1. Code explanation

TODO_2-1 Implement the affine matrix calculation

```
# Compute the relative rotation matrix
relative_rotation = rotation_matrix2[:2, :2] @ np.linalg.inv(rotation_matrix1[:2, :2])

# Combine the rotation and translation into the affine matrix
matrix = np.eye(3) # Extend to a 3x3 matrix for translation computation
matrix[:2, :2] = relative_rotation
matrix[:2, 2] = [translation_x, translation_y]
matrix = matrix[:2, :]

# Convert the matrix to a PyTorch tensor
matrix = torch.tensor(matrix, dtype=torch.float32)

# Return the 2x3 affine transformation matrix
return matrix
```

1. Coordinate Conversion:

The Carla coordinate system's dimensions are converted from meters to pixels to create a Bird's Eye View (BEV) map. This is achieved by dividing the BEV range (-32 to 32 meters) by the pixel resolution (0.25 meters per pixel).

2. BEV Center Calculation:

The center of the BEV map is determined in pixel coordinates using half the dimensions of the map.

3. Rotation Matrices Generation:

Two rotation matrices are generated using cv2.getRotationMatrix2D, one for the initial pose (theta1) and

another for the target pose (theta2). These matrices are centered around the BEV center and use a scaling factor of 1.0.

4. Translation Calculation:

The translations along the X and Y axes are calculated by subtracting the initial vehicle position (x1, y1) from the target position (x2, y2) and converting the result from meters to pixels using the pixel resolution.

5. Relative Rotation Matrix Calculation:

The relative rotation matrix is computed by multiplying the target rotation matrix (rotation_matrix2) with the inverse of the initial rotation matrix (rotation_matrix1). This captures the relative rotation required to align the two poses.

6. Affine Matrix Assembly:

A 3x3 identity matrix is initialized to include translation components. The top-left 2x2 submatrix is replaced with the relative rotation matrix, and the top-right column is set to the computed translations. The matrix is then reduced to a 2x3 affine transformation matrix for compatibility with affine transformation operations.

7. Conversion to Tensor:

The resulting 2x3 affine matrix is converted into a PyTorch tensor of type float32 for further use in deep learning frameworks.

8. **Output**:

The final 2x3 affine transformation matrix is returned, ready to be used for tasks like feature warping in the BEV representation.

This implementation efficiently combines rotation and translation into a single transformation matrix, enabling smooth mapping between poses.

TODO 2-2 Implement the warp features() function

This function applies affine transformations to input feature maps using affine matrices.

1. Validate Input Format:

- x is a tensor of shape (N, C, H, W), where N is the batch size, C is the number of channels, and H and W are the height and width.
- o affine_mats is a tensor of shape (N, 2, 3), where each matrix corresponds to one feature map in the batch.

2. Create an Affine Grid:

Use F.affine_grid to generate a grid of shape (N, H, W, 2) based on the affine matrices. This grid represents the transformed coordinates.

3. Sample Using the Grid:

Use F.grid_sample to sample the input feature map x based on the generated grid, applying the affine transformation through interpolation.

4. Return the Result:

The function returns the transformed feature maps with the same shape as the input (N, C, H, W).

TODO_1 Implement the future egomotion calculation

```
def mat2pose_vec(matrix):
    """
    Converts a transformation matrix into a pose vector.

Note: This is a placeholder implementation. The specific logic may depend on external libraries or requirements.
    """
    dx. dy, dz = matrix[:3, 3]  # Extract translation components
    roll, pitch, yaw = 0, 0, np.arctan2(matrix[1, 0], matrix[0, 0])  # Assume 2D planar motion
    return torch.tensor([dx, dy, dz, roll, pitch, yaw])

def get_future_egomotion(self, seq_x, seq_y, seq_theta):
    """
    Computes the future egomotion transformations for a sequence of ego vehicle poses.

Args:
    seq_x (list or array): Sequence of x-coordinates of the ego vehicle.
    seq_y (list or array): Sequence of y-coordinates of the ego vehicle.
    seq_theta (list or array): Sequence of orientations (angles) of the ego vehicle in degrees.

Returns:
    torch.Tensor: A tensor containing the future egomotion vectors for the sequence.
    """
    future_egomotions = []
    # Ensure input sequences have the same length
    if len(seq_x) != len(seq_y) or len(seq_x) != len(seq_theta):
        raise ValueError("Input sequences must have the same length")

# Convert angles from degrees to radians
    seq_theta = np.radians(seq_theta)
```

The code computes the **future egomotion transformations** for a sequence of ego vehicle poses. It converts positional and orientation data into motion vectors that represent how the vehicle moves between consecutive time steps.

