Self-Paced Robust Learning for Leveraging Clean Labels in Noisy Data

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A Related Work

The work related to this paper is summarized in three categories below.

A.1 Self-Paced Learning

In recent years, self-paced learning (Kumar *et al.* 2010) has received widespread attention for various applications in machine learning, such as image classification (Jiang *et al.* 2015), event detection (Jiang *et al.* 2014a) and object tracking (Supancic and Ramanan 2013; Zhang *et al.* 2016). Inspired by the learning processes used by humans and animals (Bengio *et al.* 2009), self-paced learning (*SPL*) (Kumar *et al.* 2010) considers training data in a meaningful order, from easy to hard, to facilitate the learning process. Unlike standard curriculum learning (Bengio *et al.* 2009), which learns the data in a predefined curriculum design based on prior knowledge, *SPL* learns the training data in an order that is dynamically determined by feedback from the learning process itself, which means it can be more extensively utilized in practice. Furthermore, a wide assortment of *SPL*-based methods (Pi *et al.* 2016; Ma *et al.* 2017a) have been developed, including self-paced curriculum learning (Jiang *et al.* 2015), self-paced learning with diversity (Jiang *et al.* 2014b), multi-view (Xu *et al.* 2015) and multi-task (Li *et al.* 2017a; Keerthiram Murugesan 2017) self-paced learning. In addition, several researchers have conducted theoretical analyses of self-paced learning. Meng et al. (Meng *et al.* 2015) provides a theoretical analysis of the robustness of *SPL*, revealing that the implicit objective function of *SPL* has a similar configuration to a non-convex regularized penalty. Such regularization restricts the contributions of noisy examples to the objective, and thus enhances the learning robustness. Ma et al. (Ma *et al.* 2017b) proved that the learning process of *SPL* always converges to critical points of its implicit objective under mild conditions. However, none of the existing self-paced learning approaches can be applied to our problem of leveraging clean labels in noisy data.

A.2 Robust Learning

A large body of literature on the robust learning problem has been established over the last few decades. Most of the studies aim to directly learn from noisy labels and focus on noise-robust algorithms. For instance, Chen et al. (Chen *et al.* 2013) proposed a robust algorithm based on trimmed inner product. McWilliams et al. (McWilliams *et al.* 2014) proposed a sub-sampling algorithm for large-scale corrupted linear regression. Bhatia et al. (Bhatia *et al.* 2015) and Zhang et al. (Zhang *et al.* 2017b) proposed hard-thresholding based methods with strong guarantees of coefficient recovery under a mild assumption on datasets. Another group of methods focuses on removing or correcting mislabeled data. For example, some work utilized heavy-tailed distributions (Zhu *et al.* 2013) such as Student t-distribution and Poisson distribution, to model the mislabeled data, while others detected these outliers based on Gaussian distribution (Solberg and Lahti 2005; Hodge and Austin 2004) under the assumption that outliers have a small probability of occurrence in the population. Some methods do not assume any prior knowledge on the data distribution based on kernel functions (Latecki *et al.* 2007; Roth 2006). These approaches utilize kernel functions to approximate the actual density distribution and declare the instances lying in the low probability area of the kernel density function as outliers. However, all these approaches typically jointly learn the clean and noisy data together, but cannot fully leverage the information contained in the clean set.

A.3 Weakly-Supervised Learning

Recently, some work in weakly-supervised learning (Medlock and Briscoe 2007) utilized additional clean labels in learning a noisy dataset. For instance, Azadi et al. (Zhang *et al.* 2017a) proposed an auxiliary image regularization to train a deep convolutional neural network in noisy labeled image data, in which a limited number of training examples are supplied with clean labels. In order to classify images from weakly labeled data, Li et al. (Li *et al.* 2017b) used not only a small clean dataset, but some other "side" information of label relations in a knowledge graph. Veit et al. (Veit *et al.* 2017) used millions of images with noisy annotations in conjunction with a small set of cleanly-annotated images to learn effective image representations, while Jiang et al. (Jiang *et al.* 2017) designed a curriculum paradigm

to learn the instance weights in corrupted labels to prevent deep convolutional neural networks from overfitting. Compared to existing work utilizing the clean dataset, our methods are different in two ways. First, we consider the learning process from clean to noisy data in a self-paced manner, which hedges the risk of training corrupted data samples. Moreover, our model learns the instance weight determined by the feedback of the learner itself without using any additional prior knowledge, which means our methods can be applied to more general problems in practice.

