1 Computational Geometr

57

1.1 Geometry.cpp

```
58
                                                 59
1 template<typename T>
2 struct point{
    T x,y;
                                                 61
    point(){}
    point(const T&x,const T&y):x(x),y(y){}
                                                 63
    point operator+(const point &b)const{
      return point(x+b.x,y+b.y);}
    point operator-(const point &b)const{
      return point(x-b.x,y-b.y);}
    point operator*(const T &b)const{
                                                 66
       return point(x*b,y*b);}
                                                 67
    point operator/(const T &b)const{
13
      return point(x/b,y/b);}
                                                 69
14
    bool operator==(const point &b)const{
                                                 70
15
      return x==b.x&&y==b.y;}
16
    T dot(const point &b)const{
                                                 71
17
      return x*b.x+y*b.y;}
    T cross(const point &b)const{
18
                                                 72
19
      return x*b.y-y*b.x;}
                                                 73
    point normal()const{//求法向量
20
                                                 74
      return point(-y,x);}
21
    T abs2()const{//向量長度的平方
                                                 75
      return dot(*this);
24
25
    T rad(const point &b)const{//兩向量的弧度
      return fabs(atan2(fabs(cross(b)),dot(b))
26
           );
27
28
   };
   template<typename T>
                                                 79
   struct line{
                                                 80
    line(){}
    point<T> p1,p2;
    T a,b,c;//ax+by+c=0
    line(const point<T>&x,const point<T>&y):p1
          (x),p2(y){}
    void pton(){//轉成一般式
35
36
      a=p1.y-p2.y;
37
      b=p2.x-p1.x;
38
      c=-a*p1.x-b*p1.v:
39
    T cross(const point<T> &p)const{//點和有向
          直線的關係, >0左邊、=0在線上<0右邊
41
      return (p2-p1).cross(p-p1);
42
                                                 89
43
    bool point on segment(const point<T>&p)
          const{//點是否線段上
      return cross(p) == 0&&(p1-p).dot(p2-p) <= 0;</pre>
44
45
                                                 92
46
    T dis2(const point<T> &p,bool is_segment
                                                 93
          =0) const { // 點 跟 直 線 / 線 段 的 距 離 平 方
                                                 94
       point < T > v = p2 - p1, v1 = p - p1;
       if(is segment){
         point<T> v2=p-p2;
                                                 96
50
         if(v.dot(v1)<=0)return v1.abs2();</pre>
        if(v.dot(v2)>=0)return v2.abs2();
51
52
      T tmp=v.cross(v1);
```

```
return tmp*tmp/v.abs2();
point<T> projection(const point<T> &p)
                                          100
    const{//點對直線的投影
                                          101
  point<T> n=(p2-p1).normal();
                                          102
 return p-n*(p-p1).dot(n)/n.abs2();
                                          103
                                          104
point<T> mirror(const point<T> &p)const{// 105
    點對直線的鏡射
  //要先呼叫pton轉成一般式
                                          106
 point<T> ans:
                                          107
 T d=a*a+b*b;
  ans.x=(b*b*p.x-a*a*p.x-2*a*b*p.y-2*a*c)/
  ans.v = (a*a*p.v-b*b*p.v-2*a*b*p.x-2*b*c)/
      d;
  return ans;
bool equal(const line &l)const{//直線相等
 return cross(1.p1)==0&&cross(1.p2)==0;
bool parallel(const line &1)const{//直線平
  return (p1-p2).cross(1.p1-1.p2)==0;
                                          117
                                          118
bool cross seg(const line &1)const{//直線
     是否交線段
  return (p2-p1).cross(1.p1)*(p2-p1).cross _{120}
      (1.p2) <= 0;
                                          121
                                          122
char line_intersect(const line &1)const{// 123
     直線相交情況,-1無限多點、1交於一點、0124
  return parallel(1)?(cross(1.p1)==0?-1:0)
char seg_intersect(const line &l)const{//
     線段相交情況,-1無限多點、1交於一點、0129
                                          131
 T c1=(p2-p1).cross(l.p1-p1);
 T c2=(p2-p1).cross(1.p2-p1);
                                          132
 T c3=(1.p2-1.p1).cross(p1-1.p1);
                                          133
 T c4=(1.p2-1.p1).cross(p2-1.p1);
  if(c1==0&&c2==0){
    if(p1==1.p1&&(p2-p1).dot(1.p2)<=0)
         return 1;
    if(p1==1.p2&&(p2-p1).dot(1.p1)<=0)
        return 1:
                                          136
    if(p2==1.p1&&(p1-p2).dot(1.p2)<=0)
        return 1:
                                          137
    if(p2==1.p2&&(p1-p2).dot(1.p1)<=0)
                                          138
        return 1;
    return -1:
                                          139
  }else if(c1*c2<=0&&c3*c4<=0)return 1;</pre>
                                          140
 return 0;
                                          141
                                          142
point<T> line_intersection(const line &1)
    const{/*直線交點*/
                                          143
  point<T> a=p2-p1,b=l.p2-l.p1,s=l.p1-p1; 144
  //if(a.cross(b)==0)return INF;
  return p1+a*s.cross(b)/a.cross(b);
                                          145
                                          146
                                          147
```

```
point<T> seg intersection(const line &1)
          const{//線段交點
                                                 149
       T c1=(p2-p1).cross(l.p1-p1);
       T c2=(p2-p1).cross(1.p2-p1);
                                                 150
       T c3=(1.p2-1.p1).cross(p1-1.p1);
                                                 151
       T c4=(1.p2-1.p1).cross(p2-1.p1);
                                                 152
                                                 153
       if(c1==0&&c2==0){
         if(p1==1.p1&&(p2-p1).dot(1.p2)<=0)
                                                 154
                                                 155
              return p1;
         if(p1==1.p2\&\&(p2-p1).dot(1.p1)<=0)
              return p1;
         if(p2==1.p1&&(p1-p2).dot(1.p2) <= 0)
                                                 157
              return p2;
                                                 158
         if(p2==1.p2&&(p1-p2).dot(1.p1) <=0)
                                                 159
              return p2;
                                                 160
       }else if(c1*c2<=0&&c3*c4<=0)return
                                                 161
            line intersection(1);
                                                 162
       //return INF;
                                                 163
113 template<typename T>
                                                 164
   struct polygon{
     polygon(){}
                                                 165
     vector<point<T> > p;//逆時針順序
                                                 166
     T area()const{//面積
                                                 167
                                                 168
       T ans=0;
       for(int i=p.size()-1,j=0;j<(int)p.size()</pre>
            :i=i++)
         ans+=p[i].cross(p[j]);
       return ans/2:
                                                 170
     point<T> center of mass()const{//重心
       T cx=0, cy=0, w=0;
       for(int i=p.size()-1, j=0; j<(int)p.size() 174</pre>
            ;i=j++){
         T a=p[i].cross(p[j]);
         cx+=(p[i].x+p[j].x)*a;
         cy+=(p[i].y+p[j].y)*a;
                                                 177
         w+=a;
                                                 178
                                                 179
       return point<T>(cx/3/w,cy/3/w);
     char ahas(const point<T>& t)const{//點是否 181
          在簡單多邊形內,是的話回傳1、在邊上回 182
          傳-1、否則回傳0
                                                 184
                                                 185
       for(int i=0,j=p.size()-1;i<p.size();j=i</pre>
                                                 187
         if(line<T>(p[i],p[j]).point_on_segment
              (t))return -1;
                                                 189
         else if((p[i].v>t.v)!=(p[j].v>t.v)&&
         t.x<(p[j].x-p[i].x)*(t.y-p[i].y)/(p[j
              ].y-p[i].y)+p[i].x)
                                                 191
           c=!c;
       return c;
                                                 192
                                                 193
     char point_in_convex(const point<T>&x)
          const{
       int l=1,r=(int)p.size()-2;
                                                 194
       while(l<=r){//點是否在凸多邊形內,是的話
                                                 195
            回傳1、在邊上回傳-1、否則回傳0
                                                 196
         int mid=(1+r)/2;
                                                 197
         T a1=(p[mid]-p[0]).cross(x-p[0]);
                                                 198
         T a2=(p[mid+1]-p[0]).cross(x-p[0]);
```

```
if(a1>=0&&a2<=0){
      T res = (p[mid+1]-p[mid]).cross(x-p[
           mid]);
      return res>0?1:(res>=0?-1:0);
    }else if(a1<0)r=mid-1;</pre>
    else l=mid+1:
 return 0;
polygon cut(const line<T> &l)const{//△包
     對直線切割,得到直線1左側的凸包
  polygon ans:
  for(int n=p.size(),i=n-1,j=0;j<n;i=j++){</pre>
    if(1.cross(p[i])>=0){
      ans.p.push back(p[i]);
      if(1.cross(p[j])<0)
        ans.p.push_back(1.
             line intersection(line<T>(p[i
             ],p[j])));
    }else if(1.cross(p[j])>0)
      ans.p.push back(1.line intersection(
          line<T>(p[i],p[j])));
  return ans;
static bool graham cmp(const point<T>& a,
    const point<T>& b){
  return (a.x<b.x)||(a.x==b.x&&a.y<b.y);//</pre>
       凸包排序函數
void graham(vector<point<T> > &s){//凸包
  sort(s.begin(),s.end(),graham cmp);
  p.resize(s.size()+1);
  for(int i=0;i<(int)s.size();++i){</pre>
    while(m \ge 2\&\&(p[m-1]-p[m-2]).cross(s[i])
         ]-p[m-2])<=0)--m;
    p[m++]=s[i];
  for(int i=s.size()-2,t=m+1;i>=0;--i){
    while (m>=t&&(p[m-1]-p[m-2]).cross(s[i
        ]-p[m-2])<=0)--m;
    p[m++]=s[i];
  if(s.size()>1)--m;
  p.resize(m);
inline static char sign(const point<T>&t){
  return (t.y==0?t.x:t.y)<0;</pre>
inline static bool angle cmp(const line<T
     >& A, const line<T>& B){
  point<T> a=A.p2-A.p1,b=B.p2-B.p1;
  return sign(a)<sign(b) | | (sign(a) == sign(b)</pre>
      )&&a.cross(b)>0);
int halfplane intersection(vector<line<T>
    > &s){//半平面交
  sort(s.begin(),s.end(),angle cmp);//線段
       左側為該線段半平面
  int L.R.n=s.size():
  vector<point<T> > px(n);
  vector<line<T> > q(n);
  q[L=R=0]=s[0];
```

```
for(int i=1;i<n;++i){</pre>
199
          while(L<R&&s[i].cross(px[R-1])<=0)--R; 258
200
          while(L<R&&s[i].cross(px[L])<=0)++L;</pre>
201
202
          q[++R]=s[i];
                                                    260
203
          if(q[R].parallel(q[R-1])){
                                                    261
204
205
            if(q[R].cross(s[i].p1)>0)q[R]=s[i];
206
          if(L<R)px[R-1]=q[R-1].
207
               line intersection(q[R]);
                                                    265
208
                                                    266
        while (L < R \& a [L]. cross(px[R-1]) <= 0) -- R:
209
        p.clear();
210
                                                    267
211
        if(R-L<=1)return 0:
                                                    268 };
212
        px[R]=q[R].line intersection(q[L]);
213
        for(int i=L;i<=R;++i)p.push_back(px[i]);</pre>
                                                    270
        return R-L+1:
214
215
216
                                                    273
    template<typename T>
217
218
    struct triangle{
     point<T> a.b.c:
219
220
     triangle(){}
221
     triangle(const point<T> &a,const point<T>
           &b,const point<T> &c):a(a),b(b),c(c){}^{276}
     T area()const{
222
                                                    278
        T t=(b-a).cross(c-a)/2;
223
                                                    279
224
        return t>0?t:-t:
                                                    280
225
                                                    281
226
      point<T> barycenter()const{//重心
                                                    282
       return (a+b+c)/3;
227
                                                    283
228
                                                    284
229
      point<T> circumcenter()const{//外心
        static line<T> u,v;
230
                                                    285
231
        u.p1=(a+b)/2;
                                                    286
        u.p2=point<T>(u.p1.x-a.y+b.y,u.p1.y+a.x-
232
                                                    287
             b.x);
                                                    288
233
        v.p1=(a+c)/2;
234
        v.p2=point<T>(v.p1.x-a.y+c.y,v.p1.y+a.x-
235
        return u.line_intersection(v);
                                                    290
236
237
      point<T> incenter()const{//內心
       T A=sqrt((b-c).abs2()),B=sqrt((a-c).abs2 291
238
             ()),C=sqrt((a-b).abs2());
                                                    292
        return point<T>(A*a.x+B*b.x+C*c.x,A*a.y+
239
                                                    293
             B*b.y+C*c.y)/(A+B+C);
                                                    294
240
     point<T> perpencenter()const{//垂心
241
                                                    295
242
        return barycenter()*3-circumcenter()*2;
243
                                                    296
244
    };
                                                    297 };
245
    template<tvpename T>
                                                    298
    struct point3D{
246
     T x, y, z;
247
                                                    300
248
     point3D(){}
249
     point3D(const T&x,const T&y,const T&z):x(x
           ),y(y),z(z){}
250
     point3D operator+(const point3D &b)const{
        return point3D(x+b.x,y+b.y,z+b.z);}
251
252
     point3D operator-(const point3D &b)const{
253
        return point3D(x-b.x,y-b.y,z-b.z);}
                                                    304
                                                    305
     point3D operator*(const T &b)const{
254
        return point3D(x*b,y*b,z*b);}
                                                    306
255
     point3D operator/(const T &b)const{
```

```
return point3D(x/b,y/b,z/b);}
     bool operator==(const point3D &b)const{
       return x==b.x&&y==b.y&&z==b.z;}
                                                 308
     T dot(const point3D &b)const{
                                                 309
       return x*b.x+y*b.y+z*b.z;}
                                                 310
      point3D cross(const point3D &b)const{
       return point3D(y*b.z-z*b.y,z*b.x-x*b.z,x 311
            *b.y-y*b.x);}
     T abs2()const{//向量長度的平方
                                                 312
       return dot(*this);}
     T area2(const point3D &b)const{//和b、原點 313
          圍成面積的平方
       return cross(b).abs2()/4;}
                                                 315
269 template<typename T>
                                                 316
    struct line3D{
      point3D<T> p1,p2;
                                                 317
     line3D(){}
     line3D(const point3D<T> &p1,const point3D< 318
          T> &p2):p1(p1),p2(p2){}
     T dis2(const point3D<T> &p,bool is_segment _{320}| };
          =0) const { // 點 跟 直 線 / 線 段 的 距 離 平 方
        point3D<T> v=p2-p1,v1=p-p1;
        if(is segment){
          point3D<T> v2=p-p2;
          if(v.dot(v1)<=0)return v1.abs2();</pre>
         if(v.dot(v2)>=0)return v2.abs2();
        point3D<T> tmp=v.cross(v1);
                                                 326
       return tmp.abs2()/v.abs2();
                                                 327
      pair<point3D<T>,point3D<T> > closest pair(
          const line3D<T> &1)const{
        point3D<T> v1=(p1-p2), v2=(1.p1-1.p2);
                                                 328
        point3D<T> N=v1.cross(v2),ab(p1-l.p1);
                                                 329 };
       //if(N.abs2()==0)return NULL;平行或重合
       T tmp=N.dot(ab),ans=tmp*tmp/N.abs2();//
            最近點對距離
        point3D < T > d1 = p2 - p1, d2 = 1.p2 - 1.p1, D = d1.
                                                 333
            cross(d2):
       T t1=((1.p1-p1).cross(d2)).dot(D)/D.abs2
            ();
       T t2=((1.p1-p1).cross(d1)).dot(D)/D.abs2
            ();
       return make_pair(p1+d1*t1,1.p1+d2*t2);
     bool same side(const point3D<T> &a,const
                                                 338
          point3D<T> &b)const{
                                                 330
        return (p2-p1).cross(a-p1).dot((p2-p1).
                                                 340
            cross(b-p1))>0;
                                                 341
                                                 342
    template<typename T>
                                                 343
299 struct plane{
                                                 344
     point3D<T> p0,n;//平面上的點和法向量
                                                 345
     plane(){}
     plane(const point3D<T> &p0,const point3D<T 347
          > &n):p0(p0),n(n){}
     T dis2(const point3D<T> &p)const{//點到平
                                                 349
                                                 350
          面距離的平方
                                                 351
       T tmp=(p-p0).dot(n);
                                                 352
       return tmp*tmp/n.abs2();
                                                 353
```

```
point3D<T> projection(const point3D<T> &p) 354
       return p-n*(p-p0).dot(n)/n.abs2();
     point3D<T> line intersection(const line3D
          T> &1)const{
       T tmp=n.dot(1.p2-1.p1);//等於0表示平行或
                                                  359
             重合該平面
       return 1.p1+(1.p2-1.p1)*(n.dot(p0-1.p1)/ 360
                                                  361
     line3D<T> plane intersection(const plane &
                                                  362
          pl)const{
       point3D<T> e=n.cross(pl.n),v=n.cross(e); ^{363}
       T tmp=pl.n.dot(v);//等於0表示平行或重合
       point3D < T > q = p0 + (v*(pl.n.dot(pl.p0-p0))/
            tmp):
       return line3D<T>(q,q+e);
                                                  366
                                                 367
321 template<typename T>
                                                 368
   struct triangle3D{
                                                 369
     point3D<T> a,b,c;
                                                 370
     triangle3D(){}
                                                 371
     triangle3D(const point3D<T> &a,const
                                                 372
          point3D<T> &b, const point3D<T> &c):a(a373
          ),b(b),c(c){}
     bool point in(const point3D<T> &p)const{//
                                                 375
          點在該平面上的投影在三角形中
                                                  376
       return line3D<T>(b,c).same side(p,a)&&
                                                 377
            line3D<T>(a,c).same_side(p,b)&&
                                                 378
            line3D<T>(a,b).same_side(p,c);
                                                 379
                                                  380
                                                 381
330 template<typename T>
                                                  382
   struct tetrahedron{//四面體
                                                  383
     point3D<T> a,b,c,d;
     tetrahedron(){}
                                                 384
     tetrahedron(const point3D<T> &a,const
                                                 385
          point3D<T> &b, const point3D<T> &c,
          const point3D<T> &d):a(a),b(b),c(c),d(386
          d){}
                                                 387
     T volume6()const{//體積的六倍
                                                  388
       return (d-a).dot((b-a).cross(c-a));
                                                  389
                                                  390
     point3D<T> centroid()const{
                                                  391
       return (a+b+c+d)/4;
                                                  392
                                                  393
     bool point in(const point3D<T> &p)const{
       return triangle3D<T>(a,b,c).point in(p)
            &&triangle3D<T>(c,d,a).point in(p); 395
                                                  396
                                                  397
   };
   template<typename T>
                                                  398
   struct convexhull3D{
                                                  399
     static const int MAXN=105;
                                                  400
     struct face{
                                                  401
       int a,b,c;
       bool use;
                                                  402
       face(){}
                                                  403
       face(int a,int b,int c):a(a),b(b),c(c),
                                                 404
                                                  405
            use(1){}
     };
                                                  406
```

```
vector<point3D<T> > pt;
vector<face> fc;
int fid[MAXN][MAXN];
static bool point cmp(const point3D<T> &a,
     const point3D<T> &b){
  return a.x<b.x||(a.x==b.x&&(a.y<b.y||(a.
      v==b.v&&a.z<b.z)));
bool outside(int p,int a,int b,int c)const
  return tetrahedron<T>(pt[a],pt[b],pt[c],
       pt[p]).volume6()<0:</pre>
bool outside(int p,int f)const{return
     outside(p,fc[f].a,fc[f].b,fc[f].c);}
void AddFace(int a,int b,int c,int p){
  if(outside(p,a,b,c))fid[c][b]=fid[b][a]=
       fid[a][c]=fc.size(),fc.push_back(
       face(c,b,a));
  else fid[a][b]=fid[b][c]=fid[c][a]=fc.
       size(),fc.push_back(face(a,b,c));
bool dfs(int p,int f){
  if(!fc[f].use)return true;
  if(outside(p,f)){
    int a=fc[f].a,b=fc[f].b,c=fc[f].c;
    fc[f].use=false;
    if(!dfs(p,fid[b][a]))AddFace(p,a,b,c);
    if(!dfs(p,fid[c][b]))AddFace(p,b,c,a);
    if(!dfs(p,fid[a][c]))AddFace(p,c,a,b);
    return true:
  }else return false;
void build(){
  bool ok=false;
  fc.clear();
  sort(pt.begin(),pt.end(),point_cmp);
  pt.resize(unique(pt.begin(),pt.end())-pt
       .begin());
  for(size_t i=2;i<pt.size();++i){</pre>
    if((pt[0]-pt[i]).area2(pt[1]-pt[i])
         !=0){
      ok=true;
      swap(pt[i],pt[2]);
      break;
  if(!ok)return;
  ok=false;
  for(size t i=3;i<pt.size();++i){</pre>
    if(tetrahedron<T>(pt[0],pt[1],pt[2],pt
         [i]).volume6()!=0){
      ok=true:
      swap(pt[i],pt[3]);
      break;
  if(!ok)return:
  for(int i=0;i<4;++i)AddFace(i,(i+1)%4,(i</pre>
       +2)%4,(i+3)%4);
  for(size t i=4;i<pt.size();++i){</pre>
    for(int j=fc.size()-1;j>=0;--j){
      if(outside(i,j)){
        dfs(i,j);
        break;
```

```
410
        size t sz=0;
                                                        32
        for(size t i=0;i<fc.size();++i)if(fc[i].</pre>
              use)fc[sz++]=fc[i];
                                                        34
412
        fc.resize(sz);
                                                        35
413
                                                        36
      point3D<T> centroid()const{
                                                        37
414
415
        point3D\langle T \rangle res(0,0,0);
                                                        38
416
                                                        39
417
        for(size t i=0;i<fc.size();++i){</pre>
                                                        40
          T tmp=pt[fc[i].a].dot(pt[fc[i].b].
418
                                                        41
                cross(pt[fc[i].c]));
419
           res=res+(pt[fc[i].a]+pt[fc[i].b]+pt[fc 42
                [i].c])*tmp;
                                                        43
          vol+=tmp;
420
                                                        44
421
                                                        45
        return res/(vol*4);
422
                                                        46
423
424 };
```

1.2 SmallestCircle.cpp

2 Data Structure

Double(double d=0):d(d){}

return d-b.d<-EPS;}</pre>

return d-b.d>EPS;}

return d-b.d<=EPS;}</pre>

return d-b.d>=-EPS;}

operator double()const{return d:}

bool operator <(const Double &b)const{</pre>

bool operator >(const Double &b)const{

bool operator ==(const Double &b)const{

bool operator !=(const Double &b)const{

bool operator <=(const Double &b)const{</pre>

bool operator >=(const Double &b)const{

return fabs(d-b.d)<=EPS:}</pre>

return fabs(d-b.d)>EPS;}

2.1 DLX.cpp

1 #define MAXN 4100 2 #define MAXM 1030 3 #define MAXND 16390 55 4 struct DLX{ int n,m,sz,ansd;//高是n · 寬是m的稀疏矩陣 int S[MAXM],H[MAXN]; int row[MAXND], col[MAXND]; //每個節點代表的 int L[MAXND],R[MAXND],U[MAXND],D[MAXND]; vector<int> ans,anst; 62 void init(int _n,int _m){ 10 63 n = n, m = m;64 for(int i=0;i<=m;++i){</pre> 65 U[i]=D[i]=i,L[i]=i-1,R[i]=i+1;S[i]=0; 14 67 68 R[m]=0,L[0]=m;sz=m, ansd=INT MAX; //ansd 存 最 優 解 的 個 數 for(int i=1;i<=n;++i)H[i]=-1;</pre> 71 19 72 void add(int r,int c){ 20 73 21 ++S[col[++sz]=c]; 74 row[sz]=r; D[sz]=D[c],U[D[c]]=sz,U[sz]=c,D[c]=sz;**if**(H[r]<0)H[r]=L[sz]=R[sz]=sz; else R[sz]=R[H[r]],L[R[H[r]]]=sz,L[sz]=H [r],R[H[r]]=sz; 26 #define DFOR(i,A,s) for(int i=A[s];i!=s;i= void remove(int c){//刪除第c行和所有當前覆 蓋到第c行的列 L[R[c]]=L[c],R[L[c]]=R[c];//這裡刪除第c 行,若有些行不需要處理可以在開始時呼 86 DFOR(i,D,c)DFOR(j,R,i){U[D[j]]=U[j],D[U[j]]=D[j],--S[col[j]];}

