

# Lecture 14: Sensors and Actuators

Seyed-Hosein Attarzadeh-Niaki

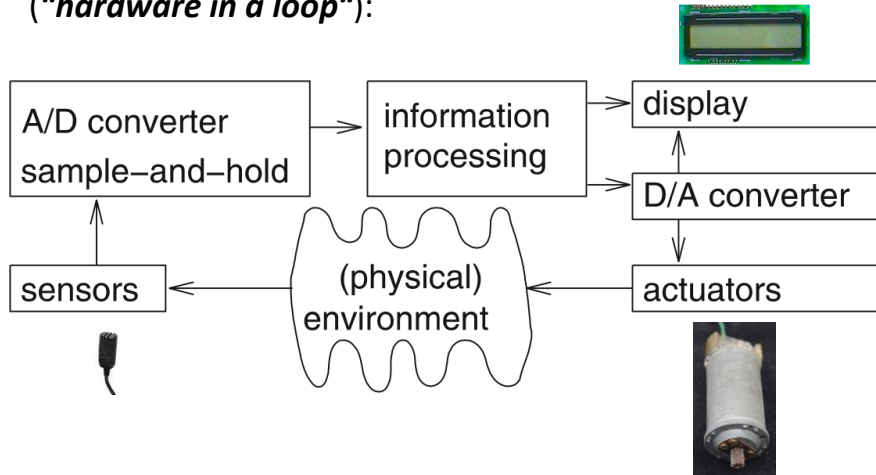
Some Slides from Edward Lee and Peter Marwedel

## Review

- IO Hardware and Mechanisms
  - Connecting Cyber and physical worlds: practical issues
  - Interrupts and concurrency
  - Modeling an interrupt controller

## CPS & ES Hardware

- CPS & ES hardware is frequently used in a loop (*“hardware in a loop”*):



Embedded Real-Time Systems

3

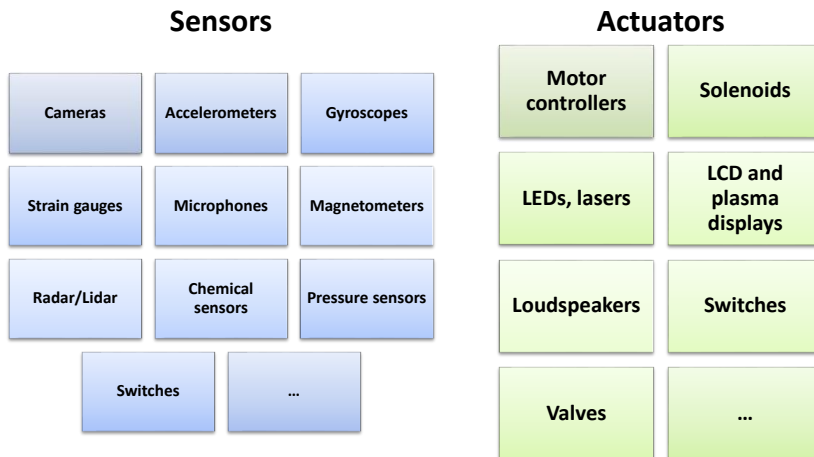
## What is A Sensor? What is An Actuator?

- A sensor is a device that **measures** a physical quantity
  - Input / “Read from physical world”
- Many physical effects used for constructing sensors
  - law of induction (generat. of voltages in a magnetic field)
  - light-electric effects
- An actuator is a device that **modifies** a physical quantity
  - Output / “Write to physical world”
- Huge variety of actuators and output devices

Embedded Real-Time Systems

4

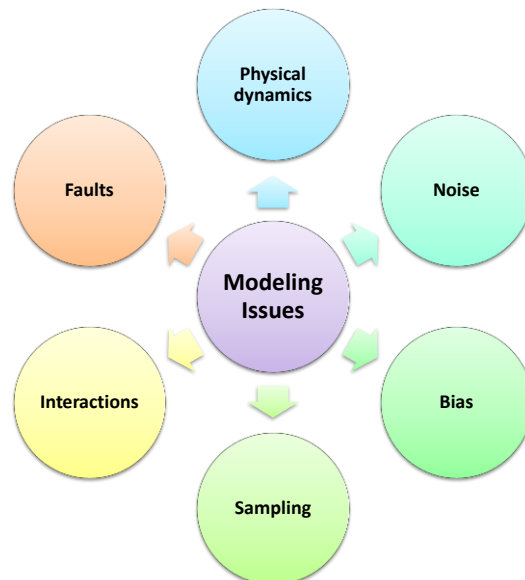
## Sensors and Actuators – The Bridge between the Cyber and the Physical



