

Problem 3: [24 marks]

1. [8 marks] For the given pair of functions, mark all the correct statements regarding their asymptotic behaviour.

(a) $f_1(n) = n^2 \log(n)$; $g_1(n) = n^2 \log(n^2 + n + c)$

(b) $f_2(n) = (n)^{\sqrt{n}}$; $g_2(n) = (\sqrt{n})^n$

(c) $f_3(n) = e^n$; $g_3(n) = n^n$

(d) $f_4(n) = 2^n$; $g_4(n) = \text{factorial}(n)$

Statement	$f_1(n), g_1(n)$	$f_2(n), g_2(n)$	$f_3(n), g_3(n)$	$f_4(n), g_4(n)$
$f(n) = \text{big-O}(g(n))$	✓	✓	✓	✓
$g(n) = \text{big-O}(f(n))$	✓			
$f(n) = \Theta(g(n))$	✓			
$f(n) = \text{small-o}(g(n))$	✗	✓	✓	✓
$f(n) = \text{big-}\Omega(g(n))$	✓			
$g(n) = \text{small-}\omega(f(n))$		✓	✓	✓