1.3 最近點對.cpp

```
1 #include "Geometry.cpp"
2 struct Circle{
      typedef point<double> p;
      typedef const point<double> cp;
      px;
      double r2:
      bool incircle(cp &c)const{return (x-c).
           abs2()<=r2;}
8 };
  Circle TwoPointCircle(Circle::cp &a, Circle
       ::cp &b) {
      Circle::p m=(a+b)/2;
      return (Circle){m,(a-m).abs2()};
12
13
  Circle outcircle(Circle::p a, Circle::p b,
       Circle::p c) {
      if(TwoPointCircle(a,b).incircle(c))
           return TwoPointCircle(a,b);
      if(TwoPointCircle(b,c).incircle(a))
           return TwoPointCircle(b,c);
      if(TwoPointCircle(c,a).incircle(b))
           return TwoPointCircle(c,a);
      Circle::p ret;
      double a1=b.x-a.x, b1=b.y-a.y, c1=(a1*a1
           +b1*b1)/2;
      double a2=c.x-a.x, b2=c.y-a.y, c2=(a2*a2
           +b2*b2)/2;
      double d = a1*b2 - a2*b1;
      ret.x=a.x+(c1*b2-c2*b1)/d;
      ret.y=a.y+(a1*c2-a2*c1)/d;
      return (Circle){ret,(ret-a).abs2()};
  //rand required
  Circle SmallestCircle(std::vector<Circle::p>
       int n=p.size();
      if(n==1) return (Circle){p[0],0.0};
```

```
1 | #define INF LLONG MAX/*預設是Long Long最大值
2 template<typename T>
3 T closest_pair(vector<point<T> >&v,vector<</pre>
        point<T> >&t, int 1, int r){
     T dis=INF, tmd;
     if(l>=r)return dis;
     int mid=(1+r)/2;
    if((tmd=closest_pair(v,t,l,mid))<dis)dis=</pre>
     if((tmd=closest pair(v,t,mid+1,r))<dis)dis</pre>
     t.clear();
10
     for(int i=1:i<=r:++i)</pre>
      if((v[i].x-v[mid].x)*(v[i].x-v[mid].x)
            dis)t.push back(v[i]);
     sort(t.begin(),t.end(),point<T>::y_cmp);/*
          如果用merge sort的方式可以O(n)*/
     for(int i=0;i<(int)t.size();++i)</pre>
      for(int j=1;j<=3&&i+j<(int)t.size();++j)</pre>
15
         if((tmd=(t[i]-t[i+j]).abs2()) < dis)dis=
              tmd;
    return dis;
17 }
  template<typename T>
   inline T closest pair(vector<point<T> > &v){
    vector<point<T> >t;
     sort(v.begin(),v.end(),point<T>::x_cmp);
     return closest_pair(v,t,0,v.size()-1);/*最
          近點對距離*/
23 }
```

1.4 浮點數誤差模板.cpp

```
1 const double EPS=1e-9;
2 struct Double{
3 double d;
```

```
void restore(int c){//恢復第c行和所有當前
         覆蓋到第c行的列·remove的逆操作
      DFOR(i,U,c)DFOR(j,L,i){++S[col[j]],U[D[j
33
          ]]=j,D[U[j]]=j;}
      L[R[c]]=c,R[L[c]]=c;
34
35
    void remove2(int nd){//刪除nd所在的行當前
36
         所有點(包括虛擬節點),只保留nd
      DFOR(i,D,nd)L[R[i]]=L[i],R[L[i]]=R[i];
37
38
    void restore2(int nd){//刪除nd所在的行當前
39
         所有點,為remove2的逆操作
40
      DFOR(i,U,nd)L[R[i]]=R[L[i]]=i;
41
    bool vis[MAXM];
    int h(){//估價函數 for IDA*
      int res=0;
      memset(vis,0,sizeof(vis));
      DFOR(i,R,0)if(!vis[i]){
        vis[i]=1;
        ++res;
        DFOR(j,D,i)DFOR(k,R,j)vis[col[k]]=1;
50
51
      return res;
52
    bool dfs(int d){//for精確覆蓋問題
      if(d+h()>=ansd)return 0;//找最佳解用,找
           任意解可以刪掉
      if(!R[0]){ansd=d;return 1;}
      int c=R[0];
      DFOR(i,R,0)if(S[i]<S[c])c=i;</pre>
      remove(c);
      DFOR(i,D,c){
        ans.push_back(row[i]);
        DFOR(j,R,i)remove(col[j]);
        if(dfs(d+1))return 1;
        ans.pop back();
        DFOR(j,L,i)restore(col[j]);
      restore(c);
      return 0:
    void dfs2(int d){//for最小重複覆蓋問題
      if(d+h()>=ansd)return;
      if(!R[0]){ansd=d;ans=anst;return;}
      int c=R[0];
      DFOR(i,R,0)if(S[i] < S[c])c=i;
      DFOR(i,D,c){
        anst.push_back(row[i]);
        remove2(i):
        DFOR(j,R,i)remove2(j),--S[col[j]];
        dfs2(d+1);
        anst.pop back();
        DFOR(j,L,i)restore2(j),++S[col[j]];
        restore2(i);
    bool exact cover(){//解精確覆蓋問題
      ans.clear()://答案
      return dfs(0);
    void min cover() { // 解最小重複覆蓋問題
      anst.clear();//暫存用,答案還是存在ans裡
```

```
dfs2(0);
                                                            cmp.sort id=k;
                                                                                                                                                        165
                                                                                                                                                                  for(int i=0;i<n;++i)A[i]=new node(p[i</pre>
                                                            std::nth element(A.begin()+1,A.begin() 110
                                                   52
                                                                                                                 --u->s;
    #undef DFOR
                                                                 +mid, A. begin()+r+1, cmp);
                                                                                                                 cmp.sort id=k;
                                                                                                                                                                  root=build(0,0,n-1);
92
                                                                                                     111
                                                                                                                                                        166
                                                   53
                                                            node *ret=A[mid];
                                                                                                     112
                                                                                                                 u->pid=findmin(u->r,(k+1)%kd)->pid;
                                                                                                                                                        167
                                                   54
                                                            ret->l=build(k+1,l,mid-1);
                                                                                                                 return erase(u->r,(k+1)%kd,u->pid);
                                                                                                                                                                void insert(const point &x){
                                                                                                     113
                                                                                                                                                       168
                                                            ret->r=build(k+1,mid+1,r);
                                                   55
                                                                                                     114
                                                                                                                                                                  insert(root,0,x, lg(size(root))/loga)
                                                   56
                                                            ret->up():
                                                                                                     115
                                                                                                               cmp.sort id=k:
                                                            return ret;
                                                                                                               if(erase(cmp(x,u->pid)?u->1:u->r,(k+1)) 170
                                                                                                                                                                  if(root->s>maxn)maxn=root->s;
                                                   57
                                                                                                     116
  2.2 Dynamic KD_tree.cpp
                                                                                                                    %kd,x)){
                                                                                                                                                        171
                                                          bool isbad(node*o){
                                                                                                                  --u->s; return 1;
                                                                                                                                                                bool erase(const point &p){
                                                   59
                                                                                                     117
                                                                                                                                                        172
                                                                                                               }else return 0;
                                                                                                                                                                  bool d=erase(root,0,p);
                                                   60
                                                            return size(o->1)>alpha*o->s||size(o-> 118
                                                                                                                                                        173
1 template<typename T, size_t kd>//有kd個維度
                                                                 r)>alpha*o->s:
                                                                                                                                                                  if(root&&root->s<alpha*maxn)rebuild();</pre>
                                                                                                     119
                                                                                                                                                        174
class kd tree{
                                                                                                             T heuristic(const T h[])const{
                                                                                                                                                                  return d;
                                                   61
                                                                                                     120
                                                                                                                                                        175
    public:
                                                   62
                                                          void flatten(node *u.tvpename std::
                                                                                                     121
                                                                                                                                                        176
       struct point{
                                                                                                                                                                void rebuild(){
                                                               vector<node*>::iterator &it){
                                                                                                     122
                                                                                                               for(size t i=0;i<kd;++i)ret+=h[i];</pre>
                                                                                                                                                        177
         T d[kd];
                                                            if(!u)return;
                                                                                                     123
                                                                                                               return ret;
                                                                                                                                                        178
                                                                                                                                                                  if(root)rebuild(root,0);
                                                   63
         T dist(const point &x)const{
                                                            flatten(u->1.it):
                                                                                                                                                                  maxn=root->s:
                                                   64
                                                                                                     124
                                                                                                                                                        179
           T ret=0;
                                                   65
                                                            *it=u;
                                                                                                     125
                                                                                                             int qM;
                                                                                                                                                        180
           for(size_t i=0;i<kd;++i)ret+=std::</pre>
                                                                                                             std::priority_queue<std::pair<T,point >
                                                                                                                                                                T nearest(const point &x,int k){
                                                   66
                                                            flatten(u->r,++it);
                                                                                                     126
                                                                                                                                                        181
                abs(d[i]-x.d[i]);
                                                   67
                                                                                                                                                        182
           return ret;
                                                                                                                                                                  T mndist=INF,h[kd]={};
                                                   68
                                                          void rebuild(node*&u,int k){
                                                                                                             void nearest(node *u,int k,const point & 183
                                                                                                     127
                                                            if((int)A.size()<u->s)A.resize(u->s);
                                                                                                                  x.T *h.T &mndist){
                                                                                                                                                                  nearest(root,0,x,h,mndist);
                                                   69
                                                                                                                                                        184
         bool operator == (const point &p){
                                                                                                                                                                  mndist=pQ.top().first;
                                                   70
                                                            typename std::vector<node*>::iterator
                                                                                                    128
                                                                                                               if(u==0||heuristic(h)>=mndist)return: 185
           for(size t i=0;i<kd;++i)</pre>
                                                                 it=A.begin();
                                                                                                     129
                                                                                                               T dist=u->pid.dist(x),old=h[k];
                                                                                                                                                                  pQ=std::priority_queue<std::pair<T,
                                                                                                                                                        186
13
             if(d[i]!=p.d[i])return 0;
                                                                                                               /*mndist=std::min(mndist,dist);*/
                                                                                                                                                                       point > >();
                                                   71
                                                            flatten(u,it);
                                                                                                     130
14
           return 1;
                                                   72
                                                            u=build(k,0,u->s-1);
                                                                                                     131
                                                                                                               if(dist<mndist){</pre>
                                                                                                                                                                  return mndist;//回傳離x第k近的點的距離
                                                                                                                                                        187
                                                                                                                 pQ.push(std::make_pair(dist,u->pid)) 188
                                                   73
                                                                                                     132
         bool operator<(const point &b)const{</pre>
                                                          bool insert(node*&u.int k.const point &x
                                                                                                                                                                const std::vector<point> &range(const
           return d[0]<b.d[0];</pre>
                                                               ,int dep){
                                                                                                                 if((int)pQ.size()==qM+1)
                                                                                                     133
                                                                                                                                                                     point&mi,const point&ma){
18
                                                   75
                                                            if(!u){
                                                                                                     134
                                                                                                                   mndist=pQ.top().first,pQ.pop();
                                                                                                                                                        190
                                                                                                                                                                  in range.clear();
19
       };
                                                   76
                                                              u=new node(x);
                                                                                                     135
                                                                                                                                                                  range(root,0,mi,ma);
                                                                                                                                                        191
20
     private:
                                                   77
                                                              return dep<=0;
                                                                                                     136
                                                                                                               if(x.d[k]<u->pid.d[k]){
                                                                                                                                                                  return in range;//回傳介於mi到ma之間的
                                                                                                                                                        192
21
       struct node{
                                                   78
                                                                                                                 nearest(u->1,(k+1)%kd,x,h,mndist);
                                                                                                     137
                                                                                                                                                                       點vector
22
         node *1,*r;
                                                                                                                 h[k]=std::abs(x.d[k]-u->pid.d[k]);
                                                   79
                                                            ++u->s;
                                                                                                     138
                                                                                                                                                        193
         point pid;
23
                                                            cmp.sort id=k;
                                                                                                                 nearest(u->r,(k+1)%kd,x,h,mndist);
                                                                                                     139
                                                                                                                                                                int size(){return root?root->s:0;}
                                                                                                                                                        194
24
         int s;
                                                            if(insert(cmp(x,u->pid)?u->1:u->r,(k
                                                                                                     140
                                                                                                               }else{
                                                                                                                                                        195 };
         node(const point &p):1(0),r(0),pid(p),
25
                                                                                                                 nearest(u->r,(k+1)%kd,x,h,mndist);
                                                                 +1)%kd,x,dep-1)){
                                                                                                     141
              s(1)\{\}
                                                              if(!isbad(u))return 1;
                                                                                                                 h[k]=std::abs(x.d[k]-u->pid.d[k]);
                                                                                                     142
         ~node(){delete 1,delete r;}
26
                                                              rebuild(u,k);
                                                                                                     143
                                                                                                                 nearest(u->1,(k+1)%kd,x,h,mndist);
         void up(){s=(1?1->s:0)+1+(r?r->s:0);}
27
                                                                                                     144
                                                                                                                                                            2.3 kd tree replace segment tr
28
                                                            return 0;
                                                                                                     145
                                                                                                               h[k]=old;
                                                   85
       const double alpha,loga;
                                                   86
                                                                                                     146
       const T INF;//記得要給INF,表示極大值
                                                          node *findmin(node*o,int k){
30
                                                                                                     147
                                                                                                             std::vector<point>in range;
       int maxn:
                                                            if(!o)return 0;
                                                                                                             void range(node *u,int k,const point&mi,
                                                                                                                                                          1 /*kd樹代替高維線段樹*/
31
                                                   88
                                                                                                     148
                                                            if(cmp.sort_id==k)return o->l?findmin(
                                                                                                                                                          2 struct node{
       struct __cmp{
                                                                                                                  const point&ma){
32
                                                   89
33
         int sort id;
                                                                 o->1,(k+1)%kd):o;
                                                                                                     149
                                                                                                               if(!u)return;
                                                                                                                                                              node *1,*r;
         bool operator()(const node*x,const
                                                            node *l=findmin(o->l,(k+1)%kd);
                                                                                                               bool is=1:
                                                                                                                                                              point pid, mi, ma;
34
                                                   90
                                                                                                     150
              node*y)const{
                                                            node *r=findmin(o->r,(k+1)%kd);
                                                                                                               for(int i=0;i<kd;++i)</pre>
                                                                                                                                                              int s;
                                                   91
                                                                                                     151
                                                            if(1&&!r)return cmp(1,0)?1:0;
                                                                                                                 if(u->pid.d[i]<mi.d[i]||ma.d[i]<u->
           return operator()(x->pid,y->pid);
                                                   92
                                                                                                     152
                                                            if(!1&&r)return cmp(r,o)?r:o;
                                                                                                                                                              node(const point &p,int d):1(0),r(0),pid(p
36
                                                   93
                                                                                                                      pid.d[i]){
         bool operator()(const point &x,const
                                                            if(!1&&!r)return o;
                                                                                                                                                                   ),mi(p),ma(p),s(1),data(d),dmin(d),
                                                   94
                                                                                                     153
                                                                                                                   is=0;break;
                                                            if(cmp(1,r))return cmp(1,o)?1:o;
              point &y)const{
                                                   95
                                                                                                     154
                                                                                                                                                                   dmax(d){}
           if(x.d[sort id]!=y.d[sort id])
                                                            return cmp(r,o)?r:o;
                                                                                                               if(is)in range.push back(u->pid);
                                                   96
                                                                                                     155
                                                                                                                                                              void up(){
             return x.d[sort_id]<y.d[sort_id];</pre>
                                                                                                     156
                                                                                                               if(mi.d[k]<=u->pid.d[k])range(u->1,(k
                                                                                                                                                                mi=ma=pid;
                                                          bool erase(node *&u,int k,const point &x
           for(size t i=0;i<kd;++i)</pre>
                                                                                                                    +1)%kd,mi,ma);
                                                                                                                                                                s=1;
             if(x.d[i]!=y.d[i])return x.d[i]<y.</pre>
                                                                                                               if(ma.d[k]>=u->pid.d[k])range(u->r,(k
                                                                                                                                                                if(1){
                                                                                                     157
                  d[i];
                                                            if(!u)return 0;
                                                                                                                    +1)%kd,mi,ma);
                                                                                                                                                                  for(int i=0;i<kd;++i){</pre>
                                                                                                                                                         12
                                                            if(u->pid==x){
                                                                                                                                                                    mi.d[i]=min(mi.d[i],1->mi.d[i]);
           return 0;
                                                  100
                                                                                                     158
                                                                                                                                                         13
                                                                                                           public:
43
                                                  101
                                                              if(u->r);
                                                                                                     159
                                                                                                                                                                    ma.d[i]=max(ma.d[i],1->ma.d[i]);
44
       }cmp;
                                                  102
                                                              else if(u->1){
                                                                                                     160
                                                                                                             kd tree(const T &INF, double a=0.75):root 15
       int size(node *o){return o?o->s:0;}
                                                                                                                  (0),alpha(a),loga(log2(1.0/a)),INF(
                                                  103
                                                                u->r=u->l;
                                                                                                                                                                  s+=1->s;
       std::vector<node*> A;
                                                  104
                                                                u - > 1 = 0;
                                                                                                                  INF), maxn(1){}
                                                                                                                                                         17
       node* build(int k,int l,int r){
                                                  105
                                                              }else{
                                                                                                     161
                                                                                                             ~kd tree(){delete root;}
                                                                                                                                                                if(r){
                                                                                                                                                                  for(int i=0;i<kd;++i){</pre>
         if(1>r)return 0;
                                                  106
                                                                delete u;
                                                                                                     162
                                                                                                             void clear(){delete root,root=0,maxn=1;}
         if(k==kd)k=0;
                                                                u=0;
                                                                                                             void build(int n,const point *p){
                                                                                                                                                                    mi.d[i]=min(mi.d[i],r->mi.d[i]);
49
                                                  107
                                                                                                     163
                                                                                                                                                         20
         int mid=(1+r)/2;
                                                  108
                                                                return 1;
                                                                                                               delete root, A.resize(maxn=n);
                                                                                                                                                                    ma.d[i]=max(ma.d[i],r->ma.d[i]);
```

```
4 struct RefCounter{
                                                       return;
                                                                                                    int insert(int l,int r,int rt,int x,int d){
23
        s+=r->s;
                                                 76
                                                                                                                                                       T data;
                                                                                                      if(x<1||r<x)return rt;</pre>
                                                                                                                                                       int ref;
24
                                                77
                                                     if(point_in_range(o,L,R)){
25
                                                       //這個點在(L,R)區間,但是他的左右子樹不
                                                                                                      int nd=new node(nds[rt]);
                                                                                                                                                       RefCounter(const T&d=0):data(d),ref(0){}
                                                 78
    void up2(){
                                                                                                      if(l==r&&l==x)nds[nd].data+=d;
26
                                                                                                 34
                                                            一定在區間中
      //其他懶惰標記向上更新
                                                                                                 35
                                                                                                      else{
                                                                                                                                                     template<typename T>
                                                       //單點懶惰標記修改
                                                                                                 36
                                                                                                        int mid=(1+r)/2;
                                                                                                                                                     struct ref pointer{
                                                 80
                                                                                                        int L=insert(1,mid,nds[nd].1,x,d);
                                                                                                                                                        RefCounter<T> *p;
    void down(){
                                                                                                                                                  11
                                                81
                                                     if(o->l&&range include(o->l,L,R))update(o
                                                                                                                                                       T *operator->(){return &(*p).data;}
                                                                                                        int R=insert(mid+1,r,nds[nd].r,x,d);
      //其他懶惰標記下推
30
                                                          ->1,L,R,data);
                                                                                                        nds[nd].1=L;
                                                                                                                                                       T &operator*(){return p->data;}
31
                                                     if(o->r&&range include(o->r,L,R))update(o
                                                                                                        nds[nd].r=R;
                                                                                                                                                  14
                                                                                                                                                       operator int(){return(int)(long long)p;}
   }*root;
32
                                                          ->r,L,R,data);
                                                                                                        up(nd,L,R);
                                                                                                                                                       ref pointer&operator=(const ref pointer &t
                                                                                                 41
                                                 83
                                                     o->up2();
                                                                                                 42
   /*檢查區間包含用的函數*/
                                                84
                                                                                                 43
                                                                                                      return nd:
                                                                                                                                                  16
                                                                                                                                                         if(p&&--(*p).ref==0)delete p;
   inline bool range include(node *o,const
                                                 85
                                                                                                 44
                                                                                                                                                  17
                                                                                                                                                         p=t.p;
       point &L,const point &R){
                                                    /*區間查詢,以總和為例*/
                                                                                                    inline int cal(int L,int R){
                                                                                                                                                  18
                                                                                                                                                         p&&++(*p).ref;
    for(int i=0;i<kd;++i){</pre>
                                                 87 int query(node *o,const point &L,const point
                                                                                                      return nds[R].data-nds[L].data;
                                                                                                                                                         return*this:
                                                                                                                                                  19
      if(L.d[i]>o->ma.d[i]||R.d[i]<o->mi.d[i])
                                                         &R){
                                                                                                 47
                                                                                                                                                  20
           return 0;
                                                     if(!o)return 0:
                                                                                                    int find(int 1, int r, int L, int R, int k){
                                                                                                                                                  21
                                                                                                                                                       ref_pointer(_RefCounter<T> *t=0):p(t){
    }//只要(L,R)區間有和o的區間有交集就回傳
                                                     o->down();
                                                                                                      if(l==r)return 1:
                                                                                                                                                  22
                                                                                                                                                         p&&++(*p).ref;
         true
                                                     if(range_in_range(o,L,R))return o->sum;
                                                                                                      int mid=(1+r)/2;
                                                                                                 50
                                                                                                                                                  23
    return 1;
                                                91
                                                     int ans=0;
39
                                                                                                      int add=cal(nds[L].1,nds[R].1);
                                                                                                                                                       ref pointer(const ref pointer &t):p(t.p){
                                                                                                 51
                                                                                                                                                  24
40
                                                     if(point_in_range(o,L,R))ans+=o->data;
                                                                                                      if(k<=add)return find(l,mid,nds[L].l,nds[R 25</pre>
                                                                                                                                                         p&&++(*p).ref;
   inline bool range_in_range(node *o,const
                                                     if(o->1&&range_include(o->1,L,R))ans+=
                                                                                                           1.1,k);
                                                                                                                                                  26
       point &L,const point &R){
                                                          query(o->1,L,R);
                                                                                                      return find(mid+1,r,nds[L].r,nds[R].r,k-
                                                                                                 53
                                                                                                                                                  27
                                                                                                                                                       ~ref pointer(){
    for(int i=0;i<kd;++i){</pre>
                                                     if(o->r&&range_include(o->r,L,R))ans+=
                                                                                                                                                         if(p&&--(*p).ref==0)delete p;
                                                          query(o->r,L,R);
      if(L.d[i]>o->mi.d[i]||o->ma.d[i]>R.d[i])
                                                                                                                                                  29
                                                                                                 54
           return 0:
                                                     return ans:
                                                                                                 55 int n.m:
                                                                                                                                                  30
                                                                                                                                                     };
    }//如果(L,R)區間完全包含o的區間就回傳true
                                                                                                 56 int s[100005];
                                                                                                                                                  31
                                                                                                                                                     template<typename T>
45
    return 1;
                                                                                                 57 int root[100005];
                                                                                                                                                     inline const ref_pointer<T> new_ref(const T&
46
                                                                                                    int main(){
   inline bool point in range(node *o,const
                                                                                                      while(~scanf("%d%d",&n,&m)){
                                                                                                                                                       return ref_pointer<T>(new _RefCounter<T>(
                                                    2.4 persistent segment tree.cps
       point &L,const point &R){
                                                                                                        nds.clear();
                                                                                                                                                            nd));
    for(int i=0;i<kd;++i){</pre>
                                                                                                        vector<int> lsh;
                                                                                                                                                  34
      if(L.d[i]>o->pid.d[i]||R.d[i]<o->pid.d[i
                                                                                                        for(int i=1;i<=n;++i){</pre>
                                                                                                                                                  35
                                                                                                                                                     struct P{
                                                  1 | #include < bits / stdc++.h > //POJ 2104
           ])return 0;
                                                                                                          scanf("%d",&s[i]);
                                                                                                                                                       int a,b;
                                                                                                  63
                                                                                                                                                  36
                                                 2 using namespace std;
    }//如果(L,R)區間完全包含o->pid這個點就回傳
                                                                                                 64
                                                                                                          lsh.push_back(s[i]);
                                                                                                                                                  37
                                                                                                                                                       P(int A, int B):a(A),b(B){}
                                                   struct node{
         true
                                                                                                  65
                                                                                                                                                  38
                                                                                                                                                     }p(2,3);
                                                     int 1.r:
51
    return 1:
                                                                                                  66
                                                                                                        sort(lsh.begin(),lsh.end());
                                                                                                                                                     int main(){
                                                     int data:
52
                                                                                                        lsh.resize(unique(lsh.begin(),lsh.end())
                                                                                                                                                       ref_pointer<int>b=new_ref(int(5));
                                                     node(int 1,int r,int d):1(1),r(r),data(d)
                                                                                                             -lsh.begin());
                                                                                                                                                       ref pointer<int>a=new ref(*b);
53
                                                                                                        int N=(int)lsh.size()-1;
                                                                                                                                                       ref pointer<P>c=new ref(p);
   /*單點修改·以單點改值為例*/
                                                                                                  68
                                                                                                        root[0]=build tree(0,N);
   void update(node *u,const point &x,int data,
                                                                                                  69
                                                                                                                                                       return 0;
                                                    vector<node> nds;
                                                                                                        for(int i=1;i<=n;++i){</pre>
                                                                                                 70
                                                                                                                                                  44 }
       int k=0){
                                                    inline void up(int o,int l,int r){
                                                                                                          s[i]=lower_bound(lsh.begin(),lsh.end()
    if(!u)return;
                                                     nds[o].data=nds[1].data+nds[r].data;
    u->down();
                                                                                                               ,s[i])-lsh.begin();
                                                11 }
                                                                                                          root[i]=insert(0,N,root[i-1],s[i],1);
    if(u->pid==x){
                                                                                                  72
                                                   inline int new node(int 1,int r,int d){
                                                                                                                                                     2.6 skew heap.cpp
      u->data=data;
                                                                                                  73
                                                     nds.push back(node(1,r,d));
                                                                                                        while(m--){
      u->up2();
                                                                                                  74
                                                     return nds.size()-1;
      return;
                                                                                                  75
                                                                                                          int a,b,k;
                                                15 }
                                                                                                          scanf("%d%d%d",&a,&b,&k);
                                                                                                                                                    1 | template < typename T, typename _Compare = std::</pre>
62
                                                    inline int new node(const node &nd){
                                                                                                          int res=find(0,N,root[a-1],root[b],k);
                                                                                                                                                          less<T> >
    cmp.sort id=k:
                                                                                                 77
63
                                                     nds.push back(nd);
                                                                                                          printf("%d\n",lsh[res]);
                                                                                                                                                     class skew heap{
    update(cmp(x,u->pid)?u->l:u->r,x,data,(k
                                                                                                  78
                                                     return nds.size()-1;
         +1)%kd);
                                                                                                 79
                                                                                                                                                       private:
                                                19
                                                                                                  80
                                                                                                                                                         struct node{
65
    u->up2();
                                                    int build tree(int 1.int r){
                                                                                                  81
                                                                                                      return 0;
                                                                                                                                                           T data;
66
                                                     int nd=new node(-1,-1,0);
                                                                                                                                                           node *1,*r;
67
                                                     if(l==r)return nd;
                                                                                                                                                           node(const T&d):data(d),1(0),r(0){}
   /*區間修改*/
                                                     int mid=(1+r)/2;
                                                                                                                                                           ~node(){delete l,delete r;}
   void update(node *o,const point &L,const
                                                     int L=build tree(1, mid); //執行時vector會被
                                                                                                                                                         }*root:
       point &R, int data){
                                                                                                    2.5 reference point.cpp
                                                                                                                                                         int size;
    if(!o)return;
                                                      int R=build tree(mid+1,r);//一定要這樣寫
                                                                                                                                                         Compare cmp;
    o->down();
                                                      nds[nd].l=L;
                                                                                                                                                         node *merge(node *a, node *b){
    if(range_in_range(o,L,R)){
                                                                                                  1 | #include < bits / stdc++.h>
                                                      nds[nd].r=R;
                                                                                                                                                           if(!a||!b)return a?a:b;
      //區間懶惰標記修改
                                                     //up(nd,L,R);
                                                                                                  2 using namespace std;
                                                                                                                                                           if(cmp(a->data,b->data))return merge(b
                                                28
      o->down();
                                                     return nd;
                                                                                                  3 template<typename T>
                                                                                                                                                                ,a);
```

