

Math553-hw4

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1 Assignment 4

1.1 Problem 1

Since G is a forest with 7 trees, we know that it doesn't have cycle inside. So, $C(G) = 0$.

Also, we have already know that $\dim(\text{cut space}) + \dim(\text{cycle space}) = |E|$ and $\dim(\text{cycle space}) = 0$. So what we get is $\dim(\text{cut space}) = |E(G)|$.

$$\begin{aligned} |E(G)| &= |E(T_1)| + |E(T_2)| + |E(T_3)| + \cdots + |E(T_7)| \\ &= V(T_1) - 1 + V(T_2) - 1 + V(T_3) - 1 + \cdots + V(T_7) - 1 \\ &= V(G) - 7 \\ &= 2 \end{aligned}$$