## 1 Computational\_Geometral

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# 1.1 Geometry.cpp

```
60
1 const double PI=atan2(0.0,-1.0);
                                                61
  template<typename T>
   struct point{
    T x,y;
                                                63
    point(){}
    point(const T&x,const T&y):x(x),y(y){}
                                                64
    point operator+(const point &b)const{
      return point(x+b.x,y+b.y);}
    point operator-(const point &b)const{
      return point(x-b.x,y-b.y);}
                                                66
    point operator*(const T &b)const{
                                                67
       return point(x*b,v*b);}
                                                68
13
    point operator/(const T &b)const{
      return point(x/b,v/b);}
14
    bool operator==(const point &b)const{
                                                70
16
      return x==b.x&&v==b.v:
                                                71
17
    T dot(const point &b)const{
                                                72
18
      return x*b.x+y*b.y;}
                                                73
19
    T cross(const point &b)const{
20
      return x*b.y-y*b.x;}
                                                74
    point normal()const{//求法向量
      return point(-y,x);}
                                                75
23
    T abs2()const{//向量長度的平方
                                                 76
      return dot(*this);
^{24}
                                                77
25
                                                78
26
    T rad(const point &b)const{//兩向量的弧度
      return fabs(atan2(fabs(cross(b)),dot(b))
28
                                                81
    T getA()const{//對x軸的弧度
                                                82
      T A=atan2(y,x);//超過180度會變負的
      if(A<=-PI/2)A+=PI*2;
      return A:
32
                                                84
33
34
   };
                                                85
   template<typename T>
   struct line{
    line(){}
    point<T> p1,p2;
    T a,b,c;//ax+by+c=0
    line(const point<T>&x,const point<T>&y):p1
         (x),p2(y){}
    void pton(){//轉成一般式
41
42
      a=p1.y-p2.y;
43
      b=p2.x-p1.x;
                                                90
44
      c=-a*p1.x-b*p1.v:
45
    T cross(const point<T> &p)const{//點和有向
          直線的關係, >0左邊、=0在線上<0右邊
       return (p2-p1).cross(p-p1);
47
48
    bool point on segment(const point<T>&p)
49
         const{//點是否線段上
      return cross(p) == 0&&(p1-p).dot(p2-p) <= 0;</pre>
50
51
52
    T dis2(const point<T> &p,bool is segment
         =0) const { // 點 跟 直 線 / 線 段 的 距 離 平 方
       point<T> v=p2-p1,v1=p-p1;
```

```
if(is segment){
    point<T> v2=p-p2;
                                           100
    if(v.dot(v1)<=0)return v1.abs2();</pre>
                                          101
   if(v.dot(v2)>=0)return v2.abs2();
                                          102
                                          103
 T tmp=v.cross(v1);
  return tmp*tmp/v.abs2();
                                           104
                                           105
T seg_dis2(const line<T> &1)const{//兩線段 106
  return min({dis2(l.p1,1),dis2(l.p2,1),l. 108
      dis2(p1,1),1.dis2(p2,1)});
                                           109
point<T> projection(const point<T> &p)
                                          110
                                          111
     const{//點對直線的投影
  point<T> n=(p2-p1).normal();
                                          112
                                          113
  return p-n*(p-p1).dot(n)/n.abs2();
                                          114
point<T> mirror(const point<T> &p)const{//
     點對直線的鏡射
  //要先呼叫pton轉成一般式
                                           116
  noint<T> ans:
 T d=a*a+b*b:
  ans.x=(b*b*p.x-a*a*p.x-2*a*b*p.y-2*a*c)/ 117
  ans.y=(a*a*p.y-b*b*p.y-2*a*b*p.x-2*b*c)/<sup>118</sup>
                                           119
  return ans:
                                           120
                                          121
bool equal(const line &1)const{//直線相等
  return cross(1.p1)==0&&cross(1.p2)==0;
bool parallel(const line &l)const{//直線平
  return (p1-p2).cross(1.p1-1.p2)==0;
bool cross_seg(const line &1)const{//直線
     是否交線段
  return (p2-p1).cross(1.p1-p1)*(p2-p1).
                                          130
      cross(1.p2-p1)<=0;
                                          131
char line intersect(const line &1)const{// 133
     直線相交情況,-1無限多點、1交於一點、0134
  return parallel(1)?(cross(1.p1)==0?-1:0) 135
                                          136
char seg intersect(const line &l)const{// 138
     線段相交情況,-1無限多點、1交於一點、0139
                                           140
                                          141
 T c1=(p2-p1).cross(l.p1-p1);
                                           142
 T c2=(p2-p1).cross(1.p2-p1);
 T c3=(1.p2-1.p1).cross(p1-1.p1);
 T c4=(1.p2-1.p1).cross(p2-1.p1):
  if(c1==0&&c2==0){
                                           143
    if(p1==1.p1&&(p2-p1).dot(1.p2)<=0)</pre>
                                          144
        return 1:
    if(p1==1.p2&&(p2-p1).dot(l.p1)<=0)
                                           145
        return 1:
    if(p2==1.p1&&(p1-p2).dot(1.p2)<=0)
                                           146
        return 1;
                                          147
    if(p2==1.p2&&(p1-p2).dot(1.p1)<=0)
        return 1;
                                           148
```

```
return -1:
                                                  149
       }else if(c1*c2<=0&&c3*c4<=0)return 1;</pre>
                                                  150
       return 0;
                                                  151
     point<T> line intersection(const line &l)
          const{/*直線交點*/
       point<T> a=p2-p1,b=l.p2-l.p1,s=l.p1-p1;
       //if(a.cross(b)==0)return INF;
                                                  154
       return p1+a*s.cross(b)/a.cross(b);
                                                  155
                                                  156
     point<T> seg intersection(const line &1)
                                                  157
          const{//線段交點
       T c1=(p2-p1).cross(l.p1-p1);
       T c2=(p2-p1).cross(1.p2-p1);
                                                  159
       T c3=(1.p2-1.p1).cross(p1-1.p1);
                                                  160
       T c4=(1.p2-1.p1).cross(p2-1.p1);
                                                  161
       if(c1==0&&c2==0){
                                                  162
          if(p1==1.p1&&(p2-p1).dot(1.p2)<=0)
                                                  163
               return p1;
                                                  164
          if(p1==1.p2&&(p2-p1).dot(1.p1)<=0)
                                                  165
              return p1;
                                                  166
          if(p2==1.p1&&(p1-p2).dot(1.p2) <= 0)
                                                  167
              return p2;
                                                  168
          if(p2==1.p2&&(p1-p2).dot(1.p1) <=0)
               return p2;
                                                  169
       }else if(c1*c2<=0&&c3*c4<=0)return
                                                  170
            line_intersection(1);
                                                  171
       //return INF:
                                                  172
   };
122 template<typename T>
                                                  173
123 struct polygon{
     polygon(){}
                                                  174
     vector<point<T> > p;//逆時針順序
     T area()const{//面積
                                                  175
       T ans=0;
                                                  176
       for(int i=p.size()-1,j=0;j<(int)p.size()</pre>
                                                  177
          ans+=p[i].cross(p[j]);
                                                  178
       return ans/2;
                                                  179
                                                  180
     point<T> center of mass()const{//重心
                                                  181
       T cx=0, cy=0, w=0;
                                                  182
       for(int i=p.size()-1,j=0;j<(int)p.size()</pre>
             ;i=j++){
          T a=p[i].cross(p[j]);
                                                  183
          cx+=(p[i].x+p[j].x)*a;
                                                  184
          cy+=(p[i].y+p[j].y)*a;
          w+=a;
                                                  185
                                                  186
       return point<T>(cx/3/w,cy/3/w);
                                                  187
     char ahas(const point<T>& t)const{//點是否
          在簡單多邊形內,是的話回傳1、在邊上回 189
          傳-1、否則回傳0
                                                  190
       bool c=0;
       for(int i=0,j=p.size()-1;i<p.size();j=i 191</pre>
          if(line<T>(p[i],p[j]).point_on_segment 193
               (t))return -1;
          else if((p[i].y>t.y)!=(p[j].y>t.y)&&
                                                 195
          t.x<(p[j].x-p[i].x)*(t.y-p[i].y)/(p[j]
               ].y-p[i].y)+p[i].x)
            c=!c;
                                                  197
```

```
return c;
char point in convex(const point<T>&x)
    const{
  int l=1,r=(int)p.size()-2;
  while(1<=r){//點是否在凸多邊形內,是的話
       回傳1、在邊上回傳-1、否則回傳0
    int mid=(1+r)/2;
   T a1=(p[mid]-p[0]).cross(x-p[0]);
   T a2=(p[mid+1]-p[0]).cross(x-p[0]);
   if(a1>=0&&a2<=0){
     T res=(p[mid+1]-p[mid]).cross(x-p[
          mid]);
     return res>0?1:(res>=0?-1:0);
   }else if(a1<0)r=mid-1:</pre>
   else l=mid+1;
 return 0;
vector<T> getA()const{//凸包邊對x軸的夾角
 vector<T>res;//一定是遞增的
  for(size t i=0;i<p.size();++i)</pre>
   res.push_back((p[(i+1)%p.size()]-p[i])
         .getA());
 return res;
bool line intersect(const vector<T>&A,
    const line<T> &1)const{//O(logN)
  int f1=upper_bound(A.begin(),A.end(),(1.
      p1-l.p2).getA())-A.begin();
  int f2=upper bound(A.begin(), A.end(),(1.
      p2-1.p1).getA())-A.begin();
  return 1.cross_seg(line<T>(p[f1],p[f2]))
polygon cut(const line<T> &l)const{//△包
     對直線切割,得到直線 L左側的凸包
  polvgon ans:
  for(int n=p.size(),i=n-1,j=0;j<n;i=j++){</pre>
   if(1.cross(p[i])>=0){
      ans.p.push back(p[i]);
     if(1.cross(p[i])<0)
        ans.p.push back(1.
            line intersection(line<T>(p[i
            ],p[j])));
    }else if(1.cross(p[j])>0)
      ans.p.push_back(1.line_intersection(
          line<T>(p[i],p[j])));
 return ans;
static bool graham cmp(const point<T>& a,
    const point<T>& b){
 return (a.x<b.x)||(a.x==b.x&&a.y<b.y);//</pre>
      凸包排序函數
void graham(vector<point<T> > &s){// □ 包
 sort(s.begin(),s.end(),graham cmp);
 p.resize(s.size()+1);
 int m=0:
 for(int i=0;i<(int)s.size();++i){</pre>
   while (m>=2\&(p[m-1]-p[m-2]).cross(s[i
        ]-p[m-2])<=0)--m;
    p[m++]=s[i];
```

```
250
199
        for(int i=s.size()-2,t=m+1;i>=0;--i){
          while(m>=t&&(p[m-1]-p[m-2]).cross(s[i 252
200
               ]-p[m-2])<=0)--m;
201
          p[m++]=s[i];
                                                    253
202
203
       if(s.size()>1)--m:
                                                    254
       p.resize(m);
204
                                                    255
205
                                                    256
                                                    257
206
     T diam(){//直徑
                                                    258
207
       int n=p.size(),t=1;
                                                    259
208
       T ans=0;p.push_back(p[0]);
                                                    260
209
        for(int i=0;i<n;i++){</pre>
                                                    261
210
          point<T> now=p[i+1]-p[i];
211
          while(now.cross(p[t+1]-p[i])>now.cross
               (p[t]-p[i]))t=(t+1)%n;
          ans=max(ans,max((p[i]-p[t]).abs2(),(p[ 263
212
               i+1]-p[t+1]).abs2()));
                                                    264
                                                    265
^{214}
        return p.pop_back(),ans;
215
216
     T min_cover_rectangle(){//最小覆蓋矩形
                                                    266
217
       int n=p.size(),t=1,r=1,l;
218
       if(n<3)return 0;//也可以做最小周長矩形
                                                    267
       T ans=1e99; p. push back(p[0]);
219
                                                    268
220
        for(int i=0;i<n;i++){</pre>
                                                    269
221
          point<T> now=p[i+1]-p[i];
                                                    270
222
          while(now.cross(p[t+1]-p[i])>now.cross 271
               (p[t]-p[i]))t=(t+1)%n;
223
          while(now.dot(p[r+1]-p[i])>now.dot(p[r 273
               ]-p[i]))r=(r+1)%n;
                                                    274
          if(!i)l=r;
224
225
          while (now.dot(p[l+1]-p[i]) < =now.dot(p[276])
               l]-p[i]))l=(l+1)%n;
          T d=now.abs2();
226
          T tmp=now.cross(p[t]-p[i])*(now.dot(p[ 279
227
               r]-p[i])-now.dot(p[l]-p[i]))/d;
228
          ans=min(ans,tmp);
                                                    280
229
                                                    281
        return p.pop_back(),ans;
230
                                                    282
231
                                                    283
                                                    284
     T max_triangle(){//最大內接三角形
232
233
        int n=p.size(),a=1,b=2;
                                                    285
234
        if(n<3)return 0;</pre>
                                                    286
235
       T ans=0,tmp;p.push back(p[0]);
                                                    287
                                                    288 };
236
       for(int i=0;i<n;++i){</pre>
          while((p[a]-p[i]).cross(p[b+1]-p[i])>( 289
237
               tmp=(p[a]-p[i]).cross(p[b]-p[i])))^{290}
               b=(b+1)%n;
          ans=max(ans,tmp);
238
239
          while((p[a+1]-p[i]).cross(p[b]-p[i])>(293)
               tmp=(p[a]-p[i]).cross(p[b]-p[i])))
               a=(a+1)%n:
                                                    295
          ans=max(ans,tmp);
                                                    296
241
                                                    297
242
        return p.pop_back(),ans/2;
243
                                                    298
     T dis2(polygon &pl){//凸包最近距離平方
                                                    299
244
                                                    300
245
        vector < point < T > & P = p, & Q = pl.p;
       int n=P.size(), m=Q.size(), l=0, r=0;
246
                                                    301
247
        for(int i=0;i<n;++i)if(P[i].y<P[1].y)l=i 302</pre>
        for(int i=0;i<m;++i)if(Q[i].y<Q[r].y)r=i 304</pre>
248
249
        P.push_back(P[0]),Q.push_back(Q[0]);
```

```
T ans=1e99:
                                               306
    for(int i=0;i<n;++i){</pre>
      while((P[1]-P[1+1]).cross(Q[r+1]-Q[r]) 307
           <0)r=(r+1)%m;
                                               308
      ans=min(ans,line<T>(P[1],P[1+1]).
                                               309
           seg dis2(line\langle T \rangle (Q[r],Q[r+1])));
      1=(1+1)%n:
   return P.pop_back(),Q.pop_back(),ans;
                                               312
 static char sign(const point<T>&t){
                                               313
   return (t.y==0?t.x:t.y)<0;</pre>
                                               314
                                               315
 static bool angle cmp(const line<T>& A,
                                               316
       const line<T>& B){
    point<T> a=A.p2-A.p1,b=B.p2-B.p1;
                                               318
   return sign(a)<sign(b)||(sign(a)==sign(b 319
         )&&a.cross(b)>0);
                                               320
 int halfplane intersection(vector<line<T>
      > &s){//半平面交
    sort(s.begin(),s.end(),angle_cmp);//線段 323
         左側為該線段半平面
    int L,R,n=s.size();
                                               325
                                               326
    vector<point<T> > px(n);
                                               327
    vector<line<T> > q(n);
                                               328
    q[L=R=0]=s[0];
                                               329
    for(int i=1;i<n;++i){</pre>
     while(L<R&&s[i].cross(px[R-1])<=0)--R; 330
     while(L<R&&s[i].cross(px[L])<=0)++L;</pre>
      q[++R]=s[i];
                                               332
      if(q[R].parallel(q[R-1])){
                                               333
        if(q[R].cross(s[i].p1)>0)q[R]=s[i];
      if(L<R)px[R-1]=q[R-1].
                                               336
           line_intersection(q[R]);
                                               337
    while (L < R\&q[L].cross(px[R-1]) <= 0) -- R;
    p.clear();
                                               339
    if(R-L<=1)return 0;</pre>
                                               340 };
    px[R]=q[R].line_intersection(q[L]);
    for(int i=L;i<=R;++i)p.push_back(px[i]); 342
    return R-L+1;
                                               344
                                               345
template<typename T>
struct triangle{
                                               346
 point<T> a,b,c;
 triangle(){}
  triangle(const point<T> &a,const point<T>
      &b, const point <T> &c):a(a),b(b),c(c)\{\}_{349}^{349}
 T area()const{
                                               350
   T t=(b-a).cross(c-a)/2;
                                               351
    return t>0?t:-t;
                                               352
                                               353
  point<T> barycenter()const{//重心
                                               354
   return (a+b+c)/3;
                                               355
                                               356
 point<T> circumcenter()const{//外心
   static line<T> u,v;
                                               357
   u.p1=(a+b)/2;
                                               358
   u.p2=point<T>(u.p1.x-a.y+b.y,u.p1.y+a.x-359
         b.x):
   v.p1=(a+c)/2;
```

```
v.p2=point<T>(v.p1.x-a.y+c.y,v.p1.y+a.x- 360
       return u.line_intersection(v);
     point<T> incenter()const{//內心
                                                 362
       T = sqrt((b-c).abs2()), B=sqrt((a-c).abs2
            ()),C=sqrt((a-b).abs2());
       return point<T>(A*a.x+B*b.x+C*c.x,A*a.y+
            B*b.y+C*c.y)/(A+B+C);
                                                 364
                                                 365
     point<T> perpencenter()const{//垂心
                                                 366
       return barycenter()*3-circumcenter()*2;
                                                 367
                                                 368
317 template<typename T>
                                                 369
   struct point3D{
     T x,y,z;
     point3D(){}
     point3D(const T&x,const T&y,const T&z):x(x 372
          ),y(y),z(z){}
     point3D operator+(const point3D &b)const{ 374
       return point3D(x+b.x,y+b.y,z+b.z);}
     point3D operator-(const point3D &b)const{ 375
       return point3D(x-b.x,y-b.y,z-b.z);}
     point3D operator*(const T &b)const{
                                                 376
       return point3D(x*b,y*b,z*b);}
                                                 377
     point3D operator/(const T &b)const{
                                                 378
       return point3D(x/b,y/b,z/b);}
                                                 379
     bool operator == (const point3D &b)const{
       return x==b.x&&y==b.y&&z==b.z;}
                                                 380
     T dot(const point3D &b)const{
                                                 381
       return x*b.x+y*b.y+z*b.z;}
                                                 382
     point3D cross(const point3D &b)const{
       return point3D(y*b.z-z*b.y,z*b.x-x*b.z,x
            *b.y-y*b.x);}
     T abs2()const{//向量長度的平方
                                                 384
       return dot(*this);}
     T area2(const point3D &b)const{//和b、原點
                                                 385
           圍成面積的平方
                                                 386
       return cross(b).abs2()/4;}
                                                 387
341 template<typename T>
                                                 388
   struct line3D{
     point3D<T> p1,p2;
                                                 389
     line3D(){}
     line3D(const point3D<T> &p1,const point3D<
          T > &p2):p1(p1),p2(p2){}
     T dis2(const point3D<T> &p,bool is_segment
                                                 392
          =0) const { // 點 跟 直 線 / 線 段 的 距 離 平 方
                                                 393
       point3D<T> v=p2-p1,v1=p-p1;
                                                 394
       if(is segment){
          point3D<T> v2=p-p2;
          if(v.dot(v1)<=0)return v1.abs2();</pre>
                                                 397
         if(v.dot(v2)>=0)return v2.abs2();
       point3D<T> tmp=v.cross(v1);
       return tmp.abs2()/v.abs2();
     pair<point3D<T>,point3D<T> > closest pair(
          const line3D<T> &1)const{
       point3D<T> v1=(p1-p2), v2=(1.p1-l.p2);
                                                 400
       point3D<T> N=v1.cross(v2),ab(p1-l.p1);
       //if(N.abs2()==0)return NULL;平行或重合
```

```
T tmp=N.dot(ab),ans=tmp*tmp/N.abs2();//
            最折點對距離
       point3D<T> d1=p2-p1,d2=l.p2-l.p1,D=d1.
           cross(d2);
       T t1=((1.p1-p1).cross(d2)).dot(D)/D.abs2
       T t2=((1.p1-p1).cross(d1)).dot(D)/D.abs2
       return make_pair(p1+d1*t1,l.p1+d2*t2);
     bool same side(const point3D<T> &a,const
         point3D<T> &b)const{
       return (p2-p1).cross(a-p1).dot((p2-p1).
           cross(b-p1))>0;
   };
   template<typename T>
   struct plane{
     point3D<T> p0,n;//平面上的點和法向量
     plane(){}
     plane(const point3D<T> &p0,const point3D<T</pre>
         > &n):p0(p0),n(n){}
     T dis2(const point3D<T> &p)const{//點到平
          面距離的平方
       T tmp=(p-p0).dot(n);
       return tmp*tmp/n.abs2();
     point3D<T> projection(const point3D<T> &p)
       return p-n*(p-p0).dot(n)/n.abs2();
     point3D<T> line intersection(const line3D<
         T> &1)const{
       T tmp=n.dot(1.p2-1.p1);//等於0表示平行或
            重合該平面
       return 1.p1+(1.p2-1.p1)*(n.dot(p0-1.p1)/
           tmp);
     line3D<T> plane_intersection(const plane &
         pl)const{
       point3D<T> e=n.cross(pl.n),v=n.cross(e);
       T tmp=pl.n.dot(v);//等於0表示平行或重合
       point3D<T> q=p0+(v*(pl.n.dot(pl.p0-p0))/
           tmp);
       return line3D<T>(q,q+e);
   template<typename T>
   struct triangle3D{
     point3D<T> a,b,c;
     triangle3D(){}
     triangle3D(const point3D<T> &a,const
         point3D<T> &b,const point3D<T> &c):a(a
          ),b(b),c(c){}
     bool point_in(const point3D<T> &p)const{//
          點在該平面上的投影在三角形中
       return line3D<T>(b,c).same_side(p,a)&&
           line3D<T>(a,c).same_side(p,b)&&
           line3D<T>(a,b).same side(p,c);
402 template<typename T>
403 struct tetrahedron{//四面體
```

