

# 1 Computational\_Geometry

## 1.1 Geometry.cpp

```

1 const double PI=atan2(0.0,-1.0);
2 template<typename T>
3 struct point{
4     T x,y;
5     point(){
6     point(const T&x,const T&y):x(x),y(y){
7     point operator+(const point &b)const{
8         return point(x+b.x,y+b.y);
9     point operator-(const point &b)const{
10        return point(x-b.x,y-b.y);
11    point operator*(const T &b)const{
12        return point(x*b,y*b);
13    point operator/(const T &b)const{
14        return point(x/b,y/b);
15    bool operator==(const point &b)const{
16        return x==b.x&&y==b.y;
17    T dot(const point &b)const{
18        return x*b.x+y*b.y;
19    T cross(const point &b)const{
20        return x*b.y-y*b.x;
21    point normal()const{//求法向量
22        return point(-y,x);
23    T abs2()const{//向量長度的平方
24        return dot(*this);
25    }
26    T rad(const point &b)const{//兩向量的弧度
27        return fabs(atan2(fabs(cross(b)),dot(b)));
28    }
29    T getA()const{//對x軸的弧度
30        T A=atan2(y,x);{//超過180度會變負的
31        if(A<=-PI/2)A+=PI*2;
32        return A;
33    }
34};
35template<typename T>
36struct line{
37    line(){
38    point<T> p1,p2;
39    T a,b,c;//ax+by+c=0
40    line(const point<T>&x,const point<T>&y):p1(x),p2(y){
41    void pton()const{//轉成一般式
42        a=p1.y-p2.y;
43        b=p2.x-p1.x;
44        c=-a*p1.x-b*p1.y;
45    }
46    T cross(const point<T> &p)const{//點和有向
47        //直線的關係，>0左邊、=0在線上、<0右邊
48        return (p2-p1).cross(p-p1);
49    }
50    bool point_on_segment(const point<T>&p)
51        const{//點是否線段上
52        return cross(p)==0&&(p1-p).dot(p2-p)<=0;
53    }
54    T dis2(const point<T> &p,bool is_segment
55        =0)const{//點跟直線/線段的距離平方
56    point<T> v=p2-p1,v1=p-p1;
57    if(is_segment){
58        point<T> v2=p-p2;
59        if(v.dot(v1)<=0)return v1.abs2();
60        if(v.dot(v2)>=0)return v2.abs2();
61    }
62    T tmp=v.cross(v1);
63    return tmp*tmp/v.abs2();
64    }
65    T seg_dis2(const line<T> &l)const{//兩線段
66        //距離平方
67        return min({dis2(l.p1,1),dis2(l.p2,1),l.
68            dis2(p1,1),l.dis2(p2,1)});
69    }
70    point<T> projection(const point<T> &p)
71        const{//點對直線的投影
72    point<T> n=(p2-p1).normal();
73    return p-n*(p-p1).dot(n)/n.abs2();
74    }
75    point<T> mirror(const point<T> &p)const{//
76        //點對直線的鏡射
77        //要先呼叫pton轉成一般式
78    point<T> ans;
79    T d=a*p+b*b;
80    ans.x=(b*b*p.x-a*a*p.x-2*a*b*p.y-2*a*c)/
81        d;
82    ans.y=(a*a*p.y-b*b*p.y-2*a*b*p.x-2*b*c)/
83        d;
84    return ans;
85    }
86    bool equal(const line &l)const{//直線相等
87    return cross(l.p1)==0&&cross(l.p2)==0;
88    }
89    bool parallel(const line &l)const{//直線平
90        //行
91    return (p1-p2).cross(l.p1-l.p2)==0;
92    }
93    bool cross_seg(const line &l)const{//直線
94        //是否交線段
95    return (p2-p1).cross(l.p1-p1)*(p2-p1).
96        cross(l.p2-p1)<=0;
97    }
98    char line_intersect(const line &l)const{//
99        //直線相交情況，-1無限多點、1交於一點、0
100        //不相交
101    return parallel(l)?(cross(l.p1)==0?-1:0)
102        :1;
103    }
104    char seg_intersect(const line &l)const{//
105        //線段相交情況，-1無限多點、1交於一點、0
106        //不相交
107    T c1=(p2-p1).cross(l.p1-p1);
108    T c2=(p2-p1).cross(l.p2-p1);
109    T c3=(l.p2-l.p1).cross(p1-l.p1);
110    T c4=(l.p2-l.p1).cross(p2-l.p1);
111    if(c1==0&&c2==0){
112        if(p1==l.p1&&(p2-p1).dot(l.p2)<=0)
113            return 1;
114        if(p1==l.p2&&(p2-p1).dot(l.p1)<=0)
115            return 1;
116        if(p2==l.p1&&(p1-p2).dot(l.p2)<=0)
117            return 1;
118        if(p2==l.p2&&(p1-p2).dot(l.p1)<=0)
119            return 1;
120        return 1;
121    }
122    if(c1==0&&c2==0){
123        if(p1==l.p1&&(p2-p1).dot(l.p2)<=0)
124            return 1;
125        if(p1==l.p2&&(p2-p1).dot(l.p1)<=0)
126            return 1;
127        if(p2==l.p1&&(p1-p2).dot(l.p2)<=0)
128            return 1;
129        if(p2==l.p2&&(p1-p2).dot(l.p1)<=0)
130            return 1;
131        return 1;
132    }
133    return 0;
134    }
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195    }
196    }
197    }

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198 }
199 for(int i=s.size()-2,t=m+1;i>=0;--i){
200     while(m>=t&&(p[m-1]-p[m-2]).cross(s[i]
201         ]-p[m-2])<=0)--m;
202     p[m++]=s[i];
203 }
204 if(s.size()>1)--m;
205 p.resize(m);
206 }
207 T diam(){//直徑
208     int n=p.size(),t=1;
209     T ans=0;p.push_back(p[0]);
210     for(int i=0;i<n;i++){
211         point<T> now=p[i+1]-p[i];
212         while(now.cross(p[t+1]-p[i])>now.cross
213             (p[t]-p[i]))t=(t+1)%n;
214         ans=max(ans,max((p[i]-p[t]).abs2(),(p[
215             i+1]-p[t+1]).abs2()));
216     }
217     return p.pop_back(),ans;
218 }
219 T min_cover_rectangle(){//最小覆蓋矩形
220     int n=p.size(),t=1,r=1,l;
221     if(n<3)return 0;//也可以做最小周長矩形
222     T ans=1e99;p.push_back(p[0]);
223     for(int i=0;i<n;i++){
224         point<T> now=p[i+1]-p[i];
225         while(now.cross(p[t+1]-p[i])>now.cross
226             (p[t]-p[i]))t=(t+1)%n;
227         while(now.dot(p[r+1]-p[i])>now.dot(p[r]
228             ]-p[i]))r=(r+1)%n;
229         if(l==r;
230         while(now.dot(p[l+1]-p[i])<=now.dot(p[
231             l]-p[i]))l=(l+1)%n;
232         T d=now.abs2();
233         T tmp=now.cross(p[t]-p[i])*(now.dot(p[
234             r]-p[i])-now.dot(p[l]-p[i]))/d;
235         ans=min(ans,tmp);
236     }
237     return p.pop_back(),ans;
238 }
239 T max_triangle(){//最大內接三角形
240     int n=p.size(),a=1,b=2;
241     if(n<3)return 0;
242     T ans=0,tmp;p.push_back(p[0]);
243     for(int i=0;i<n;i++){
244         while((p[a]-p[i]).cross(p[b+1]-p[i])>
245             (p[a]-p[i]).cross(p[b]-p[i]))
246             b=(b+1)%n;
247         ans=max(ans,tmp);
248         while((p[a+1]-p[i]).cross(p[b]-p[i])>
249             (p[a]-p[i]).cross(p[b]-p[i]))
250             a=(a+1)%n;
251         ans=max(ans,tmp);
252     }
253     return p.pop_back(),ans/2;
254 }
255 T dis2(polygon &p1){//凸包最近距離平方
256     vector<point<T> > &P=p,Q=p1.p;
257     int n=P.size(),m=Q.size(),l=0,r=0;
258     for(int i=0;i<n;i++){
259         if(P[i].y<P[l].y)l=i
260     }
261     for(int i=0;i<m;i++){
262         if(Q[i].y<Q[r].y)r=i
263     }
264     P.push_back(P[0]),Q.push_back(Q[0]);
265
266     T ans=1e99;
267     for(int i=0;i<n;i++){
268         while((P[i]-P[l+1]).cross(Q[r+1]-Q[r])
269             <0)r=(r+1)%m;
270         ans=min(ans,line<T>(P[i],P[l+1]).
271             seg_dis2(line<T>(Q[r],Q[r+1])));
272         l=(l+1)%n;
273     }
274     return P.pop_back(),Q.pop_back(),ans;
275 }
276 static char sign(const point<T>&t){
277     return (t.y==0?t.x:t.y)<0;
278 }
279 static bool angle_cmp(const line<T> &A,
280     const line<T> &B){
281     point<T> a=A.p2-A.p1,b=B.p2-B.p1;
282     return sign(a)<sign(b)||((sign(a)==sign(b)
283         )&&a.cross(b)>0);
284 }
285 int halfplane_intersection(vector<line<T>
286     > &s){//半平面交
287     sort(s.begin(),s.end(),angle_cmp);
288     //線段
289     //左側為該線段半平面
290     int L,R,n=s.size();
291     vector<point<T> > px(n);
292     vector<line<T> > q(n);
293     q[L=R=0]=s[0];
294     for(int i=1;i<n;i++){
295         while(L<R&&s[i].cross(px[R-1])<=0)--R;
296         while(L<R&&s[i].cross(px[L])<=0)+L;
297         q[++R]=s[i];
298         if(q[R].parallel(q[R-1])){
299             --R;
300             if(q[R].cross(s[i].p1)>0)q[R]=s[i];
301         }
302         if(L<R)px[R-1]=q[R-1].
303             line_intersection(q[R]);
304     }
305     while(L<R&&q[L].cross(px[R-1])<=0)--R;
306     p.clear();
307     if(R-L==1)return 0;
308     px[R]=q[R].line_intersection(q[L]);
309     for(int i=L;i<R;i++)p.push_back(px[i]);
310     return R-L+1;
311 }
312 template<typename T>
313 struct triangle{
314     point<T> a,b,c;
315     triangle(){
316     }
317     triangle(const point<T> &a,const point<T>
318         &b,const point<T> &c):a(a),b(b),c(c){
319     }
320     T area()const{
321         T t=(b-a).cross(c-a)/2;
322         return t>0?t:-t;
323     }
324 }
325 point<T> barycenter()const{//重心
326     return (a+b+c)/3;
327 }
328 point<T> circumcenter()const{//外心
329     static line<T> u,v;
330     u.p1=(a+b)/2;
331     u.p2=point<T>(u.p1.x-a.y+b.y,u.p1.y+a.x-
332         b.x);
333     v.p1=(a+c)/2;
334     v.p2=point<T>(v.p1.x-a.y+c.y,v.p1.y+a.x-
335         c.x);
336     return u.line_intersection(v);
337 }
338 point<T> incenter()const{//內心
339     T A=sqrt((b-c).abs2()),B=sqrt((a-c).abs2
340         ()),C=sqrt((a-b).abs2());
341     return point<T>(A*a.x+B*b.x+C*c.x,A*a.y+
342         B*b.y+C*c.y)/(A+B+C);
343 }
344 point<T> perpercenter()const{//垂心
345     return barycenter()*3-circumcenter()*2;
346 }
347 template<typename T>
348 struct point3D{
349     T x,y,z;
350     point3D(){
351     }
352     point3D(const T&x,const T&y,const T&z):x(x
353         ),y(y),z(z){
354     }
355     point3D operator+(const point3D &b)const{
356         return point3D(x+b.x,y+b.y,z+b.z);
357     }
358     point3D operator-(const point3D &b)const{
359         return point3D(x-b.x,y-b.y,z-b.z);
360     }
361     point3D operator*(const T &b)const{
362         return point3D(x*b,y*b,z*b);
363     }
364     point3D operator/(const T &b)const{
365         return point3D(x/b,y/b,z/b);
366     }
367     bool operator==(const point3D &b)const{
368         return x==b.x&&y==b.y&&z==b.z;
369     }
370     T dot(const point3D &b)const{
371         return x*b.x+y*b.y+z*b.z;
372     }
373     point3D cross(const point3D &b)const{
374         return point3D(y*b.z-z*b.y,z*b.x-x*b.z,x
375             *b.y-y*b.x);
376     }
377     T abs2()const{//向量長度的平方
378         return dot(*this);
379     }
380     T area2(const point3D &b)const{//和b、原點
381         //圍成面積的平方
382         return cross(b).abs2()/4;
383     }
384 };
385 template<typename T>
386 struct line3D{
387     point3D<T> p1,p2;
388     line3D(){
389     }
390     line3D(const point3D<T> &p1,const point3D<
391         T> &p2):p1(p1),p2(p2){
392     }
393     T dis2(const point3D<T> &p,bool is_segment
394         =0)const{//點跟直線/線段的距離平方
395         point3D<T> v=p2-p1,v1=p-p1;
396         if(is_segment){
397             point3D<T> v2=p-p2;
398             if(v.dot(v1)<=0)return v1.abs2();
399             if(v.dot(v2)>=0)return v2.abs2();
400         }
401         point3D<T> tmp=v.cross(v1);
402         return tmp.abs2()/v.abs2();
403     }
404 }
405 pair<point3D<T>,point3D<T> > closest_pair(
406     const line3D<T> &l1)const{
407     point3D<T> v1=(p1-p2),v2=(l1.p1-l.p2);
408     point3D<T> N=v1.cross(v2),ab(p1-l.p1);
409     //if(N.abs2()==0)return NULL;平行或重合
410
411     T tmp=N.dot(ab),ans=tmp*tmp/N.abs2();//
412     //最近點對距離
413     point3D<T> d1=p2-p1,d2=l.p2-l.p1,D=d1.
414         cross(d2);
415     T t1=((l.p1-p1).cross(d2)).dot(D)/D.abs2
416         ();
417     T t2=((l.p1-p1).cross(d1)).dot(D)/D.abs2
418         ();
419     return make_pair(p1+d1*t1,l.p1+d2*t2);
420 }
421 bool same_side(const point3D<T> &a,const
422     point3D<T> &b)const{
423     return (p2-p1).cross(a-p1).dot((p2-p1).
424         cross(b-p1))>0;
425 }
426 template<typename T>
427 struct plane{
428     point3D<T> p0,n;//平面上的點和法向量
429     plane(){
430     }
431     plane(const point3D<T> &p0,const point3D<T>
432         &n):p0(p0),n(n){
433     }
434     T dis2(const point3D<T> &p)const{//點到平
435         //面距離的平方
436         T tmp=(p-p0).dot(n);
437         return tmp*tmp/n.abs2();
438     }
439     point3D<T> projection(const point3D<T> &p)
440         const{
441         return p-n*(p-p0).dot(n)/n.abs2();
442     }
443     point3D<T> line_intersection(const line3D<
444         T> &l1)const{
445         T tmp=n.dot(l1.p2-l.p1);//等於0表示平行或
446             //重合該平面
447         return l1.p1+(l1.p2-l.p1)*(n.dot(p0-l.p1)/
448             tmp);
449     }
450     line3D<T> plane_intersection(const plane &
451         p1)const{
452         point3D<T> e=n.cross(p1.n),v=n.cross(e);
453         T tmp=p1.n.dot(v);//等於0表示平行或重合
454             //該平面
455         point3D<T> q=p0+(v*(p1.n.dot(p1.p0-p0))/
456             tmp);
457         return line3D<T>(q,q+e);
458     }
459 };
460 template<typename T>
461 struct triangle3D{
462     point3D<T> a,b,c;
463     triangle3D(){
464     }
465     triangle3D(const point3D<T> &a,const
466         point3D<T> &b,const point3D<T> &c):a(a)
467         ,b(b),c(c){
468     }
469     bool point_in(const point3D<T> &p)const{//
470         //點在該平面上的投影在三角形中
471         return line3D<T>(b,c).same_side(p,a)&&
472             line3D<T>(a,c).same_side(p,b)&&
473             line3D<T>(a,b).same_side(p,c);
474     }
475 };
476 template<typename T>
477 struct tetrahedron{//四面體

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404 point3D<T> a,b,c,d;
405 tetrahedron(){}
406 tetrahedron(const point3D<T> &a,const
    point3D<T> &b,const point3D<T> &c,
    const point3D<T> &d):a(a),b(b),c(c),d(
    d){}
407 T volume6()const{//體積的六倍
408     return (d-a).dot((b-a).cross(c-a));
409 }
410 point3D<T> centroid()const{
411     return (a+b+c+d)/4;
412 }
413 bool point_in(const point3D<T> &p)const{
414     return triangle3D<T>(a,b,c).point_in(p)
        &&triangle3D<T>(c,d,a).point_in(p);
415 }
416 };
417 template<typename T>
418 struct convexhull3D{
419     static const int MAXN=105;
420     struct face{
421         int a,b,c;
422         bool use;
423         face(){}
424         face(int a,int b,int c):a(a),b(b),c(c),
            use(1){}
425 };
426 vector<point3D<T> > pt;
427 vector<face> fc;
428 int fid[MAXN][MAXN];
429 static bool point_cmp(const point3D<T> &a,
    const point3D<T> &b){
430     return a.x<b.x|| (a.x==b.x&&(a.y<b.y|| (a.
        y==b.y&&a.z<b.z)));
431 }
432 bool outside(int p,int a,int b,int c)const
    {
433     return tetrahedron<T>(pt[a],pt[b],pt[c],
        pt[p]).volume6()<0;
434 }
435 bool outside(int p,int f)const{return
    outside(p,fc[f].a,fc[f].b,fc[f].c);}
436 void AddFace(int a,int b,int c,int p){
437     if(outside(p,a,b,c))fid[c][b]=fid[b][a]=
        fid[a][c]=fc.size(),fc.push_back(
        face(c,b,a));
438     else fid[a][b]=fid[b][c]=fid[c][a]=fc.
        size(),fc.push_back(face(a,b,c));
439 }
440 bool dfs(int p,int f){
441     if(!fc[f].use)return true;
442     if(outside(p,f)){
443         int a=fc[f].a,b=fc[f].b,c=fc[f].c;
444         fc[f].use=false;
445         if(!dfs(p,fid[b][a]))AddFace(p,a,b,c);
446         if(!dfs(p,fid[c][b]))AddFace(p,b,c,a);
447         if(!dfs(p,fid[a][c]))AddFace(p,c,a,b);
448         return true;
449     }else return false;
450 }
451 void build(){
452     bool ok=false;
453     fc.clear();
454     sort(pt.begin(),pt.end(),point_cmp);
455     pt.resize(unique(pt.begin(),pt.end())-pt.
        .begin());
456     for(size_t i=2;i<pt.size();++i){
457         if((pt[0]-pt[i]).area2(pt[1]-pt[i])
            !=0){
458             ok=true;
459             swap(pt[i],pt[2]);
460             break;
461         }
462     }
463     if(!ok)return;
464     ok=false;
465     for(size_t i=3;i<pt.size();++i){
466         if(tetrahedron<T>(pt[0],pt[1],pt[2],pt
            [i]).volume6()!=0){
467             ok=true;
468             swap(pt[i],pt[3]);
469             break;
470         }
471     }
472     if(!ok)return;
473     for(int i=0;i<4;++i)AddFace(i,(i+1)%4,(i
        +2)%4,(i+3)%4);
474     for(size_t i=4;i<pt.size();++i){
475         for(int j=fc.size()-1;j>=0;--j){
476             if(outside(i,j)){
477                 dfs(i,j);
478                 break;
479             }
480         }
481     }
482     size_t sz=0;
483     for(size_t i=0;i<fc.size();++i)if(fc[i].
        use)fc[sz++]=fc[i];
484     fc.resize(sz);
485 }
486 point3D<T> centroid()const{
487     point3D<T> res(0,0,0);
488     T vol=0;
489     for(size_t i=0;i<fc.size();++i){
490         T tmp=pt[fc[i].a].dot(pt[fc[i].b].
            cross(pt[fc[i].c]));
491         res=res+(pt[fc[i].a]+pt[fc[i].b]+pt[fc
            [i].c])*tmp;
492         vol+=tmp;
493     }
494     return res/(vol*4);
495 }
496 };

