LETTER

Three-dimensional printing of hierarchical liquid–crystal–polymer structures

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Fibre-reinforced polymer structures are often used when stiff lightweight materials are required, such as in aircraft, vehicles and biomedical implants. Despite their very high stiffness and strength[1], such lightweight materials require energy- and labour-intensive fabrication processes[2], exhibit typically brittle fracture and are difficult to shape and recycle[3,4]. This is in stark contrast to lightweight biological materials such as bone, silk and wood, which form by directed self-assembly into complex, hierarchically structured shapes with outstanding mechanical properties[5–11], and are circularly integrated into the environment. Here we demonstrate a three-dimensional (3D) printing approach to generate recyclable lightweight structures with hierarchical architectures, complex geometries and unprecedented stiffness and toughness. Their features arise from the self-assembly of liquid-crystal polymer molecules into highly oriented domains during extrusion of the molten feedstock material. By orienting the molecular domains with the print path, we are able to reinforce the polymer structure according to the expected mechanical stresses, leading to stiffness, strength and toughness that outperform state-of-the-art 3D-printed polymers by an order of magnitude and are comparable with the highest-performance lightweight composites[1,12]. The ability to combine the top-down shaping freedom of 3D printing with bottom-up molecular control over polymer orientation opens up the possibility to freely design and realize structures without the typical restrictions of current manufacturing processes.

The manufacture of polymer-based lightweight structures is currently limited either to 3D-printed complex parts, which show poor molecular orientation and mechanical strength[13,14] (Extended Data Fig. 1), or to highly oriented stiff polymers, the shapes of which are restricted to simple geometries[15,16]. To combine shaping freedom with molecular orientation, the 3D printing of liquid-crystal elastomers has been recently exploited[17–19]. Although desirable shape-morphing effects can be achieved, the Young's modulus of such soft elastomers is three to four orders of magnitude lower than those of high-performance liquid-crystal synthetic fibres. This is explained by the presence of relatively long, flexible segments in the molecular structure of the polymer.

To fully exploit the shaping freedom of 3D printing and the favourable mechanical properties expected from molecularly oriented liquid-crystal polymers (LCPs), we propose an approach that conceptually follows two design principles that are used in nature to grow strong and tough biological materials[20]. First, anisotropy is achieved during the printing process by self-assembly of the LCP along the print path. Second, anisotropy and the complex-shaping capabilities offered by 3D printing are exploited to tailor the local stiffness and strength of the structure according to the specific loading conditions imposed by the environment.

The rigid molecular segments of aromatic thermotropic polyesters are known to self-assemble into nematic domains at temperatures higher than the melting temperature of the material (Fig. 1a, b). In the polymer melt at rest, there is no preferred orientation of the individual ordered nematic domains, leading to a globally random orientation distribution (Fig. 1c). Extrusion of the polymer melt through the nozzle of the 3D printer gives rise to shear and extensional flow fields that align the nematic domains in the direction of flow (Fig. 1d). As the molten polymer exits the nozzle, the flow ceases and the extruded filament is exposed to the ambient temperature. A temperature gradient is then formed between the cold surface of the filament and its hot interior. Rapid cooling at the surface leads to solidification of the nematic order in the flow-aligned arrangement. By contrast, polymer chains present in the interior of the filament experience slower cooling, and therefore have sufficient time to re-orient, driven by thermal motion. As a result, the extruded filaments possess a core–shell structure, in which a highly aligned skin encloses a less oriented core (Figs. 1e, f, 2a). The thickness of the skin depends on the filament diameter and the operating temperatures. A simple analytical heat-transfer model was used to predict the effect of these relevant printing parameters on the final core–shell architecture (Fig. 2b and equation (16) in Methods). Optical microscopy and X-ray scattering experiments confirm the formation of a highly aligned skin, the relative fraction of which increases as the filament size decreases (Fig. 2b–d, Extended Data Fig. 2). Although the possibility of aligning thermotropic LCPs in the nozzle of a fused deposition modelling (FDM) printer has been suggested previously, the mechanical properties of the obtained objects remained below those of their conventional injection-moulded counterparts[21]. By contrast, the core–shell filaments produced in our study showed notable mechanical strength and elastic modulus (Fig. 2).

The effect of the core–shell architecture on the tensile mechanical behaviour of individual filaments was investigated in order to establish a quantitative correlation between mechanical performance and relevant printing parameters. Individual filaments can be extruded vertically starting from the build platform, or horizontally onto the substrate at a constant height. The vertically extruded filament cools symmetrically in air and its diameter is controlled by the diameter of the nozzle (Fig. 1e). During the deposition of horizontal filaments, inhomogeneous heat-transfer conditions at the boundary of the filament and the substrate result in non-uniform skin thickness in the filament cross-section (Fig. 1f). Regardless of the printing configuration, the Young's modulus of the printed filaments increases as much as threefold when the nozzle diameter is decreased from 800 μm to 150 μm, and as much as sevenfold when the layer height is decreased from 400 μm to 50 μm (Fig. 2e, f). A similar trend was observed for the tensile strength of the filaments. This can be qualitatively explained by the increase in the relative fraction of aligned molecules as the filament diameter or layer height decreases. For vertical filaments, the dependence of the Young's modulus on the nozzle diameter is well described by a simple scaling law that is derived from the heat-transfer model used to predict the thickness of the skin layer (equation (16) in Methods). According to this model, the Young's modulus (E) scales with the inverse of the nozzle diameter ($1/d_N$). The ability to produce filaments thinner than the nozzle diameter and thus increase considerably the fraction of aligned domains (Fig. 2c) makes the horizontal