sort(pt.begin(),pt.end(),point\_cmp);

```
point3D<T> a,b,c,d;
                                                           pt.resize(unique(pt.begin(),pt.end())-pt 10 | Circle TwoPointCircle(Circle::cp &a, Circle
                                                                                                                                                              for(int i=1;i<=r;++i)</pre>
                                                  455
     tetrahedron(){}
                                                                                                                                                                if((v[i].x-v[mid].x)*(v[i].x-v[mid].x)
                                                                .begin());
                                                                                                               ::cp &b) {
                                                                                                              Circle::p m=(a+b)/2;
     tetrahedron(const point3D<T> &a,const
                                                           for(size t i=2;i<pt.size();++i){</pre>
                                                                                                                                                                      dis)t.push back(v[i]);
406
                                                  456
                                                             if((pt[0]-pt[i]).area2(pt[1]-pt[i])
                                                                                                              return (Circle){m,(a-m).abs2()};
          point3D<T> &b, const point3D<T> &c,
                                                                                                      12
                                                                                                                                                               sort(t.begin(),t.end(),point<T>::y cmp);//
          const point3D<T> &d):a(a),b(b),c(c),d(
                                                                  !=0){
                                                                                                      13 }
                                                                                                                                                                    如果用merge sort的方式可以O(n)
          d){}
                                                               ok=true;
                                                                                                      14
                                                                                                                                                              for(int i=0;i<(int)t.size();++i)</pre>
                                                  459
                                                               swap(pt[i],pt[2]);
                                                                                                         Circle outcircle(Circle::p a, Circle::p b,
                                                                                                                                                                 for(int j=1;j<=3&&i+j<(int)t.size();++j)</pre>
     T volume6()const{//體積的六倍
                                                               break;
                                                                                                              Circle::p c) {
       return (d-a).dot((b-a).cross(c-a));
                                                  460
                                                                                                                                                                   if((tmd=(t[i]-t[i+j]).abs2())<dis)dis=</pre>
408
                                                  461
                                                                                                              if(TwoPointCircle(a,b).incircle(c))
409
                                                                                                                   return TwoPointCircle(a,b);
                                                  462
     point3D<T> centroid()const{
                                                                                                                                                              return dis;
410
                                                  463
                                                           if(!ok)return;
                                                                                                      17
                                                                                                              if(TwoPointCircle(b,c).incircle(a))
       return (a+b+c+d)/4;
                                                                                                                                                          17 }
411
                                                          ok=false:
                                                                                                                   return TwoPointCircle(b,c);
                                                  464
412
                                                                                                                                                            template<typename T>
                                                           for(size t i=3;i<pt.size();++i){</pre>
                                                                                                              if(TwoPointCircle(c,a).incircle(b))
     bool point in(const point3D<T> &p)const{
                                                                                                                                                            inline T closest pair(vector<point<T> > &v){
413
       return triangle3D<T>(a,b,c).point in(p)
                                                            if(tetrahedron<T>(pt[0],pt[1],pt[2],pt
                                                                                                                   return TwoPointCircle(c.a):
414
                                                                                                                                                              vector<point<T> >t:
                                                                  [i]).volume6()!=0){
                                                                                                      19
                                                                                                              Circle::p ret:
                                                                                                                                                               sort(v.begin(),v.end(),point<T>::x_cmp);
            &&triangle3D<T>(c,d,a).point_in(p);
                                                               ok=true;
                                                                                                      20
                                                                                                              double a1=b.x-a.x, b1=b.y-a.y, c1=(a1*a1
                                                                                                                                                              return closest pair(v,t,0,v.size()-1);//最
415
                                                               swap(pt[i],pt[3]);
                                                                                                                   +b1*b1)/2:
                                                  468
416 };
                                                                                                                                                                    近點對距離
                                                                                                              double a2=c.x-a.x, b2=c.y-a.y, c2=(a2*a2 23 3
                                                  469
                                                               break:
                                                                                                      21
   template<typename T>
                                                  470
                                                                                                                   +b2*b2)/2:
   struct convexhull3D{
                                                                                                              double d = a1*b2 - a2*b1:
     static const int MAXN=105;
                                                  471
                                                                                                      22
                                                  472
                                                           if(!ok)return;
                                                                                                              ret.x=a.x+(c1*b2-c2*b1)/d;
420
     struct face{
                                                           for(int i=0;i<4;++i)AddFace(i,(i+1)%4,(i</pre>
                                                                                                              ret.y=a.y+(a1*c2-a2*c1)/d;
                                                  473
                                                                                                      24
421
       int a,b,c;
                                                                +2)\%4,(i+3)\%4);
                                                                                                              return (Circle){ret,(ret-a).abs2()};
422
       bool use;
                                                           for(size_t i=4;i<pt.size();++i){</pre>
                                                                                                      26 }
                                                  474
423
       face(){}
                                                             for(int j=fc.size()-1;j>=0;--j){
                                                  475
                                                                                                      27 //rand required
424
       face(int a,int b,int c):a(a),b(b),c(c),
                                                               if(outside(i,j)){
                                                                                                         Circle SmallestCircle(std::vector<Circle::p>
            use(1){}
                                                                 dfs(i,j);
                                                  477
                                                                                                               &p){
     };
                                                                                                                                                              double d:
                                                  478
                                                                 break;
                                                                                                      29
                                                                                                              int n=p.size();
426
     vector<point3D<T> > pt;
                                                                                                              if(n==1) return (Circle){p[0],0.0};
                                                  479
                                                                                                      30
     vector<face> fc;
427
                                                  480
                                                                                                      31
                                                                                                              if(n==2) return TwoPointCircle(p[0],p
428
     int fid[MAXN][MAXN];
                                                                                                                   [1]);
     static bool point cmp(const point3D<T> &a, 481
429
                                                           size t sz=0;
                                                                                                              random_shuffle(p.begin(),p.end());
          const point3D<T> &b){
                                                           for(size t i=0;i<fc.size();++i)if(fc[i].</pre>
                                                                                                              Circle c = \{p[0], 0.0\};
                                                                                                      33
       return a.x < b.x | |(a.x == b.x & (a.v < b.v)| |(a. 483)|
430
                                                               use)fc[sz++]=fc[i];
                                                                                                              for(int i=0;i<n;++i){</pre>
            v==b.v&&a.z<b.z)));
                                                          fc.resize(sz);
                                                                                                      35
                                                                                                                  if(c.incircle(p[i])) continue;
431
                                                                                                                  c=Circle{p[i],0.0};
                                                                                                      36
432
     bool outside(int p,int a,int b,int c)const 485
                                                         point3D<T> centroid()const{
                                                                                                      37
                                                                                                                  for(int j=0;j<i;++j){</pre>
                                                          point3D<T> res(0,0,0);
       return tetrahedron<T>(pt[a],pt[b],pt[c], 487
                                                                                                      38
                                                                                                                      if(c.incircle(p[j])) continue;
433
                                                                                                                      c=TwoPointCircle(p[i],p[j]);
                                                          T vol=0:
                                                                                                      39
            pt[p]).volume6()<0;</pre>
                                                           for(size_t i=0;i<fc.size();++i){</pre>
                                                                                                                      for(int k=0;k<j;++k){</pre>
                                                  489
                                                                                                       40
434
                                                            T tmp=pt[fc[i].a].dot(pt[fc[i].b].
                                                                                                                          if(c.incircle(p[k]))
                                                  490
     bool outside(int p,int f)const{return
435
                                                                  cross(pt[fc[i].c]));
                                                                                                                               continue;
          outside(p,fc[f].a,fc[f].b,fc[f].c);}
                                                             res=res+(pt[fc[i].a]+pt[fc[i].b]+pt[fc 42
                                                                                                                          c=outcircle(p[i],p[j],p[k]);
     void AddFace(int a,int b,int c,int p){
436
                                                                  [i].c])*tmp;
437
       if(outside(p,a,b,c))fid[c][b]=fid[b][a]=
                                                                                                      43
                                                             vol+=tmp;
            fid[a][c]=fc.size(),fc.push_back(
                                                  492
                                                                                                      44
                                                                                                                  }
                                                                                                       45
             face(c,b,a));
                                                          return res/(vol*4);
                                                                                                              return c;
       else fid[a][b]=fid[b][c]=fid[c][a]=fc.
                                                  494
                                                                                                       46
438
            size(),fc.push_back(face(a,b,c));
                                                  496 };
439
     bool dfs(int p,int f){
440
441
       if(!fc[f].use)return true;
                                                                                                                最近點對.cpp
       if(outside(p,f)){
442
443
         int a=fc[f].a,b=fc[f].b,c=fc[f].c;
                                                      1.2 SmallestCircle.cpp
                                                                                                                                                          1 | #define MAXN 4100
         fc[f].use=false;
444
                                                                                                       1 | #define INF LLONG MAX
445
         if(!dfs(p,fid[b][a]))AddFace(p,a,b,c);
                                                                                                       1 template<typename T>
         if(!dfs(p,fid[c][b]))AddFace(p,b,c,a);
446
                                                                                                                                                           4 struct DLX{
                                                    1 | #include "Geometry.cpp"
                                                                                                       3 T closest pair(vector<point<T> >&v, vector<</pre>
         if(!dfs(p,fid[a][c]))AddFace(p,c,a,b);
447
                                                    2 struct Circle{
                                                                                                              point<T> >&t,int 1,int r){
         return true;
448
                                                           typedef point<double> p;
                                                                                                           T dis=INF, tmd;
       }else return false;
449
                                                           typedef const point<double> cp:
                                                                                                           if(l>=r)return dis:
450
                                                                                                                                                                    列跟行
     void build(){
                                                          p x;
                                                                                                           int mid=(1+r)/2;
451
       bool ok=false;
                                                           double r2;
                                                                                                           if((tmd=closest pair(v,t,l,mid))<dis)dis=</pre>
452
                                                          bool incircle(cp &c)const{return (x-c).
       fc.clear();
453
```

abs2()<=r2;}

8 };

### 1.4 浮點數誤差模板.cpp

```
1 const double EPS=1e-9:
 struct Double{
    Double(double d=0):d(d){}
    bool operator <(const Double &b)const{</pre>
         return d-b.d<-EPS;}</pre>
    bool operator >(const Double &b)const{
         return d-b.d>EPS;}
    bool operator ==(const Double &b)const{
         return fabs(d-b.d)<=EPS:}</pre>
    bool operator !=(const Double &b)const{
         return fabs(d-b.d)>EPS:}
    bool operator <=(const Double &b)const{</pre>
         return d-b.d<=EPS;}</pre>
   bool operator >=(const Double &b)const{
         return d-b.d>=-EPS;}
   operator double()const{return d;}
```

## Data Structure

#### 2.1 DLX.cpp

if((tmd=closest pair(v,t,mid+1,r))<dis)dis</pre>

=tmd;

t.clear();

```
2 #define MAXM 1030
3 #define MAXND 16390
   int n,m,sz,ansd;//高是n、寬是m的稀疏矩陣
   int S[MAXM],H[MAXN];
    int row[MAXND], col[MAXND]; //每個節點代表的
    int L[MAXND],R[MAXND],U[MAXND],D[MAXND];
   vector<int> ans,anst;
   void init(int n,int m){
     n = n, m = m;
      for(int i=0;i<=m;++i){</pre>
```

```
U[i]=D[i]=i,L[i]=i-1,R[i]=i+1;
                                                      restore(c);
14
        S[i]=0;
                                                66
15
                                                67
                                                      return 0;
16
      R[m]=0,L[0]=m;
                                                68
17
      sz=m, ansd=INT MAX; //ansd存最優解的個數
                                                69
                                                     void dfs2(int d){//for最小重複覆蓋問題
      for(int i=1;i<=n;++i)H[i]=-1;</pre>
                                                70
                                                      if(d+h()>=ansd)return;
18
                                                      if(!R[0]){ansd=d;ans=anst;return;}
19
                                                71
                                                      int c=R[0];
20
    void add(int r,int c){
                                                72
                                                      DFOR(i,R,0)if(S[i]<S[c])c=i;</pre>
21
      ++S[col[++sz]=c];
                                                73
                                                      DFOR(i,D,c){
22
      row[sz]=r;
                                                74
23
      D[sz]=D[c],U[D[c]]=sz,U[sz]=c,D[c]=sz;
                                                        anst.push back(row[i]);
24
      if(H[r]<0)H[r]=L[sz]=R[sz]=sz;
                                                        remove2(i);
25
      else R[sz]=R[H[r]],L[R[H[r]]]=sz,L[sz]=H
                                               77
                                                        DFOR(j,R,i)remove2(j),--S[col[j]];
           [r],R[H[r]]=sz;
                                                        dfs2(d+1):
                                                        anst.pop_back();
26
    #define DFOR(i,A,s) for(int i=A[s];i!=s;i= 80
                                                        DFOR(j,L,i)restore2(j),++S[col[j]];
27
         A[i])
                                                        restore2(i);
    void remove(int c){//刪除第c行和所有當前覆
                                               82
         蓋到第c行的列
                                                    bool exact cover(){//解精確覆蓋問題
                                                84
29
      L[R[c]]=L[c],R[L[c]]=R[c];//這裡刪除第c
                                                      ans.clear();//答案
           行,若有些行不需要處理可以在開始時呼 85
                                                      return dfs(0):
      DFOR(i,D,c)DFOR(i,R,i)\{U[D[i]]=U[i],D[U[i],D[U[i]]\}
                                                    void min cover(){//解最小重複覆蓋問題
           i]]=D[i],--S[col[i]];}
                                                      anst.clear();//暫存用,答案還是存在ans裡
31
                                                      dfs2(0);
                                                90
    void restore(int c){//恢復第c行和所有當前
32
                                                91
         覆蓋到第c行的列,remove的逆操作
                                                    #undef DFOR
      DFOR(i,U,c)DFOR(j,L,i){++S[col[j]],U[D[j
33
                                                93 };
           ]]=j,D[U[j]]=j;}
      L[R[c]]=c,R[L[c]]=c;
34
35
    void remove2(int nd){//刪除nd所在的行當前
                                                  2.2 Dynamic KD tree.cpp
         所有點(包括虛擬節點),只保留nd
      DFOR(i,D,nd)L[R[i]]=L[i],R[L[i]]=R[i];
37
38
                                                 1 | template < typename T, size t kd>//有kd個維度
    void restore2(int nd){//刪除nd所在的行當前
39
                                                   class kd tree{
         所有點,為remove2的逆操作
                                                    public:
      DFOR(i,U,nd)L[R[i]]=R[L[i]]=i;
40
                                                      struct point{
41
                                                        T d[kd]:
    bool vis[MAXM];
                                                        T dist(const point &x)const{
    int h(){//估價函數 for IDA*
43
                                                          T ret=0;
      int res=0;
                                                           for(size t i=0:i<kd:++i)ret+=std::</pre>
44
45
      memset(vis,0,sizeof(vis));
                                                               abs(d[i]-x.d[i]);
46
      DFOR(i,R,0)if(!vis[i]){
                                                           return ret;
47
        vis[i]=1;
                                                10
48
        ++res;
                                                        bool operator==(const point &p){
                                                11
        DFOR(j,D,i)DFOR(k,R,j)vis[col[k]]=1;
49
                                                          for(size_t i=0;i<kd;++i)</pre>
                                                            if(d[i]!=p.d[i])return 0;
50
                                                13
      return res;
                                                14
                                                           return 1;
52
                                                15
                                                        bool operator<(const point &b)const{</pre>
    bool dfs(int d){//for精確覆蓋問題
                                                16
                                                           return d[0] < b.d[0];</pre>
      if(d+h()>=ansd)return 0;//找最佳解用,找
           任意解可以刪掉
                                                      };
                                                19
55
      if(!R[0]){ansd=d;return 1;}
                                                20
                                                     private:
56
      int c=R[0];
                                                      struct node{
57
      DFOR(i,R,0)if(S[i]<S[c])c=i;</pre>
                                                        node *1,*r;
58
      remove(c);
                                                        point pid;
                                                23
59
      DFOR(i,D,c){
                                                24
60
        ans.push_back(row[i]);
                                                25
                                                        node(const point &p):1(0),r(0),pid(p),
        DFOR(j,R,i)remove(col[j]);
61
                                                             s(1){}
62
        if(dfs(d+1))return 1;
                                                26
                                                        ~node(){delete 1,delete r;}
        ans.pop back();
63
                                                        void up()\{s=(1?1->s:0)+1+(r?r->s:0);\}
                                                27
        DFOR(j,L,i)restore(col[j]);
```

```
const double alpha,loga;
const T INF: //記得要給 INF,表示極大值
                                            86
int maxn;
                                            87
struct __cmp{
                                            88
  int sort id;
  bool operator()(const node*x,const
       node*y)const{
                                            90
    return operator()(x->pid,y->pid);
                                            91
  bool operator()(const point &x,const
                                            94
       point &y)const{
    if(x.d[sort_id]!=y.d[sort_id])
                                            95
      return x.d[sort_id]<y.d[sort_id];</pre>
                                            96
    for(size t i=0:i<kd:++i)</pre>
      if(x.d[i]!=y.d[i])return x.d[i]<y.</pre>
           d[i];
                                            99
    return 0;
                                            100
                                           101
}cmp:
int size(node *o){return o?o->s:0;}
                                            102
                                            103
std::vector<node*> A;
node* build(int k,int l,int r){
                                            104
 if(1>r)return 0;
                                            105
                                            106
  if(k==kd)k=0;
                                            107
  int mid=(1+r)/2;
                                            108
  cmp.sort id=k;
  std::nth element(A.begin()+1,A.begin() 109
                                            110
       +mid, A. begin()+r+1, cmp);
  node *ret=A[mid];
                                           111
  ret->l=build(k+1,1,mid-1);
                                           112
                                           113
  ret->r=build(k+1,mid+1,r);
                                           114
  ret->up();
                                           115
  return ret:
                                           116
bool isbad(node*o){
  return size(o->1)>alpha*o->s||size(o-> 117
       r)>alpha*o->s;
                                           118
                                            119
                                            120
void flatten(node *u,typename std::
     vector<node*>::iterator &it){
                                            121
                                            122
  if(!u)return:
                                            123
  flatten(u->1,it);
                                            124
                                            125
  flatten(u->r,++it);
                                            126
void rebuild(node*&u.int k){
  if((int)A.size()<u->s)A.resize(u->s);
  typename std::vector<node*>::iterator
       it=A.begin():
                                            128
                                            129
  flatten(u,it);
                                            130
  u=build(k,0,u->s-1);
                                            131
bool insert(node*&u,int k,const point &x 132
     ,int dep){
                                            133
  if(!u){
                                            134
    u=new node(x);
                                            135
    return dep<=0;</pre>
                                            136
  ++u->s;
                                            137
                                            138
  cmp.sort id=k:
  if(insert(cmp(x,u->pid)?u->1:u->r,(k
                                           139
       +1)%kd,x,dep-1)){
                                            140
                                            141
    if(!isbad(u))return 1;
                                            142
    rebuild(u,k);
                                           143
```

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82

```
return 0;
node *findmin(node*o,int k){
  if(!o)return 0;
  if(cmp.sort id==k)return o->l?findmin(
       o->1,(k+1)%kd):o;
  node *l=findmin(o->l,(k+1)%kd);
  node *r=findmin(o->r,(k+1)%kd);
  if(1&&!r)return cmp(1,0)?1:0;
  if(!1&&r)return cmp(r,o)?r:o;
  if(!1&&!r)return o;
  if(cmp(1,r))return cmp(1,o)?1:o:
  return cmp(r,o)?r:o;
bool erase(node *&u,int k,const point &x
  if(!u)return 0:
  if(u->pid==x){
    if(u->r);
    else if(u->1){
      u->r=u->1;
      u - > 1 = 0:
    }else{
      delete u:
      u=0:
      return 1;
    --11->5:
    cmp.sort id=k;
    u->pid=findmin(u->r,(k+1)%kd)->pid;
    return erase(u->r,(k+1)%kd,u->pid);
  cmp.sort id=k:
  if(erase(cmp(x,u->pid)?u->l:u->r,(k+1)
      %kd,x)){
    --u->s:return 1:
  }else return 0;
T heuristic(const T h[])const{
  T ret=0;
  for(size t i=0;i<kd;++i)ret+=h[i];</pre>
  return ret:
int aM:
std::priority_queue<std::pair<T,point >
void nearest(node *u,int k,const point &
    x,T *h,T &mndist){
  if(u==0||heuristic(h)>=mndist)return;
  T dist=u->pid.dist(x),old=h[k];
  /*mndist=std::min(mndist,dist);*/
  if(dist<mndist){</pre>
    pQ.push(std::make pair(dist,u->pid))
    if((int)pQ.size()==qM+1)
      mndist=pQ.top().first,pQ.pop();
  if(x.d[k]<u->pid.d[k]){
    nearest(u->1,(k+1)\%kd,x,h,mndist);
    h[k]=std::abs(x.d[k]-u->pid.d[k]);
    nearest(u->r,(k+1)%kd,x,h,mndist);
  }else{
    nearest(u->r,(k+1)%kd,x,h,mndist);
    h[k]=std::abs(x.d[k]-u->pid.d[k]);
    nearest(u->1,(k+1)%kd,x,h,mndist);
```

h[k]=old;