```

## 1.2 SmallestCircle.cpp

```

1 #include "Geometry.cpp"
2 struct Circle{
3     typedef point<double> p;
4     typedef const point<double> cp;
5     p x;
6     double r2;
7     bool incircle(cp &c)const{return (x-c).
        abs2()<=r2;}
8 };
9

```

```

10 Circle TwoPointCircle(Circle::cp &a, Circle
    ::cp &b) {
11     Circle::p m=(a+b)/2;
12     return (Circle){m,(a-m).abs2()};
13 }
14
15 Circle outcircle(Circle::p a, Circle::p b,
    Circle::p c) {
16     if(TwoPointCircle(a,b).incircle(c))
        return TwoPointCircle(a,b);
17     if(TwoPointCircle(b,c).incircle(a))
        return TwoPointCircle(b,c);
18     if(TwoPointCircle(c,a).incircle(b))
        return TwoPointCircle(c,a);
19     Circle::p ret;
20     double a1=b.x-a.x, b1=b.y-a.y, c1=(a1*a1
        +b1*b1)/2;
21     double a2=c.x-a.x, b2=c.y-a.y, c2=(a2*a2
        +b2*b2)/2;
22     double d = a1*b2 - a2*b1;
23     ret.x=a.x+(c1*b2-c2*b1)/d;
24     ret.y=a.y+(a1*c2-a2*c1)/d;
25     return (Circle){ret,(ret-a).abs2()};
26 }
27 //rand required
28 Circle SmallestCircle(std::vector<Circle::p>
    &p){
29     int n=p.size();
30     if(n==1) return (Circle){p[0],0.0};
31     if(n==2) return TwoPointCircle(p[0],p
        [1]);
32     random_shuffle(p.begin(),p.end());
33     Circle c = {p[0],0.0};
34     for(int i=0;i<n;++i){
35         if(c.incircle(p[i])) continue;
36         c=Circle{p[i],0.0};
37         for(int j=0;j<i;++j){
38             if(c.incircle(p[j])) continue;
39             c=TwoPointCircle(p[i],p[j]);
40             for(int k=0;k<j;++k){
41                 if(c.incircle(p[k]))
                    continue;
42                 c=outcircle(p[i],p[j],p[k]);
43             }
44         }
45     }
46     return c;
47 }

```

## 2 Data\_Structure

### 2.1 DLX.cpp

```

1 const int MAXN=4100, MAXM=1030, MAXND=16390;
2 struct DLX{
3     int n,m,sz,ansd;//高是n · 寬是m的稀疏矩陣
4     int S[MAXN],H[MAXN];
5     int row[MAXN],col[MAXND]//每個節點代表的
        列跟行
6     int L[MAXN],R[MAXN],U[MAXN],D[MAXN];
7     vector<int> ans,ans1;
8     void init(int _n,int _m){
9         n=_n,m=_m;
10        for(int i=0;i<m;++i){
11            U[i]=D[i]=i,L[i]=i-1,R[i]=i+1;
12            S[i]=0;
13        }
14        R[m]=0,L[0]=m;
15        sz=m,ansd=INT_MAX;//ansd存最優解的個數
16        for(int i=1;i<n;++i)H[i]=-1;
17    }
18    void add(int r,int c){
19        ++S[col[++sz]=c];
20        row[sz]=r;
21        D[sz]=D[c],U[D[c]]=sz,U[sz]=c,D[c]=sz;
22        if(H[r]<0)H[r]=L[sz]=R[sz]=sz;
23        else R[sz]=R[H[r]],L[R[H[r]]]=sz,L[sz]=H
            [r],R[H[r]]=sz;
24    }
25    #define DFOR(i,A,s) for(int i=A[s];i!=s;i=
        A[i])
26    void remove(int c){//刪除第c行和所有當前覆
        蓋到第c行的列
27        L[R[c]]=L[c],R[L[c]]=R[c]//這裡刪除第c
        行 · 若有些行不需要處理可以在開始時呼
        叫他
28        DFOR(i,D,c)DFOR(j,R,i){U[D[j]]=U[j],D[U
            [j]]=D[j],--S[col[j]]};
29    }

```

### 1.3 最近點對.cpp

```

1 #define INF LLONG_MAX
2 template<typename T>
3 T closest_pair(vector<point<T> >&v,vector<
    point<T> >&t,int l,int r){
4     T dis=INF, tmd;
5     if(l==r)return dis;
6     int mid=(l+r)/2;
7     if((tmd=closest_pair(v,t,l,mid))<dis)dis=
        tmd;
8     if((tmd=closest_pair(v,t,mid+1,r))<dis)dis
        =tmd;
9     t.clear();

```

```

30 void restore(int c){//恢復第c行和所有當前
    覆蓋到第c行的列 · remove的逆操作
31     DFOR(i,U,c)DFOR(j,L,i){++S[col[j]],U[D[j]]
        =j,D[U[j]]=j;}
32     L[R[c]]=c,R[L[c]]=c;
33 }
34 void remove2(int nd){//刪除nd所在的行當前
    所有點(包括虛擬節點) · 只保留nd
35     DFOR(i,D,nd)L[R[i]]=L[i],R[L[i]]=R[i];
36 }
37 void restore2(int nd){//刪除nd所在的行當前
    所有點 · 為remove2的逆操作
38     DFOR(i,U,nd)L[R[i]]=R[L[i]]=i;
39 }
40 bool vis[MAXM];
41 int h(){//估價函數 for IDA*
42     int res=0;
43     memset(vis,0,sizeof(vis));
44     DFOR(i,R,0)if(!vis[i]){
45         vis[i]=1;
46         ++res;
47         DFOR(j,D,i)DFOR(k,R,j)vis[col[k]]=1;
48     }
49     return res;
50 }
51 bool dfs(int d){//for精確覆蓋問題
52     if(d+h()>=ansd)return 0;//找最佳解用 · 找
        任意解可以刪掉
53     if(!R[0]){ansd=d;return 1;}
54     int c=R[0];
55     DFOR(i,R,0)if(S[i]<S[c])c=i;
56     remove(c);
57     DFOR(i,D,c){
58         ans.push_back(row[i]);
59         DFOR(j,R,i)remove(col[j]);
60         if(dfs(d+1))return 1;
61         ans.pop_back();
62         DFOR(j,L,i)restore(col[j]);
63     }
64     restore(c);
65     return 0;
66 }
67 void dfs2(int d){//for最小重複覆蓋問題
68     if(d+h()>=ansd)return;
69     if(!R[0]){ansd=d;ans=ansd;return;}
70     int c=R[0];
71     DFOR(i,R,0)if(S[i]<S[c])c=i;
72     DFOR(i,D,c){
73         anst.push_back(row[i]);
74         remove2(i);
75         DFOR(j,R,i)remove2(j)--S[col[j]];
76         dfs2(d+1);
77         anst.pop_back();
78         DFOR(j,L,i)restore2(j),++S[col[j]];
79         restore2(i);
80     }
81 }
82 bool exact_cover(){//解精確覆蓋問題
83     return ans.clear(), dfs(0);
84 }
85 void min_cover(){//解最小重複覆蓋問題
86     anst.clear();//暫存用 · 答案還是存在ans裡
87     dfs2(0);
88 }

```

## 2.2 Dynamic\_KD\_tree.cpp

```

1 template<typename T,size_t kd>//有kd個維度
2 struct kd_tree{
3     struct point{
4         T d[kd];
5         T dist(const point &x)const{
6             T ret=0;
7             for(size_t i=0;i<kd;++i)ret+=std::abs(
                d[i]-x.d[i]);
8             return ret;
9         }
10        bool operator==(const point &p){
11            for(size_t i=0;i<kd;++i)
12                if(d[i]!=p.d[i])return 0;
13            return 1;
14        }
15        bool operator<(const point &b)const{
16            return d[0]<b.d[0];
17        }
18    };
19 private:
20     struct node{
21         node *l,*r;
22         point pid;
23         int s;
24         node(const point &p):l(0),r(0),pid(p),s
            (1){}
25         ~node(){delete l;delete r;}
26         void up(){s=(l?l->s:0)+1+(r?r->s:0);}
27     }*root;
28     const double alpha,loga;
29     const T INF;//記得要給INF · 表示極大值
30     int maxn;
31     struct __cmp{
32         int sort_id;
33         bool operator()(const node*x,const node*
            y)const{
34             return operator()(x->pid,y->pid);
35         }
36         bool operator()(const point &x,const
            point &y)const{
37             if(x.d[sort_id]!=y.d[sort_id])
38                 return x.d[sort_id]<y.d[sort_id];
39             for(size_t i=0;i<kd;++i)
40                 if(x.d[i]!=y.d[i])return x.d[i]<y.d[
                    i];
41             return 0;
42         }
43     }cmp;
44     int size(node *o){return o?o->s:0;}
45     std::vector<node*> A;
46     node* build(int k,int l,int r){
47         if(l>r) return 0;
48         if(k==kd) k=0;
49         int mid=(l+r)/2;
50         cmp.sort_id = k;
51         std::nth_element(A.begin()+l,A.begin()+
            mid,A.begin()+r+1,cmp);

```

```

52         node *ret=A[mid];
53         ret->l = build(k+1,l,mid-1);
54         ret->r = build(k+1,mid+1,r);
55         ret->up();
56         return ret;
57     }
58     bool isbad(node*o){
59         return size(o->l)>alpha*o->s||size(o->r)
            >alpha*o->s;
60     }
61     void flatten(node *u,typename std::vector<
        node*>::iterator &it){
62         if(!u)return;
63         flatten(u->l,it);
64         *it=u;
65         flatten(u->r,++it);
66     }
67     void rebuild(node*&u,int k){
68         if((int)A.size()<u->s)A.resize(u->s);
69         typename std::vector<node*>::iterator it
            =A.begin();
70         flatten(u,it);
71         u=build(k,0,u->s-1);
72     }
73     bool insert(node*&u,int k,const point &x,
        int dep){
74         if(!u) return u=new node(x), dep<=0;
75         ++u->s;
76         cmp.sort_id=k;
77         if(insert(cmp(x,u->pid)?u->l:u->r,(k+1)%
            kd,x,dep-1)){
78             if(!isbad(u))return 1;
79             rebuild(u,k);
80         }
81         return 0;
82     }
83     node *findmin(node*o,int k){
84         if(!o)return 0;
85         if(cmp.sort_id==k)return o->l?findmin(o
            ->l,(k+1)%kd):o;
86         node *l=findmin(o->l,(k+1)%kd);
87         node *r=findmin(o->r,(k+1)%kd);
88         if(l&l)return cmp(l,o)?l:o;
89         if(!l&r)return cmp(r,o)?r:o;
90         if(!l&l&r)return o;
91         if(cmp(l,r))return cmp(l,o)?l:o;
92         return cmp(r,o)?r:o;
93     }
94     bool erase(node *&u,int k,const point &x){
95         if(!u)return 0;
96         if(u->pid==x){
97             if(u->r);
98             else if(u->l) u->r=u->l, u->l=0;
99             else{
100                 delete u;
101                 return u=0, 1;
102             }
103             --u->s;
104             cmp.sort_id=k;
105             u->pid=findmin(u->r,(k+1)%kd->pid;
106             return erase(u->r,(k+1)%kd,u->pid);
107         }
108         cmp.sort_id=k;
109         if(erase(cmp(x,u->pid)?u->l:u->r,(k+1)%
            kd,x))
110             return --u->s, 1;

```

```

111         return 0;
112     }
113     T heuristic(const T h[])const{
114         T ret=0;
115         for(size_t i=0;i<kd;++i)ret+=h[i];
116         return ret;
117     }
118     int qM;
119     std::priority_queue<std::pair<T,point > >
        pQ;
120     void nearest(node *u,int k,const point &x,
        T *h,T &mndist){
121         if(u==0||heuristic(h)>=mndist)return;
122         T dist=u->pid.dist(x),old=h[k];
123         /*mndist=std::min(mndist,dist);*/
124         if(dist<mndist){
125             pQ.push(std::make_pair(dist,u->pid));
126             if((int)pQ.size()==qM+1)
127                 mndist=pQ.top().first,pQ.pop();
128         }
129         if(x.d[k]<u->pid.d[k]){
130             nearest(u->l,(k+1)%kd,x,h,mndist);
131             h[k]=std::abs(x.d[k]-u->pid.d[k]);
132             nearest(u->r,(k+1)%kd,x,h,mndist);
133         }else{
134             nearest(u->r,(k+1)%kd,x,h,mndist);
135             h[k]=std::abs(x.d[k]-u->pid.d[k]);
136             nearest(u->l,(k+1)%kd,x,h,mndist);
137         }
138         h[k]=old;
139     }
140     std::vector<point>in_range;
141     void range(node *u,int k,const point&mi,
        const point&ma){
142         if(!u)return;
143         bool is=1;
144         for(int i=0;i<kd;++i)
145             if(u->pid.d[i]<mi.d[i]||ma.d[i]<u->pid
                .d[i]){
146                 is=0;break;
147             }
148         if(is)in_range.push_back(u->pid);
149         if(mi.d[k]<u->pid.d[k])range(u->l,(k+1)
            %kd,mi,ma);
150         if(ma.d[k]>u->pid.d[k])range(u->r,(k+1)
            %kd,mi,ma);
151     }
152 public:
153     kd_tree(const T &INF,double a=0.75):root
        (0),alpha(a),loga(log2(1.0/a)),INF(INF
            ),maxn(1){}
154     ~kd_tree(){delete root;}
155     void clear(){delete root;root=0,maxn=1;}
156     void build(int n,const point *p){
157         delete root,A.resize(maxn=n);
158         for(int i=0;i<n;++i)A[i]=new node(p[i]);
159         root=build(0,0,n-1);
160     }
161     void insert(const point &x){
162         insert(root,0,x,__lg(size(root))/loga);
163         if(root->s>maxn)maxn=root->s;
164     }
165     bool erase(const point &p){
166         bool d=erase(root,0,p);
167         if(root&&root->s>alpha*maxn)rebuild();
168         return d;

```



```

169 }
170 void rebuild(){
171     if(root)rebuild(root,0);
172     maxn=root->s;
173 }
174 T nearest(const point &x,int k){
175     qM=k;
176     T mndist=INF,h[kd]={};
177     nearest(root,0,x,h,mndist);
178     mndist=pQ.top().first;
179     pQ=std::priority_queue<std::pair<T,point
180         >>());
181     return mndist;//回傳離x第k近的點的距離
182 }
183 const std::vector<point> &range(const
184     point&mi,const point&ma){
185     in_range.clear();
186     range(root,0,mi,ma);
187     return in_range;//回傳介於mi到ma之間的點
188     vector
189 }
190 int size(){return root?root->s:0;}
191 };
```

## 2.3 kd\_tree\_replace\_segment

```

1 /*kd樹代替高維線段樹*/
2 struct node{
3     node *l,*r;
4     point pid,mi,ma;
5     int s;
6     int data;
7     node(const point &p,int d):l(0),r(0),pid(p
8         ),mi(p),ma(p),s(1),data(d),dmin(d),
9         dmax(d){}
10 void up(){
11     mi=ma=pid;
12     s=1;
13     if(l){
14         for(int i=0;i<kd;++i){
15             mi.d[i]=min(mi.d[i],l->mi.d[i]);
16             ma.d[i]=max(ma.d[i],l->ma.d[i]);
17         }
18     }
19     if(r){
20         for(int i=0;i<kd;++i){
21             mi.d[i]=min(mi.d[i],r->mi.d[i]);
22             ma.d[i]=max(ma.d[i],r->ma.d[i]);
23         }
24     }
25     s+=l->s;
26     s+=r->s;
27 }
28 void up2(){
29     //其他懶惰標記向上更新
30 }
31 void down(){
32     //其他懶惰標記下推
33 }
34 }*root;
35 }
36 /*檢查區間包含用的函數*/
```

```

35 inline bool range_include(node *o,const
36     point &L,const point &R){
37     for(int i=0;i<kd;++i){
38         if(L.d[i]>o->ma.d[i]||R.d[i]<o->mi.d[i])
39             return 0;
40     }
41     //只要(L,R)區間有和o的區間有交集就回傳
42     true
43     return 1;
44 }
45 inline bool range_in_range(node *o,const
46     point &L,const point &R){
47     for(int i=0;i<kd;++i){
48         if(L.d[i]>o->ma.d[i]||o->ma.d[i]>R.d[i])
49             return 0;
50     }
51     //如果(L,R)區間完全包含o的區間就回傳true
52     return 1;
53 }
54 inline bool point_in_range(node *o,const
55     point &L,const point &R){
56     for(int i=0;i<kd;++i){
57         if(L.d[i]>o->pid.d[i]||R.d[i]<o->pid.d[i]
58             ])return 0;
59     }
60     //如果(L,R)區間完全包含o->pid這個點就回傳
61     true
62     return 1;
63 }
64 /*單點修改 · 以單點改值為例*/
65 void update(node *u,const point &x,int data,
66     int k=0){
67     if(!u)return;
68     u->down();
69     if(u->pid==x){
70         u->data=data;
71         u->up2();
72         return;
73     }
74     cmp.sort_id=k;
75     update(cmp(x,u->pid)?u->l:u->r,x,data,(k
76         +1)%kd);
77     u->up2();
78 }
79 /*區間修改*/
80 void update(node *o,const point &L,const
81     point &R,int data){
82     if(!o)return;
83     o->down();
84     if(range_in_range(o,L,R)){
85         //區間懶惰標記修改
86         o->down();
87         return;
88     }
89     if(point_in_range(o,L,R)){
90         //這個點在(L,R)區間 · 但是他的左右子樹不
91         一定在區間中
92         //單點懶惰標記修改
93     }
94     if(o->l&&range_include(o->l,L,R))update(o
95         ->l,L,R,data);
96     if(o->r&&range_include(o->r,L,R))update(o
97         ->r,L,R,data);
98     o->up2();
99 }
100 }
```

```

85 /*區間查詢 · 以總和為例*/
86 int query(node *o,const point &L,const point
87     &R){
88     if(!o)return 0;
89     o->down();
90     if(range_in_range(o,L,R))return o->sum;
91     int ans=0;
92     if(point_in_range(o,L,R))ans+=o->data;
93     if(o->l&&range_include(o->l,L,R))ans+=
94         query(o->l,L,R);
95     if(o->r&&range_include(o->r,L,R))ans+=
96         query(o->r,L,R);
97     return ans;
98 }
```

