

1 Computational_Geometry

1.1 formula.tex

Pick 公式給定頂點坐標均是整點的簡單多邊形，有：面積 = 內部格點數 + 邊上格點數 / 2 - 1

1.2 Geometry.cpp

```
1 template<typename T>
2 struct point{
3     T x,y;
4     point(){ }
5     point(const T&x,const T&y):x(x),y(y){ }
6     point operator+(const point &b)const{
7         return point(x+b.x,y+b.y);
8     }
9     point operator-(const point &b)const{
10        return point(x-b.x,y-b.y);
11    }
12    point operator*(const T &b)const{return
13        point(x*b,y*b);}
14    point operator/(const T &b)const{return
15        point(x/b,y/b);}
16    bool operator==(const point &b)const{
17        return x==b.x&&y==b.y;
18    }
19    T dot(const point &b)const{
20        return x*b.x+y*b.y;
21    }
22    T cross(const point &b)const{
23        return x*b.y-y*b.x;
24    }
25    point normal()const{/*求法向量*/
26        return point(-y,x);
27    }
28    T abs2()const{/*向量長度的平方*/
29        return dot(*this);
30    }
31    T rad(const point &b)const{/*兩向量的弧度(
32        夾角)*/
33        return fabs(atan2(fabs(cross(b)),dot(b))
34            );
35    }
36 };
37 template<typename T>
38 struct line{
39     line(){ }
40     point<T> p1,p2;
41     T a,b,c; /*ax+by+c=0*/
42     line(const point<T>&x,const point<T>&y):p1
43         (x),p2(y){ }
44     void pton(){/*轉成一般式*/
45         a=p1.y-p2.y;
46         b=p2.x-p1.x;
47         c=-a*p1.x-b*p1.y;
48     }
49     T cross(const point<T> &p)const{/*點和有向
50         直線的關係，>0左邊，=0在線上<0右邊*/
51         return (p2-p1).cross(p-p1);
52     }
```

```
53     bool point_on_segment(const point<T>&p)
54     const{/*點是否線段上*/
55         return cross(p)==0&&(p1-p1).dot(p2-p1)<=0;
56     }
57     T dis2(const point<T> &p,bool is_segment
58         =0)const{/*點跟直線/線段的距離平方*/
59     point<T> v=p2-p1,v1=p-p1;
60     if(is_segment){
61         point<T> v2=p-p2;
62         if(v.dot(v1)<=0)return v1.abs2();
63         if(v.dot(v2)>=0)return v2.abs2();
64     }
65     T tmp=v.cross(v1);
66     return tmp*tmp/v.abs2();
67 }
68 point<T> projection(const point<T> &p)
69 const{/*點對直線的投影
70     point<T> n=(p2-p1).normal();
71     return p-n*(p-p1).dot(n)/n.abs2();
72 }
73 point<T> mirror(const point<T> &p)const{/*
74     點對直線的鏡射*/
75     /*要先呼叫 pton 轉成一般式*/
76     point<T> ans;
77     T d=a*a+b*b;
78     ans.x=(b*b*p.x-a*a*p.x-2*a*b*p.y-2*a*c)/
79         d;
80     ans.y=(a*a*p.y-b*b*p.y-2*a*b*p.x-2*b*c)/
81         d;
82     return ans;
83 }
84 bool equal(const line &l1)const{/*直線相等
85     */
86     return cross(l1.p1)==0&&cross(l1.p2)==0;
87 }
88 bool parallel(const line &l1)const{/*直線平
89     行*/
90     return (p1-p2).cross(l1.p1-l1.p2)==0;
91 }
92 bool cross_seg(const line &l1)const{/*直線
93     是否交線段*/
94     return (p2-p1).cross(l1.p1)*(p2-p1).cross
95         (l1.p2)<=0;
96 }
97 char line_intersect(const line &l1)const{/*
98     直線相交情況，-1無限多點，1交於一點，0
99     不相交*/
100    return parallel(l1)?(cross(l1.p1)==0?-1:0):
101        1;
102 }
103 char seg_intersect(const line &l1)const{/*
104     線段相交情況，-1無限多點，1交於一點，0
105     不相交*/
106    T c1=(p2-p1).cross(l1.p1-p1);
107    T c2=(p2-p1).cross(l1.p2-p1);
108    T c3=(l1.p2-l1.p1).cross(p1-l1.p1);
109    T c4=(l1.p2-l1.p1).cross(p2-l1.p1);
110    if(c1==0&&c2==0){
111        if(p1==l1.p1&&(p2-p1).dot(l1.p2)<=0)
112            return 1;
113        if(p1==l1.p2&&(p2-p1).dot(l1.p1)<=0)
114            return 1;
115    }
116    if(c1==0&&c2==0){
117        if(p1==l1.p1&&(p2-p1).dot(l1.p2)<=0)
118            return 1;
119        if(p1==l1.p2&&(p2-p1).dot(l1.p1)<=0)
120            return 1;
121    }
122    return 0;
123 }
124 point<T> line_intersection(const line &l1)
125 const{/*直線交點*/
126     point<T> a=p2-p1,b=l1.p2-l1.p1,s=l1.p1-p1;
127     //if(a.cross(b)==0)return INF;
128     return p1+a*s.cross(b)/a.cross(b);
129 }
130 point<T> seg_intersection(const line &l1)
131 const{/*線段交點*/
132     T c1=(p2-p1).cross(l1.p1-p1);
133     T c2=(p2-p1).cross(l1.p2-p1);
134     T c3=(l1.p2-l1.p1).cross(p1-l1.p1);
135     T c4=(l1.p2-l1.p1).cross(p2-l1.p1);
136     if(c1==0&&c2==0){
137         if(p1==l1.p1&&(p2-p1).dot(l1.p2)<=0)
138             return p1;
139         if(p1==l1.p2&&(p2-p1).dot(l1.p1)<=0)
140             return p1;
141         if(p2==l1.p1&&(p1-p2).dot(l1.p2)<=0)
142             return p2;
143         if(p2==l1.p2&&(p1-p2).dot(l1.p1)<=0)
144             return p2;
145     }else if(c1*c2<=0&&c3*c4<=0)return
146         line_intersection(l1);
147     //return INF;
148 }
149 template<typename T>
150 struct polygon{
151     polygon(){ }
152     vector<point<T> > p; //逆時針順序
153     T area()const{/*多邊形面積*/
154         T ans=0;
155         for(int i=p.size()-1,j=0;j<(int)p.size()
156             ;i=j++){
157             ans+=p[i].cross(p[j]);
158         }
159         return ans/2;
160     }
161     point<T> center_of_mass()const{/*多邊形重
162         心*/
163         T cx=0,cy=0,w=0;
164         for(int i=p.size()-1,j=0;j<(int)p.size()
165             ;i=j++){
166             T a=p[i].cross(p[j]);
167             cx+=(p[i].x+p[j].x)*a;
168             cy+=(p[i].y+p[j].y)*a;
169             w+=a;
170         }
171         return point<T>(cx/3/w,cy/3/w);
172     }
173     char ahas(const point<T>& t)const{/*點是否
174         在簡單多邊形內，是的話回傳1、在邊上回
175         傳-1、否則回傳0*/
176         bool c=0;
177         for(int i=0,j=p.size()-1;i<p.size();j=i
178             ++)
```

```
179         if(line<T>(p[i],p[j]).point_on_segment
180             (t))return -1;
181         else if((p[i].y>t.y)!=p[j].y>t.y)&&
182             t.x<(p[j].x-p[i].x)*(t.y-p[i].y)/(p[j]
183                 .y-p[i].y)+p[i].x)
184             c=1;
185         return c;
186     }
187     char point_in_convex(const point<T>&x)
188     const{
189         int l=1,r=(int)p.size()-2;
190         while(l<r){/*點是否在凸多邊形內，是的話
191             回傳1、在邊上回傳-1、否則回傳0*/
192             int mid=(l+r)/2;
193             T a1=(p[mid]-p[0]).cross(x-p[0]);
194             T a2=(p[mid+1]-p[0]).cross(x-p[0]);
195             if(a1>0&&a2<=0){
196                 T res=(p[mid+1]-p[mid]).cross(x-p[
197                     mid]);
198                 return res>0?1:(res>0?-1:0);
199             }else if(a1<0)r=mid-1;
200             else l=mid+1;
201         }
202         return 0;
203     }
204     polygon cut(const line<T> &l1)const{/*凸包
205         對直線切割，得到直線l左側的凸包*/
206     polygon ans;
207     for(int n=p.size(),i=n-1,j=0;j<n;i=j++){
208         if(l1.cross(p[i])>=0){
209             ans.p.push_back(p[i]);
210             if(l1.cross(p[j])<0)
211                 ans.p.push_back(l1.
212                     line_intersection(line<T>(p[i]
213                         ,p[j])));
214         }else if(l1.cross(p[j])>0)
215             ans.p.push_back(l1.line_intersection(
216                 line<T>(p[i],p[j])));
217         }
218     }
219     return ans;
220 }
221 static bool graham_cmp(const point<T>& a,
222     const point<T>& b){
223     return (a.x<b.x)||a.x==b.x&&a.y<b.y;/*
224         凸包排序函數*/
225 }
226 void graham(vector<point<T> > &s){/*凸包*/
227     sort(s.begin(),s.end(),graham_cmp);
228     p.resize(s.size()+1);
229     int m=0;
230     for(int i=0;i<(int)s.size();i++){
231         while(m>2&&(p[m-1]-p[m-2]).cross(s[i]
232             -p[m-2])<=0)--m;
233         p[m++]=s[i];
234     }
235     for(int i=s.size()-2,t=m+1;i>0;--i){
236         while(m>2&&(p[m-1]-p[m-2]).cross(s[i]
237             -p[m-2])<=0)--m;
238         p[m++]=s[i];
239     }
240     if(s.size())>1--m;
241     p.resize(m);
242 }
243 inline static char sign(const point<T>&t){
244     return (t.y==0?t.x:t.y)<0;
```



```

392 pt.resize(unique(pt.begin(),pt.end())-pt
    .begin());
393 for(size_t i=2;i<pt.size();++i){
394     if((pt[0]-pt[i]).area2(pt[1]-pt[i])
        !=0){
395         ok=true;
396         swap(pt[i],pt[2]);
397         break;
398     }
399 }
400 if(!ok)return;
401 ok=false;
402 for(size_t i=3;i<pt.size();++i){
403     if(tetrahedron<T>(pt[0],pt[1],pt[2],pt
        [i]).volume6()!=0){
404         ok=true;
405         swap(pt[i],pt[3]);
406         break;
407     }
408 }
409 if(!ok)return;
410 for(int i=0;i<4;++i)add_face(i,(i+1)%4,(
    i+2)%4,(i+3)%4);
411 for(size_t i=4;i<pt.size();++i){
412     for(int j=fc.size()-1;j>0;--j){
413         if(outside(i,j)){
414             dfs(i,j);
415             break;
416         }
417     }
418 }
419 size_t sz=0;
420 for(size_t i=0;i<fc.size();++i)if(fc[i].
    use)fc[sz++]=fc[i];
421 fc.resize(sz);
422 }
423 point3D<T> centroid()const{
424     point3D<T> res(0,0,0);
425     T vol=0;
426     for(size_t i=0;i<fc.size();++i){
427         T tmp=pt[fc[i].a].dot(pt[fc[i].b].
            cross(pt[fc[i].c]));
428         res=res+(pt[fc[i].a]+pt[fc[i].b]+pt[fc
            [i].c])*tmp;
429         vol+=tmp;
430     }
431     return res/(vol*4);
432 }
433 };

```

1.3 SmallestCircle.cpp

```

1 #include "Geometry.cpp"
2 #include <vector>
3 struct Circle{
4     typedef point<double> p;
5     typedef const point<double> cp;
6     p x;
7     double r2;
8     bool incircle(cp &c)const{return (x-c).
        abs2()<=r2;};
9 };
10

```

```

11 Circle TwoPointCircle(Circle::cp &a, Circle
    ::cp &b) {
12     Circle::p m=(a+b)/2;
13     return Circle{m,(a-m).abs2()};
14 }
15
16 Circle outcircle(Circle::p a, Circle::p b,
    Circle::p c) {
17     if(TwoPointCircle(a,b).incircle(c))
        return TwoPointCircle(a,b);
18     if(TwoPointCircle(b,c).incircle(a))
        return TwoPointCircle(b,c);
19     if(TwoPointCircle(c,a).incircle(b))
        return TwoPointCircle(c,a);
20     Circle::p ret;
21     double a1=b.x-a.x, b1=b.y-a.y, c1=(a1*a1
        +b1*b1)/2;
22     double a2=c.x-a.x, b2=c.y-a.y, c2=(a2*a2
        +b2*b2)/2;
23     double d = a1*b2 - a2*b1;
24     ret.x=a.x+(c1*b2-c2*b1)/d;
25     ret.y=a.y+(a1*c2-a2*c1)/d;
26     return Circle{ret,(ret-a).abs2()};
27 }
28 //rand required
29 Circle SmallestCircle(std::vector<Circle::p>
    &p){
30     int n=p.size();
31     if(n==1) return Circle{p[0],0.0};
32     if(n==2) return TwoPointCircle(p[0],p
        [1]);
33     random_shuffle(p.begin(),p.end());
34     Circle c = {p[0],0.0};
35     for(int i=0;i<n;++i){
36         if(c.incircle(p[i])) continue;
37         c=Circle{p[i],0.0};
38         for(int j=0;j<i;++j){
39             if(c.incircle(p[j])) continue;
40             c=TwoPointCircle(p[i],p[j]);
41             for(int k=0;k<j;++k){
42                 if(c.incircle(p[k]))
                    continue;
43                 c=outcircle(p[i],p[j],p[k]);
44             }
45         }
46     }
47     return c;
48 }

```

1.4 最近點對.cpp

```

1 #define INF LLONG_MAX/*預設是Long Long最大值
    */
2 template<typename T>
3 T closest_pair(vector<point<T> >&v,vector<
    point<T> >&t,int l,int r){
4     T dis=INF,tmd;
5     if(l==r)return dis;
6     int mid=(l+r)/2;
7     if((tmd=closest_pair(v,t,l,mid))<dis)dis=
        tmd;
8     if((tmd=closest_pair(v,t,mid+1,r))<dis)dis
        =tmd;

```

```

9     t.clear();
10    for(int i=l;i<=r;++i)
11        if((v[i].x-v[mid].x)*(v[i].x-v[mid].x)<
            dis)t.push_back(v[i]);
12    sort(t.begin(),t.end(),point<T>::y_cmp);/*
        如果用merge_sort的方式可以O(n)*
13    for(int i=0;i<(int)t.size();++i)
14        for(int j=1;j<=3&&i+j<(int)t.size();++j)
15            if((tmd=(t[i]-t[i+j]).abs2())<dis)dis=
                tmd;
16    return dis;
17 }
18 template<typename T>
19 inline T closest_pair(vector<point<T> > &v){
20     vector<point<T> >t;
21     sort(v.begin(),v.end(),point<T>::x_cmp);
22     return closest_pair(v,t,0,v.size()-1);/*最
        近點對距離*/
23 }

```

1.5 浮點數誤差模板.cpp

```

1 const double EPS=1e-9;
2 struct Double{
3     double d;
4     Double(double d=0):d(d){}
5     bool operator <(const Double &b)const{
6         return d-b.d<-EPS;};
7     bool operator >(const Double &b)const{
8         return d-b.d>EPS;};
9     bool operator ==(const Double &b)const{
10        return fabs(d-b.d)<=EPS;};
11     bool operator !=(const Double &b)const{
12        return fabs(d-b.d)>EPS;};
13     bool operator <=(const Double &b)const{
14        return d-b.d<=EPS;};
15     bool operator >=(const Double &b)const{
16        return d-b.d>=-EPS;};
17     operator double()const{return d;};
18 };

```

2 Data_Structure

2.1 DLX.cpp

```

1 #define MAXN 4100
2 #define MAXM 1030
3 #define MAXND 16390
4 struct DLX{
5     int n,m,sz,ansd;//高是n·寬是m的稀疏矩陣
6     int S[MAXN],H[MAXN];
7     int row[MAXN],col[MAXND];/*每個節點代表的
        列跟行
8     int L[MAXND],R[MAXND],U[MAXND],D[MAXND];
9     vector<int> ans,ans1;
10    void init(int _n,int _m){
11        n=_n,m=_m;

