

3. (6 marks) You are given a hash table with 11 slots, initialized to be empty. The hash functions used for this hash table are:  $h_1(x) = x \bmod 11$ ,  $h_2(x) = 1 + (x \bmod 10)$ . The collision resolution strategy is the following: for the  $i$ -th probe for the key  $k$  the formula followed is:  $p(i, k) = (h_1(k) + c_1 \cdot i + c_2 \cdot i^2 + h_2(k) \cdot i) \bmod 11$ . Here  $c_1 = 1$  and  $c_2 = 3$ . Show the insertion of the following keys in to the hashtable: [21, 32, 43, 25, 36]

$$(h_1(k) + i + 3i^2 + ih_2(k)) \bmod 11$$

0	
1	
2	
3	25
4	
5	
6	32
7	43
8	
9	36
10	21

initial hash table is empty.

a 11-slot HT has 0-10 keys.

# first value  $\Rightarrow$  21.

$$\text{hashkey} = h_1(21) = 21 \bmod 11 = 10$$

0th probe  $\therefore i=0$

insert 21 in HT with key 10 (as shown)

# 2nd value = 32. probe = 0

$$\text{hash key} = h_1(32) = 32 \bmod 11 = 10$$

but 10 is already filled i.e collision

Thus probe is increased by 1. ( $i=1$ )

$$\begin{aligned} \text{new hash key} &= [32 \bmod 11 + 1 + 3 + (1 + 32 \bmod 10)] \bmod 11 \\ &= [10 + 4 + 3] \bmod 11 = 6. \end{aligned}$$

insert 32 at key 6 as shown

1st next value = 43.

hash key for probe 0 ( $i=0$ )  $\Rightarrow 43 \bmod 11 = 10$

but 10 is filled so  $i=1$ ; new hash key =

$$[43 \bmod 11 + 1 + 3 + (1 + 43 \bmod 10)] \bmod 11$$

$$[10 + 4 + 1 + 3] \bmod 11 = 7 = \text{new hash key}$$

insert 43 at key = 7

next value = 25

hash key for  $i=0$  (initial)  $\Rightarrow 25 \bmod 11 = 3$

$\therefore$  insert 25 at key 3 in the HT.

③ next value = 36

hash key for  $i=0$  (initial)  $\Rightarrow 36 \bmod 11 = 3$  but 3 is filled.

so increase  $i$ ,  $i=1$ .

$$\text{new hash key} \Rightarrow [36 \bmod 11 + 1 + 3 + (1 + 36 \bmod 10)] \bmod 11$$
$$[3 + 5 + 6] \bmod 11 = 3 \Rightarrow \text{again collision}$$

change  $i$ ,  $i=2$

$$\text{new hash key} \Rightarrow [36 \bmod 11 + 2 + 3(2)^2 + 2(1 + 36 \bmod 10)] \bmod 11$$
$$[3 + 14 + 14] \bmod 11 = 31 \bmod 11 = 9$$

thus insert 36 at key = 9. the final HT is on the previous page

25  $\Rightarrow$  key 3    32  $\Rightarrow$  key 6    43  $\Rightarrow$  key 7  
36  $\Rightarrow$  key 9    21  $\Rightarrow$  key 10

Problem 3: [24 marks]