

Задание 4, задание 1

$$a) \lim_{x \rightarrow 6} \frac{x^2 - 36}{x^2 - x - 30} = \frac{12}{11}$$

$$b) \lim_{x \rightarrow 7} \frac{x^2 - 49}{x^2 - 13x + 42} = 14$$

$$c) \lim_{x \rightarrow 7} \frac{\sqrt[3]{x+2} - \sqrt[3]{x+20}}{\sqrt{x+9} - 2} = \frac{1}{254} (3 - 8\sqrt[3]{3}) = \frac{3 - 8\sqrt[3]{3}}{254} = -0,5405358$$

$$d) \lim_{x \rightarrow 0} \frac{3x \operatorname{tg} 4x}{1 - \cos 4x} = \frac{3}{2} \left(\frac{12x \operatorname{tg}^2 4x + 12x + 3 \operatorname{tg} 4x}{4 \cos 4x} \right)$$

$$e) \lim_{x \rightarrow 0} \frac{\sqrt{2} x^2 \sin 4x}{(1 - \cos 2x)^{3/2}} = \frac{\sqrt{2} x^2 \sin 4x}{\frac{1}{2}(1 - \cos(2x))^3} =$$

$$= \frac{2\sqrt{2} x^2 \sin 4x}{(1 - \cos 2x)^3} = \frac{8\sqrt{2} x^2 \cos 4x + 4\sqrt{2} x^2 \sin 4x}{6 \sin 2x \cdot \cos^2 2x - 12 \sin 2x \cos 2x + 6 \sin 2x}$$

$$= 4868712,08837285$$