```

```

12    for(int i=0;i<=m;++i){
13        U[i]=D[i]=i,L[i]=i-1,R[i]=i+1;
14        S[i]=0;
15    }
16    R[m]=0,L[0]=m;
17    sz=m,ansd=INT_MAX;/*ansd存最優解的個數
18    for(int i=1;i<=n;++i)H[i]=-1;
19 }
20 void add(int r,int c){
21     ++S[col[+sz]=c];
22     row[sz]=r;
23     D[sz]=D[c],U[D[c]]=sz,U[sz]=c,D[c]=sz;
24     if(H[r]<0)H[r]=L[sz]=R[sz]=sz;
25     else R[sz]=R[H[r]],L[R[H[r]]]=sz,L[sz]=H
        [r],R[H[r]]=sz;
26 }
27 #define DFOR(i,A,s) for(int i=A[s];i!=s;i=
    A[i])
28 void remove(int c){//刪除第c行和所有當前覆
    蓋到第c行的列
29     L[R[c]]=L[c],R[L[c]]=R[c];/*這裡刪除第c
        行·若有些行不需要處理可以在開始時呼
        叫他
30     DFOR(i,D,c)DFOR(j,R,i){U[D[j]]=U[j],D[U
        [j]]=D[j],--S[col[j]]};
31 }
32 void restore(int c){//恢復第c行和所有當前
    覆蓋到第c行的列·remove的逆操作
33     DFOR(i,U,c)DFOR(j,L,i){++S[col[j]],U[D[j
        ]]=j,D[U[j]]=j;};
34     L[R[c]]=c,R[L[c]]=c;
35 }
36 void remove2(int nd){//刪除nd所在的行當前
    所有點(包括虛擬節點)·只保留nd
37     DFOR(i,D,nd)L[R[i]]=L[i],R[L[i]]=R[i];
38 }
39 void restore2(int nd){//刪除nd所在的行當前
    所有點·為remove2的逆操作
40     DFOR(i,U,nd)L[R[i]]=R[L[i]]=i;
41 }
42 bool vis[MAXN];
43 int h();//估價函數 for IDA*
44 int res=0;
45 memset(vis,0,sizeof(vis));
46 DFOR(i,R,0)if(!vis[i]){
47     vis[i]=1;
48     ++res;
49     DFOR(j,D,i)DFOR(k,R,j)vis[col[k]]=1;
50 }
51 return res;
52 }
53 bool dfs(int d){//for精確覆蓋問題
54     if(d+h()>=ansd)return 0;/*找最佳解用·找
        任意解可以刪掉
55     if(!R[0]){ansd=d;return 1;};
56     int c=R[0];
57     DFOR(i,R,0)if(S[i]<S[c])c=i;
58     remove(c);
59     DFOR(i,D,c){
60         ans.push_back(row[i]);
61         DFOR(j,R,i)remove(col[j]);
62         if(dfs(d+1))return 1;
63         ans.pop_back();

```

```

143         nearest(u->l, (k+1)%kd, x, h, mndist);
144     }
145     h[k]=old;
146 }
147 std::vector<point> in_range;
148 void range(node *u, int k, const point &mi,
149           const point &ma){
150     if(!u) return;
151     bool is=1;
152     for(int i=0; i<kd; ++i)
153         if(u->pid.d[i]<mi.d[i] || ma.d[i]<u->
154            pid.d[i]){
155             is=0; break;
156         }
157     if(is) in_range.push_back(u->pid);
158     if(mi.d[k]<=u->pid.d[k]) range(u->l, (k
159                                     +1)%kd, mi, ma);
160     if(ma.d[k]>=u->pid.d[k]) range(u->r, (k
161                                     +1)%kd, mi, ma);
162 }
163 public:
164 kd_tree(const T &INF, double a=0.75):root
165     (0), alpha(a), loga(log2(1.0/a)), INF(
166     INF), maxn(1){}
167 ~kd_tree(){delete root;}
168 void clear(){delete root; root=0, maxn=1;}
169 void build(int n, const point *p){
170     delete root, A.resize(maxn=n);
171     for(int i=0; i<n; ++i) A[i]=new node(p[i
172     ]);
173     root=build(0,0,n-1);
174 }
175 void insert(const point &x){
176     insert(root,0,x, __lg(size(root))/loga)
177     ;
178     if(root->s>maxn) maxn=root->s;
179 }
180 bool erase(const point &p){
181     bool d=erase(root,0,p);
182     if(root&&root->s<alpha*maxn) rebuild();
183     return d;
184 }
185 void rebuild(){
186     if(root) rebuild(root,0);
187     maxn=root->s;
188 }
189 T nearest(const point &x, int k){
190     qM=k;
191     T mndist=INF, h[kd]={};
192     nearest(root,0,x,h,mndist);
193     mndist=pQ.top().first;
194     pQ=std::priority_queue<std::pair<T,
195         point >>()>;
196     return mndist; /*!^Gg00x^20k000I00gZ00*/
197 }
198 const std::vector<point> &range(const
199     point &mi, const point &ma){
200     in_range.clear();
201     range(root,0,mi,ma);
202     return in_range; /*!^Gg00mi^0ma05g;000
203         Ivector*/
204 }
205 int size(){return root?root->s:0;}
206 };

```


2.3 kd_tree_replace_segment_tree

```

1  /*kd樹代替高維線段樹*/
2  struct node{
3      node *l,*r;
4      point pid,mi,ma;
5      int s;
6      int data;
7      node(const point &p,int d):l(0),r(0),pid(p),mi(p),ma(p),s(1),data(d),dmin(d),dmax(d){}
8      void up(){
9          mi=ma=pid;
10         s=1;
11         if(l){
12             for(int i=0;i<kd;++i){
13                 mi.d[i]=min(mi.d[i],l->mi.d[i]);
14                 ma.d[i]=max(ma.d[i],l->ma.d[i]);
15             }
16             s+=l->s;
17         }
18         if(r){
19             for(int i=0;i<kd;++i){
20                 mi.d[i]=min(mi.d[i],r->mi.d[i]);
21                 ma.d[i]=max(ma.d[i],r->ma.d[i]);
22             }
23             s+=r->s;
24         }
25     }
26     void up2(){
27         //其他懶惰標記向上更新
28     }
29     void down(){
30         //其他懶惰標記下推
31     }
32 }*root;
33
34 /*檢查區間包含用的函數*/
35 inline bool range_include(node *o,const point &L,const point &R){
36     for(int i=0;i<kd;++i){
37         if(L.d[i]>o->ma.d[i]||R.d[i]<o->mi.d[i])
38             return 0;
39     }
40     //只要(L,R)區間有和o的區間有交集就回傳true
41     return 1;
42 }
43 inline bool range_in_range(node *o,const point &L,const point &R){
44     for(int i=0;i<kd;++i){
45         if(L.d[i]>o->mi.d[i]||o->ma.d[i]>R.d[i])
46             return 0;
47     }
48     //如果(L,R)區間完全包含o的區間就回傳true
49     return 1;
50 }
51 inline bool point_in_range(node *o,const point &L,const point &R){
52     for(int i=0;i<kd;++i){
53         if(L.d[i]>o->pid.d[i]||R.d[i]<o->pid.d[i])
54             return 0;
55     }
56     //如果(L,R)區間完全包含o->pid這個點就回傳true
57     return 1;
58 }

```

```

54 /*單點修改·以單點改值為例*/
55 void update(node *u,const point &x,int data,int k=0){
56     if(!u)return;
57     u->down();
58     if(u->pid==x){
59         u->data=data;
60         u->up2();
61         return;
62     }
63     cmp.sort_id=k;
64     update(cmp(x,u->pid)?u->l:u->r,x,data,(k+1)%kd);
65     u->up2();
66 }
67
68 /*區間修改*/
69 void update(node *o,const point &L,const point &R,int data){
70     if(!o)return;
71     o->down();
72     if(range_in_range(o,L,R)){
73         //區間懶惰標記修改
74         o->down();
75         return;
76     }
77     if(point_in_range(o,L,R)){
78         //這個點在(L,R)區間·但是他的左右子樹不一定在區間中
79         //單點懶惰標記修改
80     }
81     if(o->l&&range_include(o->l,L,R))update(o->l,L,R,data);
82     if(o->r&&range_include(o->r,L,R))update(o->r,L,R,data);
83     o->up2();
84 }
85
86 /*區間查詢·以總和為例*/
87 int query(node *o,const point &L,const point &R){
88     if(!o)return 0;
89     o->down();
90     if(range_in_range(o,L,R))return o->sum;
91     int ans=0;
92     if(point_in_range(o,L,R))ans+=o->data;
93     if(o->l&&range_include(o->l,L,R))ans+=query(o->l,L,R);
94     if(o->r&&range_include(o->r,L,R))ans+=query(o->r,L,R);
95     return ans;
96 }

```

2.4 persistent_segment_tree.cpp

```

1  #include<bits/stdc++.h>//POJ 2104
2  using namespace std;
3  struct node{
4      int l,r;
5      int data;

```

```

6      node(int l,int r,int d):l(l),r(r),data(d){}
7  };
8  vector<node> nds;
9  inline void up(int o,int l,int r){
10     nds[o].data=nds[l].data+nds[r].data;
11 }
12 inline int new_node(int l,int r,int d){
13     nds.push_back(node(l,r,d));
14     return nds.size()-1;
15 }
16 inline int new_node(const node &nd){
17     nds.push_back(nd);
18     return nds.size()-1;
19 }
20 int build_tree(int l,int r){
21     int nd=new_node(-1,-1,0);
22     if(l==r)return nd;
23     int mid=(l+r)/2;
24     int L=build_tree(l,mid);//執行時vector會被重構
25     int R=build_tree(mid+1,r);//一定要這樣寫
26     nds[nd].l=L;
27     nds[nd].r=R;
28     //up(nd,L,R);
29     return nd;
30 }
31 int insert(int l,int r,int rt,int x,int d){
32     if(x<l||r<x)return rt;
33     int nd=new_node(nds[rt]);
34     if(l==r&&l==x)nds[nd].data+=d;
35     else{
36         int mid=(l+r)/2;
37         int L=insert(l,mid,nds[nd].l,x,d);
38         int R=insert(mid+1,r,nds[nd].r,x,d);
39         nds[nd].l=L;
40         nds[nd].r=R;
41         up(nd,L,R);
42     }
43     return nd;
44 }
45 inline int cal(int L,int R){
46     return nds[R].data-nds[L].data;
47 }
48 int find(int l,int r,int L,int R,int k){
49     if(l==r)return l;
50     int mid=(l+r)/2;
51     int add=cal(nds[L].l,nds[R].l);
52     if(k<=add)return find(l,mid,nds[L].l,nds[R].l,k);
53     return find(mid+1,r,nds[L].r,nds[R].r,k-add);
54 }
55 int n,m;
56 int s[100005];
57 int root[100005];
58 int main(){
59     while(~scanf("%d",&n,&m)){
60         nds.clear();
61         vector<int> lsh;
62         for(int i=1;i<=n;++i){
63             scanf("%d",&s[i]);
64             lsh.push_back(s[i]);
65         }
66         sort(lsh.begin(),lsh.end());

```

```

67         lsh.resize(unique(lsh.begin(),lsh.end())-lsh.begin());
68         int N=(int)lsh.size()-1;
69         root[0]=build_tree(0,N);
70         for(int i=1;i<=m;++i){
71             s[i]=lower_bound(lsh.begin(),lsh.end(),s[i])-lsh.begin();
72             root[i]=insert(0,N,root[i-1],s[i],1);
73         }
74         while(m--){
75             int a,b,k;
76             scanf("%d%d",&a,&b,&k);
77             int res=find(0,N,root[a-1],root[b],k);
78             printf("%d\n",lsh[res]);
79         }
80     }
81     return 0;
82 }

```

2.5 reference_point.cpp

```

1  #include<bits/stdc++.h>
2  using namespace std;
3  template<typename T>
4  struct _RefCounter{
5      T data;
6      int ref;
7      _RefCounter(const T&d=0):data(d),ref(0){}
8  };
9  template<typename T>
10 struct reference_pointer{
11     _RefCounter<T> *p;
12     T *operator->(){return &(*p).data;}
13     T &operator*(){return p->data;}
14     operator int(){return (int)(long long)p;}
15     reference_pointer&operator=(const reference_pointer &t){
16         if(p&&--(*p).ref==0)delete p;
17         p=t.p;
18         p&&+(*p).ref;
19         return *this;
20     }
21     reference_pointer(_RefCounter<T> *t=0):p(t){}
22     p&&+(*p).ref;
23 }
24 reference_pointer(const reference_pointer &t):p(t.p){
25     p&&+(*p).ref;
26 }
27 ~reference_pointer(){
28     if(p&&--(*p).ref==0)delete p;
29 }
30 };
31 template<typename T>
32 inline const reference_pointer<T> new_reference(const T&nd){
33     return reference_pointer<T>(new _RefCounter<T>(nd));
34 }
35 struct P{
36     int a,b;
37     P(int A,int B):a(A),b(B){}

```

```

38 }p(2,3);
39 int main(){
40     reference_pointer<int >b=new_reference(int
41         (5));
42     reference_pointer<int >a=new_reference(*b)
43         ;
44     reference_pointer<P >c=new_reference(p);
45     return 0;
46 }

```

2.6 skew_heap.cpp

```

1 template<typename T,typename _Compare=std::
2     less<T> >
3 class skew_heap{
4     private:
5         struct node{
6             T data;
7             node *l,*r;
8             node(const T&d):data(d),l(0),r(0){}
9             ~node(){delete l,delete r;}
10        }*root;
11        int _size;
12        _Compare cmp;
13        node *merge(node *a,node *b){
14            if(!a||!b)return a?a:b;
15            if(cmp(a->data,b->data))return merge(b,a);
16            node *t=a->r;
17            a->r=a->l;
18            a->l=merge(b,t);
19            return a;
20        }
21        public:
22        skew_heap():root(0),_size(0){}
23        ~skew_heap(){delete root;}
24        void clear(){delete root,root=0,_size=0;}
25        void join(skew_heap &o){
26            root=merge(root,o.root);
27            o.root=0;
28            _size+=o._size;
29            o._size=0;
30        }
31        void swap(skew_heap &o){
32            node *t=root;
33            root=o.root;
34            o.root=t;
35            int st=_size;
36            _size=o._size;
37            o._size=st;
38        }
39        void push(const T&data){
40            _size++;
41            root=merge(root,new node(data));
42        }
43        void pop(){
44            if(_size)_size--;
45            node *tmd=merge(root->l,root->r);
46            root->l=root->r=0;
47            delete root;
48            root=tmd;
49        }

```

2.7 split_merge.cpp

```

49 const T& top(){return root->data;}
50 int size(){return _size;}
51 bool empty(){return !_size;}
52 };
2 void split(node *o,node *a,node *b,int k){
3     if(!o)a=b=0;
4     else{
5         //o=new node(*o);
6         o->down();
7         if(k<=size(o->l)){
8             b=0;
9             split(o->l,a,b->l,k);
10        }else{
11            a=0;
12            split(o->r,a->r,b,k-size(o->l)-1);
13        }
14        o->up();
15    }
16    node *merge(node *a,node *b){
17        if(!a||!b)return a?a:b;
18        static int x;
19        if(x++%(a->s+b->s)<a->s){
20            //a=new node(*a);
21            a->down();
22            a->r=merge(a->r,b);
23            a->up();
24            return a;
25        }else{
26            //b=new node(*b);
27            b->down();
28            b->l=merge(a,b->l);
29            b->up();
30            return b;
31        }
32    }

```

2.8 treap.cpp

```

1 template<typename T>
2 class treap{
3     private:
4         struct node{
5             T data;
6             unsigned fix;
7             int s;
8             node *ch[2];
9             node(const T&d):data(d),s(1){}
10            node():s(0){ch[0]=ch[1]=this;}
11        }*nil,*root;
12        unsigned x;
13        unsigned ran(){return x=x*0xdefaced+1;}
14        void rotate(node *a,bool d){
15            node *b=a;
16            a=a->ch[!d];
17            a->s=b->s;
18            b->ch[!d]=a->ch[d];

```

```

19        a->ch[d]=b;
20        b->s=b->ch[0]->s+b->ch[1]->s+1;
21    }
22    void insert(node *o,const T &data){
23        if(!o->s){
24            o=new node(data),o->fix=ran();
25            o->ch[0]=o->ch[1]=nil;
26        }else{
27            o->s++;
28            bool d=o->data<data;
29            insert(o->ch[d],data);
30            if(o->ch[d]->fix>o->fix)rotate(o,!d);
31        }
32    }
33    node *merge(node *a,node *b){
34        if(!a->s||!b->s)return a->s?a:b;
35        if(a->fix>b->fix){
36            a->ch[1]=merge(a->ch[1],b);
37            a->s=a->ch[0]->s+a->ch[1]->s+1;
38            return a;
39        }else{
40            b->ch[0]=merge(a,b->ch[0]);
41            b->s=b->ch[0]->s+b->ch[1]->s+1;
42            return b;
43        }
44    }
45    bool erase(node *o,const T &data){
46        if(!o->s)return 0;
47        if(o->data==data){
48            node *t=o;
49            o=merge(o->ch[0],o->ch[1]);
50            delete t;
51            return 1;
52        }
53        if(erase(o->ch[o->data<data],data)){
54            o->s--;return 1;
55        }else return 0;
56    }
57    void clear(node *o){
58        if(o->s)clear(o->ch[0]),clear(o->ch[1]),delete o;
59    }
60    public:
61    treap(unsigned s=20150119):nil(new node),root(nil),x(s){}
62    ~treap(){clear(root),delete nil;}
63    void clear(){clear(root),root=nil;}
64    void insert(const T &data){
65        insert(root,data);
66    }
67    bool erase(const T &data){
68        return erase(root,data);
69    }
70    bool find(const T&data){
71        for(node *o=root;o->s;){
72            if(o->data==data)return 1;
73            else o=o->ch[o->data<data];
74            return 0;
75        }
76    }
77    int rank(const T&data){
78        int cnt=0;
79        for(node *o=root;o->s;){
80            if(o->data<data)cnt+=o->ch[0]->s+1,o=o->ch[1];
81            else o=o->ch[0];
82        }