if(x++%(a->s+b->s)<a->s){

//a=new node(*a);

a->down();

46

47

if(!o->s)**return** 0;

if(o->data==data){

node *t=o;

tree_order_statistics_node_update>

```
2.9 操作分治.cpp
         node *t=a->r:
                                                         a->r=merge(a->r,b);
                                                                                                               o=merge(o->ch[0],o->ch[1]);
16
         a \rightarrow r = a \rightarrow 1;
                                                  23
                                                         a->up();
                                                                                                    50
                                                                                                                delete t;
         a->l=merge(b,t);
                                                  24
                                                         return a;
                                                                                                    51
                                                                                                                return 1;
17
18
         return a;
                                                  25
                                                       }else{
                                                                                                    52
                                                                                                                                                        1 void dq(int 1,int r){
                                                  26
                                                         //b=new node(*b);
                                                                                                    53
                                                                                                              if(erase(o->ch[o->data<data],data)){</pre>
                                                                                                                                                           if(l==r)return;
19
                                                                                                               o->s--; return 1;
20
     public:
                                                  27
                                                         b->down();
                                                                                                    54
                                                                                                                                                           int mid=(1+r)/2:
21
       skew heap():root(0), size(0){}
                                                  28
                                                         b->1=merge(a,b->1);
                                                                                                    55
                                                                                                              }else return 0:
                                                                                                                                                           dq(1,mid);
       ~skew heap(){delete root;}
                                                         b->up();
                                                                                                    56
22
                                                  29
                                                                                                                                                            處理[1,mid]的操作對[mid+1,r]的影響
       void clear(){delete root, root=0, size
                                                                                                           void clear(node *&o){
23
                                                  30
                                                         return b;
                                                                                                    57
                                                                                                                                                           dq(mid+1,r);
                                                                                                             if(o->s)clear(o->ch[0]),clear(o->ch
                                                  31
       void join(skew heap &o){
                                                                                                                  [1]), delete o;
24
         root=merge(root,o.root);
25
                                                                                                    59
         o.root=0;
                                                                                                         public:
26
                                                                                                    60
         _size+=o._size:
                                                                                                           treap(unsigned s=20150119):nil(new node)
27
                                                                                                    61
                                                                                                                                                         2.10 整體二分.cpp
         o._size=0;
                                                     2.8 treap.cpp
28
                                                                                                                 ,root(nil),x(s){}
29
                                                                                                    62
                                                                                                           ~treap(){clear(root), delete nil;}
       void swap(skew heap &o){
                                                                                                           void clear(){clear(root),root=nil;}
30
                                                                                                    63
                                                                                                                                                        1 | void BS(int 1, int r, vector < Item > &vs){
         node *t=root;
                                                   1 | template < typename T>
                                                                                                           void insert(const T &data){
31
                                                                                                    64
                                                                                                             insert(root,data);
                                                                                                                                                           //答案該<L會有的已經做完了
         root=o.root;
                                                     class treap{
                                                                                                    65
32
                                                       private:
33
         o.root=t:
                                                                                                    66
                                                                                                                                                           if(l==r)整個vs的答案=1;//??????
34
         int st=_size;
                                                         struct node{
                                                                                                    67
                                                                                                           bool erase(const T &data){
                                                                                                                                                           int mid=(1+r)/2;
         _size=o._size;
                                                                                                              return erase(root.data):
35
                                                           T data:
                                                                                                    68
                                                                                                                                                           do thing(1, mid);//做答案<=mid會做的事
36
         o. size=st;
                                                           unsigned fix:
                                                                                                    69
                                                                                                                                                           vector<Item> left=vs裡滿足的:
                                                           int s;
                                                                                                    70
                                                                                                           bool find(const T&data){
37
                                                                                                                                                            vector<Item> right=vs-left:
       void push(const T&data){
                                                           node *ch[2];
                                                                                                             for(node *o=root;o->s;)
38
                                                                                                    71
                                                                                                                                                           undo_thing(l,mid);
         size++;
                                                           node(const T&d):data(d),s(1){}
                                                                                                    72
                                                                                                              if(o->data==data)return 1:
39
                                                                                                                                                            BS(1,mid,left):
         root=merge(root, new node(data));
                                                           node():s(0){ch[0]=ch[1]=this;}
                                                                                                    73
                                                                                                              else o=o->ch[o->data<data];</pre>
40
                                                                                                                                                           do_thing(1,mid);
                                                  11
                                                         }*nil.*root:
                                                                                                    74
                                                                                                              return 0:
41
                                                                                                                                                       11
                                                                                                                                                           BS(mid+1,r,right);//??????
       void pop(){
                                                         unsigned x;
                                                                                                    75
42
                                                  12
                                                                                                                                                      12 }
43
         if(_size)_size--;
                                                  13
                                                         unsigned ran(){return x=x*0xdefaced+1;}
                                                                                                    76
                                                                                                           int rank(const T&data){
                                                         void rotate(node *&a,bool d){
         node *tmd=merge(root->1,root->r);
                                                  14
                                                                                                    77
                                                                                                             int cnt=0:
44
45
         root->l=root->r=0;
                                                  15
                                                           node *b=a;
                                                                                                    78
                                                                                                              for(node *o=root;o->s;)
         delete root:
                                                  16
                                                           a=a->ch[!dl:
                                                                                                    79
                                                                                                              if(o->data<data)cnt+=o->ch[0]->s+1,o=o
46
                                                           a->s=b->s;
         root=tmd;
                                                  17
                                                                                                                  ->ch[1];
47
                                                                                                                                                               default
                                                           b->ch[!d]=a->ch[d];
                                                                                                              else o=o->ch[0];
48
                                                  18
                                                                                                    80
       const T& top(){return root->data;}
                                                           a->ch[d]=b;
49
                                                  19
                                                                                                    81
                                                                                                              return cnt;
50
       int size(){return _size;}
                                                  20
                                                           b->s=b->ch[0]->s+b->ch[1]->s+1;
                                                                                                    82
                                                                                                                                                          3.1 debug.cpp
       bool empty(){return !_size;}
                                                  ^{21}
                                                                                                    83
                                                                                                           const T&kth(int k){
                                                         void insert(node *&o,const T &data){
                                                                                                              for(node *o=root;;)
52 };
                                                  22
                                                                                                    84
                                                  23
                                                           if(!o->s){
                                                                                                              if(k<=o->ch[0]->s)o=o->ch[0];
                                                  24
                                                             o=new node(data),o->fix=ran();
                                                                                                              else if(k==o->ch[0]->s+1)return o->
                                                                                                                                                       1 | #ifdef Jinkela
                                                  25
                                                             o->ch[0]=o->ch[1]=nil;
                                                                                                                                                       2 #define debug(...) {\
          split merge.cpp
                                                  26
                                                           }else{
                                                                                                              else k-=o->ch[0]->s+1,o=o->ch[1];
                                                                                                    87
                                                                                                                                                            fprintf(stderr, "%s - %d : (%s) = ",
                                                  27
                                                             0->5++;
                                                                                                    88
                                                                                                                                                                 __PRETTY_FUNCTION__,_LINE__,#
                                                             bool d=o->data<data;</pre>
                                                                                                           const T&operator[](int k){
                                                                                                    89
                                                                                                                                                                  _VA_ARGS__);\
1 void split(node *o, node *&a, node *&b, int k){
                                                             insert(o->ch[d],data);
                                                                                                             return kth(k);
                                                                                                                                                            _DO(__VA_ARGS__);\
    if(!o)a=b=0;
                                                             if(o->ch[d]->fix>o->fix)rotate(o,!d)
                                                                                                    91
    else{
                                                                                                           const T&preorder(const T&data){
                                                                                                                                                         template<typename I> void DO(I&&x){cerr<<x</pre>
       //o=new node(*o);
                                                                                                             node *x=root,*y=0;
                                                  31
                                                                                                    93
                                                                                                                                                              <<endl:}
                                                                                                              while(x->s)
       o->down();
                                                  32
                                                                                                    94
                                                                                                                                                         template<typename I, typename...T> void _DO(I
       if(k<=size(o->1)){
                                                         node *merge(node *a, node *b){
                                                                                                              if(x->data<data)y=x,x=x->ch[1];
                                                  33
                                                                                                                                                              &&x,T&&...tail){cerr<<x<<", ";_DO(tail
                                                           if(!a->s||!b->s)return a->s?a:b;
        b=o;
                                                  34
                                                                                                    96
                                                                                                              else x=x->ch[0];
                                                                                                                                                              ...);}
         split(o->1,a,b->1,k);
                                                           if(a->fix>b->fix){
                                                                                                             if(y)return y->data;
                                                  35
                                                                                                    97
                                                                                                                                                        8 #else
       }else{
                                                  36
                                                             a->ch[1]=merge(a->ch[1],b);
                                                                                                    98
                                                                                                              return data;
                                                                                                                                                       9 #define debug(...)
                                                  37
                                                             a->s=a->ch[0]->s+a->ch[1]->s+1;
                                                                                                    99
                                                                                                                                                       10 #endif
                                                             return a;
                                                                                                           const T&successor(const T&data){
         split(o->r,a->r,b,k-size(o->l)-1);
                                                  38
                                                                                                    100
12
                                                  39
                                                                                                    101
                                                                                                             node *x=root,*y=0;
                                                             b->ch[0]=merge(a,b->ch[0]);
                                                                                                              while(x->s)
       o->up();
                                                  40
                                                                                                    102
                                                             b->s=b->ch[0]->s+b->ch[1]->s+1;
                                                                                                              if(data<x->data)y=x,x=x->ch[0];
14
                                                  41
                                                                                                                                                         3.2 ext.cpp
15
                                                  42
                                                             return b:
                                                                                                    104
                                                                                                              else x=x->ch[1];
   node *merge(node *a,node *b){
                                                  43
                                                                                                    105
                                                                                                             if(y)return y->data;
    if(!a||!b)return a?a:b;
                                                  44
                                                                                                   106
                                                                                                              return data;
                                                                                                                                                          __gnu_pbds::tree<int,null_type,less<int>,
    static int x;
                                                  45
                                                         bool erase(node *&o,const T &data){
                                                                                                    107
                                                                                                                                                               rb tree tag,
```

108

109 };

int size(){return root->s;}

3.3 IncStack.cpp

```
1 //Magic
#pragma GCC optimize "Ofast"
3 //stack resize, change esp to rsp if 64-bit
4 asm("mov %0, %%esp\n" :: "q"(mem+10000000));
5 //linux stack resize
6 #include < sys/resource.h>
   void increase stack(){
    const rlim_t ks=64*1024*1024;
    struct rlimit rl;
    int res=getrlimit(RLIMIT_STACK,&rl);
    if(!res&&rl.rlim cur<ks){</pre>
12
       rl.rlim cur=ks;
       res=setrlimit(RLIMIT_STACK,&rl);
13
14
```

3.4 input.cpp

```
inline int read(){
   int x=0; bool f=0; char c=getchar();
   while(ch<'0'||'9'<ch)f|=ch=='-',ch=
       getchar();

while('0'<=ch&&ch<='9')x=x*10-'0'+ch,ch=
       getchar();
   return f?-x:x;

//g++ -std=c++11 -02 -Wall -Wextra -Wno-
   unused-variable $1 && ./a.out</pre>
```

4 Flow

4.1 dinic.cpp

```
1 template<typename T>
   struct DINIC{
    static const int MAXN=105:
    static const T INF=INT MAX;
    int n;//點數
    int level[MAXN], cur[MAXN];
    struct edge{
      int v,pre;
      T cap,flow,r;
      edge(int v,int pre,T cap):v(v),pre(pre),
           cap(cap),flow(0),r(cap){}
    };
    int g[MAXN];
    vector<edge> e;
    void init(int n){
      memset(g,-1,sizeof(int)*((n= n)+1));
16
      e.clear();
17
    void add edge(int u,int v,T cap,bool
         directed=false){
      e.push back(edge(v,g[u],cap));
```

4.2 ISAP with cut.cpp

g[u]=e.size()-1;

g[v]=e.size()-1;

int bfs(int s,int t){

queue<int >q;

while(q.size()){

q.push(s);

return 0;

T df:

level[s]=1;

e.push_back(edge(u,g[v],directed?0:cap))

memset(level.0.sizeof(int)*(n+1));

for(int i=g[u];~i;i=e[i].pre){

if(e[i].v==t)return 1;

dfs(int u,int t,T cur flow=INF){

for(int &i=cur[u];~i;i=e[i].pre){

T dinic(int s,int t,bool clean=true){

for(size t i=0;i<e.size();++i){</pre>

while(bfs(s,t))while(mf=dfs(s,t))ans+=mf

if(level[e[i].v]==level[u]+1&&e[i].r){

if(df=dfs(e[i].v,t,min(cur_flow,e[i]

if(u==t)return cur flow;

].r))){

e[i].r-=df;

return df;

return level[u]=0;

e[i].flow=0;

e[i].r=e[i].cap;

if(clean){

T ans=0, mf=0;

return ans;

e[i^1].r+=df;

e[i].flow+=df:

 $e[i^1].flow-=df;$

if(!level[e[i].v]&&e[i].r){

level[e[i].v]=level[u]+1;

memcpy(cur,g,sizeof(int)*(n+1));

int u=q.front();q.pop();

q.push(e[i].v);

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

30

31

33

35

36

37

38

39

40

41

42

43

44

45

48

49

50

53

55

56

62

64

65

66

21

22

23

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47

48

49

50

51

52

53

54

55

56

57

58

59

60

61

62

63

64

65

67

68

69 };

```
template<typename T>
struct ISAP{
static const int MAXN=105;
static const T INF=INT_MAX;
int n;//點數
int d[MAXN],gap[MAXN],cur[MAXN];
struct edge{
```

```
T min cut(int s,int t){
  int v,pre;
  T cap, flow, r;
                                                   T ans=isap(s,t);
  edge(int v,int pre,T cap):v(v),pre(pre),
                                                   memset(vis,0,sizeof(bool)*(n+1));
                                                   dfs cut(s), cut e.clear();
       cap(cap),flow(0),r(cap){}
                                                   for(int u=0;u<=n;++u){</pre>
                                            71
int g[MAXN];
                                                     if(vis[u])for(int i=g[u];~i;i=e[i].pre
                                            72
vector<edge> e:
void init(int _n){
                                                        if(!vis[e[i].v])cut_e.push_back(i);
                                            73
  memset(g, -1, \overline{sizeof(int)}*((n=n)+1));
                                            74
  e.clear();
                                            75
                                            76
                                                   return ans;
void add edge(int u,int v,T cap,bool
                                            77
    directed=false){
  e.push_back(edge(v,g[u],cap));
  g[u]=e.size()-1;
  e.push_back(edge(u,g[v],directed?0:cap))
                                               4.3 MinCostMaxFlow.cpp
  g[v]=e.size()-1;
T dfs(int u,int s,int t,T cur flow=INF){
                                              1 template < typename T>
  if(u==t)return cur flow;
                                               struct MCMF{
  T tf=cur flow,df;
                                                 static const int MAXN=440:
  for(int &i=cur[u];~i;i=e[i].pre){
                                                 if(e[i].r&&d[u]==d[e[i].v]+1){
                                                 struct edge{
      df=dfs(e[i].v,s,t,min(tf,e[i].r));
                                                   int v,pre;
      e[i].flow+=df:
                                                    _T cap,cost;
      e[i^1].flow-=df;
                                                   edge(int v,int pre,_T cap,_T cost):v(v),
      e[i].r-=df;
                                                        pre(pre), cap(cap), cost(cost){}
      e[i^1].r+=df;
      if(!(tf-=df)||d[s]==n)return
                                                 int n,S,T;
                                                  T dis[MAXN],piS,ans;
           cur flow-tf;
                                            11
                                                 bool vis[MAXN];
                                                 vector<edge> e;
                                                 int g[MAXN];
  int mh=n;
                                            14
  for(int i=cur[u]=g[u];~i;i=e[i].pre){
                                                 void init(int _n){
    if(e[i].r&&d[e[i].v]<mh)mh=d[e[i].v];</pre>
                                                   memset(g, -1, sizeof(int)*((n= n)+1));
                                            17
                                                   e.clear();
  if(!--gap[d[u]])d[s]=n;
                                            18
  else ++gap[d[u]=++mh];
                                            19
                                                 void add_edge(int u,int v,_T cap,_T cost,
  return cur_flow-tf;
                                                      bool directed=false){
                                                   e.push back(edge(v,g[u],cap,cost));
                                            20
T isap(int s,int t,bool clean=true){
                                            21
                                                   g[u]=e.size()-1;
  memset(d,0,sizeof(int)*(n+1));
                                                   e.push_back(edge(u,g[v],directed?0:cap,-
                                            22
  memset(gap,0,sizeof(int)*(n+1));
                                                        cost));
  memcpy(cur,g,sizeof(int)*(n+1));
                                                   g[v]=e.size()-1;
                                            23
  if(clean){
                                            ^{24}
    for(size t i=0;i<e.size();++i){</pre>
                                                 T augment(int u, T cur flow){
      e[i].flow=0;
                                                   if(u==T||!cur flow)return ans+=piS*
      e[i].r=e[i].cap;
                                                        cur_flow,cur_flow;
                                                   vis[u]=1;
                                            27
                                                   _T r=cur_flow,d;
                                                   for(int i=g[u];~i;i=e[i].pre){
  T max flow=0;
  for(gap[0]=n;d[s]<n;)max flow+=dfs(s,s,t 30</pre>
                                                     if(e[i].cap&&!e[i].cost&&!vis[e[i].v])
  return max flow;
                                            31
                                                       d=augment(e[i].v,min(r,e[i].cap));
                                            32
                                                       e[i].cap-=d;
                                                       e[i^1].cap+=d;
vector<int> cut e;//最小割邊集
                                                       if(!(r-=d))break;
                                            34
bool vis[MAXN];
void dfs_cut(int u){
                                            35
                                            36
  vis[u]=1;//表示u屬於source的最小割集
                                            37
                                                   return cur flow-r;
  for(int i=g[u];~i;i=e[i].pre){
    if(e[i].flow<e[i].cap&&!vis[e[i].v])</pre>
                                                 bool modlabel(){
         dfs_cut(e[i].v);
                                                   for(int u=0;u<=n;++u)dis[u]=INF;</pre>
                                                   static deque<int>q;
                                            41
```

dis[T]=0,q.push back(T);

27 }

```
while(q.size()){
         int u=q.front();q.pop front();
44
45
         for(int i=g[u];~i;i=e[i].pre){
46
           if(e[i^1].cap&&(dt=dis[u]-e[i].cost)
                 <dis[e[i].v]){
             if((dis[e[i].v]=dt)<=dis[q.size()?</pre>
                  q.front():S]){
                q.push front(e[i].v);
             }else q.push_back(e[i].v);
51
52
53
54
       for(int u=0:u<=n:++u)</pre>
55
         for(int i=g[u];~i;i=e[i].pre)
56
           e[i].cost+=dis[e[i].v]-dis[u];
57
       piS+=dis[S]:
       return dis[S]<INF;</pre>
58
59
     _T mincost(int s,int t){
60
61
       S=s,T=t;
       piS=ans=0:
62
       while(modlabel()){
63
         do memset(vis,0,sizeof(bool)*(n+1));
65
         while(augment(S,INF));
66
67
       return ans;
68
69 };
```

Graph

5.1 Augmenting Path.cpp

```
1 #define MAXN1 505
2 #define MAXN2 505
3 int n1, n2; //n1 個點連向n2個點
4 int match[MAXN2]; //屬於n2的點匹配了哪個點
5 vector<int > g[MAXN1];// \B
6 bool vis[MAXN2];//是否走訪過
  bool dfs(int u){
    for(size_t i=0;i<g[u].size();++i){</pre>
      int v=g[u][i];
      if(vis[v])continue;
       vis[v]=1;
      if(match[v]==-1||dfs(match[v])){
        match[v]=u;
14
         return 1;
15
16
    }
    return 0;
17
   inline int max_match(){
    int ans=0:
    memset(match,-1,sizeof(int)*n2);
    for(int i=0;i<n1;++i){</pre>
      memset(vis,0,sizeof(bool)*n2);
24
      if(dfs(i))++ans;
25
    return ans;
```