1. Function: mat2pose vec(matrix)

This helper function takes a **4x4 transformation matrix** as input and converts it into a **pose vector**.

Input:

• A 4x4 matrix representing a spatial transformation. The matrix encodes translation and rotation information.

Process:

- Extract the translation components: dx, dy, dz (last column of the matrix).
- Compute the **yaw angle** from the rotation matrix elements (matrix[1, 0] and matrix[0, 0]) using arctan2.
 - Assumes 2D motion, so roll and pitch are set to 0.

Output:

• A tensor [dx, dy, dz, roll, pitch, yaw] representing the position and orientation in 3D space.

${\bf 2.\ Function:\ get_future_egomotion(seq_x,\ seq_y,\ seq_theta)}$

This function calculates a sequence of future egomotion vectors based on the input vehicle poses.

Input:

- seq_x: Sequence of the vehicle's x-coordinates.
- seq_y: Sequence of the vehicle's y-coordinates.
- seq_theta: Sequence of the vehicle's orientations in degrees.

Process:

1. Input Validation:

o Ensure seq_x, seq_y, and seq_theta have the same length.

2. Angle Conversion:

 Convert seq_theta (angles in degrees) to radians for trigonometric calculations.

3. Iterate Over Consecutive Poses:

For each pair of consecutive poses:

• Compute relative translation:

$$dx = x_2 - x_1, \quad dy = y_2 - y_1$$

• Compute relative rotation (change in angle):

$$d\theta = \theta_2 - \theta_1$$

• Construct the **transformation matrix** relative to the first pose:

This matrix encodes the translation (dx, dy) and the rotation $(\cos(\theta 1), \sin(\theta 1))$.

4. Convert Transformation Matrix to Motion Vector:

 Use mat2pose_vec to extract translation and yaw rotation from the matrix.

5. Store the Result:

 Append the resulting pose vector to the future_egomotions list.

6. Output:

 Convert the list of pose vectors into a PyTorch tensor and return it.

TODO 3 Complete the calculate birds eye view features() function

```
def calculate_birds_eye_view_features(self, x, intrinsics, extrinsics, affine_mats, depths):

"""

This function processes input image and camera's parameters to compute the bird's-eye view features.

Please follow the steps below to implement this function:

1. Encode the input features using the encoder_forward() function.

2. Project the encoded features to the bird's-eye view using the projection_to_birds_eye_view() function.

3. After get each frame's BEV feature, warp them to ego's current coordinate using the warp_features() function.

4. With self.temporal_coef, Apply the temporal fusion to the warped features.

b, s, n, c, h, w = x.shape

# Step 1: Reshape and pack sequence dimension

x = pack_sequence_dim(x)    # Shape: (b*s, n, c, h, w)
    intrinsics = pack_sequence_dim(intrinsics)    # Shape: (b*s, n, 3, 3)
    extrinsics = pack_sequence_dim(extrinsics)    # Shape: (b*s, n, 4, 4)
    affine_mats = pack_sequence_dim(affine_mats)    # Shape: (b*s, 2, 3)

# Step 2: Compute geometry using intrinsics and extrinsics

geometry = self.get_geometry(intrinsics, extrinsics)    # Shape: (b*s, n, depth_bins, h, w, 3)

# Step 3: Encode input features

encoded_features, depth_distributions, cam_front = self.encoder_forward(x)

# encoded_features: (b*s, n, c', h', w')

# depth_distributions: (b*s, n, depth_bins, h', w')

# cam_front: (b*s, c', h', w') or None

# Step 4: Project encoded features to bird's-eye view

bev_features = self.projection_to_birds_eye_view(encoded_features, geometry)  # Shape: (b*s, c', bev_h, bev_w)

# Step 5: Warp BEV features to ego's current coordinate

bev_features_warped = self.warp_features(bev_features, affine_mats)  # Shape: (b*s, c', bev_h, bev_w)

# Step 6: Apply temporal_fusion

fused_features = self.temporal_fusion(bev_features_warped, self.temporal_coef)  # Shape: (b, c', bev_h, bev_w)
```

```
# Step 7: Unpack sequence dimension
geometry = unpack_sequence_dim(geometry, b, s)
depth_distributions = unpack_sequence_dim(depth_distributions, b, s)
cam_front = unpack_sequence_dim(cam_front, b, s)[:, -1] if cam_front is not None else None
fused_features = fused_features.view(b, s, *fused_features.shape[1:])
return fused_features, depth_distributions, cam_front
```

This function, calculate_birds_eye_view_features, processes input images and camera parameters to compute bird's-eye view (BEV) features while incorporating temporal fusion for multiple frames. Below is a detailed explanation:

Function Overview

This function uses multiple inputs (image features, camera intrinsic and extrinsic parameters, affine transformation matrices, and depth distributions) to generate BEV features and applies temporal fusion to integrate information from multiple frames. The output includes multiframe BEV features, depth distributions, and optional frontal-view features.