## 2.4 reference\_point.cpp

```

1 template<typename T>
2 struct _RefC{
3     T data;
4     int ref;
5     _RefC(const T&d=0):data(d),ref(0){}
6 };
7 template<typename T>
8 struct _rp{
9     _RefC<T> *p;
10    T *operator->(){return &p->data;}
11    T &operator*(){return p->data;}
12    operator _RefC<T>*(){return p;}
13    _rp &operator=(const _rp &t){
14        if(p&&!--p->ref)delete p;
15        p=t.p,p&&+p->ref;
16        return *this;
17    }
18    _rp(_RefC<T> *t=0):p(t){p&&+p->ref;}
19    _rp(const _rp &t):p(t.p){p&&+p->ref;}
20    ~_rp(){if(p&&!--p->ref)delete p;}
21 };
22 template<typename T>
23 inline _rp<T> new_rp(const T&nd){
24     return _rp<T>(new _RefC<T>(nd));
25 }
```

## 2.5 skew\_heap.cpp

```

1 node *merge(node *a,node *b){
2     if(!a||!b) return a?a:b;
3     if(b->data<a->data) swap(a,b);
4     swap(a->l,a->r);
5     a->l=merge(b,a->l);
6     return a;
7 }
```

## 2.6 整體二分.cpp

```

1 void totBS(int L, int R, vector<Item> M){
2     if(Q.empty()) return; //維護全域B陣列
3     if(L==R) 整個M的答案=r, return;
4     int mid = (L+R)/2;
5     vector<Item> mL, mR;
6     do_modify_B_with_divide(mid,M);
7     //讓B陣列在遞迴的時候只會保留[L~mid]的資訊
8     undo_modify_B(mid,M);
9     totBS(L,mid,mL);
10    totBS(mid+1,R,mR);
11 }
```

## 3 default

### 3.1 debug.cpp

```

1 //volatile
2 #ifdef DEBUG
3 #define dbg(...) {\
4     fprintf(stderr,"%s - %d : (%s) = ",
5         __PRETTY_FUNCTION__, __LINE__,#
6         __VA_ARGS__); \
7     _DO(__VA_ARGS__); \
8 }
9 template<typename I> void _DO(I&&x){cerr<<x
10     <<endl;}
11 template<typename I,typename...T> void _DO(I
12     &&x,T&&...tail){cerr<<x<<" ";_DO(tail
13     ...);}
14 #else
15 #define dbg(...)
16 #endif
```

### 3.2 ext.cpp

```

1 #include<bits/extc++.h>
2 #include<ext/pd_ds/assoc_container.hpp>
3 #include<ext/pd_ds/tree_policy.hpp>
4 using namespace __gnu_cxx;
5 using namespace __gnu_pbds;
6 template<typename T>
7 using pbds_set = tree<T,null_type,less<T>,
8     rb_tree_tag,
9     tree_order_statistics_node_update>;
10 template<typename T,typename U>
11 using pbds_map = tree<T,U,less<T>,
12     rb_tree_tag,
13     tree_order_statistics_node_update>;
14 using heap = __gnu_pbds::priority_queue<int
15     >;
16 //s.find_by_order(1);//0 base
17 //s.order_of_key(1);
```

### 3.3 IncStack.cpp

```

1 //Magic
2 #pragma GCC optimize "Ofast"
3 //stack resize, change esp to rsp if 64-bit
  system
4 asm("mov %0, %%esp\n" :: "g"(mem+10000000));
5 -Wl,--stack,214748364 -trigraphs
6 //linux stack resize
7 #include<sys/resource.h>
8 void increase_stack(){
9     const rlim_t ks=64*1024*1024;
10    struct rlimit rl;
11    int res=getrlimit(RLIMIT_STACK,&rl);
12    if(!res&&rl.rlim_cur<ks){
13        rl.rlim_cur=ks;
14        res=setrlimit(RLIMIT_STACK,&rl);
15    }
16 }

```

### 3.4 input.cpp

```

1 inline int read(){
2     int x=0; bool f=0; char c=getchar();
3     while(ch<'0' || '9'<ch)f|=ch=='-',ch=getchar();
4     while('0'<=ch&&ch<'9')x=x*10-'0'+ch,ch=getchar();
5     return f?-x:x;
6 }
7 // #!/bin/bash
8 // g++ -std=c++11 -O2 -Wall -Wextra -Wno-
  unused-result -DDEBUG $1 && ./a.out
9 // -fsanitize=address -fsanitize=undefined
  -fsanitize=return

```

## 4 Flow

### 4.1 dinic.cpp

```

1 template<typename T>
2 struct DINIC{
3     static const int MAXN=105;
4     static const T INF=INT_MAX;
5     int n, level[MAXN], cur[MAXN];
6     struct edge{
7         int v,pre;
8         T cap,flow,r;
9         edge(int v,int pre,T cap):v(v),pre(pre),
10            cap(cap),flow(0),r(cap){}
11 };
12 int g[MAXN];
13 vector<edge> e;
14 void init(int _n){
15     memset(g,-1,sizeof(int)*((n=_n)+1));
16     e.clear();

```

```

17 void add_edge(int u,int v,T cap,bool
  directed=false){
18     e.push_back(edge(v,g[u],cap));
19     g[u]=e.size()-1;
20     e.push_back(edge(u,g[v],directed?0:cap));
21     g[v]=e.size()-1;
22 }
23 int bfs(int s,int t){
24     memset(level,0,sizeof(int)*(n+1));
25     memcpy(cur,g,sizeof(int)*(n+1));
26     queue<int> q;
27     q.push(s);
28     level[s]=1;
29     while(q.size()){
30         int u=q.front();q.pop();
31         for(int i=g[u];~i;i=e[i].pre){
32             if(!level[e[i].v]&&e[i].r){
33                 level[e[i].v]=level[u]+1;
34                 q.push(e[i].v);
35                 if(e[i].v==t)return 1;
36             }
37         }
38     }
39     return 0;
40 }
41 T dfs(int u,int t,T cur_flow=INF){
42     if(u==t)return cur_flow;
43     T df;
44     for(int &i=cur[u];~i;i=e[i].pre){
45         if(level[e[i].v]==level[u]+1&&e[i].r){
46             if(df=dfs(e[i].v,t,min(cur_flow,e[i].r))){
47                 e[i].flow+=df;
48                 e[i^1].flow-=df;
49                 e[i].r-=df;
50                 e[i^1].r+=df;
51                 return df;
52             }
53         }
54     }
55     return level[u]=0;
56 }
57 T dinic(int s,int t,bool clean=true){
58     if(clean){
59         for(size_t i=0;i<e.size();++i){
60             e[i].flow=0;
61             e[i].r=e[i].cap;
62         }
63     }
64     T ans=0, mf=0;
65     while(bfs(s,t))while(mf=dfs(s,t))ans+=mf;
66     return ans;
67 }
68 };

```

### 4.2 ISAP\_with\_cut.cpp

```

1 template<typename T>
2 struct ISAP{
3     static const int MAXN=105;
4     static const T INF=INT_MAX;

```

```

5     int n;//點數
6     int d[MAXN],gap[MAXN],cur[MAXN];
7     struct edge{
8         int v,pre;
9         T cap,flow,r;
10        edge(int v,int pre,T cap):v(v),pre(pre),
11           cap(cap),flow(0),r(cap){}
12 };
13 int g[MAXN];
14 vector<edge> e;
15 void init(int _n){
16     memset(g,-1,sizeof(int)*((n=_n)+1));
17     e.clear();
18 }
19 void add_edge(int u,int v,T cap,bool
  directed=false){
20     e.push_back(edge(v,g[u],cap));
21     g[u]=e.size()-1;
22     e.push_back(edge(u,g[v],directed?0:cap));
23     g[v]=e.size()-1;
24 }
25 T dfs(int u,int s,int t,T cur_flow=INF){
26     if(u==t)return cur_flow;
27     T tf=cur_flow,df;
28     for(int &i=cur[u];~i;i=e[i].pre){
29         if(e[i].r&&d[u]==d[e[i].v]+1){
30             df=dfs(e[i].v,s,t,min(tf,e[i].r));
31             e[i].flow+=df;
32             e[i^1].flow-=df;
33             e[i].r-=df;
34             e[i^1].r+=df;
35             if(!((tf=df)&&d[s]==n))return
36                cur_flow-tf;
37         }
38     }
39     int mh=n;
40     for(int i=cur[u]=g[u];~i;i=e[i].pre){
41         if(e[i].r&&d[e[i].v]<mh)mh=d[e[i].v];
42     }
43     if(!--gap[d[u]])d[s]=n;
44     else ++gap[d[u]=++mh];
45     return cur_flow-tf;
46 }
47 T isap(int s,int t,bool clean=true){
48     memset(d,0,sizeof(int)*(n+1));
49     memset(gap,0,sizeof(int)*(n+1));
50     memcpy(cur,g,sizeof(int)*(n+1));
51     if(clean) for(size_t i=0;i<e.size();++i){
52         {
53             e[i].flow=0;
54             e[i].r=e[i].cap;
55         }
56     }
57     T max_flow=0;
58     for(gap[0]=n;d[s]<n;)max_flow+=dfs(s,s,t);
59     return max_flow;
60 }
61 vector<int> cut_e;//最小割邊集
62 bool vis[MAXN];
63 void dfs_cut(int u){
64     vis[u]=1;//表示u屬於source的最小割集
65     for(int i=g[u];~i;i=e[i].pre){
66         if(e[i].flow<e[i].cap&&!vis[e[i].v])
67             dfs_cut(e[i].v);

```

```

63     }
64     T min_cut(int s,int t){
65         T ans=isap(s,t);
66         memset(vis,0,sizeof(bool)*(n+1));
67         dfs_cut(s); cut_e.clear();
68         for(int u=0;u<n;++u)
69             if(vis[u])for(int i=g[u];~i;i=e[i].pre)
70                 if(!vis[e[i].v])cut_e.push_back(i);
71         return ans;
72     }
73 };

```

### 4.3 MinCostMaxFlow.cpp

```

1 template<typename _T>
2 struct MCMF{
3     static const int MAXN=440;
4     static const _T INF=999999999;
5     struct edge{
6         int v,pre;
7         _T cap,cost;
8         edge(int v,int pre,_T cap,_T cost):v(v),
9            pre(pre),cap(cap),cost(cost){}
10 };
11 int n,S,T;
12 _T dis[MAXN],piS,ans;
13 bool vis[MAXN];
14 vector<edge> e;
15 int g[MAXN];
16 void init(int _n){
17     memset(g,-1,sizeof(int)*((n=_n)+1));
18     e.clear();
19 }
20 void add_edge(int u,int v,_T cap,_T cost,
  bool directed=false){
21     e.push_back(edge(v,g[u],cap,cost));
22     g[u]=e.size()-1;
23     e.push_back(edge(u,g[v],directed?0:cap,-
  cost));
24     g[v]=e.size()-1;
25 }
26 _T augment(int u,_T cur_flow){
27     if(u==T||!cur_flow)return ans+=piS*
  cur_flow,cur_flow;
28     vis[u]=1;
29     _T r=cur_flow,d;
30     for(int i=g[u];~i;i=e[i].pre){
31         if(e[i].cap&&!e[i].cost&&vis[e[i].v])
32             {
33                 d=augment(e[i].v,min(r,e[i].cap));
34                 e[i].cap-=d;
35                 e[i^1].cap+=d;
36                 if(!((r-=d)&&r))break;
37             }
38     }
39     return cur_flow-r;
40 }
41 bool modlabel(){
42     for(int u=0;u<n;++u)dis[u]=INF;
43     static deque<int> q;
44     dis[T]=0,q.push_back(T);
45     while(q.size()){

```

```

44 int u=q.front();q.pop_front();
45 _T dt;
46 for(int i=g[u];~i;i=e[i].pre){
47     if(e[i^1].cap&&(dt=dis[u]-e[i].cost)
48         <dis[e[i].v]){
49         if((dis[e[i].v]=dt)<=dis[q.size()])
50             q.front():S){
51             q.push_front(e[i].v);
52         }else q.push_back(e[i].v);
53     }
54 }
55 for(int u=0;u<n;++u)
56     for(int i=g[u];~i;i=e[i].pre)
57         e[i].cost+=dis[e[i].v]-dis[u];
58 return piS+=dis[S], dis[S]<INF;
59 }
60 _T mincost(int s,int t){
61     S=s,T=t;
62     piS=ans=0;
63     while(modlabel()){
64         do memset(vis,0,sizeof(bool)*(n+1));
65         while(augment(S,INF));
66     }return ans;
67 };

```

## 5 Graph

### 5.1 Augmenting\_Path.cpp

```

1 #define MAXN1 505
2 #define MAXN2 505
3 int n1,n2;//n1個點連向n2個點
4 int match[MAXN2];//屬於n2的點匹配了哪個點
5 vector<int> g[MAXN1];//圖
6 bool vis[MAXN2];//是否走訪過
7 bool dfs(int u){
8     for(size_t i=0;i<g[u].size();++i){
9         int v=g[u][i];
10        if(vis[v])continue;
11        vis[v]=1;
12        if(match[v]==-1||dfs(match[v]))
13            return match[v]=u, 1;
14    }
15    return 0;
16 }
17 inline int max_match(){
18     int ans=0;
19     memset(match,-1,sizeof(int)*n2);
20     for(int i=0;i<n1;++i){
21         memset(vis,0,sizeof(bool)*n2);
22         if(dfs(i))++ans;
23     }
24     return ans;
25 }

```

### 5.2 Augmenting\_Path\_multiple

```

1 #define MAXN1 1005
2 #define MAXN2 505
3 int n1,n2;//n1個點連向n2個點·其中n2個點可以
4     匹配很多邊
5 vector<int> g[MAXN1];//圖
6 int c[MAXN2];//每個屬於n2點最多可以接受幾條
7     匹配邊
8 vector<int> match_list[MAXN2];//每個屬於n2的
9     點匹配了那些點
10 bool vis[MAXN2];//是否走訪過
11 bool dfs(int u){
12     for(size_t i=0;i<g[u].size();++i){
13         int v=g[u][i];
14         if(vis[v])continue;
15         vis[v]=true;
16         if((int)match_list[v].size()<c[v]){
17             return match_list[v].push_back(u),
18                 true;
19         }else{
20             for(size_t j=0;j<match_list[v].size()
21                 ;++j){
22                 int next_u=match_list[v][j];
23                 if(dfs(next_u))
24                     return match_list[v][j]=u, true;
25             }
26         }
27     }
28     return false;
29 }
30 int max_match(){
31     for(int i=0;i<n2;++i)match_list[i].clear()
32     ;
33     int cnt=0;
34     for(int u=0;u<n1;++u){
35         memset(vis,0,sizeof(bool)*n2);
36         if(dfs(u))++cnt;
37     }
38     return cnt;
39 }

```

### 5.3 blossom\_matching.cpp

```

1 #define MAXN 505
2 vector<int> g[MAXN];
3 int pa[MAXN],match[MAXN],st[MAXN],S[MAXN],v[
4     MAXN];
5 int t,n;
6 int lca(int x,int y){
7     for(++t;;swap(x,y)){
8         if(x==0)continue;
9         if(v[x]==t)return x;
10        v[x]=t;
11        x=st[pa[match[x]]];
12    }
13 }
14 #define qpush(x) q.push(x),S[x]=0
15 void flower(int x,int y,int l,queue<int> &q){
16     while(st[x]!=1){

```

```

17     pa[x]=y;
18     if(S[y==match[x]]==1)qpush(y);
19     st[x]=st[y]=1, x=pa[y];
20 }
21 bool bfs(int x){
22     for(int i=1;i<=n;++i)st[i]=i;
23     memset(S+1,-1,sizeof(int)*n);
24     queue<int>q; qpush(x);
25     while(q.size()){
26         x=q.front(),q.pop();
27         for(size_t i=0;i<g[x].size();++i){
28             int y=g[x][i];
29             if(S[y]==-1){
30                 pa[y]=x,S[y]=1;
31                 if(!match[y]){
32                     for(int lst=x;y=lst,x=pa[y])
33                         lst=match[x],match[x]=y,match[y]
34                             =x;
35                     return 1;
36                 }
37                 qpush(match[y]);
38             }else if(!S[y]&&st[y]!=st[x]){
39                 int l=lca(y,x);
40                 flower(y,x,l,q),flower(x,y,l,q);
41             }
42         }
43     }
44     return 0;
45 }
46 int blossom(){
47     int ans=0;
48     for(int i=1;i<=n;++i)
49         if(!match[i]&&bfs(i))++ans;
50     return ans;
51 }

```

### 5.4 graphISO.cpp

```

1 const int MAXN=1005,K=30;//K要夠大
2 const long long A=3,B=11,C=2,D=19,P=0
3     xdefaced;
4 long long f[K+1][MAXN];
5 vector<int> g[MAXN],rg[MAXN];
6 int n;
7 void init(){
8     for(int i=0;i<n;++i){
9         f[0][i]=1;
10        g[i].clear(), rg[i].clear();
11    }
12 }
13 void add_edge(int u,int v){
14     g[u].push_back(v), rg[v].push_back(u);
15 }
16 long long point_hash(int u){//O(N)
17     for(int t=1;t<=K;++t){
18         for(int i=0;i<n;++i){
19             f[t][i]=f[t-1][i]*A%P;
20             for(int j:g[i])f[t][i]=(f[t][i]+f[t-1][j]*B%P)%P;
21             for(int j:rg[i])f[t][i]=(f[t][i]+f[t-1][j]*C%P)%P;

```

```

21     if(i==u)f[t][i]+=D;//如果圖太大的話·
22     把這行刪掉·執行一次後f[K]就會是所
23     有點的答案
24     f[t][i]%P;
25 }
26 }
27 return f[K][u];
28 }
29 vector<long long> graph_hash(){
30     vector<long long> ans;
31     for(int i=0;i<n;++i)ans.push_back(
32         point_hash(i));
33     sort(ans.begin(),ans.end());
34     return ans;
35 }

