### Computational Geometal T dis2(const point<T> &p,bool is\_segment

55

56

57

58

59

60

61

62

70

74

76

77

78

79

80

83

85

88

#### 1.1 Geometry.cpp

```
1 const double PI=atan2(0.0,-1.0);
2 template<typename T>
3 struct point{
    T x,y;
    point(){}
    point(const T&x,const T&y):x(x),y(y){}
    point operator+(const point &b)const{
      return point(x+b.x,y+b.y); }
                                               65
    point operator-(const point &b)const{
      return point(x-b.x,y-b.y); }
    point operator*(const T &b)const{
                                               67
      return point(x*b,y*b); }
                                               68
    point operator/(const T &b)const{
                                               69
      return point(x/b,y/b); }
    bool operator == (const point &b)const{
                                               71
      return x==b.x&&y==b.y; }
                                               72
    T dot(const point &b)const{
                                               73
      return x*b.x+y*b.y; }
    T cross(const point &b)const{
      return x*b.y-y*b.x; }
21
    point normal()const{//求法向量
22
      return point(-y,x); }
    T abs2()const{//向量長度的平方
      return dot(*this); }
    T rad(const point &b)const{//兩向量的弧度
                                               81
   return fabs(atan2(fabs(cross(b)),dot(b))); }
                                               82
27
    T getA()const{//對x軸的弧度
      T A=atan2(y,x);//超過180度會變負的
                                               84
      if(A<=-PI/2)A+=PI*2;
      return A:
31
32
   template<typename T>
   struct line{
    line(){}
    point<T> p1,p2;
    T a,b,c;//ax+by+c=0
    line(const point<T>&x,const point<T>&y):p1
         (x),p2(y){}
    void pton(){//轉成一般式
40
      a=p1.y-p2.y;
      b=p2.x-p1.x;
41
      c=-a*p1.x-b*p1.v:
42
43
    T ori(const point<T> &p)const{//點和有向直
                                               97
         線的關係,>0左邊、=0在線上<0右邊
      return (p2-p1).cross(p-p1);
45
                                               99
46
                                               100
    T btw(const point<T> &p)const{//點投影落在 101
         線段 上 <=0
                                              102
48
      return (p1-p).dot(p2-p);
                                              103
49
    bool point_on_segment(const point<T>&p)
50
                                              104
         const{//點是否在線段上
                                              105
      return ori(p) == 0&&btw(p) <= 0;</pre>
                                              106
                                              107
```

```
=0) const { // 點 跟 直 線 / 線 段 的 距 離 平 方
  point<T> v=p2-p1.v1=p-p1:
                                           109
  if(is_segment){
                                           110
    point<T> v2=p-p2;
                                           111
    if(v.dot(v1)<=0)return v1.abs2();</pre>
                                           112
    if(v.dot(v2)>=0)return v2.abs2();
                                           113
                                           114
 T tmp=v.cross(v1);
                                           115 };
  return tmp*tmp/v.abs2();
T seg dis2(const line<T> &1)const{//兩線段 118
  return min({dis2(1.p1,1),dis2(1.p2,1),1. 120
       dis2(p1,1),1.dis2(p2,1)});
                                           121
                                           122
point<T> projection(const point<T> &p)
     const { // 點對直線的投影
                                           123
                                           124
  point<T> n=(p2-p1).normal();
                                           125
 return p-n*(p-p1).dot(n)/n.abs2();
                                           126
point<T> mirror(const point<T> &p)const{
                                          127
  //點對直線的鏡射,要先呼叫pton轉成一般式 128
 noint<T> R:
 T d=a*a+b*b:
 R.x=(b*b*p.x-a*a*p.x-2*a*b*p.y-2*a*c)/d; 130
  R.y=(a*a*p.y-b*b*p.y-2*a*b*p.x-2*b*c)/d; 131
  return R:
                                           133
                                          134
bool equal(const line &1)const{//直線相等
 return ori(1.p1)==0&&ori(1.p2)==0;
                                           136
bool parallel(const line &1)const{
 return (p1-p2).cross(1.p1-1.p2)==0;
                                           137
bool cross seg(const line &1)const{
                                           138
 return (p2-p1).cross(l.p1-p1)*(p2-p1).
       cross(1.p2-p1)<=0;//直線是否交線段
                                          139
int line intersect(const line &l)const{// 140
     直線相交情況,-1無限多點、1交於一點、0141
  return parallel(1)?(ori(1.p1)==0?-1:0)
                                           143
                                           144
                                           145
int seg intersect(const line &1)const{
 T c1=ori(l.p1), c2=ori(l.p2);
 T c3=1.ori(p1), c4=1.ori(p2);
                                           147
  if(c1==0&&c2==0){//共線
    bool b1=btw(1.p1)>=0,b2=btw(1.p2)>=0;
    T a3=1.btw(p1),a4=1.btw(p2);
                                           148
                                           149
    if(b1&&b2&&a3==0&&a4>=0) return 2;
                                           150
    if(b1&&b2&&a3>=0&&a4==0) return 3;
                                           151
   if(b1&&b2&&a3>=0&&a4>=0) return 0;
                                           152
    return -1://無限交點
  }else if(c1*c2<=0&&c3*c4<=0)return 1;</pre>
                                           153
 return 0;//不相交
                                           154
                                           155
point<T> line intersection(const line &l)
                                           156
     const{/*直線交點*/
                                           157
  point<T> a=p2-p1,b=l.p2-l.p1,s=l.p1-p1;
                                           158
  //if(a.cross(b)==0)return INF;
  return p1+a*(s.cross(b)/a.cross(b));
```

```
point<T> seg intersection(const line &1)
          const{//線段交點
                                                 162
       int res=seg intersect(1);
       if(res<=0) assert(0);</pre>
                                                 163
       if(res==2) return p1;
                                                 164
       if(res==3) return p2;
                                                 165
       return line intersection(1);
                                                 166
                                                 167
116 template<typename T>
   struct polygon{
                                                 168
     polygon(){}
     vector<point<T> > p;//逆時針順序
                                                 169
     T area()const{//面積
                                                 170
       T ans=0;
       for(int i=p.size()-1,j=0;j<(int)p.size()</pre>
                                                 17
            ;i=j++)
                                                 172
         ans+=p[i].cross(p[j]);
                                                 173
       return ans/2;
                                                 174
                                                 175
     point<T> center of mass()const{//重心
                                                 176
       T cx=0, cy=0, w=0;
       for(int i=p.size()-1,j=0;j<(int)p.size()</pre>
            ;i=j++){
                                                 177
         T a=p[i].cross(p[j]);
                                                 178
         cx+=(p[i].x+p[j].x)*a;
         cy+=(p[i].y+p[j].y)*a;
                                                 179
                                                 180
                                                 181
       return point<T>(cx/3/w,cy/3/w);
     char ahas(const point<T>& t)const{//點是否
          在簡單多邊形內,是的話回傳1、在邊上回 183
                                                 184

值 - 1 、 否 則 回 值 a

       bool c=0;
                                                 186
       for(int i=0,j=p.size()-1;i<p.size();j=i</pre>
                                                 188
         if(line<T>(p[i],p[j]).point_on_segment
              (t))return -1;
                                                 190
         else if((p[i].y>t.y)!=(p[j].y>t.y)&&
         t.x<(p[j].x-p[i].x)*(t.y-p[i].y)/(p[j]
                                                 191
              ].y-p[i].y)+p[i].x)
                                                 192
           c=!c;
                                                 193
       return c;
                                                 194
     char point_in_convex(const point<T>&x)
                                                 195
                                                 196
       int l=1,r=(int)p.size()-2;
                                                 197
       while(l<=r){//點是否在凸多邊形內,是的話
                                                 198
            回傳1、在邊上回傳-1、否則回傳0
                                                 199
         int mid=(1+r)/2;
                                                 200
         T a1=(p[mid]-p[0]).cross(x-p[0]);
         T a2=(p[mid+1]-p[0]).cross(x-p[0]);
                                                 202
         if(a1>=0&&a2<=0){
                                                 203
           T res=(p[mid+1]-p[mid]).cross(x-p[
                                                 204
                mid]);
                                                 205
           return res>0?1:(res>=0?-1:0);
         }else if(a1<0)r=mid-1;</pre>
                                                 206
         else l=mid+1:
                                                 207
                                                 208
       return 0;
                                                 209
     vector<T> getA()const{//凸包邊對x軸的夾角
       vector<T>res;//一定是遞增的
```

```
for(size t i=0;i<p.size();++i)</pre>
    res.push back((p[(i+1)\%p.size()]-p[i])
         .getA());
  return res:
bool line intersect(const vector<T>&A,
     const line<T> &1)const{//O(LoaN)
  int f1=upper bound(A.begin(), A.end(),(1.
       p1-l.p2).getA())-A.begin();
  int f2=upper bound(A.begin(), A.end(),(1.
       p2-l.p1).getA())-A.begin();
  return 1.cross seg(line<T>(p[f1],p[f2]))
polygon cut(const line<T> &l)const{//△包
     對 直 線 切 割 , 得 到 直 線 L 左 側 的 凸 包
  polygon ans;
  for(int n=p.size(),i=n-1,j=0;j<n;i=j++){</pre>
    if(l.ori(p[i])>=0){
      ans.p.push back(p[i]);
      if(1.ori(p[j])<0)
        ans.p.push_back(1.
             line intersection(line<T>(p[i
             ],p[j])));
    }else if(l.ori(p[j])>0)
      ans.p.push back(1.line intersection(
           line<T>(p[i],p[j])));
  return ans;
static bool graham cmp(const point<T>& a,
     const point<T>& b){//凸包排序函數
  return (a.x<b.x)||(a.x==b.x&&a.y<b.y);</pre>
void graham(vector<point<T> > &s){//凸包
  sort(s.begin(),s.end(),graham cmp);
  p.resize(s.size()+1);
  for(size t i=0;i<s.size();++i){</pre>
    while (m \ge 2\&\&(p[m-1]-p[m-2]).cross(s[i
         ]-p[m-2])<=0)--m;
    p[m++]=s[i];
  for(int i=s.size()-2,t=m+1;i>=0;--i){
    while (m>=t&&(p[m-1]-p[m-2]).cross(s[i
         ]-p[m-2])<=0)--m;
    p[m++]=s[i];
  if(s.size()>1)--m;
  p.resize(m);
T diam(){//直徑
  int n=p.size(),t=1;
  T ans=0;p.push_back(p[0]);
  for(int i=0;i<n;i++){</pre>
    point<T> now=p[i+1]-p[i];
    while(now.cross(p[t+1]-p[i])>now.cross
         (p[t]-p[i]))t=(t+1)%n;
    ans=\max(ans,(p[i]-p[t]).abs2());
  return p.pop back(),ans;
T min_cover_rectangle(){//最小覆蓋矩形
  int n=p.size(),t=1,r=1,1;
```

```
if(n<3)return 0;//也可以做最小周長矩形
                                                           vector<line<T> > q(n);
213
        T ans=1e99; p. push back(p[0]);
                                                   264
                                                           q[L=R=0]=s[0];
        for(int i=0;i<n;i++){</pre>
                                                           for(int i=1;i<n;++i){</pre>
214
                                                   265
215
         point<T> now=p[i+1]-p[i];
                                                   266
                                                             while(L<R&&s[i].ori(px[R-1])<=0)--R;</pre>
         while(now.cross(p[t+1]-p[i])>now.cross 267
                                                             while(L<R&&s[i].ori(px[L])<=0)++L;</pre>
216
               (p[t]-p[i]))t=(t+1)%n;
                                                             q[++R]=s[i];
217
          while(now.dot(p[r+1]-p[i])>now.dot(p[r 269
                                                             if(q[R].parallel(q[R-1])){
               ]-p[i]))r=(r+1)%n;
                                                   270
                                                                --R:
218
          if(!i)l=r;
                                                   271
                                                               if(q[R].ori(s[i].p1)>0)q[R]=s[i];
          while (now.dot(p[l+1]-p[i]) < =now.dot(p[272])
219
               1]-p[i]))1=(1+1)%n;
                                                             if(L < R)px[R-1] = q[R-1].
                                                                  line intersection(q[R]);
220
         T d=now.abs2():
          T tmp=now.cross(p[t]-p[i])*(now.dot(p[274]
221
              r]-p[i])-now.dot(p[l]-p[i]))/d;
                                                           while(L<R&&q[L].ori(px[R-1])<=0)--R;</pre>
222
         ans=min(ans,tmp);
                                                   276
                                                           p.clear();
                                                   277
                                                           if(R-L<=1)return 0;</pre>
223
                                                           px[R]=q[R].line intersection(q[L]);
224
       return p.pop_back(),ans;
                                                   278
                                                           for(int i=L;i<=R;++i)p.push_back(px[i]);</pre>
225
                                                   279
                                                   280
                                                           return R-L+1;
     T max_triangle(){//最大內接三角形
226
                                                   281
227
        int n=p.size(),a=1,b=2;
                                                   282 };
228
       if(n<3)return 0;</pre>
                                                   283 template<typename T>
229
       T ans=0,tmp;p.push back(p[0]);
                                                   284 struct triangle{
        for(int i=0;i<n;++i){</pre>
230
                                                         point<T> a,b,c;
          while((p[a]-p[i]).cross(p[b+1]-p[i])>( 285
231
                                                         triangle(){}
               tmp=(p[a]-p[i]).cross(p[b]-p[i])))^{286}
                                                         triangle(const point<T> &a,const point<T>
              b=(b+1)%n;
                                                              &b, const point<T> &c):a(a),b(b),c(c){}^{342}
          ans=max(ans,tmp);
                                                         T area()const{
233
          while((p[a+1]-p[i]).cross(p[b]-p[i])>( 288
                                                           T t=(b-a).cross(c-a)/2;
               tmp=(p[a]-p[i]).cross(p[b]-p[i])))^{289}
                                                           return t>0?t:-t;
              a=(a+1)%n;
         ans=max(ans,tmp);
                                                   291
234
235
                                                   292
                                                         point<T> barycenter()const{//重心
236
       return p.pop_back(),ans/2;
                                                   293
                                                           return (a+b+c)/3:
237
                                                   294
     T dis2(polygon &pl){//凸包最近距離平方
238
                                                   295
                                                         point<T> circumcenter()const{//外心
239
       vector<point<T> > &P=p,&Q=pl.p;
                                                   296
                                                           static line<T> u,v;
240
       int n=P.size(), m=Q.size(), l=0, r=0;
                                                   297
                                                           u.p1=(a+b)/2;
     for(int i=0;i<n;++i)if(P[i].y<P[1].y)l=i;</pre>
241
                                                  298
                                                           u.p2=point<T>(u.p1.x-a.y+b.y,u.p1.y+a.x-
     for(int i=0;i<m;++i)if(Q[i].y<Q[r].y)r=i;</pre>
242
                                                                b.x);
243
       P.push back(P[0]), Q.push back(Q[0]);
                                                   299
                                                           v.p1=(a+c)/2;
244
       T ans=1e99;
                                                           v.p2=point<T>(v.p1.x-a.y+c.y,v.p1.y+a.x-
245
       for(int i=0;i<n;++i){</pre>
         while((P[1]-P[1+1]).cross(Q[r+1]-Q[r]) 301
246
                                                           return u.line_intersection(v);
               <0)r=(r+1)%m;
          ans=min(ans,line\langle T \rangle (P[1],P[1+1]).
                                                         point<T> incenter()const{//內心
                                                   303
               seg_dis2(line<T>(Q[r],Q[r+1])));
                                                           T A=sqrt((b-c).abs2()),B=sqrt((a-c).abs2
                                                  304
         1=(1+1)%n;
                                                                ()),C=sqrt((a-b).abs2());
249
                                                           return point<T>(A*a.x+B*b.x+C*c.x,A*a.y+
                                                   305
250
       return P.pop_back(),Q.pop_back(),ans;
                                                                B*b.y+C*c.y)/(A+B+C);
251
                                                   306
252
     static char sign(const point<T>&t){
                                                   307
                                                         point<T> perpencenter()const{//垂心
       return (t.y==0?t.x:t.y)<0;</pre>
253
                                                   308
                                                           return barycenter()*3-circumcenter()*2;
254
                                                   309
     static bool angle cmp(const line<T>& A,
255
                                                   310 };
           const line<T>& B){
                                                       template<typename T>
                                                   311
        point < T > a=A.p2-A.p1.b=B.p2-B.p1:
256
                                                   312 struct point3D{
       return sign(a)<sign(b)||(sign(a)==sign(b 313
257
                                                         T x,y,z;
            )&&a.cross(b)>0);
                                                         point3D(){}
258
                                                         point3D(const T&x,const T&y,const T&z):x(x
259
     int halfplane_intersection(vector<line<T>
                                                              ),y(y),z(z){}
          > &s){//半平面交
                                                         point3D operator+(const point3D &b)const{
       sort(s.begin(),s.end(),angle_cmp);//線段 317
                                                           return point3D(x+b.x,y+b.y,z+b.z);}
260
                                                         point3D operator-(const point3D &b)const{ 371
             左側為該線段半平面
                                                   318
                                                           return point3D(x-b.x,y-b.y,z-b.z);}
        int L.R.n=s.size():
                                                   319
261
                                                         point3D operator*(const T &b)const{
                                                   320
262
        vector<point<T> > px(n);
```

```
return point3D(x*b,y*b,z*b);}
     point3D operator/(const T &b)const{
       return point3D(x/b,y/b,z/b);}
     bool operator==(const point3D &b)const{
       return x==b.x&&y==b.y&&z==b.z;}
     T dot(const point3D &b)const{
       return x*b.x+v*b.v+z*b.z:}
     point3D cross(const point3D &b)const{
       return point3D(y*b.z-z*b.y,z*b.x-x*b.z,x 378
            *b.y-y*b.x);}
     T abs2()const{//向量長度的平方
       return dot(*this);}
     T area2(const point3D &b)const{//和b、原點
          圍成面積的平方
       return cross(b).abs2()/4;}
334 };
335 template<typename T>
   struct line3D{
     point3D<T> p1,p2;
     line3D(){}
     line3D(const point3D<T> &p1,const point3D< 386
          T> &p2):p1(p1),p2(p2){}
     T dis2(const point3D<T> &p,bool is_segment 388
          =0) const { // 點 跟 直 線 / 線 段 的 距 離 平 方
       point3D<T> v=p2-p1,v1=p-p1;
       if(is segment){
         point3D<T> v2=p-p2;
         if(v.dot(v1)<=0)return v1.abs2();</pre>
         if(v.dot(v2)>=0)return v2.abs2();
       point3D<T> tmp=v.cross(v1);
       return tmp.abs2()/v.abs2();
     pair<point3D<T>,point3D<T> > closest_pair( 394
          const line3D<T> &1)const{
       point3D < T > v1 = (p1 - p2), v2 = (1.p1 - 1.p2);
       point3D<T> N=v1.cross(v2),ab(p1-l.p1);
       //if(N.abs2()==0)return NULL;平行或重合
       T tmp=N.dot(ab),ans=tmp*tmp/N.abs2();//
             最近點對距離
       point3D<T> d1=p2-p1,d2=l.p2-l.p1,D=d1.
            cross(d2),G=1.p1-p1;
       T t1=(G.cross(d2)).dot(D)/D.abs2();
       T t2=(G.cross(d1)).dot(D)/D.abs2();
       return make_pair(p1+d1*t1,l.p1+d2*t2);
     bool same_side(const point3D<T> &a,const
          point3D<T> &b)const{
       return (p2-p1).cross(a-p1).dot((p2-p1).
            cross(b-p1))>0;
363 };
   template<typename T>
365 struct plane{
     point3D<T> p0,n;//平面上的點和法向量
     plane(){}
     plane(const point3D<T> &p0, const point3D<T 413
          > &n):p0(p0),n(n){}
     T dis2(const point3D<T> &p)const{//點到平
                                                415
          面距離的平方
       T tmp=(p-p0).dot(n);
       return tmp*tmp/n.abs2();
372
```