Parameters

- x: Raw image features with shape (b, s, n, c, h, w), where b is the batch size, s is the sequence length, n is the number of cameras, c is the number of channels, and h and w are the height and width of the images.
- **intrinsics**: Camera intrinsics, shape (b, s, n, 3, 3).
- extrinsics: Camera extrinsics, shape (b, s, n, 4, 4).
- **affine_mats**: Affine transformation matrices, shape (b, s, 2, 3).
- **depths**: Depth information used for geometric projection.

Execution Steps

1. Flatten Sequence Dimension (pack sequence dim):

Flattens the sequence dimension from (b, s, ...) to (b*s, ...), simplifying subsequent operations.

2. Compute Geometry (self.get_geometry):

- Uses camera intrinsics and extrinsics to compute the 3D spatial points corresponding to each pixel.
- The output geometry has the shape (b*s, n, depth_bins, h, w, 3), representing 3D points for each pixel at various depth levels.

3. Encode Input Features (self.encoder_forward):

- Encodes raw input features into high-level features:
 - encoded_features: Encoded image features, shape (b*s, n, c', h', w').
 - depth_distributions: Depth distributions, shape (b*s, n, depth_bins, h', w').
 - cam_front: Optional frontal-view features.

4. Project to Bird's-Eye View (self.projection_to_birds_eye_view):

- Projects the encoded features to the BEV coordinate system.
- o Outputs bev_features with shape (b*s, c', bev_h, bev_w).

5. Warp BEV Features (self.warp_features):

- Aligns BEV features to the ego vehicle's coordinate system using affine transformation matrices.
- Outputs bev_features_warped with shape (b*s, c', bev_h, bev_w).

6. Temporal Fusion (self.temporal_fusion):

- Combines multi-frame BEV features using the temporal coefficient self.temporal coef.
- o Outputs fused features with shape (b, c', bev h, bev w).

7. Restore Sequence Dimension (unpack_sequence_dim):

• Restores the sequence dimension to (b, s, ...) for maintaining the multi-frame structure.

Outputs

1. fused_features:

Temporally fused BEV features with shape (b, s, c', bev_h, bev_w).

2. depth_distributions:

 Depth distributions for each frame, useful for depth-related processing.

3. cam_front:

 Frontal-view features from the last frame (if available), with shape (b, c', h', w').

TODO 4 Implement the basic control logic

```
def get_our_control(output):
    """
    Use the output of the model to control the vehicle.
    """
    # Initialize control parameters
    steer = 0.0  # Steering handled by autonomous driving logic
    throttle = 0.0
    brake = 0.0

# Extract segmentation information from the model output
    segmentation = output.get("segmentation")  # Assumes a segmentation map indicating the future path
    if segmentation is None:
        raise ValueError("Model output does not contain segmentation information.")

# Decision-making logic (determine path status based on segmentation information)
    if is_path_clear(segmentation):  # Assumes a function to check if the path is clear
    throttle = 0.5  # Accelerate
    brake = 0.0
    else:
        throttle = 0.0  # Apply brakes

# Return control parameters
    return carla.VehicleControl(steer=steer, throttle=throttle, brake=brake)

def is_path_clear(segmentation):
    """

Determine if the path in the segmentation map is clear.
    The logic here can be based on pixel statistics or other geometric information.
    """

# Assume 1 represents traversable areas and 0 represents obstacles
    clear_pixels = (segmentation.size
    return clear_pixels / total_pixels > 0.9  # Path is clear if 90% of the area is traversable
```

This code aims to control a vehicle based on the output of an autonomous driving model, such as a segmentation map.

1. get_our_control(output)

This function extracts the segmentation map from the model's output, determines whether it is safe to drive based on the map, and generates appropriate vehicle control commands.

Function Details:

1. Initialize Control Parameters:

- steer (steering angle): Initialized to 0, meaning the vehicle will drive straight.
- throttle (acceleration): Initialized to 0, meaning the vehicle will not accelerate.
- brake (braking): Initialized to 0, meaning the vehicle will not decelerate.