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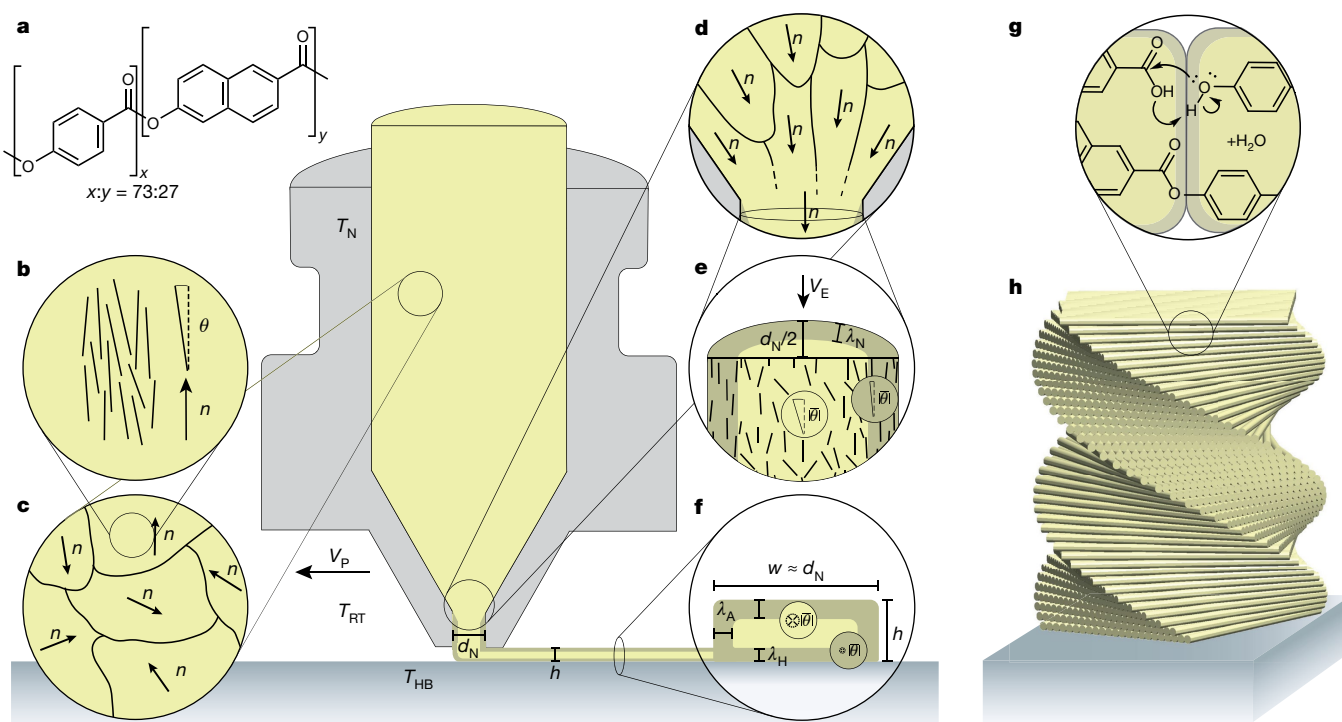
Fig. 1 | Printing hierarchical, thermotropic LCPs using fused deposition modelling. a, An aromatic random copolyester consisting of the rigid monomers *p*-hydroxybenzoic acid and 2-hydroxy-6-naphthoic acid forms short rod-like polymer chains. **b**, The rigid polymer rods align along the same director *n* in the melt. They are not perfectly oriented but show a certain misalignment θ towards the director, forming a nematically ordered domain. **c**, Locally aligned nematic domains with randomly oriented directors form the quasi-isotropic bulk of the polymer. **d**, The directors are subjected to elongational and shear forces during the extrusion through the heated nozzle (at temperature T_N) with diameter d_N. These forces can rearrange the polymers in the melt and align the directors along the extrusion direction. **e**, The material starts to lose its orientation once it has been extruded. At the same time the solidification front freezes the nematic order in place, starting from the surface. These two effects result in a core–shell microstructure with a highly aligned shell of thickness λ_N. **f**, Depositing material on a surface at a height *h* promotes further alignment of the director in the print direction and forms a core–shell structure with different skin thicknesses due to the distinct cooling rates for air, the glass surface and the polymer substrate. T_{HB}, temperature of the heated bed or substrate; T_{RT}, temperature of the environment (room temperature); V_E, velocity of extrusion; V_P printing velocity; *w*, print width; λ_A, thickness of skin aligned towards air; λ_H, thickness of skin aligned towards the heated bed or substrate. **g**, **h**, After printing, chain ends can chemically crosslink via thermal annealing, which increases the molecular weight and enhances stress transfer between filaments.

printing configuration very effective for improving the stiffness and the strength of the printed materials.

In addition to the nozzle diameter and layer height, temperature is another parameter that can be controlled conveniently during the printing process. Our experimental data show that both the Young's modulus and the tensile strength of printed filaments increase as the temperature at the nozzle is decreased. This correlation can be qualitatively explained by the fact that the solidification process is faster if the nozzle temperature is closer to the melting temperature of the polymer. Faster solidification results in thicker skins and therefore improved stiffness and strength. This effect can also be quantitatively illustrated using the scaling law obtained from the analytical heat-transfer model (Fig. 2g and equation (16) in Methods).

An important additional feature of the aromatic polyester used as the liquid-crystal feedstock is that its printed filaments can be chemically cross-linked by thermal annealing. Cross-linking occurs via post-condensation reactions between carboxylic acid and hydroxy groups present at the end of the macromolecules (Fig. 1g). The formation of cross-links is expected to increase the molecular weight and enhance stress transfer between adjacent macromolecules, thereby improving the tensile behaviour of the polymer under load. Indeed, annealing for 96 h was found to increase the tensile strength of printed filaments by a factor of two, reaching a value of 1 GPa for filaments printed horizontally. Within the first 10 h of thermal treatment, the tensile strength of the filament was observed to follow a square-root dependence on the annealing time. This suggests that the cross-linking reaction is controlled by the diffusion of reaction products—such as

water molecules—away from the reaction sites, which supports the hypothesis that a post-condensation reaction is responsible for the observed strengthening effect (Extended Data Fig. 3a).

After analysing the structure and properties of individual filaments, we then turned our attention to more complex fibre laminates that are obtained by printing filaments adjacent to one another in a specific direction (Fig. 3). As expected, maximal Young's modulus and tensile strength are achieved by printing filaments parallel to the mechanical-loading direction (Fig. 3a). Increasing the angle between filament orientation and the loading direction decreases the Young's modulus of the printed structure substantially, as predicted from classical laminate theory (Fig. 3a, Extended Data Fig. 4 and equation (18) in Methods). Overall, the structure, stiffness and strength of the printed laminates can be tuned over a wide range using the same control parameters that were investigated for individual filaments, namely layer height and temperature (Extended Data Fig. 5).