5.2 Augmenting Path multiple.

11

16

17

26

27

28

29

30

31

32

33

34

36

37

38

39

40

41

42

43

44

45

46

```
1 #define MAXN1 1005
2 #define MAXN2 505
3 int n1, n2; //n1個點連向n2個點,其中n2個點可以
        匹配很多邊
4 vector<int > g[MAXN1];// 🗐
5 int c[MAXN2]; //每個屬於 n2 點最多可以接受幾條
 6 | vector<int> match list[MAXN2];//每個屬於n2的
        點匹配了那些點
  bool vis[MAXN2];//是否走訪過
  bool dfs(int u){
    for(size_t i=0;i<g[u].size();++i){</pre>
      int v=g[u][i];
11
      if(vis[v])continue;
       vis[v]=true;
12
       if((int)match_list[v].size()<c[v]){</pre>
        match list[v].push back(u);
14
        return true;
15
16
       }else{
17
         for(size_t j=0;j<match_list[v].size()</pre>
             ;++j){
           int next u=match list[v][j];
18
19
           if(dfs(next u)){
20
             match list[v][j]=u;
21
             return true;
^{22}
23
24
    return false;
27
   inline int max match(){
    for(int i=0;i<n2;++i)match_list[i].clear()</pre>
    int cnt=0:
30
     for(int u=0;u<n1;++u){</pre>
31
      memset(vis,0,sizeof(bool)*n2);
33
      if(dfs(u))++cnt;
34
     return cnt;
```

blossom matching.cpp

```
1 #define MAXN 505
vector<int>g[MAXN];
int pa[MAXN], match[MAXN], st[MAXN], S[MAXN], v[
4 int t,n;
5 inline int lca(int x,int y){
    for(++t;;swap(x,y)){
      if(x==0)continue;
      if(v[x]==t)return x;
      v[x]=t;
```

```
x=st[pa[match[x]]];
12 }
13 #define qpush(x) q.push(x),S[x]=0
   inline void flower(int x,int y,int l,queue
     while(st[x]!=1){
       pa[x]=y;
       if(S[y=match[x]]==1)qpush(y);
       st[x]=st[y]=1,x=pa[y];
20
   inline bool bfs(int x){
    for(int i=1:i<=n:++i)st[i]=i;</pre>
     memset(S+1,-1,sizeof(int)*n);
     queue<int>q;qpush(x);
     while(q.size()){
       x=q.front(),q.pop();
       for(size_t i=0;i<g[x].size();++i){</pre>
         int y=g[x][i];
         if(S[y]==-1){
           pa[y]=x,S[y]=1;
           if(!match[y]){
             for(int lst;x;y=lst,x=pa[y])
               lst=match[x], match[x]=y, match[y
                    ]=x;
             return 1;
           qpush(match[y]);
         }else if(!S[y]&&st[y]!=st[x]){
           int l=lca(y,x);
           flower(y,x,1,q),flower(x,y,1,q);
    return 0;
  inline int blossom(){
    int ans=0:
    for(int i=1;i<=n;++i)</pre>
      if(!match[i]&&bfs(i))++ans;
    return ans:
```

5.4 graphISO.cpp

```
1 const int MAXN=1005, K=30; // K要 夠 大
2 const long long A=3,B=11,C=2,D=19,P=0
       xdefaced:
 3 long long f[K+1][MAXN];
4 vector<int> g[MAXN],rg[MAXN];
5 int n;
6 inline void init(){
     for(int i=0;i<n;++i){</pre>
       f[0][i]=1;
      g[i].clear();
       rg[i].clear();
11
12 }
  inline void add edge(int u,int v){
    g[u].push_back(v);
15
    rg[v].push_back(u);
```

```
17 inline long long point hash(int u){//0(N)
    for(int t=1;t<=K;++t){
      for(int i=0;i<n;++i){</pre>
        f[t][i]=f[t-1][i]*A%P;
20
        for(int j:g[i])f[t][i]=(f[t][i]+f[t
             -1][j]*B%P)%P;
        for(int j:rg[i])f[t][i]=(f[t][i]+f[t
             -1][j]*C%P)%P;
        if(i==u)f[t][i]+=D;//如果圖太大的話
             把這行刪掉,執行一次後f[K]就會是所
             有點的答案
        f[t][i]%=P;
24
25
26
27
    return f[K][u];
28
   inline vector<long long> graph hash(){
    vector<long long> ans;
    for(int i=0;i<n;++i)ans.push back(</pre>
         point hash(i))://0(N^2)
    sort(ans.begin(),ans.end());
32
33
    return ans:
```

5.5 KM.cpp

```
1 | #define MAXN 100
3 int g[MAXN][MAXN], lx[MAXN], ly[MAXN], slack y[
       MAXN];
  int match_y[MAXN];
5 bool vx[MAXN], vy[MAXN]; //要保證g是完全二分圖
6|bool dfs(int x,bool adjust=1){//DFS找增廣
        路, is=1表示要交換邊
    if(vx[x])return 0;
     vx[x]=1;
     for(int y=0;y<n;++y){</pre>
      if(vy[y])continue;
      int t=lx[x]+ly[y]-g[x][y];
11
12
      if(t==0){
13
         vy[y]=1;
14
         if(match_y[y]==-1||dfs(match_y[y],
              adjust)){
           if(adjust)match_y[y]=x;
16
           return 1;
17
      }else if(slack_y[y]>t)slack_y[y]=t;
18
19
20
    return 0;
21
  inline int km(){
     memset(ly,0,sizeof(int)*n);
     memset(match y,-1,sizeof(int)*n);
     for(int x=0;x<n;++x){
27
       for(int y=0;y<n;++y){</pre>
28
        1x[x]=max(1x[x],g[x][y]);
29
30
     for(int x=0;x<n;++x){
       for(int y=0;y<n;++y)slack_y[y]=INT_MAX;</pre>
       memset(vx,0,sizeof(bool)*n);
```

if(dep+dp[u]<=ans)return 0;</pre>

return false;

```
memset(vy,0,sizeof(bool)*n);
                                                            for(int j=i+1; j<ns; ++j){</pre>
                                                                                                                                                               return cost<e.cost;</pre>
       if(dfs(x))continue;
35
                                                  26
                                                              int v=stk[dep][i];
                                                                                                     39
                                                                                                                                                        23
36
       bool flag=1;
                                                  27
                                                              if(g[u][v])stk[dep+1][cnt++]=v;
                                                                                                          int solve() {
                                                                                                                                                        24
                                                                                                     40
                                                                                                                                                          };
                                                                                                                                                          struct bit node{
37
       while(flag){
                                                  28
                                                                                                     41
                                                                                                            // find a match
         int cut=INT MAX;
                                                  29
                                                            tmp[dep]=u;
                                                                                                            for (int i=0; i<n; i+=2){</pre>
                                                                                                                                                            T mi;
38
                                                                                                     42
                                                                                                                                                        26
                                                           if(dfs(cnt,dep+1))return 1;
39
         for(int y=0;y<n;++y){</pre>
                                                  30
                                                                                                     43
                                                                                                              match[i] = i+1;
                                                                                                                                                        27
                                                                                                                                                            int id:
           if(!vy[y]&&cut>slack y[y])cut=
                                                  31
                                                                                                     44
                                                                                                              match[i+1] = i:
                                                                                                                                                            bit node(const T&mi=INF, int id=-1):mi(mi).
                slack_y[y];
                                                                                                     45
                                                                                                                                                                 id(id){}
                                                  32
                                                         return 0;
41
                                                  33
                                                                                                     46
                                                                                                            for(;;){
         for(int j=0;j<n;++j){</pre>
                                                       int clique(){
                                                                                                     47
                                                                                                              int found = 0;
                                                                                                                                                          std::vector<bit_node> bit;
42
                                                  34
43
           if(vx[i])lx[i]-=cut;
                                                  35
                                                         int u,v,ns;
                                                                                                     48
                                                                                                              for (int i=0; i<n; i++)</pre>
                                                                                                                                                          inline void bit update(int i,const T&data,
           if(vy[j])ly[j]+=cut;
                                                         for(ans=0,u=N-1;u>=0;--u){
                                                                                                                dis[i] = onstk[i] = 0:
                                                                                                                                                               int id){
44
                                                  36
                                                                                                     49
           else slack_y[j]-=cut;
                                                            for(ns=0, tmp[0]=u, v=u+1; v<N; ++v)</pre>
                                                                                                              for (int i=0; i<n; i++){</pre>
                                                                                                                                                             for(;i;i-=i&(-i)){
45
                                                  37
                                                                                                     50
                                                                                                                                                        32
                                                                                                                                                              if(data<bit[i].mi)bit[i]=bit node(data,</pre>
46
                                                  38
                                                              if(g[u][v])stk[1][ns++]=v;
                                                                                                     51
                                                                                                                stk.clear():
47
         for(int y=0;y<n;++y){</pre>
                                                  39
                                                            dfs(ns,1),dp[u]=ans;
                                                                                                     52
                                                                                                                if (!onstk[i] && SPFA(i)){
           if(!vy[y]&&slack_y[y]==0){
                                                  40
                                                                                                     53
                                                                                                                  found = 1;
                                                                                                                                                        34
                                                                                                                  while (stk.size()>=2){
49
             vy[y]=1;
                                                  41
                                                         return ans;
                                                                                                     54
                                                                                                                                                        35
             if(match_y[y]==-1||dfs(match_y[y
                                                                                                                    int u = stk.back(); stk.pop_back
                                                                                                                                                          inline int bit_find(int i,int m){
50
                                                  42
                                                                                                                                                       36
                                                                                                                                                            bit node x;
                                                  43 };
                  ],0)){
                                                                                                                    int v = stk.back(); stk.pop back 38
                                                                                                                                                             for(;i<=m;i+=i&(-i)){</pre>
               flag=0;//測試成功,有增廣路
                                                                                                                                                        39
                                                                                                                                                              if(bit[i].mi<x.mi)x=bit[i];</pre>
               break;
                                                                                                                    match[u] = v;
                                                                                                                                                        40
                                                     5.7 Minimum General Weighter
                                                                                                                    match[v] = u;
                                                                                                                                                        41
                                                                                                                                                            return x.id;
54
                                                                                                                                                        42
                                                                                                                                                          inline std::vector<edge> build graph(int n,
                                                   1 | struct Graph {
                                                                                                     61
                                                                                                                                                               point p[]){
       memset(vx,0,sizeof(bool)*n);
                                                       // Minimum General Weighted Matching (
                                                                                                              if (!found) break;
                                                                                                     62
                                                                                                                                                             std::vector<edge> e;//回傳的邊就可以用來求
       memset(vy,0,sizeof(bool)*n);
                                                            Perfect Match) 0-base
                                                                                                     63
       dfs(x);//最後要記得將邊翻反轉
                                                                                                                                                                  最小生成樹
                                                       static const int MXN = 105;
                                                                                                     64
                                                                                                            int ret = 0;
60
                                                                                                                                                             for(int dir=0;dir<4;++dir){//4種座標變換
                                                                                                                                                        45
                                                                                                     65
                                                                                                            for (int i=0; i<n; i++)</pre>
     int ans=0;
                                                                                                                                                               if(dir%2){
                                                       int n, edge[MXN][MXN];
                                                                                                     66
                                                                                                              ret += edge[i][match[i]];
    for(int y=0;y<n;++y)ans+=g[match_y[y]][y];</pre>
                                                                                                                                                                 for(int i=0;i<n;++i)std::swap(p[i].x,p</pre>
                                                       int match[MXN], dis[MXN], onstk[MXN];
                                                                                                     67
                                                                                                            ret /= 2;
    return ans;
                                                                                                                                                                      [i].y);
                                                       vector<int> stk:
                                                                                                     68
                                                                                                            return ret:
64
                                                                                                                                                               }else if(dir==2){
                                                                                                     69
                                                                                                                                                                 for(int i=0;i<n;++i)p[i].x=-p[i].x;</pre>
                                                                                                                                                        49
                                                       void init(int _n) {
                                                                                                     70 } graph;
                                                                                                                                                        50
                                                                                                                                                        51
                                                                                                                                                               std::sort(p,p+n,cmpx);
                                                         for (int i=0; i<n; i++)</pre>
  5.6 MaximumClique.cpp
                                                                                                                                                              std::vector<T>ga(n),gb;
                                                            for (int j=0; j<n; j++)</pre>
                                                   12
                                                                                                                                                               for(int i=0;i<n;++i)ga[i]=p[i].y-p[i].x;</pre>
                                                  13
                                                              edge[i][j] = 0;
                                                                                                        5.8 Rectilinear Steiner tree.cpt
                                                                                                                                                               gb=ga;
                                                  14
                                                                                                                                                               std::sort(gb.begin(),gb.end());
1 | struct MaxClique{
                                                       void add edge(int u, int v, int w) {
                                                  15
                                                                                                                                                               gb.resize(std::unique(gb.begin(),gb.end
     static const int MAXN=105;
                                                         edge[u][v] = edge[v][u] = w;
                                                   16
                                                                                                                                                                    ())-gb.begin());
     int N,ans;
                                                                                                      1 // 平面曼哈頓最小生成樹構造圖(去除非必要邊)
                                                                                                                                                               int m=gb.size();
     int g[MAXN][MAXN], dp[MAXN], stk[MAXN][MAXN
                                                                                                      2 #include < vector >
                                                        bool SPFA(int u){
                                                                                                                                                               bit=std::vector<bit node>(m+1);
                                                                                                      3 #include < algorithm>
                                                         if (onstk[u]) return true;
                                                                                                                                                        59
                                                                                                                                                               for(int i=n-1;i>=0;--i){
                                                                                                      4 #define T int
     int sol[MAXN], tmp[MAXN]; //sol[0~ans-1]為答
                                                         stk.push back(u);
                                                                                                                                                        60
                                                                                                                                                                 int pos=std::lower_bound(gb.begin(),gb
                                                                                                      5 #define INF 0x3f3f3f3f
                                                         onstk[u] = 1;
                                                                                                                                                                      .end(),ga[i])-gb.begin()+1;
                                                                                                      6 struct point{
     void init(int n){
                                                          for (int v=0; v<n; v++){</pre>
                                                                                                                                                                 int ans=bit_find(pos,m);
                                                                                                         T x, y;
                                                           if (u != v && match[u] != v && !onstk[
       N=n;//0-base
                                                                                                                                                                 if(~ans)e.push back(edge(p[i].id,p[ans
                                                                                                          int id;//每個點的編號都要不一樣,從0開始編
       memset(g,0,sizeof(g));
                                                                v]){
                                                                                                                                                                      ].id,p[i].dist(p[ans])));
                                                              int m = match[v];
                                                                                                                                                                 bit_update(pos,p[i].x+p[i].y,i);
     void add edge(int u,int v){
                                                  25
                                                              if (dis[m] > dis[u] - edge[v][m] +
                                                                                                          point(){}
                                                                                                                                                        64
                                                                                                          T dist(const point &p)const{
       g[u][v]=g[v][u]=1;
                                                                   edge[u][v]){
12
                                                                dis[m] = dis[u] - edge[v][m] +
                                                                                                            return std::abs(x-p.x)+std::abs(y-p.y);
                                                                                                                                                             return e;
     int dfs(int ns,int dep){
                                                                     edge[u][v];
                                                                                                     12
                                                                                                     13 };
       if(!ns){
                                                                onstk[v] = 1;
15
         if(dep>ans){
                                                                stk.push back(v);
                                                                                                     14 inline bool cmpx(const point &a,const point
                                                  28
           ans=dep;
                                                                if (SPFA(m)) return true;
                                                                                                          return a.x<b.x||(a.x==b.x&&a.y<b.y);</pre>
           memcpy(sol,tmp,sizeof tmp);
                                                                stk.pop_back();
                                                                                                                                                          5.9 treeISO.cpp
           return 1:
                                                  31
                                                                onstk[v] = 0;
                                                                                                     16 }
19
         }else return 0;
                                                  32
                                                                                                     17 struct edge{
20
                                                  33
                                                                                                          int u,v;
       for(int i=0;i<ns;++i){</pre>
                                                  34
                                                                                                                                                         1 | const int MAXN=100005;
                                                                                                                                                        const long long X=12327,P=0xdefaced;
22
         if(dep+ns-i<=ans)return 0;</pre>
                                                         onstk[u] = 0;
                                                                                                          edge(int u,int v,const T&c):u(u),v(v),cost
         int u=stk[dep][i],cnt=0;
                                                         stk.pop_back();
                                                                                                                                                        3 vector<int> g[MAXN];
23
```

bool operator<(const edge&e)const{</pre>

4 bool vis[MAXN];

```
5 long long dfs(int u){
                                                           return (int)flower[b].size()-pr;
                                                                                                                                                          158
                                                                                                                                                                       else if(S[x]==0)d=min(d,e delta(g[
     vis[u]=1;
                                                   42
                                                        }else return pr;
                                                                                                            set slack(b);
                                                                                                                                                                            slack[x]][x])/2);
     vector<long long> tmp;
                                                    43 }
                                                                                                       99
                                                                                                                                                          159
     for(auto v:g[u])if(!vis[v])tmp.push back(
                                                   44 void set match(int u,int v){
                                                                                                       100
                                                                                                          void expand blossom(int b){ // S[b] == 1
                                                                                                                                                          160
                                                                                                                                                                  for(int u=1;u<=n;++u){</pre>
                                                         match[u]=g[u][v].v;
                                                                                                            for(size t i=0;i<flower[b].size();++i)</pre>
                                                                                                                                                                    if(S[st[u]]==0){
                                                   45
                                                                                                       101
                                                                                                                                                          161
     if(tmp.empty())return 177;
                                                    46
                                                        if(u>n){
                                                                                                      102
                                                                                                               set st(flower[b][i],flower[b][i]);
                                                                                                                                                          162
                                                                                                                                                                       if(lab[u]<=d)return 0;</pre>
10
     long long ret=4931:
                                                   47
                                                           edge e=g[u][v];
                                                                                                       103
                                                                                                            int xr=flower_from[b][g[b][pa[b]].u],pr=
                                                                                                                                                          163
                                                                                                                                                                       lab[u]-=d:
     sort(tmp.begin(),tmp.end());
                                                           int xr=flower_from[u][e.u],pr=get_pr(u,
                                                                                                                  get_pr(b,xr);
                                                                                                                                                                    }else if(S[st[u]]==1)lab[u]+=d;
11
                                                    48
                                                                                                                                                          164
12
    for(auto v:tmp)ret=((ret*X)^v)%P;
                                                                                                      104
                                                                                                            for(int i=0;i<pr;i+=2){</pre>
                                                                                                                                                          165
13
                                                           for(int i=0;i<pr;++i)set_match(flower[u</pre>
                                                                                                               int xs=flower[b][i],xns=flower[b][i+1];
                                                                                                                                                                  for(int b=n+1;b<=n_x;++b)</pre>
    return ret;
                                                    49
                                                                                                      105
                                                                                                                                                          166
                                                                [i],flower[u][i^1]);
14
                                                                                                               pa[xs]=g[xns][xs].u;
                                                                                                                                                                    if(st[b]==b){
                                                                                                       106
                                                                                                                                                          167
                                                           set match(xr.v):
                                                                                                                                                                       if(S[st[b]]==0)lab[b]+=d*2;
                                                   50
                                                                                                       107
                                                                                                               S[xs]=1,S[xns]=0;
                                                                                                                                                          168
                                                           rotate(flower[u].begin(),flower[u].begin 108
                                                                                                               slack[xs]=0, set_slack(xns);
                                                                                                                                                                       else if(S[st[b]]==1)lab[b]-=d*2;
                                                   51
                                                                                                                                                          169
                                                                ()+pr,flower[u].end());
                                                                                                      109
                                                                                                               q push(xns);
                                                                                                                                                          170
  5.10 一般圖最大權匹配.cpp
                                                    52
                                                                                                      110
                                                                                                                                                          171
                                                                                                                                                                  q=queue<int>();
                                                    53
                                                                                                      111
                                                                                                            S[xr]=1,pa[xr]=pa[b];
                                                                                                                                                                  for(int x=1;x<=n x;++x)</pre>
                                                                                                                                                          172
                                                                                                                                                                    if(st[x]==x&&slack[x]&&st[slack[x]]!=x
                                                    54
                                                       void augment(int u,int v){
                                                                                                      112
                                                                                                            for(size t i=pr+1;i<flower[b].size();++i){ 173</pre>
1 #include < bits / stdc++.h>
                                                    55
                                                         for(;;){
                                                                                                      113
                                                                                                               int xs=flower[b][i];
                                                                                                                                                                          &&e_delta(g[slack[x]][x])==0)
2 using namespace std;
                                                    56
                                                           int xnv=st[match[u]];
                                                                                                               S[xs]=-1, set_slack(xs);
                                                                                                                                                                       if(on_found_edge(g[slack[x]][x]))
                                                                                                      114
                                                                                                                                                          174
3 #define INF INT MAX
                                                           set match(u,v);
                                                    57
                                                                                                      115
                                                                                                                                                                            return true;
4 #define MAXN 400
                                                                                                                                                                  for(int b=n+1;b<=n_x;++b)</pre>
                                                    58
                                                           if(!xnv)return;
                                                                                                      116
                                                                                                            st[b]=0;
                                                                                                                                                          175
  struct edge{
                                                           set_match(xnv,st[pa[xnv]]);
                                                                                                                                                                     if(st[b]==b&&S[b]==1&&lab[b]==0)
                                                    59
                                                                                                      117
                                                                                                                                                          176
    int u,v,w;
                                                    60
                                                          u=st[pa[xnv]],v=xnv;
                                                                                                      118
                                                                                                          bool on found edge(const edge &e){
                                                                                                                                                                          expand blossom(b):
    edge(){}
                                                                                                            int u=st[e.u],v=st[e.v];
                                                    61
                                                                                                      119
                                                                                                                                                          177
    edge(int u,int v,int w):u(u),v(v),w(w){}
                                                    62 }
                                                                                                      120
                                                                                                            if(S[v]==-1){
                                                                                                                                                          178
                                                                                                                                                                return false;
                                                    63 int get_lca(int u,int v){
                                                                                                               pa[v]=e.u,S[v]=1;
                                                                                                       121
                                                                                                                                                          179
   int n,n_x;
                                                                                                               int nu=st[match[v]];
                                                    64
                                                         static int t=0;
                                                                                                      122
                                                                                                                                                          180
                                                                                                                                                              pair<long long,int> weight_blossom(){
   edge g[MAXN*2+1][MAXN*2+1];
                                                    65
                                                         for(++t;u||v;swap(u,v)){
                                                                                                               slack[v]=slack[nu]=0;
                                                                                                                                                                memset(match+1,0,sizeof(int)*n);
                                                                                                      123
  int lab[MAXN*2+1];
                                                          if(u==0)continue;
                                                                                                               S[nu]=0,q_push(nu);
                                                                                                      124
                                                                                                                                                          182
                                                                                                                                                                n_x=n;
int match[MAXN*2+1], slack[MAXN*2+1], st[MAXN
                                                          if(vis[u]==t)return u;
                                                                                                            }else if(S[v]==0){
                                                                                                                                                          183
                                                                                                                                                                int n_matches=0;
                                                                                                       125
        *2+1],pa[MAXN*2+1];
                                                                                                               int lca=get lca(u,v);
                                                                                                                                                                long long tot_weight=0;
                                                           vis[u]=t;//這種方法可以不用清空ν陣列
                                                                                                       126
                                                                                                                                                          184
14 int flower from[MAXN*2+1][MAXN+1],S[MAXN
                                                                                                               if(!lca){
                                                                                                                                                                for(int u=0;u<=n;++u)st[u]=u,flower[u].</pre>
                                                                                                       127
                                                                                                                                                          185
                                                           u=st[match[u]];
        *2+1], vis[MAXN*2+1];
                                                                                                       128
                                                                                                                 augment(u,v),augment(v,u);
                                                                                                                                                                     clear();
                                                          if(u)u=st[pa[u]];
                                                    70
  vector<int> flower[MAXN*2+1];
                                                                                                       129
                                                                                                                 return true;
                                                                                                                                                          186
                                                                                                                                                                int w max=0;
                                                    71
   queue<int> q;
                                                                                                                                                                for(int u=1;u<=n;++u)</pre>
                                                                                                       130
                                                                                                               }else add_blossom(u,lca,v);
                                                        return 0;
                                                                                                                                                          187
  int e_delta(const edge &e){ // does not work
                                                                                                                                                                  for(int v=1;v<=n;++v){</pre>
                                                                                                       131
                                                                                                                                                          188
                                                    73 }
         inside blossoms
                                                                                                            return false;
                                                                                                                                                                    flower_from[u][v]=(u==v?u:0);
                                                       void add blossom(int u,int lca,int v){
                                                                                                       132
                                                                                                                                                          189
    return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
                                                                                                       133
                                                                                                                                                          190
                                                                                                                                                                     w_max=max(w_max,g[u][v].w);
                                                         int b=n+1:
19
                                                                                                       134
                                                                                                          bool matching(){
                                                                                                                                                          191
                                                         while(b \le n \times \&st[b])++b;
   void update slack(int u,int x){
                                                                                                            memset(S+1,-1,sizeof(int)*n_x);
                                                         if(b>n x)++n x;
                                                                                                                                                          192
                                                                                                                                                                for(int u=1;u<=n;++u)lab[u]=w_max;</pre>
    if(!slack[x]||e delta(g[u][x])<e delta(g[</pre>
                                                                                                       136
                                                                                                            memset(slack+1,0,sizeof(int)*n x);
                                                                                                                                                          193
                                                                                                                                                                while(matching())++n matches;
                                                         lab[b]=0,S[b]=0;
          slack[x]][x]))slack[x]=u;
                                                                                                                                                                for(int u=1;u<=n;++u)</pre>
                                                                                                       137
                                                                                                            q=queue<int>();
                                                         match[b]=match[lca];
                                                                                                                                                          194
22
                                                                                                                                                                  if(match[u]&&match[u]<u)</pre>
                                                         flower[b].clear();
                                                                                                       138
                                                                                                            for(int x=1;x \le n x;++x)
                                                                                                                                                          195
   void set_slack(int x){
23
                                                                                                              if(st[x]==x&&!match[x])pa[x]=0,S[x]=0,
                                                                                                                                                                     tot_weight+=g[u][match[u]].w;
                                                                                                       139
                                                         flower[b].push_back(lca);
                                                                                                                                                          196
24
    slack[x]=0;
                                                                                                                                                                return make_pair(tot_weight,n_matches);
                                                         for(int x=u,y;x!=lca;x=st[pa[y]])
                                                                                                                    q_push(x);
                                                                                                                                                          197
    for(int u=1:u<=n:++u)</pre>
25
                                                                                                       140
                                                                                                            if(q.empty())return false;
                                                                                                                                                          198
                                                           flower[b].push back(x),flower[b].
       if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)
26
                                                                                                            for(;;){
                                                                                                                                                              void init_weight_graph(){
                                                                push_back(y=st[match[x]]),q_push(y); 141
                                                                                                                                                          199
            update slack(u,x);
                                                                                                                                                                for(int u=1;u<=n;++u)</pre>
                                                         reverse(flower[b].begin()+1,flower[b].end 142
                                                                                                               while(q.size()){
                                                                                                                                                          200
                                                   84
27
                                                                                                                 int u=q.front();q.pop();
                                                                                                       143
                                                                                                                                                                  for(int v=1;v<=n;++v)</pre>
                                                              ());
   void q_push(int x){
28
                                                                                                                 if(S[st[u]]==1)continue;
                                                                                                                                                                     g[u][v]=edge(u,v,0);
                                                         for(int x=v,y;x!=lca;x=st[pa[y]])
29
    if(x<=n)q.push(x);</pre>
                                                                                                      145
                                                                                                                 for(int v=1; v<=n;++v)</pre>
                                                                                                                                                          203
                                                           flower[b].push back(x),flower[b].
    else for(size_t i=0;i<flower[x].size();i</pre>
30
                                                                                                                   if(g[u][v].w>0&&st[u]!=st[v]){
                                                                                                                                                              int main(){
                                                                push back(y=st[match[x]]),q push(y); 146
          ++)q push(flower[x][i]);
                                                                                                                     if(e delta(g[u][v])==0){
                                                    87
                                                         set_st(b,b);
31
                                                         for(int x=1;x<=n_x;++x)g[b][x].w=g[x][b].w 148
                                                                                                                       if(on_found_edge(g[u][v]))return 206
                                                                                                                                                                scanf("%d%d",&n,&m);
   void set_st(int x,int b){
32
                                                                                                                             true;
                                                                                                                                                                init weight graph();
33
    st[x]=b;
                                                                                                                     }else update_slack(u,st[v]);
                                                                                                                                                                for(int i=0;i<m;++i){</pre>
                                                         for(int x=1;x<=n;++x)flower_from[b][x]=0;</pre>
34
    if(x>n)for(size_t i=0;i<flower[x].size()</pre>
                                                         for(size t i=0;i<flower[b].size();++i){</pre>
                                                                                                      150
                                                                                                                                                          209
                                                                                                                                                                  int u,v,w;
                                                                                                                                                                  scanf("%d%d%d",&u,&v,&w);
                                                          int xs=flower[b][i];
                                                                                                       151
                                                   91
35
         set st(flower[x][i],b);
                                                           for(int x=1;x<=n_x;++x)</pre>
                                                                                                       152
                                                                                                                                                          211
                                                                                                                                                                  g[u][v].w=g[v][u].w=w;
                                                   92
36
                                                                                                               for(int b=n+1;b \le n x;++b)
                                                             if(g[b][x].w==0||e_delta(g[xs][x])
                                                                                                       153
                                                    93
37
   int get pr(int b,int xr){
                                                                                                      154
                                                                                                                if(st[b]==b\&\&S[b]==1)d=min(d,lab[b]/2) 213
                                                                                                                                                                printf("%lld\n", weight blossom().first);
                                                                  e_delta(g[b][x]))
    int pr=find(flower[b].begin(),flower[b].
                                                                                                                                                                for(int u=1;u<=n;++u)printf("%d ",match[u</pre>
                                                               g[b][x]=g[xs][x],g[x][b]=g[x][xs];
                                                   94
          end(),xr)-flower[b].begin();
                                                                                                               for(int x=1;x<=n x;++x)</pre>
                                                                                                                                                                     ]);puts("");
                                                           for(int x=1;x<=n;++x)</pre>
    if(pr%2==1){//檢查他在前一層是奇點還是偶點
                                                             if(flower_from[xs][x])flower_from[b][x 156
                                                                                                                 if(st[x]==x\&\&slack[x])
                                                                                                                                                                return 0;
       reverse(flower[b].begin()+1,flower[b].
                                                                                                                   if(S[x]==-1)d=min(d,e_delta(g[slack[ 216
                                                                                                                                                              }/*7 20
                                                                  ]=xs;
            end());
                                                                                                                        x]][x]));
                                                                                                                                                          217 5 7 9 3 7 4 3 6 6 2 5 8 5 1 9 1 3 6 6 5 1
```

```
218 2 7 4 2 3 5 6 4 2 7 1 5 5 4 4 4 1 3 5 3 9
219 7 6 4 2 1 3 4 3 9 6 2 7 4 2 8 6 1 10
   _____
221 28
222 6 0 4 3 7 1 5*/
  5.11 全局最小割.cpp
 1 const int INF=0x3f3f3f3f3;
   template<typename T>
 3 struct stoer wagner{// 0-base
    static const int MAXN=150:
    T g[MAXN][MAXN], dis[MAXN];
    int nd[MAXN],n,s,t;
    void init(int _n){
```

```
for(int i=0;i<n;++i)</pre>
10
          for(int j=0;j<n;++j)g[i][j]=0;</pre>
11
12
     void add edge(int u,int v,T w){
13
       g[u][v]=g[v][u]+=w;
14
15
     T min cut(){
       T ans=INF;
16
17
       for(int i=0;i<n;++i)nd[i]=i;</pre>
       for(int ind,tn=n;tn>1;--tn){
18
19
          for(int i=1;i<tn;++i)dis[nd[i]]=0;</pre>
20
          for(int i=1;i<tn;++i){</pre>
21
            ind=i;
22
            for(int j=i;j<tn;++j){</pre>
23
              dis[nd[j]]+=g[nd[i-1]][nd[j]];
              if(dis[nd[ind]]<dis[nd[j]])ind=j;</pre>
24
25
26
            swap(nd[ind],nd[i]);
27
28
          if(ans>dis[nd[ind]])ans=dis[t=nd[ind
               ]],s=nd[ind-1];
          for(int i=0;i<tn;++i)</pre>
29
            g[nd[ind-1]][nd[i]]=g[nd[i]][nd[ind
30
                 -1]]+=g[nd[i]][nd[ind]];
31
32
       return ans;
33
34 };
```