2. Extract Segmentation Map:

Retrieves the segmentation map information from output. It assumes that segmentation represents the future path's state.

If the segmentation map is not present, an error is raised.

3. Path Decision and Control:

Uses the function is_path_clear(segmentation) to check if the path is clear:

- o If the path is clear, the vehicle accelerates (throttle = 0.5) and braking remains inactive (brake = 0.0).
- o If the path is not clear, the vehicle stops accelerating (throttle = 0.0) and activates the brakes (brake = 1.0).

4. Output Control Command:

Returns a carla. VehicleControl object containing the steering, throttle, and brake commands.

2. is_path_clear(segmentation)

This helper function determines if the path is clear by analyzing pixel information in the segmentation map.

Function Details:

1. Segmentation Map Assumptions:

- o 1 represents drivable areas (e.g., roads).
- o 0 represents obstacles (e.g., walls or other vehicles).

2. Clearance Calculation:

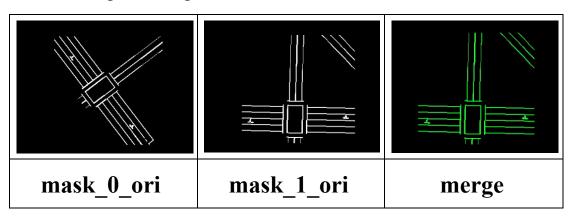
Counts the number of pixels in the segmentation map that correspond to drivable areas (clear_pixels) and compares them to the total number of pixels (total_pixels).

3. Decision Logic:

If the proportion of drivable area exceeds 90%, it returns True (path is clear); otherwise, it returns False.

2. Results and discussion

The following is the alignment result of the affine matrix:



The following are the evaluation results of the three scenarios:

Start Time	2024-12-01 20:35:05		
End Time	2024-12-01 20:35:08		
System Time	3.0s		
Game Time	0.55s		
Ratio (Game / System)	0.183	0.183	
Criterion	Result	Value	
RouteCompletionTest	FAILURE	0.0 %	
OutsideRouteLanesTest	SUCCESS	0 %	
CollisionTest	SUCCESS	0 times	
RunningRedLightTest	SUCCESS	0 times	
RunningStopTest	SUCCESS	0 times	
MinSpeedTest	SUCCESS	100 %	
InRouteTest	SUCCESS		
AgentBlockedTest	SUCCESS		
ScenarioTimeoutTest	SUCCESS	0 times	
Timeout	SUCCESS		

Start Time	2024-12-01 20:35:13		
End Time	2024-12-01 20:35:15		
System Time	2.0s		
Game Time	0.55s		
Ratio (Game / System)	0.275		
Criterion	Result	Value	
RouteCompletionTest	FAILURE	0 %	
OutsideRouteLanesTest	SUCCESS	0 %	
CollisionTest	SUCCESS	0 times	
RunningRedLightTest	SUCCESS	0 times	
RunningStopTest	SUCCESS	0 times	
MinSpeedTest	SUCCESS	100 %	
InRouteTest	SUCCESS		
AgentBlockedTest	SUCCESS		
ScenarioTimeoutTest	SUCCESS	0 times	
Timeout	SUCCESS		

Start Time	2024-12-01 20:35:19		
End Time	2024-12-01 20:35:22		
System Time	3.0s		
Game Time	0.55s		
Ratio (Game / System)	0.183		
Criterion	Result	Value	
RouteCompletionTest	FAILURE	0.0 %	
OutsideRouteLanesTest	SUCCESS	0 %	
CollisionTest	SUCCESS	0 times	
RunningRedLightTest	SUCCESS	0 times	
RunningStopTest	SUCCESS	0 times	
MinSpeedTest	SUCCESS	100 %	
InRouteTest	SUCCESS		
AgentBlockedTest	SUCCESS		
Timeout	SUCCESS		

Discuss:

Because my RouteCompletionTest failed, the following parts could not be executed smoothly.

I guess it may be the result of the problem of affine matrix, but I still can't figure it out after reading relevant information on the Internet.

But I tried my best.

