

✓ P-8-3) A doppler radar is used to determine⁽⁸⁾ the speed of an moving vehicle by measuring the frequency shift of the wave reflected from the vehicle. determine the speed u in (km/hr) if $\Delta f = -2.33$ (kHz) with $f = 10.5$ GHz.
Ans:

$$\Delta f = \frac{-2u}{c} f$$

$$u = 120 \text{ (km/hr)}$$

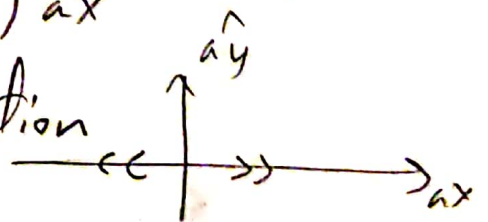
* Polarization of plane waves:

polarization: describes the time varying behavior of the electric field intensity vector at a specific point in space.

* Types:

$$* E = E_x \hat{a}_x = E_0 \cos(\omega t) \hat{a}_x$$

linearly polarized in x direction



$$* \text{ The same for } \vec{E} = E_y \hat{a}_y$$

linearly polarized in y direction

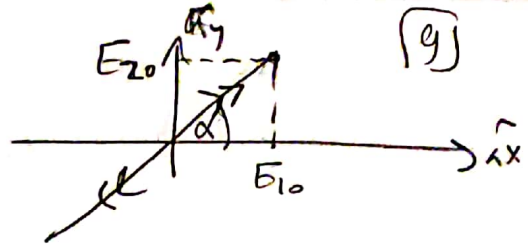
$$* E = E_x \hat{a}_x + E_y \hat{a}_y$$

$$= E_{10} \cos(\omega t) \hat{a}_x + E_{20} \cos(\omega t) \hat{a}_y$$

Linearly polarized

$$\alpha = \tan^{-1} \left(\frac{E_{20}}{E_{10}} \right)$$

For $E_1 = E_2 \longrightarrow \alpha = 45^\circ$



* $E(z, t) = \hat{x} E_{10} \cos(\omega t - \beta z) + \hat{y} E_{20} \sin(\omega t - \beta z)$

$$E(0, t) = \hat{x} E_{10} \cos(\omega t) + \hat{y} E_{20} \sin(\omega t)$$

$$= \hat{x} E_{10} \cos(\omega t) + \hat{y} E_{20} \cos(\omega t - \frac{\pi}{2})$$

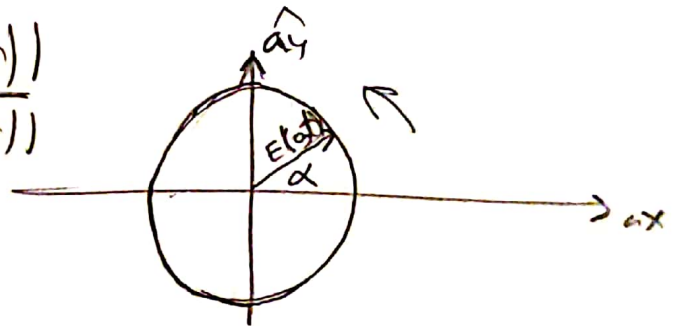
$E_{10} \neq E_{20} \longrightarrow$ elliptical polarization

$E_{10} = E_{20} \longrightarrow$ Circular ~

For $E_{10} = E_{20}$

$$\alpha = \tan^{-1} \left(\frac{E_{20} \sin(\omega t)}{E_{10} \cos(\omega t)} \right)$$

$$\alpha = \omega t$$



at $t=0 \longrightarrow \alpha=0$

$t = \frac{T}{8} \longrightarrow \alpha = \omega t = 2\pi f t = \frac{2\pi t}{T} = \left[\frac{\pi}{4} \right]$

$t = \frac{T}{4} \longrightarrow \alpha = \frac{2\pi}{T} \times \frac{T}{4} = \left[\frac{\pi}{2} \right]$

مع تغير الزمن فإن α تزيد في اتجاه عقارب الساعة (+ve)
(Counterclockwise polarization)

من هذه الحالة فإن أصابع اليد اليمنى تتبع اتجاه الدوران، وأصبع
اليد يسار يشير إلى اتجاه الانتشار
(right hand (+ve) polarization)

