

SGD-NEURAL-NET( $\mathcal{D}_n, T, L, (m^1, \dots, m^L), (f^1, \dots, f^L)$ )

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1  for l = 1 to L
2       $W_{ij}^l \sim \text{Gaussian}(0, 1/m^l)$ 
3       $W_{0j}^l \sim \text{Gaussian}(0, 1)$ 
4  for t = 1 to T
5      i = random sample from  $\{1, \dots, n\}$ 
6       $A^0 = x^{(i)}$ 
7      // forward pass to compute the output  $A^L$ 
8      for l = 1 to L
9           $Z^l = W^{lT} A^{l-1} + W_0^l$ 
10          $A^l = f^l(Z^l)$ 
11     loss = Loss( $A^L, y^{(i)}$ )
12     for l = L to 1:
13         // error back-propagation
14          $\partial \text{loss} / \partial A^l = \text{if } l < L \text{ then } \partial \text{loss} / \partial Z^{l+1} \cdot \partial Z^{l+1} / \partial A^l \text{ else } \partial \text{loss} / \partial A^L$ 
15          $\partial \text{loss} / \partial Z^l = \partial \text{loss} / \partial A^l \cdot \partial A^l / \partial Z^l$ 
16         // compute gradient with respect to weights
17          $\partial \text{loss} / \partial W^l = \partial \text{loss} / \partial Z^l \cdot \partial Z^l / \partial W^l$ 
18          $\partial \text{loss} / \partial W_0^l = \partial \text{loss} / \partial Z^l \cdot \partial Z^l / \partial W_0^l$ 
19         // stochastic gradient descent update
20          $W^l = W^l - \eta(t) \cdot \partial \text{loss} / \partial W^l$ 
21          $W_0^l = W_0^l - \eta(t) \cdot \partial \text{loss} / \partial W_0^l$ 
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