5.12 最小樹形圖 朱劉.cpp

```
1 #define INF 0x3f3f3f3f
2 template<typename T>
3 struct zhu_liu{
    static const int MAXN=110;
    struct edge{
      int u,v;
      edge(int u=0, int v=0, T w=0):u(u),v(v),w(
    };
    vector<edge>E;// 0-base
    int pe[MAXN],id[MAXN],vis[MAXN];
    T in[MAXN];
```

language

n=cntnode:

return ans;

root=id[root];

void init(){E.clear();}

T build(int root,int n){

int cntnode=0:

int v=u;

vis[v]=u;

T ans=0; int N=n;

for(;;){

void add edge(int u,int v,T w){

if(u!=v)E.push_back(edge(u,v,w));

for(int u=0;u<n;++u)in[u]=INF;</pre>

for(size t i=0;i<E.size();++i)</pre>

for(int $u=0;u<n;++u)//\mu L$

memset(id,-1,sizeof(int)*N);

if(u!=root)ans+=in[u];

=E[pe[v]].u)

]].u)

if(v!=root&&id[v]==-1){

id[x]=cntnode;

id[v]=cntnode++;

if(!cntnode)break;//µL22

l=cntnode++;

E[i].u=id[E[i].u];

E[i].v=id[E[i].v];

int v=E[i].v;

for(int u=0;u<n;++u){</pre>

memset(vis,-1,sizeof(int)*N);

if(E[i].u!=E[i].v&&E[i].w<in[E[i].v])</pre>

pe[E[i].v]=i,in[E[i].v]=E[i].w;

if(u!=root&&in[u]==INF)return -INF;

for(;vis[v]!=u&&id[v]==-1&&v!=root;v

for(int u=0;u<n;++u)if(id[u]==-1)id[u</pre>

if(E[i].u!=E[i].v)E[i].w-=in[v];

for(size t i=0;i<E.size();++i){</pre>

for(int x=E[pe[v]].u;x!=v;x=E[pe[x 28

14

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47

48

49

51

52

53 };

CNF.cpp

```
1 #define MAXN 55
2 struct CNF{
   int s,x,y;//s->xy \mid s->x, if y==-1
   int cost:
    CNF(){}
    CNF(int s,int x,int y,int c):s(s),x(x),y(y
        ),cost(c){}
s|int state;//規則數量
9 | map<char, int > rule; // 每個字元對應到的規則
      小寫字母為終端字符
```

```
cnf.clear();
  inline void add to cnf(char s.const string &
       p, int cost){
    //加入一個s -> 的文法,代價為cost
    if(rule.find(s)==rule.end())rule[s]=state
     for(auto c:p)if(rule.find(c)==rule.end())
         rule[c]=state++;
     if(p.size()==1){
       cnf.push_back(CNF(rule[s],rule[p[0]],-1,
            cost));
     }else{
       int left=rule[s];
       int sz=p.size();
                                                  11
       for(int i=0;i<sz-2;++i){</pre>
                                                  12
         cnf.push back(CNF(left,rule[p[i]],
                                                  13
             state,0));
         left=state++;
       cnf.push_back(CNF(left,rule[p[sz-2]],
                                                  16
            rule[p[sz-1]],cost));
                                                  17
                                                  18
31 }
32 vector<long long> dp[MAXN][MAXN];
                                                  19
33 | vector<bool> neg_INF[MAXN][MAXN];//如果花費
                                                  21
        是負的可能會有無限小的情形
34 inline void relax(int l,int r,const CNF &c,
                                                  23
       long long cost,bool neg c=0){
     if(!neg_INF[1][r][c.s]&&(neg_INF[1][r][c.x
         ]||cost<dp[1][r][c.s])){
       if(neg_c||neg_INF[l][r][c.x]){
         dp[1][r][c.s]=0;
                                                  26
         neg_INF[1][r][c.s]=true;
       }else dp[l][r][c.s]=cost;
                                                  27
                                                  28
  inline void bellman(int l,int r,int n){
                                                  29
    for(int k=1;k<=state;++k)</pre>
                                                  30
       for(auto c:cnf)
         if(c.y==-1)relax(1,r,c,dp[1][r][c.x]+c
                                                  32
              .cost.k==n);
                                                  33
  inline void cyk(const vector<int> &tok){
    for(int i=0;i<(int)tok.size();++i){</pre>
                                                  36
       for(int j=0;j<(int)tok.size();++j){</pre>
         dp[i][j]=vector<long long>(state+1,
                                                  37
              INT MAX):
                                                  38
         neg_INF[i][j]=vector<bool>(state+1,
                                                  39
              false);
                                                  40
                                                  41
       dp[i][i][tok[i]]=0;
       bellman(i,i,tok.size());
                                                  43
                                                  44
     for(int r=1;r<(int)tok.size();++r){</pre>
                                                  45
       for(int l=r-1;l>=0;--1){
         for(int k=1;k<r;++k)</pre>
```

10 | vector<CNF> cnf;

state=0;

inline void init(){

rule.clear();

11

12

13

14

15

19

20

22

23

26

27

29

30

36

37

38

39

40

41

46

49

50

51

52

53

54

59

60

for(auto c:cnf)

bellman(1,r,tok.size());

if(~c.y)relax(1,r,c,dp[1][k][c.x]+

dp[k+1][r][c.y]+c.cost);

earley.cpp

63

```
1 struct Rule{
     vector<vector<Rule*> > p;
     void add(const vector<Rule*> &1){
      p.push_back(1);
  };
  map<string,Rule*> NameRule;
  map<Rule*,string> RuleName;
   inline void init_Rule(){
    for(auto r:RuleName)delete r.first;
    RuleName.clear();
    NameRule.clear();
  inline Rule *add rule(const string &s){
    if(NameRule.find(s)!=NameRule.end())return
           NameRule[s];
     Rule *r=new Rule():
    RuleName[r]=s;
    NameRule[s]=r;
    return r;
  typedef vector<Rule*> production;
  struct State{
    Rule *r:
    int rid, dot id, start, end;
    State(Rule *r,int rid,int dot,int start):r
          (r),rid(rid),dot id(dot),start(start),
          end(-1){}
    State(Rule *r=0, int col=0):r(r),rid(-1),
          dot id(-1), start(-1), end(col){}
    bool completed()const{
      return rid==-1||dot id>=(int)r->p[rid].
            size();
    Rule *next term()const{
      if(completed())return 0;
      return r->p[rid][dot_id];
     bool operator<(const State& b)const{</pre>
      if(start!=b.start)return start<b.start;</pre>
      if(dot_id!=b.dot_id)return dot_id<b.</pre>
            dot id;
      if(r!=b.r)return r<b.r;</pre>
      return rid<b.rid;</pre>
     void print()const{
      cout<<RuleName[r]<<"->";
      if(rid!=-1)for(size t i=0;;++i){
         if((int)i==dot_id)cout<<" "<<"$";</pre>
         if(i>=r->p[rid].size())break;
         cout<<" "<<RuleName[r->p[rid][i]];
       cout<<" "<<"["<<start<<","<<end<<"]"<<
49 };
50 struct Column{
```

```
Rule *term:
                                                                                                         }else o=pa->child.back().back();
                                                 105
                                                                                                                                                           E.clear();
                                                                                                                                                           for(int i=1;i<=n;++i)de[i]=pv[i]=0;</pre>
     string value;
                                                 106 }
                                                                                                   159
                                                                                                         amb=0;
53
     vector<State> s;
                                                 inline pair <bool, State > parse(Rule *GAMMA,
                                                                                                         for(auto div:table[s.end].div[s]){
                                                                                                   160
                                                                                                                                                      14
                                                                                                                                                         void add edge(int u,int v,T w){
     map<State,set<pair<State,State>>> div;
                                                          const vector<Column > &token){
                                                                                                           if(!amb) build tree(div.first,pa);
                                                       table.resize(token.size()+1);
                                                                                                           build tree(div.second,o,amb);
                                                                                                                                                           E.push back(edge(u,v,w));
     //div比較像一棵 左兄右子的樹
                                                                                                   162
                                                       for(size t i=0;i<token.size();++i)table[i</pre>
     Column(Rule *r, const string &s):term(r),
                                                                                                   163
                                                                                                           amb=1:
                                                                                                                                                      17
                                                                                                                                                           de[u]+=w, de[v]+=w;
                                                            +1]=Column(token[i]):
                                                                                                   164
                                                                                                                                                      18
          value(s){}
                                                       table[0]=Column();
                                                                                                         if(s.completed())cache[s]=o;
                                                                                                                                                      19 T U; // 二分搜的最大值
     Column(){}
                                                 110
                                                                                                   165
57
                                                       table[0].add(State(GAMMA,0,0,0),0);
                                                 111
                                                                                                   166
     bool add(const State &st,int col){
58
                                                                                                                                                      20
                                                                                                                                                         void get_U(){
                                                       for(size t i=0;i<table.size();++i){</pre>
                                                                                                       inline node *build tree(const State &s){
                                                 112
                                                                                                                                                           U=0;
       if(div.find(st)==div.end()){
                                                                                                                                                      21
                                                 113
                                                         for(size t j=0;j<table[i].s.size();++j){ 168</pre>
                                                                                                         init cache();
                                                                                                                                                           for(int i=1;i<=n;++i)U+=2*pv[i];</pre>
         div[st];
                                                                                                                                                      22
                                                           State state=table[i].s[i]:
                                                                                                         node o:
                                                 114
         s.push back(st);
                                                                                                                                                           for(size t i=0;i<E.size();++i)U+=E[i].w;</pre>
                                                           if(state.completed())complete(i,state) 170
                                                                                                         build tree(s,&o);
62
         s.back().end=col;
                                                 115
                                                                                                         assert(o.child.size()==1):
         return true:
                                                                                                                                                         ISAP<T> isap;//網路流
                                                 116
                                                           else{
                                                                                                   172
                                                                                                         assert(o.child.back().size()==1);
       }else return false;
                                                                                                                                                         int s,t;//原匯點
                                                 117
                                                              Rule *term=state.next term();
                                                                                                   173
                                                                                                         return o.child.back().back();
                                                                                                                                                         void build(T L){
                                                              if(term->p.size())predict(i,term);
                                                 118
                                                                                                   174 }
                                                                                                                                                           isap.init(n+2);
                                                              else if(i+1<table.size())scan(i+1,</pre>
                                                                                                       void print_tree(node *o,int dep=0){
                                                 119
                                                                                                   175
   inline vector<Column> lexer(string text){
                                                                                                                                                           for(size_t i=0;i<E.size();++i){</pre>
                                                                                                         cout<<string(dep, ' '),o->s.print();
                                                                  state, term);
                                                                                                   176
     //tokenize,要自己寫,以下為範例
                                                                                                                                                             isap.add edge(E[i].u,E[i].v,E[i].w);
                                                                                                         for(auto div:o->child){
                                                 120
                                                                                                   177
     //他會把 input stream 變成 token stream
                                                                                                                                                      31
                                                 121
                                                                                                   178
                                                                                                           for(auto nd:div){
                                                                                                                                                           for(int v=1;v<=n;++v){</pre>
          就是(terminal.value)pair
                                                                                                                                                      32
                                                                                                             print tree(nd,dep+2);
                                                 122
                                                                                                   179
     vector<Column> token;
                                                                                                                                                             isap.add edge(s.v.U):
                                                 123
                                                       for(size t i=0:i<table.back().s.size():++i 180</pre>
     replace(text.begin(),text.end(),',',' ');
                                                                                                                                                      34
                                                                                                                                                             isap.add_edge(v,t,U+2*L-de[v]-2*pv[v]);
                                                                                                   181
                                                                                                                                                      35
72
     stringstream ss(text);
                                                         if(table.back().s[i].r==GAMMA&&table.
                                                                                                   182 }
                                                                                                                                                      36
73
     while(ss>>text){
                                                              back().s[i].completed()){
                                                                                                   183 / / 開始寫 code: 以下為加入語法的範例
                                                                                                                                                         int main(){
       if(text=="a"||text=="of")continue;
                                                                                                                                                      37
74
                                                            return make_pair(true, table.back().s[i 184
                                                                                                       inline Rule *get my Rule(){
                                                 125
                                                                                                                                                           while(~scanf("%d%d",&n,&m)){
       if(text=="list"){
                                                                                                         Rule *S=add_rule("S"),*E=add_rule("E"),*L=
                                                                                                                                                             if(!m){
         token.push_back(Column(NameRule["("],"
                                                 126
                                                                                                              add rule("L");
                                                                                                                                                               puts("1\n1");
              ("));
                                                                                                         Rule *list=add rule("("),*AND=add rule(
                                                 127
                                                                                                                                                               continue:
       }else if(text=="and"){
                                                       return make pair(false, State(0,-1));
                                                                                                              ),*T=add rule("T");
         token.push_back(Column(NameRule[")"],
                                                                                                                                                      42
                                                                                                         S->add({list,E});
                                                                                                                                                      43
                                                                                                                                                             init();
                                                 130 struct node{//語法樹的節點
                                                                                                         S->add({list,L}):
                                                                                                                                                      44
                                                                                                                                                             int u,v;
       }else token.push_back(Column(NameRule["]
                                                       State s:
                                                                                                         L->add({E,L});
                                                 131
                                                                                                                                                      45
                                                                                                                                                             for(int i=0;i<m;++i){</pre>
             "l,text));
                                                       vector<vector<node*> > child://vector<node 190</pre>
                                                                                                         L->add({E,AND,E});
                                                                                                                                                               scanf("%d%d",&u,&v);
                                                                                                                                                      46
                                                            *>.size()>1表示ambiquous
                                                                                                         E->add({T});
                                                                                                                                                      47
                                                                                                                                                               add edge(u,v,1);
     return token;
                                                                                                         E->add({S});
                                                 133
                                                       node(const State &s):s(s){}
                                                                                                         Rule *GAMMA=add_rule("GAMMA");//一定要有
                                                 134
                                                       node(){}
                                                                                                   193
                                                                                                                                                      49
                                                                                                                                                             get U();
    vector<Column> table;
                                                 135 };
                                                                                                              aamma rule當作是最上層的語法
                                                                                                                                                      50
                                                                                                                                                             s=n+1, t=n+2;
    inline void predict(int col,Rule *rul){
                                                 136 struct State end cmp{
                                                                                                         GAMMA->add({S});
                                                                                                                                                             T l=0,r=U,k=1.0/(n*n);
                                                                                                   194
     for(size t i=0;i<rul->p.size();++i){
                                                       bool operator()(const State &a,const State 195
                                                                                                         return GAMMA:
                                                                                                                                                             while(r-1>k){//二分搜最大值
       table[col].add(State(rul,i,0,col),col);
                                                             &b)const{
                                                                                                                                                               T mid=(1+r)/2;
87
     }
                                                         return a.end<b.end||(a.end==b.end&&a<b);</pre>
88
                                                                                                                                                               build(mid):
    inline void scan(int col,const State &s,Rule 139
                                                                                                                                                               T res=(U*n-isap.isap(s,t))/2;
                                                                                                                                                               if(res>0)l=mid;
                                                 141 | map<State, node*, State_end_cmp> cache;
     if(r!=table[col].term)return;
                                                                                                                                                               else r=mid;
                                                                                                            Linear Programming
                                                     vector<node*> node set:
     State ns(s.r,s.rid,s.dot id+1,s.start);
                                                     inline void init cache(){
     table[col].add(ns.col):
                                                                                                                                                             build(1):
                                                       for(auto d:node set)delete d;
93
     table[col].div[ns].insert(make pair(s,
                                                                                                                                                             isap.min cut(s,t);
                                                       cache.clear();
                                                                                                       7.1 最大密度子圖.cpp
                                                 145
          State(r,col)));
                                                                                                                                                             vector<int> ans;
                                                 146
                                                       node set.clear();
                                                                                                                                                             for(int i=1;i<=n;++i){</pre>
94
   inline void complete(int col,const State &s) 147 | }
                                                                                                                                                      63
                                                                                                                                                               if(isap.vis[i])ans.push back(i);
                                                          build tree(const State &s, node *pa,
                                                                                                     1 typedef double T;//POJ 3155
                                                                                                                                                      64
                                                          bool amb=0){
     for(size t i=0;i<table[s.start].s.size()</pre>
                                                                                                     const int MAXN=105;
                                                                                                                                                             printf("%d\n",ans.size());
                                                       if(cache.find(s)!=cache.end()){
          ;++i){
                                                                                                                                                             for(size_t i=0;i<ans.size();++i){</pre>
                                                                                                     3 struct edge{
                                                         pa->child.push back(vector<node*>(1.
       State &st=table[s.start].s[i];
                                                                                                                                                               printf("%d\n",ans[i]);
97
                                                                                                         int u,v;
                                                              cache[s]));
98
       Rule *term=st.next term():
                                                                                                         Tw;
                                                 151
                                                         return;
       if(!term||term->p.size()==0)continue;
99
                                                                                                         edge(int u=0,int v=0,T w=0):u(u),v(v),w(w)
                                                 152
100
       if(term==s.r){
                                                                                                                                                           return 0:
                                                       node *o;
                                                 153
101
         State nst(st.r,st.rid,st.dot_id+1,st.
                                                       if(s.completed()){
              start);
                                                                                                     8 vector<edge> E;
                                                         o=new node(s);
                                                 155
         table[col].add(nst,col);
102
                                                                                                     9 int n,m;// 1-base
                                                         if(amb)pa->child.back().push back(o);
                                                 156
         table[col].div[nst].insert(make_pair(
103
                                                                                                    10 | T de [MAXN], pv [MAXN]; // 每 個 點 的 邊 權 和 和 點 權 (
                                                         else pa->child.push back(vector<node</pre>
              st,s));
                                                                                                            有些題目會給)
                                                              *>(1,o));
104
                                                                                                    11 void init(){
```