node(int 1,int r,int d):1(1),r(r),data(d)

```
146
                                                                                                                                                             {}
       std::vector<point>in range;
147
                                                                                                  void update(node *u, const point &x, int data,
                                                                                                                                                      };
                                                  1 | /*kd樹代替高維線段樹*/
       void range(node *u,int k,const point&mi,
                                                                                                          int k=0){
                                                                                                                                                      vector<node> nds;
            const point&ma){
                                                                                                                                                      inline void up(int o,int l,int r){
                                                   struct node{
                                                                                                       if(!u)return;
         if(!u)return;
                                                                                                                                                        nds[o].data=nds[1].data+nds[r].data;
149
                                                      node *1.*r:
                                                                                                  57
                                                                                                       u->down();
150
         bool is=1:
                                                      point pid, mi, ma;
                                                                                                       if(u->pid==x){
         for(int i=0;i<kd;++i)</pre>
                                                      int s;
                                                                                                                                                      inline int new node(int l,int r,int d){
151
                                                                                                         u->data=data;
           if(u->pid.d[i]<mi.d[i]||ma.d[i]<u->
                                                                                                                                                        nds.push back(node(1,r,d));
152
                                                      int data:
                                                                                                         u->up2();
                pid.d[i]){
                                                                                                                                                        return nds.size()-1;
                                                      node(const point &p,int d):1(0),r(0),pid(p
                                                                                                                                                   14
                                                                                                         return:
             is=0; break;
                                                           ),mi(p),ma(p),s(1),data(d),dmin(d),
                                                                                                                                                   15
153
                                                                                                                                                      inline int new node(const node &nd){
154
                                                           dmax(d){}
                                                                                                       cmp.sort id=k;
         if(is)in_range.push_back(u->pid);
                                                                                                                                                        nds.push back(nd);
155
                                                      void up(){
                                                                                                  64
                                                                                                       update(cmp(x,u->pid)?u->l:u->r,x,data,(k
156
         if(mi.d[k]<=u->pid.d[k])range(u->1.(k
                                                        mi=ma=pid:
                                                                                                                                                        return nds.size()-1;
                                                                                                            +1)%kd);
              +1)%kd,mi,ma);
                                                        s=1;
                                                                                                                                                   19
                                                  10
                                                                                                       u->up2();
         if(ma.d[k]>=u->pid.d[k])range(u->r,(k
                                                        if(1){
                                                                                                                                                   20
                                                                                                                                                      int build tree(int 1,int r){
157
                                                 11
                                                                                                  66
              +1)%kd.mi.ma);
                                                                                                                                                        int nd=new node(-1,-1,0);
                                                          for(int i=0;i<kd;++i){</pre>
                                                                                                                                                   21
                                                 12
                                                                                                  67
                                                                                                                                                        if(l==r)return nd;
158
                                                 13
                                                            mi.d[i]=min(mi.d[i],1->mi.d[i]);
                                                                                                                                                   22
                                                                                                  68 / *區間修改*/
     public:
                                                                                                                                                        int mid=(1+r)/2;
                                                            ma.d[i]=max(ma.d[i],1->ma.d[i]);
159
                                                 14
                                                                                                     void update(node *o,const point &L,const
       kd tree(const T &INF, double a=0.75):root
160
                                                                                                                                                        int L=build_tree(l,mid);//執行時vector會被
                                                                                                          point &R.int data){
            (0),alpha(a),loga(log2(1.0/a)),INF(
                                                 16
                                                          s+=1->s;
                                                                                                       if(!o)return;
            INF).maxn(1){}
                                                 17
                                                                                                  71
                                                                                                       o->down();
                                                                                                                                                        int R=build tree(mid+1,r)://一定要這樣寫
161
       ~kd tree(){delete root:}
                                                        if(r){
                                                 18
                                                                                                       if(range in range(o,L,R)){
                                                                                                                                                        nds[nd].l=L;
162
       void clear(){delete root,root=0,maxn=1;}
                                                          for(int i=0;i<kd;++i){</pre>
                                                                                                  73
                                                                                                         //區間懶惰標記修改
                                                                                                                                                   27
                                                                                                                                                        nds[nd].r=R;
       void build(int n,const point *p){
                                                            mi.d[i]=min(mi.d[i],r->mi.d[i]);
163
                                                 20
                                                                                                         o->down();
                                                                                                                                                        //up(nd.L.R):
                                                                                                  74
         delete root.A.resize(maxn=n);
                                                            ma.d[i]=max(ma.d[i],r->ma.d[i]);
164
                                                                                                  75
                                                                                                                                                        return nd;
                                                                                                         return;
                                                                                                                                                   29
         for(int i=0;i<n;++i)A[i]=new node(p[i</pre>
165
                                                 22
                                                                                                  76
              1);
                                                 23
                                                          s+=r->s;
                                                                                                                                                      int insert(int l,int r,int rt,int x,int d){
                                                                                                  77
                                                                                                       if(point in range(o,L,R)){
         root=build(0,0,n-1);
166
                                                 24
                                                                                                         //這個點在(L,R)區間·但是他的左右子樹不
                                                                                                                                                        if(x<1||r<x)return rt;</pre>
                                                 25
167
                                                                                                                                                        int nd=new node(nds[rt]);
                                                                                                                                                   33
                                                                                                              一定在區間中
168
       void insert(const point &x){
                                                      void up2(){
                                                                                                                                                   34
                                                                                                                                                        if(l==r&&l==x)nds[nd].data+=d;
                                                                                                         //單點懶惰標記修改
         insert(root,0,x,__lg(size(root))/loga)
                                                                                                  79
169
                                                        //其他懶惰標記向上更新
                                                                                                                                                   35
                                                                                                                                                        else{
                                                                                                  80
                                                 28
                                                                                                                                                          int mid=(1+r)/2:
                                                                                                       if(o->1&&range include(o->1,L,R))update(o
         if(root->s>maxn)maxn=root->s;
170
                                                 29
                                                      void down(){
                                                                                                                                                          int L=insert(1,mid,nds[nd].1,x,d);
                                                                                                            ->1,L,R,data);
171
                                                        //其他懶惰標記下推
                                                                                                                                                          int R=insert(mid+1,r,nds[nd].r,x,d);
                                                 30
                                                                                                       if(o->r&&range include(o->r,L,R))update(o
       bool erase(const point &p){
172
                                                 31
                                                                                                                                                          nds[nd].l=L:
                                                                                                            ->r,L,R,data);
173
         bool d=erase(root,0,p);
                                                                                                                                                          nds[nd].r=R;
                                                 32
                                                    }*root:
                                                                                                                                                   40
         if(root&&root->s<alpha*maxn)rebuild();</pre>
                                                                                                       o->up2();
174
                                                                                                  83
                                                                                                                                                   41
                                                                                                                                                          up(nd,L,R);
175
         return d:
                                                                                                  84
                                                    /*檢查區間包含用的函數*/
                                                                                                                                                   42
                                                                                                  85
176
                                                 inline bool range_include(node *o,const
                                                                                                                                                   13
                                                                                                                                                        return nd;
       void rebuild(){
177
                                                                                                     /*區間查詢,以總和為例*/
                                                         point &L, const point &R){
         if(root)rebuild(root,0);
178
                                                                                                     int query(node *o,const point &L,const point
                                                                                                                                                      inline int cal(int L,int R){
                                                      for(int i=0;i<kd;++i){</pre>
         maxn=root->s;
179
                                                                                                           &R){
                                                        if(L.d[i]>o->ma.d[i]||R.d[i]<o->mi.d[i])
                                                                                                                                                   46
                                                                                                                                                        return nds[R].data-nds[L].data;
                                                                                                       if(!o)return 0;
180
                                                                                                                                                   47
                                                             return 0:
       T nearest(const point &x,int k){
181
                                                                                                       o->down();
                                                                                                                                                      int find(int 1,int r,int L,int R,int k){
                                                      }//只要(L,R)區間有和o的區間有交集就回傳
182
         qM=k;
                                                                                                       if(range in range(o,L,R))return o->sum;
                                                                                                                                                        if(l==r)return 1;
                                                                                                                                                   49
                                                           true
         T mndist=INF,h[kd]={};
183
                                                                                                       int ans=0;
                                                                                                                                                   50
                                                                                                                                                        int mid=(1+r)/2:
                                                      return 1;
         nearest(root,0,x,h,mndist);
                                                 39
184
                                                                                                       if(point in range(o,L,R))ans+=o->data;
                                                                                                                                                        int add=cal(nds[L].1,nds[R].1);
                                                 40
         mndist=pQ.top().first;
185
                                                                                                       if(o->l&&range include(o->l,L,R))ans+=
                                                                                                                                                        if(k<=add)return find(1,mid,nds[L].1,nds[R</pre>
                                                    inline bool range_in_range(node *o,const
186
         pQ=std::priority queue<std::pair<T,
                                                                                                            query(o->1,L,R);
                                                                                                                                                             ].1,k);
                                                         point &L, const point &R){
                                                                                                       if(o->r&&range include(o->r,L,R))ans+=
              point > >();
                                                                                                                                                        return find(mid+1,r,nds[L].r,nds[R].r,k-
                                                      for(int i=0:i<kd:++i){</pre>
                                                                                                            querv(o->r,L,R);
187
         return mndist;//回傳離x第k近的點的距離
                                                                                                                                                             add):
                                                        if(L.d[i]>o->mi.d[i]||o->ma.d[i]>R.d[i])
                                                                                                       return ans;
188
                                                                                                                                                   54
       const std::vector<point> &range(const
189
                                                                                                                                                   55
                                                                                                                                                      int n,m;
                                                      }//如果(L,R)區間完全包含o的區間就回傳true
                                                 44
            point&mi,const point&ma){
                                                                                                                                                      int s[100005];
                                                      return 1:
                                                 45
         in range.clear();
190
                                                                                                                                                      int root[100005];
                                                 46 }
         range(root,0,mi,ma);
191
                                                                                                                                                      int main(){
                                                    inline bool point_in_range(node *o,const
192
         return in range;//回傳介於mi到ma之間的
                                                                                                                                                        while(~scanf("%d%d",&n,&m)){
                                                                                                     2.4 persistent segment tree.com
                                                         point &L, const point &R){
              點vector
                                                                                                                                                          nds.clear();
                                                      for(int i=0;i<kd;++i){</pre>
                                                                                                                                                          vector<int> lsh;
193
                                                        if(L.d[i]>o->pid.d[i]||R.d[i]<o->pid.d[i
       int size(){return root?root->s:0;}
                                                                                                                                                          for(int i=1;i<=n;++i){</pre>
194
                                                             ])return 0;
                                                                                                   1 #include <bits/stdc++.h>//POJ 2104
                                                                                                                                                            scanf("%d",&s[i]);
195 };
                                                      }//如果(L,R)區間完全包含o->pid這個點就回傳
                                                                                                   using namespace std;
                                                                                                                                                   64
                                                                                                                                                            lsh.push back(s[i]);
                                                                                                   3 struct node{
                                                      return 1;
                                                                                                       int 1,r;
                                                 51
                                                                                                                                                          sort(lsh.begin(),lsh.end());
                                                                                                       int data;
```

2.3 kd tree replace segment 53

```
lsh.resize(unique(lsh.begin(),lsh.end()) 30|
                                                       return b:
            -lsh.begin());
                                                31
       int N=(int)lsh.size()-1;
                                                32 }
68
       root[0]=build tree(0,N);
69
       for(int i=1;i<=n;++i){</pre>
70
        s[i]=lower bound(lsh.begin(),lsh.end()
              ,s[i])-lsh.begin();
                                                   2.7 操作分治.cpp
        root[i]=insert(0,N,root[i-1],s[i],1);
72
73
74
       while(m--){
75
        int a,b,k;
                                                 1 | void dg(int 1,int r){
         scanf("%d%d%d",&a,&b,&k);
76
                                                     if(l==r)return;
        int res=find(0,N,root[a-1],root[b],k);
                                                     int mid=(1+r)/2;
        printf("%d\n",lsh[res]);
                                                     dq(l,mid);
79
                                                      處理[1,mid]的操作對[mid+1,r]的影響
80
                                                     dq(mid+1,r);
    return 0:
```

#### skew heap.cpp

```
1 | node *merge(node *a, node *b){
   if(!a||!b)return a?a:b;
   if(b->data<a->data)swap(a,b);
   swap(a->1.a->r):
   a->l=merge(b,a->l);
   return a;
```

#### 2.6 split merge.cpp

**if**(!o)a=b=0:

b->up();

```
else{
      //o=new node(*o);
      o->down();
       if(k<=size(o->1)){
        b=o:
        split(o->1,a,b->1,k);
      }else{
         split(o->r,a->r,b,k-size(o->l)-1);
12
13
      o->up();
14
15
   node *merge(node *a,node *b){
    if(!a||!b)return a?a:b;
    static int x;
    if(x++%(a->s+b->s)<a->s){
      //a=new node(*a);
      a->down();
      a->r=merge(a->r,b);
      a->up();
       return a;
    }else{
      //b=new node(*b);
      b->down();
      b->1=merge(a,b->1);
```

# 2.8 整體二分.cpp

```
1 void BS(int 1,int r,vector<Item> &vs){
                                                   //答案該<//>
(1.會有的已經做完了
                                                   if(l==r)整個vs的答案=1;//??????
                                                   int mid=(1+r)/2;
                                                   do_thing(1, mid); // 做答案 <= mid 會做的事
                                                   vector<Item> left=vs裡滿足的:
                                                   vector<Item> right=vs-left;
                                                   undo thing(l,mid);
                                                   BS(1,mid,left);
                                                   do thing(1,mid);
                                               10
                                                   BS(mid+1,r,right);//??????
                                               11
1 void split(node *o, node *&a, node *&b, int k){ 12 }
```

#### default

### 3.1 debug.cpp

```
1 | #ifdef DEBUG
2 #define dbg(...) {\
    fprintf(stderr, "%s - %d : (%s) = ",
         __PRETTY_FUNCTION__,_LINE__,#
           _VA_ARGS__);\
    _DO(__VA_ARGS__);\
6 template<typename I> void _DO(I&&x){cerr<<x</pre>
       <<end1;}
7 template<typename I, typename...T> void _DO(I
       &&x,T&&...tail){cerr<<x<<", ";_DO(tail
       ...);}
8 #else
9 #define dbg(...)
10 #endif
```

#### 3.2 ext.cpp

```
1 #include < bits / extc++.h>
2 #include<ext/pd ds/assoc container.hpp>
3 #include<ext/pd ds/tree policy.hpp>
4 using namespace __gnu_cxx;
5 using namespace __gnu_pbds;
6 template<typename T>
vsing pbds set = tree<T,null type,less<T>,
       rb tree tag,
       tree order statistics node update>;
8 template<typename T, typename U>
9 using pbds map = tree<T,U,less<T>,
       rb tree tag,
       tree order statistics node update>:
using heap = __gnu_pbds::priority_queue<int</pre>
11 //s.find_by_order(1);//0 base
12 //s.order_of_key(1);
```

#### 3.3 IncStack.cpp

```
1 //Maaic
2 #pragma GCC optimize "Ofast"
3 //stack resize, change esp to rsp if 64-bit
       svstem
  asm("mov %0, \%%esp n" :: "g"(mem+1000000));
5 //linux stack resize
  #include<svs/resource.h>
  void increase stack(){
    const rlim t ks=64*1024*1024;
    struct rlimit rl:
    int res=getrlimit(RLIMIT_STACK,&rl);
    if(!res&&rl.rlim cur<ks){</pre>
12
       rl.rlim cur=ks;
       res=setrlimit(RLIMIT_STACK,&rl);
13
14
15 }
```

### 3.4 input.cpp

```
1 inline int read(){
   int x=0; bool f=0; char c=getchar();
    while(ch<'0'||'9'<ch)f|=ch=='-',ch=getchar
    while ('0' <= ch\&ch <= '9') x = x*10 - '0' + ch, ch =
         getchar();
    return f?-x:x;
7 volatile
8 // #!/bin/bash
9 // q++ -std=c++11 -02 -Wall -Wextra -Wno-
       unused-result -DDEBUG $1 && ./a.out
     -fsanitize=address -fsanitize=undefined
       -fsanitize=return
```

#### Flow

#### 4.1 dinic.cpp

```
1 template < typename T>
  struct DINIC{
    static const int MAXN=105;
    static const T INF=INT_MAX;
     int n://點數
     int level[MAXN], cur[MAXN];
     struct edge{
      int v.pre:
      T cap,flow,r;
       edge(int v,int pre,T cap):v(v),pre(pre),
           cap(cap),flow(0),r(cap){}
    int g[MAXN];
12
13
     vector<edge> e;
     void init(int n){
15
      memset(g,-1,sizeof(int)*((n= n)+1));
16
      e.clear();
17
    void add edge(int u,int v,T cap,bool
         directed=false){
      e.push_back(edge(v,g[u],cap));
19
      g[u]=e.size()-1;
20
      e.push_back(edge(u,g[v],directed?0:cap))
      g[v]=e.size()-1;
22
23
    int bfs(int s,int t){
24
25
      memset(level,0,sizeof(int)*(n+1));
26
      memcpy(cur,g,sizeof(int)*(n+1));
27
      queue<int >q;
28
      q.push(s);
29
       level[s]=1;
30
      while(q.size()){
        int u=q.front();q.pop();
31
32
         for(int i=g[u];~i;i=e[i].pre){
33
           if(!level[e[i].v]&&e[i].r){
34
             level[e[i].v]=level[u]+1;
35
             q.push(e[i].v);
36
             if(e[i].v==t)return 1;
37
38
39
40
      return 0;
    T dfs(int u, int t, T cur flow=INF){
      if(u==t)return cur flow;
44
      T df;
45
       for(int &i=cur[u];~i;i=e[i].pre){
        if(level[e[i].v]==level[u]+1&&e[i].r){
47
           if(df=dfs(e[i].v,t,min(cur flow,e[i
                ].r))){
             e[i].flow+=df;
49
             e[i^1].flow-=df;
             e[i].r-=df;
51
             e[i^1].r+=df;
52
             return df;
53
54
```

**if**(!--gap[d[u]])d[s]=n;

return true;

```
Graph
       return level[u]=0;
                                                         else ++gap[d[u]=++mh];
                                                                                                         void add_edge(int u,int v,_T cap,_T cost,
                                                         return cur flow-tf;
                                                                                                              bool directed=false){
57
                                                  43
58
    T dinic(int s,int t,bool clean=true){
                                                                                                           e.push_back(edge(v,g[u],cap,cost));
                                                  44
                                                                                                    20
                                                       T isap(int s,int t,bool clean=true){
59
       if(clean){
                                                  45
                                                                                                    21
                                                                                                           g[u]=e.size()-1;
                                                                                                                                                         5.1 Augmenting Path.cpp
60
         for(size t i=0;i<e.size();++i){</pre>
                                                         memset(d,0,sizeof(int)*(n+1));
                                                                                                           e.push_back(edge(u,g[v],directed?0:cap,-
                                                  46
                                                         memset(gap,0,sizeof(int)*(n+1));
           e[i].flow=0;
                                                  47
                                                                                                                cost));
                                                                                                           g[v]=e.size()-1;
62
           e[i].r=e[i].cap;
                                                  48
                                                         memcpy(cur,g,sizeof(int)*(n+1));
                                                                                                    23
                                                                                                                                                       1 | #define MAXN1 505
63
                                                         if(clean){
                                                  49
                                                                                                    ^{24}
                                                                                                                                                       2 #define MAXN2 505
                                                           for(size t i=0;i<e.size();++i){</pre>
64
                                                                                                    25
                                                                                                         T augment(int u, T cur flow){
                                                                                                                                                       3 int n1, n2; //n1 個點連向n2個點
65
       T ans=0, mf=0;
                                                             e[i].flow=0;
                                                                                                           if(u==T||!cur flow)return ans+=piS*
                                                  51
                                                                                                                                                         int match[MAXN2];//屬於n2的點匹配了哪個點
       while(bfs(s,t))while(mf=dfs(s,t))ans+=mf
                                                 52
                                                             e[i].r=e[i].cap;
                                                                                                                cur flow, cur flow;
                                                                                                                                                       5 vector<int > g[MAXN1];//圖
                                                                                                    27
                                                                                                           vis[u]=1:
                                                  53
                                                                                                           _T r=cur_flow,d;
for(int i=g[u];~i;i=e[i].pre){
                                                                                                                                                       6 bool vis[MAXN2];//是否走訪過
       return ans;
                                                                                                    28
67
                                                  54
                                                                                                                                                         bool dfs(int u){
68
                                                  55
                                                         T max flow=0:
                                                         for(gap[0]=n;d[s]<n;)max_flow+=dfs(s,s,t</pre>
                                                                                                                                                           for(size t i=0;i<g[u].size();++i){</pre>
69 };
                                                                                                             if(e[i].cap&&!e[i].cost&&!vis[e[i].v])
                                                                                                                                                             int v=g[u][i];
                                                                                                                                                             if(vis[v])continue;
                                                         return max flow:
                                                                                                               d=augment(e[i].v,min(r,e[i].cap));
                                                  57
                                                                                                    31
                                                                                                                                                             vis[v]=1;
                                                                                                               e[i].cap-=d;
                                                                                                                                                      11
                                                  58
                                                                                                    32
  4.2 ISAP with cut.cpp
                                                                                                               e[i^1].cap+=d;
                                                                                                                                                      12
                                                                                                                                                             if(match[v]==-1||dfs(match[v])){
                                                                                                    33
                                                       vector<int> cut e://最小割邊集
                                                                                                                                                               match[v]=u;
                                                                                                               if(!(r-=d))break;
                                                                                                                                                      13
                                                       bool vis[MAXN];
                                                                                                    34
                                                       void dfs_cut(int u){
                                                                                                    35
                                                                                                                                                      14
                                                                                                                                                               return 1;
1 template<typename T>
                                                                                                                                                      15
                                                                                                    36
                                                         vis[u]=1;//表示u屬於source的最小割集
                                                  62
   struct ISAP{
                                                                                                    37
                                                                                                           return cur flow-r;
                                                                                                                                                      16
                                                         for(int i=g[u];~i;i=e[i].pre){
                                                  63
    static const int MAXN=105;
                                                                                                                                                      17
                                                                                                                                                           return 0;
                                                                                                    38
                                                           if(e[i].flow<e[i].cap&&!vis[e[i].v])</pre>
                                                  64
    static const T INF=INT MAX;
                                                                                                         bool modlabel(){
                                                                                                                                                      18
                                                                                                    39
                                                                dfs_cut(e[i].v);
                                                                                                                                                         inline int max_match(){
    int n://點數
                                                                                                    40
                                                                                                           for(int u=0;u<=n;++u)dis[u]=INF;</pre>
                                                  65
    int d[MAXN],gap[MAXN],cur[MAXN];
                                                                                                                                                           int ans=0:
                                                                                                    41
                                                                                                           static deque<int>q;
                                                  66
                                                                                                                                                           memset(match, -1, sizeof(int)*n2);
    struct edge{
                                                                                                    42
                                                                                                           dis[T]=0,q.push back(T);
                                                  67
                                                       T min_cut(int s,int t){
                                                                                                                                                           for(int i=0;i<n1;++i){</pre>
       int v,pre;
                                                                                                    43
                                                                                                           while(q.size()){
                                                        T ans=isap(s,t);
                                                                                                                                                             memset(vis,0,sizeof(bool)*n2);
       T cap,flow,r;
                                                                                                    44
                                                                                                             int u=q.front();q.pop_front();
                                                         memset(vis,0,sizeof(bool)*(n+1));
       edge(int v,int pre,T cap):v(v),pre(pre),
                                                                                                    45
                                                                                                                                                      24
                                                                                                                                                             if(dfs(i))++ans:
                                                         dfs cut(s),cut e.clear();
            cap(cap),flow(0),r(cap){}
                                                                                                    46
                                                                                                             for(int i=g[u];~i;i=e[i].pre){
                                                                                                                                                      25
                                                         for(int u=0;u<=n;++u){</pre>
                                                  71
                                                                                                               if(e[i^1].cap&&(dt=dis[u]-e[i].cost)
                                                                                                                                                           return ans;
                                                  72
                                                           if(vis[u])for(int i=g[u];~i;i=e[i].pre
    int g[MAXN];
                                                                                                                    <dis[e[i].v]){
12
13
    vector<edge> e;
                                                                                                                 if((dis[e[i].v]=dt)<=dis[q.size()?</pre>
                                                             if(!vis[e[i].v])cut_e.push_back(i);
    void init(int n){
                                                                                                                      q.front():S]){
                                                  74
       memset(g, -1, sizeof(int)*((n=_n)+1));
15
                                                                                                                   q.push_front(e[i].v);
                                                  75
                                                                                                                                                         5.2 Augmenting Path multiple.c
16
       e.clear();
                                                                                                    50
                                                                                                                 }else q.push_back(e[i].v);
                                                  76
                                                         return ans;
17
                                                                                                    51
                                                  77
18
    void add_edge(int u,int v,T cap,bool
                                                                                                    52
                                                                                                            }
                                                  78 };
         directed=false){
                                                                                                    53
                                                                                                                                                       1 | #define MAXN1 1005
       e.push_back(edge(v,g[u],cap));
                                                                                                                                                       2 #define MAXN2 505
                                                                                                    54
                                                                                                           for(int u=0;u<=n;++u)</pre>
                                                                                                             for(int i=g[u];~i;i=e[i].pre)
                                                                                                    55
20
       g[u]=e.size()-1;
                                                                                                                                                       3 int n1, n2; //n1 個點 連向 n2 個點, 其中 n2 個點可以
       e.push_back(edge(u,g[v],directed?0:cap))
                                                                                                    56
                                                                                                               e[i].cost+=dis[e[i].v]-dis[u];
                                                                                                                                                              匹配很多邊
                                                          MinCostMaxFlow.cpp
                                                                                                           piS+=dis[S];
                                                                                                                                                       4 vector<int > g[MAXN1];// 

22
       g[v]=e.size()-1;
                                                                                                           return dis[S]<INF;</pre>
                                                                                                                                                       5 int c[MAXN2]; // 每個屬於 n2 點 最多可以接受幾條
23
                                                                                                    59
24
      dfs(int u,int s,int t,T cur_flow=INF){
                                                   1 | template < typename T>
                                                                                                    60
                                                                                                         T mincost(int s,int t){
                                                                                                                                                       6 | vector<int> match list[MAXN2];//每個屬於n2的
       if(u==t)return cur_flow;
                                                     struct MCMF{
                                                                                                    61
                                                                                                           S=s,T=t;
       T tf=cur flow,df;
                                                                                                                                                              點匹配了那些點
                                                       static const int MAXN=440;
26
                                                                                                    62
                                                                                                           piS=ans=0;
                                                       static const _T INF=9999999999;
                                                                                                           while(modlabel()){
                                                                                                                                                       7 bool vis[MAXN2];//是否走訪過
       for(int &i=cur[u];~i;i=e[i].pre){
                                                                                                             do memset(vis,0,sizeof(bool)*(n+1));
                                                                                                                                                        | bool dfs(int u){
         if(e[i].r&&d[u]==d[e[i].v]+1){
28
                                                       struct edge{
                                                                                                    64
           df=dfs(e[i].v,s,t,min(tf,e[i].r));
                                                                                                    65
                                                                                                             while(augment(S,INF));
                                                                                                                                                           for(size t i=0;i<g[u].size();++i){</pre>
29
                                                         int v,pre;
30
           e[i].flow+=df;
                                                         _T cap,cost;
                                                                                                                                                             int v=g[u][i];
           e[i^1].flow-=df;
                                                         edge(int v,int pre, T cap, T cost):v(v),
                                                                                                           return ans;
                                                                                                                                                      11
                                                                                                                                                             if(vis[v])continue;
           e[i].r-=df;
                                                              pre(pre), cap(cap), cost(cost){}
                                                                                                                                                             vis[v]=true;
32
                                                                                                    68
           e[i^1].r+=df;
                                                                                                    69 };
                                                                                                                                                             if((int)match_list[v].size()<c[v]){</pre>
           if(!(tf-=df)||d[s]==n)return
                                                                                                                                                               match list[v].push back(u);
                                                       int n.S.T:
                                                       _T dis[MAXN],piS,ans;
                cur_flow-tf;
                                                                                                                                                      15
                                                                                                                                                               return true;
                                                       bool vis[MAXN];
35
                                                                                                                                                             }else{
36
                                                       vector<edge> e;
                                                                                                                                                               for(size t j=0;j<match list[v].size()</pre>
                                                       int g[MAXN];
                                                                                                                                                                    ;++i){
       for(int i=cur[u]=g[u];~i;i=e[i].pre){
                                                       void init(int n){
                                                                                                                                                                 int next u=match list[v][j];
                                                         memset(g,-1,sizeof(int)*((n=_n)+1));
         if(e[i].r&&d[e[i].v]<mh)mh=d[e[i].v];
                                                                                                                                                      19
                                                                                                                                                                 if(dfs(next u)){
                                                  17
                                                         e.clear();
                                                                                                                                                                   match list[v][i]=u;
40
                                                                                                                                                      20
```