The molecular cross-links formed by thermal annealing also have a considerable effect on the strength of the printed laminates. For low alignment angles (0° and 30°), the bending strength of the laminate increases by 50% to 100% after the thermal treatment (Fig. 3b). Annealed samples tested in tensile mode at 90° also show an almost 100% increase in strength after 96 h (Fig. 3c), while simultaneously increasing the Young's modulus owing to enhanced load transfer between filaments in the composite. The observed strengthening effect follows the diffusion-controlled kinetics that are expected for the post-condensation reaction (Extended Data Fig. 3b). More importantly, thermally induced cross-linking markedly changes the fracture
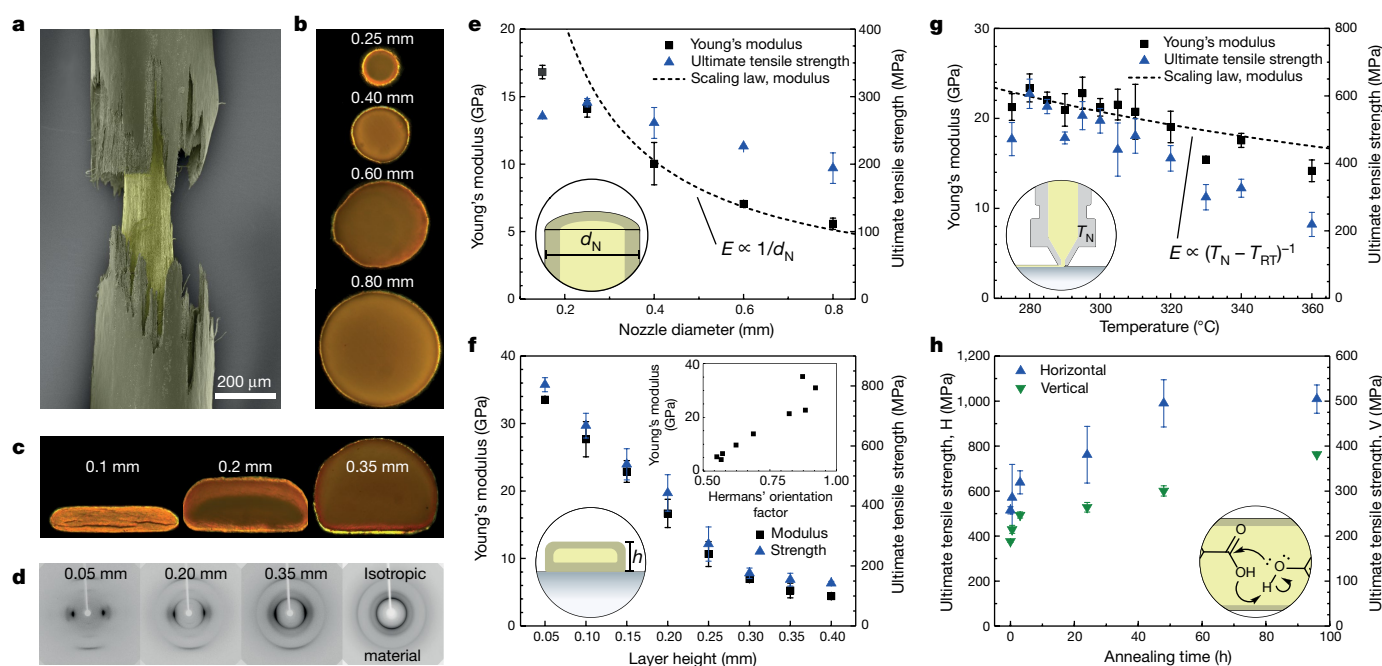
Fig. 2 | The LCP filament properties correlate strongly with the printing conditions. a, False-coloured scanning electron microscopy image of the tensile-tested vertical filament confirms a core–shell structure. The fact that the core of the fibre is still intact indicates that the shell of the LCP fibre is the stiffer phase. **b, c**, Polarized light microscopy of a 100-μm cross-section confirms the presence of a core–shell structure in both vertical (**b**) and horizontal (**c**) filaments, as indicated by the more intense illumination of the skin of the printed filaments compared to the core. **d**, X-ray diffraction measurements confirm a higher fraction of oriented polymers in thinner samples. **e**, The Young's modulus and the strength of vertically extruded lines increase with decreasing nozzle diameter because of the increased fraction of oriented polymer in the print line. This hypothesis is supported by a scaling law that successfully captures the dependence behaviour of the printed laminates (Fig. 3d). Complete fracture of lam-

of the Young's modulus on the nozzle diameter d_N. **f**, This effect of the core–shell architecture also translates to horizontally printed filaments, where the Young's modulus and strength increase with decreasing print filament height, reaching a maximum reported modulus of 34 GPa and a maximum strength of 800 MPa. **g**, Increased printing temperatures lead to longer cooling times, and therefore longer times for the freezing of the aligned nematic microstructure. This results in an inverse correlation between the Young's modulus and the temperature difference ($T_N - T_{RT}$). **h**, Solid-state annealing further enhances the properties by increasing the molecular weight of the polymer. The strength increases up to 400 MPa for vertically extruded filaments (V) and up to 1 GPa for horizontally printed filaments (H). Error bars indicate the standard deviation for five to ten measurements at each data point.

inates subjected to annealing is possible only after more than 8% tensile strain is applied. During such straining, multiple peak loads have to be overcome, which leads to substantial energy dissipation during the fracture process. The multiple stress peaks observed resemble those of toughening mechanisms in resilient biological materials such as mollusc shells and bone. This toughening effect contrasts with the abrupt failure of the unannealed specimens after a peak stress is achieved. On the basis of these results and the increased shear strength of the laminates (Extended Data Fig. 6a), we infer that the thermal treatment not only strengthens the individual filaments but also establishes cross-links between filaments in the laminate. Such cross-links are expected to enhance stress transfer between filaments (Extended Data Fig. 6b) and to prevent their delamination through crack-arresting mechanisms. Therefore, the high toughness of the annealed laminates probably emerges from the hierarchical cross-linking of macromolecules and of filaments at increasing length scales.

Besides the self-assembly and hierarchical cross-linking of macromolecules, our 3D printing approach provides a means to replicate other design principles of biological materials. Analogous to the biological growth of living tissues, 3D printing is unique in its ability to create customized material architectures in a layer-by-layer additive fashion. We illustrate this capability by 3D-printing laminate architectures in which the filament orientation is designed to best respond to the local strains imposed by a specific mechanical loading condition. In our example, a plate with a central hole is subjected to a global tensile strain in one specific direction (Fig. 4a). Two distinct laminate architectures containing either straight (unidirectional) or curvilinear (directional) filaments (Extended Data Fig. 7) were tested and compared to a reference sample that comprised isotropic hot-pressed LCPs.

The higher intrinsic strength and stiffness of printed filaments leads to a threefold increase in stiffness and a fivefold increase in strength of the unidirectional architecture compared to isotropic LCPs. The use of a load-specific print architecture that follows the stress lines that develop around the hole doubles the strength of the sample compared to the unidirectional sample. Thermal annealing further increases the strength and stiffness of both sample geometries.

Laminates with unidirectional and curvilinear designs contain filaments lying predominantly parallel to the loading direction to arrest cracks that propagate from the central hole, which acts as a stress concentrator. The high local strains in the periphery of the hole were experimentally confirmed by strain maps obtained by digital image correlation analysis (Fig. 4b). Similar to the fibre architectures found in wood and bone, the aligned reinforcement of such laminates prevents catastrophic failure by promoting crack-arresting mechanisms within the material as well as providing strength and toughness via the core–shell structure of the printed filament. As a result, the modulus of toughness of laminates with aligned architectures is about 30- to 55-fold higher than that of the isotropic reference specimen. The higher strength and Young's modulus of specimens that display the curvilinear reinforcement design demonstrates our ability to produce high-performance laminates by tuning the fibre orientation to best match the stress lines developed throughout the mechanically loaded structure.