322

323

325

326

327

328

330

332

333

336

338

339

340

344

345

346

347

348

349

350

351

353

354

356

357

359

360

361

362

370

```
point3D<T> projection(const point3D<T> &p)
374
       return p-n*(p-p0).dot(n)/n.abs2();
375
     point3D<T> line intersection(const line3D
376
          T> &1)const{
       T tmp=n.dot(1.p2-1.p1);//等於 Ø表示平行或
377
             重合該平面
       return 1.p1+(1.p2-1.p1)*(n.dot(p0-1.p1)/
            tmp):
379
     line3D<T> plane intersection(const plane &
380
          pl)const{
381
       point3D<T> e=n.cross(pl.n),v=n.cross(e);
382
       T tmp=pl.n.dot(v);//等於0表示平行或重合
       point3D<T> q=p0+(v*(pl.n.dot(pl.p0-p0))/
383
            tmp);
       return line3D<T>(q,q+e);
384
385
387
   template<typename T>
   struct triangle3D{
     point3D<T> a,b,c;
     triangle3D(){}
     triangle3D(const point3D<T> &a,const
          point3D<T> &b, const point3D<T> &c):a(a
          ),b(b),c(c){}
392
     bool point in(const point3D<T> &p)const{//
           點在該平面上的投影在三角形中
       return line3D<T>(b,c).same side(p,a)&&
393
            line3D<T>(a,c).same_side(p,b)&&
            line3D<T>(a,b).same_side(p,c);
395
   template<typename T>
396
   struct tetrahedron{//四面體
397
     point3D<T> a,b,c,d;
398
399
     tetrahedron(){}
     tetrahedron(const point3D<T> &a,const
          point3D<T> &b,const point3D<T> &c,
          const point3D<T> &d):a(a),b(b),c(c),d(
          d){}
     T volume6()const{//體積的六倍
       return (d-a).dot((b-a).cross(c-a));
403
     point3D<T> centroid()const{
404
405
       return (a+b+c+d)/4;
406
     bool point in(const point3D<T> &p)const{
       return triangle3D<T>(a,b,c).point in(p)
408
            &&triangle3D<T>(c,d,a).point_in(p);
409
410
   };
411
   template<typename T>
   struct convexhull3D{
     static const int MAXN=1005;
     struct face{
414
       int a,b,c;
416
       face(int a,int b,int c):a(a),b(b),c(c){}
417
418
     vector<point3D<T>> pt;
     vector<face> ans;
419
     int fid[MAXN][MAXN];
```

```
void build(){
                                                    15 Circle outcircle(Circle::p a, Circle::p b,
422
       int n=pt.size();
       ans.clear();
                                                            Circle::p c) {
423
424
       memset(fid,0,sizeof(fid));
                                                           if(TwoPointCircle(a,b).incircle(c))
                                                                return TwoPointCircle(a,b);
425
       ans.emplace back(0,1,2);//注意不能共線
       ans.emplace back(2,1,0);
                                                           if(TwoPointCircle(b,c).incircle(a))
426
                                                                return TwoPointCircle(b,c);
       int ftop = 0;
427
                                                           if(TwoPointCircle(c,a).incircle(b))
       for(int i=3, ftop=1; i<n; ++i,++ftop){</pre>
428
                                                                return TwoPointCircle(c,a);
429
         vector<face> next;
                                                           Circle::p ret;
          for(auto &f:ans){
430
                                                           double a1=b.x-a.x, b1=b.y-a.y, c1=(a1*a1
           T d=(pt[i]-pt[f.a]).dot((pt[f.b]-pt[ 20
431
                 f.a]).cross(pt[f.c]-pt[f.a]));
                                                           double a2=c.x-a.x, b2=c.y-a.y, c2=(a2*a2
           if(d<=0) next.push back(f);</pre>
432
                                                                +b2*b2)/2;
433
           int ff=0:
                                                    22
                                                           double d = a1*b2 - a2*b1:
           if(d>0) ff=ftop;
434
                                                    23
                                                           ret.x=a.x+(c1*b2-c2*b1)/d;
           else if(d<0) ff=-ftop;</pre>
435
                                                           ret.v=a.v+(a1*c2-a2*c1)/d:
                                                   24
            fid[f.a][f.b]=fid[f.c]=fid[f.c
436
                                                           return (Circle){ret,(ret-a).abs2()};
                                                    25
                 ][f.a]=ff;
                                                    26 }
437
                                                    27 //rand required
438
          for(auto &f:ans){
                                                    28 Circle SmallestCircle(std::vector<Circle::p>
439
           if(fid[f.a][f.b]>0 && fid[f.a][f.b
                                                             &p){
                 ]!=fid[f.b][f.a])
                                                           int n=p.size():
              next.emplace back(f.a,f.b,i);
                                                    29
                                                           if(n==1) return (Circle){p[0],0.0};
            if(fid[f.b][f.c]>0 && fid[f.b][f.c
                                                    30
                                                           if(n==2) return TwoPointCircle(p[0],p
                                                    31
                 ]!=fid[f.c][f.b])
                                                                [1]);
              next.emplace back(f.b,f.c,i);
442
                                                           random_shuffle(p.begin(),p.end());
443
            if(fid[f.c][f.a]>0 && fid[f.c][f.a
                                                   32
                                                           Circle c = \{p[0], 0.0\};
                                                    33
                 ]!=fid[f.a][f.c])
                                                           for(int i=0;i<n;++i){</pre>
              next.emplace_back(f.c,f.a,i);
                                                    34
444
                                                    35
                                                               if(c.incircle(p[i])) continue;
445
                                                    36
                                                               c=Circle{p[i],0.0};
446
          ans=next;
                                                    37
                                                               for(int j=0;j<i;++j){</pre>
447
                                                                    if(c.incircle(p[j])) continue;
                                                    38
448
                                                                    c=TwoPointCircle(p[i],p[j]);
                                                    39
     point3D<T> centroid()const{
449
                                                                   for(int k=0;k<j;++k){</pre>
                                                    40
450
       point3D<T> res(0.0.0):
                                                                        if(c.incircle(p[k]))
                                                    41
451
       T vol=0;
                                                                             continue:
       for(auto &f:ans){
452
         T tmp=pt[f.a].dot(pt[f.b].cross(pt[f.c 42
                                                                        c=outcircle(p[i],p[j],p[k]);
453
                                                    43
              1));
         res=res+(pt[f.a]+pt[f.b]+pt[f.c])*tmp;
454
                                                    45
455
         vol+=tmp;
                                                    46
                                                           return c;
456
       return res/(vol*4);
457
458
459 };
```

## 1.2 SmallestCircle.cpp

```
1 #include "Geometry.cpp"
2 struct Circle{
       typedef point<double> p;
       typedef const point < double > cp;
      p x;
      bool incircle(cp &c)const{return (x-c).
           abs2()<=r2;}
8 };
  Circle TwoPointCircle(Circle::cp &a, Circle
       ::cp &b) {
       Circle::p m=(a+b)/2;
       return (Circle){m,(a-m).abs2()};
12
```

## 1.3 最近點對.cpp

```
1 template < typename IT = point < T > * >
2 T cloest_pair(_IT L, _IT R){
    if(R-L <= 1) return INF;</pre>
     IT mid = L+(R-L)/2;
     T x = mid -> x;
     T d = min(cloest pair(L,mid),cloest pair(
          mid,R));
     inplace merge(L, mid, R, ycmp);
     static vector<point> b; b.clear();
     for(auto u=L;u<R;++u){</pre>
10
       if((u->x-x)*(u->x-x)>=d) continue;
       for(auto v=b.rbegin();v!=b.rend();++v){
12
        T dx=u->x-v->x, dy=u->y-v->y;
         if(dy*dy>=d) break;
13
14
         d=min(d,dx*dx+dy*dy);
15
       b.push back(*u);
```

```
return d;
19
20 T closest pair(vector<point<T>> &v){
    sort(v.begin(),v.end(),xcmp);
21
    return closest pair(v.begin(), v.end());
```

1 const int MAXN=4100, MAXM=1030, MAXND=16390;

**int** n,m,sz,ansd;//高是n · 寬是m的稀疏矩陣

38

41

43

44

46

47

48

49

51

## Data Structure

## 2.1 DLX.cpp

int S[MAXM],H[MAXN];

2 struct DLX{

31

```
int row[MAXND], col[MAXND]; //每個節點代表的
    int L[MAXND],R[MAXND],U[MAXND],D[MAXND];
    vector<int> ans,anst;
    void init(int _n,int _m){
                                               61
      n = n, m = m;
                                               62
      for(int i=0;i<=m;++i){</pre>
10
                                               63
11
        U[i]=D[i]=i,L[i]=i-1,R[i]=i+1;
                                               64
12
        S[i]=0;
                                               65
13
                                               66
14
      R[m]=0,L[0]=m;
                                               67
15
      sz=m, ansd=INT MAX; //ansd 存 最 優 解 的 個 數
                                               68
16
      for(int i=1;i<=n;++i)H[i]=-1;</pre>
                                               69
17
                                               70
    void add(int r,int c){
                                               71
      ++S[col[++sz]=c];
20
      row[sz]=r;
                                               73
      D[sz]=D[c],U[D[c]]=sz,U[sz]=c,D[c]=sz;
                                               74
      if(H[r]<0)H[r]=L[sz]=R[sz]=sz;
      else R[sz]=R[H[r]],L[R[H[r]]]=sz,L[sz]=H
23
           [r],R[H[r]]=sz;
                                               77
24
25
    #define DFOR(i,A,s) for(int i=A[s];i!=s;i=
         A[i])
    void remove(int c){//刪除第c行和所有當前覆
                                               81
         蓋到第c行的列
27
      L[R[c]]=L[c],R[L[c]]=R[c];//這裡刪除第c
           行,若有些行不需要處理可以在開始時呼 84
      DFOR(i,D,c)DFOR(j,R,i){U[D[j]]=U[j],D[U[
28
           j]]=D[j],--S[col[j]];}
                                               89
    void restore(int c){//恢復第c行和所有當前
30
          覆蓋到第c行的列,remove的逆操作
      DFOR(i,U,c)DFOR(j,L,i)\{++S[col[j]],U[D[j]\}\}
           ]]=i,D[U[i]]=i;}
      L[R[c]]=c,R[L[c]]=c;
33
    void remove2(int nd){//刪除nd所在的行當前
34
         所有點(包括虛擬節點),只保留nd
      DFOR(i,D,nd)L[R[i]]=L[i],R[L[i]]=R[i];
```

```
void restore2(int nd){//刪除nd所在的行當前
         所有點,為remove2的逆操作
      DFOR(i,U,nd)L[R[i]]=R[L[i]]=i;
39
40
    bool vis[MAXM];
    int h(){//估價函數 for IDA*
      int res=0:
      memset(vis,0,sizeof(vis));
      DFOR(i,R,0)if(!vis[i]){
        vis[i]=1;
        DFOR(j,D,i)DFOR(k,R,j)vis[col[k]]=1;
      return res;
50
    bool dfs(int d){//for精確覆蓋問題
      if(d+h()>=ansd)return 0;//找最佳解用,找
           任意解可以刪掉
      if(!R[0]){ansd=d;return 1;}
      int c=R[0];
      DFOR(i,R,0)if(S[i]<S[c])c=i;</pre>
      remove(c);
      DFOR(i,D,c){
        ans.push_back(row[i]);
        DFOR(j,R,i)remove(col[j]);
        if(dfs(d+1))return 1;
        ans.pop_back();
        DFOR(j,L,i)restore(col[j]);
      restore(c);
      return 0;
    void dfs2(int d){//for最小重複覆蓋問題
      if(d+h()>=ansd)return;
      if(!R[0]){ansd=d;ans=anst;return;}
      int c=R[0];
      DFOR(i,R,0)if(S[i]<S[c])c=i;</pre>
      DFOR(i,D,c){
        anst.push_back(row[i]);
        remove2(i);
        DFOR(j,R,i)remove2(j),--S[col[j]];
        dfs2(d+1);
        anst.pop back();
        DFOR(j,L,i)restore2(j),++S[col[j]];
        restore2(i);
    bool exact cover(){//解精確覆蓋問題
      return ans.clear(), dfs(0);
    void min cover() { // 解最小重複覆蓋問題
      anst.clear();//暫存用,答案還是存在ans裡
      dfs2(0);
    #undef DFOR
90 };
```

### 2.2 Dynamic KD tree.cpp

1 template < typename T, size t kd>//有kd個維度 2 struct kd tree{

```
struct point{
                                                       void flatten(node *u, typename std::vector< 120|</pre>
                                                                                                          void nearest(node *u,int k,const point &x, 179
                                                                                                                                                              pQ=std::priority queue<std::pair<T,point
                                                            node*>::iterator &it){
                                                                                                               T *h,T &mndist){
       T d[kd];
                                                                                                                                                                    > >();
       T dist(const point &x)const{
                                                         if(!u)return;
                                                                                                            if(u==0||heuristic(h)>=mndist)return;
                                                  62
                                                                                                                                                              return mndist://回傳離x第k近的點的距離
                                                                                                                                                       180
                                                                                                            T dist=u->pid.dist(x),old=h[k];
                                                         flatten(u->1,it);
                                                                                                    122
                                                                                                                                                       181
         for(size t i=0;i<kd;++i)ret+=std::abs(</pre>
                                                         *it=u;
                                                                                                    123
                                                                                                            /*mndist=std::min(mndist,dist);*/
                                                  64
                                                                                                                                                       182
                                                                                                                                                            const std::vector<point> &range(const
              d[i]-x.d[i]);
                                                         flatten(u->r,++it);
                                                                                                            if(dist<mndist){</pre>
                                                                                                    124
                                                                                                                                                                 point&mi,const point&ma){
         return ret:
                                                  66
                                                                                                    125
                                                                                                              pO.push(std::make pair(dist.u->pid));
                                                                                                                                                      183
                                                                                                                                                               in range.clear();
                                                        void rebuild(node*&u,int k){
                                                                                                    126
                                                                                                              if((int)p0.size()==qM+1)
                                                  67
                                                                                                                                                              range(root,0,mi,ma);
                                                                                                                                                       184
       bool operator == (const point &p){
                                                                                                                mndist=pQ.top().first,pQ.pop();
                                                         if((int)A.size()<u->s)A.resize(u->s);
                                                                                                    127
                                                                                                                                                               return in_range;//回傳介於mi到ma之間的點
                                                                                                                                                       185
         for(size t i=0;i<kd;++i)</pre>
                                                         typename std::vector<node*>::iterator it 128
12
           if(d[i]!=p.d[i])return 0;
                                                              =A.begin();
                                                                                                    129
                                                                                                            if(x.d[k]<u->pid.d[k]){
                                                                                                                                                       186
13
         return 1:
                                                         flatten(u.it):
                                                                                                              nearest(u->1.(k+1)%kd.x.h.mndist);
                                                  70
                                                                                                    130
                                                                                                                                                            int size(){return root?root->s:0;}
                                                                                                                                                       187
                                                         u=build(k,0,u->s-1);
                                                                                                              h[k]=std::abs(x.d[k]-u->pid.d[k]);
14
                                                  71
                                                                                                    131
                                                                                                                                                       188 };
       bool operator<(const point &b)const{</pre>
15
                                                  72
                                                                                                    132
                                                                                                              nearest(u->r,(k+1)%kd,x,h,mndist):
16
         return d[0]<b.d[0];</pre>
                                                       bool insert(node*&u,int k,const point &x,
                                                                                                    133
17
                                                            int dep){
                                                                                                    134
                                                                                                              nearest(u->r,(k+1)%kd,x,h,mndist);
                                                  74
                                                         if(!u) return u=new node(x), dep<=0;</pre>
                                                                                                              h[k]=std::abs(x.d[k]-u->pid.d[k]);
18
    };
                                                                                                    135
                                                                                                                                                          2.3 kd tree replace segment tr
                                                  75
                                                                                                              nearest(u->1,(k+1)%kd,x,h,mndist);
19
   private:
                                                         ++u->s;
                                                                                                    136
    struct node{
                                                  76
                                                         cmp.sort id=k;
20
                                                                                                    137
       node *1,*r;
                                                         if(insert(cmp(x,u->pid)?u->l:u->r,(k+1)% 138
                                                                                                            h[k]=old;
22
       point pid;
                                                              kd,x,dep-1)){
                                                                                                    139
                                                                                                                                                        1 /*kd樹代替高維線段樹*/
                                                           if(!isbad(u))return 1;
                                                                                                          std::vector<point>in range;
23
       int s:
                                                                                                    140
                                                                                                                                                          struct node{
       node(const point &p):1(0),r(0),pid(p),s
                                                  79
                                                           rebuild(u,k);
                                                                                                    141
                                                                                                          void range(node *u.int k.const point&mi.
                                                                                                                                                            node *1.*r:
                                                                                                               const point&ma){
                                                                                                                                                            point pid, mi, ma;
       ~node(){delete l,delete r;}
                                                                                                            if(!u)return:
25
                                                  81
                                                         return 0;
                                                                                                    142
                                                                                                                                                            int s;
                                                                                                            bool is=1:
26
       void up()\{s=(1?1->s:0)+1+(r?r->s:0);\}
                                                                                                    143
                                                  82
                                                                                                                                                            int data:
     }*root;
                                                  83
                                                       node *findmin(node*o,int k){
                                                                                                            for(int i=0;i<kd;++i)</pre>
27
                                                                                                    144
                                                                                                                                                            node(const point &p,int d):1(0),r(0),pid(p
     const double alpha,loga;
                                                  84
                                                         if(!o)return 0:
                                                                                                              if(u->pid.d[i]<mi.d[i]||ma.d[i]<u->pid
                                                                                                    145
                                                                                                                                                                  ), mi(p), ma(p), s(1), data(d), dmin(d),
                                                         if(cmp.sort_id==k)return o->l?findmin(o
                                                                                                                   .d[i]){
29
     const T INF;//記得要給INF,表示極大值
                                                                                                                                                                 dmax(d){}
                                                              ->1,(k+1)%kd):o;
                                                                                                                is=0;break;
     int maxn:
                                                                                                    146
                                                                                                                                                            void up(){
                                                  86
                                                         node *l=findmin(o->l,(k+1)%kd);
                                                                                                    147
     struct cmp{
                                                                                                                                                              mi=ma=pid;
                                                         node *r=findmin(o->r,(k+1)%kd);
                                                                                                    148
                                                                                                            if(is)in_range.push_back(u->pid);
       int sort id;
                                                         if(1&&!r)return cmp(1,o)?1:o;
                                                                                                    149
                                                                                                            if(mi.d[k] <= u - > pid.d[k]) range(u - > 1,(k+1))
       bool operator()(const node*x,const node*
                                                                                                                                                               if(1){
                                                         if(!1&&r)return cmp(r,o)?r:o;
                                                                                                                 %kd,mi,ma);
                                                                                                                                                                 for(int i=0;i<kd;++i){</pre>
                                                         if(!1&&!r)return o;
                                                                                                            if(ma.d[k]>=u->pid.d[k])range(u->r,(k+1)
                                                                                                    150
34
         return operator()(x->pid,y->pid);
                                                                                                                                                                  mi.d[i]=min(mi.d[i],1->mi.d[i]);
                                                         if(cmp(1,r))return cmp(1,0)?1:0;
                                                                                                                 %kd,mi,ma);
                                                  91
35
                                                                                                                                                                  ma.d[i]=max(ma.d[i],l->ma.d[i]);
                                                                                                                                                       14
                                                  92
                                                         return cmp(r,o)?r:o;
36
       bool operator()(const point &x,const
                                                                                                    151
                                                                                                                                                       15
                                                                                                    152 public:
            point &v)const{
                                                  93
                                                                                                                                                                s+=1->s;
                                                                                                                                                       16
                                                  94
                                                       bool erase(node *&u,int k,const point &x){ 153
                                                                                                         kd tree(const T &INF, double a=0.75):root
         if(x.d[sort id]!=y.d[sort id])
                                                  95
                                                         if(!u)return 0;
                                                                                                               (0),alpha(a),loga(log2(1.0/a)),INF(INF
           return x.d[sort id]<y.d[sort id];</pre>
                                                                                                                                                               if(r){
                                                  96
                                                         if(u->pid==x){
                                                                                                               ),maxn(1){}
         for(size t i=0;i<kd;++i)</pre>
                                                                                                                                                       19
                                                                                                                                                                 for(int i=0;i<kd;++i){</pre>
                                                           if(u->r);
                                                                                                          ~kd tree(){delete root;}
           if(x.d[i]!=y.d[i])return x.d[i]<y.d[</pre>
                                                                                                    154
                                                                                                                                                                  mi.d[i]=min(mi.d[i],r->mi.d[i]);
                                                                                                                                                       20
                                                           else if(u->1) u->r=u->1, u->1=0;
                                                                                                          void clear(){delete root,root=0,maxn=1;}
                                                  98
                i];
                                                                                                                                                                  ma.d[i]=max(ma.d[i],r->ma.d[i]);
                                                                                                                                                       21
                                                  99
                                                           else{
                                                                                                          void build(int n,const point *p){
                                                                                                    156
         return 0;
                                                                                                                                                       22
                                                                                                            delete root, A.resize(maxn=n);
                                                 100
                                                              delete u;
                                                                                                    157
42
                                                                                                                                                       23
                                                                                                                                                                s+=r->s;
                                                                                                            for(int i=0;i<n;++i)A[i]=new node(p[i]);</pre>
                                                 101
                                                              return u=0, 1;
                                                                                                    158
43
     }cmp;
                                                                                                                                                       24
                                                 102
                                                                                                    159
                                                                                                            root=build(0,0,n-1);
     int size(node *o){return o?o->s:0;}
                                                                                                                                                       25
                                                 103
                                                           --u->s;
                                                                                                    160
     std::vector<node*> A;
                                                                                                                                                       26
                                                                                                                                                            void up2(){
                                                           cmp.sort id=k;
                                                                                                          void insert(const point &x){
    node* build(int k,int l,int r){
                                                 104
                                                                                                                                                              //其他懶惰標記向上更新
                                                           u->pid=findmin(u->r,(k+1)%kd)->pid;
                                                                                                            insert(root,0,x,__lg(size(root))/loga);
       if(1>r) return 0;
                                                 105
                                                                                                    162
                                                           return erase(u->r,(k+1)%kd,u->pid);
                                                                                                            if(root->s>maxn)maxn=root->s;
       if(k==kd) k=0;
                                                 106
                                                                                                    163
                                                                                                                                                            void down(){
                                                 107
                                                                                                    164
49
       int mid=(1+r)/2;
                                                                                                                                                              //其他懶惰標記下推
                                                                                                                                                       30
                                                                                                          bool erase(const point &p){
       cmp.sort id = k;
                                                 108
                                                         cmp.sort id=k:
                                                                                                                                                       31
       std::nth_element(A.begin()+1,A.begin()+
                                                         if(erase(cmp(x,u->pid)?u->l:u->r,(k+1)%
                                                                                                            bool d=erase(root,0,p);
                                                                                                                                                          }*root;
                                                              kd,x))
                                                                                                    167
                                                                                                            if(root&&root->s<alpha*maxn)rebuild();</pre>
            mid, A. begin()+r+1, cmp);
                                                            return --u->s, 1;
                                                                                                            return d;
                                                 110
                                                                                                    168
       node *ret=A[mid];
                                                                                                                                                           /*檢查區間包含用的函數*/
                                                 111
                                                         return 0;
                                                                                                    169
       ret \rightarrow l = build(k+1,l,mid-1):
                                                                                                                                                          inline bool range include(node *o,const
                                                                                                          void rebuild(){
                                                 112
                                                                                                    170
       ret->r = build(k+1,mid+1,r);
                                                                                                                                                               point &L, const point &R){
                                                       T heuristic(const T h[])const{
                                                                                                            if(root)rebuild(root,0);
       ret->up();
                                                                                                                                                            for(int i=0;i<kd;++i){</pre>
                                                                                                            maxn=root->s:
56
       return ret:
                                                                                                                                                              if(L.d[i]>o->ma.d[i]||R.d[i]<o->mi.d[i])
                                                         for(size t i=0;i<kd;++i)ret+=h[i];</pre>
57
                                                                                                    173
                                                                                                                                                                   return 0:
    bool isbad(node*o){
                                                 116
                                                         return ret;
                                                                                                    174
                                                                                                          T nearest(const point &x,int k){
                                                                                                                                                            }//只要(L,R)區間有和o的區間有交集就回傳
                                                                                                    175
       return size(o->1)>alpha*o->s||size(o->r) 117
                                                                                                            T mndist=INF,h[kd]={};
                                                                                                    176
                                                                                                                                                                 true
            >alpha*o->s;
                                                       std::priority_queue<std::pair<T,point > >
                                                                                                            nearest(root,0,x,h,mndist);
                                                                                                                                                            return 1;
                                                                                                            mndist=pQ.top().first;
```

```
41 inline bool range in range(node *o,const
       point &L, const point &R){
    for(int i=0;i<kd;++i){</pre>
      if(L.d[i]>o->mi.d[i]||o->ma.d[i]>R.d[i])
    }//如果(L,R)區間完全包含o的區間就回傳true
45
    return 1;
46
  inline bool point_in_range(node *o,const
       point &L,const point &R){
    for(int i=0;i<kd;++i){</pre>
      if(L.d[i]>o->pid.d[i]||R.d[i]<o->pid.d[i
           ])return 0;
    }//如果(L,R)區間完全包含o->pid這個點就回傳
    return 1;
51
52
53
   /* 單 點 修 改 , 以 單 點 改 值 為 例 */
  void update(node *u,const point &x,int data,
       int k=0){
    if(!u)return:
    u->down();
    if(u->pid==x){
      u->data=data:
60
      u->up2();
      return;
61
62
63
    cmp.sort id=k;
    update(cmp(x,u->pid)?u->l:u->r,x,data,(k
         +1)%kd);
    u->up2();
66
67
   /*區間修改*/
   void update(node *o,const point &L,const
       point &R, int data){
    if(!o)return;
    o->down();
    if(range in range(o,L,R)){
      //區間懶惰標記修改
74
      o->down();
75
      return;
76
    if(point_in_range(o,L,R)){
      //這個點在(L,R)區間,但是他的左右子樹不
           一定在區間中
      //單點懶惰標記修改
80
    if(o->1&&range include(o->1,L,R))update(o
         ->1,L,R,data);
    if(o->r&&range include(o->r,L,R))update(o
         ->r,L,R,data);
    o->up2();
84
   /*區間查詢,以總和為例*/
  int query(node *o,const point &L,const point
        &R){
    if(!o)return 0;
    o->down();
    if(range_in_range(o,L,R))return o->sum;
    int ans=0;
    if(point_in_range(o,L,R))ans+=o->data;
```