tie(u,v,w)=e;

```
5.6 MaximumClique.cpp
                                                                                                       4 int g[MAXN][MAXN], lx[MAXN], ly[MAXN], pa[MAXN
                                                       return 0;
                                                                                                              ],slack v[MAXN];
                                                                                                         int match_y[MAXN], match_x[MAXN];
24
                                                   44
                                                                                                       6 bool vx[MAXN],vy[MAXN];
25
                                                   45 inline int blossom(){
                                                                                                                                                            struct MaxClique{
    return false;
                                                                                                         void augment(int y){
                                                                                                                                                              static const int MAXN=105:
26
                                                   46
27
                                                        for(int i=1;i<=n;++i)</pre>
                                                                                                           for(int x,z;y;y=z){
                                                                                                                                                              int N, ans;
   inline int max match(){
                                                   48
                                                          if(!match[i]&&bfs(i))++ans;
                                                                                                             x=pa[y],z=match x[x];
                                                                                                                                                              int g[MAXN][MAXN], dp[MAXN], stk[MAXN][MAXN
    for(int i=0;i<n2;++i)match_list[i].clear()</pre>
                                                        return ans;
                                                                                                             match_y[y]=x,match_x[x]=y;
                                                  49
                                                                                                      11
                                                                                                                                                              int sol[MAXN], tmp[MAXN]; //sol[0~ans-1]為答
     int cnt=0;
                                                                                                      12
30
     for(int u=0;u<n1;++u){</pre>
31
                                                                                                      13
                                                                                                         void bfs(int st){
                                                                                                                                                              void init(int n){
       memset(vis,0,sizeof(bool)*n2);
                                                                                                           for(int i=1;i<=n;++i)slack y[i]=INF,vx[i]=</pre>
32
                                                                                                                                                                N=n;//0-base
       if(dfs(u))++cnt;
33
                                                      5.4 graphISO.cpp
                                                                                                                vy[i]=0;
                                                                                                                                                                memset(g,0,sizeof(g));
34
                                                                                                      15
                                                                                                           queue<int> q;q.push(st);
35
    return cnt;
                                                                                                      16
                                                                                                           for(;;){
                                                                                                                                                              void add_edge(int u,int v){
                                                                                                      17
                                                                                                             while(q.size()){
                                                                                                                                                                g[u][v]=g[v][u]=1;
                                                    1 const int MAXN=1005, K=30; // K要夠大
                                                                                                               int x=q.front();q.pop();
                                                                                                      18
                                                                                                                                                         12
                                                    2 const long long A=3,B=11,C=2,D=19,P=0
                                                                                                      19
                                                                                                               vx[x]=1;
                                                                                                                                                         13
                                                                                                                                                              int dfs(int ns,int dep){
                                                                                                      20
                                                                                                               for(int y=1;y<=n;++y)if(!vy[y]){</pre>
                                                                                                                                                                if(!ns){
                                                                                                                                                         14
          blossom matching.cpp
                                                    3 long long f[K+1][MAXN]:
                                                                                                                  int t=lx[x]+ly[y]-g[x][y];
                                                                                                      21
                                                                                                                                                                  if(dep>ans){
                                                                                                                                                         15
                                                      vector<int> g[MAXN],rg[MAXN];
                                                                                                      22
                                                                                                                                                         16
                                                                                                                                                                    ans=dep;
                                                                                                      23
                                                                                                                    pa[y]=x;
                                                                                                                                                                    memcpy(sol,tmp,sizeof tmp);
                                                                                                                                                         17
                                                     inline void init(){
1 #define MAXN 505
                                                                                                      24
                                                                                                                    if(!match_y[y]){augment(y); return
                                                                                                                                                                    return 1;
                                                        for(int i=0;i<n;++i){</pre>
vector<int>g[MAXN];
                                                                                                                                                                  }else return 0;
                                                          f[0][i]=1;
int pa[MAXN], match[MAXN], st[MAXN], S[MAXN], v[
                                                                                                                    vy[y]=1,q.push(match_y[y]);
                                                                                                      25
                                                                                                                                                         20
                                                          g[i].clear();
                                                                                                                  }else if(slack_y[y]>t)pa[y]=x,
                                                                                                      26
                                                                                                                                                         21
                                                                                                                                                                 for(int i=0;i<ns;++i){</pre>
                                                          rg[i].clear();
                                                                                                                      slack_y[y]=t;
                                                                                                                                                         22
                                                                                                                                                                  if(dep+ns-i<=ans)return 0;</pre>
                                                   11
  inline int lca(int x,int y){
                                                                                                      27
                                                                                                                                                                  int u=stk[dep][i],cnt=0;
                                                                                                                                                         23
                                                   12
    for(++t;;swap(x,y)){
                                                                                                      28
                                                                                                                                                                  if(dep+dp[u]<=ans)return 0;</pre>
                                                                                                                                                         24
                                                      inline void add edge(int u,int v){
       if(x==0)continue;
                                                                                                      29
                                                                                                             int cut=INF;
                                                                                                                                                         25
                                                                                                                                                                   for(int j=i+1;j<ns;++j){</pre>
                                                        g[u].push back(v);
       if(v[x]==t)return x;
                                                                                                      30
                                                                                                             for(int y=1;y<=n;++y){</pre>
                                                                                                                                                                    int v=stk[dep][j];
                                                       rg[v].push_back(u);
                                                   15
                                                                                                      31
                                                                                                               if(!vy[y]&&cut>slack_y[y])cut=slack_y[
       v[x]=t;
                                                                                                                                                                    if(g[u][v])stk[dep+1][cnt++]=v;
                                                   16
       x=st[pa[match[x]]];
                                                                                                                    у];
                                                      inline long long point_hash(int u){//O(N)
                                                   17
11
                                                                                                      32
                                                                                                                                                         29
                                                                                                                                                                   tmp[dep]=u;
                                                        for(int t=1;t<=K;++t){</pre>
12 }
                                                                                                      33
                                                                                                             for(int j=1;j<=n;++j){</pre>
                                                                                                                                                         30
                                                                                                                                                                  if(dfs(cnt,dep+1))return 1;
                                                   19
                                                          for(int i=0;i<n;++i){</pre>
13 #define qpush(x) q.push(x),S[x]=0
                                                                                                      34
                                                                                                               if(vx[j])lx[j]-=cut;
                                                                                                                                                         31
                                                            f[t][i]=f[t-1][i]*A%P;
   inline void flower(int x,int y,int l,queue<</pre>
                                                                                                      35
                                                                                                               if(vy[j])ly[j]+=cut;
                                                                                                                                                         32
                                                                                                                                                                return 0;
                                                            for(int j:g[i])f[t][i]=(f[t][i]+f[t
       int > &q){
                                                                                                      36
                                                                                                               else slack_y[j]-=cut;
                                                                                                                                                         33
                                                                 -1][j]*B%P)%P;
     while(st[x]!=1){
                                                                                                      37
                                                                                                                                                               int clique(){
                                                            for(int j:rg[i])f[t][i]=(f[t][i]+f[t
                                                   22
16
       pa[x]=y;
                                                                                                      38
                                                                                                             for(int y=1;y<=n;++y){</pre>
                                                                                                                                                         35
                                                                                                                                                                int u,v,ns;
                                                                 -1][j]*C%P)%P;
       if(S[y=match[x]]==1)qpush(y);
                                                                                                               if(!vy[y]&&slack_y[y]==0){
                                                                                                      39
                                                                                                                                                         36
                                                                                                                                                                for(ans=0,u=N-1;u>=0;--u){
                                                            if(i==u)f[t][i]+=D;//如果圖太大的話
                                                   23
       st[x]=st[y]=1,x=pa[y];
                                                                                                      40
                                                                                                                 if(!match_y[y]){augment(y);return;}
                                                                                                                                                         37
                                                                                                                                                                  for(ns=0,tmp[0]=u,v=u+1;v<N;++v)</pre>
                                                                 把這行刪掉,執行一次後f[K]就會是所 41
                                                                                                                  vy[y]=1,q.push(match_y[y]);
19
                                                                                                                                                                    if(g[u][v])stk[1][ns++]=v;
                                                                                                                                                         38
20
                                                                                                      42
                                                                                                                                                                  dfs(ns,1),dp[u]=ans;
                                                                                                                                                         39
   inline bool bfs(int x){
                                                                                                      43
                                                   24
                                                            f[t][i]%=P;
                                                                                                                                                         40
    for(int i=1;i<=n;++i)st[i]=i;</pre>
                                                                                                      44
                                                                                                           }
                                                   25
                                                                                                                                                         41
                                                                                                                                                                return ans;
    memset(S+1,-1,sizeof(int)*n);
                                                                                                      45
                                                   26
                                                                                                                                                         42
    queue<int>q;qpush(x);
                                                                                                         long long KM(){
                                                   27
                                                       return f[K][u];
                                                                                                                                                         43 };
                                                                                                           memset(match_y,0,sizeof(int)*(n+1));
    while(q.size()){
                                                   28
26
       x=q.front(),q.pop();
                                                                                                           memset(ly,0,sizeof(int)*(n+1));
                                                      inline vector<long long> graph_hash(){
                                                   29
       for(size_t i=0;i<g[x].size();++i){</pre>
                                                                                                           for(int x=1;x<=n;++x){</pre>
                                                                                                      49
                                                        vector<long long> ans;
28
         int y=g[x][i];
                                                                                                      50
                                                                                                             1x[x]=-INF;
                                                        for(int i=0;i<n;++i)ans.push back(</pre>
                                                                                                                                                            5.7 MinimumMeanCycle.cpp
                                                                                                             for(int y=1;y<=n;++y)</pre>
         if(S[y]==-1){
                                                             point_hash(i));//O(N^2)
           pa[y]=x,S[y]=1;
                                                        sort(ans.begin(),ans.end());
                                                                                                      52
                                                                                                               lx[x]=max(lx[x],g[x][y]);
                                                   32
           if(!match[y]){
                                                                                                      53
                                                   33
                                                        return ans;
                                                                                                           for(int x=1;x<=n;++x)bfs(x);</pre>
                                                                                                                                                          1 #include < cstdint > // for DBL_MAX
             for(int lst;x;y=lst,x=pa[y])
                                                   34 }
               lst=match[x],match[x]=y,match[y
                                                                                                           long long ans=0;
                                                                                                                                                          2 int dp[maxN+1][maxN+1];
                                                                                                                                                          3 double mnc(int n){
                                                                                                           for(int y=1;y<=n;++y)ans+=g[match y[y]][y</pre>
             return 1;
                                                                                                                ];
                                                                                                      57
                                                                                                           return ans;
                                                                                                                                                                const int inf=0x7f7f7f7f;
                                                             KM.cpp
           qpush(match[y]);
                                                                                                      58 }
                                                                                                                                                                memset(dp,0x7f,sizeof(dp));
         }else if(!S[y]&&st[y]!=st[x]){
                                                                                                                                                                memset(dp[0],0,sizeof(dp[0]));
           int l=lca(y,x);
                                                                                                                                                                for(int i=0;i<n;++i){</pre>
                                                    1 #define MAXN 405
           flower(y,x,1,q),flower(x,y,1,q);
                                                                                                                                                                     for(auto e:E){//tuple<int,int,int>
                                                    2 #define INF 0x3f3f3f3f
40
                                                                                                                                                                          of u,v,w
```

3 int n; // 1-base, 0表示沒有匹配

// find a match

25 struct bit node{

```
if(dp[i][u]!=inf)
                                                         for (int i=0; i<n; i+=2){</pre>
                                                                                                        T mi:
                                                                                                                                                           for(auto v:g[u])if(!vis[v])tmp.push back(
                   dp[i+1][v]=min(dp[i+1][v],dp 43
                                                           match[i] = i+1;
                                                                                                         int id;
                                                                                                                                                                dfs(v));
12
                                                           match[i+1] = i;
                                                                                                         bit node(const T&mi=INF,int id=-1):mi(mi),
                                                                                                                                                           if(tmp.empty())return 177;
                        [i][u]+w);
                                                 44
                                                                                                                                                           long long ret=4931;
                                                  45
                                                                                                              id(id){}
           double res = DBL MAX;
                                                         for(;;){
                                                                                                                                                           sort(tmp.begin(),tmp.end());
14
                                                  46
           for(int i=1;i<=n;++i){</pre>
                                                           int found = 0;
                                                                                                    30 std::vector<bit node> bit;
                                                                                                                                                           for(auto v:tmp)ret=((ret*X)^v)%P;
                                                  47
               double val = DBL MIN:
                                                  48
                                                           for (int i=0: i<n: i++)</pre>
                                                                                                       inline void bit update(int i.const T&data.
                                                                                                                                                           return ret:
               for(int j=0;j<n;++j)</pre>
                                                             dis[i] = onstk[i] = 0;
                                                                                                            int id){
                                                                                                                                                      14
17
                                                  49
                   val=max(val,double(dp[n][i]-
                                                                                                         for(;i;i-=i&(-i)){
                                                 50
                                                           for (int i=0; i<n; i++){</pre>
                                                                                                           if(data<bit[i].mi)bit[i]=bit node(data,</pre>
                        dp[i][j])/(n-j));
                                                             stk.clear();
                                                                                                                                                         string dfs(int x,int p){
                                                 51
               res=min(res,val);
                                                  52
                                                             if (!onstk[i] && SPFA(i)){
                                                                                                                                                           vector<string> c;
                                                               found = 1:
                                                                                                                                                           for(int y:g[x])
20
                                                  53
                                                                                                    34
                                                  54
                                                               while (stk.size()>=2){
                                                                                                    35
                                                                                                                                                            if(y!=p)c.emplace_back(dfs(y,x));
21
22
       return res:
                                                  55
                                                                 int u = stk.back(); stk.pop back
                                                                                                   36
                                                                                                       inline int bit find(int i.int m){
                                                                                                                                                           sort(c.begin(),c.end());
                                                                                                                                                           string ret("(");
                                                                 int v = stk.back(); stk.pop back
                                                                                                   38
                                                                                                         for(;i<=m;i+=i&(-i)){</pre>
                                                                                                                                                      22
                                                                                                                                                           for(auto &s:c)ret+=s;
                                                                                                          if(bit[i].mi<x.mi)x=bit[i];</pre>
                                                                                                                                                           ret+=")";
                                                                      ();
                                                                                                    39
                                                                 match[u] = v;
                                                                                                                                                           return ret;
                                                                                                    40
  5.8 Minimum General Weighte
                                                                 match[v] = u;
                                                                                                    41
                                                                                                         return x.id;
                                                                                                    42
                                                                                                       inline std::vector<edge> build graph(int n,
1 | struct Graph {
                                                  61
                                                                                                            point p[]){
                                                                                                                                                         5.11 全局最小割.cpp
    // Minimum General Weighted Matching (
                                                  62
                                                           if (!found) break:
                                                                                                         std::vector<edge> e;//回傳的邊就可以用來求
          Perfect Match) 0-base
                                                  63
                                                                                                              最小牛成樹
    static const int MXN = 105:
                                                  64
                                                         int ret = 0:
                                                                                                         for(int dir=0; dir<4; ++dir){//4種座標變換
                                                                                                    45
                                                                                                                                                       1 const int INF=0x3f3f3f3f;
                                                  65
                                                         for (int i=0: i<n: i++)</pre>
                                                                                                           if(dir%2){
                                                                                                                                                         template<tvpename T>
    int n, edge[MXN][MXN];
                                                  66
                                                          ret += edge[i][match[i]];
                                                                                                             for(int i=0;i<n;++i)std::swap(p[i].x,p</pre>
                                                                                                                                                         struct stoer wagner{// 0-base
    int match[MXN], dis[MXN], onstk[MXN];
                                                  67
                                                         ret /= 2:
                                                                                                                  [i].y);
                                                                                                                                                           static const int MAXN=150;
    vector<int> stk;
                                                  68
                                                         return ret;
                                                                                                           }else if(dir==2){
                                                                                                                                                           T g[MAXN][MAXN], dis[MAXN];
                                                  69
                                                                                                             for(int i=0;i<n;++i)p[i].x=-p[i].x;</pre>
                                                                                                    49
                                                                                                                                                           int nd[MAXN],n,s,t;
    void init(int n) {
                                                  70 }graph;
                                                                                                    50
                                                                                                                                                           void init(int _n){
10
                                                                                                    51
                                                                                                           std::sort(p,p+n,cmpx);
                                                                                                                                                             n= n;
       for (int i=0; i<n; i++)
                                                                                                           std::vector<T>ga(n),gb;
                                                                                                                                                             for(int i=0;i<n;++i)</pre>
         for (int j=0; j<n; j++)</pre>
                                                                                                           for(int i=0;i<n;++i)ga[i]=p[i].y-p[i].x;</pre>
                                                                                                                                                               for(int j=0;j<n;++j)g[i][j]=0;</pre>
13
           edge[i][j] = 0;
                                                     5.9 Rectilinear Steiner tree.cpt
                                                                                                           gb=ga;
14
                                                                                                           std::sort(gb.begin(),gb.end());
                                                                                                                                                           void add_edge(int u,int v,T w){
15
    void add_edge(int u, int v, int w) {
                                                                                                           gb.resize(std::unique(gb.begin(),gb.end
                                                                                                                                                             g[u][v]=g[v][u]+=w;
       edge[u][v] = edge[v][u] = w;
16
                                                                                                                ())-gb.begin());
                                                   1 //平面曼哈頓最小生成樹構造圖(去除非必要邊)
                                                                                                                                                      14
17
                                                                                                           int m=gb.size();
                                                   2 #include < vector >
                                                                                                                                                      15
                                                                                                                                                           T min_cut(){
18
    bool SPFA(int u){
                                                                                                    58
                                                                                                           bit=std::vector<bit node>(m+1);
                                                   3 #include < algorithm >
                                                                                                                                                             T ans=INF:
       if (onstk[u]) return true;
19
                                                                                                    59
                                                                                                           for(int i=n-1;i>=0;--i){
                                                   4 #define T int
                                                                                                                                                             for(int i=0;i<n;++i)nd[i]=i;</pre>
20
       stk.push back(u);
                                                                                                    60
                                                                                                             int pos=std::lower_bound(gb.begin(),gb
                                                                                                                                                             for(int ind,tn=n;tn>1;--tn){
                                                   5 #define INF 0x3f3f3f3f3f
       onstk[u] = 1;
                                                                                                                  .end(),ga[i])-gb.begin()+1;
                                                                                                                                                               for(int i=1;i<tn;++i)dis[nd[i]]=0;</pre>
                                                   6 struct point{
       for (int v=0; v<n; v++){</pre>
                                                                                                             int ans=bit find(pos,m);
                                                      T x,y;
                                                                                                                                                               for(int i=1;i<tn;++i){</pre>
         if (u != v && match[u] != v && !onstk[
                                                                                                             if(~ans)e.push_back(edge(p[i].id,p[ans
                                                                                                                                                                 ind=i:
                                                       int id://每個點的編號都要不一樣,從0開始編
                                                                                                                  ].id,p[i].dist(p[ans])));
                                                                                                                                                                 for(int j=i;j<tn;++j){</pre>
           int m = match[v];
                                                                                                             bit update(pos,p[i].x+p[i].y,i);
                                                                                                    63
                                                                                                                                                                   dis[nd[j]]+=g[nd[i-1]][nd[j]];
25
           if (dis[m] > dis[u] - edge[v][m] +
                                                       point(){}
                                                                                                    64
                                                                                                                                                                   if(dis[nd[ind]]<dis[nd[j]])ind=j;</pre>
                                                                                                                                                      24
                                                      T dist(const point &p)const{
                edge[u][v]){
                                                                                                                                                      25
             dis[m] = dis[u] - edge[v][m] +
                                                         return std::abs(x-p.x)+std::abs(y-p.y);
                                                                                                         return e;
                                                                                                                                                      26
                                                                                                                                                                 swap(nd[ind],nd[i]);
                  edge[u][v];
                                                  12
                                                                                                                                                      27
             onstk[v] = 1;
                                                  13 };
                                                                                                                                                      28
                                                                                                                                                               if(ans>dis[nd[ind]])ans=dis[t=nd[ind
             stk.push back(v);
                                                  14 inline bool cmpx(const point &a,const point
                                                                                                                                                                    ]],s=nd[ind-1];
             if (SPFA(m)) return true;
                                                                                                                                                               for(int i=0;i<tn;++i)</pre>
                                                                                                                                                      29
             stk.pop back();
                                                       return a.x<b.x||(a.x==b.x&&a.y<b.y);
                                                                                                                                                                 g[nd[ind-1]][nd[i]]=g[nd[i]][nd[ind
                                                                                                                                                      30
                                                  16 }
             onstk[v] = 0;
                                                                                                       5.10 treeISO.cpp
                                                                                                                                                                      -1]]+=g[nd[i]][nd[ind]];
                                                     struct edge{
32
                                                                                                                                                      31
                                                      int u.v:
                                                                                                                                                      32
                                                                                                                                                             return ans;
                                                                                                                                                      33
                                                       edge(int u,int v,const T&c):u(u),v(v),cost 1 const int MAXN=100005;
       onstk[u] = 0;
                                                                                                     const long long X=12327,P=0xdefaced;
       stk.pop back();
       return false;
                                                       bool operator<(const edge&e)const{</pre>
                                                                                                     3 vector<int> g[MAXN];
                                                  22
                                                         return cost<e.cost;</pre>
                                                                                                     4 bool vis[MAXN];
                                                                                                     5 long long dfs(int u){//hash ver
                                                  23
                                                                                                                                                         5.12 平面圖判定.cpp
    int solve() {
                                                 24 };
                                                                                                         vis[u]=1;
```