```

### 5.5 KM.cpp

```

1 #define MAXN 405
2 #define INF 0x3f3f3f3f
3 int n;// 1-base · 0表示沒有匹配
4 int g[MAXN][MAXN],lx[MAXN],ly[MAXN],pa[
5     MAXN],slack_y[MAXN];
6 int match_y[MAXN],match_x[MAXN];
7 bool vx[MAXN],vy[MAXN];
8 void augment(int y){
9     for(int x=z;y=y=z){
10        x=pa[y],z=match_x[x];
11        match_y[y]=x,match_x[x]=y;
12    }
13 }
14 void bfs(int st){
15     for(int i=1;i<=n;++i)slack_y[i]=INF,vx[i]=
16         vy[i]=0;
17     queue<int> q;q.push(st);
18     for(;;){
19         while(q.size()){
20             int x=q.front(),q.pop();
21             vx[x]=1;
22             for(int y=1;y<=n;++y)if(!vy[y]){
23                 int t=lx[x]+ly[y]-g[x][y];
24                 if(t==0){
25                     pa[y]=x;
26                     if(!match_y[y]){augment(y);return
27                         ;}
28                     vy[y]=1,q.push(match_y[y]);
29                 }else if(slack_y[y]>t)pa[y]=x,
30                     slack_y[y]=t;
31             }
32         }
33     }
34     int cut=INF;
35     for(int y=1;y<=n;++y){
36         if(!vy[y]&&cut>slack_y[y])cut=slack_y[
37             y];
38     }
39     for(int y=1;y<=n;++y){
40         if(!vy[y]&&slack_y[y]==0){

```

```

40     if(!match_y[y]){augment(y);return;}
41     vy[y]=1,q.push(match_y[y]);
42 }
43 }
44 }
45 }
46 long long KM(){
47     memset(match_y,0,sizeof(int)*(n+1));
48     memset(ly,0,sizeof(int)*(n+1));
49     for(int x=1;x<=n;++x){
50         lx[x]=-INF;
51         for(int y=1;y<=n;++y)
52             lx[x]=max(lx[x],g[x][y]);
53     }
54     for(int x=1;x<=n;++x)bfs(x);
55     long long ans=0;
56     for(int y=1;y<=n;++y)ans+=g[match_y[y]][y];
57     return ans;
58 }

```

## 5.6 MaximumClique.cpp

```

1 struct MaxClique{
2     static const int MAXN=105;
3     int N,ans;
4     int g[MAXN][MAXN],dp[MAXN],stk[MAXN][MAXN];
5     int sol[MAXN],tmp[MAXN];//sol[0~ans-1]為答案
6     void init(int n){
7         N=n;//0-base
8         memset(g,0,sizeof(g));
9     }
10    void add_edge(int u,int v){
11        g[u][v]=g[v][u]=1;
12    }
13    int dfs(int ns,int dep){
14        if(!ns){
15            if(dep>ans){
16                ans=dep;
17                memcpy(sol,tmp,sizeof tmp);
18                return 1;
19            }else return 0;
20        }
21        for(int i=0;i<ns;++i){
22            if(dep+ns-i<=ans)return 0;
23            int u=stk[dep][i],cnt=0;
24            if(dep+dp[u]<=ans)return 0;
25            for(int j=i+1;j<ns;++j){
26                int v=stk[dep][j];
27                if(g[u][v])stk[dep+1][cnt++]=v;
28            }
29            tmp[dep]=u;
30            if(dfs(cnt,dep+1))return 1;
31        }
32        return 0;
33    }
34    int clique(){
35        int u,v,ns;
36        for(ans=0,u=N-1;u>=0;--u){
37            for(ns=0,tmp[0]=u,v=u+1;v<N;++v)

```

```

38            if(g[u][v])stk[1][ns++]=v;
39            dfs(ns,1),dp[u]=ans;
40        }
41        return ans;
42    }
43 };

```

## 5.7 MinimumMeanCycle.cpp

```

1 #include<cstdio>//for DBL_MAX
2 int dp[maxN+1][maxN+1];
3 double mnc(int n){
4     int u,v,w;
5     const int inf=0x7f7f7f7f;
6     memset(dp,0x7f,sizeof(dp));
7     memset(dp[0],0,sizeof(dp[0]));
8     for(int i=0;i<n;++i){
9         for(auto e:E){
10             tie(u,v,w)=e;
11             if(dp[i][u]!=inf)
12                 dp[i+1][v]=min(dp[i+1][v],dp[i][u]+w);
13         }
14         double res = DBL_MAX;
15         for(int i=1;i<=n;++i){
16             double val = DBL_MIN;
17             for(int j=0;j<n;++j)
18                 val=max(val,double(dp[n][i]-dp[i][j])/(n-j));
19             res=min(res,val);
20         }
21     }
22     return res;
23 }

```

## 5.8 Minimum\_General\_Weighted

```

1 struct Graph {
2     // Minimum General Weighted Matching (
3     // Perfect Match) 0-base
4     static const int MXN = 105;
5     int n, edge[MXN][MXN];
6     int match[MXN],dis[MXN],onstk[MXN];
7     vector<int> stk;
8     void init(int _n) {
9         n = _n;
10        for (int i=0; i<n; i++)
11            for (int j=0; j<n; j++)
12                edge[i][j] = 0;
13    }
14    void add_edge(int u, int v, int w) {
15        edge[u][v] = edge[v][u] = w;
16    }
17    bool SPFA(int u){
18        if (onstk[u]) return true;
19        stk.push_back(u);
20        onstk[u] = 1;
21        for (int v=0; v<n; v++){
22            if (u != v && match[u] != v && !onstk[

```

```

23            if (dis[m] > dis[u] - edge[v][m] +
24                edge[u][v]){
25                dis[m] = dis[u] - edge[v][m] +
26                    edge[u][v];
27                onstk[v] = 1;
28                stk.push_back(v);
29                if (SPFA(m)) return true;
30                stk.pop_back();
31                onstk[v] = 0;
32            }
33        }
34        onstk[u] = 0;
35        stk.pop_back();
36        return false;
37    }
38    int solve() {
39        // find a match
40        for (int i=0; i<n; i+=2){
41            match[i] = i+1, match[i+1] = i;
42        }
43        for(;;){
44            int found = 0;
45            for (int i=0; i<n; i++) dis[i] = onstk[i] = 0;
46            for (int i=0; i<n; i++){
47                stk.clear();
48                if (!onstk[i] && SPFA(i)){
49                    found = 1;
50                    while (stk.size()>2){
51                        int u = stk.back(); stk.pop_back();
52                        int v = stk.back(); stk.pop_back();
53                        match[u] = v;
54                        match[v] = u;
55                    }
56                }
57                if (!found) break;
58            }
59            int ret = 0;
60            for (int i=0; i<n; i++)
61                ret += edge[i][match[i]];
62            ret /= 2;
63            return ret;
64        }
65    }graph;

```

## 5.9 Rectilinear\_MST.cpp

```

1 //平面曼哈頓最小生成樹構造圖(去除非必要邊)
2 #define T int
3 #define INF 0x3f3f3f3f
4 struct point{
5     T x,y;
6     int id;//每個點的編號都要不一樣，從0開始編號
7     point(){}
8     T dist(const point &p)const{
9         return abs(x-p.x)+abs(y-p.y);
10    }

```

```

11 };
12 bool cmpx(const point &a,const point &b){
13     return a.x<b.x||(a.x==b.x&&a.y<b.y);
14 }
15 struct edge{
16     int u,v;
17     T cost;
18     edge(int u,int v,T c):u(u),v(v),cost(c){}
19     bool operator<(const edge&e)const{
20         return cost<e.cost;
21     }
22 };
23 struct bit_node{
24     T mi;
25     int id;
26     bit_node(const T&mi=INF,int id=-1):mi(mi),id(id){}
27 };
28 vector<bit_node> bit;
29 void bit_update(int i,const T&data,int id){
30     for(;;i=i&(-i)){
31         if(data<bit[i].mi)bit[i]=bit_node(data,id);
32     }
33 }
34 int bit_find(int i,int m){
35     bit_node x;
36     for(;;i=i&(-i)) if(bit[i].mi<x.mi)x=bit[i];
37     return x.id;
38 }
39 vector<edge> build_graph(int n,point p[]){
40     vector<edge> e;//edge for MST
41     for(int dir=0;dir<4;++dir){//4種座標變換
42         if(dir%2) for(int i=0;i<n;++i) swap(p[i].x,p[i].y);
43         else if(dir==2) for(int i=0;i<n;++i) p[i].x=-p[i].x;
44         sort(p,p+n,cmpx);
45         vector<T> ga(n), gb;
46         for(int i=0;i<n;++i)ga[i]=p[i].y-p[i].x;
47         gb=ga, sort(gb.begin(),gb.end());
48         gb.erase(unique(gb.begin(),gb.end()),gb.end());
49         int m=gb.size();
50         bit=vector<bit_node>(m+1);
51         for(int i=n-1;i>=0;--i){
52             int pos=lower_bound(gb.begin(),gb.end(),ga[i])-gb.begin()+1;
53             int ans=bit_find(pos,m);
54             if(~ans)e.push_back(edge(p[i].id,p[ans].id,p[i].dist(p[ans])));
55             bit_update(pos,p[i].x+p[i].y,i);
56         }
57     }
58     return e;
59 }

```

## 5.10 treeISO.cpp

```

1 const int MAXN=100005;
2 const long long X=12327,P=0xdefaced;
3 vector<int> g[MAXN];

```



```

4 bool vis[MAXN];
5 long long dfs(int u){//hash ver
6     vis[u]=1;
7     vector<long long> tmp;
8     for(auto v:g[u])if(!vis[v])tmp.pb(dfs(v));
9     if(tmp.empty())return 177;
10    long long ret=4931;
11    sort(tmp.begin(),tmp.end());
12    for(auto v:tmp)ret=((ret*X)^v)%P;
13    return ret;
14 }
15 //-----
16 string dfs(int x,int p){
17     vector<string> c;
18     for(int y:g[x])
19         if(y!=p)c.emplace_back(dfs(y,x));
20     sort(c.begin(),c.end());
21     string ret("(");
22     for(auto &s:c)ret+=s;
23     ret+=")";
24     return ret;
25 }

```

## 5.11 全局最小割.cpp

```

1 const int INF=0x3f3f3f3f;
2 template<typename T>
3 struct stoer_wagner{// 0-base
4     static const int MAXN=150;
5     T g[MAXN][MAXN],dis[MAXN];
6     int nd[MAXN],n,s,t;
7     void init(int _n){
8         n=_n;
9         for(int i=0;i<n;++i)
10            for(int j=0;j<n;++j)g[i][j]=0;
11    }
12    void add_edge(int u,int v,T w){
13        g[u][v]=g[v][u]+=w;
14    }
15    T min_cut(){
16        T ans=INF;
17        for(int i=0;i<n;++i)nd[i]=i;
18        for(int ind,tn=n;tn>1;--tn){
19            for(int i=1;i<tn;++i)dis[nd[i]]=0;
20            for(int i=1;i<tn;++i){
21                ind=i;
22                for(int j=i;j<tn;++j){
23                    dis[nd[j]]+=g[nd[i-1]][nd[j]];
24                    if(dis[nd[ind]]<dis[nd[j]])ind=j;
25                }
26                swap(nd[ind],nd[i]);
27            }
28            if(ans>dis[nd[ind]])ans=dis[t=nd[ind]];
29            for(int i=0;i<tn;++i)
30                g[nd[ind-1]][nd[i]]=g[nd[i]][nd[ind-1]]+=g[nd[i]][nd[ind]];
31        }
32        return ans;
33    }
34 };

```

## 5.12 平面圖判定.cpp

```

1 static const int MAXN = 20;
2 struct Edge{
3     int u, v;
4     Edge(int s, int d) : u(s), v(d) {}
5 };
6 bool isK33(int n, int degree[]){
7     int t = 0, z = 0;
8     for(int i=0;i<n;++i){
9         if(degree[i] == 3)++t;
10        else if(degree[i] == 0)++z;
11        else return false;
12    }
13    return t == 6 && t + z == n;
14 }
15 bool isK5(int n, int degree[]){
16     int f = 0, z = 0;
17     for(int i=0;i<n;++i){
18         if(degree[i] == 4)++f;
19         else if(degree[i] == 0)++z;
20         else return false;
21    }
22    return f == 5 && f + z == n;
23 }
24 // it judge a given graph is Homeomorphic
25 // with K33 or K5
26 bool isHomeomorphic(bool G[MAXN][MAXN],
27                     const int n){
28     for(;;){
29         int cnt = 0;
30         for(int i=0;i<n;++i){
31             vector<Edge> E;
32             for(int j=0;j<n&&E.size()<3;++j)
33                 if(G[i][j] && i != j)
34                     E.push_back(Edge(i, j));
35             if(E.size() == 1){
36                 G[i][E[0].v] = G[E[0].v][i] = false;
37             }else if(E.size() == 2){
38                 G[i][E[0].v] = G[E[0].v][i] = false;
39                 G[i][E[1].v] = G[E[1].v][i] = false;
40                 G[E[0].v][E[1].v] = G[E[1].v][E[0].v]
41                     = true;
42                 ++cnt;
43             }
44         }
45         if(cnt == 0)break;
46     }
47     static int degree[MAXN];
48     fill(degree, degree + n, 0);
49     for(int i=0;i<n;++i){
50         for(int j=i+1;j<n;++j){
51             if(!G[i][j])continue;
52             ++degree[i];
53             ++degree[j];
54         }
55     }
56     return !(isK33(n, degree) || isK5(n, degree));
57 }

```

## 5.13 弦圖完美消除序列.cpp

```

1 struct chordal{
2     static const int MAXN=1005;
3     int n;// 0-base
4     vector<int>G[MAXN];
5     int rank[MAXN],label[MAXN];
6     bool mark[MAXN];
7     void init(int _n){n=_n;
8         for(int i=0;i<n;++i)G[i].clear();
9     }
10    void add_edge(int u,int v){
11        G[u].push_back(v);
12        G[v].push_back(u);
13    }
14    vector<int> MCS(){
15        memset(rank,-1,sizeof(int)*n);
16        memset(label,0,sizeof(int)*n);
17        priority_queue<pair<int,int> > pq;
18        for(int i=0;i<n;++i)pq.push(make_pair(0, i));
19        for(int i=n-1;i>=0;--i)for(;;){
20            int u=pq.top().second;pq.pop();
21            if(~rank[u])continue;
22            rank[u]=i;
23            for(auto v:G[u])if(rank[v]==-1){
24                pq.push(make_pair(++label[v],v));
25            }
26            break;
27        }
28        vector<int> res(n);
29        for(int i=0;i<n;++i)res[rank[i]]=i;
30        return res;
31    }
32    bool check(vector<int> ord){//弦圖判定
33        for(int i=0;i<n;++i)rank[ord[i]]=i;
34        memset(mark,0,sizeof(bool)*n);
35        for(int i=0;i<n;++i){
36            vector<pair<int,int> > tmp;
37            for(auto u:G[ord[i]])if(!mark[u])
38                tmp.push_back(make_pair(rank[u],u));
39            sort(tmp.begin(),tmp.end());
40            if(tmp.size()){
41                int u=tmp[0].second;
42                set<int> S;
43                for(auto v:G[u])S.insert(v);
44                for(size_t j=1;j<tmp.size();++j)
45                    if(!S.count(tmp[j].second))return 0;
46            }
47            mark[ord[i]]=1;
48        }
49        return 1;
50    }
51 };

```

## 5.14 最小斯坦納樹 DP.cpp

```

1 //n個點，其中r個要構成斯坦納樹
2 //答案在max(dp[(1<r)-1][k]) k=0~n-1
3 //p表示要構成斯坦納樹的點集
4 //O( n^3 + n^3*r + n^2*2^r )
5 #define REP(i,n) for(int i=0;i<(int)n;++i)
6 const int MAXN=30,MAXM=8;// 0-base

```

```

7 const int INF=0x3f3f3f3f;
8 int dp[1<MAXM][MAXN];
9 int g[MAXN][MAXN];
10 void init(){memset(g,0,sizeof(g));}
11 void add_edge(int u,int v,int w){
12     g[u][v]=g[v][u]=min(g[v][u],w);
13 }
14 void steiner(int n,int r,int *p){
15     REP(k,n)REP(i,n)REP(j,n)
16         g[i][j]=min(g[i][j],g[i][k]+g[k][j]);
17     REP(i,n)g[i][i]=0;
18     REP(i,r)REP(j,n)dp[1<i][j]=g[p[i]][j];
19     for(int i=1;i<(1<r);++i){
20         if(!(i&(i-1)))continue;
21         REP(j,n)dp[i][j]=INF;
22         REP(j,n){
23             int tmp=INF;
24             for(int s=i&(i-1);s;s=i&(s-1))
25                 tmp=min(tmp,dp[s][j]+dp[i^s][j]);
26             REP(k,n)dp[i][k]=min(dp[i][k],g[j][k]+tmp);
27         }
28     }
29 }

```

## 5.15 最小樹形圖 朱劉.cpp

```

1 template<typename T>
2 struct zhu_liu{
3     static const int MAXN=110,MAXM=10005;
4     struct node{
5         int u,v;
6         T w,tag;
7         node *l,*r;
8         node(int u=0,int v=0,T w=0):u(u),v(v),w(w),tag(0),l(0),r(0){}
9     }
10    void down(){
11        w+=tag;
12        if(l)l->tag+=tag;
13        if(r)r->tag+=tag;
14        tag=0;
15    }
16    mem[MAXN];
17    node *pq[MAXN*2],*E[MAXN*2];
18    int st[MAXN*2],id[MAXN*2],m;
19    void init(int n){
20        for(int i=1;i<n;++i){
21            pq[i]=E[i]=0, st[i]=id[i]=i;
22            m+=0;
23        }
24        node *merge(node *a,node *b){//skew heap
25            if(!a||!b)return a?a:b;
26            a->down(),b->down();
27            if(b->w<a->w)return merge(b,a);
28            swap(a->l,a->r);
29            a->l=merge(b,a->l);
30            return a;
31        }
32    void add_edge(int u,int v,T w){
33        if(u!=v)pq[v]=merge(pq[v],&(mem[m++]=node(u,v,w)));
34    }
35    int find(int x,int *st){
36
37    }
38 }

```

```

35     return st[x]==x?x:st[x]=find(st[x],st);
36 }
37 T build(int root,int n){
38     T ans=0;int N=n,all=n;
39     for(int i=1;i<=N;++i){
40         if(i==root||!pq[i])continue;
41         while(pq[i]){
42             pq[i]->down(),E[i]=pq[i];
43             pq[i]=merge(pq[i]->l,pq[i]->r);
44             if(find(E[i]->u,id)!=find(i,id))
45                 break;
46         }
47         if(find(E[i]->u,id)==find(i,id))
48             continue;
49         ans+=E[i]->w;
50         if(find(E[i]->u,st)==find(i,st)){
51             if(pq[i])pq[i]->tag-=E[i]->w;
52             pq[++N]=pq[i];id[N]=N;
53             for(int u=find(E[i]->u,id);u!=i;u=
54                 find(E[u]->u,id)){
55                 if(pq[u])pq[u]->tag-=E[u]->w;
56                 id[find(u,id)]=N;
57                 pq[N]=merge(pq[N],pq[u]);
58             }
59             st[N]=find(i,st);
60             id[find(i,id)]=N;
61             }else st[find(i,st)]=find(E[i]->u,st)
62             ,--all;
63     }
64     return all==1?ans:-INT_MAX;//圖不連通就
65     無解
66 }

