

# 1 Computational Geometry

## 1.1 delaunay

```

1 template<class T>
2 class Delaunay{
3     struct PT:public point<T>{
4         int g[2];
5         PT(const point<T> &p):
6             point<T>(p){ g[0]=g[1]=-1; }
7     };
8     static bool cmp(const PT &a,const PT &b){
9         return a.x<b.x||(a.x==b.x&&a.y<b.y);
10    }
11    struct edge{
12        int v,g[2];
13        edge(int v,int g0,int g1):
14            v(v){g[0]=g0,g[1]=g1;}
15    };
16    vector<PT> S;
17    vector<edge> E;
18    bool convex(int &from,int to,T LR){
19        for(int i=0;i<2;++i){
20            int c = E[S[from].g[i]].v;
21            auto A=S[from]-S[to], B=S[c]-S[to];
22            T v = A.cross(B)*LR;
23            if(v>0||(v==0&&B.abs2()<A.abs2()))
24                return from = c, true;
25        }
26        return false;
27    }
28    void addEdge(int v,int g0,int g1){
29        E.emplace_back(v,g0,g1);
30        E[E.back().g[0]].g[1] = E.size()-1;
31        E[E.back().g[1]].g[0] = E.size()-1;
32    }
33    void climb(int &p, int e, int n, int nl,
34              int nr, int LR){
35        for(int i=E[e].g[LR]; (S[nr]-S[nl]).
36            cross(S[E[i].v]-S[nl])>0;){
37            if(inCircle(S[E[i].v],S[nl],S[nr],S[E[
38                i].g[LR]].v))>0)
39                { p = i; break; }
40            for(int j=0;j<4;++j)
41                E[E[i^j/2].g[j%2^1]].g[j%2] = E[i^j
42                    /2].g[j%2];
43            int j=i; i=E[i].g[LR];
44            E[j].g[0]=E[j].g[1]=E[j^1].g[0]=E[j
45                ^1].g[1]=-1;
46        }
47    }
48    T det3(T a11,T a12,T a13,T a21,T a22,T a23
49        ,T a31,T a32,T a33){
50        return a11*(a22*a33-a32*a23)-a12*(a21*
51            a33-a31*a23)+a13*(a21*a32-a31*a22);
52    }
53    int inCircle(const PT &a, const PT &b,
54                const PT &c, const PT &p){
55        T as = a.abs2(), bs = b.abs2(), cs = c.abs2
56            (), ps = p.abs2();
57        T res = a.x * det3(b.y,bs,1,c.y,cs,1,p.y,ps
58            ,1)
59            -a.y * det3(b.x,bs,1,c.x,cs,1,p.x,ps,1)
60            +as * det3(b.x,b.y,1,c.x,c.y,1,p.x,p.y,1)
61            -det3(b.x,b.y,bs,c.x,c.y,cs,p.x,p.y,ps);
62        return res<0 ? 1 : (res>0 ? -1 : 0);
63    }
64    void divide(int l, int r){
65        if(l==r)return;
66        if(l+1==r){
67            int A=S[l].g[0]=S[l].g[1]=E.size();
68            E.emplace_back(r,A,A);
69            int B=S[r].g[0]=S[r].g[1]=E.size();
70            E.emplace_back(l,B,B);
71            return;
72        }
73        int mid = (l+r)/2;
74        divide(l,mid), divide(mid+1, r);
75        int nl = mid, nr = mid+1;
76        for(;;){
77            if(convex(nl,nr,1)) continue;
78            if(S[nr].g[0]!=-1&&convex(nr,nl,-1))
79                continue;
80            break;
81        }
82        addEdge(nr,S[nl].g[0],S[nl].g[1]);
83        S[nl].g[1] = E.size()-1;
84        if(S[nr].g[0]==-1){
85            addEdge(nl,E.size(),E.size());
86            S[nr].g[1] = E.size()-1;
87        }else addEdge(nl,S[nr].g[0],S[nr].g[1]);
88        S[nr].g[0] = E.size()-1;
89        int cl = nl, cr = nr;
90        for(;;){
91            int pl=-1, pr=-1, side;
92            climb(pl,E.size()-2,nl,nl,nr,1);
93            climb(pr,E.size()-1,nr,nl,nr,0);
94            if(pl==pr==-1) break;
95            if(pl==-1||pr==-1) side = pl==-1;
96            else side=inCircle(S[E[pl].v],S[nl],S[
97                nr],S[E[pr].v])<=0;
98            if(side){
99                nr = E[pr].v;
100            }
101            addEdge(nr,E.size()-2,E[E.size()-2].g[1]);
102            addEdge(nl,E[pr^1].g[0],pr^1);
103        }else{
104            nl = E[pl].v;
105            addEdge(nr,pl^1,E[pl^1].g[1]);
106            addEdge(nl,E[E.size()-2].g[0],E.size()-2);
107        }
108        if(cl==nl&&cr==nr) return; //Collinearity
109        S[nl].g[0] = E.size()-2;
110        S[nr].g[1] = E.size()-1;
111    }
112    public:
113    void solve(const vector<point<T>> &P){
114        S.clear(), E.clear();
115        for(const auto &p:P) S.emplace_back(p);
116        sort(S.begin(),S.end(),cmp);
117        divide(0,int(S.size())-1);
118    }
119    vector<pair<int,int>> getEdge(){
120        vector<pair<int,int>> res;
121        for(size_t i=0;i<E.size();i+=2)
122            if(E[i].g[0]!=-1)

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## 1.2 Geometry

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111     res.emplace_back(E[i].v,E[i^1].v);
112     return res;
113 }
114 };
115
116 const double PI=atan2(0.0,-1.0);
117 template<typename T>
118 struct point{
119     T x,y;
120     point(){}
121     point(const T&x,const T&y):x(x),y(y){}
122     point operator+(const point &b)const{
123         return point(x+b.x,y+b.y); }
124     point operator-(const point &b)const{
125         return point(x-b.x,y-b.y); }
126     point operator*(const T &b)const{
127         return point(x*b,y*b); }
128     point operator/(const T &b)const{
129         return point(x/b,y/b); }
130     bool operator==(const point &b)const{
131         return x==b.x&&y==b.y; }
132     T dot(const point &b)const{
133         return x*b.x+y*b.y; }
134     T cross(const point &b)const{
135         return x*b.y-y*b.x; }
136     point normal()const{//求法向量
137         return point(-y,x); }
138     T abs2()const{//向量長度的平方
139         return dot(*this); }
140     T rad(const point &b)const{//兩向量的弧度
141         return fabs(atan2(fabs(cross(b)),dot(b))); }
142     T getA()const{//對x軸的弧度
143         T A=atan2(y,x); //超過180度會變負的
144         if(A<=-PI/2)A+=PI*2;
145         return A;
146     }
147 };
148 template<typename T>
149 struct line{
150     line(){}
151     point<T> p1,p2;
152     T a,b,c;//ax+by+c=0
153     line(const point<T>&x,const point<T>&y):p1
154         (x),p2(y){}
155     void pton()const{//轉成一般式
156         a=p1.y-p2.y;
157         b=p2.x-p1.x;
158         c=-a*p1.x-b*p1.y;
159     }
160     T ori(const point<T> &p)const{//點和有向直
161         線的關係，>0左邊、=0在線上、<0右邊
162         return (p2-p1).cross(p-p1);
163     }
164     T btw(const point<T> &p)const{//點投影落在
165         線段上<=0
166         return (p1-p).dot(p2-p);
167     }
168     bool point_on_segment(const point<T>&p)
169         const{//點是否在線段上
170         return ori(p)==0&&btw(p)<=0;
171     }
172     T dis2(const point<T> &p,bool is_segment
173         =0)const{//點跟直線/線段的距離平方
174         point<T> v=p2-p1,v1=p-p1;
175         if(is_segment){
176             point<T> v2=p-p2;
177             if(v.dot(v1)<=0)return v1.abs2();
178             if(v.dot(v2)>=0)return v2.abs2();
179         }
180         T tmp=v.cross(v1);
181         return tmp*tmp/v.abs2();
182     }
183     T seg_dis2(const line<T> &l)const{//兩線段
184         距離平方
185         return min({dis2(l.p1,1),dis2(l.p2,1),l.
186             dis2(p1,1),l.dis2(p2,1)});
187     }
188     point<T> projection(const point<T> &p)
189         const{//點對直線的投影
190         point<T> n=(p2-p1).normal();
191         return p-n*(p-p1).dot(n)/n.abs2();
192     }
193     point<T> mirror(const point<T> &p)const{
194         //點對直線的鏡射，要先呼叫pton轉成一般式
195         point<T> R;
196         T d=a*a+b*b;
197         R.x=(b*b*p.x-a*a*p.x-2*a*b*p.y-2*a*c)/d;
198         R.y=(a*a*p.y-b*b*p.y-2*a*b*p.x-2*b*c)/d;
199         return R;
200     }
201     bool equal(const line &l)const{//直線相等
202         return ori(l.p1)==0&&ori(l.p2)==0;
203     }
204     bool parallel(const line &l)const{
205         return (p1-p2).cross(l.p1-l.p2)==0;
206     }
207     bool cross_seg(const line &l)const{
208         return (p2-p1).cross(l.p1-p1)*(p2-p1).
209             cross(l.p2-p1)<=0; //直線是否交線段
210     }
211     int line_intersect(const line &l)const{//
212         直線相交情況，-1無限多點、1交於一點、0
213         不相交
214         return parallel(l)?(ori(l.p1)==0?-1:0)
215             :1;
216     }
217     int seg_intersect(const line &l)const{
218         T c1=ori(l.p1), c2=ori(l.p2);
219         T c3=l.ori(p1), c4=l.ori(p2);
220         if(c1==0&&c2==0){ //共線
221             bool b1=btw(l.p1)>=0,b2=btw(l.p2)>=0;
222             T a3=l.btw(p1),a4=l.btw(p2);
223             if(b1&&b2&&a3==0&&a4>=0) return 2;
224             if(b1&&b2&&a3>=0&&a4==0) return 3;
225             if(b1&&b2&&a3>=0&&a4>=0) return 0;
226             return -1; //無限交點
227         }else if(c1*c2<=0&&c3*c4<=0)return 1;
228         return 0; //不相交
229     }
230     point<T> line_intersection(const line &l)
231         const{//直線交點*/
232         point<T> a=p2-p1,b=l.p2-l.p1,s=l.p1-p1;
233         //if(a.cross(b)==0)return INF;

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106     return p1+a*(s.cross(b)/a.cross(b));
107 }
108 point<T> seg_intersection(const line &l)
109     const{//線段交點
110     int res=seg_intersect(l);
111     if(res<=0) assert(0);
112     if(res==2) return p1;
113     if(res==3) return p2;
114     return line_intersection(l);
115 };
116 template<typename T>
117 struct polygon{
118     polygon(){
119         vector<point<T> > p;//逆時針順序
120         T area();//面積
121         T ans=0;
122         for(int i=p.size()-1,j=0;j<(int)p.size()
123             ;i=j++){
124             ans+=p[i].cross(p[j]);
125             return ans/2;
126         }
127     }
128     point<T> center_of_mass()const{//重心
129         T cx=0,cy=0,w=0;
130         for(int i=p.size()-1,j=0;j<(int)p.size()
131             ;i=j++){
132             T a=p[i].cross(p[j]);
133             cx+=(p[i].x+p[j].x)*a;
134             cy+=(p[i].y+p[j].y)*a;
135             w+=a;
136         }
137         return point<T>(cx/3/w,cy/3/w);
138     }
139     char ahas(const point<T>& t)const{//點是否
140         在簡單多邊形內、是的話回傳1、在邊上回
141         傳-1、否則回傳0
142         bool c=0;
143         for(int i=0,j=p.size()-1;i<p.size();j=i
144             ++){
145             if(line<T>(p[i],p[j]).point_on_segment
146                 (t))return -1;
147             else if((p[i].y>t.y)!=p[j].y>t.y)&&
148                 t.x<(p[j].x-p[i].x)*(t.y-p[i].y)/(p[j]
149                     .y-p[i].y)+p[i].x)
150                 c=!c;
151             return c;
152         }
153     }
154     char point_in_convex(const point<T>&x)
155         const{
156         int l=1,r=(int)p.size()-2;
157         while(l<r){//點是否在凸多邊形內、是的話
158             回傳1、在邊上回傳-1、否則回傳0
159             int mid=(l+r)/2;
160             T a1=(p[mid]-p[0]).cross(x-p[0]);
161             T a2=(p[mid+1]-p[0]).cross(x-p[0]);
162             if(a1>=0&&a2<=0){
163                 T res=(p[mid+1]-p[mid]).cross(x-p[
164                     mid]);
165                 return res>0?1:(res>0?-1:0);
166             }else if(a1<0)r=mid-1;
167             else l=mid+1;
168         }
169         return 0;
170     }
171 };
172 vector<T> getA()const{//凸包邊對x軸的夾角
173     vector<T> res;//一定是遞增的
174     for(size_t i=0;i<p.size();++i)
175         res.push_back((p[(i+1)%p.size()]-p[i])
176             .getA());
177     return res;
178 }
179 bool line_intersect(const vector<T>&A,
180     const line<T> &l)const{//O(logN)
181     int f1=upper_bound(A.begin(),A.end(),(l.
182         p1-l.p2).getA())-A.begin();
183     int f2=upper_bound(A.begin(),A.end(),(l.
184         p2-l.p1).getA())-A.begin();
185     return l.cross_seg(line<T>(p[f1],p[f2]))
186         ;
187 }
188 polygon cut(const line<T> &l)const{//凸包
189     對直線切割、得到直線l左側的凸包
190     polygon ans;
191     for(int n=p.size(),i=n-1,j=0;j<n;i=j++){
192         if(l.ori(p[i])>=0){
193             ans.p.push_back(p[i]);
194             if(l.ori(p[j])<0)
195                 ans.p.push_back(l.
196                     line_intersection(line<T>(p[i]
197                         ,p[j])));
198         }else if(l.ori(p[j])>0)
199             ans.p.push_back(l.line_intersection(
200                 line<T>(p[i],p[j])));
201         }
202     }
203     return ans;
204 }
205 static bool monotone_chain_cmp(const point
206     <T>& a,const point<T>& b){//凸包排序函
207     數
208     return (a.x<b.x)|| (a.x==b.x&&a.y<b.y);
209 }
210 void monotone_chain(vector<point<T> > &s){
211     //凸包
212     sort(s.begin(),s.end(),
213         monotone_chain_cmp);
214     p.resize(s.size()+1);
215     int m=0;
216     for(size_t i=0;i<s.size();++i){
217         while(m>=2&&(p[m-1]-p[m-2]).cross(s[i]
218             -p[m-2])<=0)--m;
219         p[m++]=s[i];
220     }
221     for(int i=s.size()-2,t=m+1;i>0;--i){
222         while(m>=t&&(p[m-1]-p[m-2]).cross(s[i]
223             -p[m-2])<=0)--m;
224         p[m++]=s[i];
225     }
226     if(s.size())>1--m;
227     p.resize(m);
228 }
229 T diam()const{//直徑
230     int n=p.size(),t=1;
231     T ans=0;p.push_back(p[0]);
232     for(int i=0;i<n;i++){
233         point<T> now=p[i+1]-p[i];
234         while(now.cross(p[t+1]-p[i])>now.cross
235             (p[t]-p[i]))t=(t+1)%n;
236         ans=max(ans,(p[i]-p[t]).abs2());
237     }
238 }
239 }
240 T min_cover_rectangle()const{//最小覆蓋矩形
241     int n=p.size(),t=1,r=1,l=1;
242     if(n<3)return 0;//也可以做最小周長矩形
243     T ans=1e99;p.push_back(p[0]);
244     for(int i=0;i<n;i++){
245         point<T> now=p[i+1]-p[i];
246         while(now.cross(p[t+1]-p[i])>now.cross
247             (p[t]-p[i]))t=(t+1)%n;
248         while(now.dot(p[r+1]-p[i])>now.dot(p[r]
249             -p[i]))r=(r+1)%n;
250         if(!i)l=r;
251         while(now.dot(p[l+1]-p[i])<now.dot(p[
252             l]-p[i]))l=(l+1)%n;
253         T d=now.abs2();
254         T tmp=now.cross(p[t]-p[i])*(now.dot(p[
255             r]-p[i])-now.dot(p[l]-p[i]))/d;
256         ans=min(ans,tmp);
257     }
258     return p.pop_back(),ans;
259 }
260 T dis2(polygon &p1){//凸包最近距離平方
261     vector<point<T> > &P=p,&Q=p1.p;
262     int n=P.size(),m=Q.size(),l=0,r=0;
263     for(int i=0;i<n;++i)if(P[i].y<P[l].y)l=i;
264     for(int i=0;i<m;++i)if(Q[i].y<Q[r].y)r=i;
265     P.push_back(P[0]),Q.push_back(Q[0]);
266     T ans=1e99;
267     for(int i=0;i<n;++i){
268         while((P[l]-P[l+1]).cross(Q[r+1]-Q[r])
269             <0)r=(r+1)%m;
270         ans=min(ans,line<T>(P[l],P[l+1]).
271             seg_dis2(line<T>(Q[r],Q[r+1])));
272         l=(l+1)%n;
273     }
274     return P.pop_back(),Q.pop_back(),ans;
275 }
276 static char sign(const point<T>&t){
277     return (t.y==0?t.x:t.y)<0;
278 }
279 static bool angle_cmp(const line<T> &A,
280     const line<T> &B){
281     point<T> a=A.p2-A.p1,b=B.p2-B.p1;
282     return sign(a)<sign(b)|| (sign(a)==sign(b)
283         )&&a.cross(b)>0;
284 }
285 int halfplane_intersection(vector<line<T>
286     > &s){//半平面交
287     sort(s.begin(),s.end(),angle_cmp);//線段
288     左側為該線段半平面
289     int L,R,n=s.size();
290     vector<point<T> > px(n);
291     vector<line<T> > q(n);
292     q[L=R=0]=s[0];
293     for(int i=1;i<n;++i){
294         while(L<R&&s[i].ori(px[R-1])<=0)--R;
295         while(L<R&&s[i].ori(px[L])<=0)++L;
296         q[++R]=s[i];
297         if(q[R].parallel(q[R-1])){
298             --R;
299             if(q[R].ori(s[i].p1)>0)q[R]=s[i];
300         }
301     }
302 }
303 if(L<R)px[R-1]=q[R-1].
304     line_intersection(q[R]);
305 }
306 while(L<R&&q[L].ori(px[R-1])<=0)--R;
307 p.clear();
308 if(R-L<=1)return 0;
309 px[R]=q[R].line_intersection(q[L]);
310 for(int i=L;i<R;++i)p.push_back(px[i]);
311 return R-L+1;
312 }
313 };
314 template<typename T>
315 struct triangle{
316     point<T> a,b,c;
317     triangle(){
318         triangle(const point<T> &a,const point<T>
319             &b,const point<T> &c):a(a),b(b),c(c){}
320     }
321     T area()const{
322         T t=(b-a).cross(c-a)/2;
323         return t>0?t:-t;
324     }
325     point<T> barycenter()const{//重心
326         return (a+b+c)/3;
327     }
328 }
329 point<T> circumcenter()const{//外心
330     static line<T> u,v;
331     u.p1=(a+b)/2;
332     u.p2=point<T>(u.p1.x-a.y+b.y,u.p1.y+a.x-
333         b.x);
334     v.p1=(a+c)/2;
335     v.p2=point<T>(v.p1.x-a.y+c.y,v.p1.y+a.x-
336         c.x);
337     return u.line_intersection(v);
338 }
339 point<T> incenter()const{//內心
340     T A=sqrt((b-c).abs2()),B=sqrt((a-c).abs2
341         ()),C=sqrt((a-b).abs2());
342     return point<T>(A*a.x+B*b.x+C*c.x,A*a.y+
343         B*b.y+C*c.y)/(A+B+C);
344 }
345 point<T> perpcenter()const{//垂心
346     return barycenter()*3-circumcenter()*2;
347 }
348 };
349 template<typename T>
350 struct point3D{
351     T x,y,z;
352     point3D(){
353         point3D(const T&x,const T&y,const T&z):x(x
354             ),y(y),z(z){}
355     }
356     point3D operator+(const point3D &b)const{
357         return point3D(x+b.x,y+b.y,z+b.z);
358     }
359     point3D operator-(const point3D &b)const{
360         return point3D(x-b.x,y-b.y,z-b.z);
361     }
362     point3D operator*(const T &b)const{
363         return point3D(x*b,y*b,z*b);
364     }
365     point3D operator/(const T &b)const{
366         return point3D(x/b,y/b,z/b);
367     }
368     bool operator==(const point3D &b)const{
369         return x==b.x&&y==b.y&&z==b.z;
370     }
371     T dot(const point3D &b)const{
372         return x*b.x+y*b.y+z*b.z;
373     }
374     point3D cross(const point3D &b)const{
375         return point3D(y*b.z-z*b.y,z*b.x-x*b.z,x
376             *b.y-y*b.x);
377     }
378 }