The high toughness of the printed laminates is accompanied by a marked increase in specific Young's modulus without loss of the intrinsically high damping properties of aromatic polyesters (Fig. 4c). With this unique combination of properties, our printed LCP laminates clearly stand out in comparison to other existing lightweight materials. In terms of specific strength and Young's modulus, printed LCPs surpass the properties of glass fibre-reinforced polymers and
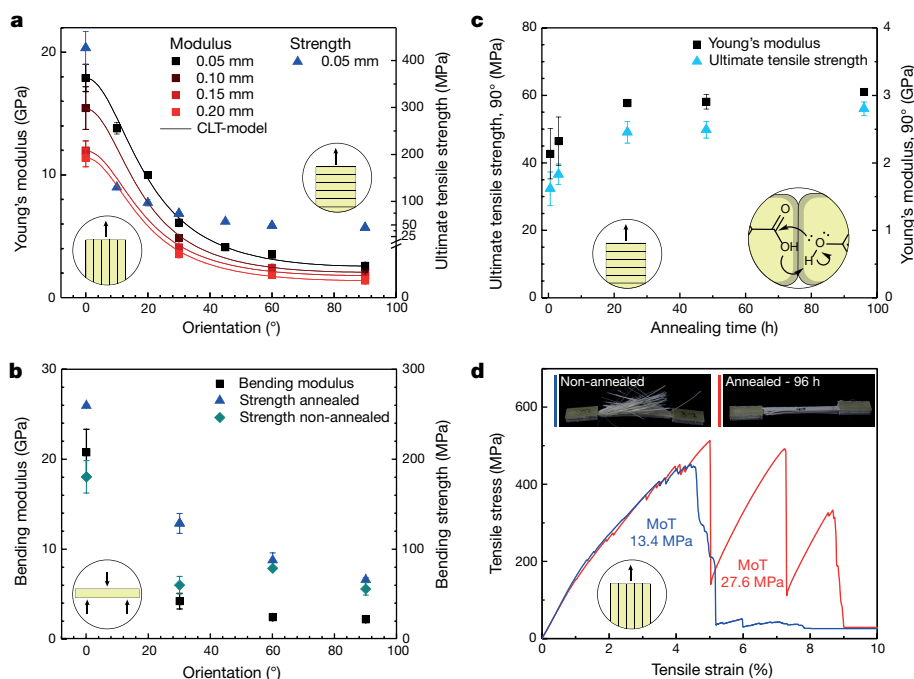
Fig. 3 | Mechanical properties of LCP parts printed through the unidirectional deposition of filaments. a, Like that of fibre-reinforced composite materials, the Young's modulus of unidirectional printed parts depends on the printing orientation, as predicted by classical laminate theory (CLT). **b**, Bending properties follow the same trend, as expected for a system composed of oriented fibres. Annealing increases the bending strength by increasing the stress transfer between different print filaments. **c**, Annealing tensile samples printed 90° to the loading direction increases the strength over time owing to the improved adhesion between filaments. Initially, this process is controlled by the

diffusion of water molecules generated during the post-condensation reaction. Error bars indicate the standard deviation for five to ten measurements at each data point. **d**, For samples with print lines oriented in the loading direction, the fracture mode changes from a broom-like to a tough layer-like fracture owing to the improved filament adhesion achieved by thermal annealing (96 h). This change also results in a saw-tooth break pattern in the stress–strain curve, which increases the amount of energy required to fracture the part (modulus of toughness, MoT) by a factor of two.
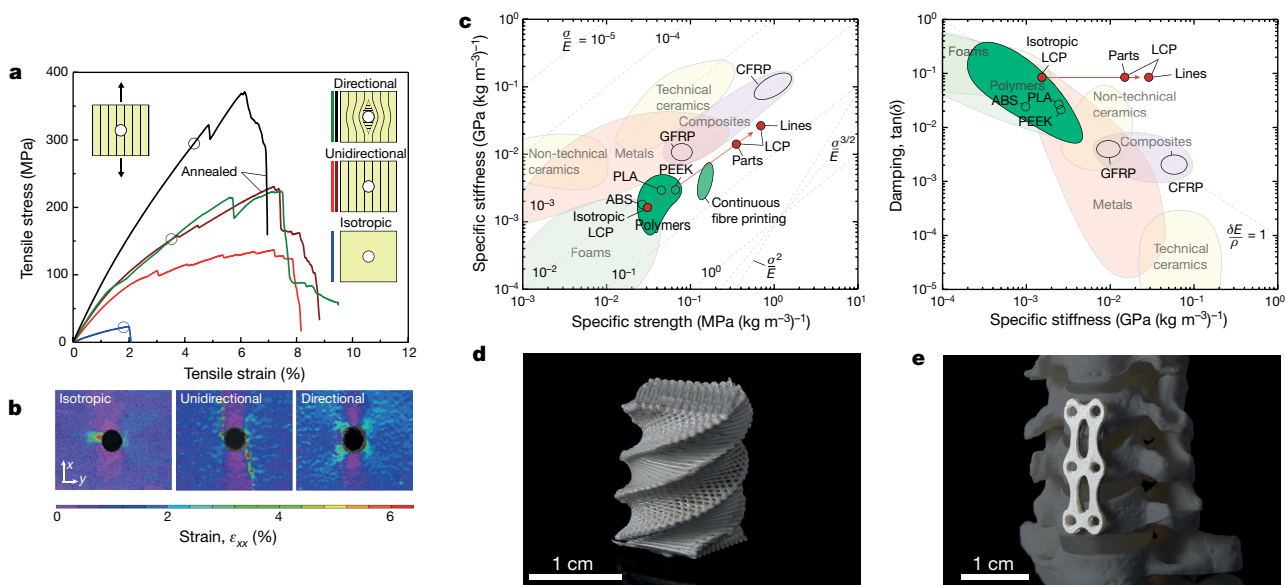
Fig. 4 | Mechanical properties and complex geometry of 3D-printed LCP laminates and parts. a, Mechanical response under tension of open-hole LCP laminates, highlighting the improved properties obtained when the filament architecture is designed to follow the stress lines developed within the loaded material. **b**, Open-hole strain maps measured by digital image correlation just before fracture. **c**, Ashby diagrams indicating the specific stiffness and specific strength (left) and damping (right) properties of LCP lines and parts compared to the isotropic counterpart and state-of-the-art polymers and reinforced composite materials[22].

σ, strength; ρ, density; ABS, acrylonitrile butadiene styrene; CFRP, carbon fibre reinforced polymer; GFRP, glass fibre reinforced polymer; PEEK, polyether ether ketone; PLA, polylactic acid. **d**, **e**, Examples of 3D-printed LCP parts with complex fibre architectures and geometries: impact-resistant Bouligand-type structure with twisted plywood arrangement of printed fibres (**d**) and biomedical implant with a local bearing enhancement where the print lines are programmed to follow the principle stress direction around holes (**e**).

continuous fibre-printed composites (Fig. 4c). Indeed, the stiffness and strength of our printed laminates approach those of carbon-fibre reinforced polymers, with the added value of recyclability (Extended Data Fig. 8), automated manufacturing and lower carbon footprint. By taking advantage of the shaping capabilities of 3D printing, special complex geometries and application-specific shapes can be produced using the proposed additive technology (Fig. 4d, e). By combining the tool path control provided by the 3D printer with the tunable orientation of self-assembled building blocks within the ink, we can reach unparalleled levels of hierarchical structural complexity (Fig. 4d). As opposed to current FDM printed polymer parts, the anisotropic filament architectures implemented in these complex geometries can be designed to achieve toughness comparable to that of the strongest polymer-based lightweight materials. This approach is in contrast with the usual strategy to reduce anisotropy in 3D-printed synthetic parts, and opens up the possibility to fabricate structures that can fulfil different performance requirements while ensuring a sustainable circular life cycle of the material.

Online content

Any methods, additional references, Nature Research reporting summaries, source data, statements of data availability and associated accession codes are available at https://doi.org/10.1038/s41586-018-0474-7.

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Skin formation due to shear at the nozzle wall. The formation of a skin in printed filaments may result from the shear-induced alignment of LCP molecules close to the walls of the nozzle, where shear rates are maximal during extrusion. To evaluate this hypothesis, we first estimate the thickness of such a shear-induced skin layer (λ) for different nozzle diameters (d_N). Because the skin thickness directly affects the Young's modulus of the filaments, this theoretical analysis is later compared with our experimental mechanical data to test the hypothesis.