```

## 5.16 穩定婚姻模板.cpp

```

1 queue<int> Q;
2 for ( i : 所有考生 ) {
3     設定在第0志願;
4     Q.push(考生i);
5 }
6 while(Q.size()){
7     當前考生=Q.front();Q.pop();
8     while ( 此考生未分發 ) {
9         指標移到下一志願;
10        if ( 已經沒有志願 or 超出志願總數 )
11            break;
12        計算該考生在該科系加權後的總分;
13        if ( 不符合科系需求 ) continue;
14        if ( 目前科系有餘額 ) {
15            依加權後分數高低順序將考生id加入科系錄取名單中;
16            break;
17        }
18        if ( 目前科系已額滿 ) {
19            if ( 此考生成績比最低分數還高 ) {
20                依加權後分數高低順序將考生id加入科系錄取名單;
21                Q.push(被踢出的考生);
22            }
23        }
24    }
25 }

```

```

22     }
23 }
24 }

```

## 6 language

### 6.1 CNF.cpp

```

1 #define MAXN 55
2 struct CNF{
3     int s,x,y;//s->xy | s->x, if y==-1
4     int cost;
5     CNF(){}
6     CNF(int s,int x,int y,int c):s(s),x(x),y(y),cost(c){}
7 };
8 int state;//規則數量
9 map<char,int> rule;//每個字元對應到的規則 ·
10    小寫字母為終端字元
11 vector<CNF> cnf;
12 void init(){
13     state=0;
14     rule.clear();
15     cnf.clear();
16 }
17 void add_to_cnf(char s,const string &p,int cost){
18     //加入一個s -> <p>的文法 · 代價為cost
19     if(rule.find(s)==rule.end())rule[s]=state++;
20     for(auto c:p)if(rule.find(c)==rule.end())rule[c]=state++;
21     if(p.size()==1){
22         cnf.push_back(CNF(rule[s],rule[p[0]],-1,cost));
23     }else{
24         int left=rule[s];
25         int sz=p.size();
26         for(int i=0;i<sz-2;++i){
27             cnf.push_back(CNF(left,rule[p[i]],state,0));
28             left=state++;
29             cnf.push_back(CNF(left,rule[p[sz-2]],rule[p[sz-1]],cost));
30         }
31     }
32     vector<long long> dp[MAXN][MAXN];
33     vector<bool> neg_INF[MAXN][MAXN];//如果花費
34     是負的可能會有無限小的情形
35     void relax(int l,int r,const CNF &c,long long cost,bool neg_c=0){
36         if(!neg_INF[l][r][c.s]&&(neg_INF[l][r][c.x]||cost>dp[l][r][c.s])){
37             if(neg_c||neg_INF[l][r][c.x]){
38                 dp[l][r][c.s]=0;
39                 neg_INF[l][r][c.s]=true;
40             }else dp[l][r][c.s]=cost;
41         }
42     }

```

```

42 void bellman(int l,int r,int n){
43     for(int k=1;k<=state;++k)
44         for(auto c:cnf)
45             if(c.y==-1)relax(l,r,c,dp[l][r][c.x]+c.cost,k=n);
46 }
47 void cyk(const vector<int> &tok){
48     for(int i=0;i<(int)tok.size();++i){
49         for(int j=0;j<(int)tok.size();++j){
50             dp[i][j]=vector<long long>(state+1,INT_MAX);
51             neg_INF[i][j]=vector<bool>(state+1,false);
52         }
53         dp[i][i][tok[i]]=0;
54         bellman(i,i,tok.size());
55     }
56     for(int r=1;r<(int)tok.size();++r){
57         for(int l=r-1;l>=0;--l){
58             for(int k=1;k<r;++k)
59                 for(auto c:cnf)
60                     if(~c.y)relax(l,r,c,dp[l][k][c.x]+dp[k+1][r][c.y]+c.cost);
61             bellman(l,r,tok.size());
62         }
63     }
64 }

```

## 7 Linear\_Programming

### 7.1 最大密度子圖.cpp

```

1 typedef double T;//POJ 3155
2 const int MAXN=105;
3 struct edge{
4     int u,v;
5     T w;
6     edge(int u=0,int v=0,T w=0):u(u),v(v),w(w){}
7 };
8 vector<edge> E;
9 int n,m;// 1-base
10 T de[MAXN],pv[MAXN];//每個點的邊權和和點權(
11    有些題目會給)
12 void init(){
13     E.clear();
14     for(int i=1;i<=n;++i)de[i]=pv[i]=0;
15 }
16 void add_edge(int u,int v,T w){
17     E.push_back(edge(u,v,w));
18     de[u]+=w,de[v]+=w;
19 }
20 T U;//二分搜的最大值
21 void get_U(){
22     U=0;
23     for(int i=1;i<=n;++i)U+=2*pv[i];
24     for(size_t i=0;i<E.size();++i)U+=E[i].w;
25 }
26 ISAP<T> isap;//網路流
27 int s,t;//原匯點

```

```

27 void build(T L){
28     isap.init(n+2);
29     for(size_t i=0;i<E.size();++i)
30         isap.add_edge(E[i].u,E[i].v,E[i].w);
31     for(int v=1;v<=n;++v){
32         isap.add_edge(s,v,U);
33         isap.add_edge(v,t,U+2*L-de[v]-2*pv[v]);
34     }
35 }
36 int main(){
37     while(~scanf("%d%d",&n,&m)){
38         if(!m){
39             puts("1\n1");
40             continue;
41         }
42         init();
43         int u,v;
44         for(int i=0;i<m;++i){
45             scanf("%d%d",&u,&v);
46             add_edge(u,v,1);
47         }
48         get_U();
49         s=n+1,t=n+2;
50         T l=0,r=U,k=1.0/(n*n);
51         while(r-l>k){//二分搜最大值
52             T mid=(l+r)/2;
53             build(mid);
54             T res=(U*n-isap.isap(s,t))/2;
55             if(res>0)l=mid;
56             else r=mid;
57         }
58         build(1);
59         isap.min_cut(s,t);
60         vector<int> ans;
61         for(int i=1;i<=n;++i)
62             if(isap.vis[i])ans.push_back(i);
63         printf("%d\n",ans.size());
64         for(size_t i=0;i<ans.size();++i)
65             printf("%d\n",ans[i]);
66     }
67     return 0;
68 }

```

## 8 Number\_Theory

### 8.1 basic.cpp

```

1 template<typename T>
2 void gcd(const T &a,const T &b,T &d,T &x,T &y){
3     if(!b) d=a,x=1,y=0;
4     else gcd(b,a%b,d,y,x), y-=x*(a/b);
5 }
6 long long int phi[N+1];
7 void phiTable(){
8     for(int i=1;i<=N;i++)phi[i]=i;
9     for(int i=1;i<=N;i++){
10         for(x=i*2;x<=N;x+=i)
11             phi[x]-=phi[i];
12     }
13 }
14 void all_divdown(const LL &n){ // all n/x
15     for(LL a=1;a<=n;a=n/(n/(a+1)))
16 }

```

```

13 // dosomething;
14 }
15 }
16 const int MAXPRIME = 1000000;
17 int iscom[MAXPRIME], prime[MAXPRIME],
    primecnt;
18 int phi[MAXPRIME], mu[MAXPRIME];
19 void sieve(void){
20     memset(iscom,0,sizeof(iscom));
21     primecnt = 0;
22     phi[1] = mu[1] = 1;
23     for(int i=2;i<MAXPRIME;++i) {
24         if(!iscom[i]) {
25             prime[primecnt++] = i;
26             mu[i] = -1;
27             phi[i] = i-1;
28         }
29         for(int j=0;j<primecnt;++j) {
30             int k = i * prime[j];
31             if(k>=MAXPRIME) break;
32             iscom[k] = prime[j];
33             if(i%prime[j]==0) {
34                 mu[k] = 0;
35                 phi[k] = phi[i] * prime[j];
36                 break;
37             } else {
38                 mu[k] = -mu[i];
39                 phi[k] = phi[i] * (prime[j]-1);
40             }
41         }
42     }
43 }
44 }
45 bool g_test(const LL &g, const LL &p, const
    vector<LL> &v) {
46     for(int i=0;i<v.size();++i)
47         if(modexp(g,(p-1)/v[i],p)==1)
48             return false;
49     return true;
50 }
51 LL primitive_root(const LL &p) {
52     if(p==2) return 1;
53     vector<LL> v;
54     Factor(p-1,v);
55     v.erase(unique(v.begin(), v.end()), v.end
        ());
56     for(LL g=2;g<p;++g)
57         if(g_test(g,p,v))
58             return g;
59     puts("primitive_root NOT FOUND");
60     return -1;
61 }
62 int Legendre(const LL &a, const LL &p) {
63     return modexp(a%p,(p-1)/2,p);
64 }
65 LL inv(const LL &a, const LL &n) {
66     LL d,x,y;
67     gcd(a,n,d,x,y);
68     return d==1 ? (x+n)%n : -1;
69 }
70 int inv[maxN];
71 LL invtable(int n,LL P){
72     inv[1]=1;
73     for(int i=2;i<n;++i)
74         inv[i]=(P-(P/i))*inv[P%i]%P;

```

```

75 }
76 }
77 LL log_mod(const LL &a, const LL &b, const
    LL &p) {
78     // a ^ x = b ( mod p )
79     int m=sqrt(p+.5), e=1;
80     LL v=inv(modexp(a,m,p), p);
81     map<LL,int> x;
82     x[1]=0;
83     for(int i=1;i<m;++i) {
84         e = LLmul(e,a,p);
85         if(!x.count(e)) x[e] = i;
86     }
87     for(int i=0;i<m;++i) {
88         if(x.count(b)) return i*m + x[b];
89         b = LLmul(b,v,p);
90     }
91     return -1;
92 }
93 }
94 LL Tonelli_Shanks(const LL &n, const LL &p)
    {
95     // x^2 = n ( mod p )
96     if(n==0) return 0;
97     if(Legendre(n,p)!=1) while(1) { puts("SQRT
        ROOT does not exist"); }
98     int S = 0;
99     LL Q = p-1;
100     while( !(Q&1) ) { Q>>=1; ++S; }
101     if(S==1) return modexp(n%p,(p+1)/4,p);
102     LL z = 2;
103     for(; Legendre(z,p)!=-1;++z)
104         LL c = modexp(z,Q,p);
105     LL R = modexp(n%p,(Q+1)/2,p), t = modexp(n
        %p,Q,p);
106     int M = S;
107     while(1) {
108         if(t==1) return R;
109         LL b = modexp(c,1L<<(M-i-1),p);
110         R = LLmul(R,b,p);
111         t = LLmul( LLmul(b,b,p), t, p);
112         c = LLmul(b,b,p);
113         M = i;
114     }
115     return -1;
116 }
117 }
118 template<typename T>
119 T Euler(T n){
120     T ans=n;
121     for(T i=2;i*i<=n;++i){
122         if(n%i==0){
123             ans=ans/i*(i-1);
124             while(n%i==0)n/=i;
125         }
126     }
127     if(n>1)ans=ans/n*(n-1);
128     return ans;
129 }
130 }
131 //Chinese_remainder_theorem
132 template<typename T>
133 T pow_mod(T n,T k,T m){
134     T ans=1;
135     for(n=(n>m?n%m:n);k;k>>=1){
136         if(k&1)ans=ans*n%m;

```

```

137     n=n*n%m;
138     }
139     return ans;
140 }
141 template<typename T>
142 T crt(vector<T> &m,vector<T> &a){
143     T M=1,tM,ans=0;
144     for(int i=0;i<(int)m.size();++i)M*=m[i];
145     for(int i=0;i<(int)a.size();++i){
146         tM=M/m[i];
147         ans=(ans+(a[i]*tM%M)*pow_mod(tM,Euler(m
            [i])-1,m[i])%M)%M;
148         /*如果m[i]是質數 · Euler(m[i])-1=m[i]-2 ·
            就不用算Euler了*/
149     }
150     return ans;
151 }
152 }
153 //java code
154 //求sqrt(N)的連分數
155 public static void Pell(int n){
156     BigInteger N,p1,p2,q1,q2,a0,a1,a2,g1,g2,h1
        ,h2,p,q;
157     g1=q2=p1=BigInteger.ZERO;
158     h1=q1=p2=BigInteger.ONE;
159     a0=a1=BigInteger.valueOf((int)Math.sqrt
        (1.0*n));
160     BigInteger ans=a0.multiply(a0);
161     if(ans.equals(BigInteger.valueOf(n))){
162         System.out.println("No solution!");
163         return ;
164     }
165     while(true){
166         g2=a1.multiply(h1).subtract(g1);
167         h2=N.subtract(g2.pow(2)).divide(h1);
168         a2=g2.add(a0).divide(h2);
169         p=a1.multiply(p2).add(p1);
170         q=a1.multiply(q2).add(q1);
171         if(p.pow(2).subtract(N.multiply(q.pow
            (2))).compareTo(BigInteger.ONE)==0)
172             break;
173         g1=g2;h1=h2;a1=a2;
174         p1=p2;p2=p;
175         q1=q2;q2=q;
176     }
177     System.out.println(p+" "+q);

```

## 8.2 bit\_set.cpp

```

1 void sub_set(int S){
2     int sub=S;
3     do{
4         //對某集合的子集合的處理
5         sub=(sub-1)&S;
6     }while(sub!=S);
7 }
8 void k_sub_set(int k,int n){
9     int comb=(1<<k)-1,S=1<n;
10    while(comb<S){
11        //對大小為k的子集合的處理
12        int x=comb&-comb,y=comb+x;

```

```

13    comb=((comb&~y)/x>>1)|y;
14 }
15 }

```

## 8.3 cantor\_expansion.cpp

```

1 int factorial[MAXN];
2 void init(){
3     factorial[0]=1;
4     for(int i=1;i<=MAXN;++i)factorial[i]=
        factorial[i-1]*i;
5 }
6 int encode(const vector<int> &s){
7     int n=s.size(),res=0;
8     for(int i=0;i<n;++i){
9         int t=0;
10        for(int j=i+1;j<n;++j)
11            if(s[j]<s[i])++t;
12        res+=t*factorial[n-i-1];
13    }
14    return res;
15 }
16 vector<int> decode(int a,int n){
17     vector<int> res;
18     vector<bool> vis(n,0);
19     for(int i=n-1;i>=0;--i){
20         int t=a/factorial[i],j;
21         for(j=0;j<n;++j)
22             if(!vis[j]){
23                 if(t==0)break;
24                 --t;
25             }
26         res.push_back(j);
27         vis[j]=1;
28         a%=factorial[i];
29     }
30     return res;
31 }

```

## 8.4 FFT.cpp

```

1 template<typename T,typename VT=vector<
    complex<T> >>
2 struct FFT{
3     const T pi;
4     FFT(const T pi=acos((-1)):pi(pi){}
5     unsigned bit_reverse(unsigned a,int len){
6         a=((a&0x55555555)<<1)|((a&0xAAAAAAAA)
            >>1);
7         a=((a&0x33333333)<<2)|((a&0xCCCCCCCC)
            >>2);
8         a=((a&0x0F0F0F0F)<<4)|((a&0xF0F0F0F0)
            >>4);
9         a=((a&0x00FF00FF)<<8)|((a&0xFF00FF00)
            >>8);
10        a=((a&0x0000FFFF)<<16)|((a&0xFFFF0000)
            >>16);
11        return a>>(32-len);
12    }

```

```

13 void fft(bool is_inv, VT &in, VT &out, int N)
14 {
15     int bitlen = __lg(N), num = is_inv ? -1 : 1;
16     for(int i=0; i<N; ++i) out[bit_reverse(i, bitlen)] = in[i];
17     for(int step=2; step<=N; step<=1){
18         const int mh=step>>1;
19         for(int i=0; i<mh; ++i){
20             complex<T> wi = exp(complex<T>(0, i*num
21                 *pi/mh));
22             for(int j=i; j<N; j+=step){
23                 int k=j+mh;
24                 complex<T> u=out[j], t=wi*out[k];
25                 out[j]=u+t;
26                 out[k]=u-t;
27             }
28         }
29     }
30     if(is_inv) for(int i=0; i<N; ++i) out[i]/=N;
31 }

```

## 8.5 find\_real\_root.cpp

```

1 // an*x^n + ... + a1x + a0 = 0;
2 int sign(double x){
3     return x < -eps ? -1 : x > eps;
4 }
5
6 double get(const vector<double>&coef, double
7     x){
8     double e = 1, s = 0;
9     for(auto i : coef) s += i*e, e *= x;
10    return s;
11 }
12
13 double find(const vector<double>&coef, int n
14     , double lo, double hi){
15     double sign_lo, sign_hi;
16     if( !(sign_lo = sign(get(coef, lo))) )
17         return lo;
18     if( !(sign_hi = sign(get(coef, hi))) )
19         return hi;
20     if(sign_lo * sign_hi > 0) return INF;
21     for(int stp = 0; stp < 100 && hi - lo >
22         eps; ++stp){
23         double m = (lo+hi)/2.0;
24         int sign_mid = sign(get(coef, m));
25         if(!sign_mid) return m;
26         if(sign_lo*sign_mid < 0) hi = m;
27         else lo = m;
28     }
29     return (lo+hi)/2.0;
30 }
31
32 vector<double> cal(vector<double>coef, int n
33 ) {
34     vector<double>res;
35     if(n == 1){
36         if(sign(coef[1])) res.pb(-coef[0]/coef
37             [1]);
38         return res;
39     }
40 }

```

## 8.6 FWT.cpp

```

1 vector<int> F_OR_T(vector<int> f, bool
2     inverse){
3     for(int i=0; (2<<i)<=f.size(); ++i)
4         for(int j=0; j<f.size(); j+=2<<i)
5             for(int k=0; k<(1<<i); ++k)
6                 f[j+k+(1<<i)] += f[j+k]*(inverse
7                     ? -1 : 1);
8     return f;
9 }
10 vector<int> rev(vector<int> A) {
11     for(int i=0; i<A.size(); i+=2)
12         swap(A[i], A[i^(A.size()-1)]);
13     return A;
14 }
15 vector<int> F_AND_T(vector<int> f, bool
16     inverse){
17     return rev(F_OR_T(rev(f), inverse));
18 }
19 vector<int> F_XOR_T(vector<int> f, bool
20     inverse){
21     for(int i=0; (2<<i)<=f.size(); ++i)
22         for(int j=0; j<f.size(); j+=2<<i)
23             for(int k=0; k<(1<<i); ++k){
24                 int u=f[j+k], v=f[j+k+(1<<i)];
25                 f[j+k+(1<<i)] = u-v, f[j+k] = u+v;
26             }
27     if(inverse) for(auto &a:f) a/=f.size();
28     return f;
29 }