#### 2.4 reference\_point.cpp

```
1 | template < typename T>
2 struct _RefC{
    T data;
    int ref;
     _RefC(const T&d=0):data(d),ref(0){}
  template<typename T>
  struct _rp{
     RefC<T> *p;
    T *operator->(){return &p->data;}
    T & operator*() { return p->data; }
    operator _RefC<T>*(){return p;}
     _rp &operator=(const _rp &t){
      if(p&&!--p->ref)delete p;
      p=t.p,p&&++p->ref;
15
      return *this;
16
17
    rp( RefC<T> *t=0):p(t){p&&++p->ref;}
    _rp(const _rp &t):p(t.p){p&&++p->ref;}
    ~ rp(){if(p&&!--p->ref)delete p;}
21 };
   template<typename T>
23 inline rp<T> new rp(const T&nd){
    return _rp<T>(new _RefC<T>(nd));
```

### 2.5 skew heap.cpp

```
node *merge(node *a,node *b){
if(!a||!b) return a?a:b;
if(b->data<a->data) swap(a,b);
swap(a->l,a->r);
a->l=merge(b,a->l);
return a;
}
```

## 2.6 undo disjoint set.cpp

```
struct DisjointSet {
    // save() is Like recursive
    // undo() is Like return
    int n, fa[MXN], sz[MXN];
    vector<pair<int*,int>> h;
    vector<int> sp;
    void init(int tn) {
        n=tn;
        for (int i=0; i<n; i++) sz[fa[i]=i]=1;</pre>
```

```
sp.clear(); h.clear();
10
11
     void assign(int *k, int v) {
12
13
       h.PB(\{k, *k\});
14
15
16
     void save() { sp.PB(SZ(h)); }
     void undo() {
17
18
       assert(!sp.empty());
       int last=sp.back(); sp.pop_back();
19
       while (SZ(h)!=last) {
20
21
         auto x=h.back(); h.pop back();
22
         *x.F=x.S;
23
24
25
     int f(int x) {
       while (fa[x]!=x) x=fa[x];
26
27
       return x;
28
     void uni(int x, int y) {
29
30
       x=f(x); y=f(y);
       if (x==y) return ;
31
32
       if (sz[x]<sz[y]) swap(x, y);</pre>
33
       assign(&sz[x], sz[x]+sz[y]);
34
       assign(&fa[y], x);
35
36 }djs;
```

## 2.7 整體二分.cpp

```
1 | void totBS(int L, int R, vector<Item> M){
2 | if(Q.empty()) return; //維護全域B陣列
3 | if(L=R) 整個例的答案=r, return;
4 | int mid = (L+R)/2;
5 | vector<Item> mL, mR;
6 | do_modify_B_with_divide(mid,M);
7 | //讓B陣列在遞迴的時候只會保留[L~mid]的資訊
8 | undo_modify_B(mid,M);
9 | totBS(L,mid,mL);
10 | totBS(mid+1,R,mR);
11 | }
```

#### 3 default

#### 3.1 debug.cpp

#### 3.2 ext.cpp

```
1 | #include < bits / extc++.h>
2 #include < ext/pd_ds/assoc_container.hpp>
3 #include < ext/pd_ds/tree_policy.hpp>
  using namespace __gnu_cxx;
  using namespace __gnu_pbds;
  template<typename T>
  using pbds set = tree<T, null type, less<T>,
       rb_tree_tag,
       tree order statistics node update>;
  template<typename T,typename U>
  using pbds map = tree<T,U,less<T>,
       rb tree tag,
       tree_order_statistics_node_update>;
10 using heap=__gnu_pbds::priority_queue<int>;
11 //s.find_by_order(1);//0 base
12 //s.order_of_key(1);
```

## 3.3 IncStack.cpp

#### 3.4 input.cpp

```
inline int read(){
   int x=0; bool f=0; char c=getchar();
   while(ch<'0'||'9'<ch)f|=ch=='-',ch=getchar();

while('0'<=ch&&ch<='9')x=x*10-'0'+ch,ch=
        getchar();
   return f?-x:x;
}</pre>
```

```
7 // #!/bin/bash
                                                               e[i^1].flow-=df;
                                                                                                                                                              memset(g,-1,sizeof(int)*((n=n)+1));
                                                  48
   // g++ -std=c++11 -02 -Wall -Wextra -Wno-
                                                  49
                                                               e[i].r-=df;
                                                                                                    36
                                                                                                                                                       17
                                                                                                                                                             e.clear();
       unused-result -DDEBUG $1 && ./a.out
                                                               e[i^1].r+=df;
                                                                                                    37
                                                                                                           int mh=n;
                                                  50
                                                                                                                                                       18
      -fsanitize=address -fsanitize=undefined
                                                  51
                                                               return df;
                                                                                                    38
                                                                                                           for(int i=cur[u]=g[u];~i;i=e[i].pre){
                                                                                                                                                            void add edge(int u,int v, T cap, T cost,
        -fsanitize=return
                                                                                                    39
                                                                                                             if(e[i].r&&d[e[i].v]<mh)mh=d[e[i].v];</pre>
                                                                                                                                                                 bool directed=false){
                                                  52
                                                  53
                                                                                                    40
                                                                                                                                                              e.push back(edge(v,g[u],cap,cost));
                                                  54
                                                                                                    41
                                                                                                           if(!--gap[d[u]])d[s]=n;
                                                                                                                                                       21
                                                                                                                                                             g[u]=e.size()-1:
                                                  55
                                                         return level[u]=0;
                                                                                                           else ++gap[d[u]=++mh];
                                                                                                                                                              e.push_back(edge(u,g[v],directed?0:cap,-
                                                                                                    42
                                                  56
                                                                                                    43
                                                                                                           return cur flow-tf;
                                                                                                                                                                  cost));
      Flow
                                                  57
                                                         dinic(int s,int t,bool clean=true){
                                                                                                                                                             g[v]=e.size()-1;
                                                                                                    44
                                                                                                                                                       23
                                                  58
                                                         if(clean){
                                                                                                    45
                                                                                                         T isap(int s,int t,bool clean=true){
                                                                                                                                                       24
                                                  59
                                                           for(size t i=0;i<e.size();++i){</pre>
                                                                                                           memset(d,0,sizeof(int)*(n+1));
                                                                                                                                                            T augment(int u, T cur flow){
                                                                                                    46
                                                                                                                                                       25
  4.1 dinic.cpp
                                                  60
                                                             e[i].flow=0;
                                                                                                           memset(gap,0,sizeof(int)*(n+1));
                                                                                                                                                              if(u==T||!cur_flow)return ans+=piS*
                                                                                                    47
                                                  61
                                                             e[i].r=e[i].cap;
                                                                                                           memcpy(cur,g,sizeof(int)*(n+1));
                                                                                                                                                                   cur flow.cur flow:
                                                  62
                                                                                                           if(clean) for(size t i=0;i<e.size();++i)</pre>
                                                                                                                                                              vis[u]=1;
1 template < typename T>
                                                  63
                                                                                                                                                              _T r=cur_flow,d;
   struct DINIC{
                                                                                                             e[i].flow=0:
                                                                                                                                                              for(int i=g[u];~i;i=e[i].pre){
                                                  64
                                                         T ans=0, mf=0:
                                                                                                    50
                                                                                                                                                       29
                                                                                                             e[i].r=e[i].cap;
    static const int MAXN=105;
                                                         while(bfs(s,t))while(mf=dfs(s,t))ans+=mf
                                                                                                                                                               if(e[i].cap&&!e[i].cost&&!vis[e[i].v])
                                                                                                    51
     static const T INF=INT MAX;
                                                                                                    52
     int n, level[MAXN], cur[MAXN];
                                                                                                                                                                  d=augment(e[i].v,min(r,e[i].cap));
                                                  66
                                                         return ans;
                                                                                                    53
                                                                                                           T max flow=0;
    struct edge{
                                                  67
                                                                                                    54
                                                                                                           for(gap[0]=n;d[s]<n;)max_flow+=dfs(s,s,t</pre>
                                                                                                                                                                  e[i].cap-=d;
                                                                                                                                                                  e[i^1].cap+=d;
       int v,pre;
                                                  68 };
                                                                                                                                                                  if(!(r-=d))break;
       T cap,flow,r:
                                                                                                    55
                                                                                                           return max flow;
                                                                                                                                                       34
       edge(int v,int pre,T cap):v(v),pre(pre),
                                                                                                    56
                                                                                                                                                       35
            cap(cap),flow(0),r(cap){}
                                                                                                                                                       36
                                                                                                         vector<int> cut e;//最小割邊集
                                                           ISAP with cut.cpp
                                                                                                                                                       37
                                                                                                                                                             return cur_flow-r;
                                                                                                         bool vis[MAXN];
     int g[MAXN];
11
                                                                                                                                                       38
                                                                                                         void dfs cut(int u){
12
     vector<edge> e;
                                                                                                                                                            bool modlabel(){
                                                                                                                                                       39
                                                                                                           vis[u]=1;//表示u屬於source的最小割集
    void init(int _n){
                                                   1 | template<typename T>
13
                                                                                                                                                       40
                                                                                                                                                              for(int u=0;u<=n;++u)dis[u]=INF;</pre>
                                                                                                           for(int i=g[u];~i;i=e[i].pre)
                                                                                                    61
                                                   2 struct ISAP{
14
       memset(g,-1,sizeof(int)*((n=_n)+1));
                                                                                                                                                       41
                                                                                                                                                              static deque<int>q;
                                                                                                             if(e[i].flow<e[i].cap&&!vis[e[i].v])</pre>
                                                                                                    62
                                                       static const int MAXN=105;
15
       e.clear();
                                                                                                                                                       42
                                                                                                                                                              dis[T]=0,q.push back(T);
                                                                                                                  dfs cut(e[i].v);
                                                       static const T INF=INT MAX;
16
                                                                                                                                                       43
                                                                                                                                                              while(q.size()){
                                                                                                    63
17
     void add edge(int u,int v,T cap,bool
                                                       int n;//點數
                                                                                                                                                       44
                                                                                                                                                               int u=q.front();q.pop_front();
                                                                                                         T min_cut(int s,int t){
          directed=false){
                                                       int d[MAXN],gap[MAXN],cur[MAXN];
                                                                                                                                                       45
                                                                                                           T ans=isap(s,t);
       e.push_back(edge(v,g[u],cap));
                                                       struct edge{
                                                                                                                                                       46
                                                                                                                                                                for(int i=g[u];~i;i=e[i].pre){
                                                                                                    66
                                                                                                           memset(vis,0,sizeof(bool)*(n+1));
                                                         int v,pre;
                                                                                                                                                                  if(e[i^1].cap&&(dt=dis[u]-e[i].cost)
19
       g[u]=e.size()-1;
                                                                                                           dfs_cut(s), cut_e.clear();
20
       e.push_back(edge(u,g[v],directed?0:cap))
                                                         T cap,flow,r;
                                                                                                                                                                       <dis[e[i].v]){
                                                                                                           for(int u=0;u<=n;++u)</pre>
                                                         edge(int v,int pre,T cap):v(v),pre(pre),
                                                                                                                                                                    if((dis[e[i].v]=dt)<=dis[q.size()?</pre>
                                                                                                             if(vis[u])for(int i=g[u];~i;i=e[i].pre
       g[v]=e.size()-1;
                                                              cap(cap),flow(0),r(cap){}
                                                                                                                                                                         q.front():S]){
21
                                                                                                                                                                      q.push_front(e[i].v);
22
                                                  11
                                                                                                               if(!vis[e[i].v])cut e.push back(i);
                                                                                                    70
                                                       int g[MAXN];
                                                                                                                                                                    }else q.push back(e[i].v);
23
     int bfs(int s,int t){
                                                  12
                                                                                                    71
                                                                                                           return ans;
       memset(level,0,sizeof(int)*(n+1));
                                                       vector<edge> e;
24
                                                  13
                                                                                                                                                       51
                                                                                                    72
       memcpy(cur,g,sizeof(int)*(n+1));
                                                       void init(int _n){
25
                                                  14
                                                                                                                                                       52
                                                                                                    73 };
       queue<int> q;
                                                  15
                                                         memset(g, -1, sizeof(int)*((n= n)+1));
                                                                                                                                                       53
26
                                                         e.clear();
                                                                                                                                                       54
                                                                                                                                                              for(int u=0;u<=n;++u)</pre>
27
       q.push(s);
                                                  16
28
       level[s]=1;
                                                  17
                                                                                                                                                                for(int i=g[u];~i;i=e[i].pre)
29
       while(q.size()){
                                                       void add_edge(int u,int v,T cap,bool
                                                                                                                                                                  e[i].cost+=dis[e[i].v]-dis[u];
                                                                                                             MinCostMaxFlow.cpp
         int u=q.front();q.pop();
                                                            directed=false){
                                                                                                                                                              return piS+=dis[S], dis[S]<INF;</pre>
30
         for(int i=g[u];~i;i=e[i].pre){
                                                         e.push_back(edge(v,g[u],cap));
32
           if(!level[e[i].v]&&e[i].r){
                                                  20
                                                         g[u]=e.size()-1;
                                                                                                                                                            T mincost(int s,int t){
                                                         e.push_back(edge(u,g[v],directed?0:cap))
                                                                                                     1 template<typename _T>
                                                                                                                                                             S=s,T=t;
33
             level[e[i].v]=level[u]+1;
                                                                                                     2 struct MCMF{
34
             q.push(e[i].v);
                                                                                                                                                             piS=ans=0;
                                                         g[v]=e.size()-1;
                                                                                                         static const int MAXN=440;
                                                                                                                                                              while(modlabel()){
             if(e[i].v==t)return 1;
                                                  22
                                                  23
                                                                                                         static const _T INF=999999999;
                                                                                                                                                               do memset(vis,0,sizeof(bool)*(n+1));
37
        }
                                                  24
                                                       T dfs(int u,int s,int t,T cur flow=INF){
                                                                                                         struct edge{
                                                                                                                                                                while(augment(S,INF));
                                                         if(u==t)return cur_flow;
38
                                                                                                           int v,pre;
                                                                                                                                                             }return ans;
       return 0;
                                                         T tf=cur flow,df;
                                                                                                           T cap,cost;
39
                                                         for(int &i=cur[u];~i;i=e[i].pre){
                                                                                                           edge(int v,int pre, T cap, T cost):v(v),
      dfs(int u,int t,T cur_flow=INF){
                                                           if(e[i].r&&d[u]==d[e[i].v]+1){
                                                                                                                pre(pre), cap(cap), cost(cost){}
42
       if(u==t)return cur flow;
                                                  29
                                                             df=dfs(e[i].v,s,t,min(tf,e[i].r));
                                                             e[i].flow+=df;
                                                                                                         int n,S,T;
44
       for(int &i=cur[u];~i;i=e[i].pre){
                                                             e[i^1].flow-=df;
                                                                                                    11
                                                                                                         _T dis[MAXN],piS,ans;
         if(level[e[i].v]==level[u]+1&&e[i].r){
                                                             e[i].r-=df;
                                                                                                         bool vis[MAXN];
           if(df=dfs(e[i].v,t,min(cur_flow,e[i
                                                             e[i^1].r+=df;
                                                                                                         vector<edge> e;
                                                             if(!(tf-=df)||d[s]==n)return
                                                                                                         int g[MAXN];
                1.r))){
                                                  34
             e[i].flow+=df;
                                                                  cur flow-tf;
                                                                                                         void init(int n){
```

## Graph

1 #define MAXN1 505

## Augmenting Path.cpp

```
2 #define MAXN2 505
3 int n1, n2; //n1 個點連向n2個點
4 | int match[MAXN2]; //屬於n2的點匹配了哪個點
5 vector<int > g[MAXN1];//

6 bool vis[MAXN2];//是否走訪過
  bool dfs(int u){
    for(size t i=0;i<g[u].size();++i){</pre>
      int v=g[u][i];
      if(vis[v])continue;
      vis[v]=1;
12
      if(match[v]==-1||dfs(match[v]))
        return match[v]=u, 1;
14
15
    return 0;
16
   inline int max match(){
    int ans=0:
    memset(match,-1,sizeof(int)*n2);
    for(int i=0;i<n1;++i){</pre>
20
21
      memset(vis,0,sizeof(bool)*n2);
      if(dfs(i))++ans;
22
23
24
    return ans:
```

## 5.2 Augmenting Path multiple.

```
1 #define MAXN1 1005
2 #define MAXN2 505
3 int n1,n2;//n1個點連向n2個點,其中n2個點可以
       匹配很多邊
4 vector<int> g[MAXN1];// \begin{align*}
5 int c[MAXN2]; // 每個屬於 n2 點 最多可以接受幾條
6 | vector<int> match list[MAXN2];//每個屬於n2的
        點匹配了那些點
7 bool vis[MAXN2];//是否走訪過
  bool dfs(int u){
    for(size_t i=0;i<g[u].size();++i){</pre>
      int v=g[u][i];
      if(vis[v])continue;
       vis[v]=true;
      if((int)match list[v].size()<c[v]){</pre>
        return match_list[v].push_back(u),
             true:
      }else{
16
         for(size_t j=0;j<match_list[v].size()</pre>
           int next_u=match_list[v][j];
18
           if(dfs(next u))
19
            return match_list[v][j]=u, true;
20
21
```

```
return false;
24
   int max match(){
     for(int i=0;i<n2;++i)match list[i].clear()</pre>
27
     int cnt=0:
28
     for(int u=0:u<n1:++u){</pre>
       memset(vis,0,sizeof(bool)*n2);
29
30
       if(dfs(u))++cnt;
31
32
     return cnt;
```

