frac{d}{dt} (t^2-1) \right)}{(t^2-1)^2} \rightarrow \frac{t^2 - 2t \cdot t}{(t^2-1)^2} \rightarrow$$

$$\rightarrow -\frac{(t^2+1)}{(t^2-1)^2}$$

$$y'_x = \frac{t(t-2)}{(t-1)^2} \cdot \frac{(t^2-1)^2}{-(t^2+1)} = -\frac{t(t-2)(t^2-1)^2}{t^2+1}$$