```

```

318 T abs2()const{//向量長度的平方
319     return dot(*this);}
320 T area2(const point3D &b)const{//和b、原點
    圍成面積的平方
321     return cross(b).abs2()/4;}
322 };
323 template<typename T>
324 struct line3D{
325     point3D<T> p1,p2;
326     line3D(){}
327     line3D(const point3D<T> &p1,const point3D<
        T> &p2):p1(p1),p2(p2){}
328 T dis2(const point3D<T> &p,bool is_segment
    =0)const{//點跟直線/線段的距離平方
329     point3D<T> v=p2-p1,v1=p-p1;
330     if(is_segment){
331         point3D<T> v2=p-p2;
332         if(v.dot(v1)<=0)return v1.abs2();
333         if(v.dot(v2)>=0)return v2.abs2();
334     }
335     point3D<T> tmp=v.cross(v1);
336     return tmp.abs2()/v.abs2();
337 }
338 pair<point3D<T>,point3D<T> > closest_pair(
    const line3D<T> &l)const{
339     point3D<T> v1=(p1-p2),v2=(l.p1-l.p2);
340     point3D<T> N=v1.cross(v2),ab(p1-l.p1);
341     //if(N.abs2()==0)return NULL;平行或重合
342     T tmp=N.dot(ab),ans=tmp*tmp/N.abs2();//
    最近點對距離
343     point3D<T> d1=p2-p1,d2=l.p2-l.p1,D=d1.
        cross(d2),G=1.p1-p1;
344     T t1=(G.cross(d2)).dot(D)/D.abs2();
345     T t2=(G.cross(d1)).dot(D)/D.abs2();
346     return make_pair(p1+d1*t1,l.p1+d2*t2);
347 }
348 bool same_side(const point3D<T> &a,const
    point3D<T> &b)const{
349     return (p2-p1).cross(a-p1).dot((p2-p1).
        cross(b-p1))>0;
350 }
351 };
352 template<typename T>
353 struct plane{
354     point3D<T> p0,n;//平面上的點和法向量
355     plane(){}
356     plane(const point3D<T> &p0,const point3D<T>
        &n):p0(p0),n(n){}
357 T dis2(const point3D<T> &p)const{//點到平
    面距離的平方
358     T tmp=(p-p0).dot(n);
359     return tmp*tmp/n.abs2();
360 }
361 point3D<T> projection(const point3D<T> &p)
    const{
362     return p-n*(p-p0).dot(n)/n.abs2();
363 }
364 point3D<T> line_intersection(const line3D<
    T> &l)const{
365     T tmp=n.dot(l.p2-l.p1);//等於0表示平行或
    重合該平面
366     return l.p1+(l.p2-l.p1)*(n.dot(p0-l.p1)/
        tmp);
367 }

```

```

368 line3D<T> plane_intersection(const plane &
    pl)const{
369     point3D<T> e=n.cross(pl.n),v=n.cross(e);
370     T tmp=p1.n.dot(v);//等於0表示平行或重合
    該平面
371     point3D<T> q=p0+(v*(pl.n.dot(pl.p0-p0))/
        tmp);
372     return line3D<T>(q,q+e);
373 }
374 };
375 template<typename T>
376 struct triangle3D{
377     point3D<T> a,b,c;
378     triangle3D(){}
379     triangle3D(const point3D<T> &a,const
        point3D<T> &b,const point3D<T> &c):a(a
        ),b(b),c(c){}
380 bool point_in(const point3D<T> &p)const{//
    點在該平面上的投影在三角形中
381     return line3D<T>(b,c).same_side(p,a)&&
        line3D<T>(a,c).same_side(p,b)&&
        line3D<T>(a,b).same_side(p,c);
382 }
383 };
384 template<typename T>
385 struct tetrahedron{//四面體
386     point3D<T> a,b,c,d;
387     tetrahedron(){}
388     tetrahedron(const point3D<T> &a,const
        point3D<T> &b,const point3D<T> &c,
        const point3D<T> &d):a(a),b(b),c(c),d(
        d){}
389 T volume6()const{//體積的六倍
390     return (d-a).dot((b-a).cross(c-a));
391 }
392 point3D<T> centroid()const{
393     return (a+b+c+d)/4;
394 }
395 bool point_in(const point3D<T> &p)const{
396     return triangle3D<T>(a,b,c).point_in(p)
        &&triangle3D<T>(c,d,a).point_in(p);
397 }
398 };
399 template<typename T>
400 struct convexhull3D{
401     static const int MAXN=1005;
402     struct face{
403         int a,b,c;
404         face(int a,int b,int c):a(a),b(b),c(c){}
405     };
406     vector<point3D<T>> pt;
407     vector<face> ans;
408     int fid[MAXN][MAXN];
409     void build(){
410         int n=pt.size();
411         ans.clear();
412         memset(fid,0,sizeof(fid));
413         ans.emplace_back(0,1,2);//注意不能共線
414         ans.emplace_back(2,1,0);
415         int ftop = 0;
416         for(int i=3, ftop=1; i<n; ++i,++ftop){
417             vector<face> next;
418             for(auto &f:ans){
419                 T d=(pt[i]-pt[f.a]).dot((pt[f.b]-pt[
                    f.a]).cross(pt[f.c]-pt[f.a]));

```

```

420         if(d<=0) next.push_back(f);
421         int ff=0;
422         if(d>0) ff=ftop;
423         else if(d<0) ff=-ftop;
424         fid[f.a][f.b]=fid[f.b][f.c]=fid[f.c]
            ][f.a]=ff;
425     }
426     for(auto &f:ans){
427         if(fid[f.a][f.b]>0 && fid[f.a][f.b]
            !=fid[f.b][f.a])
428             next.emplace_back(f.a,f.b,i);
429         if(fid[f.b][f.c]>0 && fid[f.b][f.c]
            !=fid[f.c][f.b])
430             next.emplace_back(f.b,f.c,i);
431         if(fid[f.c][f.a]>0 && fid[f.c][f.a]
            !=fid[f.a][f.c])
432             next.emplace_back(f.c,f.a,i);
433     }
434     ans=next;
435 }
436 point3D<T> centroid()const{
437     point3D<T> res(0,0,0);
438     T vol=0;
439     for(auto &f:ans){
440         T tmp=pt[f.a].dot(pt[f.b].cross(pt[f.c]
            ));
441         res=res+(pt[f.a]+pt[f.b]+pt[f.c])*tmp;
442         vol+=tmp;
443     }
444     return res/(vol*4);
445 }
446 };
447 };

```

## 1.3 SmallestCircle

```

1 using PT=point<T>; using CPT=const PT;
2 PT circumcenter(CPT &a,CPT &b,CPT &c){
3     PT u=b-a, v=c-a;
4     T c1=u.abs2()/2,c2=v.abs2()/2;
5     T d=u.cross(v);
6     return PT(a.x+(v.y*c1-u.y*c2)/d,a.y+(u.x*
            c2-v.x*c1)/d);
7 }
8 void solve(PT p[],int n,PT &c,T &r2){
9     random_shuffle(p,p+n);
10    c=p[0]; r2=0; // c,r2 = 圓心,半徑平方
11    for(int i=1;i<n;i++){if((p[i]-c).abs2())>r2){
12        c=p[i]; r2=0;
13    }
14    for(int j=0;j<i;j++){if((p[j]-c).abs2())>r2){
15        c.x=(p[i].x+p[j].x)/2;
16        c.y=(p[i].y+p[j].y)/2;
17        r2=(p[j]-c).abs2();
18    }
19    for(int k=0;k<j;k++){if((p[k]-c).abs2())>r2){
20        c=circumcenter(p[i],p[j],p[k]);
21        r2=(p[i]-c).abs2();
22    }
23 }

```

## 1.4 最近點對

```

1 template<typename _IT=point<T>* >
2 T cloest_pair(_IT L, _IT R){
3     if(R-L <= 1) return INF;
4     _IT mid = L+(R-L)/2;
5     T x = mid->x;
6     T d = min(cloest_pair(L,mid),cloest_pair(
            mid,R));
7     inplace_merge(L, mid, R, ycmp);
8     static vector<point> b; b.clear();
9     for(auto u=L;u<R;++u){
10         if((u->x-x)*(u->x-x)>=d) continue;
11         for(auto v=b.rbegin();v!=b.rend();++v){
12             T dx=u->x-v->x, dy=u->y-v->y;
13             if(dy*dy>=d) break;
14             d=min(d,dx*dx+dy*dy);
15         }
16         b.push_back(*u);
17     }
18     return d;
19 }
20 T closest_pair(vector<point<T>> &v){
21     sort(v.begin(),v.end(),xcmp);
22     return closest_pair(v.begin(),v.end());
23 }

```

## 2 Data Structure

### 2.1 CDQ DP

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 const int MAXN = 100005;
4 struct node{
5     double a,b,r,k,x,y;
6     int id;
7 } p[MAXN];
8 double DP[MAXN];
9 deque<int> q;
10 bool cmpK(const node &a,const node &b){
11     return a.k>b.k;
12 }
13 bool cmpX(const node &a,const node &b){
14     return a.x<b.x||(a.x==b.x&&a.y<b.y);
15 }
16 double Slope(int a,int b){
17     if(!b) return -1e20;
18     if(p[a].x==p[b].x) return 1e20;
19     return (p[a].y-p[b].y)/(p[a].x-p[b].x);
20 }
21 void CDQ(int l, int r){
22     if(l==r){
23         DP[l] = max(DP[l],DP[l-1]);
24         p[l].y = DP[l]/(p[l].a*p[l].r+p[l].b);
25         p[l].x = p[l].y*p[l].r;
26         return;
27     }
28     int mid = (l+r)/2;

```

```

29 stable_partition(p+l,p+r+1,&)(const node
    &d){return d.id<=mid;});
30 CDQ(l, mid); q.clear();
31 for(int i=l, j; i<=mid; ++i){
32     while((j=q.size())>1&&Slope(q[j-2],q[j-1])<Slope(q[j-1],i)) q.pop_back();
33     q.push_back(i);
34 }q.push_back(0);
35 for(int i=mid+1; i<=r; ++i){
36     while(q.size()>1&&Slope(q[0],q[1])>p[i].k) q.pop_front();
37     DP[p[i].id] = max(DP[p[i].id], p[i].a*p[q[0]].x+p[i].b*p[q[0]].y);
38 }
39 CDQ(mid+1,r);
40 inplace_merge(p+l,p+mid+1,p+r+1,cmpX);
41 }
42 double solve(int n,double S){
43     DP[0] = S;
44     sort(p+l,p+1+n,cmpK);
45     CDQ(1,n);
46     return DP[n];
47 }
48 int main(){
49     int n; double S;
50     scanf("%d%lf",&n,&S);
51     for(int i=1; i<=n; ++i){
52         scanf("%lf%lf%lf",&p[i].a,&p[i].b,&p[i].r);
53         p[i].id = i, p[i].k = -p[i].a/p[i].b;
54     }
55     printf("%.3lf\n",solve(n,S));
56     return 0;
57 }

```

## 2.2 DLX

```

1 const int MAXN=4100, MAXM=1030, MAXND=16390;
2 struct DLX{
3     int n,m,sz,ansd;//高是n·寬是m的稀疏矩陣
4     int S[MAXN],H[MAXN];
5     int row[MAXN],col[MAXND];//每個節點代表的
6     列跟行
7     int L[MAXND],R[MAXND],U[MAXND],D[MAXND];
8     vector<int> ans,anst;
9     void init(int _n,int _m){
10         n=_n,m=_m;
11         for(int i=0;i<=m;++i){
12             U[i]=D[i]=i,L[i]=i-1,R[i]=i+1;
13             S[i]=0;
14         }
15         R[m]=0,L[0]=m;
16         sz=m,ansd=INT_MAX;//ansd存最優解的個數
17         for(int i=1;i<=n;++i)H[i]=-1;
18     }
19     void add(int r,int c){
20         ++S[col[++sz]=c];
21         row[sz]=r;
22         D[sz]=D[c],U[D[c]]=sz,U[sz]=c,D[c]=sz;
23         if(H[r]<0)H[r]=L[sz]=R[sz]=sz;
24         else R[sz]=R[H[r]],L[R[H[r]]]=sz,L[sz]=H[r],R[H[r]]=sz;

```

```

24 }
25 #define DFOR(i,A,s) for(int i=A[s];i!=s;i=
    A[i])
26 void remove(int c){//刪除第c行和所有當前覆
    蓋到第c行的列
27     L[R[c]]=L[c],R[L[c]]=R[c];//這裡刪除第c
    行·若有些行不需要處理可以在開始時呼
    叫他
28     DFOR(i,D,c)DFOR(j,R,i){U[D[j]]=U[j],D[U[
    j]]=D[j],--S[col[j]]};
29 }
30 void restore(int c){//恢復第c行和所有當前
    覆蓋到第c行的列·remove的逆操作
31     DFOR(i,U,c)DFOR(j,L,i){++S[col[j]],U[D[j
    ]]=j,D[U[j]]=j};
32     L[R[c]]=c,R[L[c]]=c;
33 }
34 void remove2(int nd){//刪除nd所在的行當前
    所有點(包括虛擬節點)·只保留nd
35     DFOR(i,D,nd)L[R[i]]=L[i],R[L[i]]=R[i];
36 }
37 void restore2(int nd){//刪除nd所在的行當前
    所有點·為remove2的逆操作
38     DFOR(i,U,nd)L[R[i]]=R[L[i]]=i;
39 }
40 bool vis[MAXN];
41 int h();//估價函數 for IDA*
42 int res=0;
43 memset(vis,0,sizeof(vis));
44 DFOR(i,R,0)if(!vis[i]){
45     vis[i]=1;
46     ++res;
47     DFOR(j,D,i)DFOR(k,R,j)vis[col[k]]=1;
48 }
49 return res;
50 }
51 bool dfs(int d){//for精確覆蓋問題
52     if(d+h()>=ansd)return 0;//找最佳解用·找
    任意解可以刪掉
53     if(!R[0]){ansd=d;return 1;}
54     int c=R[0];
55     DFOR(i,R,0)if(S[i]<S[c])c=i;
56     remove(c);
57     DFOR(i,D,c){
58         ans.push_back(row[i]);
59         DFOR(j,R,i)remove(col[j]);
60         if(dfs(d+1))return 1;
61         ans.pop_back();
62         DFOR(j,L,i)restore(col[j]);
63     }
64     restore(c);
65     return 0;
66 }
67 void dfs2(int d){//for最小重複覆蓋問題
68     if(d+h()>=ansd)return;
69     if(!R[0]){ansd=d;ans=anst;return;}
70     int c=R[0];
71     DFOR(i,R,0)if(S[i]<S[c])c=i;
72     DFOR(i,D,c){
73         anst.push_back(row[i]);
74         remove2(i);
75         DFOR(j,R,i)remove2(j),--S[col[j]];
76         dfs2(d+1);

```

```

77     anst.pop_back();
78     DFOR(j,L,i)restore2(j),++S[col[j]];
79     restore2(i);
80 }
81 }
82 bool exact_cover(){//解精確覆蓋問題
83     return ans.clear(), dfs(0);
84 }
85 void min_cover(){//解最小重複覆蓋問題
86     anst.clear();//暫存用·答案還是存在ans裡
87     dfs2(0);
88 }
89 #undef DFOR
90 };

```

## 2.3 Dynamic KD tree

```

1 template<typename T,size_t kd>//有kd個維度
2 struct kd_tree{
3     struct point{
4         T d[kd];
5         T dist(const point &x)const{
6             T ret=0;
7             for(size_t i=0;i<kd;++i)ret+=abs(d[i]-
                x.d[i]);
8             return ret;
9         }
10        bool operator==(const point &p){
11            for(size_t i=0;i<kd;++i)
12                if(d[i]!=p.d[i])return 0;
13            return 1;
14        }
15        bool operator<(const point &b)const{
16            return d[0]<b.d[0];
17        }
18    };
19    private:
20    struct node{
21        node *l,*r;
22        point pid;
23        int s;
24        node(const point &p):l(0),r(0),pid(p),s
            (1){}
25        ~node(){delete l,delete r;}
26        void up(){s=(l?l->s:0)+l+(r?r->s:0);}
27    }*root;
28    const double alpha,loga;
29    const T INF;//記得要給INF·表示極大值
30    int maxn;
31    struct __cmp{
32        int sort_id;
33        bool operator()(const node*x,const node*
            y)const{
34            return operator()(x->pid,y->pid);
35        }
36        bool operator()(const point &x,const
            point &y)const{
37            if(x.d[sort_id]!=y.d[sort_id])
38                return x.d[sort_id]<y.d[sort_id];
39            for(size_t i=0;i<kd;++i)
40                if(x.d[i]!=y.d[i])return x.d[i]<y.d[
                i];

```

```

41         return 0;
42     }
43 }cmp;
44 int size(node *o){return o?o->s:0;}
45 vector<node*> A;
46 node* build(int k,int l,int r){
47     if(l>r) return 0;
48     if(k==kd) k=0;
49     int mid=(l+r)/2;
50     cmp.sort_id = k;
51     nth_element(A.begin()+l,A.begin()+mid,A.
        begin()+r+1,cmp);
52     node *ret=A[mid];
53     ret->l = build(k+1,l,mid-1);
54     ret->r = build(k+1,mid+1,r);
55     ret->up();
56     return ret;
57 }
58 bool isbad(node*o){
59     return size(o->l)>alpha*o->s||size(o->r)
        >alpha*o->s;
60 }
61 void flatten(node *u,typename vector<node
    *>::iterator &it){
62     if(!u)return;
63     flatten(u->l,it);
64     *it=u;
65     flatten(u->r,++it);
66 }
67 void rebuild(node*&u,int k){
68     if((int)A.size()<u->s)A.resize(u->s);
69     auto it=A.begin();
70     flatten(u,it);
71     u=build(k,0,u->s-1);
72 }
73 bool insert(node*&u,int k,const point &x,
    int dep){
74     if(!u) return u=new node(x), dep<=0;
75     ++u->s;
76     cmp.sort_id=k;
77     if(insert(cmp(x,u->pid)?u->l:u->r,(k+1)%
        kd,x,dep-1)){
78         if(!isbad(u))return 1;
79         rebuild(u,k);
80     }
81     return 0;
82 }
83 node *findmin(node*o,int k){
84     if(!o)return 0;
85     if(cmp.sort_id==k)return o->l?findmin(o
        ->l,(k+1)%kd):o;
86     node *l=findmin(o->l,(k+1)%kd);
87     node *r=findmin(o->r,(k+1)%kd);
88     if(l&&l)return cmp(l,o)?l:o;
89     if(!l&&r)return cmp(r,o)?r:o;
90     if(l&&l&r)return o;
91     if(cmp(l,r))return cmp(l,o)?l:o;
92     return cmp(r,o)?r:o;
93 }
94 bool erase(node *&u,int k,const point &x){
95     if(!u)return 0;
96     if(u->pid==x){
97         if(u->r);
98         else if(u->l) u->r=u->l, u->l=0;
99         else return delete(u),u=0, 1;
100         --u->s;

```



```

101     cmp.sort_id=k;
102     u->pid=findmin(u->r,(k+1)%kd)->pid;
103     return erase(u->r,(k+1)%kd,u->pid);
104 }
105 cmp.sort_id=k;
106 if(erase(cmp(x,u->pid)?u->l:u->r,(k+1)%
107     kd,x))
108     return --u->s, 1;
109 return 0;
110 }
111 T heuristic(const T h[])const{
112     T ret=0;
113     for(size_t i=0;i<kd;++i)ret+=h[i];
114     return ret;
115 }
116 int qM;
117 priority_queue<pair<T,point>> pQ;
118 void nearest(node *u,int k,const point &x,
119     T *h,T &mndist){
120     if(u==0||heuristic(h)>=mndist)return;
121     T dist=u->pid.dist(x),old=h[k];
122     /*mndist=std::min(mndist,dist);*/
123     if(dist<mndist){
124         pQ.push(std::make_pair(dist,u->pid));
125         if((int)pQ.size()==qM+1)
126             mndist=pQ.top().first,pQ.pop();
127     }
128     if(x.d[k]<u->pid.d[k]){
129         nearest(u->l,(k+1)%kd,x,h,mndist);
130         h[k] = abs(x.d[k]-u->pid.d[k]);
131         nearest(u->r,(k+1)%kd,x,h,mndist);
132     }else{
133         nearest(u->r,(k+1)%kd,x,h,mndist);
134         h[k] = abs(x.d[k]-u->pid.d[k]);
135         nearest(u->l,(k+1)%kd,x,h,mndist);
136     }
137     h[k]=old;
138 }
139 vector<point>in_range;
140 void range(node *u,int k,const point&mi,
141     const point&ma){
142     if(!u)return;
143     bool is=1;
144     for(int i=0;i<kd;++i)
145         if(u->pid.d[i]<mi.d[i]||ma.d[i]<u->pid
146             .d[i])
147             { is=0;break; }
148     if(is) in_range.push_back(u->pid);
149     if(mi.d[k]<u->pid.d[k])range(u->l,(k+1)
150         %kd,mi,ma);
151     if(ma.d[k]>u->pid.d[k])range(u->r,(k+1)
152         %kd,mi,ma);
153 }
154 public:
155 kd_tree(const T &INF,double a=0.75):
156     root(0),alpha(a),loga(log2(1.0/a)),INF(INF
157         ),maxn(1){}
158 ~kd_tree(){delete root;}
159 void clear(){delete root,root=0,maxn=1;}
160 void build(int n,const point *p){
161     delete root,A.resize(maxn=n);
162     for(int i=0;i<n;++i)A[i]=new node(p[i]);
163     root=build(0,0,n-1);
164 }
165 void insert(const point &x){
166     insert(root,0,x,__lg(size(root))/loga);

```