```

## 8.7 LinearCongruence.cpp

```

1 pair<LL, LL> LinearCongruence(LL a[], LL b[],
2     LL m[], int n) {
3     // a[i]*x = b[i] ( mod m[i] )
4     for(int i=0; i<n; ++i) {
5         LL x, y, d = extgcd(a[i], m[i], x, y);

```

```

5         if(b[i]%d!=0) return make_pair(-1LL, 0LL)
6         ;
7         m[i] /= d;
8         b[i] = LLmul(b[i]/d, x, m[i]);
9     }
10    LL lastb = b[0], lastm = m[0];
11    for(int i=1; i<n; ++i) {
12        LL x, y, d = extgcd(m[i], lastm, x, y);
13        if((lastb-b[i])%d!=0) return make_pair
14            (-1LL, 0LL);
15        lastb = LLmul((lastb-b[i])/d, x, (lastm/d)
16            ) * m[i];
17        lastm = (lastm/d) * m[i];
18        lastb = (lastb+b[i])%lastm;
19    }
20    return make_pair(lastb<0?lastb+lastm:lastb
21        , lastm);
22 }

```

## 8.8 Lucas.cpp

```

1 int mod_fact(int n, int &e){
2     e=0;
3     if(n==0) return 1;
4     int res=mod_fact(n/P, e);
5     e += n/P;
6     if((n/P)%2==0) return res*fact[n%P]%P;
7     return res*(P-fact[n%P])%P;
8 }
9 int Cmod(int n, int m){
10    int a1, a2, a3, e1, e2, e3;
11    a1=mod_fact(n, e1);
12    a2=mod_fact(m, e2);
13    a3=mod_fact(n-m, e3);
14    if(e1>e2+e3) return 0;
15    return a1*inv(a2*a3%P, P)%P;
16 }

```

## 8.9 Matrix.cpp

```

1 template<typename T>
2 struct Matrix{
3     using rt = std::vector<T>;
4     using mt = std::vector<rt>;
5     using matrix = Matrix<T>;
6     int r, c;
7     mt m;
8     Matrix(int r, int c):r(r), c(c), m(r, rt(c)){}
9     rt& operator[](int i){return m[i];}
10    matrix operator+(const matrix &a){
11        matrix rev(r, c);
12        for(int i=0; i<r; ++i)
13            for(int j=0; j<c; ++j)
14                rev[i][j]=m[i][j]+a.m[i][j];
15        return rev;
16    }
17 }
18 matrix operator-(const matrix &a){
19     matrix rev(r, c);
20     for(int i=0; i<r; ++i)
21         for(int j=0; j<c; ++j)

```

```

21         rev[i][j]=m[i][j]-a.m[i][j];
22     return rev;
23 }
24 matrix operator*(const matrix &a){
25     matrix rev(r, a.c);
26     matrix tmp(a.c, a.r);
27     for(int i=0; i<a.r; ++i)
28         for(int j=0; j<a.c; ++j)
29             tmp[j][i]=a.m[i][j];
30     for(int i=0; i<r; ++i)
31         for(int j=0; j<a.c; ++j)
32             for(int k=0; k<a.c; ++k)
33                 rev.m[i][j]+=m[i][k]*tmp[j][k];
34     return rev;
35 }
36 bool inverse(){
37     Matrix t(r, r+c);
38     for(int y=0; y<r; y++){
39         t.m[y][c+y] = 1;
40         for(int x=0; x<c; ++x)
41             t.m[y][x]=m[y][x];
42     }
43     if( !t.gas() )
44         return false;
45     for(int y=0; y<r; y++){
46         for(int x=0; x<c; ++x)
47             m[y][x]=t.m[y][c+x]/t.m[y][y];
48         return true;
49     }
50 }
51 T gas(){
52     vector<T> lazy(r, 1);
53     bool sign=false;
54     for(int i=0; i<r; ++i){
55         if( m[i][i]==0 ) {
56             int j=i+1;
57             while(j<r && !m[j][i]) j++;
58             if(j==r) continue;
59             m[i].swap(m[j]);
60             sign=!sign;
61         }
62         for(int j=0; j<r; ++j){
63             if(i==j) continue;
64             lazy[j]=lazy[j]*m[i][i];
65             T mx=m[j][i];
66             for(int k=0; k<c; ++k)
67                 m[j][k]=m[j][k]*m[i][i]-m[i][k]*mx;
68         }
69     }
70     T det=sign?-1:1;
71     for(int i=0; i<r; ++i){
72         det = det*m[i][i];
73         det = det/lazy[i];
74         for(auto &j:m[i]) j/=lazy[i];
75     }
76     return det;
77 }

```

## 8.10 MillerRobin.cpp

```

1 LL LLmul(LL a, LL b, const LL &mod) {
2     LL ans=0;

```



```

3 while(b) {
4     if(b&1) {
5         ans+=a;
6         if(ans>=mod) ans-=mod;
7     }
8     a<<=1, b>>=1;
9     if(a>=mod) a-=mod;
10 }
11 return ans;
12 }
13 LL mod_mul(LL a,LL b,LL m){
14     a%=m,b%=m; /* fast for m < 2^58 */
15     LL y=(LL)((double)a*b/m+0.5);
16     LL r=(a*b-y*m)%m;
17     return r<0?r+m:r;
18 }
19 template<typename T>
20 T pow(T a,T b,T mod){ //a^b%mod
21     T ans=1;
22     for(;b;a=mod_mul(a,a,mod),b>>=1)
23         if(b&1)ans=mod_mul(ans,a,mod);
24     return ans;
25 }
26 int sprp[3]={2,7,61}; //int範圍可解
27 int llsp[7]={2,325,9375,28178,450775,9780504,
28 1795265022}; //至少unsigned long long範圍
29 template<typename T>
30 bool isprime(T n,int *sprp,int num){
31     if(n==2)return 1;
32     if(n<2||n%2==0)return 0;
33     int t=0;
34     T u=n-1;
35     for(;u%2==0;++t)u>>=1;
36     for(int i=0;i<num;++i){
37         T a=sprp[i]%n;
38         if(a==0||a==1||a==n-1)continue;
39         T x=pow(a,u,n);
40         if(x==1||x==n-1)continue;
41         for(int j=0;j<t;++j){
42             x=mod_mul(x,x,n);
43             if(x==1)return 0;
44             if(x==n-1)break;
45         }
46         if(x==n-1)continue;
47         return 0;
48     }
49     return 1;
50 }

```

## 8.11 NTT.cpp

```

1 2615053605667*(2^18)+1,3
2 15*(2^27)+1,31
3 479*(2^21)+1,3
4 7*17*(2^23)+1,3
5 3*3*211*(2^19)+1,5
6 25*(2^22)+1,3
7 template<typename T,typename VT=vector<T>>
8 struct NTT{
9     const T P,G;
10     NTT(T p=(1<<23)*7*17+1,T g=3):P(p),G(g){}

```

```

11 unsigned bit_reverse(unsigned a,int len){
12     //Look FFT.cpp
13 }
14 T pow_mod(T n,T k,T m){
15     T ans=1;
16     for(n=(n==m?n%m:n);k;k>>=1){
17         if(k&1)ans=ans*n%m;
18         n=n*n%m;
19     }
20     return ans;
21 }
22 void ntt(bool is_inv,VT &in,VT &out,int N)
23 {
24     int bitlen=__lg(N);
25     for(int i=0;i<N;++i)out[bit_reverse(i,
26         bitlen)]=in[i];
27     for(int step=2,id=1;step<=N;step<<=1,++
28         id){
29         T wn=pow_mod(G,(P-1)>>id,P),wi=1,u,t;
30         const int mh=step>>1;
31         for(int i=0;i<mh;++i){
32             for(int j=i;j<N;j+=step){
33                 u=out[j],t=wi*out[j+mh]%P;
34                 out[j]=u+t;
35                 out[j+mh]=u-t;
36                 if(out[j]>=P)out[j]-=P;
37                 if(out[j+mh]<0)out[j+mh]+=P;
38             }
39             wi=wi*wn%P;
40         }
41         if(is_inv){
42             for(int i=1;i<N/2;++i)swap(out[i],out[
43                 N-i]);
44             T invn=pow_mod(N,P-2,P);
45             for(int i=0;i<N;++i)out[i]=out[i]*invn
46                 %P;
47         }
48     }
49 }

```

## 8.12 Simpson.cpp

```

1 double simpson(double a,double b){
2     double c=a+(b-a)/2;
3     return (F(a)+4*F(c)+F(b))*(b-a)/6;
4 }
5 double asr(double a,double b,double eps,
6     double A){
7     double c=a+(b-a)/2;
8     double L=simpson(a,c),R=simpson(c,b);
9     if( abs(L+R-A)<15*eps )
10         return L+R+(L+R-A)/15.0;
11     return asr(a,c,eps/2,L)+asr(c,b,eps/2,R);
12 }
13 double asr(double a,double b,double eps){
14     return asr(a,b,eps,simpson(a,b));
15 }

```

## 8.13 外星模運算.cpp

```

1 //a[0]^(a[1]^a[2]^...)
2 #define maxn 1000000
3 int euler[maxn+5];
4 bool is_prime[maxn+5];
5 void init_euler(){
6     is_prime[1]=1; //不是質數
7     for(int i=1;i<=maxn;i++)euler[i]=i;
8     for(int i=2;i<=maxn;i++){
9         if(!is_prime[i]){ //是質數
10             euler[i]--;
11             for(int j=i<1;j<=maxn;j+=i){
12                 is_prime[j]=1;
13                 euler[j]=euler[j]/i*(i-1);
14             }
15         }
16     }
17 }
18 LL pow(LL a,LL b,LL mod){ //a^b%mod
19     LL ans=1;
20     for(;b;a=a*a%mod,b>>=1)
21         if(b&1)ans=ans*a%mod;
22     return ans;
23 }
24 bool isless(LL *a,int n,int k){
25     if(*a==1)return k>1;
26     if(--n==0)return *a<k;
27     int next=0;
28     for(LL b=1;b<k;++next)
29         b*=*a;
30     return isless(a+1,n,next);
31 }
32 LL high_pow(LL *a,int n,LL mod){
33     if(*a==1||--n==0)return *a%mod;
34     int k=0,r=euler[mod];
35     for(LL tma=1;tma!=pow(*a,k+r,mod);++k)
36         tma=tma*(*a)%mod;
37     if(isless(a+1,n,k))return pow(*a,high_pow(
38         a+1,n,k),mod);
39     int tmd=high_pow(a+1,n,r), t=(tmd-k+r)%r;
40     return pow(*a,k+t,mod);
41 }
42 LL a[1000005];
43 int t,mod;
44 int main(){
45     init_euler();
46     scanf("%d",&t);
47     #define n 4
48     while(t--){
49         for(int i=0;i<n;++i)scanf("%Ld",&a[i]);
50         scanf("%d",&mod);
51         printf("%Ld\n",high_pow(a,n,mod));
52     }
53     return 0;
54 }

```

## 8.14 質因數分解.cpp

```

1 LL func(const LL n,const LL mod,const int c)
2 {
3     return (LLmul(n,n,mod)+c+mod)%mod;
4 }

```

```

5 LL pollrho(const LL n, const int c) { //循
6     環節長度
7     LL a=1, b=1;
8     a=func(a,n,c)%n;
9     b=func(b,n,c)%n; b=func(b,n,c)%n;
10     while(gcd(abs(a-b),n)==1) {
11         a=func(a,n,c)%n;
12         b=func(b,n,c)%n; b=func(b,n,c)%n;
13     }
14     return gcd(abs(a-b),n);
15 }
16 void prefactor(LL &n, vector<LL> &v) {
17     for(int i=0;i<12;++i) {
18         while(n%prime[i]==0) {
19             v.push_back(prime[i]);
20             n/=prime[i];
21         }
22     }
23 }
24 void smallfactor(LL n, vector<LL> &v) {
25     if(n<MAXPRIME) {
26         while(isp[prime[i]]) {
27             v.push_back(isp[prime[i]]);
28             n/=isp[prime[i]];
29         }
30     }
31     v.push_back(n);
32 } else {
33     for(int i=0;i<primecnt&&prime[i]*prime[i]
34         ]<=n;++i) {
35         while(n%prime[i]==0) {
36             v.push_back(prime[i]);
37             n/=prime[i];
38         }
39         if(n!=1) v.push_back(n);
40     }
41 }
42 void comfactor(const LL &n, vector<LL> &v) {
43     if(n<1e9) {
44         smallfactor(n,v);
45         return;
46     }
47     if(Isprime(n)) {
48         v.push_back(n);
49         return;
50     }
51     LL d;
52     for(int c=3;++c) {
53         d = pollrho(n,c);
54         if(d!=n) break;
55     }
56     comfactor(d,v);
57     comfactor(n/d,v);
58 }
59 }
60 void Factor(const LL &x, vector<LL> &v) {
61     LL n = x;
62     if(n==1) { puts("Factor 1"); return; }
63     prefactor(n,v);
64     if(n==1) return;
65     comfactor(n,v);
66     sort(v.begin(),v.end());
67 }

```

```

68 }
69
70 void AllFactor(const LL &n,vector<LL> &v) {
71     vector<LL> tmp;
72     Factor(n,tmp);
73     v.clear();
74     v.push_back(1);
75     int len;
76     LL now=1;
77     for(int i=0;i<tmp.size();++i) {
78         if(i==0 || tmp[i]!=tmp[i-1]) {
79             len = v.size();
80             now = 1;
81         }
82         now*=tmp[i];
83         for(int j=0;j<len;++j)
84             v.push_back(v[j]*now);
85     }
86 }

```

## 9 other

### 9.1 WhatDay.cpp

```

1 int whatday(int y,int m,int d){
2     if(m<=2)m+=12,-y;
3     if(y<1752||y==1752&&m<9||y==1752&&m==9&&d<3)
4         return (d+2*m+3*(m+1)/5+y+y/4+5)%7;
5     return (d+2*m+3*(m+1)/5+y+y/4-y/100+y/400)
6         %7;
}

```

### 9.2 上下最大正方形.cpp

```

1 void solve(int n,int a[],int b[]){// 1-base
2     int ans=0;
3     deque<int>da,db;
4     for(int l=1,r=1;r<n;++r){
5         while(da.size()&&a[da.back()]>a[r]){
6             da.pop_back();
7         }
8         da.push_back(r);
9         while(db.size()&&b[db.back()]>b[r]){
10             db.pop_back();
11         }
12         db.push_back(r);
13         for(int d=a[da.front()]+b[db.front()];r-1+l>d;++l){
14             if(da.front()==l)da.pop_front();
15             if(db.front()==l)db.pop_front();
16             if(da.size()&&db.size()){
17                 d=a[da.front()]+b[db.front()];
18             }
19         }
20         ans=max(ans,r-l+1);
21     }
22     printf("%d\n",ans);
}

```

23| }

### 9.3 最大矩形.cpp

```

1 LL max_rectangle(vector<int> s){
2     stack<pair<int,int> > st;
3     st.push(make_pair(-1,0));
4     s.push_back(0);
5     LL ans=0;
6     for(size_t i=0;i<s.size();++i){
7         int h=s[i];
8         pair<int,int> now=make_pair(h,i);
9         while(h<st.top().first){
10             now=st.top();
11             st.pop();
12             ans=max(ans,(LL)(i-now.second)*now.first);
13         }
14         if(h>st.top().first){
15             st.push(make_pair(h,now.second));
16         }
17     }
18     return ans;
19 }

```

## 10 String

### 10.1 AC 自動機.cpp

```

1 template<char L='a',char R='z'>
2 class ac_automaton{
3     struct joe{
4         int next[R-L+1],fail,efl,ed,cnt_dp,vis;
5         joe():ed(0),cnt_dp(0),vis(0){
6             for(int i=0;i<=R-L;++i)next[i]=0;
7         }
8     };
9     public:
10         std::vector<joe> S;
11         std::vector<int> q;
12         int qs,qe,vt;
13         ac_automaton():S(1),qs(0),qe(0),vt(0){}
14         void clear(){
15             q.clear();
16             S.resize(1);
17             for(int i=0;i<=R-L;++i)S[0].next[i]=0;
18             S[0].cnt_dp=S[0].vis=qs=qe=vt=0;
19         }
20         void insert(const char *s){
21             int o=0;
22             for(int i=0,id;s[i];++i){
23                 id=s[i]-L;
24                 if(!S[o].next[id]){
25                     S.push_back(joe());
26                     S[o].next[id]=S.size()-1;
27                 }
28                 o=S[o].next[id];
29             }
}

```

```

30 ++S[o].ed;
31 }
32 void build_fail(){
33     S[0].fail=S[0].efl=-1;
34     q.clear();
35     q.push_back(0);
36     ++qe;
37     while(qs!=qe){
38         int pa=q[qs++],id,t;
39         for(int i=0;i<=R-L;++i){
40             t=S[pa].next[i];
41             if(!t)continue;
42             id=S[pa].fail;
43             while(~id&&!S[id].next[i])id=S[id].fail;
44             S[t].fail=~id?S[id].next[i]:0;
45             S[t].efl=S[t].fail.ed?S[t].fail:S[t].fail;
46             q.push_back(t);
47             ++qe;
48         }
49     }
50 }
51 /*DP出每個前綴在字串s出現的次數並傳回所有
52 字串被s匹配成功的次數O(N*M)*/
53 int match_0(const char *s){
54     int ans=0,id,p=0,i;
55     for(i=0;s[i];++i){
56         id=s[i]-L;
57         while(!S[p].next[id]&&p=S[p].fail;
58             if(!S[p].next[id])continue;
59         p=S[p].next[id];
60         ++S[p].cnt_dp; /*匹配成功則它所有後綴都
61             可以被匹配(DP計算)*/
62     }
63     for(i=qe-1;i>=0;--i){
64         ans+=S[q[i]].cnt_dp*S[q[i]].ed;
65         if(~S[q[i]].fail)S[q[i]].fail;
66         cnt_dp+=S[q[i]].cnt_dp;
67     }
68     return ans;
69 }
70 /*多串匹配走efl邊並傳回所有字串被s匹配成功
71 的次數O(N*M^1.5)*/
72 int match_1(const char *s)const{
73     int ans=0,id,p=0,t;
74     for(int i=0;s[i];++i){
75         id=s[i]-L;
76         while(!S[p].next[id]&&p=S[p].fail;
77             if(!S[p].next[id])continue;
78         p=S[p].next[id];
79         if(S[p].ed)ans+=S[p].ed;
80         for(t=S[p].efl;~t;t=S[t].efl){
81             ans+=S[t].ed; /*因為都走efl邊所以保證
82             匹配成功*/
83         }
84     }
85     return ans;
86 }
87 /*枚舉(s的子串nA)的所有相異字串各恰一次
88 並傳回次數O(N*M^(1/3))*/
89 int match_2(const char *s){
90     int ans=0,id,p=0,t;
91     ++vt;
}