1 #define MAXN 505

4 int t.n:

vector<int>g[MAXN];

5 int lca(int x,int y){

#### blossom matching.cpp

```
for(++t;;swap(x,y)){
       if(x==0)continue;
       if(v[x]==t)return x;
       v[x]=t;
       x=st[pa[match[x]]];
11
12 }
#define qpush(x) q.push(x),S[x]=0
14 void flower(int x,int y,int l,queue<int> &q)
     while(st[x]!=1){
       pa[x]=y;
       if(S[y=match[x]]==1)qpush(y);
       st[x]=st[y]=1, x=pa[y];
19
20 | }
   bool bfs(int x){
21
     for(int i=1;i<=n;++i)st[i]=i;</pre>
     memset(S+1,-1,sizeof(int)*n);
     queue<int>q; qpush(x);
     while(q.size()){
       x=q.front(),q.pop();
       for(size_t i=0;i<g[x].size();++i){</pre>
         int y=g[x][i];
         if(S[y]==-1){
30
            pa[y]=x,S[y]=1;
31
            if(!match[y]){
32
             for(int lst;x;y=lst,x=pa[y])
                lst=match[x],match[x]=y,match[y
34
              return 1;
35
            apush(match[v]);
36
37
          }else if(!S[y]&&st[y]!=st[x]){
            int l=lca(y,x);
39
            flower(y,x,1,q),flower(x,y,1,q);
40
41
       }
     }
42
43
     return 0;
44 }
45 int blossom(){
```

```
if(!match[i]&&bfs(i))++ans;
49
     return ans;
```

#### 5.4 graphISO.cpp

for(int i=1;i<=n;++i)</pre>

int ans=0:

```
19
                                                                                                      20
                                                   1 const int MAXN=1005, K=30; // K要 夠 大
                                                                                                      21
                                                   2 const long long A=3,B=11,C=2,D=19,P=0
                                                          xdefaced;
                                                                                                      23
                                                   3 long long f[K+1][MAXN];
                                                                                                      24
                                                   4 vector<int> g[MAXN],rg[MAXN];
                                                   5 int n;
                                                                                                      25
                                                     void init(){
                                                                                                      26
                                                       for(int i=0;i<n;++i){</pre>
                                                         f[0][i]=1;
int pa[MAXN], match[MAXN], st[MAXN], S[MAXN], v[
                                                                                                      27
                                                         g[i].clear(), rg[i].clear();
                                                                                                      28
                                                  10
                                                                                                      29
                                                  11 }
                                                                                                      30
                                                     void add_edge(int u,int v){
                                                                                                      31
                                                       g[u].push_back(v), rg[v].push_back(u);
                                                  14
                                                                                                      32
                                                  15
                                                     long long point_hash(int u){//O(N)
                                                                                                      33
                                                       for(int t=1;t<=K;++t){</pre>
                                                  16
                                                                                                      34
                                                         for(int i=0;i<n;++i){</pre>
                                                  17
                                                                                                      35
                                                            f[t][i]=f[t-1][i]*A%P;
                                                  18
                                                                                                      36
                                                            for(int j:g[i])f[t][i]=(f[t][i]+f[t
                                                                                                      37
                                                                 -1][j]*B%P)%P;
                                                            for(int j:rg[i])f[t][i]=(f[t][i]+f[t
                                                                 -1][j]*C%P)%P;
                                                            if(i==u)f[t][i]+=D;//如果圖太大的話,
                                                  21
                                                                 把這行刪掉,執行一次後f[K]就會是所
                                                                                                      43
                                                            f[t][i]%=P;
                                                  22
                                                                                                      44
                                                  23
                                                                                                      45
                                                  24
                                                  ^{25}
                                                       return f[K][u];
                                                  26
                                                     vector<long long> graph_hash(){
                                                       vector<long long> ans;
                                                       for(int i=0;i<n;++i)ans.push_back(</pre>
                                                            point_hash(i));//O(N^2)
                                                                                                      52
                                                       sort(ans.begin(),ans.end());
                                                                                                      53
                                                       return ans;
                                                  31
                                                  32
```

### KM.cpp

```
1 | #define MAXN 405
2 #define INF 0x3f3f3f3f
3 int n; // 1-base · 0表示沒有匹配
4 int g[MAXN][MAXN], lx[MAXN], ly[MAXN], pa[MAXN
      ],slack y[MAXN];
int match y[MAXN], match x[MAXN];
6 bool vx[MAXN],vy[MAXN];
 void augment(int v){
    for(int x,z;y;y=z){
      x=pa[y],z=match_x[x];
```

```
for(int y=1;y<=n;++y)if(!vy[y]){</pre>
    int t=lx[x]+ly[y]-g[x][y];
    if(t==0){
      pa[y]=x;
      if(!match_y[y]){augment(y);return
      vy[y]=1,q.push(match_y[y]);
    }else if(slack_y[y]>t)pa[y]=x,
         slack y[y]=t;
int cut=INF:
for(int y=1;y<=n;++y){</pre>
 if(!vy[y]&&cut>slack y[y])cut=slack y[
      y];
for(int j=1;j<=n;++j){</pre>
 if(vx[j])1x[j]-=cut;
 if(vy[j])ly[j]+=cut;
  else slack y[j]-=cut;
```

for(int y=1;y<=n;++y){</pre>

long long KM(){

lx[x]=-INF;

long long ans=0;

return ans;

if(!vy[y]&&slack y[y]==0){

vy[y]=1,q.push(match\_y[y]);

memset(match\_y,0,sizeof(int)\*(n+1));

memset(ly,0,sizeof(int)\*(n+1));

lx[x]=max(lx[x],g[x][y]);

for(int y=1;y<=n;++y)ans+=g[match\_y[y]][y</pre>

for(int x=1;x<=n;++x){</pre>

for(int y=1;y<=n;++y)</pre>

for(int x=1;x<=n;++x)bfs(x);</pre>

if(!match\_y[y]){augment(y);return;}

match y[y]=x, match x[x]=y;

int x=q.front();q.pop();

for(int i=1;i<=n;++i)slack\_y[i]=INF,vx[i]=</pre>

void bfs(int st){

for(;;){

vy[i]=0;

while(q.size()){

queue<int> q;q.push(st);

11

12

15

16

17

18

## 5.6 MaximumClique.cpp

```
1 | struct MaxClique{
    static const int MAXN=105;
    int g[MAXN][MAXN], dp[MAXN], stk[MAXN][MAXN
```

21

22

return res;

return x.id;

```
int sol[MAXN],tmp[MAXN];//sol[0~ans-1]為答 20
     void init(int n){
       N=n;//0-base
       memset(g,0,sizeof(g));
     void add_edge(int u,int v){
       g[u][v]=g[v][u]=1;
12
     int dfs(int ns,int dep){
       if(!ns){
         if(dep>ans){
16
           ans=dep;
           memcpy(sol,tmp,sizeof tmp);
           return 1;
19
         }else return 0;
20
       for(int i=0;i<ns;++i){</pre>
         if(dep+ns-i<=ans)return 0;</pre>
22
         int u=stk[dep][i],cnt=0;
         if(dep+dp[u]<=ans)return 0;</pre>
         for(int j=i+1; j<ns; ++ j){</pre>
           int v=stk[dep][i];
           if(g[u][v])stk[dep+1][cnt++]=v;
         tmp[dep]=u;
         if(dfs(cnt,dep+1))return 1;
       return 0;
33
     int clique(){
       int u,v,ns;
       for(ans=0,u=N-1;u>=0;--u){
         for(ns=0,tmp[0]=u,v=u+1;v<N;++v)</pre>
           if(g[u][v])stk[1][ns++]=v;
         dfs(ns,1),dp[u]=ans;
40
41
       return ans:
^{42}
43 };
```

## 5.7 MinimumMeanCycle.cpp

```
1 | #include < cstdint > // for DBL MAX
2 int dp[maxN+1][maxN+1];
3 double mnc(int n){
    int u,v,w;
                                                   37
    const int inf=0x7f7f7f7f;
                                                   38
    memset(dp,0x7f,sizeof(dp));
    memset(dp[0],0,sizeof(dp[0]));
    for(int i=0;i<n;++i){</pre>
      for(auto e:E){
        tie(u,v,w)=e;
        if(dp[i][u]!=inf)
        dp[i+1][v]=min(dp[i+1][v],dp[i][u]+w); 43
      double res = DBL MAX:
      for(int i=1;i<=n;++i){</pre>
                                                   45
        double val = DBL MIN;
        for(int j=0;j<n;++j)</pre>
          val=max(val,double(dp[n][i]-dp[i][j
               1)/(n-i));
        res=min(res,val);
```

### 5.8 Rectilinear MST.cpp

```
1 / / 平面曼哈頓最小生成樹構造圖(去除非必要邊)
 2 #define T int
 3 #define INF 0x3f3f3f3f
   struct point{
    T x, y;
    int id;//從0開始編號
     point(){}
    T dist(const point &p)const{
      return abs(x-p.x)+abs(y-p.y);
11 };
12 bool cmpx(const point &a,const point &b){
    return a.x<b.x||(a.x==b.x&&a.y<b.y);
14 }
   struct edge{
    int u.v:
16
    T cost;
     edge(int u,int v,T c):u(u),v(v),cost(c){}
    bool operator<(const edge&e)const{</pre>
19
      return cost<e.cost;</pre>
20
21
22 };
23 struct bit node{
    T mi:
    int id;
     bit node(const T&mi=INF,int id=-1):mi(mi),
26
         id(id){}
27 };
28 vector<bit node> bit;
   void bit update(int i,const T&data,int id){
     for(;i;i-=i&(-i)){
      if(data<bit[i].mi)bit[i]=bit_node(data,</pre>
33 }
   int bit_find(int i,int m){
    bit node x:
     for(;i<=m;i+=i&(-i)) if(bit[i].mi<x.mi)x=</pre>
```

vector<edge> build graph(int n,point p[]){

gb=ga, sort(gb.begin(),gb.end());

for(int dir=0; dir<4; ++dir){//4種座標變換

if(dir%2) for(int i=0;i<n;++i) swap(p[i</pre>

else if(dir==2) for(int i=0;i<n;++i) p[i</pre>

vector<edge> e;//edge for MST

1.x,p[i].v);

].x=-p[i].x;

vector<T> ga(n), gb;

sort(p,p+n,cmpx);

end());

int m=gb.size();

```
1 struct Graph {
                                                // Minimum General Weighted Matching (
                                                     Perfect Match) 0-base
                                                static const int MXN = 105;
                                                int n, edge[MXN][MXN];
                                                int match[MXN], dis[MXN], onstk[MXN];
                                                vector<int> stk;
                                                void init(int n) {
                                                  for (int i=0; i<n; i++)</pre>
                                                    for (int j=0; j<n; j++)</pre>
                                                       edge[i][j] = 0;
for(int i=0;i<n;++i)ga[i]=p[i].y-p[i].x; 12</pre>
                                                void add edge(int u, int v, int w) {
                                                  edge[u][v] = edge[v][u] = w;
gb.erase(unique(gb.begin(),gb.end()),gb. 14
                                           15
                                                bool SPFA(int u){
```

```
].id,p[i].dist(p[ans])));
         bit_update(pos,p[i].x+p[i].y,i);
58
    return e;
```

int pos=lower\_bound(gb.begin(),gb.end

if(~ans)e.push\_back(edge(p[i].id,p[ans

(),ga[i])-gb.begin()+1;

bit=vector<bit node>(m+1);

int ans=bit\_find(pos,m);

for(int i=n-1;i>=0;--i){

51

52

53

57

### 5.9 treeISO.cpp

```
1 | const int MAXN=100005;
 const long long X=12327,P=0xdefaced;
 3 vector<int> g[MAXN];
 4 bool vis[MAXN];
 5 long long dfs(int u){//hash ver
    vis[u]=1;
     vector<long long> tmp;
     for(auto v:g[u])if(!vis[v])tmp.PB(dfs(v));
     if(tmp.empty())return 177;
     long long ret=4931;
     sort(tmp.begin(),tmp.end());
     for(auto v:tmp)ret=((ret*X)^v)%P;
13
    return ret:
14 }
  string dfs(int x,int p){
    vector<string> c;
     for(int y:g[x])
      if(y!=p)c.emplace_back(dfs(y,x));
     sort(c.begin(),c.end());
    string ret("(");
     for(auto &s:c)ret+=s;
23
    ret+=")";
     return ret;
```

## 5.10 一般圖最小權完美匹配.cpp

```
62
63
65 } graph;
```

# 5.11 全局最小割.cpp

if (!found) break;

for (int i=0; i<n; i++)</pre>

ret += edge[i][match[i]];

int ret = 0;

ret /= 2;

return ret:

if (onstk[u]) return true;

for (int v=0; v<n; v++){</pre>

int m = match[v];

onstk[v] = 1;

edge[u][v]){

stk.push\_back(v);

stk.pop back();

onstk[v] = 0;

for (int i=0; i<n; i+=2){</pre>

match[i] = i+1, match[i+1] = i;

for (int i=0; i<n; i++) dis[i] = onstk</pre>

int u = stk.back(); stk.pop\_back

int v = stk.back(); stk.pop\_back

edge[u][v];

if (SPFA(m)) return true;

if (u != v && match[u] != v && !onstk[

if (dis[m] > dis[u] - edge[v][m] +

dis[m] = dis[u] - edge[v][m] +

stk.push back(u);

v]){

onstk[u] = 1;

onstk[u] = 0;

return false:

int solve() {

for(;;){

stk.pop\_back();

// find a match

int found = 0;

[i] = 0;

found = 1:

stk.clear();

for (int i=0; i<n; i++){</pre>

();

match[u] = v;

match[v] = u;

if (!onstk[i] && SPFA(i)){

while (stk.size()>=2){

18

19

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

40

41

42

46

47

48

40

52

53

54

```
1 const int INF=0x3f3f3f3f;
2 template<typename T>
3 struct stoer wagner{// 0-base
    static const int MAXN=150;
   T g[MAXN][MAXN], dis[MAXN];
```

```
int nd[MAXN],n,s,t;
     void init(int n){
                                                       29
                                                       30
       for(int i=0;i<n;++i)</pre>
                                                      31
10
          for(int j=0;j<n;++j)g[i][j]=0;</pre>
                                                       32
11
                                                       33
12
     void add edge(int u.int v.T w){
                                                       34
13
       g[u][v]=g[v][u]+=w;
                                                       35
14
                                                       36
15
     T min cut(){
                                                       37
16
       T ans=INF;
                                                       38
17
       for(int i=0;i<n;++i)nd[i]=i;</pre>
       for(int ind,tn=n;tn>1;--tn){
18
                                                       39
          for(int i=1:i<tn:++i)dis[nd[i]]=0:</pre>
19
                                                       40
20
          for(int i=1;i<tn;++i){</pre>
                                                       41
21
            ind=i;
                                                       42
22
            for(int j=i;j<tn;++j){</pre>
                                                       43
              dis[nd[j]]+=g[nd[i-1]][nd[j]];
23
                                                       44
              if(dis[nd[ind]]<dis[nd[j]])ind=j;</pre>
24
                                                      45
25
                                                       46
26
            swap(nd[ind],nd[i]);
                                                       47
27
                                                       48
28
         if(ans>dis[nd[ind]])ans=dis[t=nd[ind
                                                       49
               ]],s=nd[ind-1];
                                                       50
          for(int i=0;i<tn;++i)</pre>
29
                                                       51
            g[nd[ind-1]][nd[i]]=g[nd[i]][nd[ind
                                                      52
30
                 -1]]+=g[nd[i]][nd[ind]];
                                                       53
31
32
       return ans;
33
34 };
```

## 5.12 平面圖判定.cpp

```
1 static const int MAXN = 20;
2 struct Edge{
    int u, v;
    Edge(int s, int d) : u(s), v(d) {}
5
   bool isK33(int n, int degree[]){
    int t = 0, z = 0;
    for(int i=0;i<n;++i){</pre>
       if(degree[i] == 3)++t;
       else if(degree[i] == 0)++z;
       else return false;
12
13
     return t == 6 \&\& t + z == n;
14
   bool isK5(int n, int degree[]){
    int f = 0, z = 0;
    for(int i=0;i<n;++i){</pre>
       if(degree[i] == 4)++f;
       else if(degree[i] == 0)++z;
19
       else return false;
20
^{22}
    return f == 5 \&\& f + z == n;
23
24 // it judge a given graph is Homeomorphic
       with K33 or K5
  bool isHomeomorphic(bool G[MAXN][MAXN],
        const int n){
     for(;;){
       int cnt = 0;
```

```
for(int i=0;i<n;++i){</pre>
    vector<Edge> E;
    for(int j=0;j<n&E.size()<3;++j)</pre>
      if(G[i][j] && i != j)
        E.push_back(Edge(i, j));
    if(E.size() == 1){
      G[i][E[0].v] = G[E[0].v][i] = false;
    }else if(E.size() == 2){
      G[i][E[0].v] = G[E[0].v][i] = false;
      G[i][E[1].v] = G[E[1].v][i] = false; 40
      G[E[0].v][E[1].v] = G[E[1].v][E[0].v 41
           1 = true:
      ++cnt;
 if(cnt == 0)break;
static int degree[MAXN];
fill(degree, degree + n, 0);
for(int i=0;i<n;++i){</pre>
  for(int j=i+1; j<n; ++j){</pre>
    if(!G[i][j])continue;
    ++degree[i];
    ++degree[j];
return !(isK33(n, degree) || isK5(n,
     degree));
```

## 5.13 弦圖完美消除序列.cpp

```
1 struct chordal{
     static const int MAXN=1005;
     int n;// 0-base
     vector<int>G[MAXN];
     int rank[MAXN],label[MAXN];
     bool mark[MAXN];
     void init(int _n){n=_n;
       for(int i=0;i<n;++i)G[i].clear();</pre>
10
     void add_edge(int u,int v){
11
       G[u].push back(v);
12
      G[v].push back(u);
13
     vector<int> MCS(){
14
       memset(rank,-1,sizeof(int)*n);
15
       memset(label,0,sizeof(int)*n);
16
       priority queue<pair<int,int> > pq;
17
       for(int i=0;i<n;++i)pq.push(make pair(0,</pre>
18
19
       for(int i=n-1;i>=0;--i)for(;;){
         int u=pq.top().second;pq.pop();
20
21
         if(~rank[u])continue;
         rank[u]=i:
22
         for(auto v:G[u])if(rank[v]==-1){
24
           pq.push(make pair(++label[v],v));
25
26
         break:
27
       vector<int> res(n);
       for(int i=0;i<n;++i)res[rank[i]]=i;</pre>
       return res;
```

## 5.14 最小斯坦納樹 DP.cpp

bool check(vector<int> ord){//弦圖判定

memset(mark,0,sizeof(bool)\*n);

vector<pair<int,int> > tmp;

sort(tmp.begin(),tmp.end());

int u=tmp[0].second;

for(int i=0;i<n;++i){</pre>

if(tmp.size()){

set<int> S;

mark[ord[i]]=1;

return 1;

for(int i=0;i<n;++i)rank[ord[i]]=i;</pre>

for(auto u:G[ord[i]])if(!mark[u])

for(auto v:G[u])S.insert(v);

for(size t j=1;j<tmp.size();++j)</pre>

if(!S.count(tmp[j].second))return

tmp.push back(make pair(rank[u],u));

32

33

34

35

36

37

39

42

43

44

45

46

47

48

49

50

51 };

```
1 | //n個點,其中r個要構成斯坦納樹
 2 //答案在max(dp[(1<<r)-1][k]) k=0~n-1
 3 //p表示要構成斯坦納樹的點集
 4 //0 (n^3 + n*3^r + n^2*2^r)
 5 #define REP(i,n) for(int i=0;i<(int)n;++i)</pre>
 6 const int MAXN=30, MAXM=8;// 0-base
 7 const int INF=0x3f3f3f3f;
 8 int dp[1<<MAXM][MAXN];</pre>
 9 int g[MAXN][MAXN];// 🗟
void init(){memset(g,0x3f,sizeof(g));}
void add edge(int u,int v,int w){
    g[u][v]=g[v][u]=min(g[v][u],w);
13 }
  void steiner(int n,int r,int *p){
    REP(k,n)REP(i,n)REP(j,n)
       g[i][j]=min(g[i][j],g[i][k]+g[k][j]);
     REP(i,n)g[i][i]=0;
     REP(i,r)REP(j,n)dp[1<<i][j]=g[p[i]][j];</pre>
     for(int i=1;i<(1<<r);++i){</pre>
19
20
       if(!(i&(i-1)))continue;
21
       REP(j,n)dp[i][j]=INF;
       REP(j,n){
23
         int tmp=INF:
         for(int s=i&(i-1);s;s=i&(s-1))
24
           tmp=min(tmp,dp[s][j]+dp[i^s][j]);
25
26
         REP(k,n)dp[i][k]=min(dp[i][k],g[j][k]+
              tmp);
27
    }
28
29
```