vector<long long> tmp;

```
1 static const int MAXN = 20;
                                                        int n;// 0-base
2 struct Edge{
                                                        vector<int>G[MAXN];
                                                        int rank[MAXN],label[MAXN];
    int u, v;
    Edge(int s, int d) : u(s), v(d) {}
                                                        bool mark[MAXN];
                                                        void init(int n){n= n;
   bool isK33(int n, int degree[]){
                                                         for(int i=0;i<n;++i)G[i].clear();</pre>
    int t = 0, z = 0;
    for(int i=0;i<n;++i){</pre>
                                                        void add_edge(int u,int v){
                                                   10
       if(degree[i] == 3)++t;
                                                   11
                                                         G[u].push back(v);
       else if(degree[i] == 0)++z;
                                                         G[v].push back(u);
10
                                                   12
11
       else return false;
                                                   13
                                                   14
                                                        vector<int> MCS(){
12
    return t == 6 && t + z == n;
                                                          memset(rank,-1,sizeof(int)*n);
13
                                                   15
14
                                                   16
                                                          memset(label.0.sizeof(int)*n);
   bool isK5(int n, int degree[]){
                                                   17
                                                          priority queue<pair<int,int> > pq;
16
    int f = 0, z = 0;
                                                          for(int i=0;i<n;++i)pq.push(make pair(0,</pre>
    for(int i=0;i<n;++i){</pre>
17
       if(degree[i] == 4)++f;
                                                          for(int i=n-1;i>=0;--i)for(;;){
18
                                                   19
       else if(degree[i] == 0)++z;
                                                            int u=pq.top().second;pq.pop();
19
                                                   20
       else return false:
                                                            if(~rank[u])continue;
20
                                                  21
21
                                                   22
                                                            rank[u]=i;
    return f == 5 && f + z == n;
                                                            for(auto v:G[u])if(rank[v]==-1){
22
                                                   23
                                                              pq.push(make_pair(++label[v],v));
23
                                                   24
24 // it judge a given graph is Homeomorphic
                                                   25
        with K33 or K5
                                                   26
                                                            break;
25 bool isHomeomorphic(bool G[MAXN][MAXN],
                                                   27
        const int n){
                                                   28
                                                          vector<int> res(n);
     for(;;){
                                                   29
                                                          for(int i=0;i<n;++i)res[rank[i]]=i;</pre>
26
27
       int cnt = 0;
                                                   30
                                                          return res;
28
       for(int i=0;i<n;++i){</pre>
                                                   31
29
         vector<Edge> E;
                                                        bool check(vector<int> ord){//弦圖判定
                                                   32
30
         for(int j=0;j<n&E.size()<3;++j)</pre>
                                                          for(int i=0;i<n;++i)rank[ord[i]]=i;</pre>
           if(G[i][j] && i != j)
31
                                                          memset(mark.0.sizeof(bool)*n);
                                                   34
32
             E.push back(Edge(i, j));
                                                          for(int i=0;i<n;++i){</pre>
                                                   35
33
         if(E.size() == 1){
                                                            vector<pair<int,int> > tmp;
           G[i][E[0].v] = G[E[0].v][i] = false;
34
                                                            for(auto u:G[ord[i]])if(!mark[u])
35
         }else if(E.size() == 2){
                                                              tmp.push back(make pair(rank[u],u));
           G[i][E[0].v] = G[E[0].v][i] = false;
36
                                                            sort(tmp.begin(),tmp.end());
37
           G[i][E[1].v] = G[E[1].v][i] = false; 40
                                                            if(tmp.size()){
           G[E[0].v][E[1].v] = G[E[1].v][E[0].v 41
38
                                                              int u=tmp[0].second;
                ] = true;
                                                   42
                                                              set<int> S;
39
           ++cnt;
                                                   43
                                                              for(auto v:G[u])S.insert(v);
40
                                                              for(size t j=1;j<tmp.size();++j)</pre>
                                                   44
41
                                                   45
                                                                if(!S.count(tmp[j].second))return
       if(cnt == 0)break;
42
43
                                                   46
     static int degree[MAXN];
                                                            mark[ord[i]]=1;
                                                   47
    fill(degree, degree + n, 0);
                                                   48
    for(int i=0;i<n;++i){</pre>
                                                   49
                                                         return 1;
47
       for(int j=i+1; j<n; ++j){</pre>
                                                   50
         if(!G[i][j])continue;
48
                                                  51 };
49
         ++degree[i];
50
         ++degree[j];
51
52
    }
                                                      5.14 最小斯坦納樹 DP.cpp
     return !(isK33(n, degree) || isK5(n,
          degree));
                                                   1 | //n 個 點 · 其中r 個 要 構 成 斯 坦 納 樹
                                                   3 //p表示要構成斯坦納樹的點集
```

## 5.13 弦圖完美消除序列.cpp

```
1 struct chordal{
   static const int MAXN=1005;
```

```
2 //答案在max(dp[(1<<r)-1][k]) k=0~n-1
4 //0( n^3 + n*3^r + n^2*2^r )
5 #define REP(i,n) for(int i=0;i<(int)n;++i)</pre>
6 const int MAXN=30, MAXM=8; // 0-base
7 const int INF=0x3f3f3f3f;
8 int dp[1<<MAXM][MAXN];</pre>
```

```
9 int g[MAXN][MAXN];// 🗟
void init(){memset(g,0x3f,sizeof(g));}
void add edge(int u,int v,int w){
   g[u][v]=g[v][u]=min(g[v][u],w);
13 }
  void steiner(int n,int r,int *p){
    REP(k,n)REP(i,n)REP(i,n)
       g[i][j]=min(g[i][j],g[i][k]+g[k][j]);
17
     REP(i,n)g[i][i]=0;
18
     REP(i,r)REP(j,n)dp[1<<i][j]=g[p[i]][j];</pre>
19
     for(int i=1;i<(1<<r);++i){</pre>
       if(!(i&(i-1)))continue;
20
       REP(j,n)dp[i][j]=INF;
21
22
       REP(j,n){
23
         int tmp=INF:
24
         for(int s=i&(i-1);s;s=i&(s-1))
           tmp=min(tmp,dp[s][j]+dp[i^s][j]);
25
         REP(k,n)dp[i][k]=min(dp[i][k],g[j][k]+52
26
              tmp);
27
28
```

39

40

41

42

43

44

46

47

48

49

50

51

53

54

55

56

57

58

59

60

61

62

## 5.15 最小樹形圖 朱劉.cpp

1 template<typename T>

2 struct zhu\_liu{

```
static const int MAXN=110,MAXM=10005;
     struct node{
       int u,v;
       T w, tag;
       node *1,*r;
       node(int u=0, int v=0, T w=0): u(u), v(v), w(
            w), tag(0), 1(0), r(0){}
       void down(){
10
         w+=tag;
11
         if(1)1->tag+=tag;
12
         if(r)r->tag+=tag;
13
         tag=0;
14
15
     }mem[MAXM];//靜態記憶體
     node *pq[MAXN*2],*E[MAXN*2];
16
     int st[MAXN*2],id[MAXN*2],m;
     void init(int n){
19
       for(int i=1;i<=n;++i){</pre>
20
         pq[i]=E[i]=0;
21
         st[i]=id[i]=i;
^{22}
       }m=0;
23
     node *merge(node *a,node *b){//skew heap
       if(!a||!b)return a?a:b;
       a->down(),b->down();
       if(b->w<a->w)return merge(b,a);
       swap(a->1,a->r);
29
       a->1=merge(b,a->1);
30
       return a;
31
     void add edge(int u,int v,T w){
33
       if(u!=v)pq[v]=merge(pq[v],&(mem[m++]=
            node(u,v,w)));
34
     int find(int x,int *st){
       return st[x]==x?x:st[x]=find(st[x],st);
```

```
T build(int root, int n){
       T ans=0; int N=n, all=n;
       for(int i=1;i<=N;++i){</pre>
        if(i==root||!pq[i])continue;
         while(pq[i]){
           pq[i]->down(),E[i]=pq[i];
           pq[i]=merge(pq[i]->1,pq[i]->r);
           if(find(E[i]->u,id)!=find(i,id))
                break:
         if(find(E[i]->u,id)==find(i,id))
              continue:
         ans+=E[i]->w:
         if(find(E[i]->u,st)==find(i,st)){
           if(pq[i])pq[i]->tag-=E[i]->w;
           pq[++N]=pq[i];id[N]=N;
           for(int u=find(E[i]->u,id);u!=i;u=
                find(E[u]->u,id)){
             if(pq[u])pq[u]->tag-=E[u]->w;
             id[find(u,id)]=N;
             pq[N]=merge(pq[N],pq[u]);
           st[N]=find(i,st);
           id[find(i,id)]=N;
         }else st[find(i,st)]=find(E[i]->u,st)
             ,--all;
       return all==1?ans:-INT_MAX;//圖不連通就
63 };
```

### 5.16 穩定婚姻模板.cpp

```
1 | queue < int > 0;
2 for ( i : 所有考生 ) {
   設定在第0志願;
   Q.push(考生i);
6 while(Q.size()){
   當前考生=Q.front();Q.pop();
   while ( 此考生未分發 ) {
     指標移到下一志願;
     if ( 已經沒有志願 or 超出志願總數 )
        break;
     計算該考生在該科系加權後的總分;
11
    if (不符合科系需求) continue;
12
     if (目前科系有餘額) {
13
      依加權後分數高低順序將考生id加入科系錄
14
          取名單中;
15
      break:
16
    if (目前科系已額滿) {
17
      if ( 此考生成績比最低分數還高 ) {
18
        依加權後分數高低順序將考生id加入科系
           錄取名單;
        0.push(被踢出的考生);
```

42 inline void bellman(int l,int r,int n){

27 void build(T L){

inv[1]=1;

```
for(int k=1;k<=state;++k)</pre>
                                                                                                                                                      11 | void all divdown(const LL &n) {// all n/x
                                                                                                         isap.init(n+2);
24 }
                                                                                                         for(size t i=0;i<E.size();++i){</pre>
                                                  44
                                                        for(auto c:cnf)
                                                                                                                                                           for(LL a=1;a<=n;a=n/(n/(a+1))){
                                                           if(c.y==-1)relax(l,r,c,dp[l][r][c.x]+c 30
                                                                                                          isap.add_edge(E[i].u,E[i].v,E[i].w);
                                                                                                                                                            // dosomething;
                                                  45
                                                                                                                                                      13
                                                                .cost,k==n);
                                                                                                    31
                                                                                                                                                      14
                                                                                                         for(int v=1; v<=n;++v){</pre>
                                                                                                                                                      15
                                                  46 }
                                                                                                    32
                                                  47 inline void cyk(const vector<int> &tok){
                                                                                                                                                        const int MAXPRIME = 1000000;
                                                                                                    33
                                                                                                          isap.add edge(s,v,U);
        language
                                                       for(int i=0:i<(int)tok.size():++i){</pre>
                                                                                                    34
                                                                                                           isap.add edge(v,t,U+2*L-de[v]-2*pv[v]);
                                                                                                                                                        int iscom[MAXPRIME], prime[MAXPRIME],
                                                         for(int j=0;j<(int)tok.size();++j){</pre>
                                                                                                    35
                                                                                                                                                              primecnt;
                                                  49
                                                                                                                                                        int phi[MAXPRIME], mu[MAXPRIME];
                                                           dp[i][j]=vector<long long>(state+1,
                                                                                                    36
  6.1 CNF.cpp
                                                                                                    37
                                                                                                       int main(){
                                                                                                                                                         void sieve(void){
                                                  51
                                                           neg INF[i][i]=vector<bool>(state+1,
                                                                                                    38
                                                                                                         while(~scanf("%d%d",&n,&m)){
                                                                                                                                                           memset(iscom,0,sizeof(iscom));
                                                                                                           if(!m){
                                                                                                                                                           primecnt = 0:
                                                                false):
                                                                                                    39
                                                                                                             puts("1\n1");
                                                                                                                                                           phi[1] = mu[1] = 1;
1 #define MAXN 55
                                                  52
                                                                                                    40
   struct CNF{
                                                  53
                                                         dp[i][i][tok[i]]=0;
                                                                                                    41
                                                                                                             continue:
                                                                                                                                                           for(int i=2:i<MAXPRIME:++i) {</pre>
    int s,x,y;//s->xy | s->x, if y==-1
                                                  54
                                                        bellman(i,i,tok.size());
                                                                                                    42
                                                                                                                                                             if(!iscom[i]) {
                                                  55
                                                                                                    43
                                                                                                           init();
                                                                                                                                                      25
                                                                                                                                                               prime[primecnt++] = i;
    int cost;
                                                       for(int r=1;r<(int)tok.size();++r){</pre>
                                                  56
                                                                                                    44
                                                                                                           int u.v:
                                                                                                                                                      26
                                                                                                                                                               mu[i] = -1:
                                                         for(int l=r-1;l>=0;--1){
                                                                                                           for(int i=0;i<m;++i){</pre>
                                                                                                                                                               phi[i] = i-1;
    CNF(int s, int x, int y, int c):s(s), x(x), y(y)
                                                                                                                                                      27
                                                           for(int k=1;k<r;++k)</pre>
                                                                                                             scanf("%d%d",&u,&v);
                                                                                                    46
                                                                                                                                                      28
         ),cost(c){}
                                                             for(auto c:cnf)
                                                                                                                                                             for(int j=0;j<primecnt;++j) {</pre>
                                                  59
                                                                                                    47
                                                                                                             add edge(u,v,1);
                                                                                                                                                      29
7 };
                                                  60
                                                               if(~c.y)relax(1,r,c,dp[1][k][c.x]+
                                                                                                                                                      30
                                                                                                                                                               int k = i * prime[j];
s int state://規則數量
                                                                                                   48
                                                                    dp[k+1][r][c.y]+c.cost);
                                                                                                                                                               if(k>=MAXPRIME) break;
                                                                                                    49
                                                                                                           get_U();
                                                                                                                                                      31
9 | map<char, int> rule; //每個字元對應到的規則
                                                  61
                                                           bellman(l,r,tok.size());
                                                                                                    50
                                                                                                           s=n+1,t=n+2:
                                                                                                                                                      32
                                                                                                                                                               iscom[k] = prime[j];
        小寫字母為終端字符
                                                  62
                                                                                                    51
                                                                                                           T l=0,r=U,k=1.0/(n*n);
                                                                                                                                                      33
                                                                                                                                                               if(i%prime[j]==0) {
  vector<CNF> cnf;
                                                  63
                                                                                                                                                      34
                                                                                                                                                                 mu[k] = 0;
                                                                                                           while(r-1>k){//二分搜最大值
   inline void init(){
                                                  64 }
                                                                                                                                                      35
                                                                                                                                                                 phi[k] = phi[i] * prime[j];
                                                                                                    53
                                                                                                            T mid=(1+r)/2;
    state=0;
                                                                                                                                                                 break;
                                                                                                                                                      36
                                                                                                             build(mid);
    rule.clear();
                                                                                                                                                      37
                                                                                                                                                               } else {
                                                                                                             T res=(U*n-isap.isap(s,t))/2;
    cnf.clear();
14
                                                                                                                                                      38
                                                                                                             if(res>0)l=mid;
                                                                                                                                                                 mu[k] = -mu[i];
15
                                                                                                                                                      39
                                                                                                                                                                 phi[k] = phi[i] * (prime[j]-1);
                                                                                                             else r=mid;
                                                     7 Linear Programming
  inline void add to cnf(char s,const string &
                                                                                                                                                      40
       p,int cost){
                                                                                                                                                      41
                                                                                                           build(1);
    //加入一個s -> 的文法,代價為cost
                                                                                                                                                      42
                                                                                                           isap.min cut(s,t);
                                                                                                    60
    if(rule.find(s)==rule.end())rule[s]=state
                                                     7.1 最大密度子圖.cpp
                                                                                                                                                      43
                                                                                                           vector<int> ans;
                                                                                                    61
                                                                                                                                                      44
                                                                                                           for(int i=1:i<=n:++i){</pre>
    for(auto c:p)if(rule.find(c)==rule.end())
                                                                                                                                                         bool g test(const LL &g, const LL &p, const
                                                                                                             if(isap.vis[i])ans.push_back(i);
         rule[c]=state++;
                                                                                                                                                              vector<LL> &v) {
                                                                                                    64
                                                   1 typedef double T;//POJ 3155
    if(p.size()==1){
                                                                                                           printf("%d\n",ans.size());
                                                                                                                                                           for(int i=0;i<v.size();++i)</pre>
                                                   const int MAXN=105;
                                                                                                    65
       cnf.push_back(CNF(rule[s],rule[p[0]],-1,
                                                                                                                                                             if(modexp(g,(p-1)/v[i],p)==1)
                                                                                                           for(size t i=0;i<ans.size();++i){</pre>
                                                   3 struct edge{
                                                                                                    66
            cost));
                                                                                                                                                               return false;
                                                                                                             printf("%d \ n",ans[i]);
                                                                                                    67
                                                      int u,v;
    }else{
22
                                                                                                                                                      49
                                                                                                                                                           return true;
                                                                                                    68
       int left=rule[s];
23
                                                                                                                                                      50
                                                       edge(int u=0,int v=0,T w=0):u(u),v(v),w(w)
^{24}
       int sz=p.size();
                                                                                                                                                         LL primitive root(const LL &p) {
                                                            {}
                                                                                                    70
                                                                                                        return 0;
       for(int i=0;i<sz-2;++i){</pre>
                                                                                                                                                           if(p==2) return 1;
         cnf.push_back(CNF(left,rule[p[i]],
                                                                                                                                                           vector<LL> v;
                                                  8 vector<edge> E;
             state,0));
                                                                                                                                                           Factor(p-1,v);
                                                  9 int n,m;// 1-base
27
         left=state++;
                                                                                                                                                           v.erase(unique(v.begin(), v.end()), v.end
                                                  10 | T de[MAXN], pv[MAXN]; // 每 個 點 的 邊 權 和 和 點 權 (
28
                                                                                                                                                                ());
                                                          有些題目會給)
                                                                                                            Number Theory
       cnf.push back(CNF(left,rule[p[sz-2]],
29
                                                                                                                                                           for(LL g=2;g<p;++g)</pre>
                                                  11 void init(){
            rule[p[sz-1]],cost));
                                                                                                                                                             if(g test(g,p,v))
                                                                                                                                                               return g;
                                                       for(int i=1;i<=n;++i)de[i]=pv[i]=0;</pre>
                                                  13
31
                                                                                                       8.1 basic.cpp
                                                                                                                                                           puts("primitive_root NOT FOUND");
  vector<long long> dp[MAXN][MAXN];
                                                                                                                                                           return -1:
                                                     void add edge(int u,int v,T w){
33 | vector<bool> neg INF[MAXN][MAXN];//如果花費
                                                      E.push_back(edge(u,v,w));
        是負的可能會有無限小的情形
                                                                                                     1 template<typename T>
                                                                                                                                                        int Legendre(const LL &a, const LL &p) {
                                                       de[u]+=w.de[v]+=w:
34 inline void relax(int l,int r,const CNF &c,
                                                                                                     2 void gcd(const T &a,const T &b,T &d,T &x,T &
                                                                                                                                                             return modexp(a%p,(p-1)/2,p); }
                                                  18 }
       long long cost,bool neg c=0){
                                                 19 | T U; // 二分搜的最大值
    if(!neg_INF[1][r][c.s]&&(neg_INF[1][r][c.x
                                                                                                        if(!b) d=a,x=1,y=0;
                                                                                                                                                        LL inv(const LL &a, const LL &n) {
                                                  20 void get_U(){
          ]||cost<dp[1][r][c.s])){
                                                                                                         else gcd(b,a%b,d,y,x), y-=x*(a/b);
                                                                                                                                                          LL d,x,y;
                                                      U=0;
       if(neg_c||neg_INF[1][r][c.x]){
                                                                                                                                                           gcd(a,n,d,x,y);
                                                       for(int i=1;i<=n;++i)U+=2*pv[i];</pre>
         dp[1][r][c.s]=0;
                                                                                                     6 long long int phi[N+1];
                                                                                                                                                           return d==1 ? (x+n)%n : -1;
                                                       for(size_t i=0;i<E.size();++i)U+=E[i].w;</pre>
         neg_INF[1][r][c.s]=true;
                                                                                                      void phiTable(){
                                                 24 }
       }else dp[l][r][c.s]=cost;
                                                                                                        for(int i=1;i<=N;i++)phi[i]=i;</pre>
                                                  25 | ISAP<T> isap;//網路流
                                                                                                         for(int i=1; i <= N; i++) for(x=i*2; x <= N; x+=i)
                                                                                                                                                        int inv[maxN];
                                                  26 int s,t;//原匯點
                                                                                                             phi[x]-=phi[i];
                                                                                                                                                        LL invtable(int n, LL P){
```

```
for(int i=2;i<n;++i)</pre>
                                                         for (n=(n)=m?n\%m:n); k; k>>=1)
                                                                                                              //對大小為k的子集合的處理
                                                                                                                                                                 return a>>(32-len);
       inv[i]=(P-(P/i))*inv[P%i]%P;
74
                                                  136
                                                          if(k&1)ans=ans*n%m;
                                                                                                      12
                                                                                                              int x=comb&-comb, y=comb+x;
                                                                                                                                                          12
75
                                                          n=n*n%m;
                                                                                                      13
                                                                                                              comb = ((comb\&\sim y)/x>>1)|y;
                                                                                                                                                               void fft(bool is inv, VT &in, VT &out, int N)
                                                  137
                                                                                                                                                          13
76
                                                  138
                                                                                                      14
   LL log mod(const LL &a, const LL &b, const
                                                                                                      15 }
                                                                                                                                                                 int bitlen=std::__lg(N),num=is_inv?-1:1;
                                                  139
                                                        return ans;
                                                                                                                                                          14
                                                  140 3
                                                                                                                                                          15
                                                                                                                                                                 for(int i=0;i<N;++i)out[bit reverse(i,</pre>
     // a ^ x = b \pmod{p}
                                                  141 template<typename T>
                                                                                                                                                                      bitlen) l=in[i]:
     int m=sqrt(p+.5), e=1;
                                                      T crt(vector<T> &m, vector<T> &a){
                                                                                                                                                                 for(int step=2;step<=N;step<<=1){</pre>
                                                                                                                                                          16
     LL v=inv(modexp(a,m,p), p);
                                                                                                          8.3 cantor expansion.cpp
                                                        T M=1,tM,ans=0;
                                                                                                                                                          17
                                                                                                                                                                   const int mh=step>>1;
     map<LL,int> x;
                                                         for(int i=0;i<(int)m.size();++i)M*=m[i];</pre>
                                                                                                                                                                   for(int i=0;i<mh;++i){</pre>
                                                  144
                                                                                                                                                          18
82
     x[1]=0;
                                                  145
                                                         for(int i=0;i<(int)a.size();++i){</pre>
                                                                                                                                                          19
                                                                                                                                                                     std::complex<T> wi=exp(std::complex<</pre>
     for(int i=1;i<m;++i) {</pre>
                                                                                                        1 int factorial[MAXN]:
                                                                                                                                                                          T>(0,i*num*pi/mh));
83
                                                  146
                                                          tM=M/m[i]:
                                                          ans=(ans+(a[i]*tM%M)*pow_mod(tM,Euler(m[
                                                                                                       2 void init(){
                                                                                                                                                                     for(int j=i;j<N;j+=step){</pre>
84
       e = LLmul(e,a,p);
                                                  147
                                                                                                                                                          20
85
       if(!x.count(e)) x[e] = i;
                                                                i])-1,m[i])%M)%M;
                                                                                                           factorial[0]=1:
                                                                                                                                                          21
                                                                                                                                                                       int k=i+mh;
86
                                                          /*如果m[i]是質數·Euler(m[i])-1=m[i]-2·
                                                                                                           for(int i=1:i<=MAXN:++i)factorial[i]=</pre>
                                                                                                                                                          22
                                                                                                                                                                       std::complex<T> u=out[j],t=wi*out[
                                                  148
87
     for(int i=0;i<m;++i) {</pre>
                                                                                                                factorial[i-1]*i;
                                                                                                                                                                            k];
                                                                就不用算Euler了*/
       if(x.count(b)) return i*m + x[b];
                                                                                                                                                                       out[i]=u+t:
88
                                                                                                                                                          23
                                                  149
                                                                                                         int encode(const vector<int> &s){
                                                                                                                                                                       out[k]=u-t;
89
       b = LLmul(b,v,p);
                                                                                                                                                          24
                                                        return ans;
                                                  150
                                                                                                           int n=s.size(),res=0;
                                                                                                                                                          25
90
                                                  151
91
     return -1;
                                                                                                            for(int i=0;i<n;++i){</pre>
                                                                                                                                                          26
                                                  152
92
                                                                                                              int t=0;
                                                                                                                                                          27
                                                  153 //java code
                                                                                                              for(int j=i+1; j<n;++j)</pre>
                                                                                                                                                                 if(is inv)for(int i=0;i<N;++i)out[i]/=N;</pre>
93
                                                  154 / / 求 sart (N) 的 連 分 數
   LL Tonelli Shanks(const LL &n, const LL &p)
                                                                                                       11
                                                                                                                if(s[j]<s[i])++t;
                                                                                                                                                          29
                                                   155 public static void Pell(int n){
                                                                                                              res+=t*factorial[n-i-1];
                                                                                                                                                          30 };
                                                        BigInteger N,p1,p2,q1,q2,a0,a1,a2,g1,g2,h1
     // x^2 = n \pmod{p}
                                                                                                      13
                                                              ,h2,p,q;
     if(n==0) return 0;
96
                                                                                                       14
                                                                                                           return res;
                                                         g1=q2=p1=BigInteger.ZERO;
     if(Legendre(n,p)!=1) while(1) { puts("SQRT
                                                                                                       15
                                                         h1=q1=p2=BigInteger.ONE:
           ROOT does not exist"); }
                                                                                                         vector<int> decode(int a,int n){
                                                         a0=a1=BigInteger.valueOf((int)Math.sqrt
                                                                                                                                                             8.5 find real root.cpp
     int S = 0;
                                                                                                      17
                                                                                                           vector<int> res;
                                                             (1.0*n));
99
     LL Q = p-1;
                                                                                                      18
                                                                                                            vector<bool> vis(n,0);
                                                         BigInteger ans=a0.multiply(a0);
                                                  160
100
     while( !(Q&1) ) { Q>>=1; ++S; }
                                                                                                      19
                                                                                                            for(int i=n-1;i>=0;--i){
                                                  161
                                                        if(ans.equals(BigInteger.valueOf(n))){
101
     if(S==1) return modexp(n\%p,(p+1)/4,p);
                                                                                                      20
                                                                                                             int t=a/factorial[i],j;
                                                                                                                                                          1 / / an*x^n + ... + a1x + a0 = 0;
                                                          System.out.println("No solution!");
                                                  162
                                                                                                      21
                                                                                                              for(j=0;j<n;++j)</pre>
                                                                                                                                                          1 int sign(double x){
102
     LL z = 2:
                                                  163
                                                          return :
                                                                                                      22
                                                                                                                                                              return x < -eps ? -1 : x > eps;
103
     for(;Legendre(z,p)!=-1;++z)
                                                                                                                if(!vis[j]){
                                                  164
                                                                                                      23
                                                                                                                  if(t==0)break;
104
     LL c = modexp(z,Q,p);
                                                         while(true){
                                                  165
     LL R = modexp(n\%p,(Q+1)/2,p), t = modexp(n
105
                                                                                                      24
                                                                                                                  --t;
                                                           g2=a1.multiply(h1).substract(g1);
                                                   166
          %p,Q,p);
                                                                                                      25
                                                                                                                                                             double get(const vector<double>&coef, double
                                                          h2=N.substract(g2.pow(2)).divide(h1);
                                                  167
106
     int M = S;
                                                                                                      26
                                                                                                              res.push_back(j);
                                                  168
                                                           a2=g2.add(a0).divide(h2);
107
     while(1) {
                                                                                                      27
                                                                                                              vis[j]=1;
                                                                                                                                                               double e = 1, s = 0;
                                                  169
                                                          p=a1.multiply(p2).add(p1);
       if(t==1) return R;
                                                                                                              a%=factorial[i];
                                                                                                                                                               for(auto i : coef) s += i*e, e *= x;
108
                                                                                                      28
                                                  170
                                                           q=a1.multiply(q2).add(q1);
       LL b = modexp(c,1L << (M-i-1),p);
109
                                                                                                      29
                                                                                                                                                               return s;
                                                           if(p.pow(2).substract(N.multiply(q.pow
                                                  171
       R = LLmul(R,b,p);
110
                                                                                                            return res;
                                                                (2))).compareTo(BigInteger.ONE)==0)
       t = LLmul( LLmul(b,b,p), t, p);
111
                                                                break:
       c = LLmul(b,b,p);
                                                                                                                                                             double find(const vector<double>&coef, int n
112
                                                           g1=g2;h1=h2;a1=a2;
                                                  172
                                                                                                                                                                  , double lo, double hi){
113
       M = i;
                                                  173
                                                          p1=p2;p2=p;
                                                                                                                                                               double sign_lo, sign_hi;
114
                                                  174
                                                          q1=q2;q2=q;
                                                                                                         8.4 FFT.cpp
                                                                                                                                                               if( !(sign_lo = sign(get(coef,lo))) )
115
     return -1;
                                                  175
116
                                                                                                                                                                    return lo;
                                                        System.out.println(p+" "+q);
                                                  176
                                                                                                                                                               if( !(sign_hi = sign(get(coef,hi))) )
                                                  177 }
    template<typename T>
                                                                                                       1 template<typename T, typename VT=std::vector<
                                                                                                                                                                    return hi;
                                                                                                              std::complex<T> > >
                                                                                                                                                               if(sign_lo * sign_hi > 0) return INF;
   T Euler(T n){
                                                                                                         struct FFT{
                                                                                                                                                               for(int stp = 0; stp < 100 && hi - lo >
     T ans=n;
     for(T i=2:i*i<=n:++i){</pre>
                                                                                                           const T pi:
                                                                                                                                                                    eps; ++stp){
                                                             bit set.cpp
122
       if(n%i==0){
                                                                                                           FFT(const T pi=acos((T)-1)):pi(pi){}
                                                                                                                                                                 double m = (lo+hi)/2.0;
123
          ans=ans/i*(i-1);
                                                                                                            unsigned int bit reverse(unsigned int a,
                                                                                                                                                                 int sign_mid = sign(get(coef,m));
124
         while(n%i==0)n/=i;
                                                                                                                int len){
                                                                                                                                                                 if(!sign_mid) return m;
                                                    1 | void sub set(int S){
                                                                                                              a = ((a\&0x55555555U) << 1) | ((a\&0xAAAAAAAAU))
                                                                                                                                                                 if(sign lo*sign mid < 0) hi = m;</pre>
125
                                                                                                                                                          21
                                                        int sub=S;
                                                                                                                                                          22
                                                                                                                                                                 else lo = m;
126
                                                                                                                   >>1);
                                                        do{
     if(n>1)ans=ans/n*(n-1);
                                                                                                              a=((a&0x33333333U)<<2)|((a&0xCCCCCCCU)
                                                          //對某集合的子集合的處理
     return ans:
                                                                                                                                                               return (lo+hi)/2.0;
129
                                                          sub=(sub-1)&S;
                                                                                                              a=((a\&0x0F0F0F0FU)<<4)|((a\&0xF0F0F0F0U)
130
                                                        }while(sub!=S);
   //Chinese remainder theorem
                                                                                                              a=((a&0x00FF00FFU)<<8)|((a&0xFF00FF00U)
                                                                                                                                                             vector<double> cal(vector<double>coef, int n
   template<typename T>
                                                    8 void k sub set(int k,int n){
   T pow mod(T n, T k, T m){
                                                        int comb=(1<<k)-1,S=1<<n;</pre>
                                                                                                              a=((a\&0x0000FFFFU)<<16)|((a\&0xFFFF0000U)
                                                                                                                                                               vector<double>res;
     T ans=1;
                                                        while(comb<S){</pre>
                                                                                                                                                              if(n == 1){
```