```

```

81        return cnt;
82    }
83    const T&kth(int k){
84        for(node *o=root;){
85            if(k<=o->ch[0]->s)o=o->ch[0];
86            else if(k==o->ch[0]->s+1)return o->data;
87            else k-=o->ch[0]->s+1,o=o->ch[1];
88        }
89    }
90    const T&operator[](int k){
91        return kth(k);
92    }
93    const T&preorder(const T&data){
94        node *x=root,*y=0;
95        while(x->s){
96            if(x->data<data)y=x,x=x->ch[1];
97            else x=x->ch[0];
98            if(y)return y->data;
99        }
100    }
101    const T&successor(const T&data){
102        node *x=root,*y=0;
103        while(x->s){
104            if(data<x->data)y=x,x=x->ch[0];
105            else x=x->ch[1];
106            if(y)return y->data;
107            return data;
108        }
109    }
110    int size(){return root->s;}
111 }

```

2.9 操作分治.cpp

```

1 void dq(int l,int r){
2     if(l==r)return;
3     int mid=(l+r)/2;
4     dq(l,mid);
5     //處理[l,mid]的操作對[mid+1,r]的影響
6     dq(mid+1,r);
7 }

```

2.10 整體二分.cpp

```

1 void BS(int l,int r,vector<Item> &vs){
2     //答案該<l會有的已經做完了
3     if(l==r)整個vs的答案=1;//??????
4     int mid=(l+r)/2;
5     do_thing(l,mid);//做答案<=mid會做的事
6     vector<Item> left=vs裡滿足的;
7     vector<Item> right=vs-left;
8     undo_thing(l,mid);
9     BS(l,mid,left);
10    do_thing(l,mid);
11    BS(mid+1,r,right);//??????
12 }

```

3 default

3.1 debug.cpp

```

1 #ifndef Jinkala
2 #define debug(...) {\
3     fprintf(stderr, "%s - %d : (%s) = ",
4         __PRETTY_FUNCTION__, __LINE__, #
5         __VA_ARGS__); \
6     _DO(__VA_ARGS__); \
7 }
8 template<typename I> void _DO(I&&x){cerr<<x
9     <<endl;}
10 template<typename I, typename...T> void _DO(I
11     &&x, T&&...tail){cerr<<x<<" "; _DO(tail
12     ...);}
13 #else
14 #define debug(...)
15 #endif

```

3.2 IncStack.cpp

```

1 //Magic
2 #pragma GCC optimize "Ofast"
3 //stack resize, change esp to rsp if 64-bit
4 //system
5 asm("mov %0, %%esp\n" :: "g"(mem+1000000));
6 //linux stack resize
7 #include<sys/resource.h>
8 void increase_stack(){
9     const rlim_t ks=64*1024*1024;
10    struct rlimit rl;
11    int res=getrlimit(RLIMIT_STACK, &rl);
12    if(!res&&rl.rlim_cur<ks){
13        rl.rlim_cur=ks;
14        res=setrlimit(RLIMIT_STACK, &rl);
15    }
16 }

```

3.3 input.cpp

```

1 inline int read(){
2     int x=0; bool f=0; char c=getchar();
3     while(ch<'0' || '9'<ch) f|=ch=='-'; ch=
4         getchar();
5     while('0'<=ch&&ch<='9') x=x*10-'0'+ch, ch=
6         getchar();
7     return f?-x:x;
8 }
9 //g++ -std=c++11 -O2 -Wall -Wextra -Wno-
10 unused-variable $1 && ./a.out

```

4 Flow

4.1 dinic.cpp

```

1 #define MAXN 105
2 #define INF INT_MAX
3 int n; /*number of nodes*/
4 int level[MAXN], cur[MAXN]; /*Layer, current
5     arc*/
6 struct edge{
7     int v, pre;
8     long long cap, flow, r;
9     edge(int v, int pre, long long cap):v(v), pre
10         (pre), cap(cap), flow(0), r(cap){}
11 };
12 int g[MAXN];
13 std::vector<edge> e;
14 inline void init(){
15     memset(g, -1, sizeof(int)*(n+1));
16     e.clear();
17 }
18 inline void add_edge(int u, int v, long long
19     cap, bool directed=false){
20     e.push_back(edge(v, g[u], cap));
21     g[u]=e.size()-1;
22     e.push_back(edge(u, g[v], directed?0:cap));
23     g[v]=e.size()-1;
24 }
25 inline int bfs(int s, int t){
26     memset(level, 0, sizeof(int)*(n+1));
27     memcpy(cur, g, sizeof(int)*(n+1));
28     std::queue<int> q;
29     q.push(s);
30     level[s]=1;
31     while(q.size()){
32         int u=q.front(); q.pop();
33         for(int i=g[u]; ~i; i=e[i].pre){
34             if(!level[e[i].v]&&e[i].r){
35                 level[e[i].v]=level[u]+1;
36                 q.push(e[i].v);
37                 if(e[i].v==t) return 1;
38             }
39         }
40     }
41     return 0;
42 }
43 long long dfs(int u, int t, long long cur_flow
44     =INF){
45     if(u==t || !cur_flow) return cur_flow;
46     long long df, tf=0;
47     for(int &i=cur[u]; ~i; i=e[i].pre){
48         if(level[e[i].v]==level[u]+1&&e[i].r){
49             if(df=dfs(e[i].v, t, std::min(cur_flow, e
50                 [i].r))) {
51                 e[i].flow+=df;
52                 e[i^1].flow-=df;
53                 e[i].r-=df;
54                 e[i^1].r+=df;
55                 tf+=df;
56                 if(!cur_flow==df) break;
57             }
58         }
59     }
60     return tf;
61 }

```

```

55 if(!df) level[u]=0;
56 return tf;
57 }
58 inline long long dinic(int s, int t, bool
59     clean=true){
60     if(clean){
61         for(size_t i=0; i<e.size(); ++i){
62             e[i].flow=0;
63             e[i].r=e[i].cap;
64         }
65     }
66     long long ans=0;
67     while(bfs(s, t)) ans+=dfs(s, t);
68     return ans;
69 }

```

4.2 ISAP.cpp

```

1 #define MAXN 105
2 #define INF INT_MAX
3 int n; /*點數*/
4 int d[MAXN], gap[MAXN], cur[MAXN];
5 /*層次、gap[i]=層次為i的點之個數、當前弧優化
6     */
7 struct edge{
8     int v, pre;
9     long long cap, flow, r;
10    edge(int v, int pre, long long cap):v(v), pre
11        (pre), cap(cap), flow(0), r(cap){}
12 };
13 int g[MAXN];
14 std::vector<edge> e;
15 inline void init(){
16     memset(g, -1, sizeof(int)*(n+1));
17     e.clear();
18 }
19 inline void add_edge(int u, int v, long long
20     cap, bool directed=false){
21     e.push_back(edge(v, g[u], cap));
22     g[u]=e.size()-1;
23     e.push_back(edge(u, g[v], directed?0:cap));
24     g[v]=e.size()-1;
25 }
26 long long dfs(int u, int s, int t, long long
27     cur_flow=INF){
28     if(u==t) return cur_flow;
29     long long tf=cur_flow, df;
30     for(int &i=cur[u]; ~i; i=e[i].pre){
31         if(e[i].r&&d[u]==d[e[i].v]+1){
32             df=dfs(e[i].v, s, t, std::min(tf, e[i].r))
33                 ;
34             e[i].flow+=df;
35             e[i^1].flow-=df;
36             e[i].r-=df;
37             e[i^1].r+=df;
38             if(!(tf-=df) || d[s]==n) return cur_flow-
39                 tf;
40         }
41     }
42     int minh=n;
43     for(int i=cur[u]=g[u]; ~i; i=e[i].pre){
44         if(e[i].r&&d[e[i].v]<minh) minh=d[e[i].v]
45             ;
46     }
47 }

```

```

39 }
40 if(!--gap[d[u]]) d[s]=n;
41 else ++gap[d[u]]=++minh;
42 return cur_flow-tf;
43 }
44 inline long long isap(int s, int t, bool clean
45     =true){
46     memset(d, 0, sizeof(int)*(n+1));
47     memset(gap, 0, sizeof(int)*(n+1));
48     memcpy(cur, g, sizeof(int)*(n+1));
49     if(clean){
50         for(size_t i=0; i<e.size(); ++i){
51             e[i].flow=0;
52             e[i].r=e[i].cap;
53         }
54     }
55     long long max_flow=0;
56     for(gap[0]=n; d[s]<n; ) max_flow+=dfs(s, s, t);
57     return max_flow;
58 }

```

4.3 MinCostMaxFlow.cpp

```

1 #define MAXN 440
2 #define INF 999999999
3 struct edge{
4     int v, pre;
5     int cap, cost;
6     edge(int v, int pre, int cap, int cost):v(v),
7         pre(pre), cap(cap), cost(cost){}
8 };
9 int n, S, T;
10 int dis[MAXN], piS, ans;
11 bool vis[MAXN];
12 std::vector<edge> e;
13 int g[MAXN];
14 inline void init(){
15     memset(g, -1, sizeof(int)*n);
16     e.clear();
17 }
18 inline void add_edge(int u, int v, int cost,
19     int cap, bool directed=false){
20     e.push_back(edge(v, g[u], cap, cost));
21     g[u]=e.size()-1;
22     e.push_back(edge(u, g[v], directed?0:cap, -
23         cost));
24     g[v]=e.size()-1;
25 }
26 int augment(int u, int cur_flow){
27     if(u==T || !cur_flow) return ans+=piS*
28         cur_flow, cur_flow;
29     vis[u]=1;
30     int r=cur_flow, d;
31     for(int i=g[u]; ~i; i=e[i].pre){
32         if(e[i].cap&&!e[i].cost&&vis[e[i].v]){
33             d=augment(e[i].v, std::min(r, e[i].cap))
34                 ;
35             e[i].cap-=d;
36             e[i^1].cap+=d;
37             if(!r==d) break;
38         }
39     }
40     return cur_flow-r;
41 }

```

```

36 }
37 inline bool modlabel(){
38     for(int i=0;i<n;++i)dis[i]=INF;
39     dis[T]=0;
40     static std::deque<int>q;
41     q.push_back(T);
42     while(q.size()){
43         int u=q.front();
44         q.pop_front();
45         int dt;
46         for(int i=g[u];~i;i=e[i].pre){
47             if(e[i^1].cap&&(dt=dis[u]-e[i].cost)<
48                 dis[e[i].v]){
49                 if((dis[e[i].v]=dt)<=dis[q.size()>q.
50                     front():S]){
51                     q.push_front(e[i].v);
52                 }else q.push_back(e[i].v);
53             }
54         }
55         for(int u=0;u<n;++u){
56             for(int i=g[u];~i;i=e[i].pre){
57                 e[i].cost+=dis[e[i].v]-dis[u];
58             }
59             piS+=dis[S];
60             return dis[S]<INF;
61         }
62     inline int mincost(){
63         piS=ans=0;
64         while(modlabel()){
65             do memset(vis,0,sizeof(bool)*n);
66             while(augment(S,INF));
67         }
68         return ans;
69     }

```

5 Graph

5.1 Arborescence_EV.cpp

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 struct node {
5     int from, to, cost;
6     node(int from=0,int to=0,int cost=0):
7         from(from),to(to),cost(cost){};
8 } edge[M];
9
10 int m, n, m, c;
11 int far[N], In[N], ID[N], vis[N];
12
13 bool MST(int cost,int n,int root)
14 {
15     long long int ans=0;
16     while(true)
17     {
18         for(int i=0;i<n;++i) IN[i].first =
19             INF;
20         for(int i=0;i<m;++i)

```

```

19         if(edge[i].from!=edge[i].to)
20             IN[edge[i].to] = min(IN[edge
21                 [i].to],make_pair(edge[i
22                 ].cost,edge[i].from));
23         for(int i=0;i<n;++i)
24             if(i!=root && IN[i].first==INF)
25                 return false; // NO
26                 Arborescence
27
28         int cntnode = 0;
29         memset(ID,-1,sizeof(ID));
30         memset(vis,-1,sizeof(vis));
31         In[root] = 0;
32         for(int i=0;i<n;++i) ans += IN[i].
33             first;
34         for(int i=0;i<n;++i) {
35             int x;
36             for(x=i;vis[x]!=i&&ID[x]==-1&&x
37                 !=root;x=IN[x].second)
38                 vis[x] = i;
39             if(ID[x]==-1 && x!=root) {
40                 for(int i=IN[x].second;u!=x;
41                     u=IN[u].second)
42                     ID[u] = cntnode;
43                 ++cntnode;
44             }
45             if(cntnode==0) break; // END
46
47         for(int i=0;i<n;++i)
48             if(ID[i]==-1)
49                 ID[i] = cntnode++;
50
51         for(int i=0;i<m;++i) {
52             int v = edge[i].to;
53             edge[i].from = ID[edge[i].from];
54             edge[i].to = ID[edge[i].to];
55             if(edge[i].from!=edge[i].to)
56                 edge[i].cost -= IN[edge[i].
57                     to].first;
58         }
59         n=cntnode;
60         root=ID[root];
61         return ans<=cost;
62     }

```

5.2 Augmenting_Path.cpp

```

1 #define MAXN1 505
2 #define MAXN2 505
3 int n1,n2; //n1個點連向n2個點*/
4 int match[MAXN2]; //每個屬於n2的點匹配了哪個
5     點*/
6 vector<int> g[MAXN1]; //圖*/
7 bool vis[MAXN2]; //是否走訪過*/
8 bool dfs(int u){
9     for(size_t i=0;i<g[u].size();++i){
10         int v=g[u][i];
11         if(vis[v])continue;
12         vis[v]=1;
13         if(match[v]==-1||dfs(match[v])){

```

```

13         match[v]=u;
14         return 1;
15     }
16     return 0;
17 }
18 inline int max_match(){
19     int ans=0;
20     memset(match,-1,sizeof(int)*n2);
21     for(int i=0;i<n1;++i){
22         memset(vis,0,sizeof(bool)*n2);
23         if(dfs(i))++ans;
24     }
25     return ans;
26 }
27
28 #define MAXN1 1005
29 #define MAXN2 505
30 int n1,n2; //n1個點連向n2個點，其中n2個點可以
31     匹配很多邊
32 vector<int> g[MAXN1]; //圖
33 int c[MAXN2]; //每個屬於n2點最多可以接受幾條
34     匹配邊
35 vector<int> match_list[MAXN2]; //每個屬於n2的
36     點匹配了那些點
37
38 bool vis[MAXN2]; //是否走訪過
39 bool dfs(int u){
40     for(size_t i=0;i<g[u].size();++i){
41         int v=g[u][i];
42         if(vis[v])continue;
43         vis[v]=true;
44         if((int)match_list[v].size()<c[v]){
45             match_list[v].push_back(u);
46             return true;
47         }else{
48             for(size_t j=0;j<match_list[v].size()
49                 ;++j){
50                 int next_u=match_list[v][j];
51                 if(dfs(next_u)){
52                     match_list[v][j]=u;
53                     return true;
54                 }
55             }
56         }
57     }
58     return false;
59 }
60 inline int max_match(){
61     for(int i=0;i<n2;++i)match_list[i].clear()
62         ;
63     int cnt=0;
64     for(int u=0;u<n1;++u){
65         memset(vis,0,sizeof(bool)*n2);
66         if(dfs(u))++cnt;
67     }
68     return cnt;
69 }

```

5.3 Augmenting_Path_multiple

5.4 blossom_matching.cpp

