COL202: Discrete Mathematical Sturctures. I semester, 2017-18. Quiz 3 $10~{\rm August}~2017$

Maximum Marks: 4

Name		Ent. No.
Important: Koop your answer within the how	Anythir	or written outside the box will be treated as

Important: Keep your answer within the box. Anything written outside the box will be treated as rough work. Do your rough work on the free space on the flip side of this sheet.

Given two sorted (in ascending order) integer lists A and B, the merge operation creates a third list C that contains all the elements of A and B in sorted order. Let us tweak this and define a new operation check-and-merge as follows: if the largest element of A is smaller than the smallest element of B simply concatenate B behind A. If not check again with the positions of A and B reversed. If both conditions don't hold then perform normal merging. We assume that the checking and concatenating (if possible) take 1 unit of time, while normal merging takes time equal to the size of A plus the size of B.

Now, with this new operation, we define a new algorithm *check-and-merge sort* which is the same as the usual merge sort except that it uses *check-and-merge* as a subroutine where merge sort uses the normal merge. Recall that merge sort works as follows: Divide the list into two equal parts, recursively merge sort both parts, then merge the two recursively sorted lists. As the base case: a list with a single element is considered sorted.

Q1. (2 marks) If T(n) is the time to sort an already sorted list using check-and-merge sort, find a recurrence for T(n). An answer with no argument gets 0 marks.

Continued overleaf