```

160     if(root->s>maxn)maxn=root->s;
161 }
162 bool erase(const point &p){
163     bool d=erase(root,0,p);
164     if(root&&root->s<alpha*maxn)rebuild();
165     return d;
166 }
167 void rebuild(){
168     if(root)rebuild(root,0);
169     maxn=root->s;
170 }
171 T nearest(const point &x,int k){
172     qM=k;
173     T mndist=INF,h[kd]={};
174     nearest(root,0,x,h,mndist);
175     mndist=pQ.top().first;
176     pQ = priority_queue<pair<T,point>>();
177     return mndist; // 回傳離x第k近的點的距離
178 }
179 const vector<point> &range(const point&mi,
180     const point&ma){
181     in_range.clear();
182     range(root,0,mi,ma);
183     return in_range; // 回傳介於mi到ma之間的點
184     vector
185 }
186 int size(){return root?root->s:0;}
187 };

```

## 2.4 kd tree replace segment tree

```

1 struct node{//kd樹代替高維線段樹
2     node *l,*r;
3     point pid,mi,ma;
4     int s, data;
5     node(const point &p,int d):l(0),r(0),pid(p
6         ),mi(p),ma(p),s(1),data(d),dmin(d),
7         dmax(d){}
8     void up(){
9         mi=ma=pid;
10        s=1;
11        if(l){
12            for(int i=0;i<kd;++i){
13                mi.d[i]=min(mi.d[i],l->mi.d[i]);
14                ma.d[i]=max(ma.d[i],l->ma.d[i]);
15            }
16            s+=l->s;
17        }
18        if(r){
19            for(int i=0;i<kd;++i){
20                mi.d[i]=min(mi.d[i],r->mi.d[i]);
21                ma.d[i]=max(ma.d[i],r->ma.d[i]);
22            }
23            s+=r->s;
24        }
25        void up2(){/*其他懶惰標記向上更新*/}
26        void down(){/*其他懶惰標記下推*/}
27    }*root;
28    //檢查區間包含用的函數

```

```

28 bool range_include(node *o,const point &L,
29     const point &R){
30     for(int i=0;i<kd;++i){
31         if(L.d[i]>o->ma.d[i]||R.d[i]<o->mi.d[i])
32             return 0;
33     }
34     return 1;
35 }
36 bool range_in_range(node *o,const point &L,
37     const point &R){
38     for(int i=0;i<kd;++i){
39         if(L.d[i]>o->mi.d[i]||o->ma.d[i]>R.d[i])
40             return 0;
41     }
42     return 1;
43 }
44 bool point_in_range(node *o,const point &L,
45     const point &R){
46     for(int i=0;i<kd;++i){
47         if(L.d[i]>o->pid.d[i]||R.d[i]<o->pid.d[i]
48             )return 0;
49     }
50     return 1;
51 }
52 //區間完全包含o->pid這個點就回傳true
53 return 1;
54 }
55 //單點修改 · 以單點改值為例
56 void update(node *u,const point &x,int data,
57     int k=0){
58     if(!u)return;
59     u->down();
60     if(u->pid==x){
61         u->data=data;
62         u->up2();
63         return;
64     }
65     cmp.sort_id=k;
66     update(cmp(x,u->pid)?u->l:u->r,x,data,(k
67         +1)%kd);
68     u->up2();
69 }
70 //區間修改
71 void update(node *o,const point &L,const
72     point &R,int data){
73     if(!o)return;
74     o->down();
75     if(range_in_range(o,L,R)){
76         //區間懶惰標記修改
77         o->down();
78         return;
79     }
80     if(point_in_range(o,L,R)){
81         //這個點在(L,R)區間 · 但是他的左右子樹不
82         //一定在區間中
83         //單點懶惰標記修改
84     }
85     if(o->l&&range_include(o->l,L,R))update(o
86         ->l,L,R,data);
87     if(o->r&&range_include(o->r,L,R))update(o
88         ->r,L,R,data);
89     o->up2();
90 }
91 //區間查詢 · 以總和為例
92 int query(node *o,const point &L,const point
93     &R){
94     if(!o)return 0;

```

```

79     o->down();
80     if(range_in_range(o,L,R))return o->sum;
81     int ans=0;
82     if(point_in_range(o,L,R))ans+=o->data;
83     if(o->l&&range_include(o->l,L,R))ans+=
84         query(o->l,L,R);
85     if(o->r&&range_include(o->r,L,R))ans+=
86         query(o->r,L,R);
87     return ans;
88 }

```

## 2.5 reference point

```

1 template<typename T>
2 struct _RefC{
3     T data;
4     int ref;
5     _RefC(const T&d=0):data(d),ref(0){}
6 };
7 template<typename T>
8 struct _rp{
9     _RefC<T> *p;
10    T *operator->(){return &p->data;}
11    T &operator*(){return p->data;}
12    operator _RefC<T>*(){return p;}
13    _rp &operator=(const _rp &t){
14        if(p&&!-p->ref)delete p;
15        p=t.p,p&&+p->ref;
16        return *this;
17    }
18    _rp(_RefC<T> *t=0):p(t){p&&+p->ref;}
19    _rp(const _rp &t):p(t.p){p&&+p->ref;}
20    ~_rp(){if(p&&!-p->ref)delete p;}
21 };
22 template<typename T>
23 inline _rp<T> new_rp(const T&nd){
24     return _rp<T>(new _RefC<T>(nd));
25 }

```

## 2.6 skew heap

```

1 node *merge(node *a,node *b){
2     if(!a||!b) return a?a:b;
3     if(b->data<a->data) swap(a,b);
4     swap(a->l,a->r);
5     a->l=merge(b,a->l);
6     return a;
7 }

```

## 2.7 undo disjoint set

```

1 struct DisjointSet {
2     // save() is like recursive
3     // undo() is like return
4     int n, fa[MXN], sz[MXN];
5     vector<pair<int*,int>> h;

```

```

6 vector<int> sp;
7 void init(int tn) {
8     n=tn;
9     for (int i=0; i<n; i++) sz[fa[i]=i]=1;
10    sp.clear(); h.clear();
11 }
12 void assign(int *k, int v) {
13     h.PB({k, *k});
14     *k=v;
15 }
16 void save() { sp.PB(SZ(h)); }
17 void undo() {
18     assert(!sp.empty());
19     int last=sp.back(); sp.pop_back();
20     while (SZ(h)!=last) {
21         auto x=h.back(); h.pop_back();
22         *x.F=x.S;
23     }
24 }
25 int f(int x) {
26     while (fa[x]!=x) x=fa[x];
27     return x;
28 }
29 void uni(int x, int y) {
30     x=f(x); y=f(y);
31     if (x==y) return;
32     if (sz[x]<sz[y]) swap(x, y);
33     assign(&sz[x], sz[x]+sz[y]);
34     assign(&fa[y], x);
35 }
36 }djs;

```

## 2.8 整體二分

```

1 void totBS(int L, int R, vector<Item> M){
2     if(Q.empty()) return; //維護全域B陣列
3     if(L==R) 整個M的答案=r, return;
4     int mid = (L+R)/2;
5     vector<Item> mL, mR;
6     do_modify_B_with_divide(mid,M);
7     //讓B陣列在遞迴的時候只會保留[L~mid]的資訊
8     undo_modify_B(mid,M);
9     totBS(L,mid,mL);
10    totBS(mid+1,R,mR);
11 }

```

## 3 Flow

### 3.1 dinic

```

1 template<typename T>
2 struct DINIC{
3     static const int MAXN=105;
4     static const T INF=INT_MAX;
5     int n, LV[MAXN], cur[MAXN];
6     struct edge{
7         int v,pre;

```

```

8         T cap,r;
9         edge(int v,int pre,T cap):v(v),pre(pre),
10            cap(cap),r(cap){}
11     };
12     vector<edge> e;
13     void init(int _n){
14         memset(g,-1,sizeof(int)*((n=_n)+1));
15         e.clear();
16     }
17     void add_edge(int u,int v,T cap,bool
18        directed=false){
19         e.push_back(edge(v,g[u],cap));
20         g[u]=e.size()-1;
21         e.push_back(edge(u,g[v],directed?0:cap));
22         g[v]=e.size()-1;
23     }
24     int bfs(int s,int t){
25         memset(LV,0,sizeof(int)*(n+1));
26         memcpy(cur,g,sizeof(int)*(n+1));
27         queue<int> q;
28         LV[s]=1;
29         while(q.size()){
30             int u=q.front();q.pop();
31             for(int i=g[u];~i;i=e[i].pre){
32                 if(!LV[e[i].v]&&e[i].r){
33                     LV[e[i].v]=LV[u]+1;
34                     q.push(e[i].v);
35                     if(e[i].v==t) return 1;
36                 }
37             }
38         }
39         return 0;
40     }
41     T dfs(int u,int t,T CF=INF){
42         if(u==t) return CF;
43         T df;
44         for(int &i=cur[u];~i;i=e[i].pre){
45             if(LV[e[i].v]==LV[u]+1&&e[i].r){
46                 if(df=dfs(e[i].v,t,min(CF,e[i].r))){
47                     e[i].r-=df;
48                     e[i^1].r+=df;
49                     return df;
50                 }
51             }
52         }
53         return LV[u]=0;
54     }
55     T dinic(int s,int t,bool clean=true){
56         if(clean)for(size_t i=0;i<e.size();++i)
57             e[i].r=e[i].cap;
58         T ans=0, f=0;
59         while(bfs(s,t))while(f=dfs(s,t))ans+=f;
60         return ans;
61     }
62 };

```

### 3.2 Gomory Hu

```

1 //最小割樹+求任兩點間最小割
2 //0-base, root=0

```

```

3 LL e[MAXN][MAXN]; //任兩點間最小割
4 int p[MAXN]; //parent
5 ISAP D; // original graph
6 void gomory_hu(){
7     fill(p, p+n, 0);
8     fill(e[0], e[n], INF);
9     for( int s = 1; s < n; ++s ) {
10         int t = p[s];
11         ISAP F = D;
12         LL tmp = F.min_cut(s, t);
13         for( int i = 1; i < s; ++i )
14             e[s][i] = e[i][s] = min(tmp, e[t][i]);
15         for( int i = s+1; i <= n; ++i )
16             if( p[i] == t && F.vis[i] ) p[i] = s;
17     }
18 }

```

### 3.3 ISAP with cut

```

1 template<typename T>
2 struct ISAP{
3     static const int MAXN=105;
4     static const T INF=INT_MAX;
5     int n;//點數
6     int d[MAXN],gap[MAXN],cur[MAXN];
7     struct edge{
8         int v,pre;
9         T cap,r;
10        edge(int v,int pre,T cap):v(v),pre(pre),
11           cap(cap),r(cap){}
12     };
13     vector<edge> e;
14     void init(int _n){
15         memset(g,-1,sizeof(int)*((n=_n)+1));
16         e.clear();
17     }
18     void add_edge(int u,int v,T cap,bool
19        directed=false){
20         e.push_back(edge(v,g[u],cap));
21         g[u]=e.size()-1;
22         e.push_back(edge(u,g[v],directed?0:cap));
23         g[v]=e.size()-1;
24     }
25     T dfs(int u,int s,int t,T CF=INF){
26         if(u==t) return CF;
27         T tf=CF,df;
28         for(int &i=cur[u];~i;i=e[i].pre){
29             if(e[i].r&&d[u]==d[e[i].v]+1){
30                 df=dfs(e[i].v,s,t,min(tf,e[i].r));
31                 e[i].r-=df;
32                 e[i^1].r+=df;
33                 if(!(tf-=df)||d[s]==n) return CF-tf;
34             }
35         }
36         int mh=n;
37         for(int i=cur[u]=g[u];~i;i=e[i].pre){
38             if(e[i].r&&d[e[i].v]<mh)mh=d[e[i].v];
39         }
40         if(!-gap[d[u]])d[s]=n;
41         else ++gap[d[u]]+=mh;
42         return CF-tf;

```

```

43     }
44     T isap(int s,int t,bool clean=true){
45         memset(d,0,sizeof(int)*(n+1));
46         memset(gap,0,sizeof(int)*(n+1));
47         memcpy(cur,g,sizeof(int)*(n+1));
48         if(clean) for(size_t i=0;i<e.size();++i)
49             e[i].r=e[i].cap;
50         T MF=0;
51         for(gap[0]=n;d[s]<n;)MF+=dfs(s,s,t);
52         return MF;
53     }
54     vector<int> cut_e;//最小割邊集
55     bool vis[MAXN];
56     void dfs_cut(int u){
57         vis[u]=1;//表示u屬於source的最小割集
58         for(int i=g[u];~i;i=e[i].pre)
59             if(e[i].r>0&&!vis[e[i].v])dfs_cut(e[i].v);
60     }
61     T min_cut(int s,int t){
62         T ans=isap(s,t);
63         memset(vis,0,sizeof(bool)*(n+1));
64         dfs_cut(s); cut_e.clear();
65         for(int u=0;u<n;++u)if(vis[u])
66             for(int i=g[u];~i;i=e[i].pre)
67                 if(!vis[e[i].v])cut_e.push_back(i);
68         return ans;
69     };

```

### 3.4 MinCostMaxFlow

```

1 template<typename TP>
2 struct MCMF{
3     static const int MAXN=440;
4     static const TP INF=999999999;
5     struct edge{
6         int v,pre;
7         TP r,cost;
8         edge(int v,int pre,TP r,TP cost):v(v),
9            pre(pre),r(r),cost(cost){}
10    };
11    int n,S,T;
12    TP dis[MAXN],PIS,ans;
13    bool vis[MAXN];
14    vector<edge> e;
15    int g[MAXN];
16    void init(int _n){
17        memset(g,-1,sizeof(int)*((n=_n)+1));
18        e.clear();
19    }
20    void add_edge(int u,int v,TP r,TP cost,
21        bool directed=false){
22        e.push_back(edge(v,g[u],r,cost));
23        g[u]=e.size()-1;
24        e.push_back(
25            edge(u,g[v],directed?0:r,-cost));
26        g[v]=e.size()-1;
27    }
28    TP augment(int u,TP CF){
29        if(u==T||!CF) return ans+=PIS*CF,CF;
30        vis[u]=1;

```

```

29 TP r=CF,d;
30 for(int i=g[u];~i;i=e[i].pre){
31     if(e[i].r&&!e[i].cost&&!vis[e[i].v]){
32         d=augment(e[i].v,min(r,e[i].r));
33         e[i].r-=d;
34         e[i^1].r+=d;
35         if(!(r-=d))break;
36     }
37 }
38 return CF-r;
39 }
40 bool modlabel(){
41     for(int u=0;u<n;++u)dis[u]=INF;
42     static deque<int>q;
43     dis[T]=0,q.push_back(T);
44     while(q.size()){
45         int u=q.front();q.pop_front();
46         TP dt;
47         for(int i=g[u];~i;i=e[i].pre){
48             if(e[i^1].r&&(dt=dis[u]-e[i].cost)<
49                 dis[e[i].v]){
50                 if((dis[e[i].v]=dt)<=dis[q.size()]){
51                     q.front():S(){
52                         q.push_front(e[i].v);
53                     }else q.push_back(e[i].v);
54                 }
55             }
56         }
57         for(int u=0;u<n;++u)
58             for(int i=g[u];~i;i=e[i].pre)
59                 e[i].cost+=dis[e[i].v]-dis[u];
60         return PIS+=dis[S], dis[S]<INF;
61     }
62     TP mincost(int s,int t){
63         S=s,T=t;
64         PIS=ans=0;
65         while(modlabel()){
66             do memset(vis,0,sizeof(bool)*(n+1));
67             while(augment(S,INF));
68         }return ans;
69     }
70 }

```

## 4 Graph

### 4.1 Augmenting Path

```

1 #define MAXN1 505
2 #define MAXN2 505
3 int n1,n2;//n1個點連向n2個點
4 int match[MAXN2];//屬於n2的點匹配了哪個點
5 vector<int> g[MAXN1];//圖 0-base
6 bool vis[MAXN2];//是否走訪過
7 bool dfs(int u){
8     for(int v:g[u]){
9         if(vis[v]) continue;
10        vis[v]=1;
11        if(match[v]==-1||dfs(match[v]))
12            return match[v]=u, 1;
13    }

```

```

14     return 0;
15 }
16 int max_match(){
17     int ans=0;
18     memset(match,-1,sizeof(int)*n2);
19     for(int i=0;i<n1;++i){
20         memset(vis,0,sizeof(bool)*n2);
21         if(dfs(i)) ++ans;
22     }
23     return ans;
24 }

```

### 4.2 Augmenting Path multiple

```

1 #define MAXN1 1005
2 #define MAXN2 505
3 int n1,n2;
4 //n1個點連向n2個點，其中n2個點可以匹配很多邊
5 vector<int> g[MAXN1];//圖 0-base
6 size_t c[MAXN2];
7 //每個屬於n2點最多可以接受幾條匹配邊
8 vector<int> matchs[MAXN2];
9 //每個屬於n2的點匹配了那些點
10 bool vis[MAXN2];
11 bool dfs(int u){
12     for(int v:g[u]){
13         if(vis[v])continue;
14         vis[v] = 1;
15         if(matchs[v].size()<c[v]){
16             return matchs[v].push_back(u), 1;
17         }else for(size_t j=0;j<matchs[v].size()
18             ;++j){
19             if(dfs(matchs[v][j]))
20                 return matchs[v][j]=u, 1;
21         }
22     }
23     return 0;
24 }
25 int max_match(){
26     for(int i=0;i<n2;++i) matchs[i].clear();
27     int cnt=0;
28     for(int u=0;u<n1;++u){
29         memset(vis,0,sizeof(bool)*n2);
30         if(dfs(u))++cnt;
31     }
32     return cnt;
33 }

```

### 4.3 blossom matching

```

1 #define MAXN 505
2 int n; //1-base
3 vector<int> g[MAXN];
4 int MH[MAXN]; //output MH
5 int pa[MAXN],st[MAXN],S[MAXN],v[MAXN],t;
6 int lca(int x,int y){
7     for(++t;swap(x,y)){
8         if(!x) continue;
9         if(v[x]==t) return x;

```

```

10        v[x] = t;
11        x = st[pa[MH[x]]];
12    }
13 }
14 #define qpush(x) q.push(x),S[x]=0
15 void flower(int x,int y,int l,queue<int>&q){
16     while(st[x]!=1){
17         pa[x]=y;
18         if(S[y==MH[x]]==1)qpush(y);
19         st[x]=st[y]=1, x=pa[y];
20     }
21 }
22 bool bfs(int x){
23     iota(st+1, st+n+1, 1);
24     memset(S+1,-1,sizeof(int)*n);
25     queue<int>q; qpush(x);
26     while(q.size()){
27         x=q.front(),q.pop();
28         for(int y:g[x]){
29             if(S[y]==-1){
30                 pa[y]=x,S[y]=1;
31                 if(!MH[y]){
32                     for(int lst;x=y;lst,x=pa[y])
33                         lst=MH[lst],MH[lst]=y,MH[y]=x;
34                     return 1;
35                 }
36                 qpush(MH[y]);
37             }else if(!S[y]&&st[y]!=st[x]){
38                 int l=lca(y,x);
39                 flower(y,x,l,q),flower(x,y,l,q);
40             }
41         }
42     }
43     return 0;
44 }
45 int blossom(){
46     memset(MH+1,0,sizeof(int)*n);
47     int ans=0;
48     for(int i=1;i<n;++i)
49         if(!MH[i]&&bfs(i)) ++ans;
50     return ans;
51 }

```

### 4.4 BronKerbosch

```

1 struct maximalCliques{
2     using Set = vector<int>;
3     size_t n; //1-base
4     vector<Set> G;
5     static Set setUnion(const Set &A, const
6         Set &B){
7         Set C(A.size() + B.size());
8         auto it = set_union(A.begin(),A.end(),B.
9             begin(),B.end(),C.begin());
10        C.erase(it, C.end());
11        return C;
12    }
13 }
14 static Set setIntersection(const Set &A,
15     const Set &B){
16     Set C(min(A.size(), B.size()));
17     auto it = set_intersection(A.begin(),A.
18         end(),B.begin(),B.end(),C.begin());
19     C.erase(it, C.end());

```