The thickness of the skin layer depends on the shear rate profile across the radius of the nozzle. For fully developed laminar flow, the shear rate is zero at the centre of the nozzle ($r = 0$) and increases continuously until it reaches the maximal value at the wall ($r = R$). Because the time required for alignment increases for lower shear rates, there will be a critical radius r_c above which the shear rates will be sufficiently high ($\dot{\gamma} > \dot{\gamma}_c$) to align the particles within the residence time of the material in the nozzle. Such a critical radius defines the skin thickness as $\lambda = R - r_c$.

To establish a correlation between λ and d_N ($2R$) we compare the time required for alignment (t_a) with the residence time (t_{res}). For an anisotropic rod-like particle suspended in a fluid, the alignment time should scale with the inverse of the shear rate, such that:

$$t \approx \frac{1}{\dot{\gamma}} \tag{3}$$

As a first approximation, we assume this simple relation to also be applicable to the LCP polymers investigated here. It follows that $t_a \approx 1/\dot{\gamma}_c$. To determine $\dot{\gamma}_c$ and thus t_a, we estimate the shear rate profile along the radius of the nozzle ($\dot{\gamma}(r)$).

The shear rate profile can be calculated from the derivative of the flow velocity with respect to the nozzle radius ($v(r)$). Such flow velocity depends on the rheological properties of the fluid. For a non-Newtonian fluid, the velocity profile is given by:

$$v(r) = \frac{3n + 1}{n + 1} \frac{Q}{\pi R^2} \left[1 - \left(\frac{r}{R} \right)^{1 + 1/n} \right] \tag{4}$$

where Q is the volumetric flow rate. Here, we assume the fluid to be described by a power-law relation, such that the viscosity (η) is given by $\eta = k\dot{\gamma}^{n-1}$, where k and n are constants. By taking the derivative of the velocity profile, the shear rate at different radial positions can be directly obtained:

$$|\dot{\gamma}(r)| = \frac{3n + 1}{n} \frac{Q}{\pi R^3} \left(\frac{r}{R} \right)^{1/n} \tag{5}$$

Combining equations (3) and (5) leads to the following scaling relation for the alignment time as a function of the nozzle radius:

$$t_a \approx \frac{n}{3n + 1} \frac{\pi R^3}{Q} \left(\frac{r_c}{R} \right)^{-1/n} \tag{6}$$

Comparison of the alignment time with the residence time of the material inside the nozzle enables us to predict the amount of material that aligns during the extrusion process. The residence time for a nozzle of length L is given by:

$$t_{res} = \frac{\pi R^2 L}{Q} \tag{7}$$

As shear-induced alignment occurs when $t \leq t_{res}$, equations (6) and (7) can be combined to obtain:

$$\lambda = R \left\{ 1 - cR^n \left[\frac{n}{(3n + 1)L} \right]^n \right\} \tag{8}$$

where c is a constant that is independent of the nozzle radius.

For strongly shear-thinning fluids such as the LCP melts, it is reasonable to assume that $n \to 0$. This simplifies equation (8) to $\lambda = R(1 - c)$. Combining this relation with the expected Young's modulus ($E_V = \lambda E_{skin}/d_N$, see main text), we finally obtain:

$$E_V = \frac{(1 - c)E_{skin}}{2} \tag{9}$$

This relation shows that the elastic modulus of the filament does not dependent on the nozzle diameter under the assumptions outlined above. Because our experimental data show a clear decrease of E_V with increasing nozzle diameters (Fig. 2e), our analysis suggests that skin formation is not controlled by shear-induced alignment at the nozzle wall.

Skin formation due to rapid cooling of the filament surface. Another hypothesis is that the thickness of the filament skin is determined by the cooling kinetics of the extrudate as the material exits the nozzle. This scenario can be theoretically described using a simple heat-transfer model. Such analysis assumes that the LCP nematic domains align strongly during extrusion of the feedstock material through the nozzle and that such alignment is maintained in the filament after extrusion only if the material is cooled fast enough to prevent random reorientation of domains driven by thermal motion. Moreover, the LCP domains in the extruded filament are assumed to reach the same level of orientation within the entire range of extrusion temperatures and filament thicknesses investigated in our experiments (Fig. 2).

The cooling of the filament after it leaves the printing nozzle can be described using the following equation describing the spatio-temporal evolution of the temperature of the material:

$$T(x, t) = T_{RT} + (T_N - T_{RT}) \mathrm{erf} \left(\frac{x}{2\sqrt{\alpha t}} \right) \tag{10}$$

where x is the distance from the filament surface, t is the time elapsed after the material exits the nozzle, T_N is the temperature inside the nozzle, T_{RT} is the temperature of the substrate (that is, room temperature) and α is the thermal diffusivity. Using a Taylor series expansion of the error function and considering only the first term, we obtain:

$$T(x, t) = T_{RT} + (T_N - T_{RT}) \left(\frac{x}{\sqrt{\pi \alpha t}} \right) \tag{11}$$

This simple equation can be used to predict the fraction of material that solidifies sufficiently fast to maintain the alignment of the LCP domains along the extrusion direction. Solidification requires that the temperature of the extruded material reaches the melting temperature ($T(x, t) = T_m$), whereas the preservation of flow-induced alignment is only possible if the cooling timescale t lies below the relaxation time of the LCP domains (τ). Using the skin depth λ to quantify the fraction of aligned material, we obtain the following relation:

$$\lambda = \frac{T_m - T_{RT}}{T_N - T_{RT}} \sqrt{\pi \alpha \tau} \tag{12}$$

The relaxation time τ provides a characteristic timescale for the exponential decay of the domain orientation parameter S, as described by the equation[36]:

$$S(t) = S_0 \exp \left(-\frac{t}{\tau} \right) \tag{13}$$

where S_0 is the initial flow-induced orientation. Because the orientation decays exponentially with time and minor misalignments are sufficient to strongly reduce the mechanical properties of the filament along the printing direction, we expect that cooling has to occur within timescales $t \ll \tau$ to obtain a filament shell with high mechanical properties.

Assuming that the core–shell structure is indeed controlled by thermal transport across the extrudate and that the mechanical properties of the filament are determined by the fraction of aligned LCP domains, we can use the above model to predict the dependence of the elastic modulus of the LCP filaments on the printing parameters. To this end, we estimate the elastic modulus E of the whole filament using a rule of mixture:

$$E = \phi_{skin} E_{skin} + \phi_{core} E_{core} \approx \phi_{skin} E_{skin} \tag{14}$$

Here E_{skin} is the modulus of the fully aligned polymer and ϕ_{skin} is the volume fraction of aligned material across the filament. ϕ_{skin} for horizontal and vertical filaments of diameter d_N can be geometrically described as:

$$\phi_{skin,V} = \frac{2\lambda}{d_N} \left(2 - \frac{2\lambda}{d_N} \right) \approx \frac{4\lambda}{d_N}$$
$$\phi_{skin,H} = 2\lambda \left(\frac{1}{d_N} + \frac{1}{h} \right) \tag{15}$$

Introducing these relations into the rule-of-mixture equation yields the Young's modulus as a function of print parameters for the vertically and horizontally printed filaments:

$$E_V = \frac{4E_{skin}}{d_N} \sqrt{\pi \alpha \tau} \left(\frac{T_m - T_{RT}}{T_N - T_{RT}} \right)$$
$$E_H = \left(\frac{2}{d_N} + \frac{2}{h} \right) E_{skin} \sqrt{\pi \alpha \tau} \left(\frac{T_m - T_{RT}}{T_N - T_{RT}} \right) \tag{16}$$

The experimentally measured Young's modulus of vertical filaments (Fig. 2e, g) was found to indeed scale with $1/d_N$ and $1/(T_N - T_{RT})$, as predicted by the equations proposed above. This supports the hypothesis that the mechanical properties of the filaments are controlled by the cooling kinetics of the extruded material.

