

Washington State University
School of Electrical Engineering and Computer Science
Fall 2019

CptS 440/540 Artificial Intelligence

Homework 8

Due: October 24, 2019 (11:59pm)

General Instructions: Put your answers to the following problems into a PDF document and submit as an attachment under Content → Homework 8 for the course CptS 440 Pullman (all sections of CptS 440 and 540 are merged under the CptS 440 Pullman section) on the Blackboard Learn system by the above deadline. Note that you may submit multiple times, but we will only grade the most recent entry submitted before the above deadline.

1. Suppose your agent is playing a 4x4 Wumpus world game and has visited locations (1,1), (1,2), (1,3), (2,3) and (3,3). The agent observes a breeze in (3,3), but no breeze in the other visited locations. Given this information, we want to compute the probability of a pit in (3,4). You may use $p_{x,y}$ and $\neg p_{x,y}$ as shorthand notation for $\text{Pit}_{x,y}=\text{true}$ and $\text{Pit}_{x,y}=\text{false}$, respectively. Similarly, you may use $b_{x,y}$ and $\neg b_{x,y}$ as shorthand notation for $\text{Breeze}_{x,y}=\text{true}$ and $\text{Breeze}_{x,y}=\text{false}$, respectively. Specifically:
 - a. Define the sets: *breeze*, *known*, *frontier* and *other*.
 - b. Following the method in the textbook and lecture, compute the probability *distribution* $P(\text{Pit}_{3,4} \mid \text{breeze}, \text{known})$. Show your work.
2. Recall the Halloween World from Homework 7. The full joint probability distribution for Halloween World is reproduced below. We are also given that Weather and Costume are independent of each other, and that Party depends on both Weather and Costume. Show a Bayesian network consistent with this information. Be sure to show all nodes, links and conditional probability tables (CPTs).

	<i>Weather:</i>	clear		cloudy		rain	
	<i>Costume:</i>	yes	no	yes	no	yes	no
<i>Party:</i>	yes	0.084	0.032	0.18	0.06	0.09	0.024
	no	0.036	0.048	0.12	0.14	0.09	0.096

3. Using the Bayesian network in Figure 1 below, compute the following probabilities. Show your work.
 - a. $P(\text{AIDone} = \text{true}, \text{Costume} = \text{false}, \text{Party} = \text{true}, \text{HaveFun} = \text{true}, \text{MakeFriends} = \text{true})$
 - b. $P(\text{HaveFun} = \text{true} \mid \text{AIDone} = \text{false}, \text{Costume} = \text{true})$
 - c. $P(\text{AIDone} = \text{true} \mid \text{HaveFun} = \text{true}, \text{MakeFriends} = \text{true})$

4. Given the following ten samples collected using Direct Sampling from the Bayesian network in Figure 1, estimate the $P(\text{AIDone} = \text{true} \mid \text{HaveFun} = \text{true}, \text{MakeFriends} = \text{true})$.

< AIDone = true, Costume = true, Party = true, HaveFun = true, MakeFriends = true >
< AIDone = true, Costume = true, Party = false, HaveFun = true, MakeFriends = true >
< AIDone = true, Costume = true, Party = true, HaveFun = true, MakeFriends = true >
< AIDone = false, Costume = true, Party = true, HaveFun = true, MakeFriends = true >
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< AIDone = true, Costume = true, Party = true, HaveFun = true, MakeFriends = true >
< AIDone = false, Costume = true, Party = false, HaveFun = true, MakeFriends = true >

5. Given the following ten samples collected using Markov Chain Sampling from the Bayesian network in Figure 1, estimate the $P(\text{AIDone} = \text{true} \mid \text{HaveFun} = \text{true}, \text{MakeFriends} = \text{true})$.