```

15     return C;
16 }
17 static Set setDifference(const Set &A,
18     const Set &B){
19     Set C(min(A.size(), B.size()));
20     auto it = set_difference(A.begin(),A.end
21         (),B.begin(),B.end(),C.begin());
22     C.erase(it, C.end());
23     return C;
24 }
25 void BronKerbosch1(Set R, Set P, Set X){
26     if(P.empty()&&X.empty()){
27         // R form an maximal clique
28         return;
29     }
30     for(auto v: P){
31         BronKerbosch1(setUnion(R,{v}),
32             setIntersection(P,G[v]),
33             setIntersection(X,G[v]));
34         P = setDifference(P,{v});
35         X = setUnion(X,{v});
36     }
37 }
38 void init(int _n){
39     G.clear();
40     G.resize((n = _n) + 1);
41 }
42 void addEdge(int u, int v){
43     G[u].emplace_back(v);
44     G[v].emplace_back(u);
45 }
46 void solve(int n){
47     Set P;
48     for(int i=1;i<n;++i){
49         sort(G[i].begin(), G[i].end());
50         G[i].erase(unique(G[i].begin(), G[i].end()),
51             G[i].end());
52         P.emplace_back(i);
53     }
54     BronKerbosch1({}, P, {});
55 }

```

### 4.5 graphISO

```

1 const int MAXN=1005,K=30;//K要夠大
2 const long long A=3,B=11,C=2,D=19,P=0
3 xdefaced;
4 long long f[K+1][MAXN];
5 vector<int> g[MAXN],rg[MAXN];
6 int n;
7 void init(){
8     for(int i=0;i<n;++i){
9         f[0][i]=1;
10        g[i].clear(), rg[i].clear();
11    }
12 }
13 void add_edge(int u,int v){
14     g[u].push_back(v), rg[v].push_back(u);
15 }
16 long long point_hash(int u){//O(N)
17     for(int t=1;t<=K;++t){
18         for(int i=0;i<n;++i){

```

```

18 f[t][i]=f[t-1][i]*A%P;
19 for(int j:g[i])f[t][i]=(f[t][i]+f[t
20 -1][j]*B%P)%P;
21 for(int j:rg[i])f[t][i]=(f[t][i]+f[t
22 -1][j]*C%P)%P;
23 if(i==u)f[t][i]+=D; //如果圖太大的話，
24 把這行刪掉，執行一次後f[K]就會是所
25 有點的答案
26 f[t][i]=P;
27 }
28 return f[K][u];
29 }
30 vector<long long> graph_hash(){
31 vector<long long> ans;
32 for(int i=0;i<n;++i)ans.push_back(
33 point_hash(i)); //O(N^2)
34 sort(ans.begin(),ans.end());
35 return ans;
36 }

```

## 4.6 KM

```

1 #define MAXN 405
2 #define INF 0x3f3f3f3f3f3f3f3f
3 int n; // 1-base, 0表示沒有匹配
4 LL g[MAXN][MAXN]; //input graph
5 int My[MAXN], Mx[MAXN]; //output match
6 LL lx[MAXN], ly[MAXN], pa[MAXN], Sy[MAXN];
7 bool vx[MAXN], vy[MAXN];
8 void augment(int y){
9     for(int x, z; y; y = z){
10         x=pa[y], z=Mx[x];
11         My[y]=x, Mx[x]=y;
12     }
13 }
14 void bfs(int st){
15     for(int i=1; i<=n; ++i)
16         Sy[i] = INF, vx[i]=vy[i]=0;
17     queue<int> q; q.push(st);
18     for(;;){
19         while(q.size()){
20             int x=q.front(); q.pop();
21             vx[x]=1;
22             for(int y=1; y<=n; ++y) if(!vy[y]){
23                 LL t = lx[x]+ly[y]-g[x][y];
24                 if(t==0){
25                     pa[y]=x;
26                     if(!My[y]){augment(y);return;}
27                     vy[y]=1, q.push(My[y]);
28                 }else if(Sy[y]>t) pa[y]=x, Sy[y]=t;
29             }
30         }
31         LL cut = INF;
32         for(int y=1; y<=n; ++y)
33             if(!vy[y]&&cut>Sy[y]) cut=Sy[y];
34         for(int j=1; j<=n; ++j){
35             if(vx[j]) lx[j] -= cut;
36             if(vy[j]) ly[j] += cut;
37             else Sy[j] -= cut;
38         }
39         for(int y=1; y<=n; ++y){

```

```

40         if(!vy[y]&&Sy[y]==0){
41             if(!My[y]){augment(y);return;}
42             vy[y]=1, q.push(My[y]);
43         }
44     }
45 }
46 }
47 LL KM(){
48     memset(My,0,sizeof(int)*(n+1));
49     memset(Mx,0,sizeof(int)*(n+1));
50     memset(ly,0,sizeof(LL)*(n+1));
51     for(int x=1; x<=n; ++x){
52         lx[x] = -INF;
53         for(int y=1; y<=n; ++y)
54             lx[x] = max(lx[x], g[x][y]);
55     }
56     for(int x=1; x<=n; ++x) bfs(x);
57     LL ans = 0;
58     for(int y=1; y<=n; ++y) ans+=g[My[y]][y];
59     return ans;
60 }

```

## 4.7 MaximumClique

```

1 struct MaxClique{
2     static const int MAXN=105;
3     int N,ans;
4     int g[MAXN][MAXN], dp[MAXN], stk[MAXN][MAXN];
5     int sol[MAXN], tmp[MAXN]; //sol[0~ans-1] 為答案
6     void init(int n){
7         N=n; //0-base
8         memset(g,0,sizeof(g));
9     }
10     void add_edge(int u,int v){
11         g[u][v]=g[v][u]=1;
12     }
13     int dfs(int ns,int dep){
14         if(!ns){
15             if(dep>ans){
16                 ans=dep;
17                 memcpy(sol,tmp,sizeof tmp);
18                 return 1;
19             }else return 0;
20         }
21         for(int i=0; i<ns; ++i){
22             if(dep+ns-i<=ans) return 0;
23             int u=stk[dep][i], cnt=0;
24             if(dep+dp[u]<=ans) return 0;
25             for(int j=i+1; j<ns; ++j){
26                 int v=stk[dep][j];
27                 if(g[u][v]) stk[dep+1][cnt++]=v;
28             }
29             tmp[dep]=u;
30             if(dfs(cnt,dep+1)) return 1;
31         }
32         return 0;
33     }
34     int clique(){
35         int u,v,ns;
36         for(ans=0, u=N-1; u>=0; --u){

```

```

37         for(ns=0, tmp[0]=u, v=u+1; v<N; ++v)
38             if(g[u][v]) stk[1][ns++]=v;
39         dfs(ns,1), dp[u]=ans;
40     }
41     return ans;
42 }
43 };

```

## 4.8 MinimumMeanCycle

```

1 #include<cstdio> //for DBL_MAX
2 int dp[MAXN][MAXN]; // 1-base, 0(NM)
3 vector<tuple<int,int,int>> edge;
4 double mmc(int n){ //allow negative weight
5     const int INF=0x3f3f3f3f;
6     for(int t=0; t<n; ++t){
7         memset(dp[t+1],0,sizeof(dp[t+1]));
8         for(const auto &e:edge){
9             int u,v,w;
10             tie(u,v,w) = e;
11             dp[t+1][v]=min(dp[t+1][v], dp[t][u]+w);
12         }
13     }
14     double res = DBL_MAX;
15     for(int u=1; u<=n; ++u){
16         if(dp[n][u]==INF) continue;
17         double val = -DBL_MAX;
18         for(int t=0; t<n; ++t)
19             val=max(val, (dp[n][u]-dp[t][u])*1.0/(n-t));
20         res=min(res, val);
21     }
22     return res;
23 }

```

## 4.9 Rectilinear MST

```

1 //平面曼哈頓最小生成樹構造圖(去除非必要邊)
2 #define T int
3 #define INF 0x3f3f3f3f
4 struct point{
5     T x,y;
6     int id; //從0開始編號
7     point(){
8         T dist(const point &p) const{
9             return abs(x-p.x)+abs(y-p.y);
10         }
11     };
12     bool cmpx(const point &a, const point &b){
13         return a.x<b.x || (a.x==b.x && a.y<b.y);
14     }
15     struct edge{
16         int u,v;
17         T cost;
18         edge(int u,int v,T c):u(u),v(v),cost(c){}
19         bool operator<(const edge&e) const{
20             return cost<e.cost;
21         }
22     };

```

```

23 struct bit_node{
24     T mi;
25     int id;
26     bit_node(const T&mi=INF, int id=-1):mi(mi),id(id){}
27 };
28 vector<bit_node> bit;
29 void bit_update(int i, const T&data, int id){
30     for(;; i=i&(-i)){
31         if(data<bit[i].mi) bit[i]=bit_node(data, id);
32     }
33 }
34 int bit_find(int i, int m){
35     bit_node x;
36     for(;; i=i&(-i)) if(bit[i].mi<x.mi) x=bit[i];
37     return x.id;
38 }
39 vector<edge> build_graph(int n, point p[]){
40     vector<edge> e; //edge for MST
41     for(int dir=0; dir<4; ++dir){ //4種座標變換
42         if(dir%2) for(int i=0; i<n; ++i) swap(p[i].x, p[i].y);
43         else if(dir==2) for(int i=0; i<n; ++i) p[i].x=-p[i].x;
44         sort(p, p+n, cmpx);
45         vector<T> ga(n), gb;
46         for(int i=0; i<n; ++i) ga[i]=p[i].y-p[i].x;
47         gb=ga, sort(gb.begin(), gb.end());
48         gb.erase(unique(gb.begin(), gb.end()), gb.end());
49         int m=gb.size();
50         bit=vector<bit_node>(m+1);
51         for(int i=n-1; i>=0; --i){
52             int pos=lower_bound(gb.begin(), gb.end(), ga[i])-gb.begin()+1;
53             int ans=bit.find(pos, m);
54             if(~ans) e.push_back(edge(p[i].id, p[ans].id, p[i].dist(p[ans])));
55             bit_update(pos, p[i].x+p[i].y, i);
56         }
57     }
58     return e;
59 }

```

## 4.10 treeISO

```

1 const int MAXN=100005;
2 const long long X=12327, P=0xdefaced;
3 vector<int> g[MAXN];
4 bool vis[MAXN];
5 long long dfs(int u){ //hash ver
6     vis[u]=1;
7     vector<long long> tmp;
8     for(auto v:g[u]) if(!vis[v]) tmp.pb(dfs(v));
9     if(tmp.empty()) return 177;
10     long long ret=4931;
11     sort(tmp.begin(), tmp.end());
12     for(auto v:tmp) ret=((ret*X)^v)%P;
13     return ret;
14 }
15 //-----

```



```

16 string dfs(int x,int p){
17     vector<string> c;
18     for(int y:g[x])
19         if(y!=p)c.emplace_back(dfs(y,x));
20     sort(c.begin(),c.end());
21     string ret("(");
22     for(auto &s:c)ret+=s;
23     ret+=")";
24     return ret;
25 }

```

#### 4.11 一般圖最小權完美匹配

```

1 struct Graph {
2     // Minimum General Weighted Matching (
3     Perfect Match) 0-base
4     static const int MXN = 105;
5     int n, edge[MXN][MXN];
6     int match[MXN],dis[MXN],onstk[MXN];
7     vector<int> stk;
8     void init(int _n) {
9         n = _n;
10        for (int i=0; i<n; i++)
11            for (int j=0; j<n; j++)
12                edge[i][j] = 0;
13    }
14    void add_edge(int u, int v, int w) {
15        edge[u][v] = edge[v][u] = w;
16    }
17    bool SPFA(int u){
18        if (onstk[u]) return true;
19        stk.push_back(u);
20        onstk[u] = 1;
21        for (int v=0; v<n; v++){
22            if (u != v && match[u] != v && !onstk[v]){
23                int m = match[v];
24                if (dis[m] > dis[u] - edge[v][m] +
25                    edge[u][v]){
26                    dis[m] = dis[u] - edge[v][m] +
27                        edge[u][v];
28                    onstk[v] = 1;
29                    stk.push_back(v);
30                    if (SPFA(m)) return true;
31                    stk.pop_back();
32                    onstk[v] = 0;
33                }
34            }
35            onstk[u] = 0;
36            stk.pop_back();
37            return false;
38        }
39    }
40    int solve() {
41        // find a match
42        for (int i=0; i<n; i+=2){
43            match[i] = i+1, match[i+1] = i;
44        }
45        for(;;){
46            int found = 0;
47            for (int i=0; i<n; i++) dis[i] = onstk
48                [i] = 0;
49            for (int i=0; i<n; i++){

```

```

46        stk.clear();
47        if (!onstk[i] && SPFA(i)){
48            found = 1;
49            while (stk.size()>=2){
50                int u = stk.back(); stk.pop_back
51                ();
52                int v = stk.back(); stk.pop_back
53                ();
54                match[u] = v;
55                match[v] = u;
56            }
57            if (!found) break;
58        }
59        int ret = 0;
60        for (int i=0; i<n; i++)
61            ret += edge[i][match[i]];
62        ret /= 2;
63        return ret;
64    }
65 }graph;

```

#### 4.12 全局最小割

```

1 const int INF=0x3f3f3f3f;
2 template<typename T>
3 struct stoer_wagner{// 0-base
4     static const int MAXN=150;
5     T g[MAXN][MAXN],dis[MAXN];
6     int nd[MAXN],n,s,t;
7     void init(int _n){
8         n=_n;
9         for(int i=0;i<n;++i)
10             for(int j=0;j<n;++j)g[i][j]=0;
11    }
12    void add_edge(int u,int v,T w){
13        g[u][v]=g[v][u]+=w;
14    }
15    T min_cut(){
16        T ans=INF;
17        for(int i=0;i<n;++i)nd[i]=i;
18        for(int ind,tn=n;tn>1;--tn){
19            for(int i=1;i<tn;++i)dis[nd[i]]=0;
20            for(int i=1;i<tn;++i){
21                ind=i;
22                for(int j=i;j<tn;++j){
23                    dis[nd[j]]+=g[nd[i-1]][nd[j]];
24                    if(dis[nd[ind]]<dis[nd[j]])ind=j;
25                }
26                swap(nd[ind],nd[i]);
27            }
28            if(ans>dis[nd[ind]])ans=dis[t=nd[ind
29                ],s=nd[ind-1];
30            for(int i=0;i<tn;++i)
31                g[nd[ind-1]][nd[i]]=g[nd[i]][nd[ind
32                    -1]]+=g[nd[i]][nd[ind]];
33        }
34        return ans;
35    }
36 }

```

#### 4.13 弦圖完美消除序列

```

1 struct chordal{
2     static const int MAXN=1005;
3     int n;// 0-base
4     vector<int>G[MAXN];
5     int rank[MAXN],label[MAXN];
6     bool mark[MAXN];
7     void init(int _n){n=_n;
8         for(int i=0;i<n;++i)G[i].clear();
9     }
10    void add_edge(int u,int v){
11        G[u].push_back(v);
12        G[v].push_back(u);
13    }
14    vector<int> MCS(){
15        memset(rank,-1,sizeof(int)*n);
16        memset(label,0,sizeof(int)*n);
17        priority_queue<pair<int,int> > pq;
18        for(int i=0;i<n;++i)pq.push(make_pair(0,
19            i));
20        for(int i=n-1;i>=0;--i)for(;;){
21            int u=pq.top().second;pq.pop();
22            if(~rank[u])continue;
23            rank[u]=i;
24            for(auto v:G[u])if(rank[v]==-1){
25                pq.push(make_pair(++label[v],v));
26            }
27            break;
28        }
29        vector<int> res(n);
30        for(int i=0;i<n;++i)res[rank[i]]=i;
31        return res;
32    }
33    bool check(vector<int> ord){//弦圖判定
34        for(int i=0;i<n;++i)rank[ord[i]]=i;
35        memset(mark,0,sizeof(bool)*n);
36        for(int i=0;i<n;++i){
37            vector<pair<int,int> > tmp;
38            for(auto u:G[ord[i]])if(!mark[u])
39                tmp.push_back(make_pair(rank[u],u));
40            sort(tmp.begin(),tmp.end());
41            if(tmp.size()){
42                int u=tmp[0].second;
43                set<int> S;
44                for(auto v:G[u])S.insert(v);
45                for(size_t j=1;j<tmp.size();++j)
46                    if(!S.count(tmp[j].second))return
47                        0;
48            }
49            mark[ord[i]]=1;
50        }
51        return 1;
52    }
53 }

```

#### 4.14 最小斯坦納樹 DP

```

1 //n個點，其中r個要構成斯坦納樹
2 //答案在max(dp[(1<r)-1][k]) k=0~n-1
3 //p表示要構成斯坦納樹的點集

```

```

4 //O( n^3 + n*3^n + n^2*2^n )
5 #define REP(i,n) for(int i=0;i<(int)n;++i)
6 const int MAXN=30,MAXM=8;// 0-base
7 const int INF=0x3f3f3f3f;
8 int dp[1<MAXN][MAXN];
9 int g[MAXN][MAXN];//圖
10 void init(){memset(g,0,sizeof(g));}
11 void add_edge(int u,int v,int w){
12     g[u][v]=g[v][u]=min(g[v][u],w);
13 }
14 void steiner(int n,int r,int *p){
15     REP(k,n)REP(i,n)REP(j,n)
16         g[i][j]=min(g[i][j],g[i][k]+g[k][j]);
17     REP(i,n)g[i][i]=0;
18     REP(i,r)REP(j,n)dp[1<i][j]=g[p[i]][j];
19     for(int i=1;i<(1<r);++i){
20         if(!(i&(i-1)))continue;
21         REP(j,n)dp[i][j]=INF;
22         REP(j,n){
23             int tmp=INF;
24             for(int s=i&(i-1);s=s+(s-1))
25                 tmp=min(tmp,dp[s][j]+dp[i^s][j]);
26             REP(k,n)dp[i][k]=min(dp[i][k],g[j][k]+
27                 tmp);
28         }
29     }
30 }

```

#### 4.15 最小樹形圖朱劉

```

1 template<typename T>
2 struct zhu_liu{
3     static const int MAXN=110,MAXM=10005;
4     struct node{
5         int u,v;
6         T w,tag;
7         node *l,*r;
8         node(int u=0,int v=0,T w=0):u(u),v(v),w(
9             w),tag(0),l(0),r(0){}
10        void down(){
11            w+=tag;
12            if(l)l->tag+=tag;
13            if(r)r->tag+=tag;
14            tag=0;
15        }
16    }mem[MAXN];//靜態記憶體
17    node *pq[MAXN*2],*E[MAXN*2];
18    int st[MAXN*2],id[MAXN*2],m;
19    void init(int n){
20        for(int i=1;i<n;++i){
21            pq[i]=E[i]=0, st[i]=id[i]=i;
22            m=0;
23        }
24        node *merge(node *a,node *b){//skew heap
25            if(!a||!b)return a?a:b;
26            a->down(),b->down();
27            if(b->w<a->w)return merge(b,a);
28            swap(a->l,a->r);
29            a->l=merge(b,a->l);
30            return a;
31        }
32        void add_edge(int u,int v,T w){

```

```

32 if(u!=v)pq[v]=merge(pq[v],&mem[m++]=
    node(u,v,w));
33 }
34 int find(int x,int *st){
35     return st[x]==x?x:st[x]=find(st[x],st);
36 }
37 T build(int root,int n){
38     T ans=0;int N=n,all=n;
39     for(int i=1;i<=N;++i){
40         if(i==root||!pq[i])continue;
41         while(pq[i]){
42             pq[i]->down(),E[i]=pq[i];
43             pq[i]=merge(pq[i]->l,pq[i]->r);
44             if(find(E[i]->u,id)!=find(i,id))
45                 break;
46         }
47         if(find(E[i]->u,id)==find(i,id))
48             continue;
49         ans+=E[i]->w;
50         if(find(E[i]->u,st)==find(i,st)){
51             if(pq[i]pq[i]->tag==E[i]->w;
52             pq[++N]=pq[i];id[N]=N;
53             for(int u=find(E[i]->u,id);u!=i;u=
54                 find(E[u]->u,id)){
55                 if(pq[u]pq[u]->tag==E[u]->w;
56                 id[find(u,id)]=N;
57                 pq[N]=merge(pq[N],pq[u]);
58             }
59             st[N]=find(i,st);
60             id[find(i,id)]=N;
61             }else st[find(i,st)]=find(E[i]->u,st)
62             ,--all;
63         }
64     }
65     return all==1?ans:-INT_MAX;//圖不連通就
        無解
66 }
67 }
68 }

```

## 4.16 穩定婚姻模板

```

1 queue<int> Q;
2 for ( i : 所有考生 ) {
3     設定在第0志願;
4     Q.push(考生i);
5 }
6 while(Q.size()){
7     當前考生=Q.front();Q.pop();
8     while ( 此考生未分發 ) {
9         指標移到下一志願;
10        if ( 已經沒有志願 or 超出志願總數 )
11            break;
12        計算該考生在該科系加權後的總分;
13        if ( 不符合科系需求 ) continue;
14        if ( 目前科系有餘額 ) {
15            依加權後分數高低順序將考生id加入科系錄
16            取名單中;
17            break;
18        }
19        if ( 目前科系已額滿 ) {
20            if ( 此考生成績比最低分數還高 ) {

```