Embedded Real-Time Systems

5

## Sensors and Actuators



Embedded Real-Time Systems

6

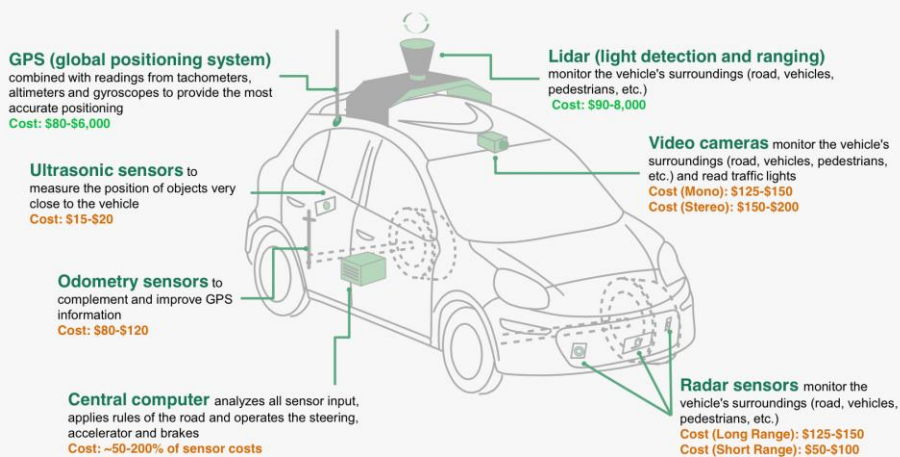
## Safe Cars

This film is for demonstrative purposes and intended to provide the viewer with a basic understanding regarding the functionality of the vehicle's safety technology Pedestrian and Cyclist detection with full Auto brake.

Embedded Real-Time Systems

7

## Sensor-Rich Cars



- Source: Wired Magazine

Embedded Real-Time Systems

8

4 00 K U  
19 mm  
x 27  
500 μm  
N-X 0.4 0.1 0.05 0.02 0.01  
— 000 —  
# 22  
I U-M I

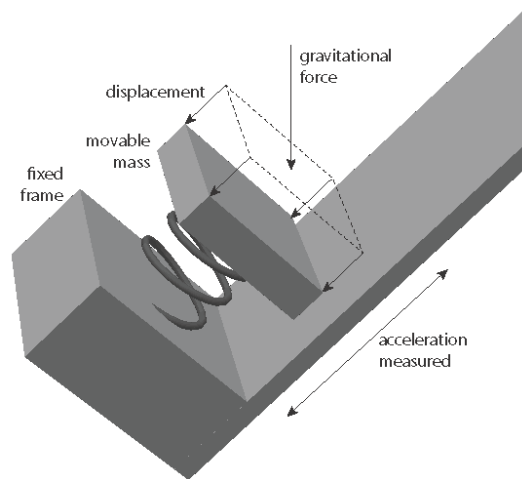
5

# Accelerometers

The most common design measures the [distance](#) between a plate fixed to the platform and one attached by a spring and damper. The measurement is typically done by measuring [capacitance](#).

## Uses:

- Navigation
- Orientation
- Drop detection
- Image stabilization
- Airbag systems



Embedded Real-Time Systems

11

## Spring-Mass-Damper Accelerometer

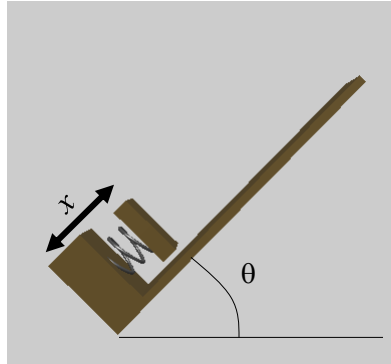
By Newton's second law,  
 $F=ma$ .

For example,  $F$  could be the Earth's gravitational force.

The force is balanced by the restoring force of the spring.



## Measuring tilt



Component of gravitational force in the direction of the accelerometer axis must equal the spring force:

$$Mg \sin(\theta) = k(p - x(t))$$

Given a measurement of  $x$ , you can solve for  $\theta$ , up to an ambiguity of  $\pi$ .