```

1 #define MAXN 505
2 vector<int>g[MAXN];
3 int pa[MAXN],match[MAXN],st[MAXN],S[MAXN],v[
4     MAXN];
5 int t,n;
6 inline int lca(int x,int y){
7     for(++t;swap(x,y)){
8         if(x==0)continue;
9         if(v[x]==t)return x;
10        v[x]=t;
11        x=st[pa[match[x]]];
12    }
13 }
14 #define qpush(x) q.push(x),S[x]=0
15 inline void flower(int x,int y,int l,queue<
16     int> &q){
17     while(st[x]!=1){
18         pa[x]=y;
19         if(S[y==match[x]]==1)qpush(y);
20         st[x]=st[y]=1,x=pa[y];
21     }
22 }
23 inline bool bfs(int x){
24     for(int i=1;i<n;++i)st[i]=i;
25     memset(S+1,-1,sizeof(int)*n);
26     queue<int>q;qqush(x);
27     while(q.size()){
28         x=q.front(),q.pop();
29         for(size_t i=0;i<g[x].size();++i){
30             int y=g[x][i];
31             if(S[y]==-1){
32                 pa[y]=x,S[y]=1;
33                 if(!match[y]){
34                     for(int lst;x;y=lst,x=pa[y])
35                         lst=match[x],match[x]=y,match[y]
36                             =x;
37                     return 1;
38                 }
39                 qqush(match[y]);
40             }else if(!S[y]&&st[y]!=st[x]){
41                 int l=lca(y,x);
42                 flower(y,x,l,q),flower(x,y,l,q);
43             }
44         }
45     }
46     return 0;
47 }
48 inline int blossom(){
49     int ans=0;
50     for(int i=1;i<n;++i)
51         if(!match[i]&&bfs(i))++ans;
52     return ans;
53 }

```

5.5 formula.tex

對於連通圖 G 最大獨立點集的大小設為 $I(G)$ 最大匹配大小設為 $M(G)$ 最小點覆蓋設為 $C_v(G)$ 最小邊覆蓋設為 $C_e(G)$ 對於任意連通圖 $I(G)+C_v(G)=|V|$ $M(G)+C_e(G)=|V|$ 對於連通二分圖 $I(G)=C_v(G)$ $M(G)=C_e(G)$ 最大團 = 補圖的最大獨立集

5.6 graphISO.cpp

```

1 const int MAXN=1005,K=30; //K要夠大
2 const long long A=3,B=11,C=2,D=19,P=0
3 xdefaced;
4 long long f[K+1][MAXN];
5 vector<int> g[MAXN],rg[MAXN];
6 int n;
7 inline void init(){
8     for(int i=0;i<n;++i){
9         f[0][i]=1;
10        g[i].clear();
11        rg[i].clear();
12    }
13    inline void add_edge(int u,int v){
14        g[u].push_back(v);
15        rg[v].push_back(u);
16    }
17    inline long long point_hash(int u){ //O(N)
18        for(int t=1;t<=K;++t){
19            for(int i=0;i<n;++i){
20                f[t][i]=f[t-1][i]*A%P;
21                for(int j:g[i])f[t][i]=(f[t][i]+f[t-1][j]*B%P)%P;
22                for(int j:rg[i])f[t][i]=(f[t][i]+f[t-1][j]*C%P)%P;
23                if(i==u)f[t][i]+=D; //如果圖太大的話，
24                //把這行刪掉，執行一次後f[K]就會是所有點的答案
25                f[t][i]%=P;
26            }
27        }
28        return f[K][u];
29    }
30    inline vector<long long> graph_hash(){
31        vector<long long> ans;
32        for(int i=0;i<n;++i)ans.push_back(
33            point_hash(i)); //O(N^2)
34        sort(ans.begin(),ans.end());
35        return ans;
36    }

```

5.7 KM.cpp

```

1 #define MAXN 100
2 int n;
3 int g[MAXN][MAXN],lx[MAXN],ly[MAXN],slack_y[
4     MAXN];
5 int match_y[MAXN];
6 bool vx[MAXN],vy[MAXN]; //要保證g是完全二分圖
7 bool dfs(int x,bool adjust=1){ //DFS找增廣
8     //路，is=1表示要交換邊
9     if(vx[x])return 0;
10    vx[x]=1;
11    for(int y=0;y<n;++y){
12        if(vy[y])continue;
13        int t=lx[x]+ly[y]-g[x][y];
14        if(t==0){
15            vy[y]=1;

```

```

14        if(match_y[y]==-1||dfs(match_y[y],
15            adjust)){
16            if(adjust)match_y[y]=x;
17            return 1;
18        }else if(slack_y[y]>t)slack_y[y]=t;
19    }
20    return 0;
21 }
22 inline int km(){
23     memset(lx,0,sizeof(int)*n);
24     memset(match_y,-1,sizeof(int)*n);
25     for(int x=0;x<n;++x){
26         lx[x]=0;
27         for(int y=0;y<n;++y){
28             lx[x]=max(lx[x],g[x][y]);
29         }
30     }
31     for(int x=0;x<n;++x){
32         for(int y=0;y<n;++y)slack_y[y]=INT_MAX;
33         memset(vx,0,sizeof(bool)*n);
34         memset(vy,0,sizeof(bool)*n);
35         if(dfs(x))continue;
36         bool flag=1;
37         while(flag){
38             int cut=INT_MAX;
39             for(int y=0;y<n;++y){
40                 if(!vy[y]&&cut>slack_y[y])cut=
41                     slack_y[y];
42             }
43             for(int j=0;j<n;++j){
44                 if(vx[j])lx[j]-=cut;
45                 if(vy[j])ly[j]+=cut;
46                 else slack_y[j]-=cut;
47             }
48             for(int y=0;y<n;++y){
49                 if(!vy[y]&&slack_y[y]==0){
50                     vy[y]=1;
51                     if(match_y[y]==-1||dfs(match_y[y],
52                         0)){
53                         flag=0; //測試成功，有增廣路
54                         break;
55                     }
56                 }
57             }
58             memset(vx,0,sizeof(bool)*n);
59             memset(vy,0,sizeof(bool)*n);
60             dfs(x); //最後要記得將邊翻反轉
61         }
62         int ans=0;
63         for(int y=0;y<n;++y)ans+=g[match_y[y]][y];
64         return ans;
65     }

```

5.8 MaximumClique.cpp

```

1 struct MaxClique{
2     static const int MAXN=105;
3     int N,ans;
4     int g[MAXN][MAXN],dp[MAXN],stk[MAXN][MAXN];

```

```

5     int sol[MAXN],tmp[MAXN]; //sol[0~ans-1]為答案
6     void init(int n){
7         N=n; //0-base
8         memset(g,0,sizeof(g));
9     }
10    void add_edge(int u,int v){
11        g[u][v]=g[v][u]=1;
12    }
13    int dfs(int ns,int dep){
14        if(!ns){
15            if(dep>ans){
16                ans=dep;
17                memcpy(sol,tmp,sizeof tmp);
18                return 1;
19            }else return 0;
20        }
21        for(int i=0;i<ns;++i){
22            if(dep+ns-i==ans)return 0;
23            int u=stk[dep][i],cnt=0;
24            if(dep+dp[u]<=ans)return 0;
25            for(int j=i+1;j<ns;++j){
26                int v=stk[dep][j];
27                if(g[u][v])stk[dep+1][cnt++]=v;
28            }
29            tmp[dep]=u;
30            if(dfs(cnt,dep+1))return 1;
31        }
32        return 0;
33    }
34    int clique(){
35        int u,v,ns;
36        for(ans=0,u=N-1;u>=0;--u){
37            for(ns=0,tmp[0]=u,v=u+1;v<N;++v)
38                if(g[u][v])stk[1][ns++]=v;
39            dfs(ns,1),dp[u]=ans;
40        }
41        return ans;
42    }
43 };

```

5.9 Minimum_General_Weighted

```

1 struct Graph {
2     // Minimum General Weighted Matching (
3     // Perfect Match) 0-base
4     static const int MXN = 105;
5
6     int n, edge[MXN][MXN];
7     int match[MXN],dis[MXN],onstk[MXN];
8     vector<int> stk;
9
10    void init(int _n) {
11        n = _n;
12        for (int i=0; i<n; i++)
13            for (int j=0; j<n; j++)
14                edge[i][j] = 0;
15
16    void add_edge(int u, int v, int w) {
17        edge[u][v] = edge[v][u] = w;
18    }
19
20    bool SPFA(int u){
21        if (onstk[u]) return true;

```

```

20    stk.push_back(u);
21    onstk[u] = 1;
22    for (int v=0; v<n; v++){
23        if (u != v && match[u] != v && !onstk[
24            v]){
25            int m = match[v];
26            if (dis[m] > dis[u] - edge[v][m] +
27                edge[u][v]){
28                dis[m] = dis[u] - edge[v][m] +
29                    edge[u][v];
30                onstk[v] = 1;
31                stk.push_back(v);
32                if (SPFA(m)) return true;
33                stk.pop_back();
34                onstk[v] = 0;
35            }
36        }
37        onstk[u] = 0;
38        stk.pop_back();
39        return false;
40    }
41    int solve() {
42        // find a match
43        for (int i=0; i<n; i+=2){
44            match[i] = i+1;
45            match[i+1] = i;
46        }
47        for(;;){
48            int found = 0;
49            for (int i=0; i<n; i++){
50                dis[i] = onstk[i] = 0;
51                for (int i=0; i<n; i++){
52                    stk.clear();
53                    if (!onstk[i] && SPFA(i)){
54                        found = 1;
55                        while (stk.size())>=2){
56                            int u = stk.back(); stk.pop_back
57                                ();
58                            int v = stk.back(); stk.pop_back
59                                ();
60                            match[u] = v;
61                            match[v] = u;
62                        }
63                    }
64                    if (!found) break;
65                }
66                int ret = 0;
67                for (int i=0; i<n; i++){
68                    ret += edge[i][match[i]];
69                }
70                ret /= 2;
71                return ret;
72            }
73        }
74    }
75 }graph;

```

5.10 Rectilinear_Steiner_tree.c

```

1 //平面曼哈頓最小生成樹構造圖(去除非必要邊)
2 #include<vector>
3 #include<algorithm>
4 #define T int

```

```

5 #define INF 0x3f3f3f3f
6 struct point{
7     T x,y;
8     int id;//每個點的編號都要不一樣，從0開始編號
9     point(){}
10    T dist(const point &p)const{
11        return std::abs(x-p.x)+std::abs(y-p.y);
12    }
13 };
14 inline bool cmpx(const point &a,const point &b){
15     return a.x<b.x||(a.x==b.x&&a.y<b.y);
16 }
17 struct edge{
18     int u,v;
19     T cost;
20     edge(int u,int v,const T&c):u(u),v(v),cost(c){}
21     bool operator<(const edge&e)const{
22         return cost<e.cost;
23     }
24 };
25 struct bit_node{
26     T mi;
27     int id;
28     bit_node(const T&mi=INF,int id=-1):mi(mi),id(id){}
29 };
30 std::vector<bit_node> bit;
31 inline void bit_update(int i,const T&data, int id){
32     for(;;i=i&(-i)){
33         if(data<bit[i].mi)bit[i]=bit_node(data,id);
34     }
35 }
36 inline int bit_find(int i,int m){
37     bit_node x;
38     for(;;i=i&(-i)){
39         if(bit[i].mi<x.mi)x=bit[i];
40     }
41     return x.id;
42 }
43 inline std::vector<edge> build_graph(int n, point p[]){
44     std::vector<edge> e;//回傳的邊就可以用來求最小生成樹
45     for(int dir=0;dir<4;dir++){//4種座標交換
46         if(dir%2){
47             for(int i=0;i<n;i++)std::swap(p[i].x,p[i].y);
48         }else if(dir==2){
49             for(int i=0;i<n;i++)p[i].x=-p[i].x;
50         }
51         std::sort(p,p+n,cmpx);
52         std::vector<T>ga(n),gb;
53         for(int i=0;i<n;i++)ga[i]=p[i].y-p[i].x;
54         gb=ga;
55         std::sort(gb.begin(),gb.end());
56         gb.resize(std::unique(gb.begin(),gb.end())-gb.begin());
57         int m=gb.size();
58         bit=std::vector<bit_node>(m+1);
59         for(int i=n-1;i>0;--i){

```

```

60         int pos=std::lower_bound(gb.begin(),gb.end(),ga[i])-gb.begin()+1;
61         int ans=bit_find(pos,m);
62         if(~ans)e.push_back(edge(p[i].id,p[ans].id,p[i].dist(p[ans])));
63         bit_update(pos,p[i].x+p[i].y,i);
64     }
65 }
66 return e;
67 }

```

5.11 treeISO.cpp

```

1 const int MAXN=100005;
2 const long long X=12327,P=0xdefaced;
3 vector<int> g[MAXN];
4 bool vis[MAXN];
5 long long dfs(int u){
6     vis[u]=1;
7     vector<long long> tmp;
8     for(auto v:g[u])if(!vis[v])tmp.push_back(dfs(v));
9     if(tmp.empty())return 177;
10    long long ret=4931;
11    sort(tmp.begin(),tmp.end());
12    for(auto v:tmp)ret=((ret*X)^v)%P;
13    return ret;
14 }

```

5.12 一般圖最大權匹配.cpp

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define INF INT_MAX
4 #define MAXN 400
5 struct edge{
6     int u,v,w;
7     edge(){}
8     edge(int u,int v,int w):u(u),v(v),w(w){}
9 };
10 int n,n_x;
11 edge g[MAXN*2+1][MAXN*2+1];
12 int lab[MAXN*2+1];
13 int match[MAXN*2+1],slack[MAXN*2+1],st[MAXN*2+1],pa[MAXN*2+1];
14 int flower_from[MAXN*2+1][MAXN+1],S[MAXN*2+1],vis[MAXN*2+1];
15 vector<int> flower[MAXN*2+1];
16 queue<int> q;
17 inline int e_delta(const edge &e){ // does not work inside blossoms
18     return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
19 }
20 inline void update_slack(int u,int x){
21     if(!slack[x]||e_delta(g[u][x])<e_delta(g[slack[x]][x]))slack[x]=u;
22 }
23 inline void set_slack(int x){
24     slack[x]=0;
25     for(int u=1;u<n;u++){

```

```

26     if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)update_slack(u,x);
27 }
28 void q_push(int x){
29     if(x<n)q.push(x);
30     else for(size_t i=0;i<flower[x].size();i++)q_push(flower[x][i]);
31 }
32 inline void set_st(int x,int b){
33     st[x]=b;
34     if(x>n)for(size_t i=0;i<flower[x].size();i++){
35         set_st(flower[x][i],b);
36     }
37 inline int get_pr(int b,int xr){
38     int pr=find(flower[b].begin(),flower[b].end(),xr)-flower[b].begin();
39     if(pr%2==1){//檢查他在前一層圖是奇點還是偶點
40         reverse(flower[b].begin()+1,flower[b].end());
41         return (int)flower[b].size()-pr;
42     }else return pr;
43 }
44 inline void set_match(int u,int v){
45     match[u]=g[u][v].v;
46     if(u>n){
47         edge e=g[u][v];
48         int xr=flower_from[u][e.u],pr=get_pr(u,xr);
49         for(int i=0;i<pr;i++)set_match(flower[u][i],flower[u][i^1]);
50         set_match(xr,v);
51         rotate(flower[u].begin(),flower[u].begin()+pr,flower[u].end());
52     }
53 }
54 inline void augment(int u,int v){
55     for(;;){
56         int xnv=st[match[u]];
57         set_match(u,v);
58         if(!xnv)return;
59         set_match(xnv,st[pa[xnv]]);
60         u=st[pa[xnv]],v=xnv;
61     }
62 }
63 inline int get_lca(int u,int v){
64     static int t=0;
65     for(++t;u||v;swap(u,v)){
66         if(u==0)continue;
67         if(vis[u]==t)return u;
68         vis[u]=t;//這種方法可以不用清空v陣列
69         u=st[match[u]];
70         if(u)u=st[pa[u]];
71     }
72     return 0;
73 }
74 inline void add_blossom(int u,int lca,int v){
75     int b=n+1;
76     while(b<=n_x&&st[b]==b)b++;
77     if(b>n_x)b=n_x;
78     lab[b]=0,S[b]=0;
79     match[b]=match[lca];
80     flower[b].clear();

```

```

81     flower[b].push_back(lca);
82     for(int x=u,y;lca;x=st[pa[y]])
83         flower[b].push_back(x),flower[b].push_back(y=st[match[x]]),q_push(y);
84     reverse(flower[b].begin()+1,flower[b].end());
85     for(int x=v,y;lca;x=st[pa[y]])
86         flower[b].push_back(x),flower[b].push_back(y=st[match[x]]),q_push(y);
87     set_st(b,b);
88     for(int x=1;x<=n_x;x++)g[b][x].w=g[x][b].w=0;
89     for(int x=1;x<=n;u++)flower_from[b][x]=0;
90     for(size_t i=0;i<flower[b].size();i++){
91         int xs=flower[b][i];
92         for(int x=1;x<=n_x;x++){
93             if(g[b][x].w==0||e_delta(g[xs][x])<e_delta(g[b][x]))
94                 g[b][x]=g[xs][x],g[x][b]=g[x][xs];
95         }
96         if(flower_from[xs][x])flower_from[b][x]=xs;
97     }
98     set_slack(b);
99 }
100 inline void expand_blossom(int b){ // S[b]==1
101     for(size_t i=0;i<flower[b].size();i++){
102         set_st(flower[b][i],flower[b][i]);
103         int xr=flower_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
104         for(int i=0;i<pr;i+=2){
105             int xs=flower[b][i],xns=flower[b][i+1];
106             pa[xs]=g[xns][xs].u;
107             S[xs]=1,S[xns]=0;
108             slack[xs]=0,set_slack(xns);
109             q_push(xns);
110         }
111         S[xr]=1,pa[xr]=pa[b];
112         for(size_t i=pr+1;i<flower[b].size();i++){
113             int xs=flower[b][i];
114             S[xs]=-1,set_slack(xs);
115         }
116         st[b]=0;
117     }
118     inline bool on_found_edge(const edge &e){
119         int u=st[e.u],v=st[e.v];
120         if(S[v]==-1){
121             pa[v]=e.u,S[v]=1;
122             int nu=st[match[v]];
123             slack[v]=slack[nu]=0;
124             S[nu]=0,q_push(nu);
125         }else if(S[v]==0){
126             int lca=get_lca(u,v);
127             if(!lca){
128                 augment(u,v),augment(v,u);
129                 return true;
130             }else add_blossom(u,lca,v);
131         }
132         return false;
133     }
134     inline bool matching(){
135         memset(S+1,-1,sizeof(int)*n_x);
136         memset(slack+1,0,sizeof(int)*n_x);
137         q=queue<int>();
138         for(int x=1;x<=n_x;x++){