## 5.15 最小樹形圖 朱劉.cpp

```
struct zhu liu{
  static const int MAXN=110, MAXM=10005;
  struct node{
    int u,v;
    T w, tag;
    node *1.*r:
    node(int u=0,int v=0,T w=0):u(u),v(v),w(
         w), tag(0), 1(0), r(0){}
    void down(){
      w+=tag;
      if(1)1->tag+=tag:
      if(r)r->tag+=tag;
      tag=0:
  }mem[MAXM];//靜態記憶體
  node *pq[MAXN*2],*E[MAXN*2];
  int st[MAXN*2],id[MAXN*2],m;
  void init(int n){
    for(int i=1;i<=n;++i){</pre>
      pq[i]=E[i]=0, st[i]=id[i]=i;
    }m=0:
  node *merge(node *a, node *b){//skew heap
    if(!a||!b)return a?a:b;
    a->down(),b->down();
    if(b->w<a->w)return merge(b,a);
    swap(a->1,a->r);
    a->l=merge(b,a->l);
    return a;
  void add edge(int u,int v,T w){
    if(u!=v)pq[v]=merge(pq[v],&(mem[m++]=
         node(u,v,w)));
  int find(int x,int *st){
    return st[x]==x?x:st[x]=find(st[x],st);
  T build(int root, int n){
    T ans=0:int N=n.all=n:
    for(int i=1;i<=N;++i){</pre>
      if(i==root||!pq[i])continue;
      while(pq[i]){
        pq[i]->down(),E[i]=pq[i];
        pq[i]=merge(pq[i]->1,pq[i]->r);
        if(find(E[i]->u,id)!=find(i,id))
             break;
      if(find(E[i]->u,id)==find(i,id))
           continue:
      ans+=E[i]->w:
      if(find(E[i]->u,st)==find(i,st)){
        if(pq[i])pq[i]->tag-=E[i]->w;
        pq[++N]=pq[i];id[N]=N;
        for(int u=find(E[i]->u,id);u!=i;u=
             find(E[u]->u,id)){
          if(pq[u])pq[u]->tag-=E[u]->w;
          id[find(u,id)]=N;
          pq[N]=merge(pq[N],pq[u]);
        st[N]=find(i,st);
        id[find(i,id)]=N;
      }else st[find(i,st)]=find(E[i]->u,st)
           ,--all;
```

1 | template<typename T>

10

11

12

13

14

15

20

21

22

23

34

35

36

37

40

41

42

43

44

45

46

47

48

49

53

54

55

56

57

14 cnf.clear();

}else{

void add to cnf(char s,const string &p,int

if(rule.find(s)==rule.end())rule[s]=state

for(auto c:p)if(rule.find(c)==rule.end())

cnf.push\_back(CNF(left,rule[p[i]],

cnf.push back(CNF(left,rule[p[sz-2]],

rule[p[sz-1]],cost));

33 | vector<bool> neg INF[MAXN][MAXN];//如果花費

是負的可能會有無限小的情形

long cost,bool neg\_c=0){

dp[1][r][c.s]=0;

34 void relax(int 1,int r,const CNF &c,long

]||cost<dp[1][r][c.s])){

if(neg\_c||neg\_INF[1][r][c.x]){

neg\_INF[1][r][c.s]=true;

}else dp[1][r][c.s]=cost;

.cost,k==n);

for(int i=0;i<(int)tok.size();++i){</pre>

for(int r=1;r<(int)tok.size();++r){</pre>

for(int j=0;j<(int)tok.size();++j){</pre>

dp[i][j]=vector<long long>(state+1,

neg INF[i][j]=vector<bool>(state+1,

dp[k+1][r][c.y]+c.cost);

47 void cyk(const vector<int> &tok){

INT MAX);

bellman(i,i,tok.size());

for(int l=r-1;l>=0;--1){

for(int k=1;k<r;++k)</pre>

for(auto c:cnf)

bellman(l,r,tok.size());

false);

dp[i][i][tok[i]]=0;

42 void bellman(int l,int r,int n){

for(int k=1;k<=state;++k)</pre>

for(auto c:cnf)

//加入一個s -> 的文法,代價為cost

rule[c]=state++;

for(int i=0;i<sz-2;++i){</pre>

state,0));

32 vector<long long> dp[MAXN][MAXN];

**if**(p.size()==1){

int left=rule[s]:

int sz=p.size();

left=state++:

15 }

21

22

23

24

25

27

28

29

31 }

37

38

39

40

41 }

46 }

49

50

51

53

62

63 }

64 }

```
return all==1?ans:-INT MAX;//圖不連通就
62 };
```

## 5.16 穩定婚姻模板.cpp

```
1 | queue < int > 0;
2 for ( i: 所有考生 ) {
   設定在第0志願;
   Q.push(考生i);
5
6 while(Q.size()){
   當前考生=0.front();0.pop();
   while ( 此考生未分發 ) {
     指標移到下一志願:
     if (已經沒有志願 or 超出志願總數)
     計算該考生在該科系加權後的總分;
     if (不符合科系需求) continue;
12
    if (目前科系有餘額) {
      依加權後分數高低順序將考生id加入科系錄
          取名單中:
15
      break;
16
    if (目前科系已額滿) {
      if ( 此考生成績比最低分數還高 ) {
        依加權後分數高低順序將考生id加入科系
19
           錄取名單:
       Q.push(被踢出的考生);
21
22
23
24 }
```

## language

### 6.1 CNF.cpp

```
1 #define MAXN 55
  struct CNF{
    int s,x,y;//s->xy \mid s->x, if y==-1
    CNF(int s,int x,int y,int c):s(s),x(x),y(y
        ),cost(c){}
s int state; //規則數量
9 map<char, int> rule; //每個字元對應到的規則
       小寫字母為終端字符
10 vector<CNF> cnf;
  void init(){
    state=0;
    rule.clear();
```

## 7 Linear Programming

## 7.1 最大密度子圖.cpp

1 typedef double T;//POJ 3155

2 const int MAXN=105:

```
3 struct edge{
  cnf.push_back(CNF(rule[s],rule[p[0]],-1,
                                                  int u,v;
                                                   edge(int u=0,int v=0,T w=0):u(u),v(v),w(w)
                                              7 };
                                              8 vector<edge> E;
                                              9 int n,m;// 1-base
                                              10 | T de[MAXN], pv[MAXN]; // 每 個 點 的 邊 權 和 和 點 權 (
                                                     有些題目會給)
                                                void init(){
                                                  E.clear():
                                                  for(int i=1;i<=n;++i)de[i]=pv[i]=0;</pre>
                                              15
                                                void add edge(int u,int v,T w){
                                                  E.push back(edge(u,v,w));
                                                  de[u]+=w, de[v]+=w;
                                              18 }
                                              19 T U; // 二分搜的最大值
                                              20
                                                void get_U(){
if(!neg INF[1][r][c.s]&&(neg INF[1][r][c.x 21
                                                  U=0:
                                                  for(int i=1;i<=n;++i)U+=2*pv[i];</pre>
                                                   for(size_t i=0;i<E.size();++i)U+=E[i].w;</pre>
                                              25 | ISAP<T> isap;//網路流
                                              26 int s,t;//原匯點
                                                 void build(T L){
                                                  isap.init(n+2);
                                                   for(size t i=0;i<E.size();++i)</pre>
                                                    isap.add edge(E[i].u,E[i].v,E[i].w);
                                                   for(int v=1; v<=n; ++v){</pre>
    if(c.y==-1)relax(l,r,c,dp[l][r][c.x]+c
                                                    isap.add edge(s,v,U);
                                              33
                                                     isap.add edge(v,t,U+2*L-de[v]-2*pv[v]);
                                              34
                                              35 }
                                              36 int main(){
                                                   while(~scanf("%d%d",&n,&m)){
                                              37
                                              38
                                                     if(!m){
                                              39
                                                       puts("1\n1");
                                              40
                                                       continue:
                                              41
                                              42
                                                     init();
                                                     int u.v:
                                                     for(int i=0;i<m;++i){</pre>
                                              45
                                                       scanf("%d%d",&u,&v);
                                                       add edge(u,v,1);
                                              46
                                              47
                                              48
                                                     get_U();
                                                     s=n+1, t=n+2;
        if(~c.y)relax(1,r,c,dp[1][k][c.x]+
                                              50
                                                     T l=0,r=U,k=1.0/(n*n);
                                                     while(r-1>k){//二分搜最大值
                                              52
                                                      T mid=(1+r)/2;
                                                       build(mid);
                                              54
                                                       T res=(U*n-isap.isap(s,t))/2;
                                              55
                                                       if(res>0)l=mid;
                                                       else r=mid;
```

```
build(1);
       isap.min cut(s,t);
       vector<int> ans;
       for(int i=1;i<=n;++i)</pre>
         if(isap.vis[i])ans.push back(i);
       printf("%d\n",ans.size());
       for(size_t i=0;i<ans.size();++i)</pre>
         printf("%d \ n", ans[i]);
66
     return 0;
```

## Number Theory

#### 8.1 basic.cpp

```
1 template<typename T>
   void gcd(const T &a,const T &b,T &d,T &x,T &
     if(!b) d=a,x=1,y=0;
     else gcd(b,a%b,d,y,x), y-=x*(a/b);
   long long int phi[N+1];
   void phiTable(){
     for(int i=1;i<=N;i++)phi[i]=i;</pre>
     for(int i=1;i<=N;i++)for(x=i*2;x<=N;x+=i)</pre>
          phi[x]-=phi[i];
   void all_divdown(const LL &n) {// all n/x
     for(LL a=1;a<=n;a=n/(n/(a+1))){</pre>
13
      // dosomething;
14
15 }
16 const int MAXPRIME = 1000000;
  int iscom[MAXPRIME], prime[MAXPRIME],
        primecnt;
   int phi[MAXPRIME], mu[MAXPRIME];
   void sieve(void){
     memset(iscom,0,sizeof(iscom));
     primecnt = 0;
     phi[1] = mu[1] = 1;
     for(int i=2;i<MAXPRIME;++i) {</pre>
       if(!iscom[i]) {
         prime[primecnt++] = i;
         mu[i] = -1;
26
         phi[i] = i-1;
27
28
       for(int j=0;j<primecnt;++j) {</pre>
         int k = i * prime[j];
         if(k>=MAXPRIME) break;
         iscom[k] = prime[i];
         if(i%prime[j]==0) {
           mu[k] = 0;
           phi[k] = phi[i] * prime[j];
           break;
         } else {
           mu[k] = -mu[i];
           phi[k] = phi[i] * (prime[j]-1);
40
```

LL z = 2;

int t=a/factorial[i],j;

```
43
                                                        for(;Legendre(z,p)!=-1;++z)
                                                                                                     163
                                                                                                             return :
                                                                                                                                                         21
                                                                                                                                                                for(i=0;i<n;++i)
                                                                                                                                                                  if(!vis[j]){
                                                        LL c = modexp(z,0,p);
44
                                                  104
                                                                                                     164
                                                                                                                                                         22
   bool g test(const LL &g, const LL &p, const
                                                        LL R = modexp(n\%p,(Q+1)/2,p), t = modexp(n_{165})
                                                                                                           while(true){
                                                                                                                                                         23
                                                                                                                                                                    if(t==0)break;
        vector<LL> &v) {
                                                                                                             g2=a1.multiply(h1).substract(g1);
                                                             %p,Q,p);
                                                                                                     166
                                                                                                                                                         24
                                                                                                                                                                    --t;
     for(int i=0;i<v.size();++i)</pre>
                                                  106
                                                        int M = S;
                                                                                                     167
                                                                                                             h2=N.substract(g2.pow(2)).divide(h1);
                                                                                                                                                         25
47
       if(modexp(g,(p-1)/v[i],p)==1)
                                                  107
                                                        while(1) {
                                                                                                     168
                                                                                                             a2=g2.add(a0).divide(h2):
                                                                                                                                                         26
                                                                                                                                                                res.push back(j);
         return false;
                                                          if(t==1) return R;
                                                                                                             p=a1.multiply(p2).add(p1);
48
                                                  108
                                                                                                     169
                                                                                                                                                         27
                                                                                                                                                                vis[j]=1;
49
    return true;
                                                  109
                                                          LL b = modexp(c,1L << (M-i-1),p);
                                                                                                     170
                                                                                                             q=a1.multiply(q2).add(q1);
                                                                                                                                                         28
                                                                                                                                                                a%=factorial[i];
                                                          R = LLmul(R,b,p);
                                                                                                             if(p.pow(2).substract(N.multiply(q.pow
50
                                                  110
                                                                                                                                                         29
                                                          t = LLmul( LLmul(b,b,p), t, p);
   LL primitive root(const LL &p) {
                                                  111
                                                                                                                  (2))).compareTo(BigInteger.ONE)==0)
                                                                                                                                                         30
                                                                                                                                                              return res;
51
52
    if(p==2) return 1:
                                                  112
                                                          c = LLmul(b,b,p);
                                                                                                                  break:
     vector<LL> v;
53
                                                  113
                                                                                                     172
                                                                                                             g1=g2;h1=h2;a1=a2;
54
     Factor(p-1,v);
                                                  114
                                                                                                     173
                                                                                                             p1=p2;p2=p;
55
    v.erase(unique(v.begin(), v.end()), v.end
                                                 115
                                                        return -1;
                                                                                                     174
                                                                                                             q1=q2;q2=q;
                                                                                                                                                            8.4 FFT.cpp
                                                  116
                                                                                                     175
          ());
56
    for(LL g=2;g<p;++g)</pre>
                                                                                                     176
                                                                                                           System.out.println(p+" "+q);
                                                  117
57
      if(g_test(g,p,v))
                                                      template<typename T>
                                                                                                     177
58
         return g;
                                                      T Euler(T n){
                                                                                                                                                          1 template<typename T, typename VT=vector<
                                                  119
    puts("primitive root NOT FOUND");
59
                                                  120
                                                        T ans=n:
                                                                                                                                                                 complex<T>>>
60
    return -1;
                                                  121
                                                        for(T i=2;i*i<=n;++i){</pre>
                                                                                                                                                            struct FFT{
                                                          if(n%i==0){
61
                                                  122
                                                                                                                bit set.cpp
                                                                                                                                                              const T pi:
   int Legendre(const LL &a, const LL &p) {
                                                  123
                                                            ans=ans/i*(i-1):
                                                                                                                                                              FFT(const T pi=acos((T)-1)):pi(pi){}
       return modexp(a%p,(p-1)/2,p); }
                                                  124
                                                            while(n%i==0)n/=i;
                                                                                                                                                              unsigned bit_reverse(unsigned a,int len){
                                                                                                                                                                a=((a&0x55555555U)<<1)|((a&0xAAAAAAAAU)
                                                  125
                                                                                                       1 void sub set(int S){
   LL inv(const LL &a, const LL &n) {
                                                  126
                                                                                                                                                                     >>1);
                                                                                                           int sub=S;
    LL d,x,y;
                                                        if(n>1)ans=ans/n*(n-1);
                                                                                                                                                                a=((a&0x33333333U)<<2)|((a&0xCCCCCCCU)
65
                                                  127
                                                                                                           do{
                                                        return ans:
    gcd(a,n,d,x,y);
                                                  128
                                                                                                                                                                     >>2);
                                                                                                             //對某集合的子集合的處理
    return d==1 ? (x+n)%n : -1;
                                                  129 }
                                                                                                                                                                a = ((a\&0x0F0F0F0FU) < <4) | ((a\&0xF0F0F0F0U)
                                                                                                             sub=(sub-1)&S:
68
                                                  130
                                                                                                           }while(sub!=S);
                                                  131
                                                      //Chinese remainder theorem
                                                                                                                                                                a=((a&0x00FF00FFU)<<8)|((a&0xFF00FF00U)
69
   int inv[maxN];
                                                      template<typename T>
                                                                                                         void k sub set(int k,int n){
   LL invtable(int n,LL P){
                                                  133 T pow mod(T n,T k,T m){
                                                                                                                                                                a=((a&0x0000FFFFU)<<16)|((a&0xFFFF0000U)
                                                                                                           int comb=(1<<k)-1,S=1<<n;</pre>
72
    inv[1]=1;
                                                  134
                                                        T ans=1:
                                                                                                                                                                     >>16);
                                                                                                           while(comb<S){</pre>
    for(int i=2;i<n;++i)</pre>
                                                        for(n=(n)=m?n\%m:n);k;k>>=1){
                                                                                                                                                                return a>>(32-len);
                                                  135
                                                                                                                                                         11
                                                                                                             //對大小為k的子集合的處理
       inv[i]=(P-(P/i))*inv[P%i]%P;
                                                         if(k&1)ans=ans*n%m;
74
                                                  136
                                                                                                                                                         12
                                                                                                             int x=comb&-comb.v=comb+x;
                                                                                                                                                              void fft(bool is_inv,VT &in,VT &out,int N)
75
                                                         n=n*n%m;
                                                                                                                                                         13
                                                  137
                                                                                                             comb = ((comb\&\sim y)/x>>1)|y;
                                                                                                      13
76
                                                  138
                                                                                                      14
   LL log mod(const LL &a, const LL &b, const
                                                        return ans;
                                                                                                                                                                int bitlen=__lg(N),num=is_inv?-1:1;
                                                  139
                                                                                                                                                         14
                                                                                                      15 }
                                                                                                                                                                for(int i=0;i<N;++i)out[bit_reverse(i,</pre>
       LL &p) {
                                                  140 }
                                                                                                                                                         15
                                                      template<typename T>
     // a ^ x = b \pmod{p}
                                                                                                                                                                     bitlen) | = in[i];
                                                      T crt(vector<T> &m, vector<T> &a){
                                                                                                                                                                for(int step=2;step<=N;step<<=1){</pre>
    int m=sqrt(p+.5), e=1;
    LL v=inv(modexp(a,m,p), p);
                                                                                                                                                                  const int mh=step>>1;
                                                        T M=1,tM,ans=0;
                                                                                                         8.3 cantor expansion.cpp
    map<LL,int> x;
                                                        for(int i=0;i<(int)m.size();++i)M*=m[i];</pre>
                                                                                                                                                                  for(int i=0;i<mh;++i){</pre>
                                                  144
                                                                                                                                                         18
                                                        for(int i=0;i<(int)a.size();++i){</pre>
                                                                                                                                                                    complex<T> wi=exp(complex<T>(0,i*num
82
    x[1]=0;
                                                  145
                                                                                                                                                         19
     for(int i=1;i<m;++i) {</pre>
                                                  146
                                                          tM=M/m[i];
                                                                                                                                                                         *pi/mh));
                                                          ans=(ans+(a[i]*tM%M)*pow mod(tM,Euler(m[
                                                                                                       1 int factorial[MAXN];
                                                                                                                                                                    for(int j=i;j<N;j+=step){</pre>
       e = LLmul(e,a,p);
                                                  147
                                                                                                                                                         20
       if(!x.count(e)) x[e] = i;
                                                                                                       void init(){
                                                                                                                                                                      int k=j+mh;
                                                               i])-1,m[i])%M)%M;
                                                                                                                                                         21
                                                          /*如果m[i]是質數·Euler(m[i])-1=m[i]-2·
                                                                                                           factorial[0]=1;
                                                                                                                                                                      complex<T> u=out[j],t=wi*out[k];
                                                  148
                                                                                                           for(int i=1;i<=MAXN;++i)factorial[i]=</pre>
     for(int i=0;i<m;++i) {</pre>
                                                                                                                                                         23
                                                                                                                                                                      out[j]=u+t;
                                                               就不用算Euler了*/
      if(x.count(b)) return i*m + x[b];
                                                                                                                factorial[i-1]*i;
                                                                                                                                                         ^{24}
                                                                                                                                                                      out[k]=u-t;
                                                  149
       b = LLmul(b,v,p);
                                                                                                                                                         25
                                                  150
                                                        return ans;
90
    }
                                                                                                         int encode(const vector<int> &s){
                                                                                                                                                         26
                                                  151
     return -1;
                                                                                                           int n=s.size(),res=0;
                                                                                                                                                         27
                                                  152
92
                                                                                                           for(int i=0;i<n;++i){</pre>
                                                                                                                                                         28
                                                                                                                                                                if(is inv)for(int i=0;i<N;++i)out[i]/=N;</pre>
                                                  153 //java code
                                                                                                                                                         29
                                                                                                             int t=0;
                                                  154 / / 求 sart (N) 的 連 分 數
                                                                                                                                                         30 };
   LL Tonelli Shanks(const LL &n, const LL &p)
                                                                                                             for(int j=i+1; j<n;++j)</pre>
                                                  155 public static void Pell(int n){
                                                                                                               if(s[j]<s[i])++t;
                                                       BigInteger N,p1,p2,q1,q2,a0,a1,a2,g1,g2,h1
    // x^2 = n \pmod{p}
                                                                                                             res+=t*factorial[n-i-1];
                                                             ,h2,p,q;
    if(n==0) return 0;
                                                        g1=q2=p1=BigInteger.ZERO;
                                                                                                                                                            8.5 find real root.cpp
    if(Legendre(n,p)!=1) while(1) { puts("SQRT
                                                                                                      14
                                                                                                           return res;
                                                        h1=q1=p2=BigInteger.ONE;
           ROOT does not exist"); }
                                                                                                      15
                                                        a0=a1=BigInteger.valueOf((int)Math.sqrt
    int S = 0:
                                                                                                         vector<int> decode(int a,int n){
                                                             (1.0*n);
    LL 0 = p-1;
                                                                                                           vector<int> res;
                                                                                                                                                          1 / / an*x^n + ... + a1x + a0 = 0;
                                                        BigInteger ans=a0.multiply(a0);
    while( !(Q&1) ) { Q>>=1; ++S; }
                                                                                                           vector<bool> vis(n,0);
                                                                                                                                                          2 int sign(double x){
                                                        if(ans.equals(BigInteger.valueOf(n))){
    if(S==1) return modexp(n\%p,(p+1)/4,p);
                                                                                                           for(int i=n-1;i>=0;--i){
                                                                                                                                                             return x \leftarrow -eps ? -1 : x > eps;
```

