# COL106 Minor 2

# ARPIT SAXENA

**TOTAL POINTS** 

# 42 / 70

**QUESTION 1** 

# **Q1** 11 pts

# 1.1 Q1-a 8 / 8

- √ + 1 pts Correct Insertion/Probes for 873/837: 3
- √ + 1 pts Correct Insertion/Probes for 9734/8843: 3, 1
- √ + 1 pts Correct Insertion/Probes for 280/640: 0
- √ + 1 pts Correct Probes for deleting 9734/8843: 3, 1
- √ + 2 pts Probes for searching 143/323 : 3, 1, 4
- √ + 2 pts Correct Insertions/Probes for inserting 14/32: 0. 3. 1
  - 1.5 pts Did not listed probes
  - + 0 pts Incorrect/Unattempted

# 1.2 Q1-b 1.5 / 3

# √ + 1.5 pts Null slot found then stop search

- + 1.5 pts Probed the slots in correct order untill repeated slot is found (when table is full and element not present) or element found
  - + 0 pts Incorrect/unattempted

# **QUESTION 2**

# 225/5

- √ + 2 pts Main final structure
  - 0.5 pts Not Setting parents field of p and g
- √ + 2 pts Correctly attaching old children of n
- **0.5 pts** Not setting parent field of "Old Children of
- √ + 1 pts Correctly setting new parent of n
  - + 0 pts Incorrect Solution

## QUESTION 3

# **3** 10 pts

# 3.1 Q3-Delete 0 / 6

√ + 0 pts Incorrect/Unattempted

- + 1 pts Correctly handles no children case
- + 1 pts Correctly handles the case when the key values matched, left subtree is NULL and right subtree is not NULL
- + 2 pts Correctly handles the case when the key values matched, left subtree is not NULL and right subtree is NULL; also include recursing again on left subtree
- + 2 pts Correctly handles 2 children case: Includes finding the inorder successor/predecessor and deleting that predecessor/successor and recursed again on root->left
- + 1 pts Incorrect handling of 2 children case
- + 1 pts Only deleted the first key found
- 0.5 pts Not mentioned about how to delete the successor or predecessor or incorrect successor deletion
  - 1 pts Didn't recurse on root->left after deleting
- + 2 pts Incomplete/Partial Correct/ Specific Case only

# 3.2 Q3-Search 4 / 4

- + O pts Incorrect/Unattempted
- √ + 1 pts Correct base case i.e. termination condition
- √ + 0.5 pts Implemented only the Binary Search
- √ + 1 pts Correctly search duplicates keys
- √ + 1 pts return the duplicates keys
- √ + 0.5 pts pseudo code attempt
  - + 0 pts Wrong search
  - storing is not allowed.

#### QUESTION 4

#### 4 Q4 2 / 5

- √ + 2 pts Used global lock/ synchronized
- Mentioned about locking the root

- + 1 pts Incorrect usage of per node lock leading to inconsistent results.
- Incomplete answer regarding lock/ synchronized. But in the right direction.
- + **0 pts** No explanation of how to implement synchronization or entirely incorrect. Not mentioning anything about how to synchronize.

Not answered.

+ 3 pts Justification - the deadlock issue if the root is not locked

#### QUESTION 5

# 5 Q5 3 / 5

- + **0** pts Incorrect/Unattempted
- + 1 pts lock whole list without proper explanation
- + 1.5 pts lock whole list with proper explanation

# √ + 1 pts Correct and precise synchronization for search with incorrect explanation

- + 2 pts Correct and precise synchronization for search with correct explanation
- √ + 1 pts Correct and precise synchronization for insert with incorrect explanation
- + **1.5 pts** Correct and precise synchronization for insert with correct explanation
- √ + 1 pts Correct and precise synchronization for delete with incorrect explanation
- + **1.5 pts** Correct and precise synchronization for delete with correct explanation

# **QUESTION 6**

# 6 Q6 7 / 10

- + 0 pts Incorrect or Unattempted
- **0.5 pts** Didn't observe that all leaves have the same height
- $\checkmark$  + 1.5 pts Part A: Observed that minimum height will happen when each node is 4-node.
- ✓ + 2 pts Part A: Derived Correct expression for maximum number of keys for a given height
   ✓ + 0.5 pts Part A: Derived Correct expression for minimum height given number of keys n
   ✓ + 1.5 pts Part B: Observed that maximum height will happen when each node is 2-node.