< AIDone = true, Costume = true, Party = true, HaveFun = true, MakeFriends = true >
< AIDone = true, Costume = true, Party = false, HaveFun = true, MakeFriends = true >
< AIDone = true, Costume = false, Party = false, HaveFun = true, MakeFriends = true >
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< AIDone = false, Costume = false, Party = false, HaveFun = true, MakeFriends = true >

6. Using direct sampling on the Bayesian network in Figure 1, what is the *most* likely sample?
7. *CptS 540 Students Only*: Using direct sampling on the Bayesian network in Figure 1, what is the *least* likely sample?

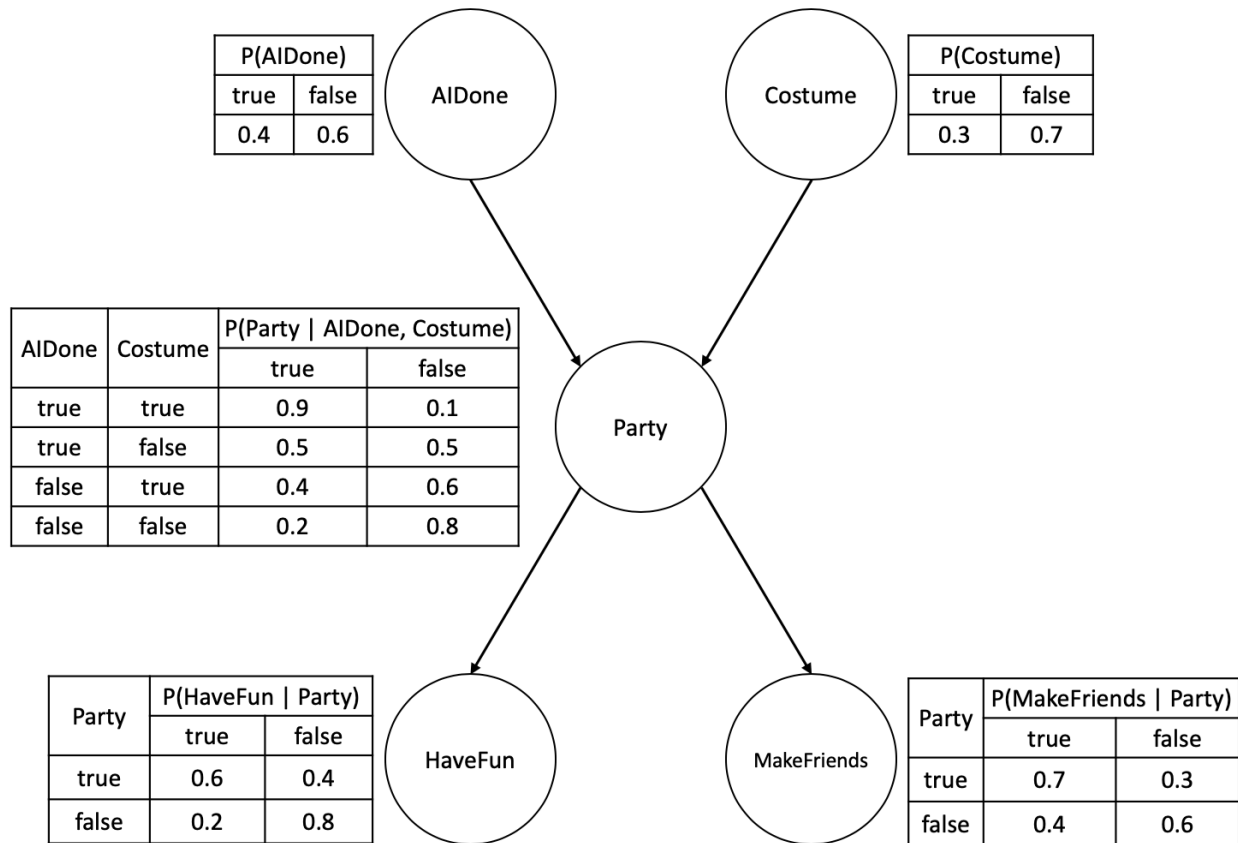


Figure 1. Bayesian Network.