```

19        依加權後分數高低順序將考生id加入科系
20        錄取名單;
21        Q.push(被踢出的考生);
22    }
23 }
24 }

```

## 5 Language

### 5.1 CNF

```

1 #define MAXN 55
2 struct CNF{
3     int s,x,y;//s->xy | s->x, if y==1
4     int cost;
5     CNF(){}
6     CNF(int s,int x,int y,int c):s(s),x(x),y(y)
7     ,cost(c){}
8 };
9 int state;//規則數量
10 map<char,int> rule;//每個字元對應到的規則・
11     小寫字母為終端字符
12 vector<CNF> cnf;
13 void init(){
14     state=0;
15     rule.clear();
16     cnf.clear();
17 }
18 void add_to_cnf(char s,const string &p,int
19     cost){
20     //加入一個s -> <p>的文法・代價為cost
21     if(rule.find(s)==rule.end())rule[s]=state
22     ++;
23     for(auto c:p)if(rule.find(c)==rule.end())
24         rule[c]=state++;
25     if(p.size()==1){
26         cnf.push_back(CNF(rule[s],rule[p[0]],-1,
27             cost));
28     }else{
29         int left=rule[s];
30         int sz=p.size();
31         for(int i=0;i<sz-2;++i){
32             cnf.push_back(CNF(left,rule[p[i]],
33                 state,0));
34             left=state++;
35         }
36         cnf.push_back(CNF(left,rule[p[sz-2]],
37             rule[p[sz-1]],cost));
38     }
39 }
40 vector<long long> dp[MAXN][MAXN];
41 vector<bool> neg_INF[MAXN][MAXN];//如果花費
42     是真的可能會有無限小的情形
43 void relax(int l,int r,const CNF &c,long
44     long cost,bool neg_c=0){
45     if(!neg_INF[l][r][c.s]&&(neg_INF[l][r][c.x
46     ]||cost<dp[l][r][c.s])){
47         if(neg_c||neg_INF[l][r][c.x]){
48             dp[l][r][c.s]=0;

```

```

38     neg_INF[l][r][c.s]=true;
39     }else dp[l][r][c.s]=cost;
40 }
41 }
42 void bellman(int l,int r,int n){
43     for(int k=1;k<=state;++k)
44         for(auto c:cnf)
45             if(c.y==1)relax(l,r,c,dp[l][r][c.x]+
46                 .cost,k==n);
47 }
48 void cyk(const vector<int> &tok){
49     for(int i=0;i<(int)tok.size();++i){
50         for(int j=0;j<(int)tok.size();++j){
51             dp[i][j]=vector<long long>(state+1,
52                 INT_MAX);
53             neg_INF[i][j]=vector<bool>(state+1,
54                 false);
55         }
56         dp[i][i][tok[i]]=0;
57         bellman(i,i,tok.size());
58     }
59     for(int r=1;r<(int)tok.size();++r){
60         for(int l=r-1;l>=0;--l){
61             for(int k=l;k<r;++k)
62                 for(auto c:cnf)
63                     if(~c.y)relax(l,r,c,dp[l][k][c.x]+
64                         dp[k+1][r][c.y]+c.cost);
65             bellman(l,r,tok.size());
66         }
67     }
68 }

```

## 6 Linear Programming

### 6.1 simplex

```

1 /*target:
2     max \sum_{j=1}^n A_{0,j}*x_j
3 condition:
4     \sum_{j=1}^n A_{i,j}*x_j <= A_{i,0} | i=1~m
5     x_j >= 0 | j=1~n
6 VDB = vector<double>*/
7 template<class VDB>
8 VDB simplex(int m,int n,vector<VDB> a){
9     vector<int> left(m+1), up(n+1);
10    iota(left.begin(), left.end(), n);
11    iota(up.begin(), up.end(), 0);
12    auto pivot = [&](int x, int y){
13        swap(left[x], up[y]);
14        auto k = a[x][y]; a[x][y] = 1;
15        vector<int> pos;
16        for(int j = 0; j <= n; ++j){
17            a[x][j] /= k;
18            if(a[x][j] != 0) pos.push_back(j);
19        }
20        for(int i = 0; i <= m; ++i){
21            if(a[i][y]==0 || i == x) continue;
22            k = a[i][y], a[i][y] = 0;
23            for(int j : pos) a[i][j] -= k*a[x][j];
24        }
25    };

```

```

26 for(int x,y;){
27     for(int i=x+1; i <= m; ++i)
28         if(a[i][0]<a[x][0]) x = i;
29     if(a[x][0]>=0) break;
30     for(int j=y+1; j <= n; ++j)
31         if(a[x][j]<a[x][y]) y = j;
32     if(a[x][y]>=0) return VDB();//infeasible
33     pivot(x, y);
34 }
35 for(int x,y;){
36     for(int j=y+1; j <= n; ++j)
37         if(a[0][j] > a[0][y]) y = j;
38     if(a[0][y]<=0) break;
39     x = -1;
40     for(int i=1; i<=m; ++i) if(a[i][y] > 0)
41         if(x == -1 || a[i][0]/a[i][y]
42             < a[x][0]/a[x][y]) x = i;
43     if(x == -1) return VDB();//unbounded
44     pivot(x, y);
45 }
46 VDB ans(n + 1);
47 for(int i = 1; i <= m; ++i)
48     if(left[i] <= n) ans[left[i]] = a[i][0];
49 ans[0] = -a[0][0];
50 return ans;
51 }

```

## 7 Number Theory

### 7.1 basic

```

1 template<typename T>
2 void gcd(const T &a,const T &b,T &d,T &x,T &
3     y){
4     if(!b) d=a,x=1,y=0;
5     else gcd(b,a%b,d,y,x), y-=x*(a/b);
6 }
7 long long int phi[N+1];
8 void phiTable(){
9     for(int i=1;i<=N;i++)phi[i]=i;
10    for(int i=1;i<=N;i++)for(x=i*2;x<=N;x+=i)
11        phi[x]-=phi[i];
12 }
13 void all_divdown(const LL &n) { // all n/x
14     for(LL a=1;a<=n;a=n/(n/(a+1))) {
15         // dosomething;
16     }
17 }
18 const int MAXPRIME = 1000000;
19 int iscom[MAXPRIME], prime[MAXPRIME],
20     primecnt;
21 int phi[MAXPRIME], mu[MAXPRIME];
22 void sieve(void){
23     memset(iscom,0,sizeof(iscom));
24     primecnt = 0;
25     phi[1] = mu[1] = 1;
26     for(int i=2;i<=MAXPRIME;++i) {
27         if(!iscom[i]) {
28             prime[primecnt++] = i;
29             mu[i] = -1;
30             phi[i] = i-1;

```

```

28 }
29 for(int j=0;j<primecnt;++j) {
30     int k = i * prime[j];
31     if(k>MAXPRIME) break;
32     iscom[k] = prime[j];
33     if(i%prime[j]==0) {
34         mu[k] = 0;
35         phi[k] = phi[i] * prime[j];
36         break;
37     } else {
38         mu[k] = -mu[i];
39         phi[k] = phi[i] * (prime[j]-1);
40     }
41 }
42 }
43 }
44 }
45 bool g_test(const LL &g, const LL &p, const
vector<LL> &v) {
46     for(int i=0;i<v.size();++i)
47         if(modexp(g,(p-1)/v[i],p)==1)
48             return false;
49     return true;
50 }
51 LL primitive_root(const LL &p) {
52     if(p==2) return 1;
53     vector<LL> v;
54     Factor(p-1,v);
55     v.erase(unique(v.begin(), v.end()), v.end
());
56     for(LL g=2;g<p;++g)
57         if(g_test(g,p,v))
58             return g;
59     puts("primitive_root NOT FOUND");
60     return -1;
61 }
62 int Legendre(const LL &a, const LL &p) {
63     return modexp(a%p,(p-1)/2,p); }
64 LL inv(const LL &a, const LL &n) {
65     LL d,x,y;
66     gcd(a,n,d,x,y);
67     return d==1 ? (x+n)%n : -1;
68 }
69 int inv[maxN];
70 LL invtable(int n,LL P){
71     inv[1]=1;
72     for(int i=2;i<n;++i)
73         inv[i]=(P-(P/i))*inv[P%i]%P;
74 }
75 }
76 LL log_mod(const LL &a, const LL &b, const
LL &p) {
77     // a ^ x = b ( mod p )
78     int m=sqrt(p+.5), e=1;
79     LL v=inv(modexp(a,m,p), p);
80     map<LL,int> x;
81     x[1]=0;
82     for(int i=1;i<m;++i) {
83         e = LLMul(e,a,p);
84         if(!x.count(e)) x[e] = i;
85     }
86     for(int i=0;i<m;++i) {
87         if(x.count(b)) return i*m + x[b];
88         b = LLMul(b,v,p);
89     }

```

```

90 }
91 return -1;
92 }
93 LL Tonelli-Shanks(const LL &n, const LL &p)
{
94     // x^2 = n ( mod p )
95     if(n==0) return 0;
96     if(Legendre(n,p)!=1) while(1) { puts("SQRT
ROOT does not exist"); }
97     int S = 0;
98     LL Q = p-1;
99     while( !(Q&1) ) { Q>>=1; ++S; }
100     if(S==1) return modexp(n%p,(p+1)/4,p);
101     LL z = 2;
102     for(; Legendre(z,p)!=-1;++z)
103         LL c = modexp(z,Q,p);
104     LL R = modexp(n%p,(Q+1)/2,p), t = modexp(n
%p,Q,p);
105     int M = S;
106     while(1) {
107         if(t==1) return R;
108         LL b = modexp(c,1L<<(M-i-1),p);
109         R = LLMul(R,b,p);
110         t = LLMul(LLmul(b,b,p), t, p);
111         c = LLMul(b,b,p);
112         M = i;
113     }
114     return -1;
115 }
116 }
117 template<typename T>
118 T Euler(T n){
119     T ans=n;
120     for(T i=2;i*i<=n;++i){
121         if(n%i==0){
122             ans=ans/i*(i-1);
123             while(n%i==0)n/=i;
124         }
125     }
126     if(n>1)ans=ans/n*(n-1);
127     return ans;
128 }
129 }
130 //Chinese_remainder_theorem
131 template<typename T>
132 T crt(vector<T> &m,vector<T> &a){
133     T M=1,tM,ans=0;
134     for(int i=0;i<(int)m.size();++i)M*=m[i];
135     for(int i=0;i<(int)a.size();++i){
136         tM=M/m[i];
137         ans=(ans+(a[i]*tM%M)*pow_mod(tM,Euler(m[
i])-1,m[i])%M)%M;
138     }
139     return ans;
140 }
141 template<typename T>
142 T crt(vector<T> &m,vector<T> &a){
143     T M=1,tM,ans=0;
144     for(int i=0;i<(int)m.size();++i)M*=m[i];
145     for(int i=0;i<(int)a.size();++i){
146         tM=M/m[i];
147         ans=(ans+(a[i]*tM%M)*pow_mod(tM,Euler(m[
i])-1,m[i])%M)%M;
148     }
149     /*如果m[i]是質數 · Euler(m[i])-1=m[i]-2 ·
就不用算Euler了*/
150 }

```

```

150 return ans;
151 }
152 //java code
153 //求sqrt(N)的連分數
154 public static void Pell(int n){
155     BigInteger N,p1,p2,q1,q2,a0,a1,a2,g1,g2,h1
,h2,p,q;
156     g1=q2=p1=BigInteger.ZERO;
157     h1=q1=p2=BigInteger.ONE;
158     a0=a1=BigInteger.valueOf((int)Math.sqrt
(1.0*n));
159     BigInteger ans=a0.multiply(a0);
160     if(ans.equals(BigInteger.valueOf(n))){
161         System.out.println("No solution!");
162         return ;
163     }
164     while(true){
165         g2=a1.multiply(h1).subtract(g1);
166         h2=N.subtract(g2.pow(2)).divide(h1);
167         a2=g2.add(a0).divide(h2);
168         p=a1.multiply(p2).add(p1);
169         q=a1.multiply(q2).add(q1);
170         if(p.pow(2).subtract(N.multiply(q.pow
(2))).compareTo(BigInteger.ONE)==0){
171             break;
172         }
173         g1=g2;h1=h2;a1=a2;
174         p1=p2;p2=p;
175         q1=q2;q2=q;
176     }
177     System.out.println(p+" "+q);

```

## 7.2 bit set

```

1 void sub_set(int S){
2     int sub=S;
3     do{
4         //對某集合的子集合的處理
5         sub=(sub-1)&S;
6     }while(sub!=S);
7 }
8 void k_sub_set(int k,int n){
9     int comb=(1<<k)-1,S=1<n;
10    while(comb<S){
11        //對大小為k的子集合的處理
12        int x=comb&~comb,y=comb+x;
13        comb=((comb&~y)/x>>1)|y;
14    }
15 }

```

## 7.3 cantor expansion

```

1 int factorial[MAXN];
2 void init(){
3     factorial[0]=1;
4     for(int i=1;i<=MAXN;++i)factorial[i]=
factorial[i-1]*i;
5 }

```

```

6 int encode(const vector<int> &s){
7     int n=s.size(),res=0;
8     for(int i=0;i<n;++i){
9         int t=0;
10        for(int j=i+1;j<n;++j)
11            if(s[j]<s[i])++t;
12        res+=t*factorial[n-i-1];
13    }
14    return res;
15 }
16 vector<int> decode(int a,int n){
17     vector<int> res;
18     vector<bool> vis(n,0);
19     for(int i=n-1;i>=0;--i){
20         int t=a/factorial[i],j;
21         for(j=0;j<n;++j)
22             if(!vis[j]){
23                 if(t==0)break;
24                 --t;
25             }
26         res.push_back(j);
27         vis[j]=1;
28         a%=factorial[i];
29     }
30     return res;
31 }

```

## 7.4 FFT

```

1 template<typename T,typename VT=vector<
complex<T> > >
2 struct FFT{
3     const T pi;
4     FFT(const T pi=acos((-1)):pi(pi)){
5         unsigned bit_reverse(unsigned a,int len){
6             a=((a&0x55555555U)<<1)|((a&0xAAAAAAAAU)>>1);
7             a=((a&0x33333333U)<<2)|((a&0xCCCCCCCCU)>>2);
8             a=((a&0xF0F0F0F0U)<<4)|((a&0xFF0F0F0F0U)>>4);
9             a=((a&0x0F0F0F0F0U)<<8)|((a&0xFFFF0F0F0U)>>8);
10            a=((a&0x000FFFFFU)<<16)|((a&0xFFFF0000U)
>>16);
11            return a>>(32-len);
12        }
13        void fft(bool is_inv,VT &in,VT &out,int N)
{
14            int bitlen=__lg(N),num=is_inv?-1:1;
15            for(int i=0;i<N;++i)out[bit_reverse(i,
bitlen)]=in[i];
16            for(int step=2;step<=N;step<=1){
17                const int mh=step>>1;
18                for(int i=0;i<mh;++i){
19                    complex<T> wi=exp(complex<T>(0,i*num
*pi/mh));
20                    for(int j=i;j<N;j+=step){
21                        int k=j+mh;
22                        complex<T> u=out[j],t=wi*out[k];
23                        out[j]=u+t;
24                        out[k]=u-t;
25                    }
26                }
27            }
28            if(is_inv)for(int i=0;i<N;++i)out[i]/=N;
29        }

```

30|};

## 7.6 FWT

```

1 vector<int> F_OR_T(vector<int> f, bool
  inverse){
2   for(int i=0; (2<<i)<=f.size(); ++i)
3     for(int j=0; j<f.size(); j+=2<<i)
4       for(int k=0; k<(1<<i); ++k)
5         f[j+k+(1<<i)] += f[j+k]*(inverse
          ?-1:1);
6   return f;
7 }
8 vector<int> rev(vector<int> A) {
9   for(int i=0; i<A.size(); i+=2)
10    swap(A[i],A[i^(A.size()-1)]);
11   return A;
12 }
13 vector<int> F_AND_T(vector<int> f, bool
  inverse){
14   return rev(F_OR_T(rev(f), inverse));
15 }
16 vector<int> F_XOR_T(vector<int> f, bool
  inverse){
17   for(int i=0; (2<<i)<=f.size(); ++i)
18     for(int j=0; j<f.size(); j+=2<<i)
19       for(int k=0; k<(1<<i); ++k){
20         int u=f[j+k], v=f[j+k+(1<<i)];
21         f[j+k+(1<<i)] = u-v, f[j+k] = u+v;
22       }
23   if(inverse) for(auto &a:f) a/=f.size();
24   return f;
25 }

```

## 7.7 LinearCongruence

```

27 vector<double> cal(vector<double>coef, int n
  ){
28   vector<double>res;
29   if(n == 1){
30     if(sign(coef[1])) res.pb(-coef[0]/coef
      [1]);
31     return res;
32   }
33   vector<double>dcoef(n);
34   for(int i = 0; i < n; ++i) dcoef[i] = coef
    [i+1]*(i+1);
35   vector<double>droot = cal(dcoef, n-1);
36   droot.insert(droot.begin(), -INF);
37   droot.pb(INF);
38   for(int i = 0; i+1 < droot.size(); ++i){
39     double tmp = find(coef, n, droot[i],
      droot[i+1]);
40     if(tmp < INF) res.pb(tmp);
41   }
42   return res;
43 }
44
45 int main () {
46   vector<double>ve;
47   vector<double>ans = cal(ve, n);
48   // 視情況把答案 +eps，避免 -0
49 }

```

## 7.8 Lucas

```

1 ll C(ll n, ll m, ll p){// n!/m!/(n-m)!
2   if(n<m) return 0;
3   return f[n]*inv(f[m],p)%p*inv(f[n-m],p)%p;
4 }
5 ll L(ll n, ll m, ll p){
6   if(!m) return 1;
7   return C(n%p,m%p,p)*L(n/p,m/p,p)%p;
8 }
9 ll Wilson(ll n, ll p){ // n!%p
10  if(!n)return 1;
11  ll res=Wilson(n/p, p);
12  if((n/p)%2) return res*(p-f[n%p])%p;
13  return res*f[n%p]%p; //(p-1)!%p=-1
14 }

```

## 7.9 Matrix

```

1 template<typename T>
2 struct Matrix{
3   using rt = std::vector<T>;
4   using mt = std::vector<rt>;
5   using matrix = Matrix<T>;
6   int r,c;
7   mt m;
8   Matrix(int r,int c):r(r),c(c),m(r,rt(c)){}
9   rt& operator[](int i){return m[i];}
10  matrix operator+(const matrix &a){
11    matrix rev(r,c);
12    for(int i=0;i<r;++i)
13      for(int j=0;j<c;++j)
14        rev[i][j]=m[i][j]+a.m[i][j];
15    return rev;
16  }
17  matrix operator*(const matrix &a){
18    matrix rev(r,c);
19    for(int i=0;i<r;++i)
20      for(int j=0;j<c;++j)
21        rev[i][j]=m[i][j]-a.m[i][j];
22    return rev;
23  }
24  matrix operator*(const matrix &a){
25    matrix rev(r,a.c);
26    matrix tmp(a.c,a.r);
27    for(int i=0;i<a.r;++i)
28      for(int j=0;j<a.c;++j)
29        tmp[j][i]=a.m[i][j];
30    for(int i=0;i<r;++i)
31      for(int j=0;j<a.c;++j)
32        for(int k=0;k<c;++k)
33          rev.m[i][j]+=m[i][k]*tmp[j][k];
34    return rev;
35  }
36  bool inverse(){
37    Matrix t(r,r+c);
38    for(int y=0;y<r;y++){
39      t.m[y][c+y] = 1;
40      for(int x=0;x<c;++x)
41        t.m[y][x]=m[y][x];
42    }
43    if( !t.gas() )
44      return false;
45    for(int y=0;y<r;y++)
46      for(int x=0;x<c;++x)

```

```

47     m[y][x]=t.m[y][c+x]/t.m[y][y];
48   return true;
49 }
50 T gas(){
51   vector<T> lazy(r,1);
52   bool sign=false;
53   for(int i=0;i<r;++i){
54     if( m[i][i]==0 ){
55       int j=i+1;
56       while(j<r&&!m[j][i])j++;
57       if(j==r)continue;
58       m[i].swap(m[j]);
59       sign=!sign;
60     }
61     for(int j=0;j<r;++j){
62       if(i==j)continue;
63       lazy[j]=lazy[j]*m[i][i];
64       T mx=m[j][i];
65       for(int k=0;k<c;++k)
66         m[j][k]=m[j][k]*m[i][i]-m[i][k]*mx;
67     }
68   }
69   T det=sign?-1:1;
70   for(int i=0;i<r;++i){
71     det = det*m[i][i];
72     det = det/lazy[i];
73     for(auto &j:m[i])j/=lazy[i];
74   }
75   return det;
76 }
77 };

```

## 7.10 MillerRobin