162

System.out.println("No solution!");

```
double get(const vector<double>&coef, double
     double e = 1, s = 0;
    for(auto i : coef) s += i*e, e *= x;
    return s:
10
11
   double find(const vector<double>&coef, int n
        , double lo, double hi){
     double sign lo, sign hi;
    if( !(sign_lo = sign(get(coef,lo))) )
14
          return lo:
     if( !(sign_hi = sign(get(coef,hi))) )
          return hi;
     if(sign lo * sign hi > 0) return INF;
     for(int stp = 0; stp < 100 && hi - lo >
17
          eps; ++stp){
       double m = (lo+hi)/2.0;
       int sign_mid = sign(get(coef,m));
19
20
       if(!sign mid) return m;
21
       if(sign lo*sign mid < 0) hi = m;</pre>
       else lo = m;
22
23
24
    return (lo+hi)/2.0;
25
26
   vector<double> cal(vector<double>coef, int n
     vector<double>res:
    if(n == 1){
29
       if(sign(coef[1])) res.pb(-coef[0]/coef
30
            [1]);
       return res;
31
32
33
     vector<double>dcoef(n);
     for(int i = 0; i < n; ++i) dcoef[i] = coef</pre>
          [i+1]*(i+1):
     vector<double>droot = cal(dcoef, n-1);
35
    droot.insert(droot.begin(), -INF);
36
    droot.pb(INF);
37
    for(int i = 0; i+1 < droot.size(); ++i){</pre>
                                                  11
       double tmp = find(coef, n, droot[i],
39
            droot[i+1]);
       if(tmp < INF) res.pb(tmp);</pre>
42
     return res;
                                                  14
   int main () {
    vector<double>ve;
    vector<double>ans = cal(ve, n);
    // 視情況把答案 +eps, 避免 -0
48
49 }
```

```
f[j+k+(1<<i)] += f[j+k]*(inverse)
                 ?-1:1);
     return f;
   vector<int> rev(vector<int> A) {
     for(int i=0; i<A.size(); i+=2)</pre>
       swap(A[i],A[i^(A.size()-1)]);
     return A;
11
12 }
13 vector<int> F_AND_T(vector<int> f, bool
        inverse){
     return rev(F OR T(rev(f), inverse));
15 }
16 vector<int> F XOR T(vector<int> f, bool
        inverse){
      for(int i=0; (2<<i)<=f.size(); ++i)</pre>
17
       for(int j=0; j<f.size(); j+=2<<i)</pre>
18
          for(int k=0; k<(1<<i); ++k){</pre>
19
            int u=f[j+k], v=f[j+k+(1<<i)];</pre>
20
            f[j+k+(1<<i)] = u-v, f[j+k] = u+v;
21
22
     if(inverse) for(auto &a:f) a/=f.size();
23
     return f:
```

#### 8.7 LinearCongruence.cpp

```
1 | pair<LL,LL> LinearCongruence(LL a[],LL b[],
        LL m[], int n) {
     // a[i]*x = b[i] \pmod{m[i]}
     for(int i=0;i<n;++i) {</pre>
      LL x, y, d = extgcd(a[i],m[i],x,y);
       if(b[i]%d!=0) return make pair(-1LL,0LL)
       m[i] /= d;
      b[i] = LLmul(b[i]/d,x,m[i]);
    LL lastb = b[0], lastm = m[0];
     for(int i=1;i<n;++i) {</pre>
      LL x, y, d = extgcd(m[i],lastm,x,y);
       if((lastb-b[i])%d!=0) return make pair
            (-1LL,0LL);
       lastb = LLmul((lastb-b[i])/d,x,(lastm/d)
           )*m[i];
      lastm = (lastm/d)*m[i];
      lastb = (lastb+b[i])%lastm;
15
16
    return make_pair(lastb<0?lastb+lastm:lastb</pre>
17
          ,lastm);
```

## 8.8 Lucas.cpp

```
1 int mod fact(int n,int &e){
   e=0:
    if(n==0)return 1;
   int res=mod fact(n/P,e);
   if((n/P)%2==0)return res*fact[n%P]%P;
   return res*(P-fact[n%P])%P;
```

```
int Cmod(int n,int m){
    int a1,a2,a3,e1,e2,e3;
    a1=mod fact(n,e1);
12
    a2=mod fact(m,e2);
    a3=mod fact(n-m,e3);
14
    if(e1>e2+e3)return 0:
    return a1*inv(a2*a3%P,P)%P;
15
```

### Matrix.cpp

using rt = std::vector<T>;

using matrix = Matrix<T>;

using mt = std::vector<rt>;

1 template < typename T>

2 struct Matrix{

int r,c;

mt m:

10

11

12

13

14

15

16

18

19

20

22

23

24

26

27

28

29

30

31

32

33

34

35

39

40

41

42

47

50

21

```
rt& operator[](int i){return m[i];}
matrix operator+(const matrix &a){
  matrix rev(r,c);
  for(int i=0;i<r;++i)</pre>
    for(int j=0;j<c;++j)</pre>
      rev[i][j]=m[i][j]+a.m[i][j];
  return rev;
matrix operator-(const matrix &a){
  matrix rev(r,c);
  for(int i=0;i<r;++i)</pre>
    for(int j=0;j<c;++j)</pre>
      rev[i][j]=m[i][j]-a.m[i][j];
  return rev;
matrix operator*(const matrix &a){
  matrix rev(r,a.c);
  matrix tmp(a.c,a.r);
  for(int i=0;i<a.r;++i)</pre>
    for(int j=0;j<a.c;++j)</pre>
      tmp[j][i]=a.m[i][j];
  for(int i=0;i<r;++i)</pre>
    for(int j=0;j<a.c;++j)</pre>
      for(int k=0;k<c;++k)</pre>
        rev.m[i][j]+=m[i][k]*tmp[j][k];
  return rev;
bool inverse(){
  Matrix t(r,r+c);
  for(int y=0;y<r;y++){</pre>
    t.m[y][c+y] = 1;
    for(int x=0;x<c;++x)
      t.m[y][x]=m[y][x];
  if(!t.gas())
    return false;
  for(int y=0;y<r;y++)</pre>
    for(int x=0;x<c;++x)
      m[y][x]=t.m[y][c+x]/t.m[y][y];
  return true;
  vector<T> lazy(r,1);
```

```
if(j==r)continue;
                                                58
                                                            m[i].swap(m[j]);
                                                            sign=!sign;
                                                59
                                                60
                                                          for(int j=0;j<r;++j){</pre>
                                                61
                                                62
                                                            if(i==j)continue;
                                                            lazy[j]=lazy[j]*m[i][i];
                                                63
                                                64
                                                            T mx=m[j][i];
                                                            for(int k=0:k<c:++k)</pre>
                                                              m[j][k]=m[j][k]*m[i][i]-m[i][k]*mx
                                                67
                                                68
                                                69
                                                       T det=sign?-1:1;
                                                       for(int i=0;i<r;++i){</pre>
                                                70
                                                71
                                                         det = det*m[i][i];
                                                         det = det/lazy[i];
Matrix(int r,int c):r(r),c(c),m(r,rt(c)){}
                                                73
                                                         for(auto &j:m[i])j/=lazy[i];
                                                74
                                                75
                                                       return det;
                                                76
```

while(j<r&&!m[j][i])j++;</pre>

bool sign=false;

for(int i=0;i<r;++i){</pre>

if( m[i][i]==0 ){

int j=i+1;

53

54

55

56

#### 8.10 MillerRobin.cpp

```
1 | LL LLmul(LL a, LL b, const LL &mod) {
    LL ans=0:
     while(b) {
      if(b&1) {
        ans+=a;
        if(ans>=mod) ans-=mod;
      a<<=1, b>>=1;
      if(a>=mod) a-=mod;
11
    return ans;
12
   LL mod_mul(LL a,LL b,LL m){
    a\%=m,b\%=m;/* fast for m < 2^58 */
    LL y=(LL)((double)a*b/m+0.5);
    LL r=(a*b-y*m)%m;
    return r<0?r+m:r;</pre>
18
  template<typename T>
  T pow(T a,T b,T mod){//a^b\%mod}
    for(;b;a=mod mul(a,a,mod),b>>=1)
      if(b&1)ans=mod mul(ans,a,mod);
^{24}
     return ans;
25
26 int sprp[3]={2,7,61};//int範圍可解
  int llsprp
        [7]={2,325,9375,28178,450775,9780504,
28 | 1795265022};//至少unsigned Long Long範圍
  template<typename T>
  bool isprime(T n, int *sprp, int num){
    if(n==2)return 1;
```

## 8.6 FWT.cpp

```
1 vector<int> F OR T(vector<int> f, bool
       inverse){
    for(int i=0; (2<<i)<=f.size(); ++i)</pre>
      for(int j=0; j<f.size(); j+=2<<i)</pre>
         for(int k=0; k<(1<<i); ++k)</pre>
```

if(out[j+mh]<0)out[j+mh]+=P;</pre>

wi=wi\*wn%P;

37

if(\*a==1)return k>1;

int next=0;

b\*=\*a;

28

if(--n==0)return \*a<k:</pre>

for(LL b=1;b<k;++next)</pre>

```
if(n<2||n%2==0)return 0;
                                                                                                                                                                for(int i=0;i<primecnt&&prime[i]*prime[i</pre>
                                                          if(is inv){
                                                                                                           return isless(a+1,n,next);
                                                            for(int i=1;i<N/2;++i)swap(out[i],out[ 31 }</pre>
    int t=0;
                                                   40
                                                                                                                                                                      1<=n;++i) {</pre>
                                                                                                                                                                   while(n%prime[i]==0) {
    T u=n-1;
                                                                 N-i]);
                                                                                                      32 LL high_pow(LL *a, int n, LL mod){
34
                                                                                                                                                         34
                                                                                                           if(*a==1||--n==0)return *a%mod;
35
     for(;u%2==0;++t)u>>=1;
                                                   41
                                                            T invn=pow mod(N,P-2,P);
                                                                                                                                                         35
                                                                                                                                                                     v.push back(prime[i]);
     for(int i=0;i<num;++i){</pre>
                                                            for(int i=0;i<N;++i)out[i]=out[i]*invn</pre>
                                                                                                           int k=0,r=euler[mod];
                                                                                                                                                                    n/=prime[i];
36
                                                   42
                                                                                                                                                         36
                                                                                                           for(LL tma=1; tma!=pow(*a,k+r,mod);++k)
37
      T a=sprp[i]%n;
                                                                                                                                                         37
38
       if(a==0||a==1||a==n-1)continue:
                                                   43
                                                                                                      36
                                                                                                             tma=tma*(*a)%mod;
       T x=pow(a,u,n);
                                                                                                           if(isless(a+1,n,k))return pow(*a,high_pow(
                                                                                                                                                                if(n!=1) v.push_back(n);
39
                                                   44
40
       if(x==1||x==n-1)continue;
                                                   45 };
                                                                                                                a+1,n,k),mod);
       for(int j=0;j<t;++j){</pre>
                                                                                                           int tmd=high_pow(a+1,n,r), t=(tmd-k+r)%r;
41
                                                                                                                                                         41
42
         x = mod mul(x,x,n);
                                                                                                      39
                                                                                                           return pow(*a,k+t,mod);
         if(x==1)return 0:
                                                                                                      40
                                                                                                                                                            void comfactor(const LL &n, vector<LL> &v) {
43
         if(x==n-1)break;
                                                                                                      41 LL a[1000005];
                                                                                                                                                              if(n<1e9) {
44
                                                               Simpson.cpp
                                                                                                                                                         44
45
                                                                                                      42 int t.mod:
                                                                                                                                                                smallfactor(n,v):
46
       if(x==n-1)continue;
                                                                                                      43 int main(){
                                                                                                                                                         46
                                                                                                                                                                return;
47
       return 0;
                                                                                                           init euler();
                                                                                                                                                         47
                                                    1 | double simpson(double a, double b){
                                                                                                           scanf("%d",&t);
                                                                                                                                                              if(Isprime(n)) {
48
                                                                                                                                                         48
                                                        double c=a+(b-a)/2;
                                                                                                                                                                v.push_back(n);
49
    return 1;
                                                                                                      46
                                                                                                           #define n 4
                                                        return (F(a)+4*F(c)+F(b))*(b-a)/6;
                                                                                                           while(t--){
                                                                                                                                                                return;
                                                                                                      47
                                                                                                             for(int i=0;i<n;++i)scanf("%lld",&a[i]);</pre>
                                                                                                      48
                                                                                                                                                         51
                                                    5 double asr(double a, double b, double eps,
                                                                                                      49
                                                                                                             scanf("%d",&mod);
                                                           double A){
                                                                                                             printf("%lld\n", high pow(a,n, mod));
                                                                                                                                                              for(int c=3;;++c) {
                                                                                                      50
                                                                                                                                                         53
                                                        double c=a+(b-a)/2;
  8.11 NTT.cpp
                                                                                                      51
                                                                                                                                                         54
                                                                                                                                                                d = pollorrho(n,c);
                                                        double L=simpson(a,c),R=simpson(c,b);
                                                                                                      52
                                                                                                                                                         55
                                                                                                                                                                if(d!=n) break;
                                                                                                           return 0;
                                                        if( abs(L+R-A)<15*eps )</pre>
                                                                                                                                                         56
                                                          return L+R+(L+R-A)/15.0;
1 2615053605667*(2^18)+1,3
                                                                                                                                                         57
                                                                                                                                                              comfactor(d,v);
                                                        return asr(a,c,eps/2,L)+asr(c,b,eps/2,R);
2 15*(2^27)+1,31
                                                                                                                                                         58
                                                                                                                                                              comfactor(n/d,v);
3 479*(2^21)+1.3
                                                                                                                                                         59
                                                   12 double asr(double a, double b, double eps){
4 7*17*(2^23)+1,3
                                                                                                         8.14 質因數分解.cpp
                                                        return asr(a,b,eps,simpson(a,b));
5 3*3*211*(2^19)+1,5
                                                                                                                                                            void Factor(const LL &x, vector<LL> &v) {
                                                                                                                                                              LL n = x;
6 25*(2^22)+1,3
  template<typename T,typename VT=vector<T> >
                                                                                                                                                              if(n==1) { puts("Factor 1"); return; }
                                                                                                       1 | LL func(const LL n, const LL mod, const int c)
   struct NTT{
                                                                                                                                                              prefactor(n,v);
                                                                                                                                                              if(n==1) return;
    const T P,G;
                                                      8.13 外星模運算.cpp
                                                                                                           return (LLmul(n,n,mod)+c+mod)%mod;
    NTT(T p=(1<<23)*7*17+1,T g=3):P(p),G(g){}
                                                                                                                                                         66
                                                                                                                                                              comfactor(n,v);
    unsigned bit reverse(unsigned a, int len){
                                                                                                                                                              sort(v.begin(),v.end());
                                                                                                                                                         67
12
      //Look FFT.cpp
                                                    1 | //a[0]^{(a[1]^a[2]^{...})}
                                                                                                         LL pollorrho(const LL n, const int c) {//循
13
                                                    2 #define maxn 1000000
                                                                                                              環節長度
                                                                                                                                                            void AllFactor(const LL &n,vector<LL> &v) {
14
    T pow mod(T n,T k,T m){
                                                    3 int euler[maxn+5];
                                                                                                           LL a=1, b=1;
                                                                                                                                                              vector<LL> tmp;
15
       T ans=1;
                                                     bool is prime[maxn+5];
       for (n=(n)=m?n\%m:n); k; k>>=1){
                                                                                                           a=func(a,n,c)%n;
16
                                                                                                                                                              Factor(n,tmp);
                                                    5 void init_euler(){
         if(k&1)ans=ans*n%m;
                                                                                                           b=func(b,n,c)%n; b=func(b,n,c)%n;
                                                                                                                                                              v.clear();
17
                                                        is prime[1]=1;//一不是質數
                                                                                                           while(gcd(abs(a-b),n)==1) {
                                                                                                                                                              v.push back(1);
18
         n=n*n%m;
                                                        for(int i=1;i<=maxn;i++)euler[i]=i;</pre>
                                                                                                             a=func(a,n,c)%n;
                                                                                                                                                              int len:
19
                                                        for(int i=2;i<=maxn;i++){</pre>
                                                                                                      11
                                                                                                             b=func(b,n,c)%n; b=func(b,n,c)%n;
                                                                                                                                                         76
20
       return ans;
                                                                                                                                                              LL now=1;
                                                          if(!is_prime[i]){//是質數
                                                                                                      12
                                                                                                                                                              for(int i=0;i<tmp.size();++i) {</pre>
     void ntt(bool is inv,VT &in,VT &out,int N)
                                                            euler[i]--;
                                                                                                      13
                                                                                                           return gcd(abs(a-b),n);
                                                                                                                                                                if(i==0 || tmp[i]!=tmp[i-1]) {
22
                                                            for(int j=i<<1;j<=maxn;j+=i){</pre>
                                                                                                      14
                                                                                                                                                                  len = v.size();
                                                   11
       int bitlen=__lg(N);
                                                              is_prime[j]=1;
                                                                                                      15
                                                                                                                                                                   now = 1;
24
       for(int i=0;i<N;++i)out[bit reverse(i,</pre>
                                                              euler[j]=euler[j]/i*(i-1);
                                                                                                         void prefactor(LL &n, vector<LL> &v) {
                                                                                                           for(int i=0;i<12;++i) {</pre>
            bitlen)]=in[i];
                                                                                                                                                                now*=tmp[i];
       for(int step=2,id=1;step<=N;step<<=1,++</pre>
                                                   15
                                                                                                      18
                                                                                                             while(n%prime[i]==0) {
                                                                                                                                                                for(int j=0;j<len;++j)</pre>
                                                                                                               v.push back(prime[i]);
                                                                                                                                                         84
            id){
                                                                                                      19
                                                                                                                                                                  v.push back(v[j]*now);
         T wn=pow_mod(G,(P-1)>>id,P),wi=1,u,t;
                                                   17
                                                                                                      20
                                                                                                               n/=prime[i];
                                                                                                                                                         85
         const int mh=step>>1;
                                                      LL pow(LL a, LL b, LL mod) { //a^b%mod
                                                                                                      21
                                                       LL ans=1;
                                                                                                      22
         for(int i=0;i<mh;++i){</pre>
           for(int j=i;j<N;j+=step){</pre>
                                                        for(;b;a=a*a%mod,b>>=1)
                                                                                                      23
             u=out[j],t=wi*out[j+mh]%P;
                                                          if(b&1)ans=ans*a%mod;
             out[j]=u+t;
                                                        return ans;
                                                                                                         void smallfactor(LL n, vector<LL> &v) {
                                                                                                                                                                  other
32
             out[j+mh]=u-t;
                                                   23 }
                                                                                                           if(n<MAXPRIME) {</pre>
                                                      bool isless(LL *a,int n,int k){
             if(out[j]>=P)out[j]-=P;
                                                                                                             while(isp[(int)n]) {
```

29

30

31

v.push\_back(isp[(int)n]);

n/=isp[(int)n];

v.push\_back(n);

} else {

9.1 WhatDay.cpp

1 int whatday(int y,int m,int d){

## 9.2 上下最大正方形.cpp

```
1 void solve(int n,int a[],int b[]){// 1-base
     int ans=0;
     deque<int>da,db;
     for(int l=1,r=1;r<=n;++r){</pre>
       while(da.size()&&a[da.back()]>=a[r]){
         da.pop back();
       da.push_back(r);
       while(db.size()&&b[db.back()]>=b[r]){
10
         db.pop back();
12
       db.push_back(r);
13
       for(int d=a[da.front()]+b[db.front()];r-
            1+1>d;++1){
         if(da.front()==1)da.pop_front();
14
         if(db.front()==1)db.pop front();
         if(da.size()&&db.size()){
16
17
           d=a[da.front()]+b[db.front()];
18
19
20
       ans=\max(ans,r-1+1);
21
    printf("%d\n",ans);
22
23
```

## 9.3 最大矩形.cpp

```
1 LL max rectangle(vector<int> s){
     stack<pair<int,int > > st;
     st.push(make pair(-1,0));
    s.push back(0);
    LL ans=0:
     for(size t i=0;i<s.size();++i){</pre>
       int h=s[i];
       pair<int,int > now=make pair(h,i);
       while(h<st.top().first){</pre>
10
         now=st.top();
         st.pop();
11
         ans=max(ans,(LL)(i-now.second)*now.
12
13
14
       if(h>st.top().first){
         st.push(make pair(h,now.second));
15
16
17
18
    return ans;
```