3. Question Answering

Part A: Turning Surrounding Images into BEV Feature Representations

Self-driving cars use advanced perception techniques to convert surrounding images into **Bird's Eye View (BEV)** feature representations. This process generally involves the following steps:

- Camera Calibration and Extrinsics: Cameras are calibrated to understand their position and orientation in the world. The transformation matrices derived from this calibration align the camera perspective with the global coordinate system.
- 2. **Perspective Transformation**: Using homography or deep learning-based techniques, the captured front-facing, side, or rear-view images are warped into a top-down view. This accounts for road geometry and the positions of objects.
- 3. **Multi-Camera Fusion**: Vehicles often have multiple cameras to capture 360° views. These images are stitched together by aligning their features in the BEV space, using methods such as feature matching or overlapping areas.
- 4. **Semantic Segmentation**: Deep learning models (e.g., CNNs) segment images into various classes (e.g., vehicles, pedestrians, lanes). These segmented features are projected onto the BEV to provide spatial context.
- 5. **Sensor Fusion**: LiDAR or radar data is fused with the BEV features. LiDAR provides depth information, which complements the visual data from cameras to build a more accurate 3D representation in the BEV.
- 6. **Dynamic Object Tracking and Mapping**: Temporal data from multiple frames helps identify and track moving objects within the BEV representation, ensuring consistency over time.

Advantages of BEV Representations:

- 1. **Simplified Spatial Understanding**: BEV provides a top-down view that simplifies path planning, obstacle avoidance, and lane recognition.
- 2. **Comprehensive Awareness**: Stitching data from multiple cameras ensures 360° coverage, critical for safety in autonomous navigation.
- 3. **Compatibility with Sensor Fusion**: BEV representations integrate well with LiDAR and radar data, improving accuracy and robustness.

4. **Ease of Planning**: A top-down perspective aligns closely with how humans conceptualize maps, making navigation and decision-making more intuitive for algorithms.

Disadvantages of BEV Representations:

- 1. **Computational Cost**: The transformation and fusion processes are computationally intensive, impacting real-time performance.
- 2. **Information Loss**: Flattening 3D data into a 2D BEV format may lose critical vertical information (e.g., overhanging obstacles).
- 3. **Complex Calibration**: Accurate BEV requires precise calibration of cameras and sensors, which can be difficult to maintain.
- 4. **Edge Case Failures**: Transformations may struggle in complex scenarios, such as heavy occlusions, steep slopes, or unusual object shapes.

Part B: Enhancing Explainability in End-to-End Models

End-to-end models map raw sensor data directly to vehicle controls, bypassing traditional modular architectures. While efficient, their "black-box" nature raises challenges in explainability.

Strategies to Enhance Explainability:

- 1. **Intermediate Representations**: Introduce interpretable layers that generate outputs like lane detection, object positions, or semantic maps before control commands are produced. These serve as a bridge between raw input and decisions.
- 2. **Attention Mechanisms**: Use attention layers to visualize which parts of the input the model focuses on during decision-making. This helps identify relevant features influencing predictions.
- 3. **Saliency Maps**: Generate saliency maps to highlight areas in the input (e.g., an image or LiDAR point cloud) that most affect the model's outputs.
- 4. Rule-Based Post-Hoc Analysis: Develop rule-based systems to interpret why the model made a certain decision. For example, tracing the path taken and correlating it with detected objects or lane markings.
- 5. **Explainability-Aware Training**: Use methods like contrastive explanations or adversarial training to make the model inherently more transparent.

- 6. **Human-in-the-Loop Systems**: Integrate human feedback during training to validate and refine model decisions, ensuring outputs align with human reasoning.
- 7. **Graph-Based Visualizations**: Represent the model's decision process as a flowchart or graph, showing the relationships between inputs, intermediate states, and outputs.

Advantages of Enhanced Explainability:

- 1. **Increased Trust**: If humans understand *why* a vehicle makes specific decisions, they are more likely to trust it.
- 2. **Improved Debugging**: Explainability helps engineers identify and correct flaws in the system.
- 3. **Regulatory Compliance**: Autonomous vehicles may need to explain their actions to meet legal or ethical standards.
- 4. **Safer Interactions**: Explainability allows vehicles to communicate their intentions to pedestrians and other drivers.

Challenges in Achieving Explainability:

- 1. **Trade-Off with Performance**: Introducing interpretable components may reduce the efficiency or accuracy of the model.
- 2. **Complexity of Sensor Fusion**: Explaining decisions involving multimodal data (e.g., combining LiDAR and images) is inherently challenging.
- 3. **Edge Case Interpretations**: Uncommon scenarios may lead to decisions that are hard to explain, even for interpretable models.

By incorporating explainability, autonomous vehicle systems can address user concerns, align with ethical considerations, and pave the way for broader acceptance and trust.