```

1 ULL LLMul(ULL a, ULL b, const ULL &mod) {
2   LL ans=0;
3   while(b) {
4     if(b&1) {
5       ans+=a;
6       if(ans>=mod) ans-=mod;
7     }
8     a<<=1, b>>=1;
9     if(a==mod) a-=mod;
10  }
11  return ans;
12 }
13 ULL mod_mul(ULL a,ULL b,ULL m){
14   a%=m,b%=m; /* fast for m < 2^58 */
15   ULL y=(ULL)((double)a*b/m+0.5);
16   ULL r=(a*b-y)%m;
17   return r<0?r+m:r;
18 }
19 template<typename T>
20 T pow(T a,T b,T mod){//a^b%mod
21   T ans=1;
22   for(;b;a=mod_mul(a,a,mod),b>>=1)
23     if(b&1)ans=mod_mul(ans,a,mod);
24   return ans;
25 }
26 int sprp[3]={2,7,61}; //int範圍可解
27 int llsp[7]={2,325,9375,28178,450775,9780504,

```



```

28 17952650222; //至少unsigned long long範圍
29 template<typename T>
30 bool isprime(T n, int *sprp, int num){
31     if(n==2) return 1;
32     if(n<2 || n%2==0) return 0;
33     int t=0;
34     T u=n-1;
35     for(; u%2==0; ++t) u>>=1;
36     for(int i=0; i<num; ++i){
37         T a=sprp[i]*n;
38         if(a==0 || a==1 || a==n-1) continue;
39         T x=pow(a, u, n);
40         if(x==1 || x==n-1) continue;
41         for(int j=0; j<t; ++j){
42             x=mod_mul(x, x, n);
43             if(x==1) return 0;
44             if(x==n-1) break;
45         }
46         if(x==n-1) continue;
47         return 0;
48     }
49     return 1;
50 }

```

## 7.11 NTT

```

1 2615053605667*(2^18)+1, 3
2 15*(2^27)+1, 31
3 479*(2^21)+1, 3
4 7*17*(2^23)+1, 3
5 3*3*211*(2^19)+1, 5
6 25*(2^22)+1, 3
7 template<typename T, typename VT=vector<T> >
8 struct NTT{
9     const T P, G;
10     NTT(T p=(1<<23)*7*17+1, T g=3): P(p), G(g){}
11     unsigned bit_reverse(unsigned a, int len){
12         //look FFT.cpp
13     }
14     T pow_mod(T n, T k, T m){
15         T ans=1;
16         for(n=(n>=m?n%m:n); k>0; k>>=1){
17             if(k&1) ans=ans*n%m;
18             n=n*n%m;
19         }
20         return ans;
21     }
22     void ntt(bool is_inv, VT &in, VT &out, int N)
23     {
24         int bitlen=__lg(N);
25         for(int i=0; i<N; ++i) out[bit_reverse(i, bitlen)]=in[i];
26         for(int step=2, id=1; step<=N; step<<=1, ++id){
27             T wn=pow_mod(G, (P-1)>>id, P), wi=1, u, t;
28             const int mh=step>>1;
29             for(int i=0; i<mh; ++i){
30                 for(int j=i; j<N; j+=step){
31                     u=out[j], t=wi*out[j+mh]%P;
32                     out[j]=u+t;
33                     out[j+mh]=u-t;
34                     if(out[j]>=P) out[j]-=P;
35                     if(out[j+mh]<0) out[j+mh]+=P;

```

```

35     }
36     wi=wi*wn%P;
37     }
38     }
39     if(is_inv){
40         for(int i=1; i<N/2; ++i) swap(out[i], out[N-i]);
41     }
42     T invn=pow_mod(N, P-2, P);
43     for(int i=0; i<N; ++i) out[i]=out[i]*invn%P;
44     }
45 }

```

## 7.12 Simpson

```

1 double simpson(double a, double b){
2     double c=a+(b-a)/2;
3     return (F(a)+4*F(c)+F(b))*(b-a)/6;
4 }
5 double asr(double a, double b, double eps,
6     double A){
7     double c=a+(b-a)/2;
8     double L=simpson(a, c), R=simpson(c, b);
9     if( abs(L+R-A)<15*eps )
10         return L+R+(L+R-A)/15.0;
11     return asr(a, c, eps/2, L)+asr(c, b, eps/2, R);
12 }
13 double asr(double a, double b, double eps){
14     return asr(a, b, eps, simpson(a, b));
15 }

```

## 7.13 外星模運算

```

1 //a[0]^(a[1]^a[2]^...)
2 #define maxn 100000
3 int euler[maxn+5];
4 bool is_prime[maxn+5];
5 void init_euler(){
6     is_prime[1]=1; //不是質數
7     for(int i=1; i<=maxn; i++) euler[i]=i;
8     for(int i=2; i<=maxn; i++){
9         if(!is_prime[i]) //是質數
10             euler[i]--;
11         for(int j=i<1; j<=maxn; j+=i){
12             is_prime[j]=1;
13             euler[j]=euler[j]/i*(i-1);
14         }
15     }
16 }
17 LL pow(LL a, LL b, LL mod){ //a^b%mod
18     LL ans=1;
19     for(; b; a=a*a%mod, b>>=1)
20         if(b&1) ans=ans*a%mod;
21     return ans;
22 }
23 bool isless(LL *a, int n, int k){
24     if(*a==1) return k>1;
25 }

```

```

26 if(--n==0) return *a<k;
27 int next=0;
28 for(LL b=1; b<k; ++next)
29     b*=a;
30 return isless(a+1, n, next);
31 }
32 LL high_pow(LL *a, int n, LL mod){
33     if(*a==1 || --n==0) return *a%mod;
34     int k=0, r=euler[mod];
35     for(LL tma=1; tma!=pow(*a, k+r, mod); ++k)
36         tma=tma*(*)%mod;
37     if(isless(a+1, n, k)) return pow(*a, high_pow(a+1, n, k), mod);
38     int tmd=high_pow(a+1, n, r), t=(tmd-k+r)%r;
39     return pow(*a, k+t, mod);
40 }
41 LL a[1000005];
42 int t, mod;
43 int main(){
44     init_euler();
45     scanf("%d", &t);
46     #define n 4
47     while(t--){
48         for(int i=0; i<n; ++i) scanf("%lld", &a[i]);
49         scanf("%d", &mod);
50         printf("%lld\n", high_pow(a, n, mod));
51     }
52     return 0;
53 }

```

## 7.14 數位統計

```

1 ll d[65], dp[65][2]; //up區間是不是完整
2 ll dfs(int p, bool is8, bool up){
3     if(!p) return 1; //回傳0是不是答案
4     if(!up&&~dp[p][is8]) return dp[p][is8];
5     int mx = up?d[p]:9; //可以用的有那些
6     ll ans=0;
7     for(int i=0; i<=mx; ++i){
8         if( is8&&i==7 ) continue;
9         ans += dfs(p-1, i==8, up&&i==mx);
10    }
11    if(!up) dp[p][is8]=ans;
12    return ans;
13 }
14 ll f(ll N){
15     int k=0;
16     while(N){ //把數字先分解到陣列
17         d[++k] = N%10;
18         N/=10;
19     }
20     return dfs(k, false, true);
21 }

```

## 7.15 質因數分解

```

1 LL func(const LL n, const LL mod, const int c)
2 {
3     return (LLmul(n, n, mod)+c+mod)%mod;

```

```

3 }
4
5 LL pollorrho(const LL n, const int c) { //循環節長度
6     LL a=1, b=1;
7     a=func(a, n, c)%n;
8     b=func(b, n, c)%n; b=func(b, n, c)%n;
9     while(gcd(abs(a-b), n)!=1) {
10         a=func(a, n, c)%n;
11         b=func(b, n, c)%n; b=func(b, n, c)%n;
12     }
13     return gcd(abs(a-b), n);
14 }
15
16 void prefactor(LL &n, vector<LL> &v) {
17     for(int i=0; i<12; ++i) {
18         while(n%prime[i]==0) {
19             v.push_back(prime[i]);
20             n/=prime[i];
21         }
22     }
23 }
24
25 void smallfactor(LL n, vector<LL> &v) {
26     if(n<MAXPRIME) {
27         while(isp[(int)n]) {
28             v.push_back(isp[(int)n]);
29             n/=isp[(int)n];
30         }
31         v.push_back(n);
32     } else {
33         for(int i=0; i<primecnt&&prime[i]*prime[i]<=n; ++i) {
34             while(n%prime[i]==0) {
35                 v.push_back(prime[i]);
36                 n/=prime[i];
37             }
38             if(n!=1) v.push_back(n);
39         }
40     }
41 }
42
43 void comfactor(const LL &n, vector<LL> &v) {
44     if(n<1e9) {
45         smallfactor(n, v);
46         return;
47     }
48     if(Isprime(n)) {
49         v.push_back(n);
50         return;
51     }
52     LL d;
53     for(int c=3; ++c) {
54         d = pollorrho(n, c);
55         if(d!=n) break;
56     }
57     comfactor(d, v);
58     comfactor(n/d, v);
59 }
60
61 void Factor(const LL &x, vector<LL> &v) {
62     LL n = x;
63     if(n==1) { puts("Factor 1"); return; }
64     prefactor(n, v);
65     if(n==1) return;

```

```

66 comfactor(n,v);
67 sort(v.begin(),v.end());
68 }
69 void AllFactor(const LL &n,vector<LL> &v) {
70     vector<LL> tmp;
71     Factor(n,tmp);
72     v.clear();
73     v.push_back(1);
74     int len;
75     LL now=1;
76     for(int i=0;i<tmp.size();++i) {
77         if(i==0 || tmp[i]!=tmp[i-1]) {
78             len = v.size();
79             now = 1;
80         }
81         now*=tmp[i];
82         for(int j=0;j<len;++j)
83             v.push_back(v[j]*now);
84     }
85 }
86 }

```

## 8 String

### 8.1 AC 自動機

```

1 template<char L='a',char R='z'>
2 class ac_automaton{
3     struct joe{
4         int next[R-L+1],fail,efl,ed,cnt_dp,vis;
5         joe():ed(0),cnt_dp(0),vis(0){
6             for(int i=0;i<R-L;++i)next[i]=0;
7         }
8     };
9 public:
10     std::vector<joe> S;
11     std::vector<int> q;
12     int qs,qe,vt;
13     ac_automaton():S(1),qs(0),qe(0),vt(0){}
14     void clear(){
15         q.clear();
16         S.resize(1);
17         for(int i=0;i<=R-L;++i)S[0].next[i]=0;
18         S[0].cnt_dp=S[0].vis=qs=qe=vt=0;
19     }
20     void insert(const char *s){
21         int o=0;
22         for(int i=0,id;s[i];++i){
23             id=s[i]-L;
24             if(!S[o].next[id]){
25                 S.push_back(joe());
26                 S[o].next[id]=S.size()-1;
27             }
28             o=S[o].next[id];
29         }
30         ++S[o].ed;
31     }
32     void build_fail(){
33         S[0].fail=S[0].efl=-1;
34         q.clear();
35         q.push_back(0);

```

```

36     ++qe;
37     while(qs!=qe){
38         int pa=q[qs++],id,t;
39         for(int i=0;i<=R-L;++i){
40             t=S[pa].next[i];
41             if(!t)continue;
42             id=S[pa].fail;
43             while(~id&&!S[id].next[i])id=S[id].fail;
44             S[t].fail=~id?S[id].next[i]:0;
45             S[t].efl=S[S[t].fail].ed?S[t].fail:S[t].fail.S[fail].efl;
46             q.push_back(t);
47             ++qe;
48         }
49     }
50 }
51 /*DP出每個前綴在字串s出現的次數並傳回所有
   字串被s匹配成功的次數O(N*M)*/
52 int match_0(const char *s){
53     int ans=0,id,p=0,i;
54     for(i=0;s[i];++i){
55         id=s[i]-L;
56         while(!S[p].next[id]&&p)p=S[p].fail;
57         if(!S[p].next[id])continue;
58         p=S[p].next[id];
59         ++S[p].cnt_dp; /*匹配成功則它所有後綴都
           可以被匹配(DP計算)*/
60     }
61     for(i=qe-1;i>=0;--i){
62         ans+=S[q[i]].cnt_dp*S[q[i]].ed;
63         if(~S[q[i]].fail)S[q[i]].fail.
64             cnt_dp+=S[q[i]].cnt_dp;
65     }
66     return ans;
67 }
68 /*多串匹配走efl邊並傳回所有字串被s匹配成功
   的次數O(N*M^1.5)*/
69 int match_1(const char *s)const{
70     int ans=0,id,p=0,t;
71     for(int i=0;s[i];++i){
72         id=s[i]-L;
73         while(!S[p].next[id]&&p)p=S[p].fail;
74         if(!S[p].next[id])continue;
75         p=S[p].next[id];
76         if(S[p].ed)ans+=S[p].ed;
77         for(t=S[p].efl;~t;t=S[t].efl){
78             ans+=S[t].ed; /*因為都走efl邊所以保證
              匹配成功*/
79         }
80     }
81     return ans;
82 }
83 /*枚舉(s的子字串nA)的所有相異字串各恰一次
   並傳回次數O(N*M^(1/3))*/
84 int match_2(const char *s){
85     int ans=0,id,p=0,t;
86     ++vt;
87     /*把戳記vt+=1. 只要vt沒溢位. 所有S[p].
       vis==vt就會變成false
88     這種利用vt的方法可以O(1)歸零vis陣列*/
89     for(int i=0;s[i];++i){
90         id=s[i]-L;
91         while(!S[p].next[id]&&p)p=S[p].fail;

```

```

91         if(!S[p].next[id])continue;
92         p=S[p].next[id];
93         if(S[p].ed&&S[p].vis!=vt){
94             S[p].vis=vt;
95             ans+=S[p].ed;
96         }
97         for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[t].efl){
98             S[t].vis=vt;
99             ans+=S[t].ed; /*因為都走efl邊所以保證
              匹配成功*/
100         }
101     }
102     return ans;
103 }
104 /*把AC自動機變成真的自動機*/
105 void evolution(){
106     for(qs=1;qs!=qe;){
107         int p=q[qs++];
108         for(int i=0;i<=R-L;++i)
109             if(S[p].next[i]==0)S[p].next[i]=S[S[p].fail].next[i];
110     }
111 }
112 };

```

### 8.2 hash

```

1 #define MAXN 1000000
2 #define mod 1073676287
3 /*mod 必須要是質數*/
4 typedef long long T;
5 char s[MAXN+5];
6 T h[MAXN+5]; /*hash陣列*/
7 T h_base[MAXN+5]; /*h_base[n]=(prime^n)%mod*/
8 void hash_init(int len,T prime){
9     h_base[0]=1;
10    for(int i=1;i<=len;++i){
11        h[i]=(h[i-1]*prime+s[i-1])%mod;
12        h_base[i]=(h_base[i-1]*prime)%mod;
13    }
14 }
15 T get_hash(int l,int r){ /*閉區間寫法. 設編號
   為0 ~ len-1*/
16     return (h[r+1]-(h[l]*h_base[r-l+1])%mod+
17         mod)%mod;

```

### 8.3 KMP

```

1 /*產生fail function*/
2 void kmp_fail(char *s,int len,int *fail){
3     int id=-1;
4     fail[0]=-1;
5     for(int i=1;i<len;++i){
6         while(~id&&s[id+1]!=s[i])id=fail[id];
7         if(s[id+1]==s[i])++id;
8         fail[i]=id;

```

```

9     }
10 }
11 /*以字串B匹配字串A. 傳回匹配成功的數量(用B的
   fail)*/
12 int kmp_match(char *A,int lenA,char *B,int
   lenB,int *fail){
13     int id=-1,ans=0;
14     for(int i=0;i<lenA;++i){
15         while(~id&&B[id+1]!=A[i])id=fail[id];
16         if(B[id+1]==A[i])++id;
17         if(id==lenB-1){ /*匹配成功*/
18             ++ans, id=fail[id];
19         }
20     }
21     return ans;
22 }

```

### 8.4 manacher

```

1 //原字串: asdsasdsa
2 //先把字串變成這樣: @#a#s#d#s#a#s#d#s#a#
3 void manacher(char *s,int len,int *z){
4     int l=0,r=0;
5     for(int i=1;i<len;++i){
6         z[i]=r>i?min(z[2*i-l],r-i):1;
7         while(s[i+z[i]]==s[i-z[i]])++z[i];
8         if(z[i]+i>r)r=z[i]+i,l=i;
9     } //ans = max(z)-1
10 }

```

### 8.5 minimal string rotation

```

1 int min_string_rotation(const string &s){
2     int n=s.size(),i=0,j=1,k=0;
3     while(i<n&&j<n&&k<n){
4         int t=s[(i+k)%n]-s[(j+k)%n];
5         ++k;
6         if(t>0)i+=k;
7         else j+=k;
8         if(i==j)++j;
9         k=0;
10    }
11    return min(i,j); //最小循環表示法起始位置
12 }

```

### 8.6 reverseBWT

```

1 const int MAXN = 305, MAXC = 'Z';
2 int ranks[MAXN], tots[MAXC], first[MAXC];
3 void rankBWT(const string &bw){
4     memset(ranks,0,sizeof(int)*bw.size());
5     memset(tots,0,sizeof(tots));
6     for(size_t i=0;i<bw.size();++i)
7         ranks[i] = tots[int(bw[i])]++;

```

```

8 }
9 void firstCol(){
10     memset(first,0,sizeof(first));
11     int totc = 0;
12     for(int c='A';c<='Z';++c){
13         if(!tots[c]) continue;
14         first[c] = totc;
15         totc += tots[c];
16     }
17 }
18 string reverseBwt(string bw,int begin){
19     rankBWT(bw, firstCol());
20     int i = begin; //原字串最後一個元素的位置
21     string res;
22     do{
23         char c = bw[i];
24         res = c + res;
25         i = first[int(c)] + ranks[i];
26     }while( i != begin );
27     return res;
28 }

```

## 8.8 Z

```

1 void z_alg(char *s,int len,int *z){
2     int l=0,r=0;
3     z[0]=len;
4     for(int i=1;i<len;++i){
5         z[i]=i>r?0:(i-l+z[i-l]<z[l]?z[i-l]:r-i+1);
6         while(i+z[i]<len&&s[i+z[i]]==s[z[i]]++)z[i];
7         if(i+z[i]-1>r)r=i+z[i]-1,l=i;
8     }
9 }

```

## 9 Tarjan

### 9.1 dominator tree

```

1 struct dominator_tree{
2     static const int MAXN=5005;
3     int n;// 1-base
4     vector<int> G[MAXN], rG[MAXN];
5     int pa[MAXN], dfn[MAXN], id[MAXN], dfnCnt;
6     int semi[MAXN], idom[MAXN], best[MAXN];
7     vector<int> tree[MAXN]; // tree here
8     void init(int _n){
9         n = _n;
10        for(int i=1; i<=n; ++i)
11            G[i].clear(), rG[i].clear();
12    }
13    void add_edge(int u, int v){
14        G[u].push_back(v);
15        rG[v].push_back(u);
16    }
17    void dfs(int u){
18        id[dfn[u]=++dfnCnt]=u;
19        for(auto v:G[u]) if(!dfn[v])
20            dfs(v),pa[dfn[v]]=dfn[u];
21    }
22    int find(int y,int x){
23        if(y <= x) return y;
24        int tmp = find(pa[y],x);
25        if(semi[best[y]] > semi[best[pa[y]]])
26            best[y] = best[pa[y]];
27        return pa[y] = tmp;
28    }
29    void tarjan(int root){
30        dfnCnt = 0;
31        for(int i=1; i<=n; ++i){
32            dfn[i] = idom[i] = 0;
33            tree[i].clear();
34            best[i] = semi[i] = i;
35        }
36        dfs(root);
37        for(int i=dfnCnt; i>1; --i){
38            int u = id[i];
39            for(auto v:rG[u]) if(v=dfn[v]){
40                find(v,i);
41                semi[i]=min(semi[i],semi[best[v]]);
42            }

```

### 8.7 suffix array lcp

```

1 #define radix_sort(x,y){\
2     for(i=0;i<A;++i)c[i]=0;\
3     for(i=0;i<n;++i)c[x[y[i]]]++;\
4     for(i=1;i<A;++i)c[i]+=c[i-1];\
5     for(i=n-1;i>=0;i--)sa[--c[x[y[i]]]]=y[i];\
6 }
7 #define AC(r,a,b)\
8     r[a]=r[b]||a+k>=n||r[a+k]!=r[b+k]
9 void suffix_array(const char *s,int n,int *
10     sa,int *rank,int *tmp,int *c){
11     int A='z'+1,i,k,id=0;
12     for(i=0;i<n;++i)rank[tmp[i]=i]=s[i];
13     radix_sort(rank,tmp);
14     for(k=1;id<n-1;k<=1){
15         for(id=0,i=n-k;i<n;++i)tmp[id++]=i;
16         for(i=0;i<n;++i)
17             if(sa[i]>=k)tmp[id++]=sa[i]-k;
18         radix_sort(rank,tmp);
19         swap(rank,tmp);
20         rank[sa[0]]=id=0,i=1;i<n;++i)
21             rank[sa[i]]=id+=AC(tmp,sa[i-1],sa[i]);
22         A=id+1;
23     }
24     //h:高度數組 sa:後綴數組 rank:排名
25     void suffix_array_lcp(const char *s,int len,
26         int *h,int *sa,int *rank){
27         for(int i=0;i<len;++i)rank[sa[i]]=i;
28         for(int i=0,k=0;i<len;++i){
29             if(rank[i]==0)continue;
30             if(k--<0)k=0;
31             while(s[i+k]==s[sa[rank[i]-1]+k])++k;
32             h[rank[i]]=k;
33         }
34         h[0]=0; // h[k]=lcp(sa[k],sa[k-1]);

```