```

```

86 /*把截記vt+=1，只要vt沒溢位，所有S[p].
87 vis==vt就會變成false
88 這種利用vt的方法可以O(1)歸零vis陣列*/
89 for(int i=0;s[i];++i){
90     id=s[i]-L;
91     while(!S[p].next[id]&&p=S[p].fail;
92         if(!S[p].next[id])continue;
93     p=S[p].next[id];
94     if(S[p].ed&&S[p].vis!=vt){
95         S[p].vis=vt;
96         ans+=S[p].ed;
97     }
98     for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[t].efl){
99         S[t].vis=vt;
100         ans+=S[t].ed; /*因為都走efl邊所以保證
101         匹配成功*/
102     }
103     return ans;
104 }
105 /*把AC自動機變成真的自動機*/
106 void evolution(){
107     for(qs=1;qs!=qe;){
108         int p=q[qs++];
109         for(int i=0;i<=R-L;++i)
110             if(S[p].next[i]==0)S[p].next[i]=S[S[p].fail].next[i];
111     }
112 }
}

```

### 10.2 hash.cpp

```

1 #define MAXN 1000000
2 #define MOD 1073676287
3 /*mod 必須要是質數*/
4 typedef long long T;
5 char s[MAXN+5];
6 T h[MAXN+5]; /*hash陣列*/
7 T h_base[MAXN+5]; /*h_base[n]=(prime^n)%mod*/
8 inline void hash_init(int len,T prime=0
9     xdefaced){
10     h_base[0]=1;
11     for(int i=1;i<=len;++i){
12         h[i]=(h[i-1]*prime+s[i-1])%mod;
13         h_base[i]=(h_base[i-1]*prime)%mod;
14     }
15 }
16 inline T get_hash(int l,int r){/*閉區間寫
17     法，設編號為0~len-1*/
18     return (h[r+1]-(h[l]*h_base[r-l+1])%mod+
19         mod)%mod;
}

```

### 10.3 KMP.cpp

```

1  /*產生fail function*/
2  void kmp_fail(char *s,int len,int *fail){
3      int id=-1;
4      fail[0]=-1;
5      for(int i=1;i<len;++i){
6          while(~id&&s[id+1]!=s[i])id=fail[id];
7          if(s[id+1]==s[i])++id;
8          fail[i]=id;
9      }
10 }
11 /*以字串B匹配字串A，傳回匹配成功的數量(用B的
    fail)*/
12 int kmp_match(char *A,int lenA,char *B,int
    lenB,int *fail){
13     int id=-1,ans=0;
14     for(int i=0;i<lenA;++i){
15         while(~id&&B[id+1]!=A[i])id=fail[id];
16         if(B[id+1]==A[i])++id;
17         if(id==lenB-1){/*匹配成功*/
18             ++ans, id=fail[id];
19         }
20     }
21     return ans;
22 }

```

## 10.4 manacher.cpp

```

1  //原字串: asdsasdsa
2  //先把字串變成這樣: @#a#s#d#s#a#s#d#s#a#
3  inline void manacher(char *s,int len,int *z)
4  {
5      int l=0,r=0;
6      for(int i=1;i<len;++i){
7          z[i]=r>i?min(z[2*i-l],r-i):1;
8          while(s[i+z[i]]==s[i-z[i]])++z[i];
9          if(z[i]+i>r)r=z[i]+i,l=i;
10 }

```

## 10.5 minimal\_string\_rotation.cpp

```

1  int min_string_rotation(const string &s){
2      int n=s.size(),i=0,j=1,k=0;
3      while(i<n&&j<n&&k<n){
4          int t=s[(i+k)%n]-s[(j+k)%n];
5          ++k;
6          if(t){
7              if(t>0)i+=k;
8              else j+=k;
9              if(i==j)++j;
10             k=0;
11         }
12     }
13     return min(i,j);/*傳回最小循環表示法起始位
        置
14 }

```

## 10.6 reverseBWT.cpp

```

1  const int MAXN = 305, MAXC = 'Z';
2  int ranks[MAXN], tots[MAXN], first[MAXN];
3  void rankBWT(const string &bw){
4      memset(ranks,0,sizeof(int)*bw.size());
5      memset(tots,0,sizeof(tots));
6      for(size_t i=0;i<bw.size();++i)
7          ranks[i] = tots[int(bw[i])]+1;
8  }
9  void firstCol(){
10     memset(first,0,sizeof(first));
11     int totc = 0;
12     for(int c='A';c<='Z';++c){
13         if(!tots[c]) continue;
14         first[c] = totc;
15         totc += tots[c];
16     }
17 }
18 string reverseBwt(const string &bw,int begin
    ){
19     rankBWT(bw), firstCol();
20     int i = begin; /*原本字串最後一個元素的位
        置
21     string res;
22     do{
23         char c = bw[i];
24         res = c + res;
25         i = first[int(c)] + ranks[i];
26     }while( i != begin );
27     return res;
28 }

```

## 10.7 suffix\_array\_lcp.cpp

```

1  #define radix_sort(x,y){\
2      for(i=0;i<A;++i)c[i]=0;\
3      for(i=0;i<n;++i)c[x[y[i]]]++;\
4      for(i=1;i<A;++i)c[i]+=c[i-1];\
5      for(i=n-1;~i;--i)sa[--c[x[y[i]]]]=y[i];\
6  }
7  #define sac(r,a,b) r[a]!=(r[b]||a+k>n||r[a+k
    ]!=r[b+k])
8  void suffix_array(const char *s,int n,int *
    sa,int *rank,int *tmp,int *c){
9      int A='Z'+1,i,k,id=0;
10     for(i=0;i<n;++i)rank[tmp[i]=i]=s[i];
11     radix_sort(rank,tmp);
12     for(k=1;id<n-1;k<=1){
13         for(id=0,i=n-k;i<n;++i)tmp[id++] = i;
14         for(i=0;i<n;++i)if(sa[i]>k)tmp[id++] = sa
            [i]-k;
15         radix_sort(rank,tmp);
16         swap(rank,tmp);
17         for(rank[sa[0]]=id=0,i=1;i<n;++i)
18             rank[sa[i]]=id+sac(tmp,sa[i-1],sa[i])
                ;
19         A=id+1;
20     }
21 }
22 //h:高度數組 sa:後綴數組 rank:排名

```

```

23 void suffix_array_lcp(const char *s,int len,
    int *h,int *sa,int *rank){
24     for(int i=0;i<len;++i)rank[sa[i]]=i;
25     for(int i=0,k=0;i<len;++i){
26         if(rank[i]==0)continue;
27         if(k)--k;
28         while(s[i+k]==s[sa[rank[i]-1]+k])++k;
29         h[rank[i]]=k;
30     }
31     h[0]=0;
32 }

```

## 10.8 Z.cpp

```

1  void z_alg(char *s,int len,int *z){
2      int l=0,r=0;
3      z[0]=len;
4      for(int i=1;i<len;++i){
5          z[i]=i>r?0:(i-l+z[i-l]<z[l]?z[i-l]:r-i
              +1);
6          while(i+z[i]<len&&s[i+z[i]]==s[z[i]]++)z
              [i];
7          if(i+z[i]-1>r)r=i+z[i]-1,l=i;
8      }
9  }

```

## 11 Tarjan

### 11.1 dominator\_tree.cpp

```

1  struct dominator_tree{
2      static const int MAXN=5005;
3      int n; /* 1-base
4      vector<int> suc[MAXN],pre[MAXN];
5      int fa[MAXN],dfn[MAXN],id[MAXN],Time;
6      int semi[MAXN],idom[MAXN];
7      int anc[MAXN],best[MAXN]; /*disjoint set
8      vector<int> dom[MAXN]; /*dominator_tree
9      void init(int _n){
10         n=_n;
11         for(int i=1;i<=n;++i)suc[i].clear(),pre[
            i].clear();
12     }
13     void add_edge(int u,int v){
14         suc[u].push_back(v);
15         pre[v].push_back(u);
16     }
17     void dfs(int u){
18         dfn[u]=++Time,id[Time]=u;
19         for(auto v:suc[u]){
20             if(dfn[v])continue;
21             dfs(v),fa[dfn[v]]=dfn[u];
22         }
23     }
24     int find(int x){
25         if(x==anc[x])return x;
26         int y=find(anc[x]);

```

```

27         if(semi[best[x]]>semi[best[anc[x]]])best
            [x]=best[anc[x]];
28         return anc[x]=y;
29     }
30     void tarjan(int r){
31         Time=0;
32         for(int t=1;t<=n;++t){
33             dfn[t]=idom[t]=0; /*u=r或是u無法到達r時
34                 idom[id[u]]=0
35             dom[t].clear();
36             anc[t]=best[t]=semi[t]=t;
37         }
38         dfs(r);
39         for(int y=Time;y>=2;--y){
40             int x=fa[y],idy=id[y];
41             for(auto z:pre[idy]){
42                 if(!(z=dfn[z]))continue;
43                 find(z);
44                 semi[y]=min(semi[y],semi[best[z]]);
45             }
46             dom[semi[y]].push_back(y);
47             anc[y]=x;
48             for(auto z:dom[x]){
49                 find(z);
50                 idom[z]=semi[best[z]]<x?best[z]:x;
51             }
52             dom[x].clear();
53         }
54         for(int u=2;u<=Time;++u){
55             if(idom[u]!=semi[u])idom[u]=idom[idom[
                u]];
56             dom[id[idom[u]]].push_back(id[u]);
57         }
58     }dom;

```

### 11.2 tnfsb017\_2\_sat.cpp

```

1  #include<bits/stdc++.h>
2  using namespace std;
3  #define MAXN 8001
4  #define MAXN2 MAXN*4
5  #define n(X) ((X)+2*MAXN)
6  vector<int> v[MAXN2], rv[MAXN2], vis_t;
7  int N,M;
8  void addedge(int s,int e){
9      v[s].push_back(e);
10     rv[e].push_back(s);
11 }
12 int scc[MAXN2];
13 bool vis[MAXN2]={false};
14 void dfs(vector<int> *uv,int n,int k=-1){
15     vis[n]=true;
16     for(int i=0;i<uv[n].size();++i)
17         if(!vis[uv[n][i]])
18             dfs(uv,uv[n][i],k);
19     if(uv==v)vis_t.push_back(n);
20     scc[n]=k;
21 }
22 void solve(){
23     for(int i=1;i<=N;++i){
24         if(!vis[i])dfs(v,i);
25         if(!vis[n(i)])dfs(v,n(i));

```

```

26 }
27 memset(vis,0,sizeof(vis));
28 int c=0;
29 for(int i=vis_t.size()-1;i>=0;--i)
30     if(!vis[vis_t[i]])
31         dfs(rv,vis_t[i],c++);
32 }
33 int main(){
34     int a,b;
35     scanf("%d%d",&N,&M);
36     for(int i=1;i<=N;++i){
37         // (A or B)&(!A & !B) A^B
38         a=i*2-1;
39         b=i*2;
40         addedge(n(a),b);
41         addedge(n(b),a);
42         addedge(a,n(b));
43         addedge(b,n(a));
44     }
45     while(M--){
46         scanf("%d%d",&a,&b);
47         a = a>0?a*2-1:-a*2;
48         b = b>0?b*2-1:-b*2;
49         // A or B
50         addedge(n(a),b);
51         addedge(n(b),a);
52     }
53     solve();
54     bool check=true;
55     for(int i=1;i<=2*N;++i)
56         if(scc[i]==scc[n(i)])
57             check=false;
58     if(check){
59         printf("%d\n",N);
60         for(int i=1;i<=2*N;i+=2){
61             if(scc[i]>scc[i+2*N]) putchar('+');
62             else putchar('-');
63         }
64         puts("");
65     }else puts("0");
66     return 0;
67 }

```

### 11.3 橋連通分量.cpp

```

1 #define N 1005
2 struct edge{
3     int u,v;
4     bool is_bridge;
5     edge(int u=0,int v=0):u(u),v(v),is_bridge
6         (0){}
7 };
8 vector<edge> E;
9 vector<int> G[N];// 1-base
10 int low[N],vis[N],Time;
11 int bcc_id[N],bridge_cnt,bcc_cnt;// 1-base
12 int st[N],top;//BCC用
13 inline void add_edge(int u,int v){
14     G[u].push_back(E.size());
15     E.push_back(edge(u,v));
16     G[v].push_back(E.size());
17     E.push_back(edge(v,u));

```

```

18 void dfs(int u,int re=-1){//u當前點·re為u連
19     接前一個點的邊
20     int v;
21     low[u]=vis[u]=++Time;
22     st[top++]=u;
23     for(size_t i=0;i<G[u].size();++i){
24         int e=G[u][i];v=E[e].v;
25         if(!vis[v]){
26             dfs(v,e^1);//e^1反向邊
27             low[u]=min(low[u],low[v]);
28             if(vis[u]<low[v]){
29                 E[e].is_bridge=E[e^1].is_bridge=1;
30                 ++bridge_cnt;
31             }else if(vis[v]<vis[u]&&e!=re)
32                 low[u]=min(low[u],vis[v]);
33         }
34         if(vis[u]==low[u]){//處理BCC
35             ++bcc_cnt;// 1-base
36             do bcc_id[v=st[--top]]=bcc_cnt;//每個點
37                 所在的BCC
38             while(v!=u);
39         }
40     }
41     inline void bcc_init(int n){
42         Time=bcc_cnt=bridge_cnt=top=0;
43         E.clear();
44         for(int i=1;i<=n;++i){
45             G[i].clear();
46             vis[i]=bcc_id[i]=0;
47         }

```

### 11.4 雙連通分量 & 割點.cpp

```

1 #define N 1005
2 vector<int> G[N];// 1-base
3 vector<int> bcc[N];//存每塊雙連通分量的點
4 int low[N],vis[N],Time;
5 int bcc_id[N],bcc_cnt;// 1-base
6 bool is_cut[N];//是否為割點
7 int st[N],top;
8 void dfs(int u,int pa=-1){//u當前點·pa父親
9     int v,child=0;
10    low[u]=vis[u]=++Time;
11    st[top++]=u;
12    for(size_t i=0;i<G[u].size();++i){
13        if(!vis[v=G[u][i]]){
14            dfs(v,u,++child;
15            low[u]=min(low[u],low[v]);
16            if(vis[u]<low[v]){
17                is_cut[u]=1;
18                bcc[++bcc_cnt].clear();
19                int t;
20                do{
21                    bcc_id[t=st[--top]]=bcc_cnt;
22                    bcc[bcc_cnt].push_back(t);
23                }while(t!=v);
24                bcc_id[u]=bcc_cnt;
25                bcc[bcc_cnt].push_back(u);
26            }

```

```

27 }else if(vis[v]<vis[u]&&v!=pa)//反向邊
28     low[u]=min(low[u],vis[v]);
29 }
30 if(pa!=-1&&child<2)is_cut[u]=0;//u是dfs樹
31     的根要特判
32 }
33 inline void bcc_init(int n){
34     Time=bcc_cnt=top=0;
35     for(int i=1;i<=n;++i){
36         G[i].clear();
37         is_cut[i]=vis[i]=bcc_id[i]=0;
38     }

```

## 12 Tree\_problem

### 12.1 HeavyLight.cpp

```

1 #include<vector>
2 #define MAXN 100005
3 int siz[MAXN],max_son[MAXN],pa[MAXN],dep[
4     MAXN];
5 int link_top[MAXN],link[MAXN],cnt;
6 vector<int> G[MAXN];
7 void find_max_son(int u){
8     siz[u]=1;
9     max_son[u]=-1;
10    for(auto v:G[u]){
11        if(v==pa[u])continue;
12        pa[v]=u;
13        dep[v]=dep[u]+1;
14        find_max_son(v);
15        if(max_son[u]==-1||siz[v]>siz[max_son[u]
16            ])max_son[u]=v;
17        siz[u]+=siz[v];
18    }
19 }
20 void build_link(int u,int top){
21     link[u]=++cnt;
22     link_top[u]=top;
23     if(max_son[u]==-1)return;
24     build_link(max_son[u],top);
25     for(auto v:G[u]){
26         if(v==pa[u])continue;
27         build_link(v,v);
28     }
29 }
30 int find_lca(int a,int b){
31     //求LCA·可以在過程中對區間進行處理
32     int ta=link_top[a],tb=link_top[b];
33     while(ta!=tb){
34         if(dep[ta]<dep[tb]){
35             swap(ta,tb);
36             swap(a,b);
37         }
38         //這裡可以對a所在的鏈做區間處理
39         //區間為(Link[ta],Link[a])
40         ta=link_top[a=pa[ta]];

```

```

41 //最後a,b會在同一條鏈·若a!=b還要在進行一
42     次區間處理
43     return dep[a]<dep[b]?a:b;
44 }

```

### 12.2 LCA.cpp

```

1 #define MAXN 100000
2 #define MAX_LOG 17
3 int pa[MAX_LOG+1][MAXN+5];
4 int dep[MAXN+5];
5 vector<int> G[MAXN+5];
6 void dfs(int x,int p){//dfs(1,-1);
7     pa[0][x]=p;
8     for(int i=0;i+1<MAX_LOG;++i)pa[i+1][x]=pa[
9         i][pa[i][x]];
10    for(auto &i:G[x]){
11        if(i==p)continue;
12        dep[i]=dep[x]+1;
13        dfs(i,x);
14    }
15 }
16 inline int jump(int x,int d){
17     for(int i=0;i<d;++i)if((x>>i)&1)x=pa[i][x];
18     return x;
19 }
20 inline int find_lca(int a,int b){
21     if(dep[a]>dep[b])swap(a,b);
22     b=jump(b,dep[b]-dep[a]);
23     if(a==b)return a;
24     for(int i=MAX_LOG;i>=0;--i){
25         if(pa[i][a]!=pa[i][b]){
26             a=pa[i][a];
27             b=pa[i][b];
28         }
29     }
30     return pa[0][a];

```

### 12.3 link\_cut\_tree.cpp

```

1 struct splay_tree{
2     int ch[2],pa;//子節點跟父母
3     bool rev;//反轉的懶惰標記
4     splay_tree():pa(0),rev(0){ch[0]=ch[1]=0;}
5 };
6 vector<splay_tree> node;
7 //有的時候用vector會TLE·要注意
8 //這邊以node[0]作為null節點
9 bool isroot(int x){//判斷是否為這棵splay
10     tree的根
11     return node[node[x].pa].ch[0]!&x&&node[
12         node[x].pa].ch[1]!&x;
13 }
14 void down(int x){//懶惰標記下推
15     if(node[x].rev){
16         if(node[x].ch[0])node[node[x].ch[0]].rev
17             ^=1;