This finding has direct implications for the 3D printing of tough LCP parts, because it implies that highly aligned filaments require not only the design of nozzles that promote shear and extensional flow, but also strategies to quickly extract heat from the extruded material. In our work, the shear and extensional flow was always above the critical value that is needed to orient the nematic domains of the LCP in the melt along the extrusion direction. The cooling was effectively achieved by depositing the material very close to the substrate or to the previously deposited (and cooled) polymer layers, such that thin print layers with low thermal diffusion length are obtained.

Classical laminate theory. The elastic modulus of printed LCP parts for distinct mechanical loading directions was theoretically estimated using classical laminate theory. To this end, we use a coordinate system in which direction 1 corresponds to the print direction and direction 2 lies perpendicular to it, both of which are orthogonal to direction 3. On the basis of this coordinate system, the following transformation matrix was applied:

$$\{\sigma\}_{12} = T\{\sigma\}_{xy}$$
$$T = \begin{bmatrix} \cos^2\theta & \sin^2\theta & 2\sin\theta\cos\theta \\ \sin^2\theta & \cos^2\theta & -2\sin\theta\cos\theta \\ -\sin\theta\cos\theta & \sin\theta\cos\theta & \cos^2\theta - \sin^2\theta \end{bmatrix} \quad (17)$$

Using this matrix transformation, the Young's modulus in tensile direction x as a function of the print orientation angle θ can be calculated by the following equation[37]:

$$\frac{1}{E_x} = \frac{\cos^4\theta}{E_{11}} + \frac{\sin^4\theta}{E_{22}} + \left(\frac{1}{G_{12}} - \frac{2\nu_{12}}{E_{11}}\right)\cos^2\theta\sin^2\theta \quad (18)$$

where E_{11} is the Young's modulus in the print direction, E_{22} is the modulus perpendicular to the print direction, G_{12} is the shear modulus and ν_{12} is Poisson's ratio. The material properties that were used for the calculations are listed in Extended Data Table 1 and were calculated from tensile tests.

Code availability. The Grasshopper files for the generation of print paths are available from the corresponding authors on reasonable request.

Data availability. The datasets generated and analysed during this study are available from the corresponding authors on reasonable request. Source Data for Figs. 2–4 and Extended Data Figs. 1–6 and 8 are provided with the online version of the paper.