```

43     tree[semi[i]].push_back(i);
44     for(auto v:tree[pa[i]]){
45         find(v, pa[i]);
46         idom[v] = semi[best[v]]==pa[i]
47             ? pa[i] : best[v];
48     }
49     tree[pa[i]].clear();
50 }
51 for(int i=2; i<=dfnCnt; ++i){
52     if(idom[i] != semi[i])
53         idom[i] = idom[idom[i]];
54     tree[id[idom[i]]].push_back(id[i]);
55 }
56 }
57 }dom;

```

### 9.2 tnfshb017 2 sat

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define MAXN 8001
4 #define MAXN2 MAXN*4
5 #define n(X) ((X)+2*MAXN)
6 vector<int> v[MAXN2], rv[MAXN2], vis_t;
7 int N,M;
8 void addedge(int s,int e){
9     v[s].push_back(e);
10    rv[e].push_back(s);
11 }
12 int scc[MAXN2];
13 bool vis[MAXN2]={false};
14 void dfs(vector<int> *uv,int n,int k=-1){
15     vis[n]=true;
16     for(int i=0;i<uv[n].size();++i)
17         if(!vis[uv[n][i]])
18             dfs(uv,uv[n][i],k);
19     if(uv==v)vis_t.push_back(n);
20     scc[n]=k;
21 }
22 void solve(){
23     for(int i=1;i<=N;++i){
24         if(!vis[i])dfs(v,i);
25         if(!vis[n(i)])dfs(v,n(i));
26     }
27     memset(vis,0,sizeof(vis));
28     int c=0;
29     for(int i=vis_t.size()-1;i>=0;--i)
30         if(!vis[vis_t[i]])
31             dfs(rv,vis_t[i],c++);
32 }
33 int main(){
34     int a,b;
35     scanf("%d%d",&N,&M);
36     for(int i=1;i<=N;++i){
37         // (A or B)&(!A & !B) A^B
38         a=i*2-1;
39         b=i*2;
40         addedge(n(a),b);
41         addedge(n(b),a);
42         addedge(a,n(b));
43         addedge(b,n(a));
44     }
45     while(M--){

```

```

46     scanf("%d%d",&a,&b);
47     a = a>0?a*2-1:-a*2;
48     b = b>0?b*2-1:-b*2;
49     // A or B
50     addedge(n(a),b);
51     addedge(n(b),a);
52 }
53 solve();
54 bool check=true;
55 for(int i=1;i<=2*N;++i)
56     if(scc[i]==scc[n(i)])
57         check=false;
58 if(check){
59     printf("%d\n",N);
60     for(int i=1;i<=2*N;i+=2){
61         if(scc[i]>scc[i+2*N]) putchar('+');
62         else putchar('-');
63     }
64     puts("");
65 }else puts("0");
66 return 0;
67 }

```

### 9.3 橋連通分量

```

1 #define N 1005
2 struct edge{
3     int u,v;
4     bool is_bridge;
5     edge(int u=0,int v=0):u(u),v(v),is_bridge
6         (0){}
7 };
8 vector<edge> E;
9 vector<int> G[N]; // 1-base
10 int low[N],vis[N],Time;
11 int bcc_id[N],bridge_cnt,bcc_cnt; // 1-base
12 int st[N],top; // BCC用
13 void add_edge(int u,int v){
14     G[u].push_back(E.size());
15     E.emplace_back(u,v);
16     G[v].push_back(E.size());
17     E.emplace_back(v,u);
18 }
19 void dfs(int u,int re=-1){ //u當前點 · re為u連
20     接前一個點的邊
21     int v;
22     low[u]=vis[u]=++Time;
23     st[top++]=u;
24     for(int e:G[u]){
25         v=E[e].v;
26         if(!vis[v]){
27             dfs(v,E[e]); //e^1 反向邊
28             low[u]=min(low[u],low[v]);
29             if(vis[u]<low[v]){
30                 E[e].is_bridge=1;
31                 ++bridge_cnt;
32             }
33         }else if(vis[v]<vis[u]&&e!=re)
34             low[u]=min(low[u],vis[v]);
35     }
36 if(vis[u]==low[u]){ //處理BCC
37     ++bcc_cnt; // 1-base

```

```

36 do bcc_id[v=st[--top]]=bcc_cnt; // 每個點
    所在的bcc
37 while(v!=u);
38 }
39 }
40 void bcc_init(int n){
41 Time=bcc_cnt=bridge_cnt=top=0;
42 E.clear();
43 for(int i=1;i<n;++i){
44 G[i].clear();
45 vis[i]=bcc_id[i]=0;
46 }
47 }

```

## 9.4 雙連通分量 & 割點

```

1 #define N 1005
2 vector<int> G[N]; // 1-base
3 vector<int> bcc[N]; // 存每塊雙連通分量的點
4 int low[N], vis[N], Time;
5 int bcc_id[N], bcc_cnt; // 1-base
6 bool is_cut[N]; // 是否為割點
7 int st[N], top;
8 void dfs(int u, int pa=-1) { // u當前點, pa父親
9 int t, child=0;
10 low[u]=vis[u]=++Time;
11 st[top++]=u;
12 for(int v:G[u]){
13 if(!vis[v]){
14 dfs(v,u), ++child;
15 low[u]=min(low[u], low[v]);
16 if(vis[u]<=low[v]){
17 is_cut[u]=1;
18 bcc[++bcc_cnt].clear();
19 do{
20 bcc_id[t=st[--top]]=bcc_cnt;
21 bcc[bcc_cnt].push_back(t);
22 }while(t!=v);
23 bcc_id[u]=bcc_cnt;
24 bcc[bcc_cnt].push_back(u);
25 }
26 }else if(vis[v]<vis[u]&&v!=pa) // 反向邊
27 low[u] = min(low[u], vis[v]);
28 } // u是dfs樹的根要特判
29 if(pa== -1 && child<2) is_cut[u]=0;
30 }
31 void bcc_init(int n){
32 Time=bcc_cnt=top=0;
33 for(int i=1;i<n;++i){
34 G[i].clear();
35 is_cut[i]=vis[i]=bcc_id[i]=0;
36 }
37 }

```

## 10 Tree Problem

### 10.1 HeavyLight

```

1 #include<vector>
2 #define MAXN 100005
3 int siz[MAXN], max_son[MAXN], pa[MAXN], dep[
    MAXN];
4 int link_top[MAXN], link[MAXN], cnt;
5 vector<int> G[MAXN];
6 void find_max_son(int u){
7 siz[u]=1;
8 max_son[u]=-1;
9 for(auto v:G[u]){
10 if(v==pa[u]) continue;
11 pa[v]=u;
12 dep[v]=dep[u]+1;
13 find_max_son(v);
14 if(max_son[u]==-1 || siz[v]>siz[max_son[u]
    ]) max_son[u]=v;
15 siz[u]+=siz[v];
16 }
17 }
18 void build_link(int u, int top){
19 link[u]=++cnt;
20 link_top[u]=top;
21 if(max_son[u]==-1) return;
22 build_link(max_son[u], top);
23 for(auto v:G[u]){
24 if(v==max_son[u] || v==pa[u]) continue;
25 build_link(v, v);
26 }
27 }
28 int find_lca(int a, int b){
29 // 求LCA, 可以在過程中對區間進行處理
30 int ta=link_top[a], tb=link_top[b];
31 while(ta!=tb){
32 if(dep[ta]<dep[tb]){
33 swap(ta, tb);
34 swap(a, b);
35 }
36 // 這裡可以對a所在的鏈做區間處理
37 // 區間為(link[ta], link[a])
38 ta=link_top[a=pa[ta]];
39 }
40 // 最後a,b會在同一條鏈, 若a!=b還要在進行一
    次區間處理
41 return dep[a]<dep[b]?a:b;
42 }

```

### 10.2 LCA

```

1 const int MAXN=100000; // 1-base
2 const int MLG=17; // log2(MAXN)+1;
3 int pa[MLG+2][MAXN+5];
4 int dep[MAXN+5];
5 vector<int> G[MAXN+5];
6 void dfs(int x, int p=0) { // dfs(root);
7 pa[0][x]=p;
8 for(int i=0; i<MLG; ++i)
9 pa[i+1][x]=pa[i][pa[i][x]];
10 for(auto &i:G[x]){
11 if(i==p) continue;
12 dep[i]=dep[x]+1;
13 dfs(i, x);
14 }

```

```

15 }
16 inline int jump(int x, int d){
17 for(int i=0; i<=MLG; ++i)
18 if((d>>i)&1) x=pa[i][x];
19 return x;
20 }
21 inline int find_lca(int a, int b){
22 if(dep[a]>dep[b]) swap(a, b);
23 b=jump(b, dep[b]-dep[a]);
24 if(a==b) return a;
25 for(int i=MLG; i>=0; --i){
26 if(pa[i][a]!=pa[i][b]){
27 a=pa[i][a];
28 b=pa[i][b];
29 }
30 }
31 return pa[0][a];
32 }

```

### 10.3 link cut tree

```

1 struct splay_tree{
2 int ch[2], pa; // 子節點跟父母
3 bool rev; // 反轉的懶惰標記
4 splay_tree(): pa(0), rev(0) { ch[0]=ch[1]=0; }
5 };
6 vector<splay_tree> nd;
7 // 有的時候用vector會TLE, 要注意
8 // 這邊以node[0]作為null節點
9 bool isroot(int x) { // 判斷是否為這棵splay
    tree的根
10 return nd[nd[x].pa].ch[0]!=x && nd[nd[x].pa]
    .ch[1]!=x;
11 }
12 void down(int x) { // 懶惰標記下推
13 if(nd[x].rev){
14 if(nd[x].ch[0]nd[nd[x].ch[0]].rev^=1;
15 if(nd[x].ch[1]nd[nd[x].ch[1]].rev^=1;
16 swap(nd[x].ch[0], nd[x].ch[1]);
17 nd[x].rev=0;
18 }
19 }
20 void push_down(int x) { // 所有祖先懶惰標記下推
21 if(!isroot(x)) push_down(nd[x].pa);
22 down(x);
23 }
24 void up(int x) { // 將子節點的資訊向上更新
25 void rotate(int x) { // 旋轉, 會自行判斷轉的方
    向
26 int y=nd[x].pa, z=nd[y].pa, d=(nd[y].ch[1]==
    x);
27 nd[x].pa=z;
28 if(!isroot(y)) nd[z].ch[nd[z].ch[1]==y]=x;
29 nd[y].ch[d]=nd[x].ch[d^1];
30 nd[nd[y].ch[d]].pa=y;
31 nd[y].pa=x, nd[x].ch[d^1]=y;
32 up(y), up(x);
33 }
34 void splay(int x) { // 將x伸展到splay tree的根
35 push_down(x);
36 while(!isroot(x)){

```

```

37 int y=nd[x].pa;
38 if(!isroot(y)){
39 int z=nd[y].pa;
40 if((nd[z].ch[0]==y)^(nd[y].ch[0]==x))
    rotate(y);
41 else rotate(x);
42 }
43 rotate(x);
44 }
45 }
46 int access(int x){
47 int last=0;
48 while(x){
49 splay(x);
50 nd[x].ch[1]=last;
51 up(x);
52 last=x;
53 x=nd[x].pa;
54 }
55 return last; // access後splay tree的根
56 }
57 void access(int x, bool is=0) { // is=0就是一般
    的access
58 int last=0;
59 while(x){
60 splay(x);
61 if(is && nd[x].pa){
62 // printf("%d\n", max(nd[last].ma, nd[nd[
    x].ch[1]].ma));
63 }
64 nd[x].ch[1]=last;
65 up(x);
66 last=x;
67 x=nd[x].pa;
68 }
69 }
70 void query_edge(int u, int v){
71 access(u);
72 access(v, 1);
73 }
74 void make_root(int x){
75 access(x), splay(x);
76 nd[x].rev^=1;
77 }
78 void make_root(int x){
79 nd[access(x)].rev^=1;
80 splay(x);
81 }
82 void cut(int x, int y){
83 make_root(x);
84 access(y);
85 splay(y);
86 nd[y].ch[0]=0;
87 nd[x].pa=0;
88 }
89 void cut_parents(int x){
90 access(x);
91 splay(x);
92 nd[nd[x].ch[0]].pa=0;
93 nd[x].ch[0]=0;
94 }
95 void link(int x, int y){
96 make_root(x);
97 nd[x].pa=y;
98 }

```



```

99 int find_root(int x){
100     x=access(x);
101     while(nd[x].ch[0])x=nd[x].ch[0];
102     splay(x);
103     return x;
104 }
105 int query(int u,int v){
106     //傳回uv路徑splay tree的根結點
107     //這種寫法無法求LCA
108     make_root(u);
109     return access(v);
110 }
111 int query_lca(int u,int v){
112     //假設求鏈上點權的總和，sum是子樹的權重和，
113     //data是節點的權重
114     access(u);
115     int lca=access(v);
116     splay(u);
117     if(u==lca){
118         //return nd[lca].data+nd[nd[lca].ch[1]].
119         //sum
120     }else{
121         //return nd[lca].data+nd[nd[lca].ch[1]].
122         //sum+nd[u].sum
123     }
124 }
125 struct EDGE{
126     int a,b,w;
127 }e[10005];
128 int n;
129 vector<pair<int,int>> G[10005];
130 //first表示子節點，second表示邊的編號
131 int pa[10005],edge_node[10005];
132 //pa是父母節點，暫存用的，edge_node是每個編
133 //被存在哪個點裡面的陣列
134 void bfs(int root){
135     //在建構的時候把每個點都設成一個splay tree
136     queue<int> q;
137     for(int i=1;i<=n;++i)pa[i]=0;
138     q.push(root);
139     while(q.size()){
140         int u=q.front();
141         q.pop();
142         for(auto P:G[u]){
143             int v=P.first;
144             if(v!=pa[u]){
145                 pa[v]=u;
146                 nd[v].pa=u;
147                 nd[v].data=e[P.second].w;
148                 edge_node[P.second]=v;
149                 up(v);
150                 q.push(v);
151             }
152         }
153     }
154 }
155 void change(int x,int b){
156     splay(x);
157     //nd[x].data=b;
158     up(x);
159 }

```

## 10.4 POJ tree

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define MAXN 10005
4 int n,k;
5 vector<pair<int,int>> g[MAXN];
6 int size[MAXN];
7 bool vis[MAXN];
8 inline void init(){
9     for(int i=0;i<=n;++i){
10         g[i].clear();
11         vis[i]=0;
12     }
13 }
14 void get_dis(vector<int> &dis,int u,int pa,
15     int d){
16     dis.push_back(d);
17     for(size_t i=0;i<g[u].size();++i){
18         int v=g[u][i].first,w=g[u][i].second;
19         if(v!=pa&&vis[v])get_dis(dis,v,u,d+w);
20     }
21 }
22 vector<int> dis;//這東西如果放在函數裡會TLE
23 int cal(int u,int d){
24     dis.clear();
25     get_dis(dis,u,-1,d);
26     sort(dis.begin(),dis.end());
27     int l=0,r=dis.size()-1,res=0;
28     while(l<r){
29         while(l<r&&dis[l]+dis[r]>k)--r;
30         res+=r-l+1;
31     }
32     return res;
33 }
34 pair<int,int> tree_centroid(int u,int pa,
35     const int sz){
36     size[u]=1;//找樹重心，second是重心
37     pair<int,int> res(INT_MAX,-1);
38     int ma=0;
39     for(size_t i=0;i<g[u].size();++i){
40         int v=g[u][i].first;
41         if(v==pa||vis[v])continue;
42         res=min(res,tree_centroid(v,u,sz));
43         size[u]+=size[v];
44         ma=max(ma,size[v]);
45     }
46     ma=max(ma,sz-size[u]);
47     return min(res,make_pair(ma,u));
48 }
49 int tree_DC(int u,int sz){
50     int center=tree_centroid(u,-1,sz).second;
51     int ans=cal(center,0);
52     vis[center]=1;
53     for(size_t i=0;i<g[center].size();++i){
54         int v=g[center][i].first,w=g[center][i].
55         second;
56         if(vis[v])continue;
57         ans+=cal(v,w);
58         ans+=tree_DC(v,size[v]);
59     }
60     return ans;
61 }
62 int main(){
63     while(scanf("%d%d",&n,&k),n||k){

```

```

61 init();
62 for(int i=1;i<=n;++i){
63     int u,v,w;
64     scanf("%d%d%d",&u,&v,&w);
65     g[u].push_back(make_pair(v,w));
66     g[v].push_back(make_pair(u,w));
67 }
68 printf("%d\n",tree_DC(1,n));
69 }
70 return 0;
71 }

```

## 11 default

### 11.1 debug

```

1 //volatile
2 #ifdef DEBUG
3 #define dbg(...) {\
4     fprintf(stderr,"%s - %d : (%s) = ",
5         __PRETTY_FUNCTION__, __LINE__,#
6         __VA_ARGS__); \
7     _DO(__VA_ARGS__); \
8 }
9 template<typename I> void _DO(I&&x){cerr<<x
10     <<endl;}
11 template<typename I,typename...T> void _DO(I
12     &&x,T&&...tail){cerr<<x<<" ";_DO(tail
13     ...);}
14 #else
15 #define dbg(...)
16 #endif

```

### 11.2 ext

```

1 #include<bits/extc++.h>
2 #include<ext/pd_ds/assoc_container.hpp>
3 #include<ext/pd_ds/tree_policy.hpp>
4 using namespace __gnu_cxx;
5 using namespace __gnu_pbds;
6 template<typename T>
7 using pbds_set = tree<T,null_type,less<T>,
8     rb_tree_tag,
9     tree_order_statistics_node_update>;
10 template<typename T,typename U>
11 using pbds_map = tree<T,U,less<T>,
12     rb_tree_tag,
13     tree_order_statistics_node_update>;
14 using heap=__gnu_pbds::priority_queue<int>;
15 //s.find_by_order(1);//0 base
16 //s.order_of_key(1);

```

### 11.3 IncStack

```

1 //Magic
2 #pragma GCC optimize "Ofast"
3 //stack resize,change esp to rsp if 64-bit
4 system
5 asm("mov %0,%esp\n" ::"g"(mem+1000000));
6 -Wl,--stack,214748364 -trigraphs
7 #pragma comment(linker, "/STACK
8 :1024000000,1024000000")
9 //linux stack resize
10 #include<sys/resource.h>
11 void increase_stack(){
12     const rlim_t ks=64*1024*1024;
13     struct rlimit rl;
14     int res=getrlimit(RLIMIT_STACK,&rl);
15     if(!res&&rl.rlim_cur<ks){
16         rl.rlim_cur=ks;
17         res=setrlimit(RLIMIT_STACK,&rl);
18     }
19 }

```

### 11.4 input

```

1 inline int read(){
2     int x=0; bool f=0; char c=getchar();
3     while(ch<'0'&&ch<'9')f|=ch=='-',ch=getchar
4     ();
5     while('0'<=ch&&ch<='9')x=x*10-'0'+ch,ch=
6     getchar();
7     return f?-x:x;
8 }
9 // #!/bin/bash
10 // g++ -std=c++11 -O2 -Wall -Wextra -Wno-
11 // unused-result -DDEBUG $1 && ./a.out
12 // -fsanitize=address -fsanitize=undefined
13 // -fsanitize=return

```

## 12 other

### 12.1 WhatDay

```

1 int whatday(int y,int m,int d){
2     if(m<=2)m+=12,--y;
3     if(y<1752||y==1752&&m<9||y==1752&&m==9&&d
4     <3)
5         return (d+2*m+3*(m+1)/5+y+y/4+y/7);
6         return (d+2*m+3*(m+1)/5+y+y/4-y/100+y/400)
7         %7;
8 }

```

### 12.2 上下最大正方形

```

1 void solve(int n,int a[],int b[]){// 1-base
2     int ans=0;
3     deque<int>da,db;

```

```

4  for(int l=1,r=1;r<=n;++r){
5      while(da.size() && a[da.back()]>=a[r]){
6          da.pop_back();
7      }
8      da.push_back(r);
9      while(db.size() && b[db.back()]>=b[r]){
10         db.pop_back();
11     }
12     db.push_back(r);
13     for(int d=a[da.front()]+b[db.front()];r-
14         1>d;--d){
15         if(da.front()==l)da.pop_front();
16         if(db.front()==l)db.pop_front();
17         if(da.size() && db.size()){
18             d=a[da.front()]+b[db.front()];
19         }
20     }
21     ans=max(ans,r-1+1);
22 }
23 printf("%d\n",ans);
24 }

```

## 12.3 最大矩形