Embedded Real-Time Systems

13

## Difficulties Using Accelerometers

- Separating **tilt** from **acceleration**
- Vibration
- Nonlinearities in the spring or damper
- Integrating twice to get position: Drift

$$p(t) = p(0) + \int_0^t v(\tau) d\tau,$$

- Position is the integral of velocity, which is the integral of acceleration.
- Bias in the measurement of acceleration causes position estimate error to increase quadratically.

$$v(t) = v(0) + \int_0^t x(\tau) d\tau.$$

Embedded Real-Time Systems

14

# Inertial Navigation Systems

Combinations of:

Dead reckoning plus GPS.

- GPS (for initialization and periodic correction).
- Three axis gyroscope measures orientation.
- Three axis accelerometer, double integrated for position after correction for orientation.

Typical drift for systems used in aircraft have to be:

- 0.6 nautical miles per hour
- tenths of a degree per hour

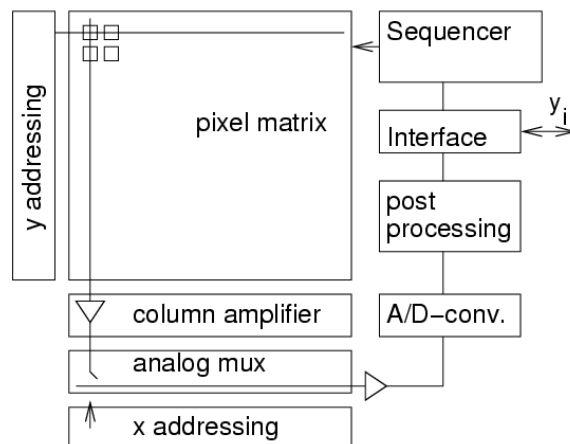
Good enough? It depends on the application!

Embedded Real-Time Systems

15

## Example: CMOS image sensors

Based on standard production process for CMOS chips, allows integration with other components.





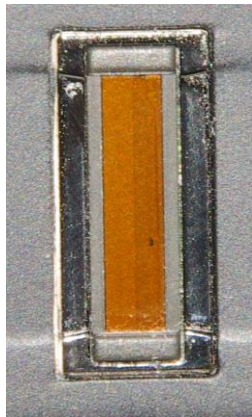
## Comparison CCD/CMOS sensors

Property	CCD	CMOS
<b>Technology optimized for</b>	Optics	VLSI technology
<b>Technology</b>	Special	Standard
<b>Smart sensors</b>	No, no logic on chip	Logic elements on chip
<b>Access</b>	Serial	Random
<b>Size</b>	Limited	Can be large
<b>Power consumption</b>	Low	Larger
<b>Video mode</b>	Possibly too slow	ok
<b>Applications</b>	Situation is changing over the years	

See also B. Diericks: CMOS image sensor concepts.  
Photonics West 2000 Short course (Web)

## Example: Biometrical Sensors

e.g.: Fingerprint sensor

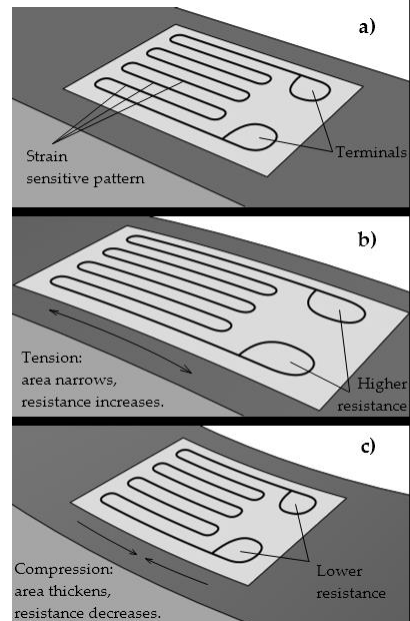


© P. Marwedel, 2010

# Strain Gauges



Mechanical strain gauge used to measure the growth of a crack in a masonry foundation. This one is installed on the Hudson-Athens Lighthouse. Photo by Roy Smith, used with permission.