57

58

60

61

65

67

68

72

74

75

76

78

79

80

82

83

84

85

91

99

100

101 102

105

107

110

T Euler(T n){

for(T i=2;i*i<=n;++i){</pre>

Number Theory

basic.cpp

```
1 template<typename T>
   void gcd(const T &a,const T &b,T &d,T &x,T &
     if(!b) d=a,x=1,y=0;
    else gcd(b,a%b,d,y,x), y-=x*(a/b);
   long long int phi[N+1];
   void phiTable(){
    for(int i=1;i<=N;i++)phi[i]=i;</pre>
    for(int i=1;i<=N;i++)for(x=i*2;x<=N;x+=i)</pre>
          phi[x]-=phi[i];
10
   void all divdown(const LL &n) {// all n/x
    for(LL a=1;a<=n;a=n/(n/(a+1))){</pre>
13
       // dosomethina:
14
15
16 const int MAXPRIME = 1000000:
  int iscom[MAXPRIME], prime[MAXPRIME],
       primecnt:
  int phi[MAXPRIME], mu[MAXPRIME];
   void sieve(void){
    memset(iscom,0,sizeof(iscom));
    primecnt = 0;
22
    phi[1] = mu[1] = 1;
     for(int i=2;i<MAXPRIME;++i) {</pre>
23
24
       if(!iscom[i]) {
25
         prime[primecnt++] = i;
26
         mu[i] = -1;
27
         phi[i] = i-1;
28
       for(int j=0;j<primecnt;++j) {</pre>
29
30
         int k = i * prime[j];
         if(k>=MAXPRIME) break;
         iscom[k] = prime[j];
32
33
         if(i%prime[j]==0) {
           mu[k] = 0;
           phi[k] = phi[i] * prime[j];
           break;
36
         } else {
           mu[k] = -mu[i];
           phi[k] = phi[i] * (prime[j]-1);
42
   bool g_test(const LL &g, const LL &p, const
       vector<LL> &v) {
     for(int i=0;i<v.size();++i)</pre>
       if(modexp(g,(p-1)/v[i],p)==1)
         return false:
49
    return true;
50
   LL primitive root(const LL &p) {
    if(p==2) return 1;
    vector<LL> v;
    Factor(p-1,v);
```

```
if(n%i==0){
     v.erase(unique(v.begin(), v.end()), v.end 115
                                                            ans=ans/i*(i-1);
           ());
                                                 116
      for(LL g=2;g<p;++g)</pre>
                                                            while(n%i==0)n/=i;
                                                 117
       if(g test(g,p,v))
                                                 118
                                                 119
      puts("primitive root NOT FOUND");
                                                       if(n>1)ans=ans/n*(n-1);
                                                 120
                                                  121
                                                       return ans:
                                                 122
    int Legendre(const LL &a, const LL &p) {
                                                 123
        return modexp(a%p,(p-1)/2,p); }
                                                      //Chinese remainder theorem
                                                     template<typename T>
64 LL inv(const LL &a, const LL &n) {
                                                     T pow mod(T n,T k,T m){
     LL d,x,v;
                                                  127
      gcd(a,n,d,x,y);
                                                  128
                                                       for(n=(n)=m?n\%m:n):k:k>>=1){
     return d==1 ? (x+n)%n : -1:
                                                  129
                                                         if(k&1)ans=ans*n%m;
                                                 130
                                                         n=n*n%m;
                                                  131
70 LL log_mod(const LL &a, const LL &b, const
                                                 132
                                                       return ans;
        LL &p) {
                                                  133
     // a ^ x = b \pmod{p}
                                                     template<typename T>
     int m=sqrt(p+.5), e=1;
                                                      T crt(vector<T> &m, vector<T> &a){
     LL v=inv(modexp(a,m,p), p);
                                                       T M=1,tM,ans=0;
      map<LL.int> x:
                                                 137
                                                       for(int i=0;i<(int)m.size();++i)M*=m[i];</pre>
     x[1]=0;
                                                 138
                                                       for(int i=0;i<(int)a.size();++i){</pre>
                                                         tM=M/m[i];
      for(int i=1;i<m;++i) {</pre>
                                                 139
       e = LLmul(e,a,p);
                                                         ans=(ans+(a[i]*tM%M)*pow_mod(tM,Euler(m[
                                                 140
       if(!x.count(e)) x[e] = i;
                                                              i])-1,m[i])%M)%M;
                                                         /*如果m[i]是質數, Euler(m[i])-1=m[i]-2。
      for(int i=0;i<m;++i) {</pre>
                                                               就不用算Euler了*/
       if(x.count(b)) return i*m + x[b];
                                                  142
       b = LLmul(b,v,p);
                                                       return ans;
                                                 143
                                                 144 }
     return -1;
    LL Tonelli Shanks(const LL &n, const LL &p)
                                                            bit set.cpp
      //x^2 = n \pmod{p}
     if(n==0) return 0:
                                                   1 void sub set(int S){
     if(Legendre(n,p)!=1) while(1) { puts("SQRT
                                                       int sub=S:
            ROOT does not exist"); }
                                                       do{
     int S = 0:
                                                         //對某集合的子集合的處理
     LL 0 = p-1;
                                                         sub=(sub-1)&S;
      while( !(Q&1) ) { Q>>=1; ++S; }
                                                       }while(sub!=S);
     if(S==1) return modexp(n%p,(p+1)/4,p);
     LL z = 2;
                                                     void k_sub_set(int k,int n){
      for(;Legendre(z,p)!=-1;++z)
                                                       int comb=(1<<k)-1,S=1<<n;</pre>
     LL c = modexp(z,Q,p);
                                                       while(comb<S){</pre>
     LL R = modexp(n\%p,(Q+1)/2,p), t = modexp(n
                                                         //對大小為k的子集合的處理
          %p,Q,p);
                                                         int x=comb&-comb, y=comb+x;
                                                  12
      int M = S;
                                                  13
                                                         comb = ((comb\&\sim y)/x>>1)|y;
      while(1) {
                                                  14
       if(t==1) return R;
       LL b = modexp(c,1L << (M-i-1),p);
       R = LLmul(R,b,p);
       t = LLmul( LLmul(b,b,p), t, p);
       c = LLmul(b,b,p);
                                                            cantor expansion.cpp
       M = i:
      return -1:
                                                   1 int factorial[MAXN];
109 }
                                                   void init(){
    template<typename T>
                                                       factorial[0]=1;
```

for(int i=1;i<=MAXN;++i)factorial[i]=</pre>

factorial[i-1]*i;

```
6 int encode(const vector<int> &s){
     int n=s.size(),res=0;
     for(int i=0;i<n;++i){</pre>
       int t=0:
       for(int j=i+1;j<n;++j)</pre>
         if(s[j]<s[i])++t;
12
       res+=t*factorial[n-i-1]:
13
14
     return res;
15
16
   vector<int> decode(int a,int n){
     vector<int> res:
     vector<bool> vis(n,0);
     for(int i=n-1:i>=0:--i){
       int t=a/factorial[i],j;
21
       for(j=0;j<n;++j)</pre>
         if(!vis[j]){
23
           if(t==0)break;
24
           --t;
25
26
       res.push_back(j);
       vis[j]=1;
28
       a%=factorial[i];
29
     return res;
```

8.4 FFT.cpp

```
1 | template < typename T, typename VT = std::vector <
        std::complex<T> > >
   struct FFT{
     const T pi;
     FFT(const T pi=acos((T)-1)):pi(pi){}
     unsigned int bit_reverse(unsigned int a,
          int len){
       a = ((a\&0x55555555U) << 1) | ((a\&0xAAAAAAAAU))
            >>1);
       a=((a&0x33333333U)<<2)|((a&0xCCCCCCCU)
       a = ((a\&0x0F0F0F0FU) < <4) | ((a\&0xF0F0F0F0U)
       a=((a&0x00FF00FFU)<<8)|((a&0xFF00FF00U)
       a=((a&0x0000FFFFU)<<16)|((a&0xFFFF0000U)
            >>16);
11
       return a>>(32-len);
12
13
     void fft(bool is inv,VT &in,VT &out,int N)
14
       int bitlen=std::__lg(N),num=is_inv?-1:1;
15
       for(int i=0;i<N;++i)out[bit reverse(i,</pre>
            bitlen)]=in[i];
       for(int step=2;step<=N;step<<=1){</pre>
         const int mh=step>>1;
         for(int i=0;i<mh;++i){</pre>
19
           std::complex<T> wi=exp(std::complex<</pre>
                T>(0,i*num*pi/mh));
20
           for(int j=i;j<N;j+=step){</pre>
21
             int k=j+mh;
22
              std::complex<T> u=out[j],t=wi*out[
                   k];
              out[j]=u+t;
```

return 0;

46

```
45 | int main () {
                                                                                                           using mt = std::vector<rt>;
             out[k]=u-t;
                                                                                                                                                                T det=sign?-1:1;
                                                        vector<double>ve;
                                                                                                           using matrix = Matrix<T>;
                                                                                                                                                                for(int i=0;i<r;++i){</pre>
25
                                                        vector<double>ans = cal(ve, n);
                                                                                                           int r,c;
                                                                                                                                                         71
                                                                                                                                                                  det = det*m[i][i];
26
27
                                                        // 視情況把答案 +eps, 避免 -0
                                                                                                           mt m:
                                                                                                                                                                  det = det/lazy[i];
       if(is inv)for(int i=0;i<N;++i)out[i]/=N; 49|}
                                                                                                           Matrix(int r, int c):r(r),c(c),m(r,rt(c))
                                                                                                                                                                  for(auto &j:m[i])j/=lazy[i];
                                                                                                                                                         73
                                                                                                           rt& operator[](int i){return m[i];}
29
                                                                                                                                                         74
30 };
                                                                                                           matrix operator+(const matrix &a){
                                                                                                                                                         75
                                                                                                                                                                return det:
                                                                                                             matrix rev(r,c);
                                                                                                      11
                                                                                                                                                         76
                                                                                                                                                         77 };
                                                      8.6 LinearCongruence.cpp
                                                                                                             for(int i=0;i<r;++i)</pre>
                                                                                                               for(int j=0;j<c;++j)</pre>
         find real root.cpp
                                                                                                      14
                                                                                                                 rev[i][j]=m[i][j]+a.m[i][j];
                                                                                                             return rev:
                                                                                                      15
                                                    1 | pair<LL,LL> LinearCongruence(LL a[],LL b[],
                                                                                                                                                            8.9 MillerRobin.cpp
                                                                                                      16
                                                           LL m[], int n) {
1 / / an*x^n + ... + a1x + a0 = 0:
                                                                                                      17
                                                                                                           matrix operator-(const matrix &a){
                                                        // a[i]*x = b[i] (mod m[i])
                                                                                                             matrix rev(r,c);
  int sign(double x){
                                                                                                      18
                                                        for(int i=0;i<n;++i) {</pre>
    return x \leftarrow -eps ? -1 : x > eps;
                                                                                                      19
                                                                                                             for(int i=0;i<r;++i)</pre>
                                                                                                                                                          1 LL LLmul(LL a, LL b, const LL &mod) {
                                                          LL x, y, d = extgcd(a[i],m[i],x,y);
                                                                                                               for(int j=0;j<c;++j)</pre>
                                                                                                                                                              LL ans=0:
                                                                                                      20
                                                          if(b[i]%d!=0) return make_pair(-1LL,0LL)
                                                                                                                 rev[i][j]=m[i][j]-a.m[i][j];
                                                                                                                                                              while(b) {
                                                                                                      21
   double get(const vector<double>&coef, double
                                                                                                      22
                                                                                                             return rev;
                                                                                                                                                                if(b&1) {
                                                                                                      23
                                                                                                                                                                  ans+=a:
                                                          b[i] = LLmul(b[i]/d,x,m[i]);
     double e = 1, s = 0;
                                                                                                      24
                                                                                                           matrix operator*(const matrix &a){
                                                                                                                                                                  if(ans>=mod) ans-=mod;
    for(auto i : coef) s += i*e, e *= x;
                                                                                                             matrix rev(r.a.c):
                                                        LL lastb = b[0], lastm = m[0];
    return s:
                                                                                                             matrix tmp(a.c.a.r):
                                                                                                                                                                a<<=1. b>>=1:
                                                        for(int i=1;i<n;++i) {</pre>
10
                                                                                                      27
                                                                                                             for(int i=0;i<a.r;++i)</pre>
                                                                                                                                                                if(a>=mod) a-=mod;
                                                          LL x, y, d = extgcd(m[i], lastm, x, y);
11
                                                                                                      28
                                                                                                               for(int j=0;j<a.c;++j)</pre>
                                                                                                                                                         10
                                                          if((lastb-b[i])%d!=0) return make pair
   double find(const vector<double>&coef, int n
                                                                                                      29
                                                                                                                 tmp[j][i]=a.m[i][j];
                                                                                                                                                         11
                                                                                                                                                              return ans;
                                                               (-1LL,0LL);
       , double lo, double hi){
                                                                                                             for(int i=0;i<r;++i)</pre>
                                                                                                                                                         12
                                                          lastb = LLmul((lastb-b[i])/d,x,(lastm/d)
                                                                                                                                                            long long mod mul(long long a, long long b,
    double sign_lo, sign_hi;
                                                                                                               for(int j=0;j<a.c;++j)</pre>
                                                               )*m[i];
    if( !(sign_lo = sign(get(coef,lo))) )
                                                                                                                 for(int k=0;k<c;++k)</pre>
                                                                                                                                                                 long long m){
14
                                                                                                      32
                                                          lastm = (lastm/d)*m[i];
                                                   14
          return lo;
                                                                                                      33
                                                                                                                   rev.m[i][j]+=m[i][k]*tmp[j][k];
                                                                                                                                                              a\%=m,b\%=m;
                                                          lastb = (lastb+b[i])%lastm;
                                                   15
    if( !(sign hi = sign(get(coef,hi))) )
                                                                                                      34
                                                                                                             return rev:
                                                                                                                                                              long long y=(long long)((double)a*b/m+0.5)
                                                   16
          return hi;
                                                                                                                                                                   :/* fast for m < 2^58 */
                                                   17
                                                        return make pair(lastb<0?lastb+lastm:lastb
    if(sign lo * sign hi > 0) return INF;
                                                                                                           bool inverse(){
                                                                                                                                                              long long r=(a*b-y*m)%m;
                                                             ,lastm);
     for(int stp = 0; stp < 100 && hi - lo >
                                                                                                             Matrix t(r,r+c);
                                                                                                                                                              return r<0?r+m:r;</pre>
          eps; ++stp){
                                                                                                             for(int y=0;y<r;y++){</pre>
                                                                                                                                                         18
       double m = (lo+hi)/2.0;
                                                                                                      39
                                                                                                               t.m[y][c+y] = 1;
                                                                                                                                                            template<typename T>
       int sign_mid = sign(get(coef,m));
                                                                                                      40
                                                                                                               for(int x=0;x<c;++x)</pre>
                                                                                                                                                         20
                                                                                                                                                            T pow(T a,T b,T mod){//a^b\%mod}
19
       if(!sign_mid) return m;
                                                                                                      41
                                                                                                                 t.m[y][x]=m[y][x];
                                                                                                                                                         21
                                                                                                                                                              T ans=1;
                                                            Lucas.cpp
       if(sign lo*sign mid < 0) hi = m;</pre>
                                                                                                      42
                                                                                                                                                              for(;b;a=mod mul(a,a,mod),b>>=1)
       else lo = m;
                                                                                                      43
                                                                                                             if(!t.gas())
                                                                                                                                                                if(b&1)ans=mod_mul(ans,a,mod);
22
                                                                                                               return false;
23
                                                                                                      44
                                                                                                                                                              return ans;
                                                    1 int mod fact(int n,int &e){
    return (lo+hi)/2.0;
                                                                                                             for(int y=0;y<r;y++)</pre>
                                                                                                                                                         25
24
                                                       e=0;
                                                                                                               for(int x=0;x<c;++x)</pre>
                                                                                                                                                            int sprp[3]={2,7,61};//int%d3@i,@
25
                                                        if(n==0)return 1;
                                                                                                                                                            int llsprp
                                                                                                      47
                                                                                                                 m[y][x]=t.m[y][c+x]/t.m[y][y];
26
                                                        int res=mod fact(n/P,e);
   vector<double> cal(vector<double>coef, int n
                                                                                                                                                                 [7] = \{2,325,9375,28178,450775,9780504,17952656\}
                                                                                                      48
                                                                                                             return true;
                                                                                                      49
                                                                                                                                                                 //¦@@unsigned Long Long%d3@
                                                        if((n/P)%2==0)return res*fact[n%P]%P;
     vector<double>res;
                                                                                                      50
                                                                                                           T gas(){
                                                                                                                                                            template<typename T>
                                                        return res*(P-fact[n%P])%P;
    if(n == 1){
                                                                                                             vector<T> lazy(r,1);
                                                                                                                                                            bool isprime(T n,int *sprp,int num){
29
       if(sign(coef[1])) res.pb(-coef[0]/coef
                                                                                                             bool sign=false;
                                                                                                                                                              if(n==2)return 1;
                                                                                                      52
                                                      int Cmod(int n,int m){
                                                                                                             for(int i=0;i<r;++i){</pre>
                                                                                                                                                              if(n<2||n%2==0)return 0;
            [1]);
                                                       int a1,a2,a3,e1,e2,e3;
                                                                                                               if( m[i][i]==0 ){
                                                                                                                                                              int t=0;
       return res;
                                                        a1=mod fact(n,e1);
32
                                                                                                      55
                                                                                                                 int j=i+1;
                                                                                                                                                              T u=n-1;
                                                        a2=mod fact(m,e2);
     vector<double>dcoef(n);
                                                                                                      56
                                                                                                                 while(j<r&&!m[j][i])j++;
                                                                                                                                                              for(;u%2==0;++t)u>>=1;
                                                        a3=mod fact(n-m,e3);
    for(int i = 0; i < n; ++i) dcoef[i] = coef</pre>
                                                                                                      57
                                                                                                                 if(j==r)continue;
                                                                                                                                                              for(int i=0;i<num;++i){</pre>
                                                        if(e1>e2+e3)return 0;
          [i+1]*(i+1);
                                                                                                      58
                                                                                                                 m[i].swap(m[j]);
                                                                                                                                                                T a=sprp[i]%n;
                                                        return a1*inv(a2*a3%P,P)%P;
     vector<double>droot = cal(dcoef, n-1);
                                                                                                                 sign=!sign;
                                                                                                                                                                if(a==0||a==1||a==n-1)continue;
                                                                                                      59
                                                                                                                                                                T x=pow(a,u,n);
    droot.insert(droot.begin(), -INF);
                                                                                                      60
    droot.pb(INF);
                                                                                                                                                                if(x==1||x==n-1)continue;
                                                                                                               for(int j=0;j<r;++j){</pre>
                                                                                                                                                                for(int j=0;j<t;++j){</pre>
    for(int i = 0; i+1 < droot.size(); ++i){</pre>
                                                                                                                 if(i==j)continue;
       double tmp = find(coef, n, droot[i],
                                                                                                      63
                                                                                                                 lazy[j]=lazy[j]*m[i][i];
                                                                                                                                                                  x=mod mul(x,x,n);
                                                      8.8 Matrix.cpp
            droot[i+1]);
                                                                                                                 T mx=m[j][i];
                                                                                                                                                                  if(x==1)return 0;
       if(tmp < INF) res.pb(tmp);</pre>
                                                                                                                 for(int k=0;k<c;++k)</pre>
                                                                                                                                                                  if(x==n-1)break;
    }
                                                                                                                   m[j][k]=m[j][k]*m[i][i]-m[i][k]*mx
41
                                                                                                                                                                if(x==n-1)continue;
42
    return res;
                                                   1 template<typename T>
```

67

2 struct Matrix{

using rt = std::vector<T>;

```
8.10 NTT.cpp
```

1 2615053605667*(2^18)+1,3

return 1;

15*(2^27)+1,31

3 479*(2^21)+1.3

12

13

14

15

16

17

21

28

30

4 7*17*(2^23)+1,3

8.11 外星模運算.cpp

 $1 / a[0]^{(a[1]^a[2]^{...})}$

for(int i=0;i<N;++i)out[i]=out[i]*invn 51</pre>

```
2 #include <bits/stdc++.h>
5 3*3*211*(2^19)+1.5
                                                     3 using namespace std;
6 25*(2^22)+1.3
                                                     4 #define maxn 1000000
   template<typename T,typename VT=std::vector<</pre>
                                                      int euler[maxn+5];
       T> >
                                                     6 bool is prime[maxn+5];
   struct NTT{
                                                      inline void init euler(){
    const T P.G:
                                                         is prime[1]=1;//一不是質數
    NTT(T p=(1<<23)*7*17+1,T g=3):P(p),G(g){}
                                                         for(int i=1;i<=maxn;i++)euler[i]=i;</pre>
    unsigned int bit_reverse(unsigned int a,
11
                                                         for(int i=2;i<=maxn;i++){</pre>
          int len){
       a = ((a\&0x55555555U) << 1) | ((a\&0xAAAAAAAAU))
                                                   11
                                                           if(!is prime[i]){//是質數
                                                             euler[i]--;
                                                    12
                                                             for(int j=i<<1;j<=maxn;j+=i){</pre>
       a=((a&0x33333333U)<<2)|((a&0xCCCCCCCU))
                                                   13
                                                               is_prime[j]=1;
                                                    14
       a=((a\&0x0F0F0F0FU)<<4)|((a\&0xF0F0F0F0U)
                                                    15
                                                               euler[j]=euler[j]/i*(i-1);
            >>4);
                                                    16
       a=((a&0x00FF00FFU)<<8)|((a&0xFF00FF00U)
                                                   17
                                                    18
       a=((a\&0x0000FFFFU)<<16)|((a\&0xFFFF0000U)
                                                   19 }
                                                   20 inline long long pow(long long a,long long b
            >>16);
       return a>>(32-len);
                                                            ,long long mod){//a^b%mod
                                                         long long ans=1;
18
                                                         for(;b;a=a*a%mod,b>>=1)
19
       pow_mod(T n,T k,T m){
       T ans=1;
                                                   23
                                                          if(b&1)ans=ans*a%mod;
20
       for(n=(n)=m?n\%m:n);k;k>>=1){
                                                   24
                                                        return ans;
22
         if(k&1)ans=ans*n%m;
                                                    25
23
         n=n*n%m:
                                                       bool isless(long long *a,int n,int k){
                                                        if(*a==1)return k>1;
24
                                                        if(--n==0)return *a<k;</pre>
25
       return ans;
26
                                                    29
                                                         int next=0:
     void ntt(bool is inv,VT &in,VT &out,int N)
                                                         for(long long b=1;b<k;++next)</pre>
27
                                                   30
                                                   31
       int bitlen=std::__lg(N);
                                                   32
                                                        return isless(a+1,n,next);
29
       for(int i=0;i<N;++i)out[bit_reverse(i,</pre>
                                                   33 }
            bitlen)]=in[i];
                                                    34 long long high_pow(long long *a,int n,long
       for(int step=2,id=1;step<=N;step<<=1,++</pre>
                                                            long mod){
                                                         if(*a==1||--n==0)return *a%mod;
            id){
         T wn=pow mod(G,(P-1)>>id,P),wi=1,u,t;
                                                         int k=0,r=euler[mod];
                                                         for(long long tma=1; tma!=pow(*a,k+r,mod)
         const int mh=step>>1;
32
33
         for(int i=0;i<mh;++i){</pre>
                                                              ;++k)
           for(int j=i;j<N;j+=step){</pre>
                                                           tma=tma*(*a)%mod;
35
             u=out[j],t=wi*out[j+mh]%P;
                                                         if(isless(a+1,n,k))return pow(*a,high_pow(
36
             out[j]=u+t;
                                                              a+1,n,k),mod);
             out[j+mh]=u-t;
                                                         int tmd=high_pow(a+1,n,r);
             if(out[i]>=P)out[i]-=P;
                                                         int t=(tmd-k+r)%r;
             if(out[j+mh]<0)out[j+mh]+=P;</pre>
                                                         return pow(*a,k+t,mod);
                                                    43 | }
           wi=wi*wn%P:
                                                       long long a[1000005];
42
                                                       int t, mod;
43
                                                       int main(){
                                                         init euler();
         for(int i=1;i<N/2;++i)std::swap(out[i</pre>
                                                         scanf("%d",&t);
              ],out[N-i]);
                                                         #define n 4
                                                    49
         T invn=pow mod(N,P-2,P);
                                                         while(t--){
```