B Proof of Theorem 1

Proof. Before we prove the convergence of Algorithm 1, we will first show that the value of objective function $\mathcal{J}$ is monotonically decreased. Objective function $\mathcal{J}$ has the following property:

$$\begin{aligned}
&\mathcal{J}(\boldsymbol{w}^{t+1}, \boldsymbol{v}^{t+1}; \lambda^{t+1}) \\
&\quad \overset{(a)}{\leq} \sum_{i=1}^{k} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t+1})\big) + \sum_{i=k+1}^{n} v_i^{t+1} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t+1})\big) \\
&\qquad + \|\boldsymbol{w}^{t+1}\|_2^2 + \theta \|\boldsymbol{w}^{t+1} - \tilde{\boldsymbol{w}}\|_2^2 - \lambda^t \sum_{i=k+1}^{n} v_i^{t+1}
\end{aligned}$$

The inequality follows from the fact that λ increases monotonically so that $\lambda^{t+1} \geq \lambda^t$ and $v_i^t \geq 0$. The optimization step in Line 7 in Algorithm 1 guarantees the following property:

$$\begin{aligned}
&\sum_{i=k+1}^{n} v_i^{t+1} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t+1})\big) - \lambda^t \sum_{i=k+1}^{n} v_i^{t+1} \\
&\qquad \leq \sum_{i=k+1}^{n} v_i^{t} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t+1})\big) - \lambda^t \sum_{i=k+1}^{n} v_i^{t}
\end{aligned}$$

Therefore, we have the following property:

$$\begin{aligned}
&\mathcal{J}(\boldsymbol{w}^{t+1}, \boldsymbol{v}^{t+1}; \lambda^{t+1}) \\
&\quad \leq \sum_{i=1}^{k} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t+1})\big) + \sum_{i=k+1}^{n} v_i^{t} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t+1})\big) \\
&\qquad + \|\boldsymbol{w}^{t+1}\|_2^2 + \theta \|\boldsymbol{w}^{t+1} - \tilde{\boldsymbol{w}}\|_2^2 - \lambda^t \sum_{i=k+1}^{n} v_i^{t}.
\end{aligned}$$

Similarly, the following inequality is satisfied since the optimizations step in Line 5 in Algorithm 1.

$$\begin{aligned}
&\mathcal{J}(\boldsymbol{w}^{t+1}, \boldsymbol{v}^{t+1}; \lambda^{t+1}) \\
&\quad \leq \sum_{i=1}^{k} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t})\big) + \sum_{i=k+1}^{n} v_i^{t} \mathcal{L}\big(y_i, f(\boldsymbol{x}_i, \boldsymbol{w}^{t})\big) \\
&\qquad + \|\boldsymbol{w}^{t}\|_2^2 + \theta \|\boldsymbol{w}^{t} - \tilde{\boldsymbol{w}}\|_2^2 - \lambda^t \sum_{i=k+1}^{n} v_i^{t} \\
&\quad = \mathcal{J}(\boldsymbol{w}^{t}, \boldsymbol{v}^{t}; \lambda^{t})
\end{aligned}$$

Since the objective function is monotonically decreased and it has a lower bound according to Lemma 1, we have $\|\mathcal{J}^{t+1} - \mathcal{J}^t\|_2 < \varepsilon$ for $\forall \varepsilon > 0$. □

C Analysis of Parameter λ

Figure 1 shows the impact of parameter λ on both the robust regression and classification tasks. In Figure 1(a), the blue line depicts the relationship between parameter λ and the coefficient recovery error. As λ increases, the recovery error continues to decrease until it reaches a critical point, after which it increases. These results indicate that the training process will keep improving the model until parameter λ becomes so large that some corrupted samples are incorporated into the training data. The red line shows the value of the objective function $\mathcal{J}$ in terms of different values of parameter λ, leading us to conclude: 1) The value of objective function $\mathcal{J}$ monotonically decreases as λ increases. 2) The objective function $\mathcal{J}$ decreases much faster once λ reaches a critical point, following the same pattern as the recovery error shown in the blue line. In Figure 1(b), the blue line shows the values of the F1 score for the binary classification task. When λ increases, the F1 score increases quickly until it reaches a peak point. After that point, the score decreases because more corrupted data is incorporated into the training set. The red line shows the size of the training set. We can conclude: 1) When parameter λ increases, the size of the training set continuously increases until it reaches its maximum value. 2) When all the data is included into the training set, the F1 score also remains stable.

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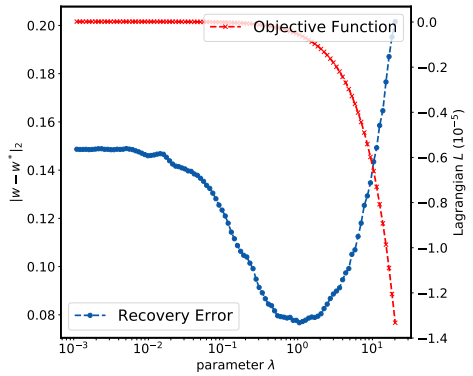
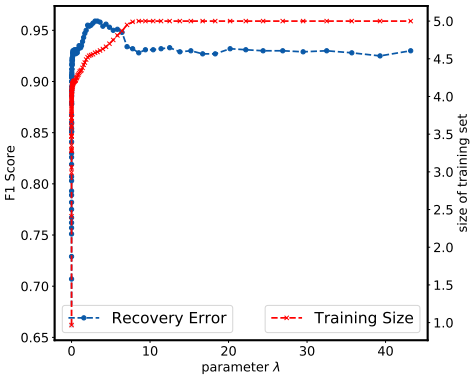


(a) Regression



(b) Classification

Figure 1: Impact of Parameter λ on Robust Regression and Classification Tasks

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