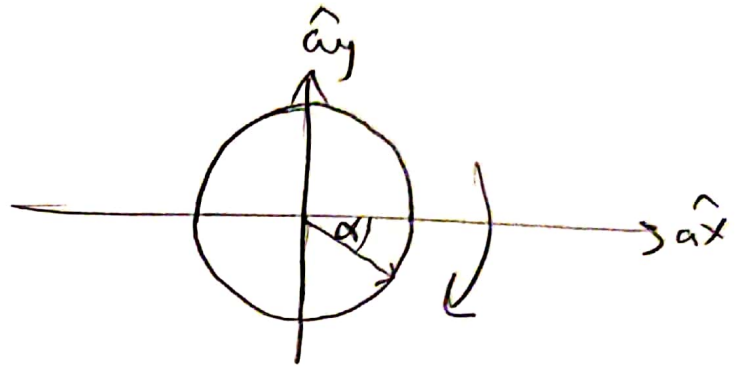
$$\begin{aligned}
 * \quad E(0, t) &= \hat{a}_x E_{10} \cos(\omega t) - \hat{a}_y E_{20} \sin(\omega t) \quad (10) \\
 &= \hat{a}_x E_{10} \cos(\omega t) + \hat{a}_y E_{20} \cos\left(\omega t - \frac{\pi}{2} + \pi\right) \\
 &= \hat{a}_x E_{10} \cos(\omega t) + \hat{a}_y E_{20} \cos\left(\omega t + \frac{\pi}{2}\right)
 \end{aligned}$$

For $E_{10} = E_{20}$

$$\alpha = -\omega t$$

$$t=0 \rightarrow \alpha = 0$$

$$t = \frac{T}{8} \rightarrow \alpha = -\frac{\pi}{4}$$



مع تغير الزمن فإن α تنزله في اتجاه عقارب الساعة
(Clockwise Polarization)

اصابع اليد اليسرى تتبع اتجاه دوران المجال الكهربائي
شعيرتي اتجاه الانتشار
(Left Hand (-ve) Polarization)

Ex: Find the Polarization of the field given by

$$\vec{E} = (2\hat{a}_x + j2\hat{a}_y) e^{+jkz}$$

Ans:

$$\vec{E}_x = 2 e^{+jkz}$$

$$\begin{aligned}
 \vec{E}_y &= j2 e^{+jkz} = 2 e^{+j\frac{\pi}{2}} e^{+jkz} \\
 &= 2 e^{+j\left(\frac{\pi}{2} + kz\right)}
 \end{aligned}$$

$$\begin{aligned}
 E_x(z, t) &= \text{Re} \left(2 e^{+jkz} e^{j\omega t} \right) \\
 &= 2 \cos(\omega t + kz)
 \end{aligned}$$

$$E_y(z,t) = \operatorname{Re} \left(2 e^{j(kz + \frac{\pi}{2})} e^{j\omega t} \right) \quad \text{III}$$

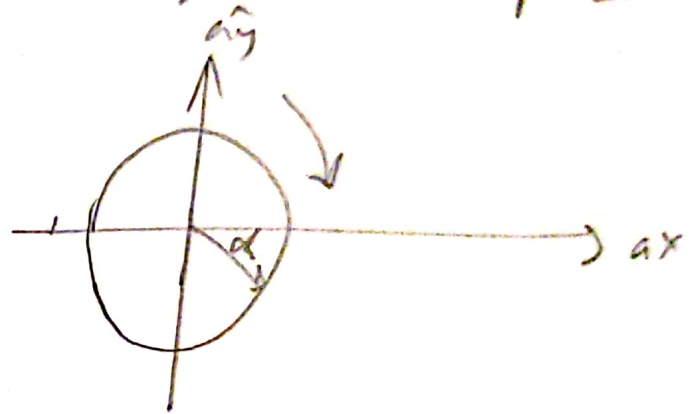
$$= 2 \cos(\omega t + kz + \frac{\pi}{2})$$

$$\vec{E}(z,t) = 2 \cos(\omega t + kz) \hat{a}_x + 2 \cos(\omega t + kz + \frac{\pi}{2}) \hat{a}_y$$

$$E(0,t) = 2 \cos(\omega t) \hat{a}_x + 2 \cos(\omega t + \frac{\pi}{2}) \hat{a}_y$$

$$\therefore E_{10} = E_{20} = 2 \Rightarrow \text{Circular Polarization}$$

clockwise
Circular polarization



Q 8-6

✓ The E-field of a uniform wave propagating in a dielectric medium is given by:

$$E(t,z) = \hat{a}_x 2 \cos(10^8 t - \frac{z}{\sqrt{3}}) - \hat{a}_y \sin(10^8 t - \frac{z}{\sqrt{3}})$$

- Determine the frequency and wavelength v_m of the wave
- What is the dielectric constant of the medium
- Describe the polarization of the wave.
- Find the corresponding H field.