```



```

15     if(node[x].ch[1]node[node[x].ch[1]].rev
16         ^=1;
17     std::swap(node[x].ch[0],node[x].ch[1]);
18     node[x].rev^=1;
19 }
20 void push_down(int x){//將所有祖先的懶惰標記
21     下推
22     if(!isroot(x))push_down(node[x].pa);
23     down(x);
24 }
25 void up(int x){//將子節點的資訊向上更新
26 void rotate(int x){//旋轉，會自行判斷轉的方向
27     int y=node[x].pa,z=node[y].pa,d=(node[y].
28     ch[1]==x);
29     node[x].pa=z;
30     if(!isroot(y))node[z].ch[node[z].ch[1]==y
31     ]=x;
32     node[y].ch[d]=node[x].ch[d^1];
33     node[node[y].ch[d]].pa=y;
34     node[y].pa=x,node[x].ch[d^1]=y;
35     up(y),up(x);
36 }
37 void splay(int x){//將節點x伸展到所在splay
38     tree的根
39     push_down(x);
40     while(!isroot(x)){
41         int y=node[x].pa;
42         if(!isroot(y)){
43             int z=node[y].pa;
44             if((node[z].ch[0]==y)^(node[y].ch[0]==
45             x))rotate(y);
46             else rotate(x);
47         }
48         rotate(x);
49     }
50 }
51 int access(int x){
52     int last=0;
53     while(x){
54         splay(x);
55         node[x].ch[1]=last;
56         up(x);
57         last=x;
58         x=node[x].pa;
59     }
60     return last;//回傳access後splay tree的根
61 }
62 void access(int x,bool is=0){//is=0就是一般
63     的access
64     int last=0;
65     while(x){
66         splay(x);
67         if(is&&!node[x].pa){
68             //printf("%d\n",max(node[last].ma,node
69             [node[x].ch[1]].ma));
70         }
71         node[x].ch[1]=last;
72         up(x);
73         last=x;
74         x=node[x].pa;
75     }
76 }
77 void query_edge(int u,int v){
78     access(u);
79     access(v,1);
80 }
81 void make_root(int x){
82     access(x),splay(x);
83     node[x].rev^=1;
84 }
85 void make_root(int x){
86     node[access(x)].rev^=1;
87     splay(x);
88 }
89 void cut(int x,int y){
90     make_root(x);
91     access(y);
92     splay(y);
93     node[y].ch[0]=0;
94     node[x].pa=0;
95 }
96 void cut_parents(int x){
97     access(x);
98     splay(x);
99     node[node[x].ch[0]].pa=0;
100     node[x].ch[0]=0;
101 }
102 void link(int x,int y){
103     make_root(x);
104     node[x].pa=y;
105 }
106 int find_root(int x){
107     x=access(x);
108     while(node[x].ch[0])x=node[x].ch[0];
109     splay(x);
110     return x;
111 }
112 int query(int u,int v){
113     //傳回uv路徑splay tree的根結點
114     //這種寫法無法求LCA
115     make_root(u);
116     return access(v);
117 }
118 int query_lca(int u,int v){
119     //假設求鏈上點權的總和，sum是子樹的權重和，
120     data是節點的權重
121     access(u);
122     int lca=access(v);
123     splay(u);
124     if(u==lca){
125         //return node[lca].data+node[node[lca].
126         ch[1]].sum
127     }else{
128         //return node[lca].data+node[node[lca].
129         ch[1]].sum+node[u].sum
130     }
131 }
132 struct EDGE{
133     int a,b,w;
134 }e[10005];
135 int n;
136 vector<pair<int,int>> >G[10005];
137 //first表示子節點，second表示邊的編號
138 int pa[10005],edge_node[10005];
139 //pa是父母節點，暫存用的，edge_node是每個編
140 號存在哪個點裡面的陣列

```

```

130 void bfs(int root){
131     //在建構的時候把每個點都設成一個splay tree，
132     不會壞掉
133     queue<int> q;
134     for(int i=1;i<=n;++i)pa[i]=0;
135     q.push(root);
136     while(q.size()){
137         int u=q.front();
138         q.pop();
139         for(int i=0;i<(int)G[u].size();++i){
140             int v=G[u][i].first;
141             if(v!=pa[u]){
142                 pa[v]=u;
143                 node[v].pa=u;
144                 node[v].data=e[G[u][i].second].w;
145                 edge_node[G[u][i].second]=v;
146                 up(v);
147                 q.push(v);
148             }
149         }
150     }
151 void change(int x,int b){
152     splay(x);
153     //node[x].data=b;
154     up(x);
155 }

```

## 12.4 POJ\_tree.cpp

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define MAXN 10005
4 int n,k;
5 vector<pair<int,int>> >G[MAXN];
6 int size[MAXN];
7 bool vis[MAXN];
8 inline void init(){
9     for(int i=0;i<=n;++i){
10         g[i].clear();
11         vis[i]=0;
12     }
13 }
14 void get_dis(vector<int> &dis,int u,int pa,
15     int d){
16     dis.push_back(d);
17     for(size_t i=0;i<G[u].size();++i){
18         int v=G[u][i].first,w=G[u][i].second;
19         if(v!=pa&&!vis[v])get_dis(dis,v,u,d+w);
20     }
21 }
22 vector<int> dis;//這東西如果放在函數裡會TLE
23 int cal(int u,int d){
24     dis.clear();
25     get_dis(dis,u,-1,d);
26     sort(dis.begin(),dis.end());
27     int l=0,r=dis.size()-1,res=0;
28     while(l<r){
29         while(l<r&&dis[l]+dis[r]>k)--r;
30         res+=r-(l++);
31     }
32     return res;

```

```

32 }
33 pair<int,int> tree_centroid(int u,int pa,
34     const int sz){
35     size[u]=1;//找樹重心，second是重心
36     pair<int,int> res(INT_MAX,-1);
37     int ma=0;
38     for(size_t i=0;i<G[u].size();++i){
39         int v=G[u][i].first;
40         if(v==pa||vis[v])continue;
41         res=min(res,tree_centroid(v,u,sz));
42         size[u]+=size[v];
43         ma=max(ma,size[v]);
44     }
45     ma=max(ma,sz-size[u]);
46     return min(res,make_pair(ma,u));
47 }
48 int tree_DC(int u,int sz){
49     int center=tree_centroid(u,-1,sz).second;
50     int ans=cal(center,0);
51     vis[center]=1;
52     for(size_t i=0;i<G[center].size();++i){
53         int v=G[center][i].first,w=G[center][i].
54         second;
55         if(vis[v])continue;
56         ans-=cal(v,w);
57         ans+=tree_DC(v,size[v]);
58     }
59     return ans;
60 }
61 int main(){
62     while(scanf("%d",&n,&k),n||k){
63         init();
64         for(int i=1;i<=n;++i){
65             int u,v,w;
66             scanf("%d%d%d",&u,&v,&w);
67             g[u].push_back(make_pair(v,w));
68             g[v].push_back(make_pair(u,w));
69         }
70         printf("%d\n",tree_DC(1,n));
71     }
72     return 0;

```

## 13 zformula

### 13.1 formula.tex

#### 13.1.1 Pick 公式

給定頂點坐標均是整點的簡單多邊形，面積 = 內部格點數 + 邊上格點數/2-1

#### 13.1.2 圖論

1.  $V - E + F = 2$
2. 對於平面圖， $F = E - V + n + 1$ ， $n$  是連通分量
3. 對於平面圖， $E < 3V - 6$
4. 對於連通圖  $G$ ，最大獨立點集的大小設為  $I(G)$ ，最大匹配大小設為  $M(G)$ ，最小點覆蓋設為  $C_v(G)$ ，最小邊覆蓋設為  $C_e(G)$ 。對於任意連通圖：

$$\begin{aligned} \text{(a)} \quad & I(G) + Cv(G) = |V| \\ \text{(b)} \quad & M(G) + Ce(G) = |V| \end{aligned}$$

5. 對於連通二分圖：

$$\begin{aligned} \text{(a)} \quad & I(G) = Cv(G) \\ \text{(b)} \quad & M(G) = Ce(G) \end{aligned}$$

6. 最大權閉合圖：

$$\begin{aligned} \text{(a)} \quad & C(u, V) = \infty, (u, v) \in E \\ \text{(b)} \quad & C(S, v) = W_v, W_v > 0 \\ \text{(c)} \quad & C(v, T) = -W_v, W_v < 0 \end{aligned}$$

7. 最大密度子圖：

$$\begin{aligned} \text{(a)} \quad & C(u, v) = 1, (u, v) \in E \\ \text{(b)} \quad & C(S, v) = U_v, v \in V \\ \text{(c)} \quad & C(v, T) = U + 2g - d_v, v \in V \end{aligned}$$

8. 弦圖：

- (a) 完美消除序列從後往前依次給每個點染色，給每個點染上可以染的最小顏色
- (b) 最大團大小 = 色數
- (c) 最大獨立集：完美消除序列從前往後能選就選
- (d) 最小團覆蓋：最大獨立集的點和他延伸的邊構成
- (e) 區間圖是弦圖
- (f) 區間圖的完美消除序列：將區間按造又端點由小到大排序
- (g) 區間圖染色：用線段樹做

```
1 double l=0,=m,stop=1.0/n/n;
2 while(r-l>stop){
3     double(mid);
4     if((n*m-sol.maxFlow(s,t))/2>eps)l=mid;
5     else r=mid;
6 }
7 build(l);
8 sol.maxFlow(s,t);
9 vector<int> ans;
10 for(int i=1;i<=n;++i)
11     if(sol.vis[i])ans.push_back(i);
```

### 13.1.3 學長公式

- $\sum_{d|n} \phi(n) = n$
- $g(n) = \sum_{d|n} f(d) \Rightarrow f(n) = \sum_{d|n} \mu(d) \times g(n/d)$
- Harmonic series  $H_n = \ln(n) + \gamma + 1/(2n) - 1/(12n^2) + 1/(120n^4)$
- $\gamma = 0.57721566490153286060651209008240243104215$
- 格雷碼  $= n \oplus (n >> 1)$
- $SG(A+B) = SG(A) \oplus SG(B)$
- 選轉矩陣  $M(\theta) = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$

### 13.1.4 基本數論

- $\sum_{d|n} \mu(n) = [n == 1]$
- $g(m) = \sum_{d|m} f(d) \Leftrightarrow f(m) = \sum_{d|m} \mu(d) \times g(m/d)$
- $\sum_{i=1}^n \sum_{j=1}^m \text{互質數量} = \sum \mu(d) \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor$
- $\sum_{i=1}^n \sum_{j=1}^m lcm(i, j) = n \sum_{d|n} d \times \phi(d)$

### 13.1.5 排組公式

- k 卡特蘭  $\frac{C_n^{kn}}{n(k-1)+1} \cdot C_m^n = \frac{n!}{m!(n-m)!}$
- $H(n, m) \cong x_1 + x_2 \dots + x_n = k, num = C_k^{n+k-1}$
- Stirling number of  $2^{nd}$ ,  $n$  入分  $k$  組方法數目
  - (a)  $S(0, 0) = S(n, n) = 1$
  - (b)  $S(n, 0) = 0$
  - (c)  $S(n, k) = kS(n-1, k) + S(n-1, k-1)$
- Bell number,  $n$  入分任意多組方法數目
  - (a)  $B_0 = 1$
  - (b)  $B_n = \sum_{i=0}^n S(n, i)$
  - (c)  $B_{n+1} = \sum_{k=0}^n C_n^k B_k$
  - (d)  $B_{p+n} \equiv B_n + B_{n+1} \pmod{p}$ ,  $p$  is prime
  - (e)  $B_{p^m+n} \equiv mB_n + B_{n+1} \pmod{p}$ ,  $p$  is prime
  - (f) From  $B_0 : 1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, 115975$

- (a)  $B_0 = 1$
- (b)  $B_n = \sum_{i=0}^n S(n, i)$
- (c)  $B_{n+1} = \sum_{k=0}^n C_n^k B_k$
- (d)  $B_{p+n} \equiv B_n + B_{n+1} \pmod{p}$ ,  $p$  is prime
- (e)  $B_{p^m+n} \equiv mB_n + B_{n+1} \pmod{p}$ ,  $p$  is prime
- (f) From  $B_0 : 1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, 115975$

5. Derangement, 錯排, 沒有人在自己位置上

- (a)  $D_n = n!(1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} \dots + (-1)^n \frac{1}{n!})$
- (b)  $D_n = (n-1)(D_{n-1} + D_{n-2}), D_0 = 1, D_1 = 0$
- (c) From  $D_0 : 1, 0, 1, 2, 9, 44, 265, 1854, 14833, 133496$

6. Binomial Equality

- (a)  $\sum_k \binom{r}{m+k} \binom{s}{n-k} = \binom{r+s}{m+n}$
- (b)  $\sum_k \binom{r}{m+k} \binom{s}{n-k} = \binom{r+s}{l-m+n}$
- (c)  $\sum_k \binom{r}{m+k} \binom{s+k}{n} (-1)^k = (-1)^{l+m} \binom{s-m}{n-l}$
- (d)  $\sum_{k \leq l} \binom{l-k}{m} \binom{s}{k-n} (-1)^k = \frac{(-1)^{l+m} \binom{s-m-1}{l-n-m}}{(-1)^{l+m} \binom{s-m-1}{l-n-m}} =$
- (e)  $\sum_{0 \leq k \leq l} \binom{l-k}{m} \binom{q+k}{n} = \binom{l+q+1}{m+n+1}$
- (f)  $\binom{r}{k} = (-1)^k \binom{k-r-1}{k}$
- (g)  $\binom{r}{m} \binom{m}{k} = \binom{r}{m-k} \binom{r-k}{m-k}$
- (h)  $\sum_{k \leq n} \binom{r+k}{k} = \binom{r+n+1}{n}$
- (i)  $\sum_{0 \leq k \leq n} \binom{k}{m} = \binom{n+1}{m+1}$
- (j)  $\sum_{k \leq m} \binom{m+r}{k} x^k y^{m-k} = \sum_{k \leq m} \binom{-r}{k} (-x)^k (x+y)^{m-k}$

### 13.1.6 幕次, 幕次和

- $a^b \% P = a^{b \% \varphi(P) + \varphi(P)}, b \geq \varphi(P)$
- $1^3 + 2^3 + 3^3 + \dots + n^3 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4}$
- $1^4 + 2^4 + 3^4 + \dots + n^4 = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30}$
- $1^5 + 2^5 + 3^5 + \dots + n^5 = \frac{n^6}{6} + \frac{n^5}{2} + \frac{5n^4}{12} - \frac{n^2}{12}$
- $0^k + 1^k + 2^k + \dots + n^k = P(k), P(k) = \frac{(n+1)^{k+1} - \sum_{i=0}^{k-1} C_i^{k+1} P(i)}{k+1}, P(0) = n+1$
- $\sum_{k=0}^{m-1} k^n = \frac{1}{n+1} \sum_{k=0}^n C_k^{n+1} B_k m^{n+1-k}$
- $\sum_{j=0}^m C_j^{m+1} B_j = 0, B_0 = 1$
- 除了  $B_1 = -1/2$  剩下的奇數項都是 0
- $B_2 = 1/6, B_4 = -1/30, B_6 = 1/42, B_8 = -1/30, B_{10} = 5/66, B_{12} = -691/2730, B_{14} = 7/6, B_{16} = -3617/510, B_{18} = 43867/798, B_{20} = -174611/330,$

### 13.1.7 Burnside's lemma

- $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- $X^g = t^{c(g)}$
- $G$  表示有幾種轉法,  $X^g$  表示在那種轉法下, 有幾種是會保持對稱的,  $t$  是顏色數,  $c(g)$  是循環節不動的面數。
- 正立方體塗三顏色, 轉 0 有  $3^6$  個元素不變, 轉 90 有 6 種, 每種有  $3^3$  不變, 180 有  $3 \times 3^4$ , 120(角) 有  $8 \times 3^2$ , 180(邊) 有  $6 \times 3^3$ , 全部  $\frac{1}{24} (3^6 + 6 \times 3^3 + 3 \times 3^4 + 8 \times 3^2 + 6 \times 3^3) =$

### 13.1.8 Count on a tree

- Rooted tree:  $s_{n+1} = \frac{1}{n} \sum_{i=1}^n (i \times a_i \times \sum_{j=1}^{\lfloor n/i \rfloor} a_{n+1-i \times j})$
- Unrooted tree:
  - (a) Odd:  $a_n - \sum_{i=1}^{n/2} a_i a_{n-i}$
  - (b) Even:  $Odd + \frac{1}{2} a_{n/2} (a_{n/2} + 1)$
- Spanning Tree
  - (a) 完全圖  $n^n - 2$
  - (b) 一般圖 (Kirchhoff's theorem)  $M[i][i] = \text{degree}(V_i), M[i][j] = -1, \text{if have } E(i, j), 0 \text{ if no edge. delete any one row and col in } A, \text{ans} = \det(A)$

## 13.2 java.tex

### 13.2.1 文件操作

```
1 import java.io.*;
2 import java.util.*;
3 import java.math.*;
4 import java.text.*;
5
6 public class Main
7 {
8
9     public static void main(String args[])
10         throws FileNotFoundException,
11         IOException
12     {
13         Scanner sc = new Scanner(new FileReader(
14             "a.in"));
15         PrintWriter pw = new PrintWriter(new
16             FileWriter("a.out"));
17         int n,m;
18         n=sc.nextInt();//读入下一个INT
19         m=sc.nextInt();
20
21         for(ci=1; ci<=c; ++ci)
22         {
23             pw.println("Case #"+ci+": easy for
24                 output");
25         }
26     }
```

```
22 | pw.close();//关闭流并释放, 这个很重要,
23 | 否则是没有输出的
24 | }
25 | }
```

### 13.2.2 优先队列

```
1 PriorityQueue queue = new PriorityQueue( 1,
2     new Comparator()
3 {
4     public int compare( Point a, Point b )
5 {
6     if( a.x < b.x || a.x == b.x && a.y < b.y )
7         return -1;
8     else if( a.x == b.x && a.y == b.y )
9         return 0;
10    else
11        return 1;
12    }
13 });
```

### 13.2.3 Map

```
1 Map map = new HashMap();
2 map.put("sa", "dd");
3 String str = map.get("sa").toString();
4
5 for(Object obj : map.keySet()){
6     Object value = map.get(obj );
7 }
```

### 13.2.4 sort

```
1 static class cmp implements Comparator
2 {
3     public int compare(Object o1, Object o2)
4     {
5         BigInteger b1=(BigInteger)o1;
6         BigInteger b2=(BigInteger)o2;
7         return b1.compareTo(b2);
8     }
9 }
10 public static void main(String[] args)
11     throws IOException
12 {
13     Scanner cin = new Scanner(System.in);
14     int n;
15     n=cin.nextInt();
16     BigInteger[] seg = new BigInteger[n];
17     for (int i=0;i<n;i++)
18         seg[i]=cin.nextBigInteger();
19     Arrays.sort(seg, new cmp());
20 }
```

# ACM ICPC TEAM REFERENCE - NTHU JINKELA

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