```

```

139 if(st[x]==x&&!match[x])pa[x]=0,S[x]=0,
    q_push(x);
140 if(q.empty())return false;
141 for(;;){
142     while(q.size()){
143         int u=q.front();q.pop();
144         if(S[st[u]]==1)continue;
145         for(int v=1;v<=n;v++){
146             if(g[u][v].w>0&&st[u]!=st[v]){
147                 if(e_delta(g[u][v])==0){
148                     if(on_found_edge(g[u][v]))return
149                         true;
150                 }else update_slack(u,st[v]);
151             }
152             int d=INF;
153             for(int b=n+1;b<=n_x;v++){
154                 if(st[b]==b&&S[b]==1)d=min(d,lab[b]/2);
155             }
156             for(int x=1;x<=n_x;v++){
157                 if(st[x]==x&&slack[x]){
158                     if(S[x]==-1)d=min(d,e_delta(g[slack[x]]
159                         [x]));
160                     else if(S[x]==0)d=min(d,e_delta(g[
161                         slack[x]][x])/2);
162                 }
163             }
164             for(int u=1;u<=n;v++){
165                 if(S[st[u]]==0){
166                     if(lab[u]<=d)return 0;
167                     lab[u]=d;
168                 }else if(S[st[u]]==1)lab[u]+=d;
169             }
170             for(int b=n+1;b<=n_x;v++){
171                 if(st[b]==b){
172                     if(S[st[b]]==0)lab[b]+=d*2;
173                     else if(S[st[b]]==1)lab[b]-=d*2;
174                 }
175             }
176             q=queue<int>();
177             for(int x=1;x<=n_x;v++){
178                 if(st[x]==x&&slack[x]&&st[slack[x]]!=x
179                     &&e_delta(g[slack[x]][x])==0)
180                 if(on_found_edge(g[slack[x]][x]))
181                     return true;
182             }
183             for(int b=n+1;b<=n_x;v++){
184                 if(st[b]==b&&S[b]==1&&lab[b]==0)
185                     expand_blossom(b);
186             }
187             return false;
188         }
189     }
190 }
191 inline pair<long long,int> weight_blossom(){
192     memset(match+1,0,sizeof(int)*n);
193     n_x=n;
194     int n_matches=0;
195     long long tot_weight=0;
196     for(int u=0;u<=n;v++){
197         st[u]=u,flower[u].
198         clear();
199     }
200     int w_max=0;
201     for(int u=1;u<=n;v++){
202         for(int v=1;v<=n;v++){
203             flower_from[u][v]=(u==v?0:0);
204             w_max=max(w_max,g[u][v].w);
205         }
206     }
207     for(int u=1;u<=n;v++){
208         lab[u]=w_max;
209         while(matching())n_matches++;
210     }
211     for(int u=1;u<=n;v++){
212         if(match[u]&&match[u]<u)

```

```

196     tot_weight+=g[u][match[u]].w;
197     return make_pair(tot_weight,n_matches);
198 }
199 inline void init_weight_graph(){
200     for(int u=1;u<=n;v++){
201         for(int v=1;v<=n;v++){
202             g[u][v]=edge(u,v,0);
203         }
204     }
205     int main(){
206         int m;
207         scanf("%d%d",&n,&m);
208         init_weight_graph();
209         for(int i=0;i<=m;v++){
210             int u,v,w;
211             scanf("%d%d%d",&u,&v,&w);
212             g[u][v].w=g[v][u].w=w;
213         }
214         printf("%Lld\n",weight_blossom().first);
215         for(int u=1;u<=n;v++){
216             puts("");
217         }
218         return 0;
219     }

```

6 language

6.1 CNF.cpp

```

1 #define MAXN 55
2 struct CNF{
3     int s,x,y;//s->xy | s->x, if y==1
4     int cost;
5     CNF(){}
6     CNF(int s,int x,int y,int c):s(s),x(x),y(y)
7         ,cost(c){}
8 };
9 int state;//規則數量
10 map<char,int> rule;//每個字元對應到的規則
11 小寫字母為終端字元
12 vector<CNF> cnf;
13 inline void init(){
14     state=0;
15     rule.clear();
16     cnf.clear();
17 }
18 inline void add_to_cnf(char s,const string &
19     p,int cost){
20     //加入一個s -> <p>的文法，代價為cost
21     if(rule.find(s)==rule.end())rule[s]=state
22         ++;
23     for(auto c:p)if(rule.find(c)==rule.end())
24         rule[c]=state++;
25     if(p.size()==1){
26         cnf.push_back(CNF(rule[s],rule[p[0]],-1,
27             cost));
28     }else{
29         int left=rule[s];
30         int sz=p.size();
31         for(int i=0;i<sz-2;v++){
32             cnf.push_back(CNF(left,rule[p[i]],
33                 state,0));
34         }
35     }
36 }

```

```

27     left=state++;
28 }
29 cnf.push_back(CNF(left,rule[p[sz-2]],
30     rule[p[sz-1]],cost));
31 }
32 vector<long long> dp[MAXN][MAXN];
33 vector<bool> neg_INF[MAXN][MAXN];//如果花費
34 是負的可能會有無限小的情形
35 inline void relax(int l,int r,const CNF &c,
36     long long cost,bool neg_c=0){
37     if(!neg_INF[l][r][c.s]&&(neg_INF[l][r][c.x]
38         ||cost<dp[l][r][c.s])){
39         if(neg_c||neg_INF[l][r][c.x]){
40             dp[l][r][c.s]=0;
41             neg_INF[l][r][c.s]=true;
42         }else dp[l][r][c.s]=cost;
43     }
44     inline void bellman(int l,int r,int n){
45         for(int k=1;k<=state;v++){
46             for(auto c:cnf)
47                 if(c.y==1)relax(l,r,c,dp[l][r][c.x]+c
48                     .cost,k==n);
49         }
50     }
51     inline void cyk(const vector<int> &tok){
52         for(int i=0;i<(int)tok.size();v++){
53             for(int j=0;j<(int)tok.size();v++){
54                 dp[i][j]=vector<long long>(state+1,
55                     INT_MAX);
56                 neg_INF[i][j]=vector<bool>(state+1,
57                     false);
58             }
59             dp[i][i][tok[i]]=0;
60             bellman(i,i,tok.size());
61         }
62     }
63     for(int r=1;r<(int)tok.size();v++){
64         for(int l=r-1;l>=0;v++){
65             for(int k=1;k<=r;v++){
66                 for(auto c:cnf)
67                     if(~c.y)relax(l,r,c,dp[l][k][c.x]+
68                         dp[k+1][r][c.y]+c.cost);
69                 bellman(l,r,tok.size());
70             }
71         }
72     }
73 }

```

6.2 earley.cpp

```

1 struct Rule{
2     vector<vector<Rule*> > p;
3     void add(const vector<Rule*> &l){
4         p.push_back(l);
5     }
6 };
7 map<string,Rule*> NameRule;
8 map<Rule*,string> RuleName;
9 inline void init_Rule(){
10     for(auto r:RuleName)delete r.first;
11     RuleName.clear();
12     NameRule.clear();
13 }

```

```

14 inline Rule *add_rule(const string &s){
15     if(NameRule.find(s)!=NameRule.end())return
16         NameRule[s];
17     Rule *r=new Rule();
18     RuleName[r]=s;
19     NameRule[s]=r;
20     return r;
21 }
22 typedef vector<Rule*> production;
23 struct State{
24     Rule *r;
25     int rid,dot_id,start,end;
26     State(Rule *r,int rid,int dot,int start):r(
27         r),rid(rid),dot_id(dot),start(start),
28         end(-1){}
29     State(Rule *r=0,int col=0):r(r),rid(-1),
30         dot_id(-1),start(-1),end(col){}
31     bool completed()const{
32         return rid==1||dot_id==(int)r->p[rid].
33             size();
34     }
35     Rule *next_term()const{
36         if(completed())return 0;
37         return r->p[rid][dot_id];
38     }
39 }
40 bool operator<(const State& b)const{
41     if(start!=b.start)return start<b.start;
42     if(dot_id!=b.dot_id)return dot_id<b.
43         dot_id;
44     if(r!=b.r)return r<b.r;
45     return rid<b.rid;
46 }
47 void print()const{
48     cout<<RuleName[r]<<"-";
49     if(rid!=-1)for(size_t i=0;v++){
50         if((int)i==dot_id)cout<<" "<<"$";
51         if(i==r->p[rid].size())break;
52         cout<<" "<<RuleName[r->p[rid][i]];
53     }
54     cout<<" "<<"["<<start<<","<<end<<"]<<
55         endl;
56 }
57 }
58 struct Column{
59     Rule *term;
60     string value;
61     vector<State> s;
62     map<State,set<pair<State,State> > > div;
63     //div比較像一棵 左右兄子的樹
64     Column(Rule *r,const string &s):term(r),
65         value(s){}
66     Column(){}
67     bool add(const State &st,int col){
68         if(div.find(st)==div.end()){
69             div[st];
70             s.push_back(st);
71             s.back().end=col;
72             return true;
73         }else return false;
74     }
75 }
76 inline vector<Column> lexer(string text){
77     //tokenize，要自己寫，以下為範例
78     //他會把 input stream 變成 token stream
79     就是 (terminal,value)pair

```

```

70 vector<Column> token;
71 replace(text.begin(),text.end(),',',' ');
72 stringstream ss(text);
73 while(ss>>text){
74     if(text=="a"||text=="of")continue;
75     if(text=="List"){
76         token.push_back(Column(NameRule["(",",",
77             ")"]);
78     }else if(text=="and"){
79         token.push_back(Column(NameRule["(","),",
80             ")"]);
81     }else token.push_back(Column(NameRule["T",
82         ""],text));
83 }
84 return token;
85 }
86 vector<Column> table;
87 inline void predict(int col,Rule *rul){
88     for(size_t i=0;i<rul->p.size();++i){
89         table[col].add(State(rul,i,0,col),col);
90     }
91 }
92 inline void scan(int col,const State &s,Rule
93     *r){
94     if(r!=table[col].term)return;
95     State ns(s.r,s.rid,s.dot_id+1,s.start);
96     table[col].add(ns,col);
97     table[col].div[ns].insert(make_pair(s,
98         State(r,col)));
99 }
100 inline void complete(int col,const State &s)
101 {
102     for(size_t i=0;i<table[s.start].s.size()
103         ;++i){
104         State &st=table[s.start].s[i];
105         Rule *term=st.next_term();
106         if(!term||term->p.size()==0)continue;
107         if(term==s.r){
108             State nst(st.r,st.rid,st.dot_id+1,st.
109                 start);
110             table[col].add(nst,col);
111             table[col].div[nst].insert(make_pair(
112                 st,s));
113         }
114     }
115 }
116 inline pair<bool,State> parse(Rule *GAMMA,
117     const vector<Column> &token){
118     table.resize(token.size()+1);
119     for(size_t i=0;i<token.size();++i)table[i
120         +1]=Column(token[i]);
121     table[0]=Column();
122     table[0].add(State(GAMMA,0,0,0),0);
123     for(size_t i=0;i<table.size();++i){
124         for(size_t j=0;j<table[i].s.size();++j){
125             State state=table[i].s[j];
126             if(state.completed())complete(i,state)
127             ;
128         }
129         Rule *term=state.next_term();
130         if(term->p.size())predict(i,term);
131         else if(i+1<table.size())scan(i+1,
132             state,term);
133     }
134 }
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```

7 Number_Theory

7.1 basic.cpp

```

1 typedef long long int LL;
2 template<typename T>
3 void gcd(const T &a,const T &b,T &d,T &x,T &y){
4     if(!b) d=a,x=1,y=0;
5     else gcd(b,a%b,d,y,x), y-=x*(a/b);
6 }
7
8 const int MAXPRIME = 1000000;
9 int iscom[MAXPRIME], prime[MAXPRIME],
10 primecnt;
11 int phi[MAXPRIME], mu[MAXPRIME];
12 void sieve(void)
13 {
14     memset(iscom,0,sizeof(iscom));
15     primecnt = 0;
16     phi[1] = mu[1] = 1;
17     for(int i=2;i<MAXPRIME;++i) {
18         if(!iscom[i]) {
19             prime[primecnt++] = i;
20             mu[i] = -1;
21             phi[i] = i-1;
22         }
23         for(int j=0;j<primecnt;++j) {
24             int k = i * prime[j];
25             if(k>MAXPRIME) break;
26             iscom[k] = prime[j];
27             if(i%prime[j]==0) {
28                 mu[k] = 0;
29                 phi[k] = phi[i] * prime[j];
30                 break;
31             } else {
32                 mu[k] = -mu[i];
33                 phi[k] = phi[i] * (prime[j]
34                     -1);
35             }
36         }
37     }
38 }
39
40 bool g_test(const LL &g, const LL &p, const
41     vector<LL> &v) {
42     for(int i=0;i<v.size();++i)
43         if(modexp(g,(p-1)/v[i],p)==1)
44             return false;
45     return true;
46 }
47
48 LL primitive_root(const LL &p) {
49     if(p==2) return 1;
50     vector<LL> v;
51     Factor(p-1,v);
52     v.erase(unique(v.begin(), v.end()), v.
53         end());
54     for(LL g=2;g<p;++g)
55         if(g_test(g,p,v))
56             return g;
57     puts("primitive_root NOT FOUND");
58     return -1;
59 }
60
61 int Legendre(const LL &a, const LL &p) {
62     return modexp(a%p,(p-1)/2,p);
63 }
64
65 LL inv(const LL &a, const LL &n) {
66     LL d,x,y;
67     gcd(a,n,d,x,y);
68     return d==1 ? (x+n)%n : -1;
69 }
70
71 LL log_mod(const LL &a, const LL &b, const
72     LL &p) {
73     // a ^ x = b ( mod p )
74     int m=sqrt(p+.5), e=1;
75     LL v=inv(modexp(a,m,p), p);
76     map<LL,int> x;
77     x[1]=0;
78     for(int i=1;i<m;++i) {
79         e = LLMul(e,a,p);
80         if(!x.count(e)) x[e] = i;
81     }
82     for(int i=0;i<m;++i) {
83         if(x.count(b)) return i*m + x[b];
84         b = LLMul(b,v,p);
85     }
86     return -1;
87 }
88
89 LL Tonelli_Shanks(const LL &n, const LL &p)
90 {
91     // x^2 = n ( mod p )
92     if(n==0) return 0;
93     if(Legendre(n,p)!=1) while(1) { puts("
94         SQRT ROOT does not exist"); }
95     int S = 0;
96     LL Q = p-1;
97     while( !(Q&1) ) { Q>>=1; ++S; }
98     if(S==1) return modexp(n%p,(p+1)/4,p);
99     LL z = 2;
100     for(; Legendre(z,p)!=-1;++z)
101         LL c = modexp(z,Q,p);
102 }

```



```

92 LL R = modexp(n%p, (Q+1)/2, p), t = modexp
    (n%p, Q, p);
93 int M = S;
94 while(1) {
95     if(t==1) return R;
96     LL b = modexp(c, 1L<<(M-i-1), p);
97     R = LLMul(R, b, p);
98     t = LLMul(LLMul(b, b, p), t, p);
99     c = LLMul(b, b, p);
100    M = i;
101 }
102 return -1;
103 }

```

7.2 bit_set.cpp

```

1 void sub_set(int S){
2     int sub=S;
3     do{
4         //對某集合的子集合的處理
5         sub=(sub-1)&S;
6     }while(sub!=S);
7 }
8 void k_sub_set(int k, int n){
9     int comb=(1<<k)-1, S=1<<n;
10    while(comb<S){
11        //對大小為k的子集合的處理
12        int x=comb&-comb, y=comb+x;
13        comb=((comb&-y)/x>>1)|y;
14    }
15 }

```

7.3 cantor_expansion.cpp

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define MAXN 11
4 int factorial[MAXN];
5 inline void init(){
6     factorial[0]=1;
7     for(int i=1; i<=MAXN; ++i) factorial[i]=
        factorial[i-1]*i;
8 }
9 inline int encode(const std::vector<int> &s)
10 {
11     int n=s.size(), res=0;
12     for(int i=0; i<n; ++i){
13         int t=0;
14         for(int j=i+1; j<n; ++j)
15             if(s[j]<s[i]) ++t;
16         res+=t*factorial[n-i-1];
17     }
18     return res;
19 }
20 inline std::vector<int> decode(int a, int n){
21     std::vector<int> res;
22     std::vector<bool> vis(n, 0);
23     for(int i=n-1; i>=0; --i){
24         int t=a/factorial[i], j;