1 2615053605667\*(2^18)+1,3

2 15\*(2^27)+1,31 3 479\*(2^21)+1,3

4 7\*17\*(2^23)+1,3

5 3\*3\*211\*(2^19)+1,5

```
8.10 MillerRobin.cpp
       if(sign(coef[1])) res.pb(-coef[0]/coef
                                                         // a[i]*x = b[i] \pmod{m[i]}
                                                                                                               matrix rev(r,c);
            [1]);
                                                         for(int i=0;i<n;++i) {</pre>
                                                                                                        19
                                                                                                               for(int i=0;i<r;++i)</pre>
       return res;
                                                           LL x, y, d = extgcd(a[i],m[i],x,y);
                                                                                                                 for(int j=0;j<c;++j)</pre>
31
                                                                                                        20
32
                                                           if(b[i]%d!=0) return make pair(-1LL,0LL)
                                                                                                       21
                                                                                                                   rev[i][j]=m[i][j]-a.m[i][j];
                                                                                                                                                             1 LL LLmul(LL a, LL b, const LL &mod) {
     vector<double>dcoef(n);
                                                                                                                                                                 LL ans=0:
33
                                                                                                        22
     for(int i = 0; i < n; ++i) dcoef[i] = coef</pre>
                                                           m[i] /= d;
                                                                                                        23
                                                                                                                                                                 while(b) {
          [i+1]*(i+1):
                                                           b[i] = LLmul(b[i]/d,x,m[i]);
                                                                                                        24
                                                                                                             matrix operator*(const matrix &a){
                                                                                                                                                                   if(b&1) {
     vector<double>droot = cal(dcoef, n-1);
                                                                                                               matrix rev(r,a.c);
35
                                                                                                        25
                                                                                                                                                                     ans+=a:
36
     droot.insert(droot.begin(), -INF);
                                                         LL lastb = b[0], lastm = m[0];
                                                                                                        26
                                                                                                               matrix tmp(a.c,a.r);
                                                                                                                                                                     if(ans>=mod) ans-=mod;
37
     droot.pb(INF);
                                                         for(int i=1;i<n;++i) {</pre>
                                                                                                        27
                                                                                                               for(int i=0;i<a.r;++i)</pre>
                                                    10
                                                           LL x, y, d = extgcd(m[i],lastm,x,y);
38
     for(int i = 0; i+1 < droot.size(); ++i){</pre>
                                                   11
                                                                                                        28
                                                                                                                 for(int j=0;j<a.c;++j)</pre>
                                                                                                                                                                   a<<=1. b>>=1:
       double tmp = find(coef, n, droot[i],
                                                           if((lastb-b[i])%d!=0) return make pair
                                                                                                                   tmp[j][i]=a.m[i][j];
                                                                                                                                                                   if(a>=mod) a-=mod;
39
                                                                                                        29
            droot[i+1]);
                                                                                                               for(int i=0;i<r;++i)</pre>
                                                                (-1LL,0LL);
                                                                                                        30
                                                                                                                                                            10
40
       if(tmp < INF) res.pb(tmp);</pre>
                                                           lastb = LLmul((lastb-b[i])/d,x,(lastm/d)
                                                                                                       31
                                                                                                                 for(int j=0;j<a.c;++j)</pre>
                                                                                                                                                            11
                                                                                                                                                                 return ans;
41
                                                                )*m[i];
                                                                                                        32
                                                                                                                   for(int k=0;k<c;++k)</pre>
                                                                                                                                                            12
42
    return res;
                                                           lastm = (lastm/d)*m[i];
                                                                                                        33
                                                                                                                      rev.m[i][j]+=m[i][k]*tmp[j][k];
                                                                                                                                                               LL mod mul(LL a, LL b, LL m){
                                                    14
                                                           lastb = (lastb+b[i])%lastm;
                                                                                                                                                                 a\%=m,b\%=m;/* fast for m < 2^58 */
43
                                                    15
                                                                                                        34
                                                                                                               return rev:
                                                                                                                                                            14
44
                                                    16
                                                                                                        35
                                                                                                                                                            15
                                                                                                                                                                 LL y=(LL)((double)a*b/m+0.5);
   int main () {
                                                         return make_pair(lastb<0?lastb+lastm:lastb</pre>
                                                    17
                                                                                                             bool inverse(){
                                                                                                                                                            16
                                                                                                                                                                 LL r=(a*b-y*m)%m;
45
                                                                                                       36
    vector<double>ve:
                                                              ,lastm);
46
                                                                                                               Matrix t(r,r+c);
                                                                                                                                                            17
                                                                                                                                                                 return r<0?r+m:r;</pre>
47
    vector<double>ans = cal(ve, n);
                                                                                                        38
                                                                                                               for(int y=0;y<r;y++){</pre>
                                                                                                                                                            18
                                                                                                                 t.m[y][c+y] = 1;
    // 視情況把答案 +eps, 避免 -0
                                                                                                        39
                                                                                                                                                               template<typename T>
                                                                                                        40
                                                                                                                 for(int x=0;x<c;++x)</pre>
                                                                                                                                                            20
                                                                                                                                                               T pow(T a,T b,T mod){//a^b\%mod}
                                                                                                        41
                                                                                                                   t.m[y][x]=m[y][x];
                                                                                                                                                                 T ans=1:
                                                                                                                                                            21
                                                       8.8 Lucas.cpp
                                                                                                                                                                 for(;b;a=mod_mul(a,a,mod),b>>=1)
                                                                                                        42
                                                                                                                                                            22
                                                                                                        43
                                                                                                               if( !t.gas() )
                                                                                                                                                            23
                                                                                                                                                                   if(b&1)ans=mod mul(ans,a,mod);
                                                                                                                 return false:
                                                                                                        44
                                                                                                                                                                 return ans:
  8.6 FWT.cpp
                                                     1 int mod fact(int n.int &e){
                                                                                                        45
                                                                                                               for(int y=0;y<r;y++)</pre>
                                                                                                                                                            25
                                                        e=0;
                                                                                                        46
                                                                                                                 for(int x=0;x<c;++x)</pre>
                                                                                                                                                            26 int sprp[3]={2,7,61};//int範圍可解
                                                         if(n==0)return 1;
                                                                                                        47
                                                                                                                   m[y][x]=t.m[y][c+x]/t.m[y][y];
                                                                                                                                                               int llsprp
1 void XORtransform(LL *P, int k=log, bool inv
                                                         int res=mod fact(n/P,e);
                                                                                                        48
                                                                                                               return true;
                                                                                                                                                                    [7] = \{2,325,9375,28178,450775,9780504,17952656\}
                                                         e += n/P:
                                                                                                        49
                                                                                                                                                                    //至少unsigned Long long範圍
     for(int len=1;2*len<=(1<<k);len<<=1)</pre>
                                                         if((n/P)%2==0)return res*fact[n%P]%P;
                                                                                                        50
                                                                                                             T gas(){
                                                                                                                                                               template<typename T>
       for(int i=0;i<(1<<k);i+=2*len)</pre>
                                                                                                               vector<T> lazy(r,1);
                                                         return res*(P-fact[n%P])%P;
                                                                                                        51
                                                                                                                                                               bool isprime(T n,int *sprp,int num){
         for (int j=0;j<len;++j){</pre>
                                                                                                               bool sign=false;
                                                                                                        52
                                                                                                                                                                 if(n==2)return 1:
           LL u=P[i+j],v=P[i+len+j];
                                                       int Cmod(int n,int m){
                                                                                                               for(int i=0;i<r;++i){</pre>
                                                                                                        53
                                                                                                                                                                 if(n<2||n%2==0)return 0;
           P[i+j]=u+v,P[i+len+j]=u-v;
                                                         int a1,a2,a3,e1,e2,e3;
                                                                                                        54
                                                                                                                 if( m[i][i]==0 ){
                                                                                                                                                                 int t=0;
                                                                                                                                                            32
                                                         a1=mod_fact(n,e1);
                                                                                                        55
                                                                                                                   int j=i+1;
                                                                                                                                                                 T u=n-1;
    if(inv)for(int i=0;i<(1<<k);++i)P[i]/=(1<<</pre>
                                                         a2=mod fact(m.e2):
                                                                                                        56
                                                                                                                   while(j<r&&!m[j][i])j++;</pre>
                                                                                                                                                                 for(;u%2==0;++t)u>>=1;
                                                         a3=mod_fact(n-m,e3);
                                                                                                        57
                                                    13
                                                                                                                   if(j==r)continue;
                                                                                                                                                                 for(int i=0;i<num;++i){</pre>
                                                         if(e1>e2+e3)return 0;
                                                    14
                                                                                                        58
                                                                                                                   m[i].swap(m[j]);
                                                                                                                                                                   T a=sprp[i]%n;
   void ANDtransform(LL *P,int k=log,bool inv
                                                         return a1*inv(a2*a3%P,P)%P;
                                                                                                                   sign=!sign;
                                                    15
                                                                                                        59
                                                                                                                                                                   if(a==0||a==1||a==n-1)continue;
                                                    16 }
                                                                                                        60
                                                                                                                                                                   T x=pow(a,u,n);
     for(int len=1;2*len<=(1<<k);len<<=1)</pre>
                                                                                                        61
                                                                                                                 for(int j=0;j<r;++j){</pre>
                                                                                                                                                                   if(x==1||x==n-1)continue;
12
       for(int i=0;i<(1<<k);i+=2*len)</pre>
                                                                                                        62
                                                                                                                   if(i==j)continue;
                                                                                                                                                                   for(int j=0;j<t;++j){</pre>
                                                                                                                                                            40
13
         for(int j=0;j<len;++j){</pre>
                                                                                                        63
                                                                                                                   lazy[j]=lazy[j]*m[i][i];
                                                                                                                                                                     x=mod mul(x,x,n);
           LL u=P[i+j],v=P[i+len+j];
14
                                                       8.9 Matrix.cpp
                                                                                                        64
                                                                                                                   T mx=m[j][i];
                                                                                                                                                                     if(x==1)return 0:
                                                                                                                                                            42
           if(!inverse){
                                                                                                        65
                                                                                                                   for(int k=0;k<c;++k)</pre>
                                                                                                                                                                     if(x==n-1)break;
             P[i+j]=v,P[i+len+j]=u+v;
16
                                                                                                                     m[j][k]=m[j][k]*m[i][i]-m[i][k]*mx
             //P[i+j]=u,P[i+len+j]=u+v; OR
17
                                                     1 template<typename T>
                                                                                                                                                                   if(x==n-1)continue;
                                                                                                                                                            45
                                                       struct Matrix{
                                                                                                        67
                                                                                                                                                            46
                                                                                                                                                                   return 0:
                                                         using rt = std::vector<T>;
                                                                                                        68
                                                                                                                                                            47
19
             P[i+j]=-u+v,P[i+len+j]=u;
                                                         using mt = std::vector<rt>;
                                                                                                               T det=sign?-1:1;
                                                                                                        69
                                                                                                                                                            48
                                                                                                                                                                 return 1;
20
             //P[i+j]=u,P[i+len+j]=v-u; OR
                                                         using matrix = Matrix<T>;
                                                                                                               for(int i=0;i<r;++i){</pre>
                                                         int r,c;
                                                                                                                 det = det*m[i][i];
21
                                                                                                        72
                                                                                                                 det = det/lazy[i];
22
                                                         Matrix(int r,int c):r(r),c(c),m(r,rt(c)){}
                                                                                                                 for(auto &j:m[i])j/=lazy[i];
                                                                                                       73
23
                                                         rt& operator[](int i){return m[i];}
                                                                                                                                                               8.11 NTT.cpp
                                                         matrix operator+(const matrix &a){
                                                                                                        75
                                                                                                               return det;
```

76 77 };

#### 8.7 LinearCongruence.cpp

matrix rev(r,c);

return rev;

13

14

15

16

for(int i=0;i<r;++i)</pre>

for(int j=0;j<c;++j)</pre>

rev[i][j]=m[i][j]+a.m[i][j];

matrix operator-(const matrix &a){

```
6 25*(2^22)+1.3
  template<typename T, typename VT=std::vector<
   struct NTT{
     const T P,G;
     NTT(T p=(1<<23)*7*17+1,T g=3):P(p),G(g){}
     unsigned int bit reverse(unsigned int a,
       a = ((a\&0x55555555U) << 1) | ((a\&0xAAAAAAAAU))
       a=((a&0x33333333U)<<2)|((a&0xCCCCCCCU)
13
       a=((a&0x0F0F0F0FU)<<4)|((a&0xF0F0F0F0U)
14
             >>4);
15
       a=((a&0x00FF00FFU)<<8)|((a&0xFF00FF00U)
       a=((a&0x0000FFFFU)<<16)|((a&0xFFFF0000U)
16
            >>16);
       return a>>(32-len);
17
18
19
       pow mod(T n,T k,T m){
20
       T ans=1:
21
       for(n=(n>=m?n%m:n);k;k>>=1){
         if(k&1)ans=ans*n%m;
22
23
         n=n*n%m:
24
25
       return ans;
26
     void ntt(bool is_inv,VT &in,VT &out,int N)
27
       int bitlen=std:: lg(N);
28
29
       for(int i=0;i<N;++i)out[bit reverse(i,</pre>
            bitlen) | = in[i];
       for(int step=2,id=1;step<=N;step<<=1,++</pre>
30
            id){
         T wn=pow mod(G,(P-1)>>id,P),wi=1,u,t;
31
         const int mh=step>>1;
32
33
         for(int i=0;i<mh;++i){</pre>
34
           for(int j=i;j<N;j+=step){</pre>
             u=out[j],t=wi*out[j+mh]%P;
35
36
             out[j]=u+t;
37
             out[j+mh]=u-t;
             if(out[j]>=P)out[j]-=P;
             if(out[j+mh]<0)out[j+mh]+=P;</pre>
39
           wi=wi*wn%P;
42
43
         for(int i=1;i<N/2;++i)std::swap(out[i</pre>
              ],out[N-i]);
         T invn=pow mod(N,P-2,P);
         for(int i=0;i<N;++i)out[i]=out[i]*invn 32</pre>
47
49
50 };
```

## 8.12 Simpson.cpp

```
double simpson(double a,double b){
   double c=a+(b-a)/2;
   return (F(a)+4*F(c)+F(b))*(b-a)/6;
```