## 10 String

## 10.1 AC 自動機.cpp

58

59

60

```
61
                                                   62
 1 template < char L='a', char R='z'>
                                                   63
   class ac automaton{
     struct joe{
                                                   64
       int next[R-L+1],fail,efl,ed,cnt dp,vis;
                                                   65
       joe():ed(0),cnt_dp(0),vis(0){
                                                   66
         for(int i=0;i<=R-L;++i)next[i]=0;</pre>
    };
   public:
                                                    69
     std::vector<joe> S;
     std::vector<int> q;
                                                    70
11
                                                   71
     int qs,qe,vt;
     ac_automaton():S(1),qs(0),qe(0),vt(0){}
                                                    72
     void clear(){
                                                    73
14
                                                   74
15
       q.clear();
                                                    75
       S.resize(1);
16
17
       for(int i=0;i<=R-L;++i)S[0].next[i]=0;</pre>
       S[0].cnt dp=S[0].vis=qs=qe=vt=0;
18
                                                    77
19
20
     void insert(const char *s){
                                                   78
                                                    79
       for(int i=0,id;s[i];++i){
22
                                                   80
         id=s[i]-L;
23
                                                   81
         if(!S[o].next[id]){
24
25
           S.push_back(joe());
            S[o].next[id]=S.size()-1;
                                                   83
27
                                                   84
28
         o=S[o].next[id];
                                                   85
29
30
       ++S[o].ed;
31
32
     void build fail(){
                                                   87
33
       S[0].fail=S[0].efl=-1;
34
                                                   89
       q.clear();
35
       q.push_back(0);
                                                   90
36
       ++qe;
                                                   91
37
       while(qs!=qe){
                                                   92
38
         int pa=q[qs++],id,t;
                                                   93
39
         for(int i=0;i<=R-L;++i){</pre>
                                                   94
40
           t=S[pa].next[i];
                                                   95
           if(!t)continue;
                                                   96
41
            id=S[pa].fail;
42
                                                   97
43
            while(~id&&!S[id].next[i])id=S[id].
                 fail;
            S[t].fail=~id?S[id].next[i]:0;
44
            S[t].efl=S[S[t].fail].ed?S[t].fail:S
45
                 [S[t].fail].efl;
                                                   100
            q.push_back(t);
46
                                                   101
47
            ++qe;
                                                   102
48
                                                   103
49
                                                   104
50
                                                   105
     /*DP出每個前綴在字串s出現的次數並傳回所有
                                                   106
          字串被s匹配成功的次數O(N+M)*/
                                                  107
     int match 0(const char *s){
                                                  108
       int ans=0,id,p=0,i;
                                                  109
       for(i=0;s[i];++i){
55
         id=s[i]-L;
                                                   110
         while(!S[p].next[id]&&p)p=S[p].fail;
```

```
if(!S[p].next[id])continue;
                                       112 };
   p=S[p].next[id];
   ++S[p].cnt_dp;/*匹配成功則它所有後綴都
        可以被匹配(DP計算)*/
 for(i=qe-1;i>=0;--i){
   ans+=S[q[i]].cnt dp*S[q[i]].ed;
   if(~S[q[i]].fail)S[S[q[i]].fail].
        cnt_dp+=S[q[i]].cnt_dp;
 return ans;
/*多串匹配走efL邊並傳回所有字串被s匹配成功
    的 次 數 O(N*M^1.5)*/
int match 1(const char *s)const{
 int ans=0,id,p=0,t;
 for(int i=0;s[i];++i){
   id=s[i]-L;
   while(!S[p].next[id]&&p)p=S[p].fail;
   if(!S[p].next[id])continue;
   p=S[p].next[id];
   if(S[p].ed)ans+=S[p].ed;
   for(t=S[p].efl;~t;t=S[t].efl){
     ans+=S[t].ed;/*因為都走efL邊所以保證
          匹配成功*/
 return ans;
/*枚舉(s的子字串nA)的所有相異字串各恰一次
    並傳回次數O(N*M^(1/3))*/
int match_2(const char *s){
 int ans=0,id,p=0,t;
 /*把戳記vt+=1,只要vt沒溢位,所有S[p].
      vis==vt 就會變成false
  這種利用vt的方法可以0(1)歸零vis陣列*/
 for(int i=0;s[i];++i){
   id=s[i]-L:
   while(!S[p].next[id]&&p)p=S[p].fail;
   if(!S[p].next[id])continue;
   p=S[p].next[id];
   if(S[p].ed&&S[p].vis!=vt){
     S[p].vis=vt;
     ans+=S[p].ed;
   for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[t
       1.ef1){
     S[t].vis=vt;
     ans+=S[t].ed;/*因為都走efL邊所以保證
          匹配成功*/
 return ans;
/*把AC自動機變成真的自動機*/
void evolution(){
 for(qs=1;qs!=qe;){
   int p=q[qs++];
   for(int i=0;i<=R-L;++i)</pre>
     if(S[p].next[i]==0)S[p].next[i]=S[S[
         p].fail].next[i];
```

### 10.2 hash.cpp

```
1 #define MAXN 1000000
2 #define mod 1073676287
 3 /*mod 必須要是質數*/
 4 typedef long long T;
  char s[MAXN+5];
6 T h[MAXN+5]; /*hash 陣列*/
 7 T h base[MAXN+5];/*h base[n]=(prime^n)%mod*/
 8 void hash_init(int len,T prime){
    h base[0]=1:
    for(int i=1;i<=len;++i){</pre>
      h[i]=(h[i-1]*prime+s[i-1])%mod;
      h base[i]=(h base[i-1]*prime)%mod;
13
14 }
15 | T get_hash(int l, int r){/*閉區間寫法,設編號
        為0 ~ Len-1*/
     return (h[r+1]-(h[1]*h_base[r-1+1])%mod+
         mod)%mod:
17 }
```

## 10.3 KMP.cpp

```
1|/*產生fail function*/
 void kmp fail(char *s,int len,int *fail){
     int id=-1;
     fail[0]=-1;
     for(int i=1;i<len;++i){</pre>
       while(~id&&s[id+1]!=s[i])id=fail[id];
       if(s[id+1]==s[i])++id;
       fail[i]=id;
|A| /*以字串B匹配字串A,傳回匹配成功的數量(用B的
12 int kmp_match(char *A,int lenA,char *B,int
        lenB,int *fail){
     int id=-1.ans=0:
     for(int i=0;i<lenA;++i){</pre>
       while(~id&&B[id+1]!=A[i])id=fail[id];
       if(B[id+1]==A[i])++id;
       if(id==lenB-1){/*匹配成功*/
         ++ans, id=fail[id];
18
19
20
21
     return ans;
```

#### 10.4 manacher.cpp

```
1 //原字串: asdsasdsa
  //先把字串變成這樣: @#a#s#d#s#a#s#d#s#a#
  void manacher(char *s,int len,int *z){
   int 1=0, r=0;
   for(int i=1;i<len;++i){</pre>
     z[i]=r>i?min(z[2*l-i],r-i):1;
     while(s[i+z[i]]==s[i-z[i]])++z[i];
     if(z[i]+i>r)r=z[i]+i,l=i;
   }//ans = max(z)-1
 10.5 minimal string rotation.
```

#### int n=s.size(),i=0,j=1,k=0; while(i<n&&j<n&&k<n){</pre> int t=s[(i+k)%n]-s[(j+k)%n]; **if**(t){ if(t>0)i+=k; else j+=k;

return min(i,j);//最小循環表示法起始位置

int min\_string\_rotation(const string &s){

## 10.6 reverseBWT.cpp

if(i==j)++j;

k=0;

11

12

13

```
1 const int MAXN = 305, MAXC = 'Z';
int ranks[MAXN], tots[MAXC], first[MAXC];
   void rankBWT(const string &bw){
    memset(ranks,0,sizeof(int)*bw.size());
    memset(tots,0,sizeof(tots);
    for(size_t i=0;i<bw.size();++i)</pre>
       ranks[i] = tots[int(bw[i])]++;
   void firstCol(){
    memset(first,0,sizeof(first));
    int totc = 0;
    for(int c='A';c<='Z';++c){</pre>
      if(!tots[c]) continue;
      first[c] = totc;
15
      totc += tots[c];
16
17
   string reverseBwt(string bw,int begin){
    rankBWT(bw), firstCol();
    int i = begin; //原字串最後一個元素的位置
21
    string res;
22
    do{
23
       char c = bw[i];
      res = c + res;
24
      i = first[int(c)] + ranks[i];
    }while( i != begin );
    return res;
```

#### suffix array lcp.cpp

1 | struct dominator tree{

int n;// 1-base

void init(int n){

void dfs(int u){

int find(int x){

n=\_n;

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

28 29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47

50

51

52

53

54

55

56

57

58 } dom;

static const int MAXN=5005;

int semi[MAXN],idom[MAXN];

i].clear();

suc[u].push back(v);

pre[v].push\_back(u);

for(auto v:suc[u]){

void add edge(int u,int v){

dfn[u]=++Time,id[Time]=u;

dfs(v),fa[dfn[v]]=dfn[u];

if(dfn[v])continue;

if(x==anc[x])return x;

for(int t=1;t<=n;++t){</pre>

dom[t].clear();

find(z);

anc[y]=x;

find(z);

dom[x].clear();

[x]=best[anc[x]];

idom[id[u]]=0

for(int y=Time;y>=2;--y){

int x=fa[y],idy=id[y];

for(auto z:pre[idy]){

for(auto z:dom[x]){

for(int u=2;u<=Time;++u){</pre>

dom[id[idom[u]]].push\_back(id[u]);

if(!(z=dfn[z]))continue;

dom[semi[y]].push back(y);

anc[t]=best[t]=semi[t]=t;

int y=find(anc[x]);

return anc[x]=y;

void tarjan(int r){

Time=0:

dfs(r):

vector<int> suc[MAXN],pre[MAXN];

int fa[MAXN],dfn[MAXN],id[MAXN],Time;

vector<int> dom[MAXN];//dominator\_tree

```
1 #define radix_sort(x,y){\
     for(i=0;i<A;++i)c[i]=0;\</pre>
     for(i=0;i<n;++i)c[x[y[i]]]++;\</pre>
     for(i=1;i<A;++i)c[i]+=c[i-1];\</pre>
     for(i=n-1;~i;--i)sa[--c[x[y[i]]]]=y[i];\
   #define AC(r,a,b)\
     r[a]!=r[b]||a+k>=n||r[a+k]!=r[b+k]
   void suffix array(const char *s,int n,int *
        sa,int *rank,int *tmp,int *c){
     int A = 'z' + 1, i, k, id = 0;
     for(i=0;i<n;++i)rank[tmp[i]=i]=s[i];</pre>
     radix sort(rank,tmp);
     for(k=1;id<n-1;k<<=1){
13
       for(id=0,i=n-k;i<n;++i)tmp[id++]=i;</pre>
       for(i=0:i<n:++i)</pre>
15
         if(sa[i]>=k)tmp[id++]=sa[i]-k;
16
17
       radix sort(rank,tmp);
       swap(rank,tmp);
18
19
       for(rank[sa[0]]=id=0,i=1;i<n;++i)</pre>
20
         rank[sa[i]]=id+=AC(tmp,sa[i-1],sa[i]);
21
       A=id+1;
22
23 }
24 | //h: 高度數組 sa:後綴數組 rank: 排名
   void suffix_array_lcp(const char *s,int len,
        int *h,int *sa,int *rank){
     for(int i=0;i<len;++i)rank[sa[i]]=i;</pre>
     for(int i=0,k=0;i<len;++i){</pre>
       if(rank[i]==0)continue;
       if(k)--k;
       while(s[i+k]==s[sa[rank[i]-1]+k])++k;
       h[rank[i]]=k;
32
     h[0]=0;// h[k]=lcp(sa[k],sa[k-1]);
```

## 10.8 Z.cpp

```
1 void z_alg(char *s,int len,int *z){
    int 1=0,r=0:
    z[0]=len:
    for(int i=1;i<len;++i){</pre>
      z[i]=i>r?0:(i-1+z[i-1]< z[1]?z[i-1]:r-i
           +1);
      while(i+z[i]<len&&s[i+z[i]]==s[z[i]])++z</pre>
           [i];
      if(i+z[i]-1>r)r=i+z[i]-1,l=i;
```

## Tarjan

#### dominator tree.cpp

## $11.2 \quad tnfshb017 \quad 2 \quad sat.cpp$

```
1 #include < bits / stdc++.h>
                                                using namespace std;
                                                 #define MAXN 8001
int anc[MAXN], best[MAXN];//disjoint set
                                                #define MAXN2 MAXN*4
                                                #define n(X)((X)+2*N)
                                                 vector<int> v[MAXN2], rv[MAXN2], vis t;
                                                 int N,M;
  for(int i=1;i<=n;++i)suc[i].clear(),pre[</pre>
                                                 void addedge(int s,int e){
                                                   v[s].push back(e);
                                                  rv[e].push_back(s);
                                              11
                                                int scc[MAXN2];
                                                 bool vis[MAXN2]={false};
                                                 void dfs(vector<int> *uv,int n,int k=-1){
                                                   vis[n]=true;
                                                   for(int i=0;i<uv[n].size();++i)</pre>
                                                     if(!vis[uv[n][i]])
                                                       dfs(uv,uv[n][i],k);
                                                   if(uv==v)vis t.push back(n);
                                              20
                                                   scc[n]=k;
                                              21
                                              22
                                                 void solve(){
                                                   for(int i=1;i<=N;++i){</pre>
                                                     if(!vis[i])dfs(v,i);
  if(semi[best[x]]>semi[best[anc[x]]])best 25
                                                     if(!vis[n(i)])dfs(v,n(i));
                                                   memset(vis,0,sizeof(vis));
                                              28
                                                   int c=0;
                                              29
                                                   for(int i=vis_t.size()-1;i>=0;--i)
                                                     if(!vis[vis_t[i]])
                                                       dfs(rv,vis t[i],c++);
                                              32
    dfn[t]=idom[t]=0://u=r或 是u無 法 到 達r時
                                              33
                                                int main(){
                                                  int a,b;
                                              34
                                                   scanf("%d%d",&N,&M);
                                                   for(int i=1;i<=N;++i){</pre>
                                                     // (A or B)&(!A & !B) A^B
                                                     a=i*2-1;
                                              39
                                                     b=i*2;
                                                     addedge(n(a),b);
                                                     addedge(n(b),a);
                                                     addedge(a,n(b));
                                                     addedge(b,n(a));
      semi[y]=min(semi[y],semi[best[z]]);
                                              44
                                                   while(M--){
                                                     scanf("%d%d",&a,&b);
                                                     a = a>0?a*2-1:-a*2;
                                                     b = b>0?b*2-1:-b*2;
                                                     // A or B
      idom[z]=semi[best[z]]<x?best[z]:x;</pre>
                                                     addedge(n(a),b);
                                              51
                                                     addedge(n(b),a);
                                                   solve();
                                                   bool check=true;
    if(idom[u]!=semi[u])idom[u]=idom[idom[
                                                   for(int i=1;i<=2*N;++i)</pre>
                                                     if(scc[i]==scc[n(i)])
                                                       check=false;
                                                   if(check){
                                                     printf("%d \ n", N);
                                                     for(int i=1;i<=2*N;i+=2){</pre>
                                                       if(scc[i]>scc[i+2*N]) putchar('+');
                                                       else putchar('-');
                                              62
```

```
puts("");
     }else puts("0");
     return 0;
   11.3 橋連通分量.cpp
 1 #define N 1005
   struct edge{
     int u,v;
     bool is bridge;
     edge(int u=0,int v=0):u(u),v(v),is_bridge
 6 };
   vector<edge> E;
   vector<int> G[N];// 1-base
 9 int low[N], vis[N], Time;
int bcc id[N], bridge cnt, bcc cnt; // 1-base
11 int st[N],top;//BCC用
inline void add edge(int u,int v){
     G[u].push_back(E.size());
     E.push back(edge(u,v));
15
     G[v].push_back(E.size());
     E.push back(edge(v,u));
16
17
   void dfs(int u,int re=-1){//u當前點,re為u連
        接前一個點的邊
     int v;
     low[u]=vis[u]=++Time;
     st[top++]=u;
     for(size t i=0;i<G[u].size();++i){</pre>
       int e=G[u][i];v=E[e].v;
       if(!vis[v]){
25
         dfs(v,e^1);//e^1反向邊
26
         low[u]=min(low[u],low[v]);
27
         if(vis[u]<low[v]){</pre>
           E[e].is_bridge=E[e^1].is_bridge=1;
28
29
           ++bridge cnt;
30
       }else if(vis[v]<vis[u]&&e!=re)</pre>
32
         low[u]=min(low[u], vis[v]);
33
34
     if(vis[u]==low[u]){//處理BCC
       ++bcc cnt;// 1-base
35
       do bcc id[v=st[--top]]=bcc cnt;//每個點
            所在的BCC
37
       while(v!=u);
38
39
   inline void bcc_init(int n){
     Time=bcc cnt=bridge cnt=top=0;
     E.clear();
42
     for(int i=1;i<=n;++i){</pre>
43
44
       G[i].clear();
45
       vis[i]=bcc_id[i]=0;
46
```

## 11.4 雙連通分量 & 割點.cpp

```
1 | #define N 1005
2 vector<int> G[N];// 1-base
3 | vector < int > bcc[N]; // 存每塊雙連通分量的點
 4 int low[N], vis[N], Time;
 5 int bcc_id[N],bcc_cnt;// 1-base
 6|bool is cut[N];//是否為割點
7 int st[N],top;
   void dfs(int u,int pa=-1){//u當前點,pa父親
     int v.child=0:
     low[u]=vis[u]=++Time;
     st[top++]=u;
     for(size t i=0;i<G[u].size();++i){</pre>
       if(!vis[v=G[u][i]]){
13
         dfs(v,u),++child;
15
         low[u]=min(low[u],low[v]);
         if(vis[u]<=low[v]){</pre>
16
17
           is cut[u]=1;
           bcc[++bcc_cnt].clear();
18
           int t;
20
             bcc_id[t=st[--top]]=bcc_cnt;
21
22
             bcc[bcc cnt].push back(t);
23
           }while(t!=v);
24
           bcc id[u]=bcc_cnt;
25
           bcc[bcc cnt].push back(u);
26
27
       }else if(vis[v]<vis[u]&&v!=pa)//反向邊
28
         low[u]=min(low[u], vis[v]);
29
    if(pa==-1&&child<2)is_cut[u]=0;//u是dfs樹
30
          的根要特判
31
32 inline void bcc init(int n){
    Time=bcc cnt=top=0;
33
     for(int i=1:i<=n:++i){</pre>
34
      G[i].clear();
35
36
       is_cut[i]=vis[i]=bcc_id[i]=0;
37
38 }
```

## 12 Tree problem

#### 12.1 HeavyLight.cpp

```
1 #include < vector >
2 #define MAXN 100005
int siz[MAXN], max son[MAXN], pa[MAXN], dep[
       MAXN];
 4 int link top[MAXN],link[MAXN],cnt;
5 vector<int> G[MAXN];
6 void find max son(int u){
     siz[u]=1:
     max_son[u]=-1;
     for(auto v:G[u]){
      if(v==pa[u])continue;
11
       pa[v]=u;
       dep[v]=dep[u]+1;
       find max son(v);
       if(max son[u]==-1||siz[v]>siz[max son[u
            ]])max son[u]=v;
```

```
siz[u]+=siz[v];
16
17 }
  void build link(int u,int top){
    link[u]=++cnt;
19
    link top[u]=top;
21
    if(max son[u]==-1)return;
    build link(max_son[u],top);
    for(auto v:G[u]){
      if(v==max son[u]||v==pa[u])continue;
24
25
      build link(v,v);
26
27
  int find lca(int a.int b){
    //求LCA · 可以在過程中對區間進行處理
    int ta=link top[a],tb=link top[b];
31
    while(ta!=tb){
      if(dep[ta]<dep[tb]){</pre>
33
        swap(ta,tb);
34
        swap(a,b);
35
      //這裡可以對a所在的鏈做區間處理
36
37
      //區間為(link[ta],link[a])
38
      ta=link top[a=pa[ta]];
39
    //最後a,b會在同一條鏈,若a!=b還要在進行一
         次區間處理
    return dep[a]<dep[b]?a:b;</pre>
41
42 }
```

#### 12.2 LCA.cpp

```
1 | #define MAXN 100000
 2 #define MAX LOG 17
 3 int pa[MAX LOG+1][MAXN+5];
 4 int dep[MAXN+5];
 5 vector<int> G[MAXN+5];
 6 void dfs(int x,int p){//dfs(1,-1);
     pa[0][x]=p;
     for(int i=0;i+1<MAX LOG;++i)pa[i+1][x]=pa[</pre>
          i][pa[i][x]];
     for(auto &i:G[x]){
       if(i==p)continue;
11
       dep[i]=dep[x]+1;
12
       dfs(i,x);
13
14 }
inline int jump(int x,int d){
16 for(int i=0;i<d;++i)if((x>>i)&1)x=pa[k][x];
    return x;
   inline int find_lca(int a,int b){
     if(dep[a]>dep[b])swap(a,b);
     b=jump(b,dep[b]-dep[a]);
     if(a==b)return a;
     for(int i=MAX LOG;i>=0;--i){
       if(pa[i][a]!=pa[i][b]){
25
         a=pa[i][a];
26
         b=pa[i][b];
27
    }
28
     return pa[0][a];
```

## 12.3 link cut tree.cpp

splay\_tree():pa(0),rev(0){ch[0]=ch[1]=0;}

**int** ch[2],pa;//子節點跟父母

bool rev; // 反轉的懶惰標記

7 // 有的時候用vector會TLE,要注意

1 | struct splay tree{

6 vector<splay tree> nd;