Ans:

$$\omega = 10^8 \Rightarrow f = \frac{10^8}{2\pi} = \boxed{1.59 \times 10^7 \text{ Hz}}$$

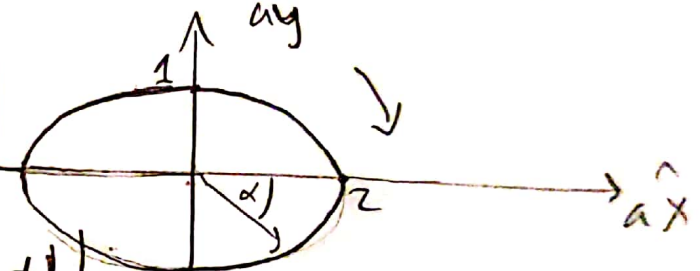
$$\beta = \frac{1}{\sqrt{3}} \Rightarrow \lambda = \frac{2\pi}{\beta} = \boxed{2\sqrt{3} \pi \text{ m}}^{(12)}$$

$$b) \quad u = \frac{c}{\sqrt{\epsilon_r}} = \frac{\omega}{\beta}$$

$$\epsilon_r = 3$$

$$c) \quad \vec{E}(0, t) = \hat{a}_x 2 \cos(10^8 t) - \hat{a}_y \sin(10^8 t) \\ = \hat{a}_x 2 \cos(10^8 t) + \hat{a}_y \cos(10^8 t - \frac{\pi}{2} + \pi) \\ = \hat{a}_x 2 \cos(10^8 t) + \hat{a}_y 0 \cos(10^8 t + \frac{\pi}{2})$$

$\therefore E_{10} \neq E_{20} \Rightarrow$ elliptical pol.

$$\alpha = \tan^{-1} \left(\frac{-\sin(10^8 t)}{2 \cos(10^8 t)} \right) \\ \Rightarrow -\tan^{-1} \left(\frac{1}{2} \tan(10^8 t) \right)$$


left hand clockwise elliptical polarization

d)

$$\vec{H} = \frac{1}{\eta} (\vec{a}_z \times \vec{E})$$

$$\eta = \sqrt{\frac{\mu}{\epsilon}} = \sqrt{\frac{\mu}{\epsilon_0 \epsilon_r}} = \frac{\sqrt{\mu_0 / \epsilon_0}}{\sqrt{\epsilon_r}} = \frac{120 \pi}{\sqrt{3}}$$

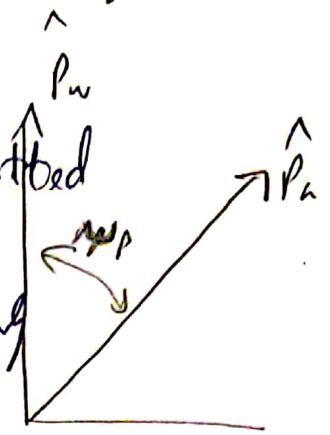
$$\vec{H} = \frac{\sqrt{3}}{120 \pi} \left[\hat{a}_x \sin \left(10^8 t - \frac{\pi}{\sqrt{3}} \right) + \hat{a}_y \cos \left(10^8 t - \frac{\pi}{\sqrt{3}} \right) \right] \text{ A/m}$$

* Polarization Loss Factor :

For max reception, the receiving antenna should be parallel to \vec{E} .

\hat{P}_w : is a unit vector for the transmitted wave

\hat{P}_a : is a unit vector for receiving antenna.



ϕ_p : angle between two vectors

$$PLF = | \hat{P}_w \cdot \hat{P}_a |^2 = | \cos \phi_p |^2$$

$$PLF_{dB} = 10 \log | \hat{P}_w \cdot \hat{P}_a |^2 \\ = 20 \log (\cos \phi_p)$$

$$P_{received} = P_{transmitted} * PLF$$

(PLF=1) means P_{trans} is P_{rec} \rightarrow $\phi_p = 0$
 ($\phi_p = 0$) is \parallel lines

(PLF=0) means $P_{rec} = 0$ \rightarrow $\phi_p = 90^\circ$

($\phi_p = 90^\circ$) \perp lines

- * TV Broadcasting (linear horizontal Polar.)
- * AM ~ (linear vertical Polar.)
- * FM ~ (Circular Polar.)