#### 8.13 外星模運算.cpp

```
1 / a[0]^{(a[1]^a[2]^{...})}
 2 #include < bits / stdc++.h>
 3 using namespace std;
 4 #define maxn 1000000
 5 int euler[maxn+5];
 6 bool is prime[maxn+5];
   inline void init euler(){
     is_prime[1]=1;//一不是質數
     for(int i=1;i<=maxn;i++)euler[i]=i;</pre>
     for(int i=2;i<=maxn;i++){</pre>
11
       if(!is prime[i]){//是質數
         euler[i]--;
12
         for(int j=i<<1; j<=maxn; j+=i){</pre>
13
14
            is prime[j]=1;
            euler[j]=euler[j]/i*(i-1);
15
16
17
18
    }
19
20 inline long long pow(long long a,long long b
        , long long mod) {//a^b\%mod}
     long long ans=1;
     for(;b;a=a*a%mod,b>>=1)
       if(b&1)ans=ans*a%mod;
     return ans;
24
25
   bool isless(long long *a,int n,int k){
    if(*a==1)return k>1;
     if(--n==0)return *a<k;</pre>
     int next=0;
     for(long long b=1;b<k;++next)</pre>
       b*=*a:
     return isless(a+1,n,next);
34 long long high pow(long long *a,int n,long
        long mod){
     if(*a==1||--n==0)return *a%mod;
     int k=0,r=euler[mod];
     for(long long tma=1; tma!=pow(*a,k+r,mod)
          ;++k)
       tma=tma*(*a)%mod;
     if(isless(a+1,n,k))return pow(*a,high pow(
          a+1,n,k),mod);
     int tmd=high pow(a+1,n,r);
     int t=(tmd-k+r)%r;
     return pow(*a,k+t,mod);
```

## 8.14 模運算模板.cpp

for(int i=0;i<n;++i)scanf("%lld",&a[i]);</pre>

printf("%lld\n",high\_pow(a,n,mod));

44 long long a[1000005];

init euler();

#define n 4

while(t--){

return 0;

scanf("%d",&t);

scanf("%d",&mod);

int t, mod;

46 int main(){

47

49

51

52

53

54

55

```
1 template < typename T, long long mod>
2 struct mod t{//mod只能是質數
    T data:
    mod_t(){}
    mod t(const T &d):data((d%mod+mod)%mod){}
    mod t pow(T b)const{
       mod t ans(1);
       for(mod t now=*this;b;now=now*now,b/=2)
        if(b%2)ans=ans*now;
       return ans;
11
12
    mod t operator-(int)const{
       return mod_t(mod-data);
13
14
    mod_t operator+(const mod_t &b)const{
16
       return mod t((data+b.data)%mod);
17
    mod_t operator-(const mod_t &b)const{
       return mod t((data-b.data+mod)%mod);
20
21
    mod t operator*(const mod t &b)const{
       return mod t((data*b.data)%mod);
23
    mod t operator/(const mod t &b)const{
24
       return *this*b.pow(mod-2);//*this *
           Inverse(b)
26
    operator T()const{return data;}
    friend istream &operator>>(istream &i,
         mod t &b){
       T d:
29
30
       i>>d;
       b=mod t(d):
32
       return i;
33
34 };
```

## 8.15 **質因數分解.cpp**

```
1 LL func(const LL n,const LL mod,const int c)
{
2 return (LLmul(n,n,mod)+c+mod)%mod;
```

```
5 LL pollorrho(const LL n, const int c) {//循
        環節長度
     LL a=1, b=1;
     a=func(a,n,c)%n;
     b=func(b,n,c)%n; b=func(b,n,c)%n;
     while(gcd(abs(a-b),n)==1) {
       a=func(a,n,c)%n;
11
       b=func(b,n,c)%n; b=func(b,n,c)%n;
12
13
    return gcd(abs(a-b),n);
14
15
   void prefactor(LL &n, vector<LL> &v) {
    for(int i=0;i<12;++i) {</pre>
       while(n%prime[i]==0) {
         v.push back(prime[i]);
20
         n/=prime[i];
21
22
23
24
   void smallfactor(LL n, vector<LL> &v) {
    if(n<MAXPRIME) {</pre>
       while(isp[(int)n]) {
         v.push_back(isp[(int)n]);
         n/=isp[(int)n];
29
30
31
       v.push_back(n);
    } else {
32
       for(int i=0;i<primecnt&&prime[i]*prime[i</pre>
33
            |<=n;++i) {</pre>
         while(n%prime[i]==0) {
34
           v.push_back(prime[i]);
35
36
           n/=prime[i];
37
38
       if(n!=1) v.push back(n);
39
40
41
42
   void comfactor(const LL &n, vector<LL> &v) {
    if(n<1e9) {
       smallfactor(n,v);
46
       return:
47
48
     if(Isprime(n)) {
       v.push back(n);
       return;
51
52
     for(int c=3;;++c) {
54
       d = pollorrho(n,c);
55
       if(d!=n) break;
56
     comfactor(d,v);
     comfactor(n/d,v);
59
60
   void Factor(const LL &x, vector<LL> &v) {
    LL n = x;
    if(n==1) { puts("Factor 1"); return; }
    prefactor(n,v);
     if(n==1) return;
```

```
comfactor(n,v);
67
     sort(v.begin(),v.end());
68
69
    /oid AllFactor(const LL &n, vector<LL> &v) {
     vector<LL> tmp;
72
     Factor(n,tmp);
73
     v.clear();
74
     v.push back(1);
75
     int len;
76
     LL now=1;
77
     for(int i=0:i<tmp.size():++i) {</pre>
       if(i==0 || tmp[i]!=tmp[i-1]) {
78
79
         len = v.size():
80
         now = 1:
81
       now*=tmp[i]:
82
       for(int j=0;j<len;++j)</pre>
83
         v.push_back(v[j]*now);
84
85
```

#### other

#### 9.1 WhatDay.cpp

```
1 int whatday(int y,int m,int d){
      if(m <= 2)m += 12, -- y;
      if(y<1752||y==1752&&m<9||y==1752&&m==9&&
          return (d+2*m+3*(m+1)/5+y+y/4+5)%7;
      return (d+2*m+3*(m+1)/5+y+y/4-y/100+y
           /400)%7;
```

# 9.2 上下最大正方形.cpp

```
1 void solve(int n,int a[],int b[]){// 1-base
    int ans=0:
    deque<int>da,db;
    for(int l=1,r=1;r<=n;++r){</pre>
      while(da.size()&&a[da.back()]>=a[r]){
        da.pop_back();
      da.push back(r):
       while(db.size()&&b[db.back()]>=b[r]){
        db.pop back();
11
12
       db.push back(r);
       for(int d=a[da.front()]+b[db.front()];r-
           l+1>d;++1){
         if(da.front()==1)da.pop front();
15
        if(db.front()==1)db.pop front();
16
        if(da.size()&&db.size()){
17
           d=a[da.front()]+b[db.front()];
18
19
       ans=max(ans,r-l+1);
```

## 最大矩形.cpp

printf("%d\n",ans);

```
stack<pair<int.int > > st;
     st.push(make_pair(-1,0));
     s.push back(0);
     long long ans=0;
     for(size t i=0;i<s.size();++i){</pre>
       int h=s[i]:
       pair<int,int > now=make_pair(h,i);
       while(h<st.top().first){</pre>
         now=st.top();
10
11
         st.pop();
12
         ans=max(ans,(long long)(i-now.second)*
              now.first);
13
       if(h>st.top().first){
14
15
         st.push(make_pair(h,now.second));
16
17
18
     return ans;
```

1 | long long max rectangle(vector<int> s){

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

45

47

48

49

50

51

53

54

55

56

57

58

59

60

return ans;

/\*多串匹配走efL邊並傳回所有字串被s匹配成

while(!S[p].next[id]&&p)p=S[p].fail;

ans+=S[t].ed;/\*因為都走efl邊所以保

功的 次數0(N\*M^1.5)\*/

int ans=0,id,p=0,t;

p=S[p].next[id];

id=s[i]-L;

return ans;

for(int i=0;s[i];++i){

int match 1(const char \*s)const{

if(!S[p].next[id])continue;

for(t=S[p].efl;~t;t=S[t].efl){

if(S[p].ed)ans+=S[p].ed;

證 匹配 成 功 \*/

# String

## 10.1 AC 自動機.cpp

```
61
 1 template < char L='a', char R='z'>
                                                     62
   class ac automaton{
                                                     63
     private:
                                                     64
       struct joe{
         int next[R-L+1], fail, efl, ed, cnt dp, vis
                                                     66
         joe():ed(0),cnt_dp(0),vis(0){
                                                     67
            for(int i=0;i<=R-L;++i)next[i]=0;</pre>
                                                     68
       };
     public:
                                                     69
       std::vector<joe> S;
                                                     70
11
       std::vector<int> q;
                                                     71
12
       int qs,qe,vt;
                                                     72
13
       ac_automaton():S(1),qs(0),qe(0),vt(0){}
15
       void clear(){
                                                     74
                                                     75
16
         q.clear();
         S.resize(1);
         for(int i=0;i<=R-L;++i)S[0].next[i]=0;</pre>
         S[0].cnt_dp=S[0].vis=qs=qe=vt=0;
                                                     78
20
       void insert(const char *s){
                                                     79
22
         int o=0;
                                                     80
23
         for(int i=0,id;s[i];++i){
                                                     81
           id=s[i]-L;
25
            if(!S[o].next[id]){
              S.push back(joe());
```

```
/*枚舉(s的子字串nA)的所有相異字串各恰一
     S[o].next[id]=S.size()-1;
                                                   次並傳回次數O(N*M^(1/3))*/
   o=S[o].next[id];
                                               int match 2(const char *s){
                                        84
                                        85
                                                int ans=0,id,p=0,t;
 ++S[o].ed;
                                        86
                                        87
                                                /*把戳記vt+=1,只要vt沒溢位,所有S[p].
void build fail(){
 S[0].fail=S[0].efl=-1;
                                                 這種利用vt的方法可以0(1)歸零vis陣列*/
                                        88
  q.clear();
                                        89
                                                for(int i=0;s[i];++i){
 q.push_back(0);
                                        90
                                                  id=s[i]-L;
  ++ae;
                                        91
                                                  while(!S[p].next[id]&&p)p=S[p].fail;
  while(as!=ae){
                                        92
                                                  if(!S[p].next[id])continue;
   int pa=q[qs++],id,t;
                                        93
                                                  p=S[p].next[id];
   for(int i=0:i<=R-L:++i){</pre>
                                        94
                                                  if(S[p].ed&&S[p].vis!=vt){
     t=S[pa].next[i];
                                        95
                                                    S[p].vis=vt;
     if(!t)continue;
                                                    ans+=S[p].ed;
     id=S[pa].fail:
     while(~id&&!S[id].next[i])id=S[id
                                                   for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[
          1.fail;
     S[t].fail=~id?S[id].next[i]:0;
                                                    S[t].vis=vt;
     S[t].efl=S[S[t].fail].ed?S[t].fail 99
                                                    ans+=S[t].ed;/*因為都走efL邊所以保
          :S[S[t].fail].efl;
     q.push back(t);
                                       101
     ++qe;
                                       102
                                       103
                                                return ans;
 }
                                       104
                                               /*把AC自動機變成真的自動機*/
/*DP出每個前級在字串s出現的次數並傳回所
                                       105
                                       106
                                              void evolution(){
     有字串被s匹配成功的次數O(N+M)*/
                                                for(qs=1;qs!=qe;){
                                       107
int match_0(const char *s){
                                       108
                                                  int p=q[qs++];
 int ans=0,id,p=0,i;
                                                  for(int i=0;i<=R-L;++i)</pre>
  for(i=0;s[i];++i){
                                       109
                                                    if(S[p].next[i]==0)S[p].next[i]=S[
                                       110
   id=s[i]-L;
   while(!S[p].next[id]&&p)p=S[p].fail;
                                       111
   if(!S[p].next[id])continue;
                                       112
   p=S[p].next[id];
   ++S[p].cnt_dp;/*匹配成功則它所有後綴 113 };
        都可以被匹配(DP計算)*/
  for(i=qe-1;i>=0;--i){
   ans+=S[q[i]].cnt dp*S[q[i]].ed;
   if(~S[q[i]].fail)S[S[q[i]].fail].
        cnt dp+=S[q[i]].cnt dp;
```

#### 10.2 hash.cpp

```
1 | #define MAXN 1000000
2 #define prime mod 1073676287
3 /*prime mod 必須要是質數*/
  typedef long long T;
  char s[MAXN+5];
6 T h[MAXN+51:/*hash陣列*/
 7 T h_base[MAXN+5]; /*h_base[n]=(prime^n)%
       prime mod*/
  inline void hash init(int len,T prime=0
       xdefaced){
    h base[0]=1;
    for(int i=1;i<=len;++i){</pre>
      h[i]=(h[i-1]*prime+s[i-1])%prime mod;
      h base[i]=(h base[i-1]*prime)%prime mod;
14 }
15 inline T get_hash(int l,int r){/*閉區間寫
        法, 設編號為0 ~ Len-1*/
     return (h[r+1]-(h[1]*h_base[r-1+1])%
         prime mod+prime mod)%prime mod;
17 }
```

vis==vt就會變成false

t].ef1){

證匹配成功\*/

S[p].fail].next[i];

**if**(i==j)++j;

k=0;

#### 10.3 KMP.cpp return min(i,j);//傳回最小循環表示法起始位 1 /\*產生fail function\*/ inline void kmp\_fail(char \*s,int len,int \* fail){ int id=-1; 10.6 suffix array lcp.cpp fail[0]=-1; for(int i=1;i<len;++i){</pre> while(~id&&s[id+1]!=s[i])id=fail[id]; 1|#define radix\_sort(x,y){\ **if**(s[id+1]==s[i])++id; for(i=0;i<A;++i)c[i]=0;\</pre> fail[i]=id; for(i=0;i<n;++i)c[x[y[i]]]++;\</pre> for(i=1;i<A;++i)c[i]+=c[i-1];\</pre> 10 } for(i=n-1;~i;--i)sa[--c[x[y[i]]]]=y[i];\ /\*以字串B匹配字串A · 傳回匹配成功的數量(用B的 **#define** sac(r,a,b) r[a]!=r[b]||a+k>=n||r[a+k inline int kmp\_match(char \*A,int lenA,char \* ]!=r[b+k] B,int lenB,int \*fail){ 8 void suffix\_array(const char \*s,int n,int \* int id=-1.ans=0: sa,int \*rank,int \*tmp,int \*c){ for(int i=0;i<lenA;++i){</pre> int A='z'+1,i,k,id=0; while(~id&&B[id+1]!=A[i])id=fail[id]; for(i=0;i<n;++i)rank[tmp[i]=i]=s[i];</pre> if(B[id+1]==A[i])++id; radix sort(rank,tmp); if(id==lenB-1){/\*匹配成功\*/ for(k=1;id<n-1;k<<=1){</pre> 12 ++ans; 13 for(id=0,i=n-k;i<n;++i)tmp[id++]=i;</pre> id=fail[id]; 19 for(i=0;i<n;++i)if(sa[i]>=k)tmp[id++]=sa 20 21 radix sort(rank,tmp); 15 return ans; 16 swap(rank,tmp); for(rank[sa[0]]=id=0,i=1;i<n;++i)</pre> rank[sa[i]]=id+=sac(tmp,sa[i-1],sa[i]) 23 A=id+1; 10.4 manacher.cpp 20 21 | } 22 //h: 高度數組 sa:後綴數組 rank:排名 void suffix\_array\_lcp(const char \*s,int len, 1 //原字串: asdsasdsa int \*h,int \*sa,int \*rank){ 2 // 先把字串變成這樣: @#a#s#d#s#a#s#d#s#a# for(int i=0;i<len;++i)rank[sa[i]]=i;</pre> 3 inline void manacher(char \*s,int len,int \*z) for(int i=0,k=0;i<len;++i){</pre> if(rank[i]==0)continue; 26 int l=0,r=0; **if**(k)--k; 27 for(int i=1;i<len;++i){</pre> while(s[i+k]==s[sa[rank[i]-1]+k])++k; z[i]=r>i?min(z[2\*l-i],r-i):1; h[rank[i]]=k; 29 while(s[i+z[i]]==s[i-z[i]])++z[i]; 30 **if**(z[i]+i>r)r=z[i]+i,l=i; h[0]=0; 31 10.5 minimal string rotation.cp 10.7 Z.cpp 1 inline void z alg(char \*s,int len,int \*z){ int min string rotation(const string &s){ int l=0,r=0; int n=s.size(),i=0,j=1,k=0; while(i<n&&j<n&&k<n){</pre> for(int i=1;i<len;++i){</pre> int t=s[(i+k)%n]-s[(j+k)%n]; z[i]=i>r?0:(i-l+z[i-l]<z[l]?z[i-l]:r-i if(t){ while(i+z[i]<len&&s[i+z[i]]==s[z[i]])++z**if**(t>0)i+=k; else j+=k;

```
Tarjan
```

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if(i+z[i]-1>r)r=i+z[i]-1,l=i;

## 11.1 dominator tree.cpp

```
11.2 tnfshb017 2 sat.cpp
1 | struct dominator_tree{
   static const int MAXN=5005;
   int n;// 1-base
                                                  1 | #include < bits / stdc++.h>
   vector<int> suc[MAXN],pre[MAXN];
                                                    using namespace std;
   int fa[MAXN],dfn[MAXN],id[MAXN],Time;
                                                    #define MAXN 8001
   int semi[MAXN],idom[MAXN];
                                                    #define MAXN2 MAXN*4
   int anc[MAXN], best[MAXN];//disjoint set
                                                    #define n(X) ((X)+2*N)
   vector<int> dom[MAXN];//dominator tree
                                                    vector<int> v[MAXN2];
   void init(int n){
                                                    vector<int> rv[MAXN2];
                                                    vector<int> vis t:
     for(int i=1;i<=n;++i)suc[i].clear(),pre[</pre>
                                                    int N,M;
          i].clear();
                                                   void addedge(int s,int e){
                                                        v[s].push back(e);
   void add edge(int u,int v){
                                                        rv[e].push_back(s);
     suc[u].push_back(v);
                                                 13
     pre[v].push_back(u);
                                                   int scc[MAXN2];
                                                   bool vis[MAXN2]={false};
   void dfs(int u){
                                                    void dfs(vector<int> *uv,int n,int k=-1){
     dfn[u]=++Time,id[Time]=u;
                                                        vis[n]=true;
     for(auto v:suc[u]){
                                                        for(int i=0;i<uv[n].size();++i)</pre>
       if(dfn[v])continue;
                                                            if(!vis[uv[n][i]])
        dfs(v),fa[dfn[v]]=dfn[u];
                                                 20
                                                                dfs(uv,uv[n][i],k);
                                                        if(uv==v)vis_t.push_back(n);
                                                 22
                                                        scc[n]=k;
   int find(int x){
                                                 23
     if(x==anc[x])return x;
                                                 24
                                                   void solve(){
     int y=find(anc[x]);
                                                        for(int i=1;i<=N;++i){</pre>
     if(semi[best[x]]>semi[best[anc[x]]])best
                                                            if(!vis[i])dfs(v,i);
          [x]=best[anc[x]];
                                                            if(!vis[n(i)])dfs(v,n(i));
     return anc[x]=y;
                                                 28
                                                 29
                                                        memset(vis,0,sizeof(vis));
   void tarjan(int r){
                                                 30
                                                        int c=0:
     Time=0:
                                                        for(int i=vis_t.size()-1;i>=0;--i)
     for(int t=1;t<=n;++t){</pre>
                                                            if(!vis[vis t[i]])
        dfn[t]=idom[t]=0;//u=r或是u無法到達r時
                                                                dfs(rv,vis t[i],c++);
             idom[id[u]]=0
                                                 34
        dom[t].clear();
                                                 35
                                                   int main(){
        anc[t]=best[t]=semi[t]=t;
                                                        int a,b;
                                                        scanf("%d%d",&N,&M);
     dfs(r);
                                                        for(int i=1;i<=N;++i){</pre>
     for(int y=Time;y>=2;--y){
                                                            // (A or B)&(!A & !B) A^B
       int x=fa[y],idy=id[y];
                                                            a=i*2-1;
        for(auto z:pre[idy]){
                                                 41
                                                            b=i*2;
                                                            addedge(n(a),b);
          if(!(z=dfn[z]))continue;
          find(z);
                                                            addedge(n(b),a);
          semi[y]=min(semi[y],semi[best[z]]);
                                                            addedge(a,n(b));
                                                            addedge(b,n(a));
        dom[semi[y]].push back(y);
                                                 46
                                                        while(M--){
        anc[y]=x;
                                                 47
        for(auto z:dom[x]){
                                                            scanf("%d%d",&a,&b);
         find(z);
                                                            a = a>0?a*2-1:-a*2;
          idom[z]=semi[best[z]]<x?best[z]:x;</pre>
                                                            b = b>0?b*2-1:-b*2;
                                                            // A or B
        dom[x].clear();
                                                 52
                                                            addedge(n(a),b);
                                                            addedge(n(b),a);
     for(int u=2;u<=Time;++u){</pre>
       if(idom[u]!=semi[u])idom[u]=idom[idom[
                                                        solve();
                                                        bool check=true;
        dom[id[idom[u]]].push back(id[u]);
```

for(int i=1;i<=2\*N;++i)</pre>

57 58 }dom;

```
if(scc[i]==scc[n(i)])
                check=false;
59
       if(check){
60
           printf("%d\n",N);
61
           for(int i=1;i<=2*N;i+=2){</pre>
62
                if(scc[i]>scc[i+2*N])
63
64
                    putchar('+');
65
                    putchar('-');
68
           putchar('\n');
69
       }else puts("0");
       return 0;
70
```

#### 11.3 橋連通分量.cpp

```
1 #define N 1005
2 struct edge{
    int u,v;
    bool is bridge:
    edge(int u=0,int v=0):u(u),v(v),is bridge
  };
  vector<edge> E;
  vector<int> G[N];// 1-base
  int low[N], vis[N], Time;
int bcc_id[N],bridge_cnt,bcc_cnt;// 1-base
int st[N],top;//BCC用
inline void add edge(int u,int v){
    G[u].push back(E.size());
    E.push back(edge(u,v));
    G[v].push back(E.size());
16
    E.push back(edge(v,u));
17 }
18 | void dfs(int u,int re=-1){//u當前點,re為u連
       接前一個點的邊
    int v;
    low[u]=vis[u]=++Time;
20
    st[top++]=u:
    for(size_t i=0;i<G[u].size();++i){</pre>
22
      int e=G[u][i];v=E[e].v;
23
24
      if(!vis[v]){
25
        dfs(v,e^1);//e^1反向邊
26
        low[u]=min(low[u],low[v]);
27
        if(vis[u]<low[v]){</pre>
          E[e].is bridge=E[e^1].is bridge=1;
29
           ++bridge_cnt;
      }else if(vis[v]<vis[u]&&e!=re)</pre>
        low[u]=min(low[u], vis[v]);
32
33
    if(vis[u]==low[u]){//處理BCC
34
35
      ++bcc_cnt;// 1-base
      do bcc id[v=st[--top]]=bcc cnt;//每個點
            所在的BCC
37
       while(v!=u);
38
39
   inline void bcc init(int n){
    Time=bcc_cnt=bridge_cnt=top=0;
```

E.clear();

```
for(int i=1;i<=n;++i){</pre>
       G[i].clear();
44
45
       vis[i]=bcc_id[i]=0;
46
47 }
```