```

```

24     for(j=0; j<n; ++j)
25         if(!vis[j]){
26             if(t==0) break;
27             --t;
28         }
29     res.push_back(j);
30     vis[j]=1;
31     a%=factorial[i];
32 }
33 return res;
34 }
35 int main(){
36     init();
37     vector<int> p={0,1,2,3,4,5,6,7,8};
38     for(int i=0; i<factorial[9]; ++i){
39         vector<int> s=decode(i, 9);
40         if(s!=p) puts("XX");
41         next_permutation(p.begin(), p.end());
42     }
43     return 0;
44 }

```

7.4 Chinese_remainder_theorem

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #ifndef CHINESE_REMAINDER_THEOREM
4 #define CHINESE_REMAINDER_THEOREM
5 template<typename T>
6 inline T Euler(T n){
7     T ans=n;
8     for(T i=2; i*i<=n; ++i){
9         if(n%i==0){
10            ans=ans/i*(i-1);
11            while(n%i==0) n/=i;
12        }
13    }
14    if(n>1) ans=ans*n*(n-1);
15    return ans;
16 }
17 template<typename T>
18 inline T pow_mod(T n, T k, T m){
19     T ans=1;
20     for(n=(n>=m?n%m:n); k>=1){
21         if(k&1) ans=ans*n%m;
22         n=n*n%m;
23     }
24     return ans;
25 }
26 template<typename T>
27 inline T crt(std::vector<T> &m, std::vector<T>
    &a){
28     T M=1, tM, ans=0;
29     for(int i=0; i<(int)m.size(); ++i) M*=m[i];
30     for(int i=0; i<(int)a.size(); ++i){
31         tM=M/m[i];
32         ans=(ans+(a[i]*tM%M)*pow_mod(tM, Euler(m[
33             i])-1, m[i]))%M;
34     }
35     /*如果m[i]是質數 · Euler(m[i])-1=m[i]-2 ·
        就不用算Euler了*/
36     return ans;
37 }

```

```

36 }
37 #endif
38 int n;
39 vector<long long> a, m;
40 int main(){
41     while(~scanf("%d", &n)){
42         for(int i=0; i<n; ++i){
43             long long x, y;
44             scanf("%lld%lld", &x, &y);
45             m.push_back(x);
46             a.push_back(y);
47         }
48         long long ans=crt(m, a);
49         printf("%lld\n", ans);
50         for(int i=0; i<n; ++i) printf("%lld %lld\n",
            m[i], ans%m[i]);
51         m.clear();
52         a.clear();
53     }
54     return 0;
55 }
56 /*
57 4
58 199 198
59 200 199
60 201 197
61 137 88
62 2
63 265163 465
64 66546165 7122
65 5
66 379 46
67 853 852
68 971 777
69 659 128
70 281 256
71 4
72 6359 1
73 4877 5
74 1627 6
75 8941 7122
76 */

```

7.5 enumerate.cpp

```

1 void all_divdown(const LL &n) { // all n/x
2     for(LL a=1; a<=n; a=n/(n/(a+1))) {
3         // dosomething;
4     }
5 }

```

7.6 eulerphi.cpp

```

1 int eulerPhi(int n){
2     int m = sqrt(n+0.5);
3     int res=n;
4     for(int i=2; i<=m; ++i){
5         if(n%i==0){
6             res = res*(i-1)/i;
7             while(n%i==0) n/=i;

```

```

8     }
9 }
10 if(n>1) res = res*(n-1)/n;
11 return res;
12 }
13 vector<int> phiTable(int n){
14     vector<int> phi(n+1, 0);
15     phi[1] = 1;
16     for(int i=2; i<=n; ++i) if(!phi[i])
17         for(int j=i; j<=n; j+=i){
18             if(!phi[j]) phi[j] = j;
19             phi[j] = phi[j]*(i-1)/i;
20         }
21     return phi;
22 }
23 }

```

7.7 Factor.cpp

```

1 LL LLMul(LL a, LL b, const LL &mod) {
2     LL ans=0;
3     while(b) {
4         if(b&1) {
5             ans+=a;
6             if(ans>=mod) ans-=mod;
7         }
8         a<<=1, b>>=1;
9         if(a>=mod) a-=mod;
10    }
11    return ans;
12 }
13 inline long long mod_mul(long long a, long
    long b, long long m){
14     a%=m, b%=m;
15     long long y=(long long)((double)a*b/m+0.5)
        ;/* fast for m < 2^58 */
16     long long r=(a*b-y*m)%m;
17     return r<0?r+m:r;
18 }
19 template<typename T>
20 inline T pow(T a, T b, T mod){ // a^b%mod
21     T ans=1;
22     for(; b; b=mod_mul(a, a, mod), b>>=1)
23         if(b&1) ans=mod_mul(ans, a, mod);
24     return ans;
25 }
26 int sprp[3]={2, 7, 61}; //int範圍可解
27 int llsp[7]={2, 325, 9375, 28178, 450775, 9780504, 17952650}
    ;//至少unsigned long long範圍
28 template<typename T>
29 inline bool isprime(T n, int *sprp, int num){
30     if(n==2) return 1;
31     if(n<2 || n%2==0) return 0;
32     int t=0;
33     T u=n-1;
34     for(; u%2==0; ++t) u>>=1;
35     for(int i=0; i<num; ++i){
36         T a=sprp[i]%n;
37         if(a==0 || a==1 || a==n-1) continue;
38         T x=pow(a, u, n);
39         if(x==1 || x==n-1) continue;

```

```

40 for(int j=0;j<t;++j){
41     x=mod_mul(x,x,n);
42     if(x==1)return 0;
43     if(x==n-1)break;
44 }
45 if(x==n-1)continue;
46 return 0;
47 }
48 return 1;
49 }
50 LL func(const LL n,const LL mod,const int c)
51 {
52     return (LLmul(n,n,mod)+c+mod)%mod;
53 }
54 LL pollorroho(const LL n, const int c) { //循環
55     環節長度
56     LL a=1, b=1;
57     a=func(a,n,c)%n;
58     b=func(b,n,c)%n; b=func(b,n,c)%n;
59     while(gcd(abs(a-b),n)==1) {
60         a=func(a,n,c)%n;
61         b=func(b,n,c)%n; b=func(b,n,c)%n;
62     }
63     return gcd(abs(a-b),n);
64 }
65 void prefactor(LL &n, vector<LL> &v) {
66     for(int i=0;i<12;++i) {
67         while(n%prime[i]==0) {
68             v.push_back(prime[i]);
69             n/=prime[i];
70         }
71     }
72 }
73 void smallfactor(LL n, vector<LL> &v) {
74     if(n<MAXPRIME) {
75         while(isp[(int)n]) {
76             v.push_back(isp[(int)n]);
77             n/=isp[(int)n];
78         }
79     }
80     v.push_back(n);
81 } else {
82     for(int i=0;i<primecnt&&prime[i]*
83         prime[i]<=n;++i) {
84         while(n%prime[i]==0) {
85             v.push_back(prime[i]);
86             n/=prime[i];
87         }
88     }
89     if(n!=1) v.push_back(n);
90 }
91 }
92 void comfactor(const LL &n, vector<LL> &v) {
93     if(n<1e9) {
94         smallfactor(n,v);
95         return;
96     }
97     if(Isprime(n)) {
98         v.push_back(n);
99         return;
100 }
101 }

```

```

102 LL d;
103 for(int c=3;++c) {
104     d = pollorroho(n,c);
105     if(d!=n) break;
106 }
107 comfactor(d,v);
108 comfactor(n/d,v);
109 }
110 void Factor(const LL &x, vector<LL> &v) {
111     LL n = x;
112     if(n==1) { puts("Factor 1"); return; }
113     prefactor(n,v);
114     if(n==1) return;
115     comfactor(n,v);
116     sort(v.begin(),v.end());
117 }
118 void AllFactor(const LL &n,vector<LL> &v) {
119     vector<LL> tmp;
120     Factor(n,tmp);
121     v.clear();
122     v.push_back(1);
123     int len;
124     LL now=1;
125     for(int i=0;i<tmp.size();++i) {
126         if(i==0 || tmp[i]!=tmp[i-1]) {
127             len = v.size();
128             now = 1;
129         }
130         now*=tmp[i];
131         for(int j=0;j<len;++j)
132             v.push_back(v[j]*now);
133     }
134 }
135 }
136 }

```

7.8 FFT.cpp

```

1 template<typename T,typename VT=std::vector<
2     std::complex<T> > >
3 struct FFT{
4     const T pi;
5     FFT(const T pi=acos((T)-1)):pi(pi){}
6     unsigned int bit_reverse(unsigned int a,
7         int len){
8         a=((a&0x55555555U)<<1)|((a&0xAAAAAAU)
9             >>1);
10        a=((a&0x33333333U)<<2)|((a&0xCCCCCCU)
11            >>2);
12        a=((a&0x0F0F0F0FU)<<4)|((a&0xFF0F0F0U)
13            >>4);
14        a=((a&0x00FF00FFU)<<8)|((a&0xFFFF000U)
15            >>8);
16        a=((a&0x0000FFFFU)<<16)|((a&0xFFFF0000U)
17            >>16);
18        return a>>(32-len);
19    }
20    void fft(bool is_inv,VT &in,VT &out,int N)
21    {
22        int bitlen=std::__lg(N),num=is_inv?-1:1;
23        for(int i=0;i<N;++i)out[bit_reverse(i,
24            bitlen)]=in[i];
25        for(int step=2;step<=N;step<=1){

```

```

17 const int mh=step>>1;
18 for(int i=0;i<mh;++i){
19     std::complex<T> wi=exp(std::complex<
20         T>(0,i*num*pi/mh));
21     for(int j=i;j<N;j+=step){
22         int k=j+mh;
23         std::complex<T> u=out[j],t=wi*out[
24             k];
25         out[j]=u+t;
26         out[k]=u-t;
27     }
28 }
29 if(is_inv)for(int i=0;i<N;++i)out[i]/=N;
30 }

```

7.9 find_real_root.cpp

```

1 // an*x^n + ... + a1x + a0 = 0;
2 int sign(double x){
3     return x < -eps ? -1 : x > eps;
4 }
5 double get(const vector<double>&coef, double
6     x){
7     double e = 1, s = 0;
8     for(auto i : coef) s += i*e, e *= x;
9     return s;
10 }
11 double find(const vector<double>&coef, int n
12     , double lo, double hi){
13     double sign_lo, sign_hi;
14     if( !(sign_lo = sign(get(coef,lo))) )
15         return lo;
16     if( !(sign_hi = sign(get(coef,hi))) )
17         return hi;
18     if(sign_lo * sign_hi > 0) return INF;
19     for(int stp = 0; stp < 100 && hi - lo >
20         eps; ++stp){
21         double m = (lo+hi)/2.0;
22         int sign_mid = sign(get(coef,m));
23         if(!sign_mid) return m;
24         if(sign_lo*sign_mid < 0) hi = m;
25         else lo = m;
26     }
27     return (lo+hi)/2.0;
28 }
29 vector<double> cal(vector<double>coef, int n
30 ) {
31     vector<double>res;
32     if(n == 1){
33         if(sign(coef[1])) res.pb(-coef[0]/
34             coef[1]);
35         return res;
36     }
37     vector<double>dcoef(n);
38     for(int i = 0; i < n; ++i) dcoef[i] =
39         coef[i+1]*(i+1);
40     vector<double>droot = cal(dcoef, n-1);
41     droot.insert(droot.begin(), -INF);

```

```

37 droot.pb(INF);
38 for(int i = 0; i+1 < droot.size(); ++i){
39     double tmp = find(coef, n, droot[i],
40         droot[i+1]);
41     if(tmp < INF) res.pb(tmp);
42 }
43 return res;
44 }
45 int main () {
46     vector<double>ve;
47     vector<double>ans = cal(ve, n);
48     // 視情況把答案 +eps · 避免 -0
49 }

```

7.10 formula.tex

$$\sum_{d|n} \phi(n) = n$$

$$\sum_{d|n} \mu(n) = (n == 1)$$

$$g(n) = \sum_{d|n} f(d) \Rightarrow f(n) = \sum_{d|n} \mu(d) * g(n/d)$$

$$\text{Catalan number} : (2n)!/n!/n!/(n+1)$$

$$\text{Harmonic series } H_n = \ln(n) + \gamma + 1/(2n) - 1/(12n) + 1/(120n^3) - \dots$$

$$\gamma = 0.57721566490153286060651209008240243104215\dots$$

$$i - \text{th gray code} : i^{(i>1)}$$

$$SG(A+B) = SG(A) \oplus SG(B)$$

7.11 Gauss_Elimination.cpp

```

1 const int MAX = 300;
2 const double EPS = 1e-8;
3 double mat[MAX][MAX];
4 void Gauss(int n) {
5     for(int i=0; i<n; i++) {
6         bool ok = 0;
7         for(int j=i; j<n; j++) {
8             if(fabs(mat[j][i]) > EPS) {
9                 swap(mat[j], mat[i]);
10                ok = 1;
11                break;
12            }
13        }
14        if(!ok) continue;
15        double fs = mat[i][i];
16        for(int j=i+1; j<n; j++) {
17            double r = mat[j][i] / fs;
18            for(int k=i; k<n; k++) {
19                mat[j][k] -= mat[i][k] * r;
20            }
21        }
22    }
23 }
24 }
25 }

```

7.12 LinearCongruence.cpp

```

1 pair<LL,LL> LinearCongruence(LL a[],LL b[],
  LL m[],int n) {
2   // a[i]*x = b[i] (mod m[i])
3   for(int i=0;i<n;++i) {
4     LL x, y, d = extgcd(a[i],m[i],x,y);
5     if(b[i]%d!=0) return make_pair(-1LL
6       ,0LL);
7     m[i] /= d;
8     b[i] = LLMul(b[i]/d,x,m[i]);
9   }
10  LL lastb = b[0], lastm = m[0];
11  for(int i=1;i<n;++i) {
12    LL x, y, d = extgcd(m[i],lastm,x,y);
13    if((lastb-b[i])%d!=0) return
14      make_pair(-1LL,0LL);
15    lastb = LLMul((lastb-b[i])/d,x,
16      lastm/d)*m[i];
17    lastm = (lastm/d)*m[i];
18    lastb = (lastb+b[i])%lastm;
19  }
20  return make_pair(lastb<0?lastb+lastm:
21    lastb,lastm);
22 }

```

7.13 Lucas.cpp

```

1 int mod_fact(int n,int &e){
2   e=0;
3   if(n==0)return 1;
4   // (n/p)! % p
5   int res=mod_fact(n/P,e);
6   e += n/P;
7   if( (n/P) %2 == 0){// = 1
8     return res*fact[n%P]%P;
9   }
10  // = -1
11  return res*(P-fact[n%P])%P;
12 }
13 int extGCD(int a,int b,int &x,int &y){
14  int d=a;
15  if(b!=0){
16    d=extGCD(b,a%b,y,x);
17    y -= (a/b)*x;
18  }else{
19    x=1;y=0;
20  }
21  return d;
22 }
23 int modInverse(int n){
24  int x,y;
25  extGCD(n,P,x,y);
26  return (P+x%P)%P;
27 }
28 int Cmod(int n,int m){
29  int a1,a2,a3,e1,e2,e3;
30  a1=mod_fact(n,e1);
31  a2=mod_fact(m,e2);
32  a3=mod_fact(n-m,e3);
33  if(e1>e2+e3)return 0;
34  return a1*modInverse(a2*a3%P)%P;
35 }

```

7.14 NTT.cpp