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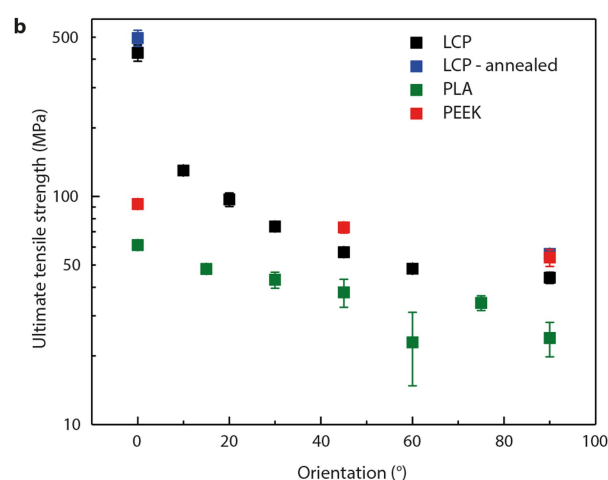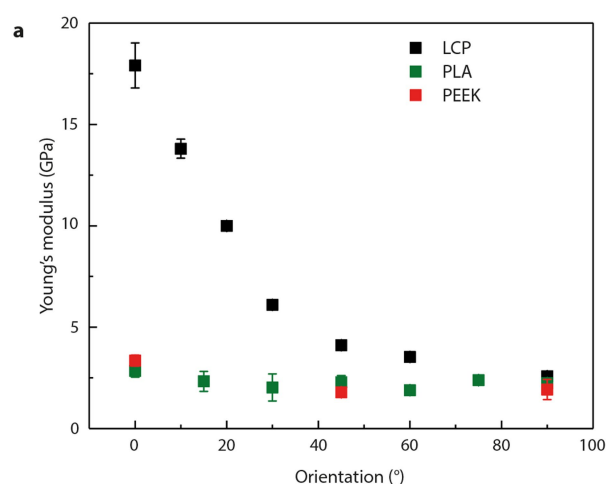
Extended Data Fig. 1 | Comparison between the mechanical properties of different FDM feedstock materials. a, Young's modulus as a function of print orientation for LCP, PLA and PEEK. **b**, Tensile strength of LCP, annealed LCP, PLA and PEEK. The strength of LCP samples is comparable to that of one of the strongest printable polymers (PEEK) at high orientation angles, and to our knowledge surpasses all other tested materials for print orientations below 20°. Error bars indicate the standard deviation for 5–10 measurements at each data point; see Source Data for details.
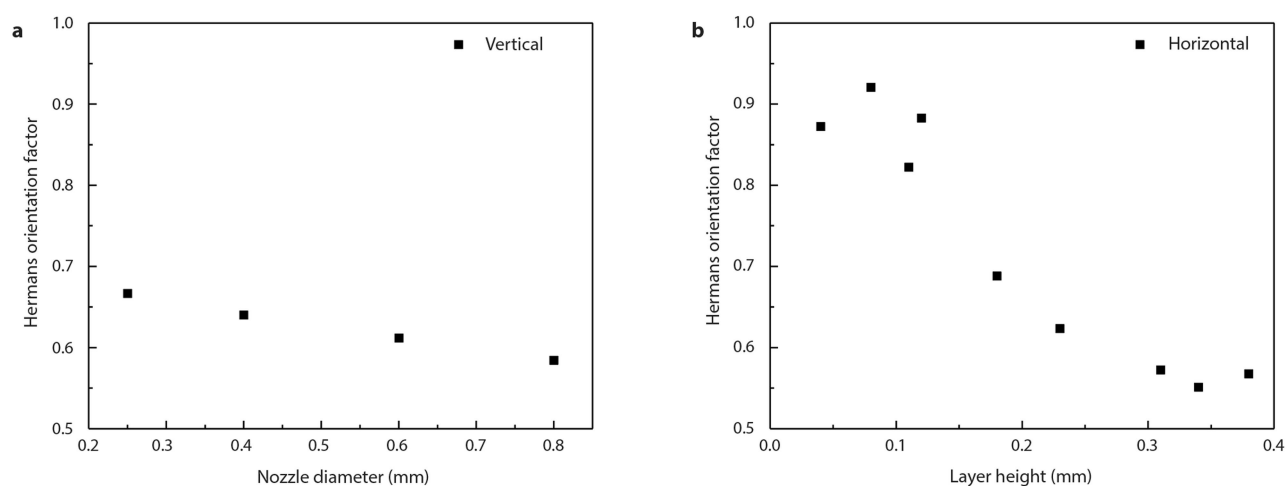
Extended Data Fig. 2 | Values of the Hermans' orientation factor for the LCPs. a, **b**, Hermans' orientation factors as a function of nozzle diameter (**a**) and layer height (**b**). Thinner samples have an increased skin-to-core material ratio and thus a higher orientation factor.
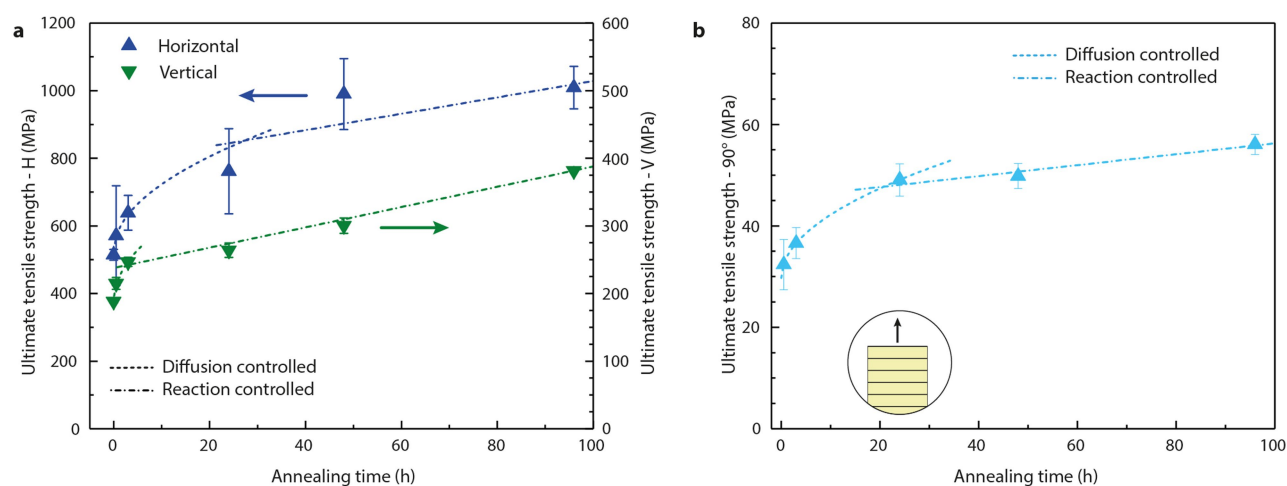
Extended Data Fig. 3 | Effect of annealing time on the ultimate strength of printed LCP filaments and parts. a, Strength (σ) as a function of annealing time (t) for single printed filaments. The experimental data suggest that the reaction is initially controlled by the diffusion of water out of the filament ($\sigma \propto t^{0.5}$) and later on by the intrinsic reaction kinetics ($\sigma \propto t$). **b**, Tensile strength as a function of annealing time for printed parts. The annealing kinetics follow the same trend as in the case of single filaments. Error bars indicate the standard deviation for 5–10 measurements at each data point; see Source Data for details.
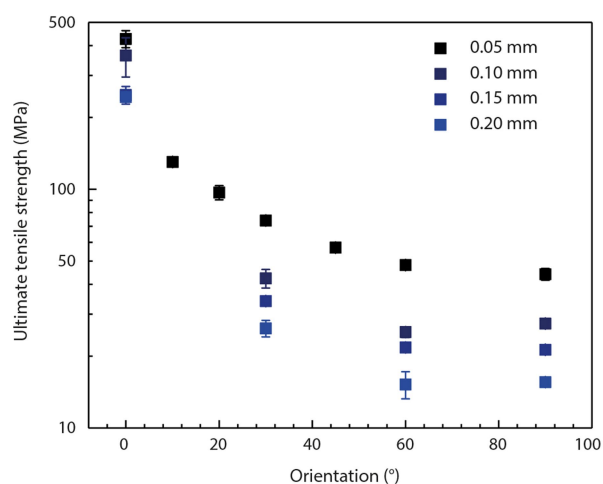
Extended Data Fig. 4 | Strength of LCP parts of different thicknesses as a function of print orientation. The observed decrease in tensile strength for increasing print orientations follows the decay in elastic modulus predicted from classical laminate theory (Fig. 3a). The lower strength at high orientation angles is also explained by a transition in failure mode from print filament fracture to interface fracture. Error bars indicate the standard deviation for 5–10 measurements at each data point; see Source Data for details.
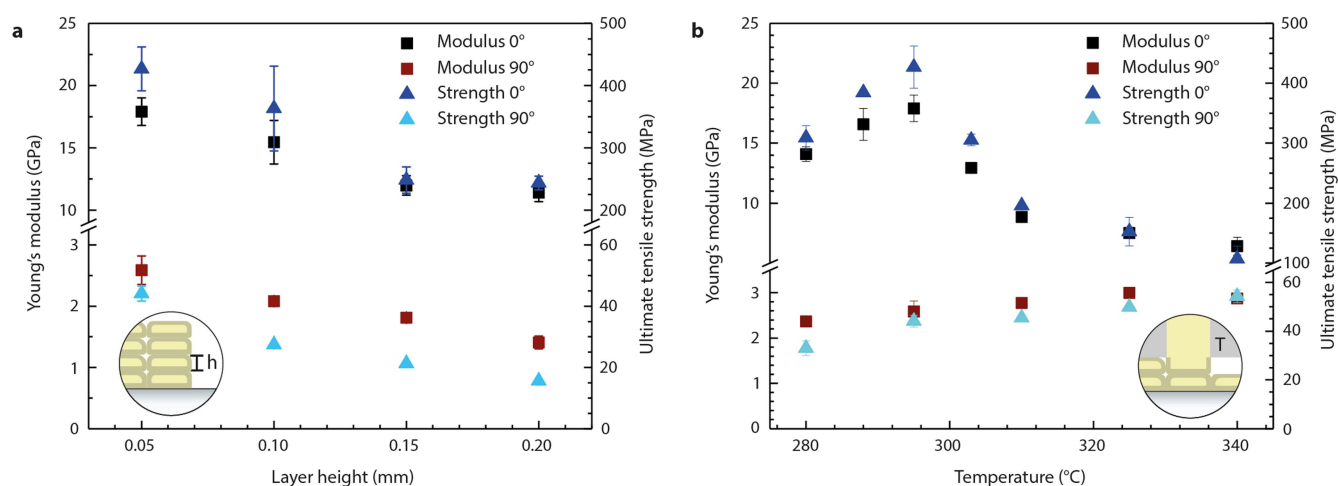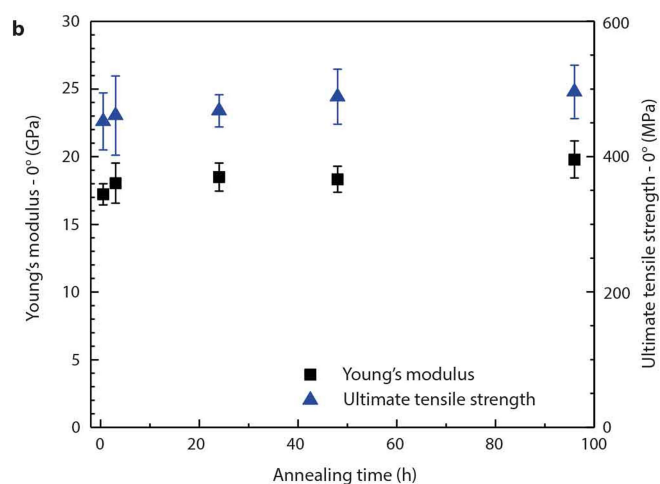
Extended Data Fig. 5 | Effect of print parameters on the Young's modulus of horizontally printed LCP parts. a, Tensile modulus and strength as a function of printed layer height. Lower layer heights lead to higher mechanical properties owing to the higher fraction of aligned skin relative to the material height. **b**, Tensile modulus and strength as a function of nozzle temperature (T_N). For temperatures higher than 300 °C, the tensile properties along the printing direction (0°) follows the behaviour observed for the Young's modulus of vertically printed filaments