```

1  LL max_rectangle(vector<int> s){
2      stack<pair<int,int> > st;
3      st.push(make_pair(-1,0));
4      s.push_back(0);
5      LL ans=0;
6      for(size_t i=0;i<s.size();++i){
7          int h=s[i];
8          pair<int,int> now=make_pair(h,i);
9          while(h<st.top().first){
10             now=st.top();
11             st.pop();
12             ans=max(ans,(LL)(i-now.second)*now.
13                 first);
14         }
15         if(h>st.top().first){
16             st.push(make_pair(h,now.second));
17         }
18     }
19     return ans;
20 }

```

## 13 other language

### 13.1 java

#### 13.1.1 文件操作

```

1  import java.io.*;
2  import java.util.*;
3  import java.math.*;
4  import java.text.*;
5
6  public class Main{

```

```

7      public static void main(String args[]){
8          throws FileNotFoundException,
9              IOException
10         Scanner sc = new Scanner(new FileReader(
11             "a.in"));
12         PrintWriter pw = new PrintWriter(new
13             FileWriter("a.out"));
14         int n,m;
15         n=sc.nextInt();//读入下一个INT
16         m=sc.nextInt();
17
18         for(ci=1; ci<=c; ++ci){
19             pw.println("Case #"+ci+": easy for
20                 output");
21         }
22
23         pw.close();//关闭流并释放。这个很重要。
24         否则是没有输出的
25         sc.close();//关闭流并释放
26     }
27 }

```

#### 13.1.2 优先队列

```

1  PriorityQueue queue = new PriorityQueue( 1,
2      new Comparator(){
3      public int compare( Point a, Point b ){
4          if( a.x < b.x || a.x == b.x && a.y < b.y )
5              return -1;
6          else if( a.x == b.x && a.y == b.y )
7              return 0;
8          else return 1;
9      });

```

#### 13.1.3 Map

```

1  Map map = new HashMap();
2  map.put("sa","dd");
3  String str = map.get("sa").toString();
4
5  for(Object obj : map.keySet()){
6      Object value = map.get(obj );
7  }

```

#### 13.1.4 sort

```

1  static class cmp implements Comparator{
2      public int compare(Object o1,Object o2){
3          BigInteger b1=(BigInteger)o1;
4          BigInteger b2=(BigInteger)o2;
5          return b1.compareTo(b2);
6      }
7  }
8  public static void main(String[] args)
9      throws IOException{

```

```

9      Scanner cin = new Scanner(System.in);
10     int n;
11     n=cin.nextInt();
12     BigInteger[] seg = new BigInteger[n];
13     for (int i=0;i<n;i++)
14         seg[i]=cin.nextBigInteger();
15     Arrays.sort(seg,new cmp());
16 }

```

## 13.2 python heap

```

1  import heapq
2
3  heap = [7,1,2,2]
4  heapq.heapify(heap)
5  print(heap) # [1, 2, 2, 7]
6  heapq.heappush(heap, 5)
7  print(heap) # [1, 2, 2, 7, 5]
8  print(heapq.heappop(heap)) # 1
9  print(heap) # [2, 2, 5, 7]

```

## 13.3 python input

```

1  ans = sum(map(float, input().split()))
2  # input: 1.1 2.2 3.3 4.4 5.5
3  print(ans) # 16.5
4
5  (n, m) = map(int, input().split()) # 300 200
6  print(n * m) # 60000
7
8  Arr = list(map(int, input().split()))
9  # input: 1 2 3 4 5
10 print(Arr) # [1, 2, 3, 4, 5]

```

## 14 zformula

### 14.1 formula

#### 14.1.1 Pick 公式

給定頂點坐標均是整點的簡單多邊形。面積 = 內部格點數 + 邊上格點數/2-1

#### 14.1.2 圖論

- 對於平面圖  $\cdot F = E - V + C + 1 \cdot C$  是連通分量數
- 對於平面圖  $\cdot E \leq 3V - 6$
- 對於連通圖  $G$   $\cdot$  最大獨立點集的大小設為  $I(G)$   $\cdot$  最大匹配大小設為  $M(G)$   $\cdot$  最小點覆蓋設為  $C_v(G)$   $\cdot$  最小邊覆蓋設為  $C_e(G)$   $\cdot$  對於任意連通圖：

- $I(G) + C_v(G) = |V|$
- $M(G) + C_e(G) = |V|$

#### 4. 對於連通二分圖：

- $I(G) = C_v(G)$
- $M(G) = C_e(G)$

#### 5. 最大權閉合圖：

- $C(u, v) = \infty, (u, v) \in E$
- $C(S, v) = W_v, W_v > 0$
- $C(v, T) = -W_v, W_v < 0$
- $ans = \sum_{W_v > 0} W_v - flow(S, T)$

#### 6. 最大密度子圖：

- 求  $\max \left( \frac{W_e + W_v}{|V'|} \right), e \in E', v \in V'$
- $U = \sum_{v \in V} 2W_v + \sum_{e \in E} W_e$
- $C(u, v) = W_{(u,v)}, (u, v) \in E$   $\cdot$  雙向邊
- $C(S, v) = U, v \in V$
- $D_u = \sum_{(u,v) \in E} W_{(u,v)}$
- $C(v, T) = U + 2g - D_v - 2W_v, v \in V$
- 二分搜  $g$  :  
 $l = 0, r = U, eps = 1/n^2$   
 if  $((U \times |V| - flow(S, T))/2 > 0)$   $l = mid$   
 else  $r = mid$
- $ans = min\_cut(S, T)$
- $|E| = 0$  要特殊判斷

#### 7. 弦圖：

- 點數大於 3 的環都要有一條弦
- 完美消除序列從後往前依次給每個點染色  $\cdot$  給每個點染上可以染的最小顏色
- 最大團大小 = 色數
- 最大獨立集：完美消除序列從前往後能選就選
- 最小團覆蓋：最大獨立集的點和他延伸的邊構成
- 區間圖是弦圖
- 區間圖的完美消除序列：將區間按造又端點由小到大排序
- 區間圖染色：用線段樹做

### 14.1.3 dinic 特殊圖複雜度

- 單位流： $O\left(\min\left(V^{3/2}, E^{1/2}\right)E\right)$
- 二分圖： $O\left(V^{1/2}E\right)$

14.1.4 0-1 分數規劃

$x_i = \{0, 1\}$  ·  $x_i$  可能會有其他限制 · 求  $max \left( \frac{\sum B_i x_i}{\sum C_i x_i} \right)$

- 1.  $D(i, g) = B_i - g \times C_i$
- 2.  $f(g) = \sum D(i, g) x_i$
- 3.  $f(g) = 0$  時  $g$  為最佳解 ·  $f(g) < 0$  沒有意義
- 4. 因為  $f(g)$  單調可以二分搜  $g$
- 5. 或用 Dinkelbach 通常比較快

```
1 binary_search(){
2   while(r-l>eps){
3     g=(l+r)/2;
4     for(i:所有元素)D[i]=B[i]-g*C[i];//D(i,g)
5     找出一組合法x[i]使f(g)最大;
6     if(f(g)>0) l=g;
7     else r=g;
8   }
9   Ans = r;
10 }
11 Dinkelbach(){
12   g=任意狀態 (通常設為0);
13   do{
14     Ans=g;
15     for(i:所有元素)D[i]=B[i]-g*C[i];//D(i,g)
16     找出一組合法x[i]使f(g)最大;
17     p=0,q=0;
18     for(i:所有元素)
19       if(x[i])p+=B[i],q+=C[i];
20     g=p/q;//更新解 · 注意q=0的情況
21   }while(abs(Ans-g)>EPS);
22   return Ans;
23 }
```

14.1.5 學長公式

- 1.  $\sum_{d|n} \phi(n) = n$
- 2.  $g(n) = \sum_{d|n} f(d) \Rightarrow f(n) = \sum_{d|n} \mu(d) \times g(n/d)$
- 3. Harmonic series  $H_n = \ln(n) + \gamma + 1/(2n) - 1/(12n^2) + 1/(120n^4)$
- 4.  $\gamma = 0.57721566490153286060651209008240243104215$
- 5. 格雷碼  $= n \oplus (n >> 1)$
- 6.  $SG(A + B) = SG(A) \oplus SG(B)$
- 7. 選轉矩陣  $M(\theta) = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$

14.1.6 基本數論

- 1.  $\sum_{d|n} \mu(n) = [n == 1]$
- 2.  $g(m) = \sum_{d|m} f(d) \Leftrightarrow f(m) = \sum_{d|m} \mu(d) \times g(m/d)$
- 3.  $\sum_{i=1}^n \sum_{j=1}^m$  互質數量  $= \sum \mu(d) \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor$
- 4.  $\sum_{i=1}^n \sum_{j=1}^n lcm(i, j) = n \sum_{d|n} d \times \phi(d)$

14.1.7 排組公式

- 1. k 卡特蘭  $\frac{C_n^{kn}}{n(k-1)+1} \cdot C_m^n = \frac{n!}{m!(n-m)!}$
- 2.  $H(n, m) \cong x_1 + x_2 \dots + x_n = k, num = C_k^{n+k-1}$
- 3. Stirling number of  $2^{nd}$ ,  $n$  入分  $k$  組方法數目
  - (a)  $S(0, 0) = S(n, n) = 1$
  - (b)  $S(n, 0) = 0$
  - (c)  $S(n, k) = kS(n-1, k) + S(n-1, k-1)$
- 4. Bell number,  $n$  入分任意多組方法數目
  - (a)  $B_0 = 1$
  - (b)  $B_n = \sum_{i=0}^n S(n, i)$
  - (c)  $B_{n+1} = \sum_{k=0}^n C_k^n B_k$
  - (d)  $B_{p+n} \equiv B_n + B_{n+1} \pmod{p}$ ,  $p$  is prime
  - (e)  $B_{p^m+n} \equiv mB_n + B_{n+1} \pmod{p}$ ,  $p$  is prime
  - (f) From  $B_0 : 1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, 115975$
- 5. Derangement, 錯排, 沒有人在自己位置上
  - (a)  $D_n = n!(1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} \dots + (-1)^n \frac{1}{n!})$
  - (b)  $D_n = (n-1)(D_{n-1} + D_{n-2}), D_0 = 1, D_1 = 0$
  - (c) From  $D_0 : 1, 0, 1, 2, 9, 44, 265, 1854, 14833, 133496$
- 6. Binomial Equality
  - (a)  $\sum_k \binom{r}{m+k} \binom{s}{n-k} = \binom{r+s}{m+n}$
  - (b)  $\sum_k \binom{m+k}{m} \binom{n-k}{n-k} = \binom{l+s}{l+m+n}$
  - (c)  $\sum_k \binom{m+k}{m} \binom{s+k}{n} (-1)^k = (-1)^{l+m} \binom{s-m}{n-l}$
  - (d)  $\sum_{k \leq l} \binom{l-k}{m} \binom{s}{k-n} (-1)^k = \frac{(-1)^{l+m} \binom{s-m-1}{l-n-m}}{(-1)^{l+m} \binom{s-m-1}{l-n-m}}$
  - (e)  $\sum_{0 \leq k \leq l} \binom{l-k}{m} \binom{q+k}{n} = \binom{l+q+1}{m+n+1}$
  - (f)  $\binom{r}{k} = (-1)^k \binom{k-r-1}{k}$
  - (g)  $\binom{r}{m} \binom{m}{k} = \binom{r}{m-k} \binom{r-k}{m-k}$
  - (h)  $\sum_{k \leq n} \binom{r+k}{k} = \binom{r+n+1}{n}$
  - (i)  $\sum_{0 \leq k \leq n} \binom{k}{m} = \binom{n+1}{m+1}$
  - (j)  $\sum_{k \leq m} \binom{m+r}{k} x^k y^{m-k} = \sum_{k \leq m} \binom{-r}{k} (-x)^k (x+y)^{m-k}$

14.1.8 冪次, 冪次和

- 1.  $a^b \% P = a^{b \% \varphi(P) + \varphi(P)}, b \geq \varphi(P)$
- 2.  $1^3 + 2^3 + 3^3 + \dots + n^3 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4}$
- 3.  $1^4 + 2^4 + 3^4 + \dots + n^4 = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$
- 4.  $1^5 + 2^5 + 3^5 + \dots + n^5 = \frac{n^6}{6} + \frac{n^5}{2} + \frac{5n^4}{12} - \frac{n^2}{12}$
- 5.  $0^k + 1^k + 2^k + \dots + n^k = P(k), P(k) = \frac{(n+1)^{k+1} - \sum_{i=0}^{k-1} C_i^{k+1} P(i)}{k+1}, P(0) = n+1$
- 6.  $\sum_{k=0}^{m-1} k^n = \frac{1}{n+1} \sum_{k=0}^n C_k^{n+1} B_k m^{n+1-k}$
- 7.  $\sum_{j=0}^m C_j^{m+1} B_j = 0, B_0 = 1$
- 8. 除了  $B_1 = -1/2$  · 剩下的奇數項都是 0
- 9.  $B_2 = 1/6, B_4 = -1/30, B_6 = 1/42, B_8 = -1/30, B_{10} = 5/66, B_{12} = -691/2730, B_{14} = 7/6, B_{16} = -3617/510, B_{18} = 43867/798, B_{20} = -174611/330,$

14.1.9 Burnside’s lemma

- 1.  $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- 2.  $X^g = t^{c(g)}$
- 3.  $G$  表示有幾種轉法 ·  $X^g$  表示在那種轉法下 · 有幾種是會保持對稱的 ·  $t$  是顏色數 ·  $c(g)$  是循環節不動的面數 ·
- 4. 正立方體塗三顏色 · 轉 0 有  $3^6$  個元素不變 · 轉 90 有 6 種 · 每種有  $3^3$  不變 · 180 有  $3 \times 3^4 \cdot 120(\text{角})$  有  $8 \times 3^2 \cdot 180(\text{邊})$  有  $6 \times 3^3 \cdot$  全部  $\frac{1}{24} (3^6 + 6 \times 3^3 + 3 \times 3^4 + 8 \times 3^2 + 6 \times 3^3) = \frac{57}{24}$

14.1.10 Count on a tree

- 1. Rooted tree:  $s_{n+1} = \frac{1}{n} \sum_{i=1}^n (i \times a_i \times \sum_{j=1}^{\lfloor n/i \rfloor} a_{n+1-i \times j})$
- 2. Unrooted tree:
  - (a) Odd:  $a_n - \sum_{i=1}^{n/2} a_i a_{n-i}$
  - (b) Even:  $Odd + \frac{1}{2} a_{n/2} (a_{n/2} + 1)$
- 3. Spanning Tree
  - (a) 完全圖  $n^n - 2$
  - (b) 一般圖 (Kirchhoff’s theorem)  $M[i][i] = \text{degree}(V_i), M[i][j] = -1, \text{if have } E(i, j), 0 \text{ if no edge. delete any one row and col in } A, ans = \det(A)$

15

15.1 ganadoQuote

- 1. ¡Allí está!
- 2. ¡Un forastero!
- 3. ¡Agarrenlo!
- 4. ¡Os voy a romper a pedazos!
- 5. ¡Cógelo!
- 6. ¡Te voy a hacer picadillo!
- 7. ¡Te voy a matar!
- 8. ¡Míralo, está herido!
- 9. ¡Sos cerdo!
- 10. ¿Dónde estás?
- 11. ¡Detrás de tí, imbécil!
- 12. ¡No dejes que se escape!
- 13. ¡Basta, hijo de puta!
- 14. Lord Saddler...
- 15.
- 16. ¡Mátalo!
- 17. ¡Allí está!
- 18. Morir es vivir.
- 19. ¡Sííííí, ¡Quiero matar!
- 20. Muere, muere, muere....
- 21. Cerebros, cerebros, cerebros...
- 22. Cógedlo, cógedlo, cógedlo...
- 23. Lord Saddler...
- 24. Dieciséis.
- 25.

- 26. ¡Va por él!
- 27. ¡Muérete!
- 28. ¡Cógelo!
- 29. ¡Te voy a matar!
- 30. ¡Bloqueale el paso!
- 31. ¡Te cogí!
- 32. ¡No dejes que se escape!
- 33.
- 34. ¿Qué carajo estás haciendo aquí? ¡Lárgate, cabrón!
- 35. Hay un rumor de que hay un extranjero entre nosotros.
- 36. Nuestro jefe se encargará de la rata.
- 37. Su "Las Plagas" es mucho mejor que la nuestra.
- 38. Tienes razón, es un hombre.
- 39. Usa los músculos.
- 40. Se vuelve loco!
- 41. ¡Hey, acá!
- 42. ¡Por aquí!
- 43. ¡El Gigante!
- 44. ¡Del Lago!
- 45. ¡Cógelo!
- 46. ¡Cógenlo!
- 47. ¡Allí!
- 48. ¡Rápido!
- 49. ¡Empieza a rezar!
- 50. ¡Mátenlos!
- 51. ¡Te voy a romper en pedazos!
- 52. ¡La campana!
- 53. Ya es hora de rezar.
- 54. Tenemos que irnos.
- 55. ¡Maldita sea, mierda!
- 56. ¡Ya es hora de aplastar!
- 57. ¡Mierda!
- 58. ¡Puedes correr, pero no te puedes esconder!
- 59. ¡Sos cerdo!
- 60. ¡Está en la trampa!
- 61. ¡Ah, que madre!
- 62. ¡Vámonos!
- 63. ¡Ándale!
- 64. ¡Cabrón!
- 65. ¡Coño!
- 66. ¡Agárrenlo!
- 67. Cógerlo, Cógerlo...
- 68. ¡Allí está, máta!
- 69. ¡No dejas que se escape de la isla vivo!
- 70. ¡Hasta luego!
- 71. ¡Rápido, es un intruso!

15.2

```
1  /*****
2  L'Internationale,
3      Sera le genre humain.
4
5
6
7
8
9
10
11
12
13
14
15
16  *****/
17 Вставай, проклятьем заклеимённый,
18 Весь мир голодных и рабов!
19 Кипит наш разум возмущённый
20 И в смертный бой вести готов.
21 Весь мир насилия мы разрушим
22 До основания, а затем
23 Мы наш, мы новый мир построим, –
24 Кто был ничем, тот станет всем.
25
26 Chorus
27 Это есть наш последний
28 И решительный бой;
29 С Интернационалом
30 Воспрянет род людской!
31
32 Никто не даст нам избавленья:
33 Ни бог, ни царь и не герой!
34 Добьёмся мы освобожденья
35 Своею собственной рукой.
36 Чтоб свергнуть гнёт рукой умелой,
37 Отвоевать своё добро, –
38 Вдувайте горн и куйте смело,
39 Пока железо горячо!
40
41 Chorus
42
43 Довольно кровь сосать, вампиры,
44 Тюрьмой, налогом, нищетой!
45 У вас — вся власть, все блага мира,
46 А наше право — звук пустой !
47 Мы жизнь построим по-иному –
48 И вот наш лозунг боевой:
49 Вся власть народу трудовому!
50 А дармоедов всех долой!
51
52 Chorus
53
54 Презренны вы в своём богатстве,
55 Угля и стали короли!
56 Вы ваши троны, тунеядцы,
57 На наших спинах возвели.
58 Заводы, фабрики, палаты –
59 Всё нашим создано трудом.
60 Пора! Мы требуем возврата
61 Того, что взято грабежом.
62
63 Chorus
```

```
64
65 Довольно королям в угоду
66 Дурманить нас в чаду войны!
67 Война тиранам! Мир Народу!
68 Бастуйте, армии сыны!
69 Когда ж тираны нас заставят
70 В бою геройски пасть за них –
71 Убийцы, в вас тогда направим
72 Мы жерла пушек боевых!
73
74 Chorus
75
76 Лишь мы, работники всемирной
77 Великой армии труда,
78 Владеть землёй имеем право,
79 Но паразиты — никогда!
80 И если гром великий грянет
81 Над сворой псов и палачей, –
82 Для нас всё так же солнце станет
83 Сиять огнём своих лучей.
84
85 Chorus
```

15.3 保佑

```
1  //      _oo0oo_
2  //      o8888888o
3  //      88" . "88
4  //      (| -_- |)
5  //      0\ = /0
6  //
7  //
8  //
9  //
10 //
11 //
12 //
13 //
14 //
15 //
16 //
17 //
18 //
19 //
20 // ~~~~~
21 //      佛祖保佑      永無BUG
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38 Chorus
```

```
39
40
41
42
43
44
45 #
46 #
47 #
48 #
49 #
50 #
51 #
52 #
53 #
54 #
55 #
56 #
57 #
58 #
59 #
60 #
61 #
62 #
63 #
64 #
65 #
66
67
68 // ##      #####
69 // ##      ##
70 // ##      ##
71 // ##      ##
72 // ##      ##
73 // ##      ##
74 // ##      ##
75 // ##      ##
76 // #####
77 //      ##      ##
78 //      ##      ##
79 //      ##      ##
80 //      ##      ##
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82 //      ##      ##
83 //      ##      ##
84 // #####      ##
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# ACM ICPC TEAM REFERENCE - ANGRY CROW TAKES FLIGHT!

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