# $\sqrt{+1.5}$ pts Part B: Derived correct expression for maximum height given number of keys n

- + 1.5 pts Part C: Observed that to find a key, number of nodes examined is at most the maximum height
- + **1.5 pts** Part C: Observed that maximum number of comparisons per node are 2 (for 3-nodes and 4-nodes).
- 1 pts PartC: not mentioned why 2 comparison in part c
- + **0 pts** Didn't notice that n denotes number of keys, not number of nodes
  - 1 pts PartC: maximum height not mentioned

#### **QUESTION 7**

# 7Q76/6

# √ + 6 pts Correct

- + 2 pts If algorithm partially or fully correct but not O(h)
- + 3 pts If algorithm not written but worked out by example
- + 0 pts If algorithm not written or incorrect
- + 1 pts Partial marks (Brute-force or almost brute force kind of approach or just writing select root as the one of the roots and attach remaining as subtree). A recursive approach on nodes is brute-force.
  - + **0 pts** Click here to replace this description.

#### QUESTION 8

# 8 Q8 0.5 / 6

- + 3 pts correct explanation
- + 3 pts correct answer
- + 0 pts Incorrect or blank
- √ + 0.5 pts explanion provided but not appropriate

#### **QUESTION 9**

# 9Q90/6

# √ + 0 pts Incorrect/Didn't attempt

- + 1 pts Recognition that Preorder traversal breaks into Root followed by left subtree and right subtree
- + 2 pts Recognition that elements in the left subtree are smaller than the root and, scanning to get there

- + 2 pts Proper book keeping in the pseudocode
- + 1 pts Proper justification

# QUESTION 10

# 10 Q10 5 / 6

- √ + 4 pts Correct non recursive algorithm
- √ + 1 pts Time complexity O(n) provided algorithm is

# correct

- + 1 pts Argument for correctness
- + 1 pts Correct recursive solution
- + 0 pts Incorrect/ Unattempted
- + **0 pts** Does not find depth of binary tree, stops

after finding depth of first leaf

# COL 106 MINOR EXAM II

# SEMESTER I 2019-2020 1 hour

Please do not allow any bag, phone or other electronic device near you. Keep your ID card next to you on the desk. Maximum marks available for questions are listed in []. Write answers in the provided space. Justify all answers.

1. (11)

a) [8] Given the Hash function h below, list the table slots touched/probed and show the status of the Hash table after each listed operation (in order from left to right, starting with an empty hash table). The table has 5 slots. Assume open addressing with  $h_i$  as given: (Deletion is by marking as deleted.)

$$h = h_0 = (\sum \text{digits}) \% 5$$
  
 $h_i = (h_0 + 3*i) \% 5$ 

Insert:837	Insert:8843	Insert:640	Delete:8843 Search 323	Insert:32
		640	640	640
	8843	8843	8845 (seleted)	32
837	837	837	837	837

Rough space 18%5 = 3 23%5 = 3 (3+3)%5 10%5 = 0 10%5 = 3 10%5 = 3 10%5 = 3

Slots probed:

3 | 3,1 | 0 | 3,1 | 3,1,4 | 0,3,1 |

b) [3] How do you conclude that a searched key does or does not exist in such a Hash table? We forst compute the bash h and check to inclock to the table.

If the securched key is there, we're done. Else, If the I & slot how been marked the deleted or there is some other ke in it, we calculate he and check from Else, we have concluded that the key does not exist.

For in in

2. [5] Write code (precise syntax not required) to tri-node restructure the following configuration. Assume references left, right, parent and value are stored for each node. Assume p.parent.left == p and n.parent.right == n. (No references should be assumed to be null.) Restructure(Node n):

Node p = n.parent, g = p.parent;

I parent = g. parent;
I g. parent != null;
g. parent. left == nett? g. parent-left = p: g. parent. right = p n

p n

else: // g-powert== ruel => g & noot.

noot = n | p. left; n. left | povert = p; g. left = n. right; n. right | povert = g n. left = p; p. bovert = n

n-right= 9; g. parent = n

3. (10) Consider a binary search tree that allows keys to be repeated in multiple nodes such that keys equal to any node's key are always in that node's left subtree. Write the pseudo-code for search and delete for this tree that each take time O(h) for a tree with height h. The search function must return all instances and the delete function must delete all

instances of the given key.