(Fig. 2g). The lower values obtained for the Young's modulus and strength at $T_N < 300$ °C probably result from poorer material flow and poorer print filament adhesion at lower nozzle temperatures. The tensile properties perpendicular to the print direction (90°) increase at higher temperatures, which inidicates an improved adhesion between hot printed filaments. Error bars indicate the standard deviation for 5–10 measurements at each data point; see Source Data for details.
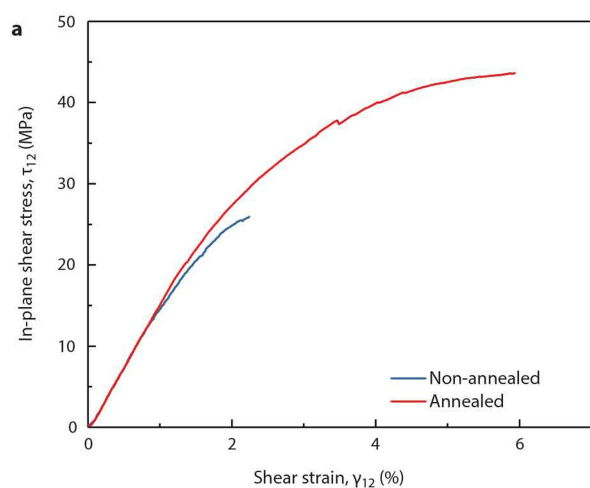
Extended Data Fig. 6 | Increased load transfer between filaments after annealing. a, Representative curve of shear stress versus strain shows that the shear strength of the LCP increases by 75% after thermal annealing for 96 h owing to the enhanced inter-filament adhesion. The shear strength data were obtained from ±45° tensile samples. **b**, The Young's modulus measured along the printing direction is found to slightly increase with longer annealing times. Error bars indicate the standard deviation for 5–10 measurements at each data point; see Source Data for details.
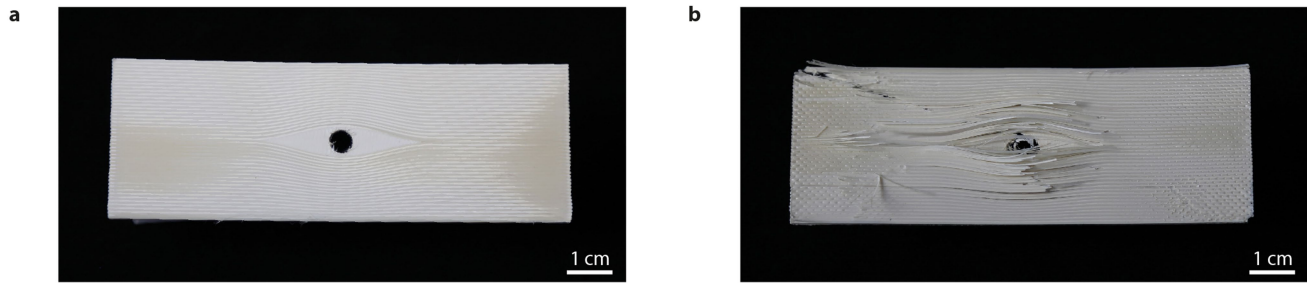
Extended Data Fig. 7 | Directional OHT sample. a, Print lines are guided around the hole, resembling a wood knot hole. The stress-shielded area next to the hole is reinforced with 90° filaments. **b**, The extensive damage to the same sample without catastrophic failure during tensile testing illustrates the high fracture toughness of the hierarchically structured architecture.

Extended Data Fig. 8 | Recyclability of printed LCP material. a, Melt flow index (MFI) of pristine pellets as well as recycled printed parts and recycled annealed printed parts (five measurements per material). The melt flow index quantifies the fluidity of the material at the indicated temperature and load. Higher indices indicate low viscosity. Non-annealed printed samples are readily recyclable owing to their high melt flow index. Although the higher molecular weight of annealed samples markedly reduces their fluidity at regular printing temperatures, this material is potentially recyclable if hydrolysis reactions are used to decrease its molecular weight and thus recover processability. Error bars indicate the standard deviation for 5 measurements at each data point; see Source Data for details. **b**, **c**, Examples of pellets (**b**) and recycled printed samples (**c**) as feedstock material.
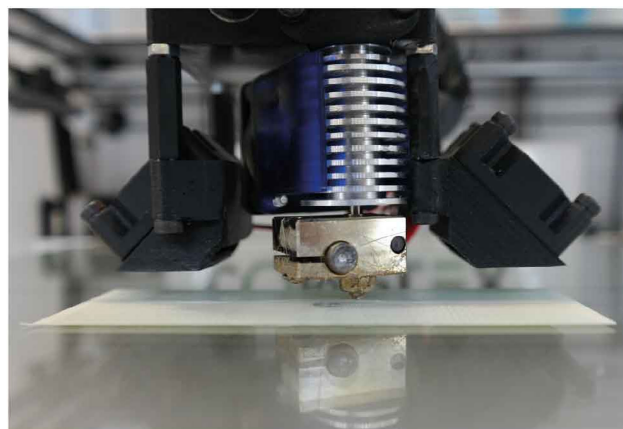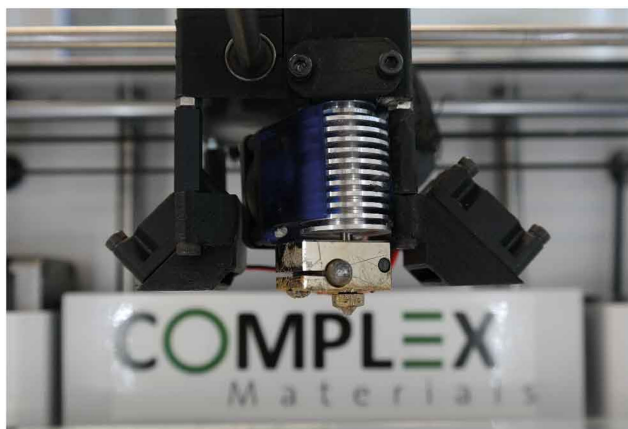
Extended Data Fig. 9 | Geared direct drive extruder with all-metal V6 hotend on an Ultimaker 2+.

Extended Data Table 1 | Classical laminate theory parameters used for print filament layer heights between 0.05 mm and 0.20 mm

Layer height (mm)	0.05	0.10	0.15	0.20
E_{11} (GPa)	17.90	15.40	11.97	11.39
E_{22} (GPa)	2.58	2.08	1.81	1.40
G_{12} (GPa)	1.70	1.30	1.10	1.00
ν_{12}	0.57	0.57	0.57	0.57