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Name:		
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Entry number:

There are 6 questions for a total of 15 points.

1. (1 point) Fill the truth-table below:

P	Q	R	$P \leftrightarrow Q$	$\neg Q \lor R$	$(P \leftrightarrow Q) \to (\neg Q \lor R)$
Т	Т	Т			
Т	Т	F			
Т	F	Т			
F	Т	Т			
Т	F	F			
F	Т	F			
F	F	Т			
F	F	F			

- 2. Let the domain of discourse consist of all real numbers and let P(x,y) mean  $yx^2 = y^3$ .
  - (a) (½ point) State whether the following quantified statement is true or false:

$$(\exists x \forall y P(x,y)) \lor (\exists y \forall x P(x,y))$$

(a) \_\_\_\_\_

(b) (1 point) Give reasons for your answer to part (a).

3.  $(2 \frac{1}{2} \text{ points})$  Let Q(p, s, z) be the statement "the price of product p in store s is z rupees", where the domain of variable p consists of all products, s consists of all stores, and z consists of all valid product prices. You may assume for this question that all stores carry all products. Use quantifiers to express the following statement: "Store A is the cheapest store for all products".

4. Let A, B, C be non-empty sets, and let  $g: A \to B$  and  $h: A \to C$  and let  $f: A \to B \times C$  defined as:

$$f(x) = (g(x), h(x)).$$

Answer the following:

(a) ( $\frac{1}{2}$  point) State true or false: If f is onto, then both g and h are onto.

(a) \_\_\_\_\_

(b)  $(\frac{1}{2} \text{ point})$  State true or false: If g and h are onto, then f is onto.

(b) \_\_\_\_\_

(c)  $(\frac{1}{2} \text{ point})$  State true or false: If at least one of g, h is one-to-one, then f is one-to-one.

(c) \_\_\_\_\_

(d) ( $\frac{1}{2}$  point) State true or false: If g and h are not one-to-one, then f is not one-to-one.

(d) \_\_\_\_\_

(e) (2 points) Give reasons for your answer to part (b).

(f) (2 points) Give reasons for your answer to part (d).

- 5. Answer the following:
  - (a)  $(\frac{1}{2} \text{ point})$  State true or false: Let  $f(n) = 5n2^n + 3^n$  and  $g(n) = n3^n$ . Then f(n) = O(g(n)).

(a) \_\_\_\_\_

(b)  $(\frac{1}{2} \text{ point})$  State true or false: Let  $f(n) = 5n2^n + 3^n$  and  $g(n) = n3^n$ . Then g(n) = O(f(n)).

(b) \_\_\_\_\_

6. (3 points) Prove or disprove: The function  $f: \mathbb{N} \to \mathbb{N}$  defined as:

$$f(n) = \begin{cases} n-1 & \text{if } n \text{ is odd} \\ n+1 & \text{if } n \text{ is even} \end{cases}$$

is one-to-one and onto. (Note that 0 is an even number)

202: Discrete Mathema	tical Structures (Semester-II-2017-18)	Minor
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space for rough work	<u> </u>	