48

49 }

50 };

8.12 模運算模板.cpp

scanf("%d",&mod);

return 0;

printf("%lld\n",high_pow(a,n,mod));

52

53

54

55

```
1 template<typename T,long long mod>
 2 struct mod_t{//mod只能是質數
    T data;
     mod t(){}
     mod_t(const T &d):data((d%mod+mod)%mod){}
     mod t pow(T b)const{
       mod t ans(1);
       for(mod t now=*this;b;now=now*now,b/=2)
         if(b%2)ans=ans*now;
10
       return ans;
11
12
     mod t operator-(int)const{
13
       return mod t(mod-data);
14
     mod t operator+(const mod t &b)const{
       return mod t((data+b.data)%mod);
16
17
     mod t operator-(const mod t &b)const{
18
19
       return mod t((data-b.data+mod)%mod);
20
     mod t operator*(const mod t &b)const{
21
       return mod t((data*b.data)%mod);
22
23
24
     mod t operator/(const mod t &b)const{
       return *this*b.pow(mod-2);//*this *
            Inverse(b)
26
27
     operator T()const{return data;}
     friend istream &operator>>(istream &i,
          mod_t &b){
29
       T d:
       i>>d;
30
       b=mod_t(d);
31
32
       return i;
33
34 };
```

質因數分解.cpp

```
1 LL func(const LL n, const LL mod, const int c)
   return (LLmul(n,n,mod)+c+mod)%mod;
5 LL pollorrho(const LL n, const int c) {//循
      環節長度
   LL a=1, b=1;
   a=func(a,n,c)%n;
   b=func(b,n,c)%n; b=func(b,n,c)%n;
   while(gcd(abs(a-b),n)==1) {
```

```
for(int i=0;i<n;++i)scanf("%lld",&a[i]); 10</pre>
                                             11
                                                    b=func(b,n,c)%n; b=func(b,n,c)%n;
                                             12
                                             13
                                                  return gcd(abs(a-b),n);
                                             14
                                             15
                                                void prefactor(LL &n, vector<LL> &v) {
                                                  for(int i=0;i<12;++i) {</pre>
                                             17
                                                    while(n%prime[i]==0) {
                                                      v.push back(prime[i]);
                                             19
                                                      n/=prime[i];
                                             20
                                             21
                                             22
                                             23
                                             24
                                             25
                                                void smallfactor(LL n, vector<LL> &v) {
                                                  if(n<MAXPRIME) {</pre>
                                             26
                                                    while(isp[(int)n]) {
                                             28
                                                      v.push_back(isp[(int)n]);
                                             29
                                                      n/=isp[(int)n];
                                             30
                                             31
                                                    v.push back(n);
                                             32
                                                  } else {
                                             33
                                                    for(int i=0;i<primecnt&&prime[i]*prime[i</pre>
                                                         ]<=n;++i) {</pre>
                                                      while(n%prime[i]==0) {
                                             34
                                                        v.push_back(prime[i]);
                                             35
                                             36
                                                        n/=prime[i];
                                             37
                                             38
                                             39
                                                    if(n!=1) v.push back(n);
                                             40
                                             41
                                             42
                                             43
                                                void comfactor(const LL &n, vector<LL> &v) {
                                             44
                                                  if(n<1e9) {
                                                    smallfactor(n,v);
                                             45
                                             46
                                                    return;
                                             47
                                             48
                                                  if(Isprime(n)) {
                                             49
                                                    v.push back(n);
                                             50
                                                    return;
                                             51
                                             52
                                                  LL d:
                                             53
                                                  for(int c=3;;++c) {
                                                    d = pollorrho(n,c);
                                             55
                                                    if(d!=n) break;
                                             56
                                                  comfactor(d,v);
                                                  comfactor(n/d,v);
                                             59
                                                void Factor(const LL &x, vector<LL> &v) {
                                                  LL n = x;
                                                  if(n==1) { puts("Factor 1"); return; }
                                                  prefactor(n,v);
                                                  if(n==1) return;
                                                  comfactor(n,v);
                                                  sort(v.begin(),v.end());
                                                void AllFactor(const LL &n, vector<LL> &v) {
                                                  vector<LL> tmp;
                                                  Factor(n,tmp);
                                                  v.clear();
                                                  v.push back(1);
```

id=S[pa].fail;

```
int len:
                                                             while(~id&&!S[id].next[i])id=S[id
                                                                                                          for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[ 12| inline int kmp match(char *A,int lenA,char *
                                                44
                                                                                                                                                       B, int lenB, int *fail){
    LL now=1;
                                                                 l.fail;
                                                                                                               t].efl){
    for(int i=0;i<tmp.size();++i) {</pre>
                                                             S[t].fail=~id?S[id].next[i]:0;
                                                                                                            S[t].vis=vt;
                                                                                                                                                     int id=-1,ans=0;
                                                45
      if(i==0 | | tmp[i]!=tmp[i-1]) {
                                                             S[t].efl=S[S[t].fail].ed?S[t].fail 100
                                                                                                                                                     for(int i=0;i<lenA;++i){</pre>
                                                46
                                                                                                            ans+=S[t].ed;/*因為都走efl邊所以保
        len = v.size();
                                                                 :S[S[t].fail].efl;
                                                                                                                                                      while(~id&&B[id+1]!=A[i])id=fail[id];
                                                                                                                 證匹配成功*/
80
        now = 1;
                                                47
                                                             q.push back(t);
                                                                                                                                                      if(B[id+1]==A[i])++id;
                                                                                               101
81
                                                48
                                                             ++qe;
                                                                                                                                                      if(id==lenB-1){/*匹配成功*/
                                                                                                                                                17
                                                                                               102
82
      now*=tmp[i];
                                                49
                                                                                                                                                        ++ans;
                                                                                                                                                18
                                                                                               103
                                                                                                         return ans;
      for(int j=0; j<len; ++ j)</pre>
83
                                                50
                                                                                                                                                        id=fail[id];
                                                                                                                                                19
                                                                                               104
84
        v.push_back(v[j]*now);
                                                51
                                                                                                      /*把AC自動機變成真的自動機*/
                                                                                                                                                20
                                                                                               105
85
                                                      /*DP出每個前綴在字串s出現的次數並傳回所
                                                52
                                                                                                                                                21
                                                                                                      void evolution(){
                                                                                               106
                                                           有字串被s匹配成功的次數O(N+M)*/
                                                                                                                                                22
                                                                                                                                                    return ans;
                                                                                               107
                                                                                                        for(qs=1;qs!=qe;){
                                                53
                                                      int match 0(const char *s){
                                                                                                          int p=q[qs++];
                                                                                               108
                                                        int ans=0,id,p=0,i;
                                                54
                                                                                                          for(int i=0;i<=R-L;++i)</pre>
                                                                                               109
                                                55
                                                        for(i=0;s[i];++i){
                                                                                               110
                                                                                                            if(S[p].next[i]==0)S[p].next[i]=S[
                                                56
       String
                                                          id=s[i]-L;
                                                                                                                 S[p].fail].next[i];
                                                57
                                                           while(!S[p].next[id]&&p)p=S[p].fail; 111
                                                                                                                                                  9.4 manacher.cpp
                                                58
                                                          if(!S[p].next[id])continue;
                                                                                               112
                                                59
                                                           p=S[p].next[id];
                                                                                               113 };
  9.1 AC 自動機.cpp
                                                          ++S[p].cnt_dp;/*匹配成功則它所有後綴
                                                60
                                                                                                                                                 1 //原字串: asdsasdsa
                                                               都可以被匹配(DP計算)*/
                                                                                                                                                2 // 先把字串變成這樣: @a#s#d#s#a#s#d#s#a#
                                                61
                                                                                                                                                 3 inline void manacher(char *s.int len.int *z)
1 template < char L='a', char R='z'>
                                                                                                        hash.cpp
                                                         for(i=qe-1;i>=0;--i){
                                                62
2 class ac automaton{
                                                63
                                                          ans+=S[q[i]].cnt dp*S[q[i]].ed;
                                                                                                                                                     int 1=0, r=0;
    private:
                                                           if(~S[q[i]].fail)S[S[q[i]].fail].
                                                64
                                                                                                                                                     for(int i=1;i<len;++i){</pre>
      struct ioe{
                                                                                                 1 | #define MAXN 1000000
                                                               cnt_dp+=S[q[i]].cnt_dp;
                                                                                                                                                      z[i]=r>i?min(z[2*l-i],r-i):1;
        int next[R-L+1],fail,efl,ed,cnt_dp,vis
                                                                                                 2 #define prime mod 1073676287
                                                                                                                                                      while(s[i+z[i]]==s[i-z[i]])++z[i];
                                                                                                 3 /*prime mod 必須要是質數*/
                                                        return ans;
                                                                                                                                                      if(z[i]+i>r)r=z[i]+i,l=i;
        joe():ed(0),cnt_dp(0),vis(0){
                                                                                                 4 typedef long long T;
                                                67
          for(int i=0;i<=R-L;++i)next[i]=0;</pre>
                                                                                                 5 char s[MAXN+5];
                                                68
                                                      /*多串匹配走efL邊並傳回所有字串被s匹配成
                                                                                                 6 T h[MAXN+5];/*hash陣列*/
      };
                                                           7 T h base[MAXN+5];/*h_base[n]=(prime^n)%
10
    public:
                                                69
                                                      int match 1(const char *s)const{
                                                                                                       prime mod*/
                                                        int ans=0,id,p=0,t;
                                                70
      std::vector<joe> S;
                                                                                                  inline void hash init(int len,T prime=0
                                                        for(int i=0;s[i];++i){
                                                                                                                                                  9.5 minimal string rotation.cpp
12
      std::vector<int> q;
                                                71
                                                                                                       xdefaced){
                                                           id=s[i]-L:
                                                72
13
      int qs,qe,vt;
                                                                                                    h base[0]=1:
                                                           while(!S[p].next[id]&&p)p=S[p].fail;
      ac_automaton():S(1),qs(0),qe(0),vt(0){}
14
                                                                                                    for(int i=1;i<=len;++i){</pre>
                                                74
                                                           if(!S[p].next[id])continue;
15
      void clear(){
                                                                                                                                                 int min string rotation(const string &s){
                                                                                                      h[i]=(h[i-1]*prime+s[i-1])%prime mod;
                                                           p=S[p].next[id];
16
        a.clear();
                                                75
                                                                                                                                                     int n=s.size(),i=0,j=1,k=0;
                                                                                                      h_base[i]=(h_base[i-1]*prime)%prime_mod;
                                                                                                12
        S.resize(1);
                                                76
                                                           if(S[p].ed)ans+=S[p].ed;
17
                                                                                                                                                     while(i<n&&j<n&&k<n){</pre>
                                                                                                13
        for(int i=0;i<=R-L;++i)S[0].next[i]=0;</pre>
                                                          for(t=S[p].efl;~t;t=S[t].efl){
18
                                                                                                                                                      int t=s[(i+k)%n]-s[(j+k)%n];
                                                                                                14 }
        S[0].cnt dp=S[0].vis=qs=qe=vt=0;
                                                            ans+=S[t].ed;/*因為都走efL邊所以保
19
                                                                                                inline T get_hash(int l,int r){/*閉區間寫
20
                                                                 證匹配成功*/
                                                                                                                                                      if(t){
                                                                                                        法, 設編號為0 ~ Len-1*/
      void insert(const char *s){
21
                                                                                                                                                        if(t>0)i+=k;
                                                                                                    return (h[r+1]-(h[1]*h base[r-1+1])%
        int o=0;
22
                                                80
                                                                                                                                                        else j+=k;
         for(int i=0,id;s[i];++i){
                                                                                                         prime mod+prime mod)%prime mod;
23
                                                81
                                                        return ans;
                                                                                                                                                        if(i==j)++j;
24
          id=s[i]-L;
                                                82
                                                                                                                                                10
                                                                                                                                                        k=0;
25
          if(!S[o].next[id]){
                                                83
                                                      /*枚舉(s的子字串nA)的所有相異字串各恰一
                                                                                                                                                11
            S.push_back(joe());
                                                                                                                                                12
                                                           次並傳回次數O(N*M^(1/3))*/
27
            S[o].next[id]=S.size()-1;
                                                                                                                                                    return min(i,j);//傳回最小循環表示法起始位
                                                                                                                                                13
                                                       int match_2(const char *s){
                                                                                                  9.3 KMP.cpp
                                                        int ans=0,id,p=0,t;
                                                85
29
          o=S[o].next[id];
                                                86
                                                                                                                                                14 }
30
                                                        /*把戳記vt+=1,只要vt沒溢位,所有S[p].
                                                87
                                                                                                 1 /*產生fail function*/
        ++S[o].ed;
                                                             vis==vt 就 會 變 成 false
                                                                                                 2 inline void kmp fail(char *s,int len,int *
32
                                                                                                       fail){
      void build_fail(){
                                                         這種利用vt的方法可以0(1)歸零vis陣列*/
                                                88
                                                                                                                                                  9.6 suffix array lcp.cpp
                                                         for(int i=0;s[i];++i){
                                                                                                    int id=-1;
        S[0].fail=S[0].efl=-1;
                                                89
                                                                                                    fail[0]=-1;
                                                          id=s[i]-L;
        q.clear();
                                                90
                                                                                                    for(int i=1;i<len;++i){</pre>
                                                           while(!S[p].next[id]&&p)p=S[p].fail;
        q.push_back(0);
                                                91
                                                                                                      while(~id&&s[id+1]!=s[i])id=fail[id];
        ++ae:
                                                92
                                                           if(!S[p].next[id])continue;
                                                                                                                                                 1 #define radix sort(x,y){\
                                                                                                      if(s[id+1]==s[i])++id;
                                                                                                                                                    for(i=0;i<A;++i)c[i]=0;\</pre>
        while(qs!=qe){
                                                93
                                                           p=S[p].next[id];
                                                                                                      fail[i]=id;
                                                                                                                                                     for(i=0;i<len;++i)c[x[y[i]]]++;\</pre>
          int pa=q[qs++],id,t;
                                                94
                                                           if(S[p].ed&&S[p].vis!=vt){
          for(int i=0;i<=R-L;++i){</pre>
                                                95
                                                            S[p].vis=vt;
                                                                                                                                                     for(i=1;i<A;++i)c[i]+=c[i-1];\</pre>
                                                                                                10 }
                                                                                                                                                     for(i=len-1;i>=0;--i)sa[--c[x[y[i]]]]=y[i
            t=S[pa].next[i];
                                                96
                                                             ans+=S[p].ed;
                                                                                                11 /*以字串B匹配字串A· 傳回匹配成功的數量(用B的
            if(!t)continue;
                                                97
42
                                                                                                                                                         ];\
```

```
10.2 tnfshb017_2_sat.cpp
7 void suffix array(const char *s,int len,int
                                                    1 | struct dominator tree{
                                                                                                                                                                             putchar('+');
                                                                                                                                                         64
        *sa,int *rank,int *tmp,int *c){
                                                        static const int MAXN=5005;
                                                                                                                                                         65
                                                                                                                                                                         else
     int A='z'+1,i,k,id,*t;
                                                        int n;// 1-base
                                                                                                                                                         66
                                                                                                                                                                             putchar('-');
     for(i=0;i<len;++i){</pre>
                                                        vector<int> suc[MAXN],pre[MAXN];
                                                                                                       1 | #include < bits / stdc++.h>
                                                                                                                                                         67
      tmp[i]=i;
                                                        int fa[MAXN],dfn[MAXN],id[MAXN],Time;
                                                                                                                                                                    putchar('\n');
10
                                                                                                       2 using namespace std;
                                                                                                                                                         68
11
       rank[i]=s[i];
                                                        int semi[MAXN],idom[MAXN];
                                                                                                       3 #define MAXN 8001
                                                                                                                                                                }else puts("0");
12
                                                        int anc[MAXN], best[MAXN]; // disjoint set
                                                                                                       4 #define MAXN2 MAXN*4
                                                                                                                                                         70
                                                                                                                                                                return 0;
                                                        vector<int> dom[MAXN];//dominator_tree
                                                                                                       5 #define n(X) ((X)+2*N)
13
     radix_sort(rank,tmp);
                                                                                                                                                         71
14
     for(k=1;id<len-1;k<<=1){</pre>
                                                        void init(int n){
                                                                                                       6 vector<int> v[MAXN2];
                                                                                                       7 vector<int> rv[MAXN2];
15
       id=0;
                                                   10
                                                          n=_n;
16
       for(i=len-k;i<len;++i)tmp[id++]=i;</pre>
                                                          for(int i=1;i<=n;++i)suc[i].clear(),pre[</pre>
                                                                                                       8 vector(int) vis t;
                                                   11
                                                                                                                                                            10.3 橋連通分量.cpp
17
       for(i=0;i<len;++i){</pre>
                                                               i].clear();
                                                                                                         int N,M;
                                                                                                         void addedge(int s,int e){
18
         if(sa[i]>=k)tmp[id++]=sa[i]-k;
                                                   12
19
                                                   13
                                                        void add_edge(int u,int v){
                                                                                                             v[s].push back(e);
20
       radix sort(rank,tmp);
                                                   14
                                                          suc[u].push back(v);
                                                                                                      12
                                                                                                             rv[e].push back(s);
                                                                                                                                                          1 | #define N 1005
       t=rank; rank=tmp; tmp=t;
                                                   15
                                                          pre[v].push_back(u);
                                                                                                      13
                                                                                                                                                            struct edge{
21
                                                                                                                                                              int u,v;
22
                                                   16
                                                                                                      14 int scc[MAXN2];
                                                                                                      15 bool vis[MAXN2]={false};
23
       rank[sa[0]]=0;
                                                   17
                                                        void dfs(int u){
                                                                                                                                                              bool is_bridge;
                                                                                                                                                              edge(int u=0,int v=0):u(u),v(v),is_bridge
       for(i=1;i<len;++i){</pre>
                                                          dfn[u]=++Time,id[Time]=u;
                                                                                                         void dfs(vector<int> *uv,int n,int k=-1){
24
                                                                                                      16
25
         if(tmp[sa[i-1]]!=tmp[sa[i]]||sa[i-1]+k 19
                                                          for(auto v:suc[u]){
                                                                                                      17
                                                                                                             vis[n]=true;
              >=len||tmp[sa[i-1]+k]!=tmp[sa[i]+k 20
                                                            if(dfn[v])continue;
                                                                                                             for(int i=0;i<uv[n].size();++i)</pre>
                                                                                                      18
                                                                                                                                                            };
                                                            dfs(v),fa[dfn[v]]=dfn[u];
              1)++id:
                                                                                                      19
                                                                                                                 if(!vis[uv[n][i]])
                                                                                                                                                            vector<edge> E;
         rank[sa[i]]=id;
                                                                                                                     dfs(uv,uv[n][i],k);
                                                                                                                                                            vector<int> G[N];// 1-base
26
                                                   22
                                                                                                      20
                                                                                                             if(uv==v)vis_t.push_back(n);
                                                                                                                                                            int low[N], vis[N], Time;
27
                                                   23
                                                                                                      ^{21}
28
       A=id+1;
                                                   24
                                                        int find(int x){
                                                                                                      22
                                                                                                             scc[n]=k;
                                                                                                                                                            int bcc_id[N],bridge_cnt,bcc_cnt;// 1-base
                                                          if(x==anc[x])return x;
                                                   25
                                                                                                      23
29
                                                                                                                                                            int st[N],top;//BCC用
                                                                                                         void solve(){
30
                                                   26
                                                          int y=find(anc[x]);
                                                                                                      24
                                                                                                                                                            inline void add_edge(int u,int v){
                                                          if(semi[best[x]]>semi[best[anc[x]]])best
                                                                                                             for(int i=1;i<=N;++i){</pre>
31 #undef radix_sort
                                                   27
                                                                                                                                                              G[u].push_back(E.size());
   //h:高度數組 sa:後綴數組 rank:排名
                                                               [x]=best[anc[x]];
                                                                                                      26
                                                                                                                 if(!vis[i])dfs(v,i);
                                                                                                                                                              E.push_back(edge(u,v));
                                                          return anc[x]=y;
                                                                                                      27
                                                                                                                 if(!vis[n(i)])dfs(v,n(i));
   inline void suffix array lcp(const char *s,
                                                                                                                                                              G[v].push_back(E.size());
       int len,int *h,int *sa,int *rank){
                                                   29
                                                                                                      28
                                                                                                                                                              E.push back(edge(v,u));
                                                        void tarjan(int r){
                                                                                                             memset(vis,0,sizeof(vis));
                                                   30
                                                                                                      29
                                                                                                                                                         17 }
     for(int i=0;i<len;++i)rank[sa[i]]=i;</pre>
                                                                                                             int c=0;
                                                   31
                                                          Time=0;
                                                                                                      30
    for(int i=0,k=0;i<len;++i){</pre>
                                                                                                                                                         18 void dfs(int u,int re=-1){//u當前點,re為u連
                                                   32
                                                          for(int t=1;t<=n;++t){</pre>
                                                                                                      31
                                                                                                             for(int i=vis_t.size()-1;i>=0;--i)
36
       if(rank[i]==0)continue;
                                                                                                                                                                 接前一個點的邊
                                                                                                                 if(!vis[vis_t[i]])
       if(k)--k;
                                                   33
                                                            dfn[t]=idom[t]=0;//u=r或 是u無法到達r時
                                                                                                                                                              int v;
                                                                                                      33
                                                                                                                      dfs(rv,vis t[i],c++);
       while(s[i+k]==s[sa[rank[i]-1]+k])++k;
                                                                 idom[id[u]]=0
                                                                                                                                                              low[u]=vis[u]=++Time;
                                                                                                                                                         20
                                                                                                      34 }
       h[rank[i]]=k;
                                                            dom[t].clear();
39
                                                   34
                                                                                                                                                              st[top++]=u;
                                                                                                      35
                                                                                                         int main(){
40
                                                            anc[t]=best[t]=semi[t]=t;
                                                   35
                                                                                                                                                              for(size_t i=0;i<G[u].size();++i){</pre>
                                                                                                      36
                                                                                                             int a,b;
41
    h[0]=0;
                                                   36
                                                                                                                                                                int e=G[u][i];v=E[e].v;
                                                                                                             scanf("%d%d",&N,&M);
                                                                                                      37
                                                   37
                                                          dfs(r);
                                                                                                                                                                if(!vis[v]){
                                                                                                      38
                                                                                                             for(int i=1;i<=N;++i){</pre>
                                                   38
                                                          for(int y=Time;y>=2;--y){
                                                                                                                                                                  dfs(v,e^1);//e^1反向邊
                                                                                                                                                         25
                                                                                                                 // (A or B)&(!A & !B) A^B
                                                            int x=fa[y],idy=id[y];
                                                                                                      39
                                                   39
                                                                                                                                                                  low[u]=min(low[u],low[v]);
                                                            for(auto z:pre[idy]){
                                                                                                                 a=i*2-1;
                                                   40
                                                                                                                                                                  if(vis[u]<low[v]){</pre>
  9.7 Z.cpp
                                                   41
                                                              if(!(z=dfn[z]))continue;
                                                                                                                 b=i*2;
                                                                                                                                                                    E[e].is_bridge=E[e^1].is_bridge=1;
                                                                                                                 addedge(n(a),b);
                                                              find(z);
                                                                                                                                                                     ++bridge cnt;
                                                                                                                 addedge(n(b),a);
                                                              semi[y]=min(semi[y],semi[best[z]]);
1 inline void z alg(char *s,int len,int *z){
                                                                                                      44
                                                                                                                 addedge(a,n(b));
                                                                                                                                                                }else if(vis[v]<vis[u]&&e!=re)</pre>
     int 1=0,r=0;
                                                                                                      45
                                                                                                                 addedge(b,n(a));
                                                            dom[semi[y]].push_back(y);
                                                   45
                                                                                                                                                                  low[u]=min(low[u], vis[v]);
                                                                                                                                                         32
    z[0]=len;
                                                   46
                                                            anc[y]=x;
                                                                                                                                                         33
     for(int i=1;i<len;++i){</pre>
                                                                                                             while(M--){
                                                                                                      47
                                                   47
                                                            for(auto z:dom[x]){
       z[i]=i>r?0:(i-1+z[i-1]< z[1]?z[i-1]:r-i
                                                                                                                                                         34
                                                                                                                                                              if(vis[u]==low[u]){//處理BCC
                                                                                                                 scanf("%d%d",&a,&b);
                                                              find(z);
                                                                                                                                                                ++bcc_cnt;// 1-base
                                                                                                                 a = a>0?a*2-1:-a*2;
                                                              idom[z]=semi[best[z]]<x?best[z]:x;</pre>
       while(i+z[i]<len&&s[i+z[i]]==s[z[i]])++z
                                                                                                                                                                do bcc_id[v=st[--top]]=bcc_cnt;//每個點
                                                                                                                                                         36
                                                                                                                 b = b>0?b*2-1:-b*2;
                                                   50
            [i];
                                                                                                      51
                                                                                                                 // A or B
                                                                                                                                                                      所在的BCC
                                                            dom[x].clear();
       if(i+z[i]-1>r)r=i+z[i]-1,l=i;
                                                                                                                 addedge(n(a),b);
                                                                                                                                                                 while(v!=u);
                                                                                                                                                         37
                                                   52
                                                                                                                 addedge(n(b),a);
                                                                                                                                                         38
                                                                                                      53
                                                   53
                                                          for(int u=2;u<=Time;++u){</pre>
                                                   54
                                                            if(idom[u]!=semi[u])idom[u]=idom[idom[
                                                                                                      54
                                                                                                             solve();
                                                                                                                                                            inline void bcc init(int n){
                                                            dom[id[idom[u]]].push_back(id[u]);
                                                                                                      56
                                                                                                             bool check=true;
                                                                                                                                                              Time=bcc cnt=bridge cnt=top=0;
                                                   55
                                                                                                             for(int i=1;i<=2*N;++i)</pre>
                                                   56
                                                                                                                                                              E.clear();
          Tarjan
                                                                                                      58
                                                                                                                 if(scc[i]==scc[n(i)])
                                                                                                                                                              for(int i=1;i<=n;++i){</pre>
                                                   57
                                                                                                      59
                                                                                                                     check=false;
                                                                                                                                                         44
                                                                                                                                                                G[i].clear();
                                                   58 }dom;
                                                                                                             if(check){
                                                                                                                                                                vis[i]=bcc_id[i]=0;
                                                                                                      60
                                                                                                                                                         45
                                                                                                      61
                                                                                                                 printf("%d \ n", N);
                                                                                                                                                         46
           dominator tree.cpp
                                                                                                                 for(int i=1;i<=2*N;i+=2){</pre>
                                                                                                                                                         47 }
                                                                                                      62
                                                                                                                      if(scc[i]>scc[i+2*N])
```

