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$$U = \frac{156}{x} + \frac{x^2}{y} + \frac{y^2}{z} + 2z$$

$$U'_x = \frac{2x}{y} - \frac{156}{x^2} \rightarrow U''_{xy} = -\frac{2x}{y^2}$$

$$U''_{xx} = \frac{512}{x^3} + \frac{2}{y}$$

$$U'_y = \frac{2y}{z} - \frac{x^2}{y^2} \rightarrow U''_{yx} = -\frac{2x}{y^2}; U''_{yz} = -\frac{2y}{z^2}$$

$$U''_{yy} = \frac{2}{z} + \frac{2x^2}{y^3}$$

$$U'_z = 2z - \frac{y^2}{z^2} \rightarrow U''_{zy} = -\frac{2y}{z^2}$$

$$U''_{zz} = 2 + \frac{2y^2}{z^3}$$

$$U''_{xy} = U''_{yx} \left(-\frac{2x}{y^2}\right); U''_{yz} = U''_{zy} \left(-\frac{2y}{z^2}\right)$$