[6] Delete(root, key):

[4] Search (root, key): Lest = [7 cevor = noot white curr != null :

if curr != key list-append (cure value) if key <= cwor.key: else:

cevor= cevor-right return list

4. [5] Consider a Red-Black tree that supports multiple threads inserting, searching or deleting in parallel. (Asume each thread uses the standard algorithms to perform these operations.) What synchronization is required to ensure that the threads do not interfere with each other's operation?

The answer is written by considering the equivalency of z-4 but and red black but. we have locks for each node. In searthang, lock the noot on, then determine which path to bake. Then go to the corresponding thild, lack it and then release for the orgent, we acquire lock as Elbove. The lock is only released cotten after we know it's while along whose fath we have to usert a not a 4-nocle. We acquire chib's parent's lock, and receir. lock and recur. For delete, lock is released of we know corr- 2-4 node of parent is not a 2-node

5. [5] You need to implement a skip-list that supports multiple threads inserting, searching or deleting in parallel. (You may assume that each thread uses the standard algorithms to perform these operations.) What synchronization is required to ensure that the threads do not interfere with each other's operation?

we need to only ensure the nodes in the avorent interval we're looking at care are locked. Nodes outside of this interval can be accessed by other threads too. Consider tower of pades in averages, we can lock the beginning array and end array of the interval. So, another thread whats wants to access towers in between them would be susperded, as only way to nade next to the beginning array is through that array.

ease write your entry number and name on each sheet.

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6. [4+3+3] Show that the height of a 2-4 tree with n keys is (a) no less than floor(0.5  $\log_2 n$ ) and (b) no more than  $\log_2 n$ . (c) Also show that the number of comparisons required to find a key is no more than  $2 \log_2 n$ . (5 extra marks to show the bound to be 1.3  $\log_2 n$ )

(a) Minimum height of a 24 bee will be obviously, when there all hodes

depth i has 4 nodes = 3 x 4 keys

Total keys for such a bree of height 
$$h = 3(1+4+-1) = 4^{h+1} = 3(4^{h+1}-1) = 4^{h+1}$$

Any 2-1 10

(6) For more height, each node is a 2 node  $\Rightarrow$  total leass for height h base =  $1+2+-+2^h=2^{h+1}-1$ 

$$n \ge 2^{h+1} - 1$$
  
 $\Rightarrow h \le \log_2(n+1) - 1 \le \log_2(n)$   
 $\Rightarrow h \le \log_2(n)$ 

(c)

7. [6] Provide an O(h) algorithm to merge two heaps with  $2^h$  keys each. (Assume that keys in the two heaps are comparable to each other and h is an integer.)

defore murge (a, b) hew heap) that a cocles

Suppose we have a given place in heap to add a new node to, and towo nodes a and by them say a how greater preority than 6. Then a goes to now the given place in heap. Let a's two children be a and a. In the heap, we make b (along with it's subfree) the left dutid of a. Now, we set a and 6 as a and an and recurrent which a and 6 both one null.

To the above method, we supply noots of the both the heaps initically. We note that by the given condition, the the binary tries of both heaps are complete (ext assuming 2"-1 keys each)

Note that is O (h) as in each step of recursion, we descend one level and do constant time operations in each step.

8. [6] In an AVL tree with with 20 nodes having numbers 1 to 20, respectively, as keys, which numbers may not appear in the root?

We know that for an AVL true with height b,

min-nocles, nois = Fh+1, where Fo=0, Fi=1,

Suppose noot has height h. Then it's children have height his and hillhow resp.

min haz

h=5, then hight \$ child has 3, 12 nodes 3, 7 nodes

h=4, then height 3 child has 7 7 nades

ease write your entry number and name on each sheet.

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9. [6] Given the keys of a Red-black tree ordered according to the pre-order traversal order, provide an algorithm to re-construct the Red-black tree. (You do not need to re-construct the nodes' original colors.)

Assuming we have at our disposal a ribbrees amplementation which has an insert implemented.

Let # face = new th free () for key in bre-order-traversal: bue . (nært (key)

10. [6] Provide non-recursive pseudo-code to compute the depth of a binary tree.

y (root == null) return queue insert (noot)

debth = @ 4 8-1 civor-nacles = 1 while queue is not empty:

new-nodes = 0; deptot;

for i = 1- curr-nodes;

hode = queue. pop()

& node != rutt:

if node left != null:

queue insert (node left)

new-norder+s

if node-right!= null:

queue insert (node night)

aur-nodes = new-nodes

return depth