15

16

17

21

24

25

34

35

36

38

39

10.4 雙連通分量 & 割點.cpp

```
1 | #define N 1005
vector<int> G[N];// 1-base
3 | vector<int> bcc[N]://存每塊雙連通分量的點
4 int low[N], vis[N], Time;
5 int bcc_id[N],bcc_cnt;// 1-base
6 bool is cut[N];//是否為割點
7 int st[N],top;
   void dfs(int u,int pa=-1){//u當前點,pa父親
    int v.child=0:
    low[u]=vis[u]=++Time;
    st[top++]=u;
    for(size t i=0;i<G[u].size();++i){</pre>
      if(!vis[v=G[u][i]]){
         dfs(v,u),++child;
        low[u]=min(low[u],low[v]);
15
        if(vis[u]<=low[v]){</pre>
17
          is cut[u]=1;
          bcc[++bcc cnt].clear();
          int t;
            bcc_id[t=st[--top]]=bcc_cnt;
            bcc[bcc cnt].push back(t);
22
           }while(t!=v);
23
24
          bcc id[u]=bcc cnt;
25
          bcc[bcc cnt].push back(u);
26
27
      }else if(vis[v]<vis[u]&&v!=pa)//反向邊
28
        low[u]=min(low[u], vis[v]);
29
30
    if(pa==-1&&child<2)is_cut[u]=0;//u是dfs樹
          的根要特判
31
   inline void bcc init(int n){
    Time=bcc_cnt=top=0;
    for(int i=1;i<=n;++i){</pre>
34
35
      G[i].clear();
36
      is cut[i]=vis[i]=bcc id[i]=0;
37
```

Tree problem

11.1 HeavyLight.cpp

```
1 | #include < vector >
2 #define MAXN 100005
3 typedef std::vector<int >::iterator VIT;
4 int siz[MAXN], max son[MAXN], pa[MAXN], dep[
       MAXN1:
5 int link_top[MAXN],link[MAXN],cnt;
 std::vector<int >G[MAXN];
  void find max son(int x){
    siz[x]=1;
    \max son[x]=-1;
    for(VIT i=G[x].begin();i!=G[x].end();++i){
      if(*i==pa[x])continue;
      pa[*i]=x;
```

```
dep[*i]=dep[x]+1;
      find max son(*i);
      if(max son[x]==-1||siz[*i]>siz[max_son[x
                                             28
           ]]) max son[x]=*i;
      siz[x]+=siz[*i];
18
   void build link(int x,int top){
    link[x]=++cnt;
    link top[x]=top;
    if(max son[x]==-1)return;
    build link(max son[x],top);
    for(VIT i=G[x].begin();i!=G[x].end();++i){
      if(*i==max son[x]||*i==pa[x])continue;
26
      build link(*i,*i);
27
28
  inline int find_lca(int a,int b){
    //求LCA · 可以在過程中對區間進行處理
    int ta=link_top[a],tb=link_top[b];
    while(ta!=tb){
      if(dep[ta]<dep[tb]){</pre>
        std::swap(ta,tb);
        std::swap(a,b);
37
      //這裡可以對a所在的鏈做區間處理
      //區間為(link[ta],link[a])
      ta=link top[a=pa[ta]];
40
    //最後a,b會在同一條鏈,若a!=b還要在進行一
         次區間處理
    return dep[a]<dep[b]?a:b;</pre>
  11.2 LCA.cpp
```

```
1 #define MAXN 100000
2 #define MAX LOG 17
3 int pa[MAX LOG+1][MAXN+5];
4 int dep[MAXN+5];
  vector<int>G[MAXN+5];
  void dfs(int x,int p){\frac{1}{fs(1,-1)}};
     pa[0][x]=p;
     for(int i=0;i+1<MAX_LOG;++i)pa[i+1][x]=pa[</pre>
          i][pa[i][x]];
     for(auto &i:G[x]){
      if(i==p)continue;
       dep[i]=dep[x]+1;
12
       dfs(i,x);
13
14 }
inline int jump(int x,int d){
   for(int i=0;i<d;++i)if((x>>i)&1)x=pa[k][x];
    return x:
18
  inline int find_lca(int a,int b){
    if(dep[a]>dep[b])swap(a,b);
     b=jump(b,dep[b]-dep[a]);
    if(a==b)return a;
     for(int i=MAX LOG;i>=0;--i){
      if(pa[i][a]!=pa[i][b]){
24
         a=pa[i][a];
```

```
link cut tree.cop
```

b=pa[i][b];

return pa[0][a];

1 | #include < vector >

27

29

}

```
2 struct splay tree{
    int ch[2],pa;//子節點跟父母
    bool rev;//反轉的懶惰標記
                                               58
    splay_tree():pa(0),rev(0){ch[0]=ch[1]=0;}
6 };
7 vector<splay tree> node;
8 //有的時候用vector會TLE,要注意
9 | // 這邊以node [0] 作為null 節點
                                               62
10 bool isroot(int x){//判斷是否為這棵splay
                                               63
       tree的根
    return node[node[x].pa].ch[0]!=x&&node[
                                               65
         node[x].pa].ch[1]!=x;
                                               66
12 }
                                               67
  void down(int x){// 懶 惰 標 記 下 推
14
    if(node[x].rev){
      if(node[x].ch[0])node[node[x].ch[0]].rev
      if(node[x].ch[1])node[node[x].ch[1]].rev
                                               72
      std::swap(node[x].ch[0],node[x].ch[1]);
17
      node[x].rev^=1;
18
                                               75
19
20 }
  void push_down(int x){//將所有祖先的懶惰標記
    if(!isroot(x))push_down(node[x].pa);
^{22}
23
    down(x);
                                               81
24 }
                                               82
25 | void up(int x){}//將子節點的資訊向上更新
                                               83
                                               84
  void rotate(int x){//旋轉·會自行判斷轉的方
    int y=node[x].pa,z=node[y].pa,d=(node[y].
         ch[1]==x);
    node[x].pa=z;
    if(!isroot(y))node[z].ch[node[z].ch[1]==y
                                               91
    node[y].ch[d]=node[x].ch[d^1];
    node[node[y].ch[d]].pa=y;
    node[y].pa=x,node[x].ch[d^1]=y;
32
33
    up(y);
34
    up(x);
                                               96
35
36 | void splay(int x){//將節點x伸展到所在splay
       tree的 根
    push_down(x);
                                              100
    while(!isroot(x)){
      int y=node[x].pa;
      if(!isroot(y)){
        int z=node[y].pa;
42
        if((node[z].ch[0]==y)^(node[y].ch[0]==
                                              105
             x))rotate(y);
        else rotate(x);
```

```
rotate(x);
46
47
   int access(int x){
48
49
     int last=0;
     while(x){
       splay(x);
51
       node[x].ch[1]=last;
       up(x);
54
       last=x;
55
       x=node[x].pa:
56
     return last://回傳access後splay tree的根
59 | void access(int x, bool is=0){//is=0就是一般
         的access
      int last=0;
     while(x){
       splav(x):
       if(is&&!node[x].pa){
         //printf("%d\n", max(node[last].ma, node
              [node[x].ch[1]].ma));
       node[x].ch[1]=last;
       up(x);
       last=x:
       x=node[x].pa;
   void query edge(int u,int v){
     access(u);
     access(v,1);
   void make root(int x){
     access(x), splay(x);
     node[x].rev^=1;
   void make root(int x){
     node[access(x)].rev^=1;
     splay(x);
   void cut(int x,int y){
     make root(x);
     access(y);
     splay(y);
     node[y].ch[0]=0;
     node[x].pa=0;
   void cut_parents(int x){
     access(x);
     splay(x);
     node[node[x].ch[0]].pa=0;
     node[x].ch[0]=0;
   void link(int x,int y){
     make root(x);
     node[x].pa=y;
   int find root(int x){
     x=access(x);
     while(node[x].ch[0])x=node[x].ch[0];
     splay(x);
     return x;
106 }
```

```
107 int query(int u,int v){
108 // 傳回uv路徑splay tree的根結點
109 // 這種寫法無法求LCA
     make root(u);
111
     return access(v);
112
int query_lca(int u,int v){
114 //假設求鏈上點權的總和, sum是子樹的權重和,
       data是節點的權重
     access(u);
     int lca=access(v);
116
     splay(u);
     if(u==lca){
118
     //return node[lca].data+node[node[lca].
119
           ch[1]].sum
     }else{
120
       //return node[lca].data+node[node[lca].
           ch[1]].sum+node[u].sum
122
123
124 struct EDGE{
    int a,b,w;
126 }e[10005];
127 int n;
128 vector<pair<int ,int > >G[10005];
129 //first表示子節點· second表示邊的編號
int pa[10005],edge_node[10005];
131 //pa是父母節點,暫存用的,edge node是每個編
        被存在哪個點裡面的陣列
132 void bfs(int root){
133 | // 在建構的時候把每個點都設成一個 splay tree ·
       不會壞掉
     queue<int > q;
     for(int i=1;i<=n;++i)pa[i]=0;</pre>
     q.push(root);
137
     while(q.size()){
138
       int u=q.front();
139
       q.pop();
140
       for(int i=0;i<(int)G[u].size();++i){</pre>
141
         int v=G[u][i].first;
         if(v!=pa[u]){
142
143
           pa[v]=u;
144
           node[v].pa=u;
           node[v].data=e[G[u][i].second].w;
145
           edge_node[G[u][i].second]=v;
146
147
           up(v);
148
           q.push(v);
149
150
151
152
   void change(int x,int b){
     splay(x);
     //node[x].data=b;
156
    up(x);
157 }
```

11.4 POJ tree.cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
```

```
3 #define MAXN 10005
 4 int n,k;
 5 vector<pair<int,int> >g[MAXN];
 6 int size[MAXN];
7 bool vis[MAXN];
 8 inline void init(){
    for(int i=0;i<=n;++i){</pre>
     g[i].clear();
11
      vis[i]=0;
12
13 }
14 void get dis(vector<int> &dis,int u,int pa,
15
     dis.push back(d);
     for(size_t i=0;i<g[u].size();++i){</pre>
      int v=g[u][i].first,w=g[u][i].second;
17
       if(v!=pa&&!vis[v])get_dis(dis,v,u,d+w);
19
20 }
21 vector < int > dis; // 這東西如果放在函數裡會TLE
22 int cal(int u,int d){
    dis.clear();
     get dis(dis,u,-1,d);
     sort(dis.begin(),dis.end());
     int l=0,r=dis.size()-1,res=0;
     while(l<r){</pre>
       while(1<r&&dis[1]+dis[r]>k)--r;
       res+=r-(1++);
30
31
    return res;
32 }
pair<int,int> tree centroid(int u,int pa,
        const int sz){
     size[u]=1;//找樹重心, second是重心
     pair<int,int> res(INT_MAX,-1);
     int ma=0;
     for(size t i=0;i<g[u].size();++i){</pre>
       int v=g[u][i].first;
       if(v==pa||vis[v])continue;
       res=min(res,tree centroid(v,u,sz));
       size[u]+=size[v];
       ma=max(ma,size[v]);
     ma=max(ma,sz-size[u]);
     return min(res,make pair(ma,u));
   int tree DC(int u,int sz){
     int center=tree centroid(u,-1,sz).second;
49
     int ans=cal(center,0);
     vis[center]=1;
51
     for(size t i=0;i<g[center].size();++i){</pre>
       int v=g[center][i].first,w=g[center][i].
            second;
       if(vis[v])continue;
53
       ans-=cal(v,w);
       ans+=tree DC(v,size[v]);
55
56
57
     return ans;
58
59
   int main(){
     while(scanf("%d%d",&n,&k),n||k){
61
       init();
       for(int i=1;i<n;++i){</pre>
62
         int u.v.w:
         scanf("%d%d%d",&u,&v,&w);
```

```
g[u].push back(make pair(v,w));
         g[v].push_back(make_pair(u,w));
67
      printf("%d \setminus n", tree DC(1,n));
69
70
    return 0;
```

zformula

12.1 formula.tex

12.1.1 Pick 公式

給定頂點坐標均是整點的簡單多邊形,面積 = 內部格點數 + 邊上格點數/2-1

12.1.2 圖論

- 1. V E + F = 2
- 2. 對於平面圖 $F = E V + n + 1 \cdot n$ 是連通分量
- 3. 對於平面圖 $\cdot E < 3V 6$
- 4. 對於連通圖 G · 最大獨立點集的大小設為 I(G) · 最 大匹配大小設為 M(G),最小點覆蓋設為 Cv(G), 最小邊覆蓋設為 Ce(G)。對於任意連通圖:

(a)
$$I(G) + Cv(G) = |V|$$

(b) $M(G) + Ce(G) = |V|$

- 5. 對於連通二分圖:
 - (a) I(G) = Cv(G)(b) M(G) = Ce(G)

12.1.3 學長公式

- 1. $\sum_{d|n} phi(n) = n$
- 2. $g(n) = \sum_{d|n} f(d) = f(n) = \sum_{d|n} mu(d) *$
- 3. $HarmonicseriesH_{n} = ln(n) + \gamma + 1/(2n) -$
- 5. 格雷碼 = $n \oplus (n >> 1)$
- 6. $SG(A+B) = SG(A) \oplus SG(B)$
- 7. 選轉矩陣 $M(\theta) = \begin{pmatrix} cos\theta & -sin\theta \\ sin\theta & cos\theta \end{pmatrix}$

12.1.4 基本數論

- 1. $\sum_{d|n} \mu(n) = (n == 1)$
- 2. $g(m) = \sum_{d|m} f(d) \Leftrightarrow f(m) = \sum_{d|m} \mu(d) *$
- g(m/d) 3. $\sum_{i=1}^{n} \sum_{j=1}^{m}$ 互質數量 $= \sum \mu(d) \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor$
- 4. $\sum_{i=1}^{n} \sum_{j=1}^{n} lcm(i,j) = n \sum_{d|n} d\phi(d)$

12.1.5 排組公式

- 1. k 卡特蘭 $\frac{C_n^{kn}}{n(k-1)+1} \cdot C_m^n = \frac{n!}{m!(n-m)!}$ 2. $H(n,m) \cong x_1 + x_2 \dots + x_n = k, num = k$
- 3. Stirling number of 2^{nd} , n 人分 k 組方法數目
 - (a) S(0,0) = S(n,n) = 1
 - (b) S(n,0) = 0
 - (c) S(n,k) = kS(n-1,k) + S(n-1,k-1)
- 4. Bell number,n 人分任意多組方法數目
 - (a) $B_0 = 1$

 - (a) $B_0 = \sum_{i=0}^{n} S(n, i)$ (b) $B_n = \sum_{i=0}^{n} S(n, i)$ (c) $B_{n+1} = \sum_{k=0}^{n} C_k^n B_k$ (d) $B_{p+n} \equiv B_n + B_{n+1} mod p$, p is prime
 - (e) $B_{p^m+n} \equiv mB_n + B_{n+1} mod p$, p is prime
 - (f) From B0:1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, 115975
- 5. Derangement, 錯排, 沒有人在自己位置上
 - (a) $D_n = n! \left(1 \frac{1}{1!} + \frac{1}{2!} \frac{1}{3!} \dots + (-1)^n \frac{1}{n!}\right)$
 - (b) $D_n = (n-1)(D_{n-1} + D_{n-2}), D_0 =$ $1, D_1 = 0$
 - (c) From D0:1, 0, 1, 2, 9, 44, 265, 1854, 14833, 133496

12.1.6 冪次, 冪次和

- 1. $a^b \% P = a^{b \% \varphi(p) + \varphi(p)}, b > \varphi(p)$

- 1. $u^{2}(n) u^{2}$ $v^{2}(p)$ 2. $1^{3} + 2^{3} + 3^{3} + \dots + n^{3} = \frac{n^{4}}{4} + \frac{n^{3}}{4} + \frac{n^{2}}{4}$ 3. $1^{4} + 2^{4} + 3^{4} + \dots + n^{4} = \frac{n^{5}}{5} + \frac{n^{4}}{2} + \frac{n^{3}}{3} \frac{n}{30}$ 4. $1^{5} + 2^{5} + 3^{5} + \dots + n^{5} = \frac{n^{6}}{6} + \frac{n^{5}}{2} + \frac{5n^{4}}{12} \frac{n^{2}}{12}$ 5. $0^{k} + 1^{k} + 2^{k} + \dots + n^{k} = P(k), P(k) = \frac{n^{2}}{2} + \frac{n^$ 5. $0+1+2+\ldots+n=P(k), P(k)=\frac{(n+1)^{k+1}-\sum_{i=0}^{k-1}C_i^{k+1}P(i)}{k+1}, P(0)=n+1$ 6. $\sum_{k=0}^{m-1}k^n=\frac{1}{n+1}\sum_{k=0}^nC_k^{n+1}B_km^{n+1-k}$ 7. $\sum_{j=0}^mC_j^{m+1}B_j=0, B_0=1$ 8. 除了 $B_1=-1/2\cdot$ 剩下的奇數項都是 0

- 9. $B_2 = 1/6, B_4 = -1/30, B_6 = 1/42, B_8 =$ -1/30, $B_{10} = 5/66$, $B_{12} = -691/2730$, $B_{14} =$

12.1.7 Burnside's lemma

- 1. $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- 2. $X^g = t^{c(g)}$
- 3. G 表示有幾種轉法, X^g 表示在那種轉法下,有幾種 是會保持對稱的,t是顏色數,c(q)是循環節不動的
- 4. 正立方體塗三顏色,轉 0 有 36 個元素不變,轉 90 有 6 種, 每種有 33 不變, 180 有 3 × 34,

12.1.8 Count on a tree

- 1. Rooted tree: $s_{n+1} = \frac{1}{n} \sum_{i=1}^{n} (i \times a_i \times a_i)$ $\sum_{j=1}^{\lfloor n/i \rfloor} a_{n+1-i \times j}$ 2. Unrooted tree:
- - (a) $\text{Odd}: a_n \sum_{i=1}^{n/2} a_i a_{n-i}$ (b) $\text{Even}: Odd + \frac{1}{2} a_{n/2} (a_{n/2} + 1)$
- 3. Spanning Tree

- (a) 完全圖 $n^n 2$
- (b) 一般圖 (Kirchhoff's theorem)M[i][i] = degree (V_i) , M[i][j] = -1, if have E(i, j), 0 if no edge. delete any one row and col in $A, \ ans = det(A)$

12.1.9 積分表

1.
$$\int \frac{1}{x} dx = \ln|x|$$

2. $\int u dv = uv - \int v du$
3. $\int a^x dx = \frac{1}{\ln a} a^x$
4. $\int \ln x dx = x \ln x - x$
5. $\int \tan x dx = \ln|\sec x|$
6. $\int \sec x dx = \ln|\sec x + \tan x|$
7. $\int \sec^2 x dx = \tan x$
8. $\int \sec \tan x dx = \sec x$

9.
$$\int \frac{a}{a^2 + x^2} dx = \tan^{-1} \frac{x}{a}$$
10.
$$\int \frac{a}{a^2 - x^2} dx = \frac{1}{2} \ln \left| \frac{x + a}{x - a} \right|$$
11.
$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a}$$
12.
$$\int \frac{a}{x \sqrt{x^2 - a^2}} dx = \sec^{-1} \frac{x}{a}$$
13.
$$\int \frac{1}{\sqrt{x^2 - a^2}} dx = \cosh^{-1} \frac{x}{a} = \ln(x + \sqrt{x^2 - a^2})$$
14.
$$\int \frac{1}{\sqrt{x^2 + a^2}} dx = \sinh^{-1} \frac{x}{a} = \ln(x + \sqrt{x^2 + a^2})$$

ACM ICPC TEAM REFERENCE - NTHU			4	Flow 4.1 dinic.cpp	7 7 7	8.11 外星模運算.cpp	15 15
JINKELA			5	Graph 5.1 Augmenting_Path.cpp	8 8 8	9 String 9.1 AC 自動機.cpp 9.2 hash.cpp 9.3 KMP.cpp 9.4 manacher.cpp	
Contents				 5.4 graphISO.cpp	8 9	9.5 minimal_string_rotation.cpp	16 16 17
1.5 1.5 1.5 1.4	2 SmallestCircle.cpp	1 1 3 3 3		5.7 Minimum_General_Weighted_Matching.cpp 5.8 Rectilinear_Steiner_tree.cpp 5.9 treeISO.cpp 5.10 一般圖最大權匹配.cpp 5.11 全局最小割.cpp 5.12 最小樹形圖 _ 朱劉.cpp	9 9 10 11 11	10 Tarjan 10.1 dominator_tree.cpp 10.2 tnfshb017_2_sat.cpp 10.3 橋連通分量.cpp 10.4 雙連通分量 & 割點.cpp	17 17
2 D. 2.1 2.2 2.2 2.4 2.5	Dynamic_KD_tree.cpp	3 3 4 4 5 5		language 6.1 CNF.cpp	11 11 11 12 12	11 Tree_problem 11.1 HeavyLight.cpp 11.2 LCA.cpp 11.3 link_cut_tree.cpp 11.4 POJ_tree.cpp	18
2.6 2.7 2.8 2.9	6 skew_heap.cpp	5 6 6 6	8	Number_Theory 8.1 basic.cpp 8.2 bit_set.cpp 8.3 cantor_expansion.cpp 8.4 FFT.cpp 8.5 find_real_root.cpp	13 13 13 13 13 14	12 zformula 12.1 formula.tex	19 19 19 19 19
3.1 3.1 3.2	e fault 1 debug.cpp	6		8.6 LinearCongruence.cpp	14 14	12.1.5 排組公式	19 19 19