1 | #define N 1005

## 11.4 雙連通分量 & 割點.cpp

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39

40

43 }

```
vector<int> G[N];// 1-base
 3 | vector<int> bcc[N]: //存每塊雙連通分量的點
 4 int low[N], vis[N], Time;
 5 int bcc_id[N],bcc_cnt;// 1-base
 6 bool is_cut[N];//是否為割點
  int st[N],top;
   void dfs(int u,int pa=-1){//u當前點,pa父親
    int v.child=0:
    low[u]=vis[u]=++Time;
11
     st[top++]=u;
     for(size_t i=0;i<G[u].size();++i){</pre>
12
      if(!vis[v=G[u][i]]){
         dfs(v,u),++child;
15
         low[u]=min(low[u],low[v]);
16
         if(vis[u]<=low[v]){</pre>
17
           is cut[u]=1;
           bcc[++bcc_cnt].clear();
18
19
           int t;
20
            bcc_id[t=st[--top]]=bcc_cnt;
21
             bcc[bcc cnt].push back(t);
22
           }while(t!=v);
23
           bcc_id[u]=bcc_cnt;
24
           bcc[bcc cnt].push back(u);
25
26
      }else if(vis[v]<vis[u]&&v!=pa)//反向邊
27
         low[u]=min(low[u], vis[v]);
29
    if(pa==-1&&child<2)is_cut[u]=0;//u是dfs樹
30
          的根要特判
31
32 inline void bcc init(int n){
     Time=bcc cnt=top=0;
34
     for(int i=1;i<=n;++i){</pre>
35
      G[i].clear();
      is_cut[i]=vis[i]=bcc_id[i]=0;
36
37
```

# Tree problem

### 12.1 HeavyLight.cpp

```
1 | #include < vector >
2 #define MAXN 100005
3 typedef std::vector<int >::iterator VIT;
4 int siz[MAXN], max son[MAXN], pa[MAXN], dep[
       MAXN];
```

```
5 int link top[MAXN],link[MAXN],cnt;
                                                   inline int find_lca(int a,int b){
6 std::vector<int >G[MAXN];
 void find max son(int x){
                                                     if(dep[a]>dep[b])swap(a,b);
                                                     b=jump(b,dep[b]-dep[a]);
   siz[x]=1;
    \max son[x]=-1;
                                                     if(a==b)return a;
    for(VIT i=G[x].begin();i!=G[x].end();++i){
                                                     for(int i=MAX LOG;i>=0;--i){
      if(*i==pa[x])continue;
                                                       if(pa[i][a]!=pa[i][b]){
      pa[*i]=x;
                                                25
                                                         a=pa[i][a];
      dep[*i]=dep[x]+1;
                                                26
                                                         b=pa[i][b];
      find_max_son(*i);
                                                27
      if(max son[x]==-1||siz[*i]>siz[max son[x 28
           ]]) max son[x]=*i;
                                                     return pa[0][a];
                                                29
      siz[x]+=siz[*i];
  void build link(int x,int top){
   link[x]=++cnt:
   link_top[x]=top;
    if(max son[x]==-1)return;
                                                  1 | struct splay_tree{
```

```
build link(max son[x],top);
 for(VIT i=G[x].begin();i!=G[x].end();++i){
                                              int ch[2],pa;//子節點跟父母
   if(*i==max son[x]||*i==pa[x])continue;
   build link(*i,*i):
                                           5 };
inline int find lca(int a,int b){
 //求LCA,可以在過程中對區間進行處理
 int ta=link top[a],tb=link top[b];
 while(ta!=tb){
   if(dep[ta]<dep[tb]){</pre>
     std::swap(ta,tb);
     std::swap(a,b);
                                          11
   //這裡可以對a所在的鏈做區間處理
   //區間為(Link[ta],Link[a])
   ta=link top[a=pa[ta]];
 //最後a,b會在同一條鏈·若a!=b還要在進行一
      次區間處理
 return dep[a]<dep[b]?a:b;</pre>
                                          17
```

#### 12.2 LCA.cpp

```
1 | #define MAXN 100000
2 #define MAX LOG 17
3 int pa[MAX_LOG+1][MAXN+5];
4 int dep[MAXN+5];
 5 vector<int>G[MAXN+5];
6 void dfs(int x, int p){//dfs(1,-1)};
    pa[0][x]=p;
     for(int i=0;i+1<MAX_LOG;++i)pa[i+1][x]=pa[</pre>
         i][pa[i][x]];
     for(auto &i:G[x]){
      if(i==p)continue;
11
       dep[i]=dep[x]+1;
12
       dfs(i,x);
13
15 inline int jump(int x, int d){
16 for(int i=0;i<d;++i)if((x>>i)&1)x=pa[k][x];
    return x;
```

#### 12.3 link cut tree.cpp

```
bool rev;//反轉的懶惰標記
    splay tree():pa(0),rev(0){ch[0]=ch[1]=0;}
 6 vector<splay tree> node;
7 //有的時候用vector會TLE,要注意
8 // 這邊以node [0] 作為null 節點
9 bool isroot(int x){//判斷是否為這棵splay
       tree的根
    return node[node[x].pa].ch[0]!=x&&node[
         node[x].pa].ch[1]!=x;
12 void down(int x){// 懶惰標記下推
    if(node[x].rev){
      if(node[x].ch[0])node[node[x].ch[0]].rev
      if(node[x].ch[1])node[node[x].ch[1]].rev
           ^=1;
      std::swap(node[x].ch[0],node[x].ch[1]);
      node[x].rev^=1;
18
19 }
  void push_down(int x){//將所有祖先的懶惰標記
    if(!isroot(x))push_down(node[x].pa);
22
    down(x);
23
  | void up(int x){}//將子節點的資訊向上更新
  void rotate(int x){//旋轉,會自行判斷轉的方
    int y=node[x].pa,z=node[y].pa,d=(node[y].
26
         ch[1]==x);
    node[x].pa=z;
    if(!isroot(y))node[z].ch[node[z].ch[1]==y
    node[y].ch[d]=node[x].ch[d^1];
29
    node[node[y].ch[d]].pa=y;
    node[y].pa=x,node[x].ch[d^1]=y;
31
32
    up(y),up(x);
33
34 void splay(int x){//將節點x伸展到所在splay
       tree的根
    push down(x);
    while(!isroot(x)){
```

```
int y=node[x].pa;
                                                99 int find root(int x){
      if(!isroot(y)){
38
                                                     x=access(x);
         int z=node[v].pa;
                                                     while(node[x].ch[0])x=node[x].ch[0];
39
40
         if((node[z].ch[0]==y)^(node[y].ch[0]== 102
                                                     splay(x);
                                                     return x;
             x))rotate(v);
                                               103
41
         else rotate(x);
                                               104 }
42
                                               int query(int u,int v){
43
      rotate(x);
                                               106 | //傳回uv路徑splay tree的根結點
44
                                               107 // 這種寫法無法求LCA
45
                                               108
                                                     make root(u);
   int access(int x){
46
                                                     return access(v);
                                               109
    int last=0:
47
                                               110 }
    while(x){
48
                                               int query_lca(int u,int v){
49
      splav(x):
                                               112 | //假設求鏈上點權的總和·sum是子樹的權重和
50
      node[x].ch[1]=last;
                                                        data 是 節 點 的 權 重
51
      up(x);
                                                     access(u);
                                               113
52
      last=x:
                                               114
                                                     int lca=access(v);
53
      x=node[x].pa;
                                                     splay(u);
                                               115
54
                                                     if(u==lca){
55
    return last;//回傳access後splay tree的根
                                                       //return node[lca].data+node[node[lca].
56
                                                            ch[1]].sum
57 | void access(int x, bool is=0){//is=0就是一般
                                                     }else{
       的access
                                                       //return node[lca].data+node[node[lca].
    int last=0;
                                                            ch[1]].sum+node[u].sum
    while(x){
59
                                                120
60
       splay(x);
                                               121 }
61
       if(is&&!node[x].pa){
                                                122 struct EDGE{
        //printf("%d\n", max(node[last].ma, node 123
62
                                                    int a,b,w;
             [node[x].ch[1]].ma));
                                               124 }e[10005];
63
                                                125 int n:
64
      node[x].ch[1]=last;
                                               126 vector<pair<int ,int > >G[10005];
65
      up(x);
                                               127 | //first表示子節點 · second表示邊的編號
66
      last=x:
                                               128 int pa[10005],edge_node[10005];
67
      x=node[x].pa;
                                               129 | //pa 是父母節點,暫存用的,edge node 是每個編
68
                                                        被存在哪個點裡面的陣列
69
                                                130 void bfs(int root){
   void query_edge(int u,int v){
                                               131 //在建構的時候把每個點都設成一個splay tree
    access(u);
71
                                                        不會壞掉
72
    access(v,1);
73
                                               132
                                                     queue<int > q;
   void make root(int x){
                                               133
                                                      for(int i=1;i<=n;++i)pa[i]=0;</pre>
    access(x),splay(x);
                                               134
                                                     a.push(root);
    node[x].rev^=1;
                                               135
                                                     while(q.size()){
76
                                                       int u=q.front();
                                               136
77
   void make_root(int x){
                                               137
                                                       q.pop();
    node[access(x)].rev^=1;
                                                       for(int i=0;i<(int)G[u].size();++i){</pre>
                                               138
                                                         int v=G[u][i].first;
80
    splay(x);
                                               139
                                               140
                                                         if(v!=pa[u]){
81
                                               141
                                                           pa[v]=u:
   void cut(int x,int y){
    make_root(x);
                                               142
                                                            node[v].pa=u;
                                               143
                                                            node[v].data=e[G[u][i].second].w;
    access(v);
                                               144
                                                            edge node[G[u][i].second]=v;
    splay(y);
                                               145
                                                           up(v);
    node[y].ch[0]=0;
                                                           q.push(v);
    node[x].pa=0;
                                               146
88
                                               147
   void cut_parents(int x){
                                               148
    access(x);
                                               149
                                               150
    splay(x);
                                                   void change(int x,int b){
    node[node[x].ch[0]].pa=0;
                                               151
                                                     splay(x);
    node[x].ch[0]=0;
                                               152
93
                                               153
                                                     //node[x].data=b;
94
                                                     up(x);
   void link(int x,int y){
                                               154
    make root(x);
                                               155 }
    node[x].pa=y;
98
```

#### 12.4 POJ\_tree.cpp

1 | #include < bits / stdc++.h>

```
using namespace std;
 3 #define MAXN 10005
 4 int n,k;
 5 vector<pair<int,int> >g[MAXN];
 6 int size[MAXN];
 7 bool vis[MAXN];
 8 inline void init(){
    for(int i=0;i<=n;++i){</pre>
       g[i].clear();
       vis[i]=0;
12
    }
13 }
  void get dis(vector<int> &dis,int u,int pa,
     dis.push back(d);
     for(size t i=0;i<g[u].size();++i){</pre>
       int v=g[u][i].first,w=g[u][i].second;
17
18
       if(v!=pa&&!vis[v])get dis(dis,v,u,d+w);
19
21 | vector < int > dis; // 這東西如果放在函數裡會TLE
  int cal(int u,int d){
     dis.clear():
     get_dis(dis,u,-1,d);
25
     sort(dis.begin(),dis.end());
     int l=0,r=dis.size()-1,res=0;
27
     while(l<r){
       while(l<r&&dis[l]+dis[r]>k)--r;
28
29
       res+=r-(1++);
30
31
    return res;
32
  pair<int,int> tree centroid(int u,int pa,
        const int sz){
     size[u]=1;//找樹重心, second是重心
34
     pair<int, int> res(INT_MAX, -1);
35
     int ma=0;
36
     for(size_t i=0;i<g[u].size();++i){</pre>
37
       int v=g[u][i].first;
38
       if(v==pa||vis[v])continue;
39
       res=min(res,tree_centroid(v,u,sz));
40
41
       size[u]+=size[v];
42
       ma=max(ma,size[v]);
43
     ma=max(ma,sz-size[u]);
45
     return min(res, make pair(ma,u));
46
47
   int tree DC(int u,int sz){
     int center=tree centroid(u,-1,sz).second;
     int ans=cal(center,0);
50
     vis[center]=1;
     for(size_t i=0;i<g[center].size();++i){</pre>
       int v=g[center][i].first,w=g[center][i].
52
            second:
53
       if(vis[v])continue;
54
       ans-=cal(v,w);
55
       ans+=tree DC(v,size[v]);
56
57
     return ans;
58
59
  int main(){
     while(scanf("%d%d",&n,&k),n||k){
```

```
init();
62
       for(int i=1;i<n;++i){</pre>
63
         int u,v,w;
         scanf("%d%d%d",&u,&v,&w);
64
65
         g[u].push back(make pair(v,w));
66
         g[v].push back(make pair(u,w));
67
       printf("%d\n",tree_DC(1,n));
68
69
70
     return 0;
71
```

#### 13 zformula

#### 13.1 formula.tex

#### 13.1.1 Pick 公式

給定頂點坐標均是整點的簡單多邊形 $\cdot$  面積 = 內部格點數 + 邊上格點數/2-1

#### 13.1.2 圖論

- 1. V E + F = 2
- 2. 對於平面圖  $\cdot F = E V + n + 1 \cdot n$  是連通分量
- 3. 對於平面圖  $\cdot E \leq 3V 6$
- 4. 對於連通圖 G·最大獨立點集的大小設為 I(G)·最大匹配大小設為 M(G)·最小點覆蓋設為 Cv(G)·最小邊覆蓋設為 Ce(G)。對於任意連通圖:
  - $\begin{array}{ll} \text{(a)} & I(G)+Cv(G)=|V| \\ \text{(b)} & M(G)+Ce(G)=|V| \end{array}$
- 5. 對於連通二分圖:
  - (a) I(G) = Cv(G)(b) M(G) = Ce(G)
- 6. 最大權閉合圖:
  - (a)  $C(u, V) = \infty, (u, v) \in E$ (b)  $C(S, v) = W_v, W_v > 0$ (c)  $C(v, T) = -W_v, W_v < 0$
- 7. 最大密度子圖:
  - (a)  $C(u, v) = 1, (u, v) \in E$
  - (b)  $C(S, v) = U_v, v \in V$ (c)  $C(v, T) = U + 2g - d_v, v \in V$
- 8. 弦圖:
  - (a) 完美消除序列從後往前依次給每個點染色,給 每個點染上可以染的最小顏色
  - b) 最大團大小 = 色數
  - (c) 最大獨立集: 完美消除序列從前往後能選就選
  - (d) 最小團覆蓋: 最大獨立集的點和他延伸的邊構成
  - (e) 區間圖是茲圖
  - (f) 區間圖的完美消除序列: 將區間按造又端點由 小到大排序
  - (g) 區間圖染色: 用線段樹做

```
1 double l=0,=m,stop=1.0/n/n;
  while(r-l>=stop){
    double(mid);
    if((n*m-sol.maxFlow(s,t))/2>eps)l=mid;
    else r=mid;
7 build(1):
  sol.maxFlow(s,t);
9 vector<int> ans;
10 for(int i=1;i<=n;++i)
if(sol.vis[i])ans.push back(i);
```

#### 13.1.3 學長公式

- 1.  $\sum_{d|n} phi(n) = n$
- 2.  $g(n) = \sum_{d|n} f(d) = f(n) = \sum_{d|n} mu(d) *$
- 3.  $HarmonicseriesH_n = ln(n) + \gamma + 1/(2n) 1/(12n^2) + 1/(120n^4)$
- 4.  $\gamma = 0.57721566490153286060651209008240243104215$
- 5. 格雷碼 =  $n \oplus (n >> 1)$
- 6.  $SG(A+B) = SG(A) \oplus SG(B)$

#### 13.1.4 基本數論

- 1.  $\sum_{d|n} \mu(n) = (n == 1)$
- 2.  $g(m) = \sum_{d|m} f(d) \Leftrightarrow f(m) = \sum_{d|m} \mu(d) *$
- 3.  $\sum_{i=1}^{n} \sum_{j=1}^{m} \overline{\Delta} = \sum_{j=1}^{m} \mu(d) \left\lfloor \frac{n}{d} \right\rfloor \left\lfloor \frac{m}{d} \right\rfloor$ 4.  $\sum_{i=1}^{n} \sum_{j=1}^{n} lcm(i,j) = n \sum_{d|n} d\phi(d)$

## 13.1.5 排組公式

- 1. k 卡特蘭  $\frac{C_n^{kn}}{n(k-1)+1} \cdot C_m^n = \frac{n!}{m!(n-m)!}$
- 2.  $H(n,m) \cong x_1 + x_2 \dots + x_n = k, num = C_k^{n+k-1}$
- 3. Stirling number of  $2^{nd}$ , n 人分 k 組方法數目
  - (a) S(0,0) = S(n,n) = 1
  - (b) S(n,0) = 0
- (c) S(n,k) = kS(n-1,k) + S(n-1,k-1)
- 4. Bell number, n 人分任意多組方法數目
  - (a)  $B_0 = 1$

  - (a)  $B_0 = 1$ (b)  $B_n = \sum_{i=0}^n S(n, i)$ (c)  $B_{n+1} = \sum_{k=0}^n C_k^k B_k$ (d)  $B_{p+n} \equiv B_n + B_{n+1} mod p$ , p is prime (e)  $B_p m_{+n} \equiv m B_n + B_{n+1} mod p$ , p is prime
  - (f) From B0:1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, 115975
- 5. Derangement, 錯排, 沒有人在自己位置上
  - (a)  $D_n = n!(1 \frac{1}{1!} + \frac{1}{2!} \frac{1}{3!} \dots + (-1)^n \frac{1}{n!})$ (b)  $D_n = (n-1)(D_{n-1} + D_{n-2}), D_0 =$  $1, D_1 = 0$
  - (c) From D0:1, 0, 1, 2, 9, 44, 265, 1854, 14833, 133496

#### 13.1.6 冪次, 冪次和

- 1.  $a^b \% P = a^{b\% \varphi(p) + \varphi(p)}, b > \varphi(p)$
- 2.  $1^3 + 2^3 + 3^3 + \ldots + n^3 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4}$
- 3.  $1^4 + 2^4 + 3^4 + \ldots + n^4 = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} \frac{n}{30}$
- 4.  $1^5 + 2^5 + 3^5 + \ldots + n^5 = \frac{n^6}{6} + \frac{n^5}{2} + \frac{5n^4}{12} \frac{n^2}{12}$ 5.  $0^k + 1^k + 2^k + \ldots + n^k = P(k), P(k) =$
- $\frac{(n+1)^{k+1} \sum_{i=0}^{k-1} C_i^{k+1} P(i)}{\sum_{i=0}^{k-1} C_i^{k}}, P(0) = n+1$ 6.  $\sum_{k=0}^{m-1} k^n = \frac{1}{n+1} \sum_{k=0}^n C_k^{n+1} B_k m^{n+1-k}$
- 7.  $\sum_{i=0}^{m} C_i^{m+1} B_i = 0, B_0 = 1$
- 8. 除了  $B_1 = -1/2$  · 剩下的奇數項都是 0
- 9.  $B_2 = 1/6, B_4 = -1/30, B_6 = 1/42, B_8 = 1/42$  $-1/30, B_{10} = 5/66, B_{12} = -691/2730, B_{14} = \frac{14}{15}$  $7/6, B_{16} = -3617/510, B_{18}$  $43867/798, B_{20} = -174611/330,$ 17

- 1.  $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- 2.  $X^g = t^{c(g)}$
- 3. G 表示有幾種轉法, $X^g$  表示在那種轉法下,有幾種  $^{23}$ 是會保持對稱的 $\cdot t$  是顏色數 $\cdot c(g)$  是循環節不動的  $^{24}$
- 4. 正立方體塗三顏色,轉 0 有 36 個元素不變,轉 90 有 6 種, 每種有 3<sup>3</sup> 不變, 180 有 3 × 3<sup>4</sup> 120(角) 有  $8 \times 3^2 \cdot 180(邊)$  有  $6 \times 3^3 \cdot$  全部  $\frac{1}{24} \left( 3^{6} + 6 \times 3^{3} + 3 \times 3^{4} + 8 \times 3^{2} + 6 \times 3^{3} \right) =$

## 2 import java.util.\*; 3 import java.math.\*; 4 import java.text.\*; public class Main

```
throws FileNotFoundException,
  IOException
Scanner sc = new Scanner(new FileReader(
```

pw.println("Case #"+ci+": easy for

pw.close();//关闭流并释放,这个很重要,

public static void main(String args[])

PrintWriter pw = new PrintWriter(new FileWriter("a.out")); int n,m;

for(ci=1; ci<=c; ++ci)</pre>

output");

否则是没有输出的

sc.close();// 关闭流并释放

1 import java.io.\*;

10

11

18

19

20 21

n=sc.nextInt();//读入下一个INTm=sc.nextInt(); = 16

#### 13.1.7 Burnside's lemma

# 13.2.2 优先队列

#### 13.1.8 Count on a tree

- 1. Rooted tree:  $s_{n+1} = \frac{1}{n} \sum_{i=1}^{n} (i \times a_i \times a_i)$
- 2. Unrooted tree:

  - (a) Odd: $a_n \sum_{i=1}^{n/2} a_i a_{n-i}$ (b) Even: $Odd + \frac{1}{2} a_{n/2} (a_{n/2} + 1)$
- 3. Spanning Tree
  - (a) 完全圖  $n^n 2$
  - (b) 一般圖 (Kirchhoff's theorem)M[i][i] = $degree(V_i), M[i][j] = -1, if have E(i, j), 0$ if no edge. delete any one row and col in A, ans = det(A)

#### 13.2 java.tex

#### 13.2.1 文件操作

```
1 | PriorityQueue queue = new PriorityQueue( 1,
      new Comparator()
   public int compare( Point a, Point b )
   if(a.x < b.x | | a.x == b.x && a.y < b.y)
     return -1;
   else if( a.x == b.x && a.y == b.y )
     return 0:
     return 1;
```

#### 13.2.3 Map

```
1 | Map map = new HashMap();
2 map.put("sa","dd");
3 String str = map.get("sa").toString;
5 for(Object obj : map.keySet()){
   Object value = map.get(obj );
```

```
13.2.4 sort
```

```
1 static class cmp implements Comparator
     public int compare(Object o1,Object o2)
     BigInteger b1=(BigInteger)o1;
     BigInteger b2=(BigInteger)o2;
    return b1.compareTo(b2);
  public static void main(String[] args)
       throws IOException
11
    Scanner cin = new Scanner(System.in);
12
     int n;
    n=cin.nextInt();
     BigInteger[] seg = new BigInteger[n];
     for (int i=0;i<n;i++)</pre>
    seg[i]=cin.nextBigInteger();
    Arrays.sort(seg,new cmp());
```

ACM ICPC		2.8	整體二分.cpp	6		anguage 5.1 CNF.cpp	<b>11</b> 11	10.4 manacher.cpp	
Team	3	3.1 3.2	ault debug.cpp	<b>6</b> 6		Linear_Programming 7.1 最大密度子圖.cpp	<b>11</b> 11	10.6 suffix_array_lcp.cpp	
Reference -	_	3.3	IncStack.cpp input.cpp	$\frac{6}{6}$	8 ]	Number_Theory 3.1 basic.cpp	11	11.1 dominator_tree.cpp	
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		4.2 4.3	ISAP_with_cut.cpp MinCostMaxFlow.cpp	7	8	FWT.cpp	13	12 Tree_problem         12.1 HeavyLight.cpp         12.2 LCA.cpp	
Contents	5	5.1 5.2	aph Augmenting_Path.cpp Augmenting_Path_multiple.cpp		8	8.8 Lucas.cpp	13 13	12.3 link_cut_tree.cpp	17
1 Computational_Geometry 1.1 Geometry.cpp 1.2 SmallestCircle.cpp 1.3 最近點對.cpp 1.4 浮點數誤差模板.cpp	. 3	5.2 5.3 5.4 5.5 5.6 5.7 5.8	blossom_matching.cpp graphISO.cpp	8 8 8 8 8 Match	8 8 8 8 8 ing.	3.10 MillerRobin.cpp	13 14 14 14 14	13 zformula 13.1 formula.tex	18 18 19 19
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