30 }

};

```
8 | // 這邊以node [0] 作為null 節點
9 bool isroot(int x){//判斷是否為這棵splay
       tree的 根
    return nd[nd[x].pa].ch[0]!=x&&nd[nd[x].pa
         ].ch[1]!=x;
11 }
  void down(int x){// 懶惰標記下推
12
    if(nd[x].rev){
      if(nd[x].ch[0])nd[nd[x].ch[0]].rev^=1;
      if(nd[x].ch[1])nd[nd[x].ch[1]].rev^=1;
      swap(nd[x].ch[0],nd[x].ch[1]);
17
      nd[x].rev=0;
18
19
  void push down(int x){//所有祖先懶惰標記下推
    if(!isroot(x))push down(nd[x].pa);
23
24 | void up(int x){}//將子節點的資訊向上更新
  void rotate(int x){//旋轉,會自行判斷轉的方
    int y=nd[x].pa,z=nd[y].pa,d=(nd[y].ch[1]==
         x);
    nd[x].pa=z;
    if(!isroot(y))nd[z].ch[nd[z].ch[1]==y]=x;
    nd[y].ch[d]=nd[x].ch[d^1];
    nd[nd[y].ch[d]].pa=y;
    nd[y].pa=x,nd[x].ch[d^1]=y;
    up(y),up(x);
33
  void splay(int x){//將x伸展到splay tree的根
    push down(x);
    while(!isroot(x)){
      int y=nd[x].pa;
      if(!isroot(y)){
        int z=nd[y].pa;
        if((nd[z].ch[0]==y)^(nd[y].ch[0]==x))
             rotate(y);
41
        else rotate(x);
42
      rotate(x);
44
  int access(int x){
    int last=0;
    while(x){
      splay(x);
      nd[x].ch[1]=last;
      up(x);
      last=x;
```

```
int lca=access(v);
       x=nd[x].pa;
54
                                                115
                                                      splay(u);
                                                     if(u==lca){
     return last;//access後splay tree的根
                                                116
55
                                                       //return nd[lca].data+nd[nd[lca].ch[1]].
56
57 void access(int x,bool is=0){//is=0就是一般
                                                     }else{
        的access
                                                119
                                                       //return nd[lca].data+nd[nd[lca].ch[1]].
     int last=0;
                                                            sum+nd[u].sum
     while(x){
59
                                                120
       splay(x);
                                                121 }
61
       if(is\&\&!nd[x].pa){
                                                122 struct EDGE{
         //printf("%d\n", max(nd[last].ma,nd[nd[
                                                     int a.b.w:
              x].ch[1]].ma));
                                                124 }e[10005];
63
                                                125 int n:
       nd[x].ch[1]=last;
64
                                                126 vector<pair<int,int>> G[10005];
65
       up(x);
                                                127 //first表示子節點 · second表示邊的編號
66
       last=x;
                                                128 int pa[10005], edge_node[10005];
       x=nd[x].pa;
                                                129 //pa是父母節點,暫存用的,edge node是每個編
68
                                                         被存在哪個點裡面的陣列
    void query edge(int u,int v){
                                                130 void bfs(int root){
     access(u);
                                                131 | //在建構的時候把每個點都設成一個splay tree
72
     access(v.1):
                                                     queue<int > q;
73
                                                      for(int i=1;i<=n;++i)pa[i]=0;</pre>
                                                133
    void make root(int x){
                                                134
                                                     q.push(root);
     access(x), splay(x);
                                                135
                                                      while(q.size()){
     nd[x].rev^=1;
76
                                                136
                                                       int u=q.front();
77
                                                137
                                                       q.pop();
78
   void make root(int x){
                                                138
                                                        for(auto P:G[u]){
     nd[access(x)].rev^=1;
                                                139
                                                         int v=P.first;
80
     splay(x);
                                                         if(v!=pa[u]){
                                                140
81
                                                141
                                                            pa[v]=u;
    void cut(int x,int y){
                                                142
                                                            nd[v].pa=u;
     make root(x);
                                                            nd[v].data=e[P.second].w;
                                                143
     access(y);
84
                                                            edge node[P.second]=v;
                                                144
     splay(y);
                                                145
                                                            up(v);
86
     nd[y].ch[0]=0;
                                                146
                                                            q.push(v);
     nd[x].pa=0;
87
                                                147
88
                                                148
   void cut parents(int x){
                                                     }
                                                149
     access(x);
                                                150
     splay(x);
                                                    void change(int x,int b){
                                                151
     nd[nd[x].ch[0]].pa=0;
92
                                                     splay(x);
                                                152
93
     nd[x].ch[0]=0;
                                                153
                                                     //nd[x].data=b;
94
                                                154
                                                     up(x);
   void link(int x,int y){
                                                155 }
     make root(x);
96
97
     nd[x].pa=y;
98
99
   int find root(int x){
                                                   12.4 POJ tree.cpp
     x=access(x);
100
     while(nd[x].ch[0])x=nd[x].ch[0];
     splay(x);
102
103
     return x;
                                                  1 | #include < bits / stdc++.h>
104
                                                 using namespace std;
int query(int u,int v){
                                                  3 #define MAXN 10005
106 // 傳回uv路徑splay tree的根結點
                                                  4 int n,k;
   //這種寫法無法求LCA
                                                  5 vector<pair<int,int> >g[MAXN];
     make root(u);
108
                                                  6 int size[MAXN];
109
     return access(v);
                                                 7 bool vis[MAXN];
110
                                                  8 inline void init(){
int query lca(int u,int v){
                                                     for(int i=0;i<=n;++i){</pre>
112 //假設求鏈上點權的總和·sum是子樹的權重和
                                                       g[i].clear();
        data是簡點的權重
                                                 11
                                                       vis[i]=0;
                                                 12
     access(u);
                                                     }
                                                 13 }
```

```
14 | void get dis(vector<int> &dis,int u,int pa,
       int d){
     dis.push back(d);
     for(size t i=0;i<g[u].size();++i){</pre>
       int v=g[u][i].first,w=g[u][i].second;
17
       if(v!=pa&&!vis[v])get dis(dis,v,u,d+w);
20 }
21 | vector<int> dis;//這東西如果放在函數裡會TLE
   int cal(int u,int d){
    dis.clear();
    get_dis(dis,u,-1,d);
     sort(dis.begin(),dis.end());
     int l=0,r=dis.size()-1,res=0;
     while(l<r){</pre>
       while(l<r&&dis[l]+dis[r]>k)--r;
28
       res+=r-(1++);
29
30
31
    return res;
32 }
  pair<int,int> tree centroid(int u,int pa,
       const int sz){
     size[u]=1;//找樹重心, second是重心
     pair<int,int> res(INT MAX,-1);
     int ma=0;
37
     for(size t i=0;i<g[u].size();++i){</pre>
       int v=g[u][i].first;
38
       if(v==pa||vis[v])continue;
39
       res=min(res, tree centroid(v,u,sz));
40
41
       size[u]+=size[v];
       ma=max(ma,size[v]);
42
43
44
     ma=max(ma,sz-size[u]);
    return min(res, make pair(ma,u));
46
   int tree_DC(int u,int sz){
47
    int center=tree centroid(u,-1,sz).second;
    int ans=cal(center,0);
    vis[center]=1;
50
     for(size t i=0;i<g[center].size();++i){</pre>
51
       int v=g[center][i].first,w=g[center][i].
            second;
       if(vis[v])continue;
53
54
       ans-=cal(v,w);
       ans+=tree DC(v,size[v]);
56
57
     return ans;
58
     while(scanf("%d%d",&n,&k),n||k){
61
       init():
       for(int i=1;i<n;++i){</pre>
62
63
         int u,v,w;
64
         scanf("%d%d%d",&u,&v,&w);
         g[u].push_back(make_pair(v,w));
65
         g[v].push back(make pair(u,w));
66
67
68
       printf("%d \setminus n", tree DC(1,n));
69
70
     return 0;
71
```

#### 13 zformula

#### 13.1 formula.tex

#### 13.1.1 Pick 公式

給定頂點坐標均是整點的簡單多邊形·面積 = 內部格點數 + 邊上格點數/2-1

#### 13.1.2 圖論

```
1. V-E+F=2
2. 對於平面圖 \cdot F=E-V+n+1\cdot n 是連通分量
```

2. 對於平面圖  $F = E - V + n + 1 \cdot n$  定建題 3. 對於平面圖 E < 3V - 6

4. 對於連通圖  $G \cdot$ 最大獨立點集的大小設為  $I(G) \cdot$ 最大匹配大小設為  $M(G) \cdot$ 最小點覆蓋設為  $Cv(G) \cdot$ 最小邊覆蓋設為  $Ce(G) \cdot$ 對於任意連通圖:

(a) 
$$I(G) + Cv(G) = |V|$$
  
(b)  $M(G) + Ce(G) = |V|$ 

5. 對於連通二分圖:

```
(a) I(G) = Cv(G)
(b) M(G) = Ce(G)
```

6. 最大權閉合圖:

```
(a) C(u, V) = \infty, (u, v) \in E

(b) C(S, v) = W_v, W_v > 0

(c) C(v, T) = -W_v, W_v < 0
```

7. 最大密度子圖:

```
(a) C(u, v) = 1, (u, v) \in E

(b) C(S, v) = U_v, v \in V

(c) C(v, T) = U + 2g - d_v, v \in V
```

8. 弦圖:

- (a) 完美消除序列從後往前依次給每個點染色·給 每個點染上可以染的最小顏色
- ) 最大團大小 = 色數
- (c) 最大獨立集: 完美消除序列從前往後能選就選
- (d) 最小團覆蓋: 最大獨立集的點和他延伸的邊構
- (e) 區間圖是弦圖
- f) 區間圖的完美消除序列: 將區間按造又端點由 小到大排序
- (g) 區間圖染色: 用線段樹做

```
1 | double l=0,=m,stop=1.0/n/n;
2 | while(r-l>=stop){
3 | double(mid);
4 | if((n*m-sol.maxFlow(s,t))/2>eps)l=mid;
5 | else r=mid;
6 |}
7 | build(l);
8 | sol.maxFlow(s,t);
9 | vector(int> ans;
10 | for(int i=1;i<=n;++i)
11 | if(sol.vis[i])ans.push_back(i);</pre>
```

#### 13.1.3 學長公式

- 1.  $\sum_{d|n} \phi(n) = n$
- 2.  $g(n) = \sum_{d|n} f(d) = \sum_{d|n} \mu(d) \times$
- 3. Harmonic series  $H_n = \ln(n) + \gamma + 1/(2n)$   $1/(12n^2) + 1/(120n^4)$
- 4.  $\gamma = 0.57721566490153286060651209008240243104215$
- 5. 格雷碼 =  $n \oplus (n >> 1)$
- 6.  $SG(A+B) = SG(A) \oplus SG(B)$
- 7. 選轉矩陣  $M(\theta) = \begin{pmatrix} cos\theta & -sin\theta \\ sin\theta & cos\theta \end{pmatrix}$

#### 13.1.4 基本數論

- 1.  $\sum_{d|n} \mu(n) = [n == 1]$
- 2.  $g(m) = \sum_{d|m} f(d) \Leftrightarrow f(m) = \sum_{d|m} \mu(d) \times$
- 4.  $\sum_{i=1}^{n} \sum_{j=1}^{n} lcm(i,j) = n \sum_{d|n} d \times \phi(d)$

#### 13.1.5 排組公式

- 1. k 卡特蘭  $\frac{C_n^{kn}}{n(k-1)+1} \cdot C_m^n = \frac{n!}{m!(n-m)!}$
- 2.  $H(n,m) \cong x_1 + x_2 \dots + x_n = k, num = C_k^{n+k-1}$
- 3. Stirling number of  $2^{nd}$ ,n 人分 k 組方法數目
  - (a) S(0,0) = S(n,n) = 1
  - (b) S(n,0) = 0
- (c) S(n,k) = kS(n-1,k) + S(n-1,k-1)
- 4. Bell number,n 人分任意多組方法數目
  - (a)  $B_0 = 1$

  - (a)  $B_0 = \sum_{i=0}^{n} S(n, i)$ (b)  $B_n = \sum_{i=0}^{n} S(n, i)$ (c)  $B_{n+1} = \sum_{k=0}^{n} C_n^k B_k$ (d)  $B_{p+n} \equiv B_n + B_{n+1} mod p$ , p is prime (e)  $B_p m_{+n} \equiv m B_n + B_{n+1} mod p$ , p is prime (f)  $E_n = B_n + B_{n+1} mod p$ , p is prime
  - (f) From  $B_0: 1, 1, 2, 5, 15, 52,$ 203, 877, 4140, 21147, 115975
- 5. Derangement, 錯排, 沒有人在自己位置上
  - (a)  $D_n = n!(1 \frac{1}{1!} + \frac{1}{2!} \frac{1}{3!} \dots + (-1)^n \frac{1}{n!})$ (b)  $D_n = (n-1)(D_{n-1} + D_{n-2}), D_0 = 0$  $1, D_1 = 0$
  - (c) From  $D_0: 1, 0, 1, 2, 9, 44$ , 265, 1854, 14833, 133496
- 6. Binomial Equality
  - (a)  $\sum_{k} {r \choose m+k} {s \choose n-k} = {r+s \choose m+n}$
  - (b)  $\sum_{k} {l \choose m+k} {s \choose n+k} = {l+s \choose l-m+n}$

  - (c)  $\sum_{k} {m+k \choose n+k} {s+k \choose n} {(-1)^k} = (-1)^{l+m} {s-m \choose n-l}$ (d)  $\sum_{k \le l} {l \choose m+k} {s \choose k-n} (-1)^k = (-1)^{l+m} {s-m \choose n-l}$
  - (e)  $\sum_{0 \le k \le l} {l-k \choose m} {q+k \choose n} = {l+q+1 \choose m+n+1}$
  - (f)  $\binom{r}{b} = (-1)^k \binom{k-r-1}{b}$

- (g)  $\binom{r}{m}\binom{m}{k} = \binom{r}{k}\binom{r-k}{m-k}$
- (h)  $\sum_{k \le n} {r+k \choose k} = {r+n+1 \choose n}$
- (i)  $\sum_{0 \le k \le n} {k \choose m} = {n+1 \choose m+1}$
- (j)  $\sum_{k \le m} {m+r \choose k} x^k y^k$  $\sum_{k \le m} {\binom{-r}{k}} (-x)^k (x+y)^{m-k}$

#### 13.1.6 冪次, 冪次和

- 1.  $a^b \% P = a^{b \% \varphi(p) + \varphi(p)}, b > \varphi(p)$
- 2.  $1^3 + 2^3 + 3^3 + \ldots + n^3 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4}$
- 3.  $1^4 + 2^4 + 3^4 + \ldots + n^4 = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} \frac{n}{30}$
- 4.  $1^5 + 2^5 + 3^5 + \ldots + n^5 = \frac{n^6}{6} + \frac{n^5}{2} + \frac{5n^4}{12} \frac{n^2}{12}$
- 5.  $0^k + 1^k + 2^k + \dots + n^k = P(k), P(k) = {}^{10}$   $\frac{(n+1)^{k+1} \sum_{i=0}^{k-1} C_i^{k+1} P(i)}{\sum_{i=0}^{k-1} C_i^{k}}, P(0) = n+1$  11
- 6.  $\sum_{k=0}^{m-1} k^n = \frac{1}{n+1} \sum_{k=0}^n C_k^{n+1} B_k m^{n+1-k}$
- 7.  $\sum_{i=0}^{m} C_i^{m+1} B_i = 0, B_0 = 1$
- 8. 除了  $B_1 = -1/2$ ,剩下的奇數項都是 0
- 9.  $B_2 = 1/6, B_4 = -1/30, B_6 = 1/42, B_8 =$  $-1/30, B_{10} = 5/66, B_{12} = -691/2730, B_{14} = {}_{17}$  $7/6, B_{16} = -3617/510, B_{18}$  $43867/798, B_{20} = -174611/330,$

#### 13.1.7 Burnside's lemma

- 1.  $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- 2.  $X^g = t^{c(g)}$
- 3. G 表示有幾種轉法, $X^g$  表示在那種轉法下,有幾種 是會保持對稱的 $\cdot t$  是顏色數 $\cdot c(q)$  是循環節不動的
- 4. 正立方體塗三顏色,轉 0 有 36 個元素不變,轉 90 有 6 種,每種有  $3^3$  不變,180 有  $3 \times 3^4$ 120(角) 有  $8 \times 3^2 \cdot 180(邊)$  有  $6 \times 3^3 \cdot$  全部  $\frac{1}{24} \left( 3^{6} + 6 \times 3^{3} + 3 \times 3^{4} + 8 \times 3^{2} + 6 \times 3^{3} \right) =$

#### 13.1.8 Count on a tree

- 1. Rooted tree:  $s_{n+1} = \frac{1}{n} \sum_{i=1}^{n} (i \times a_i \times a_i)$  $\sum_{i=1}^{\lfloor n/i \rfloor} a_{n+1-i \times i}$
- 2. Unrooted tree:
  - (a) Odd: $a_n \sum_{i=1}^{n/2} a_i a_{n-i}$
  - (b) Even: $Odd + \frac{1}{2}a_{n/2}(a_{n/2} + 1)$
- 3. Spanning Tree
  - (a) 完全圖  $n^n 2$
  - (b) 一般圖 (Kirchhoff's theorem)M[i][i] = 5 for(Object obj: map.keySet()){ if no edge. delete any one row and col in 7 } A, ans = det(A)

#### 13.2 java.tex

#### 13.2.1 文件操作

```
1 import java.io.*;
 2 import java.util.*;
 3 import java.math.*;
 4 import java.text.*;
  public class Main{
    public static void main(String args[]){
         throws FileNotFoundException.
         IOException
      Scanner sc = new Scanner(new FileReader(
      PrintWriter pw = new PrintWriter(new
           FileWriter("a.out"));
      n=sc.nextInt();//读入下一个INT
      m=sc.nextInt();
      for(ci=1; ci<=c; ++ci){</pre>
        pw.println("Case #"+ci+": easy for
             output");
      pw.close();//矣闭流并释放,这个很重要
           否则是没有输出的
20
      sc.close();// 关闭流并释放
21
```

#### 13.2.2 优先队列

```
1 | PriorityQueue queue = new PriorityQueue( 1,
      new Comparator(){
   public int compare( Point a, Point b ){
   if(a.x < b.x | | a.x == b.x && a.y < b.y)
    return -1;
   else if( a.x == b.x && a.y == b.y )
     return 0;
   else return 1;
```

#### 13.2.3 Map

```
1 | Map map = new HashMap();
                                         2 map.put("sa","dd");
                                         3 String str = map.get("sa").toString;
degree(V_i), M[i][j] = -1, \text{if have } E(i, j), 0 \quad 6 | Object value = map.get(obj);
```

#### 13.2.4 sort

```
1 | static class cmp implements Comparator{
    public int compare(Object o1,Object o2){
    BigInteger b1=(BigInteger)o1;
    BigInteger b2=(BigInteger)o2;
    return b1.compareTo(b2);
  public static void main(String[] args)
       throws IOException{
    Scanner cin = new Scanner(System.in);
    int n;
    n=cin.nextInt();
     BigInteger[] seg = new BigInteger[n];
    for (int i=0;i<n;i++)</pre>
    seg[i]=cin.nextBigInteger();
    Arrays.sort(seg, new cmp());
15
```

	ACM ICPC		3.2 3.3	ext.cpp	5 5	7	<b>Linear_Programming</b> 7.1 最大密度子圖.cpp	<b>10</b> 10	10.7 suffix_array_lcp.cpp 10.8 Z.cpp	
Ν	TEAM REFERENCE - AADE IN ABYSS		3.4  4 Flor 4.1 4.2 4.3  5 Gra 5.1	dinic.cpp	6 6 6 6		Number_Theory         8.1       basic.cpp          8.2       bit_set.cpp          8.3       cantor_expansion.cpp          8.4       FFT.cpp          8.5       find_real_root.cpp          8.6       FWT.cpp          8.7       LinearCongruence.cpp          8.8       Lucas.cpp	10 11 11 11 11 12 12	11 Tarjan	15 15 16 <b>16</b> 16
Contents			5.2 5.3 5.4	Augmenting_Path_multiple.cp blossom_matching.cpp graphISO.cpp	7		8.9 Matrix.cpp	12 12	12.2 LCA.cpp	16
1	1.1 Geometry.cpp	1 1 3 3	5.5 5.6 5.7	KM.cpp	7 7 8		8.11 NTT.cpp	13 13	13 zformula 13.1 formula.tex	17 17
2	Data_Structure         3           2.1 DLX.cpp	ructure         3           .cpp	5.10 5.11 4 5.12	treeISO.cpp	8 8	9	other         9.1 WhatDay.cpp         9.2 上下最大正方形.cpp         9.3 最大矩形.cpp	14	13.1.2       圖論	18 18 18
	2.4 reference_point.cpp		5.14 $5.15$	3 弦圖完美消除序列.cpp 1 最小斯坦納樹 DP.cpp 5 最小樹形圖 _ 朱劉.cpp 6 穩定婚姻模板.cpp	9	10	10.1 AC 自動機.cpp	14 14	13.1.7 Burnside's lemma	18 18 18
-	default 3.1 debug.cpp		6 lang	guage CNF.cpp	<b>10</b> 10		10.4 manacher.cpp	15	13.2.2 优先队列	18