```

1 2615053605667*(2^18)+1,3
2 15*(2^27)+1,31
3 479*(2^21)+1,3
4 7*17*(2^23)+1,3
5 3*3*211*(2^19)+1,5
6 25*(2^22)+1,3
7 template<typename T,typename VT=std::vector<
  T> >
8 struct NTT{
9   const T P,G;
10  NTT(T p=(1<<23)*7*17+1,T g=3):P(p),G(g){}
11  unsigned int bit_reverse(unsigned int a,
12    int len){
13    a=((a&0x55555555U)<<1)|((a&0xAAAAAAAAU)
14      >>1);
15    a=((a&0x33333333U)<<2)|((a&0xCCCCCCC)
16      >>2);
17    a=((a&0x0F0F0F0FU)<<4)|((a&0xF0F0F0FU)
18      >>4);
19    a=((a&0x00FF00FFU)<<8)|((a&0xFF00FF00U)
20      >>8);
21    a=((a&0x0000FFFFU)<<16)|((a&0xFFFF0000U)
22      >>16);
23    return a>>(32-len);
24  }
25  T pow_mod(T n,T k,T m){
26    T ans=1;
27    for(n=(n>=m?n%m:n);k;k>>=1){
28      if(k&1)ans=ans*n%m;
29      n=n*n%m;
30    }
31    return ans;
32  }
33  void ntt(bool is_inv,VT &in,VT &out,int N)
34  {
35    int bitlen=std::__lg(N);
36    for(int i=0;i<N;++i)out[bit_reverse(i,
37      bitlen)]=in[i];
38    for(int step=2,id=1;step<=N;step<=1,++
39      id){
40      T wn=pow_mod(G,(P-1)>>id,P),wi=1,u,t;
41      const int mh=step>>1;
42      for(int i=0;i<mh;++i){
43        for(int j=i;j<N;j+=step){
44          u=out[j],t=wi*out[j+mh]%P;
45          out[j]=u+t;
46          out[j+mh]=u-t;
47          if(out[j]>=P)out[j]-=P;
48          if(out[j+mh]<0)out[j+mh]+=P;
49        }
50        wi=wi*wn%P;
51      }
52    }
53    if(is_inv){
54      for(int i=1;i<N/2;++i)std::swap(out[i]
55        ,out[N-i]);
56    }
57    T invn=pow_mod(N,P-2,P);
58    for(int i=0;i<N;++i)out[i]=out[i]*invn
59      %P;
60  }
61 }
62 };

```

7.15 random.cpp

```

1 inline int random_int(){
2   static int seed=20160424;
3   return seed+=(seed<<16)+0x1db3d743;
4 }
5 inline long long random_long_long(){
6   static long long seed=20160424;
7   return seed+=(seed<<32)+0xdb3d742c265539d;
8 }

```

7.16 外星模運算.cpp

```

1 //a[0]^a[1]^a[2]^...
2 #include<bits/stdc++.h>
3 using namespace std;
4 #define maxn 1000000
5 int euler[maxn+5];
6 bool is_prime[maxn+5];
7 inline void init_euler(){
8   is_prime[1]=1;//一不是質數
9   for(int i=1;i<=maxn;i++)euler[i]=i;
10  for(int i=2;i<=maxn;i++){
11    if(!is_prime[i]){//是質數
12      euler[i]--;
13      for(int j=i<<1;j<=maxn;j+=i){
14        is_prime[j]=1;
15        euler[j]=euler[j]/i*(i-1);
16      }
17    }
18  }
19 }
20 inline long long pow(long long a,long long b
21   ,long long mod){//a^b%mod
22   long long ans=1;
23   for(;b;a=a*a%mod,b>>=1)
24     if(b&1)ans=ans*a%mod;
25   return ans;
26 }
27 bool isless(long long *a,int n,int k){
28   if(*a==1)return k>1;
29   if(--n==0)return *a<k;
30   int next=0;
31   for(long long b=1;b<k;++next)
32     b*=*a;
33   return isless(a+1,n,next);
34 }
35 long long high_pow(long long *a,int n,long
36   long mod){
37   if(*a==1||--n==0)return *a%mod;
38   int k=0,r=euler[mod];
39   for(long long tma=1;tma!=pow(*a,k+r,mod)
40     ;++k)
41     tma=tma*(*a)%mod;
42   if(isless(a+1,n,k))return pow(*a,high_pow(
43     a+1,n,k),mod);
44   int tmd=high_pow(a+1,n,r);
45   int t=(tmd-k+r)%r;
46   return pow(*a,k+t,mod);
47 }
48 }
49 long long a[1000005];

```

```

45 int t,mod;
46 int main(){
47   init_euler();
48   scanf("%d",&t);
49   #define n 4
50   while(t--){
51     for(int i=0;i<n;++i)scanf("%Lld",&a[i]);
52     scanf("%d",&mod);
53     printf("%Lld\n",high_pow(a,n,mod));
54   }
55   return 0;
56 }

```

7.17 模運算模板.cpp

```

1 template<typename T,long long mod>
2 struct mod_t{//mod只能是質數
3   T data;
4   mod_t(){}
5   mod_t(const T &d):data((d%mod+mod)%mod){}
6   mod_t pow(T b)const{
7     mod_t ans(1);
8     for(mod_t now=*this;b;now=now*b,b/=2)
9       if(b%2)ans=ans*now;
10    return ans;
11  }
12  mod_t operator-(int)const{
13    return mod_t(mod-data);
14  }
15  mod_t operator+(const mod_t &b)const{
16    return mod_t((data+b.data)%mod);
17  }
18  mod_t operator-(const mod_t &b)const{
19    return mod_t((data-b.data+mod)%mod);
20  }
21  mod_t operator*(const mod_t &b)const{
22    return mod_t((data*b.data)%mod);
23  }
24  mod_t operator/(const mod_t &b)const{
25    return *this*b.pow(mod-2);//*this *
26    Inverse(b)
27  }
28  operator T()const{return data;}
29  friend istream &operator>>(istream &i,
30    mod_t &b){
31    T d;
32    i>>d;
33    b=mod_t(d);
34    return i;
35  }
36 };

```

8 String

8.1 AC 自動機.cpp

```

1 template<char L='a',char R='z'>
2 class ac_automaton{
3 private:
4     struct joe{
5         int next[R-L+1], fail, efl, ed, cnt_dp, vis;
6     };
7     joe():ed(0),cnt_dp(0),vis(0){
8         for(int i=0;i<=R-L;++i)next[i]=0;
9     };
10 public:
11     std::vector<joe> S;
12     std::vector<int> q;
13     int qs,qe,vt;
14     ac_automaton():S(1),qs(0),qe(0),vt(0){}
15     void clear(){
16         q.clear();
17         S.resize(1);
18         for(int i=0;i<=R-L;++i)S[0].next[i]=0;
19         S[0].cnt_dp=S[0].vis=qs=qe=vt=0;
20     }
21     void insert(const char *s){
22         int o=0;
23         for(int i=0,id;s[i];++i){
24             id=s[i]-L;
25             if(!S[o].next[id]){
26                 S.push_back(joe());
27                 S[o].next[id]=S.size()-1;
28             }
29             o=S[o].next[id];
30             ++S[o].ed;
31         }
32     }
33     void build_fail(){
34         S[0].fail=S[0].efl=-1;
35         q.clear();
36         q.push_back(0);
37         ++qe;
38         while(qs!=qe){
39             int pa=q[qs++],id,t;
40             for(int i=0;i<=R-L;++i){
41                 t=S[pa].next[i];
42                 if(!t)continue;
43                 id=S[pa].fail;
44                 while(~id&&S[id].next[i])id=S[id].fail;
45                 S[t].fail=~id?S[id].next[i]:0;
46                 S[t].efl=S[S[t].fail].ed?S[t].fail:S[S[t].fail].efl;
47                 q.push_back(t);
48                 ++qe;
49             }
50         }
51     }
52     /*DP出每個前綴在字串s出現的次數並傳回所有字串被s匹配成功的次數O(N*M)*/
53     int match_0(const char *s){
54         int ans=0,id,p=0,t;
55         for(int i=0;s[i];++i){
56             id=s[i]-L;
57             while(!S[p].next[id]&&p=S[p].fail;
58             if(!S[p].next[id])continue;
59             p=S[p].next[id];
60             ++S[p].cnt_dp; /*匹配成功則它所有後綴都可以被匹配(DP計算)*/
61         }
62         for(i=qe-1;i>=0;--i){
63             ans+=S[q[i]].cnt_dp*S[q[i]].ed;
64             if(~S[q[i]].fail)S[S[q[i]].fail].cnt_dp+=S[q[i]].cnt_dp;
65         }
66         return ans;
67     }
68     /*多串匹配走efl邊並傳回所有字串被s匹配成功的次數O(N*M^1.5)*/
69     int match_1(const char *s)const{
70         int ans=0,id,p=0,t;
71         for(int i=0;s[i];++i){
72             id=s[i]-L;
73             while(!S[p].next[id]&&p=S[p].fail;
74             if(!S[p].next[id])continue;
75             p=S[p].next[id];
76             if(S[p].ed)ans+=S[p].ed;
77             for(t=S[p].efl;~t;t=S[t].efl){
78                 ans+=S[t].ed; /*因為都走efl邊所以保證匹配成功*/
79             }
80         }
81         return ans;
82     }
83     /*枚舉(s的子字串nA)的所有相異字串各恰一次並傳回次數O(N*M^(1/3))*/
84     int match_2(const char *s){
85         int ans=0,id,p=0,t;
86         ++vt;
87         /*把戳記vt+=1,只要vt沒溢位,所有S[p].vis==vt就會變成false
88         這種利用vt的方法可以O(1)歸零vis陣列*/
89         for(int i=0;s[i];++i){
90             id=s[i]-L;
91             while(!S[p].next[id]&&p=S[p].fail;
92             if(!S[p].next[id])continue;
93             p=S[p].next[id];
94             if(S[p].ed&&S[p].vis!=vt){
95                 S[p].vis=vt;
96                 ans+=S[p].ed;
97             }
98             for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[t].efl){
99                 S[t].vis=vt;
100                 ans+=S[t].ed; /*因為都走efl邊所以保證匹配成功*/
101             }
102         }
103         return ans;
104     }
105     /*把AC自動機變成真的自動機*/
106     void evolution(){
107         for(qs=1;qs!=qe;){
108             int p=q[qs++];
109             for(int i=0;i<=R-L;++i)
110                 if(S[p].next[i]==0)S[p].next[i]=S[p].fail.next[i];
111         }
112     }
113 };

```

8.2 hash.cpp

```

1 #define MAXN 1000000
2 #define prime_mod 1073676287
3 /*prime_mod 必須要要是質數*/
4 typedef long long T;
5 char s[MAXN+5];
6 T h[MAXN+5]; /*hash陣列*/
7 T h_base[MAXN+5]; /*h_base[n]=(prime^n)%prime_mod*/
8 inline void hash_init(int len,T prime=0xdefaced){
9     h_base[0]=1;
10    for(int i=1;i<=len;++i){
11        h[i]=(h[i-1]*prime+s[i-1])%prime_mod;
12        h_base[i]=(h_base[i-1]*prime)%prime_mod;
13    }
14 }
15 inline T get_hash(int l,int r){ /*閉區間寫法,設編號為0~len-1*/
16     return (h[r+1]-(h[l]*h_base[r-l+1])%prime_mod+prime_mod)%prime_mod;
17 }

```

8.3 KMP.cpp

```

1 /*產生fail function*/
2 inline void kmp_fail(char *s,int len,int *fail){
3     int id=-1;
4     fail[0]=-1;
5     for(int i=1;i<len;++i){
6         while(~id&&S[id+1]!=s[i])id=fail[id];
7         if(s[id+1]==s[i])++id;
8         fail[i]=id;
9     }
10 }
11 /*以字串B匹配字串A,傳回匹配成功的數量(用B的fail)*/
12 inline int kmp_match(char *A,int lenA,char *B,int lenB,int *fail){
13     int id=-1,ans=0;
14     for(int i=0;i<lenA;++i){
15         while(~id&&B[id+1]!=A[i])id=fail[id];
16         if(B[id+1]==A[i])++id;
17         if(id==lenB-1){ /*匹配成功*/
18             ++ans;
19             id=fail[id];
20         }
21     }
22     return ans;
23 }

```

8.4 manacher.cpp

```

1 //原字串: asdsasdsa
2 //先把字串變成這樣: @a#s#d#s#a#s#d#s#a#

```

```

3 inline void manacher(char *s,int len,int *z)
4 {
5     int l=0,r=0;
6     for(int i=1;i<len;++i){
7         z[i]=r>i?min(z[2*i-l],r-i):1;
8         while(s[i+z[i]]==s[i-z[i]])++z[i];
9         if(z[i]+i>r)r=z[i]+i,l=i;
10    }

```

8.5 minimal_string_rotation.cpp

```

1 int min_string_rotation(const string &s){
2     int n=s.size(),i=0,j=1,k=0;
3     while(i<n&&j<n&&k<n){
4         int t=s[(i+k)%n]-s[(j+k)%n];
5         ++k;
6         if(t){
7             if(t>0)i+=k;
8             else j+=k;
9             if(i==j)++j;
10            k=0;
11        }
12    }
13    return min(i,j); //傳回最小循環表示法起始位置
14 }

```

8.6 suffix_array_lcp.cpp

```

1 #define radix_sort(x,y){\
2     for(i=0;i<A;++i)c[i]=0;\
3     for(i=0;i<len;++i)c[x[y[i]]]++;\
4     for(i=1;i<A;++i)c[i]+=c[i-1];\
5     for(i=len-1;i>=0;--i)sa[--c[x[y[i]]]]=y[i];\
6 }
7 void suffix_array(const char *s,int len,int *sa,int *rank,int *tmp,int *c){
8     int A='z'+1,i,k,id,*t;
9     for(i=0;i<len;++i){
10         tmp[i]=i;
11         rank[i]=s[i];
12     }
13     radix_sort(rank,tmp);
14     for(k=1;id<len-1;k<=1){
15         id=0;
16         for(i=len-k;i<len;++i)tmp[id++]=i;
17         for(i=0;i<len;++i){
18             if(sa[i]>=k)tmp[id++]=sa[i]-k;
19         }
20         radix_sort(rank,tmp);
21         t=rank;rank=tmp;tmp=t;
22         id=0;
23         rank[sa[0]]=0;
24         for(i=1;i<len;++i){
25             if(tmp[sa[i-1]]!=tmp[sa[i]]||sa[i-1]+k>len||tmp[sa[i-1]+k]!=tmp[sa[i]+k])++id;

```



```

26     rank[sa[i]]=id;
27 }
28 A=id+1;
29 }
30 }
31 #undef radix_sort
32 //h:高度數組 sa:後綴數組 rank:排名
33 inline void suffix_array_lcp(const char *s,
34     int len,int *h,int *sa,int *rank){
35     for(int i=0;i<len;++i)rank[sa[i]]=i;
36     for(int i=0,k=0;i<len;++i){
37         if(rank[i]==0)continue;
38         if(k)--k;
39         while(s[i+k]==s[sa[rank[i]-1]+k])++k;
40         h[rank[i]]=k;
41     }
42 }

```

8.7 Z.cpp

```

1 inline void z_alg(char *s,int len,int *z){
2     int l=0,r=0;
3     z[0]=len;
4     for(int i=1;i<len;++i){
5         z[i]=i>r?0:(i-l+z[i-l]<z[l]?z[i-l]:r-i
6             +1);
7         while(i+z[i]<len&&s[i+z[i]]==s[z[i]]++)z[i]++;
8         if(i+z[i]-1>r)r=i+z[i]-1,l=i;
9     }
}

```

9 Tarjan

9.1 dominator_tree.cpp

```

1 struct dominator_tree{
2     static const int MAXN=5005;
3     int n;// 1-base
4     vector<int> suc[MAXN],pre[MAXN]; //存圖和反
5     //向圖
6     int fa[MAXN],dfn[MAXN],id[MAXN],Time;//for
7     //dfs
8     int semi[MAXN],idom[MAXN];
9     int anc[MAXN],best[MAXN]; //disjoint set
10    vector<int> dom[MAXN]; //dominator_tree存這
11    //裡
12    void init(int _n){
13        n=_n;
14        for(int i=1;i<=n;++i)suc[i].clear(),pre[i].clear();
15    }
16    void add_edge(int u,int v){
17        suc[u].push_back(v);
18        pre[v].push_back(u);
19    }
}

```

```

17 void dfs(int u){
18     dfn[u]=++Time,id[Time]=u;
19     for(auto v:suc[u]){
20         if(dfn[v])continue;
21         dfs(v),fa[dfn[v]]=dfn[u];
22     }
23 }
24 int find(int x){
25     if(x==anc[x])return x;
26     int y=find(anc[x]);
27     if(semi[best[x]]>semi[best[anc[x]]])best[x]=best[anc[x]];
28     return anc[x]=y;
29 }
30 void tarjan(int r){
31     Time=0;
32     for(int t=1;t<=n;++t){
33         dfn[t]=idom[t]=0;//u=r或是u無法到達r時
34         idom[id[u]]=0
35         dom[t].clear();
36         anc[t]=best[t]=semi[t]=t;
37     }
38     dfs(r);
39     for(int y=Time;y>=2;--y){
40         int x=fa[y],idy=id[y];
41         for(auto z:pre[idy]){
42             if(!(z=dfn[z]))continue;
43             find(z);
44             semi[y]=min(semi[y],semi[best[z]]);
45         }
46         dom[semi[y]].push_back(y);
47         anc[y]=x;
48         for(auto z:dom[x]){
49             find(z);
50             idom[z]=semi[best[z]]<x?best[z]:x;
51         }
52         dom[x].clear();
53     }
54     for(int u=2;u<=Time;++u){
55         if(idom[u]!=semi[u])idom[u]=idom[idom[u]];
56         dom[id[idom[u]]].push_back(id[u]);
57     }
58 }dom;

```

9.2 tnfsb017_2_sat.cpp

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define MAXN 8001
4 #define MAXN2 MAXN*4
5 #define n(X) ((X)+2*MAXN)
6 vector<int> v[MAXN2];
7 vector<int> rv[MAXN2];
8 vector<int> vis_t;
9 int N,M;
10 void addedge(int s,int e){
11     v[s].push_back(e);
12     rv[e].push_back(s);
13 }
14 int scc[MAXN2];
15 bool vis[MAXN2]={false};

```

```

16 void dfs(vector<int> *uv,int n,int k=-1){
17     vis[n]=true;
18     for(int i=0;i<uv[n].size();++i)
19         if(!vis[uv[n][i]])
20             dfs(uv,uv[n][i],k);
21     if(uv==v)vis_t.push_back(n);
22     scc[n]=k;
23 }
24 void solve(){
25     for(int i=1;i<=N;++i){
26         if(!vis[i])dfs(v,i);
27         if(!vis[n(i)])dfs(v,n(i));
28     }
29     memset(vis,0,sizeof(vis));
30     int c=0;
31     for(int i=vis_t.size()-1;i>=0;--i)
32         if(!vis[vis_t[i]])
33             dfs(rv,vis_t[i],c++);
34 }
35 int main(){
36     int a,b;
37     scanf("%d%d",&N,&M);
38     for(int i=1;i<=N;++i){
39         // (A or B)&(A & !B) A^B
40         a=i*2-1;
41         b=i*2;
42         addedge(n(a),b);
43         addedge(n(b),a);
44         addedge(a,n(b));
45         addedge(b,n(a));
46     }
47     while(M--){
48         scanf("%d%d",&a,&b);
49         a = a>0?a*2-1:-a*2;
50         b = b>0?b*2-1:-b*2;
51         // A or B
52         addedge(n(a),b);
53         addedge(n(b),a);
54     }
55     solve();
56     bool check=true;
57     for(int i=1;i<=2*N;++i)
58         if(scc[i]==scc[n(i)])
59             check=false;
60     if(check){
61         printf("%d\n",N);
62         for(int i=1;i<=2*N;i+=2){
63             if(scc[i]>scc[i+2*N])
64                 putchar('+');
65             else
66                 putchar('-');
67         }
68         putchar('\n');
69     }else puts("0");
70     return 0;
71 }

```

9.3 橋連通分量.cpp

```

1 #define N 1005
2 struct edge{
3     int u,v;
4     bool is_bridge;

```

```

5     edge(int u=0,int v=0):u(u),v(v),is_bridge
6     (0){}
7 };
8 vector<edge> E;
9 vector<int> G[N]; // 1-base
10 int low[N],vis[N],Time;
11 int bcc_id[N],bridge_cnt,bcc_cnt; // 1-base
12 int st[N],top; //BCC用
13 inline void add_edge(int u,int v){
14     G[u].push_back(E.size());
15     E.push_back(edge(u,v));
16     G[v].push_back(E.size());
17     E.push_back(edge(v,u));
18 }
19 void dfs(int u,int re=-1){ //u當前點·re為u連
20     //接前一個點的邊
21     int v;
22     low[u]=vis[u]=++Time;
23     st[top++]=u;
24     for(size_t i=0;i<G[u].size();++i){
25         int e=G[u][i];v=E[e].v;
26         if(!vis[v]){
27             dfs(v,e^1); //e^1反向邊
28             low[u]=min(low[u],low[v]);
29             if(vis[u]<low[v]){
30                 E[e].is_bridge=E[e^1].is_bridge=1;
31                 ++bridge_cnt;
32             }
33             else if(vis[v]<vis[u]&&e!=re)
34                 low[u]=min(low[u],vis[v]);
35         }
36         if(vis[u]==low[u]){ //處理BCC
37             ++bcc_cnt; // 1-base
38             do bcc_id[v]=st[--top]=bcc_cnt; //每個點
39                 //所在的BCC
40             while(v!=u);
41         }
42     }
43     inline void bcc_init(int n){
44         Time=bcc_cnt=bridge_cnt=top=0;
45         E.clear();
46         for(int i=1;i<=n;++i){
47             G[i].clear();
48             vis[i]=bcc_id[i]=0;
49         }
50     }
}

```

9.4 雙連通分量 & 割點.cpp

```

1 #define N 1005
2 vector<int> G[N]; // 1-base
3 vector<int> bcc[N]; //存每塊雙連通分量的點
4 int low[N],vis[N],Time;
5 int bcc_id[N],bcc_cnt; // 1-base
6 bool is_cut[N]; //是否為割點·割點的bcc_id沒
7 //意義
8 int st[N],top;
9 void dfs(int u,int pa=-1){ //u當前點·pa父親
10     int v,child=0;
11     low[u]=vis[u]=++Time;
12     st[top++]=u;

```

```

12 for(size_t i=0;i<G[u].size();++i){
13     if(!vis[v=G[u][i]]){
14         dfs(v,u,++child;
15         low[u]=min(low[u],low[v]);
16         if(vis[u]<=low[v]){
17             is_cut[u]=1;
18             bcc[++bcc_cnt].clear();
19             int t;
20             do{
21                 bcc_id[t=st[--top]]=bcc_cnt;
22                 bcc[bcc_cnt].push_back(t);
23             }while(t!=v);
24             bcc_id[u]=bcc_cnt;
25             bcc[bcc_cnt].push_back(u);
26         }
27     }else if(vis[v]<vis[u]&&v!=pa)//反向邊
28         low[u]=min(low[u],vis[v]);
29 }
30 if(pa==--1&&child<2)is_cut[u]=0;//u是dfs樹
31     的根要判判
32 inline void bcc_init(int n){
33     Time=bcc_cnt=top=0;
34     for(int i=1;i<=n;++i){
35         G[i].clear();
36         is_cut[i]=vis[i]=bcc_id[i]=0;
37     }
38 }

```

10 Tree_problem

10.1 HeavyLight.cpp

```

1 #include<vector>
2 #define MAXN 100005
3 typedef std::vector<int>::iterator VIT;
4 int siz[MAXN],max_son[MAXN],pa[MAXN],dep[
5     MAXN];
6 /*節點大小、大小最大的孩子、父母節點、深度*/
7 int link_top[MAXN],link[MAXN],cnt;
8 /*每個點所在鍊的鏈頭、樹鏈剖分的DFS序、時間
9     戳*/
10 std::vector<int> >G[MAXN];/*用vector存樹*/
11 void find_max_son(int x){
12     siz[x]=1;
13     max_son[x]=-1;
14     for(VIT i=G[x].begin();i!=G[x].end();++i){
15         if(*i==pa[x])continue;
16         pa[*i]=x;
17         dep[*i]=dep[x]+1;
18         find_max_son(*i);
19         if(max_son[x]==-1||siz[*i]>siz[max_son[x]
20             ])max_son[x]=*i;
21         siz[x]+=siz[*i];
22     }
23 }
24 void build_link(int x,int top){
25     link[x]=++cnt;/*記錄x點的時間戳*/
26     link_top[x]=top;
27     if(max_son[x]==-1)return;

```

```

25     build_link(max_son[x],top);/*優先走訪最大
26     孩子*/
27     for(VIT i=G[x].begin();i!=G[x].end();++i){
28         if(*i==max_son[x]||*i==pa[x])continue;
29         build_link(*i,*i);
30     }
31 inline int find_lca(int a,int b){
32     /*求LCA·可以在過程中對區間進行處理*/
33     int ta=link_top[a],tb=link_top[b];
34     while(ta!=tb){
35         if(dep[ta]<dep[tb]){
36             std::swap(ta,tb);
37             std::swap(a,b);
38         }
39         /*這裡可以對a所在的鏈做區間處理
40         區間為(Link[ta],Link[a])
41         ta=link_top[a=pa[ta]];
42     }
43     /*最後a,b會在同一條鏈·若a!=b還要在進行一
44     次區間處理*/
45     return dep[a]<dep[b]?a:b;

```

10.2 LCA.cpp

```

1 #define MAXN 100000
2 #define MAX_LOG 17
3 int pa[MAX_LOG+1][MAXN+5];
4 int dep[MAXN+5];
5 vector<int>G[MAXN+5];
6 void dfs(int x,int p){/*dfs(1,-1);
7     pa[0][x]=p;
8     for(int i=0;i+1<MAX_LOG;++i)pa[i+1][x]=pa[
9         i][pa[i][x]];
10     for(auto &i:G[x]){
11         if(i==p)continue;
12         dep[i]=dep[x]+1;
13         dfs(i,x);
14     }
15 inline int jump(int x,int d){
16     for(int i=0;i<d;++i)if((x>>i)&1)x=pa[i][x
17         ];
18     return x;
19 }
20 inline int find_lca(int a,int b){
21     if(dep[a]>dep[b])swap(a,b);
22     b=jump(b,dep[b]-dep[a]);
23     if(a==b)return a;
24     for(int i=MAX_LOG;i>=0;--i){
25         if(pa[i][a]!=pa[i][b]){
26             a=pa[i][a];
27             b=pa[i][b];
28         }
29     }
30     return pa[0][a];

```

10.3 link_cut_tree.cpp

```

1 #include<vector>
2 struct splay_tree{
3     int ch[2],pa;/*子節點跟父母*/
4     bool rev;/*反轉的懶惰標記*/
5     splay_tree():pa(0),rev(0){ch[0]=ch[1]=0;}
6 };
7 std::vector<splay_tree> node;
8 /*
9     有的時候用vector會TLE·要注意
10     這邊以node[0]作為null節點
11 */
12 inline bool isroot(int x){/*判斷是否為這棵
13     splay tree的根*/
14     return node[node[x].pa].ch[0]!=x&&node[
15         node[x].pa].ch[1]!=x;
16 }
17 inline void down(int x){/*懶惰標記下推*/
18     if(node[x].rev){
19         if(node[x].ch[0])node[node[x].ch[0]].rev
20             ^=1;
21         if(node[x].ch[1])node[node[x].ch[1]].rev
22             ^=1;
23         std::swap(node[x].ch[0],node[x].ch[1]);
24         node[x].rev^=1;
25     }
26 }
27 void push_down(int x){/*將所有祖先的懶惰標記
28     下推*/
29     if(!isroot(x))push_down(node[x].pa);
30     down(x);
31 }
32 inline void up(int x){/*將子節點的資訊向上
33     更新*/
34     inline void rotate(int x){/*旋轉·會自行判斷
35         轉的方向*/
36         int y=node[x].pa,z=node[y].pa,d=(node[y].
37             ch[1]==x);
38         node[x].pa=z;
39         if(!isroot(y))node[z].ch[node[z].ch[1]==y
40             ]=x;
41         node[y].ch[d]=node[x].ch[d^1];
42         node[node[y].ch[d]].pa=y;
43         node[y].pa=x,node[x].ch[d^1]=y;
44         up(y);
45         up(x);
46     }
47 inline void splay(int x){/*將節點x伸展到所在
48     splay tree的根*/
49     push_down(x);
50     while(!isroot(x)){
51         int y=node[x].pa;
52         if(!isroot(y)){
53             int z=node[y].pa;
54             if((node[z].ch[0]==y)^(node[y].ch[0]==
55                 x))rotate(y);
56             else rotate(x);
57         }
58         rotate(x);
59     }
60 }
61 inline int access(int x){

```

```

51     int last=0;
52     while(x){
53         splay(x);
54         node[x].ch[1]=last;
55         up(x);
56         last=x;
57         x=node[x].pa;
58     }
59     return last;/*回傳access後splay tree的根*/
60 }
61 inline void access(int x,bool is=0){/*is=0就
62     是一般的access*/
63     int last=0;
64     while(x){
65         splay(x);
66         if(is&&!node[x].pa){
67             //printf("%d\n",max(node[last].ma,node
68                 [node[x].ch[1]].ma));
69         }
70         node[x].ch[1]=last;
71         up(x);
72         last=x;
73         x=node[x].pa;
74     }
75 inline void query_edge(int u,int v){
76     access(u);
77     access(v,1);
78 }
79 inline void make_root(int x){
80     access(x),splay(x);
81     node[x].rev^=1;
82 }
83 inline void make_root(int x){
84     node[access(x)].rev^=1;
85     splay(x);
86 }
87 inline void cut(int x,int y){
88     make_root(x);
89     access(y);
90     splay(y);
91     node[y].ch[0]=0;
92     node[x].pa=0;
93 }
94 inline void cut_parents(int x){
95     access(x);
96     splay(x);
97     node[node[x].ch[0]].pa=0;
98     node[x].ch[0]=0;
99 }
100 inline void link(int x,int y){
101     make_root(x);
102     node[x].pa=y;
103 }
104 inline int find_root(int x){
105     x=access(x);
106     while(node[x].ch[0])x=node[x].ch[0];
107     splay(x);
108     return x;
109 }
110 inline int query(int u,int v){
111     /*
112     傳回uv路徑splay tree的根結點
113     這種寫法無法求LCA
114     */

```

```

114 make_root(u);
115 return access(v);
116 }
117 inline int query_lca(int u,int v){
118 /*假設求鏈上點權的總和，sum是子樹的權重和，
119 data是節點的權重*/
120 access(u);
121 int lca=access(v);
122 splay(u);
123 if(u==lca){
124 //return node[lca].data+node[node[lca].
125 ch[1]].sum;
126 }else{
127 //return node[lca].data+node[node[lca].
128 ch[1]].sum+node[u].sum;
129 }
130 }
131 struct EDGE{
132 int a,b,w;
133 }e[10005];
134 int n;
135 std::vector<std::pair<int ,int > >G[10005];
136 /*first表示子節點，second表示邊的編號*/
137 int pa[10005],edge_node[10005];
138 /*pa是父母節點，暫存用的，edge_node是每個編
139 被存在哪個點裡面的陣列*/
140 inline void bfs(int root){
141 /*在建構的時候把每個點都設成一個splay tree，
142 不會壞掉*/
143 std::queue<int > q;
144 for(int i=1;i<=n;++i)pa[i]=0;
145 q.push(root);
146 while(q.size()){

```

```

142 int u=q.front();
143 q.pop();
144 for(int i=0;i<(int)G[u].size();++i){
145 int v=G[u][i].first;
146 if(v!=pa[u]){
147 pa[v]=u;
148 node[v].pa=u;
149 node[v].data=e[G[u][i].second].w;
150 edge_node[G[u][i].second]=v;
151 up(v);
152 q.push(v);
153 }
154 }
155 }
156 }
157 inline void change(int x,int b){
158 splay(x);
159 //node[x].data=b;
160 up(x);
161 }

```

10.4 POJ_tree.cpp

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define MAXN 10005
4 int n,k;
5 vector<pair<int,int> >g[MAXN];
6 int size[MAXN];
7 bool vis[MAXN];
8 inline void init(){

```

```

9 for(int i=0;i<=n;++i){
10 g[i].clear();
11 vis[i]=0;
12 }
13 }
14 void get_dis(vector<int> &dis,int u,int pa,
15 int d){
16 dis.push_back(d);
17 for(size_t i=0;i<g[u].size();++i){
18 int v=g[u][i].first,w=g[u][i].second;
19 if(v!=pa&&!vis[v])get_dis(dis,v,u,d+w);
20 }
21 }
22 vector<int> dis;//這東西如果放在函數裡會TLE
23 int cal(int u,int d){
24 dis.clear();
25 get_dis(dis,u,-1,d);
26 sort(dis.begin(),dis.end());
27 int l=0,r=dis.size()-1,res=0;
28 while(l<r){
29 while(l<r&&dis[l]+dis[r]>k)--r;
30 res+=r-(l++);
31 }
32 return res;
33 }
34 pair<int,int> tree_centroid(int u,int pa,
35 const int sz){
36 size[u]=1;//找樹重心，second是重心
37 pair<int,int> res(INT_MAX,-1);
38 int ma=0;
39 for(size_t i=0;i<g[u].size();++i){
40 int v=g[u][i].first;
41 if(v==pa||vis[v])continue;

```

```

40 res=min(res,tree_centroid(v,u,sz));
41 size[u]+=size[v];
42 ma=max(ma,size[v]);
43 }
44 ma=max(ma,sz-size[u]);
45 return min(res,make_pair(ma,u));
46 }
47 int tree_DC(int u,int sz){
48 int center=tree_centroid(u,-1,sz).second;
49 int ans=cal(center,0);
50 vis[center]=1;
51 for(size_t i=0;i<g[center].size();++i){
52 int v=g[center][i].first,w=g[center][i].
53 second;
54 if(vis[v])continue;
55 ans-=cal(v,w);
56 ans+=tree_DC(v,size[v]);
57 }
58 return ans;
59 }
60 int main(){
61 while(scanf("%d%d",&n,&k),n||k){
62 init();
63 for(int i=1;i<=n;++i){
64 int u,v,w;
65 scanf("%d%d%d",&u,&v,&w);
66 g[u].push_back(make_pair(v,w));
67 g[v].push_back(make_pair(u,w));
68 }
69 printf("%d\n",tree_DC(1,n));
70 }
71 return 0;
72 }

```

ACM ICPC Team

Reference - NTHU

Jinkela

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