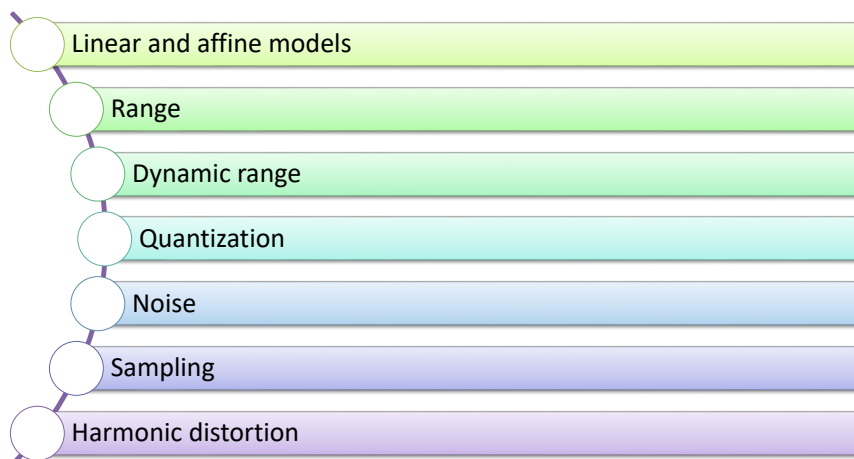


Images from the Wikipedia Commons

Embedded Real-Time Systems

19

## Models of Sensors and Actuators



Embedded Real-Time Systems

20

## Sensor Calibration (Same for Actuators)

- Assume a physical quantity  $x(t)$  is reported by the sensor to have value  $f(x(t))$
- $f$  is **linear** if there exists a proportionality constant  $a \in \mathbb{R}$  such that

$$f(x(t)) = ax(t)$$

- $f$  is **affine** if there exists a proportionality constant  $a \in \mathbb{R}$  and a bias  $b \in \mathbb{R}$  such that

$$f(x(t)) = \underbrace{a}_{\text{Sensitivity}} x(t) + \underbrace{b}_{\text{Bias}}$$

## Range and Dynamic Range

- Sensors/actuators normally have an **operating range**  $(L, H)$ 
  - Outside of that they will saturate
- An affine function model is augmented:
- The **precision**  $p$  of a digital sensor: smallest absolute difference between two values of a physical quantity whose sensor readings are distinguishable.
- Dynamic range:

$$f(x(t)) = \begin{cases} ax(t) + b & \text{if } L \leq x(t) \leq H \\ aH + b & \text{if } x(t) > H \\ aL + b & \text{if } x(t) < L, \end{cases}$$

$$D = \frac{H - L}{p}$$

In decibels:

$$D_{dB} = 20 \log_{10} \left( \frac{H - L}{p} \right)$$

Example: Look at ADXL330 accelerometer datasheet

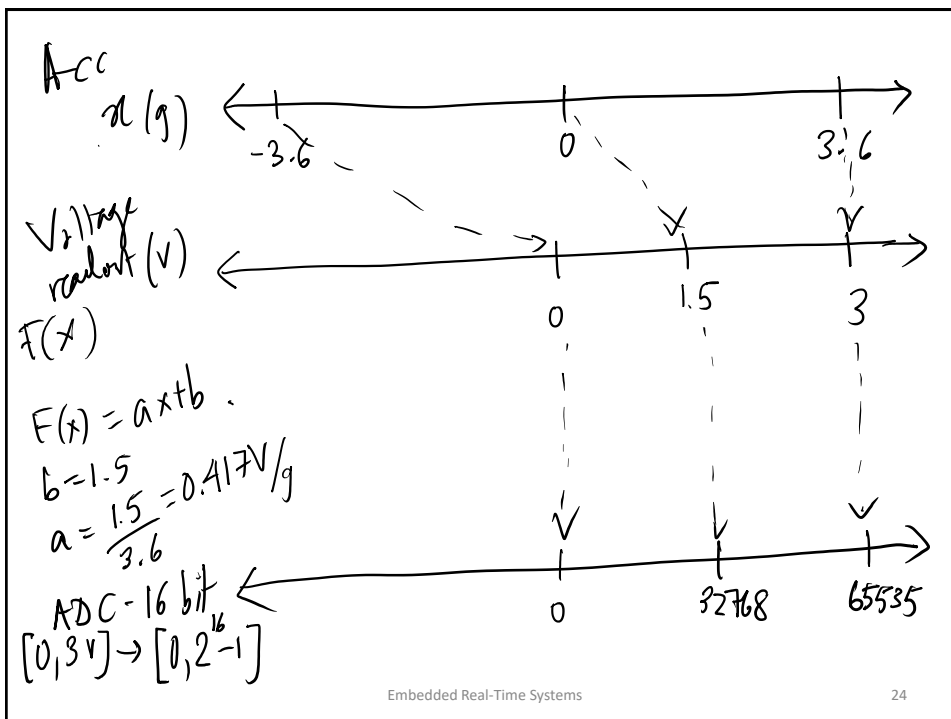
# Analog Devices ADXL330 Data Sheet

## SPECIFICATIONS

$T_A = 25^\circ\text{C}$ ,  $V_S = 3\text{ V}$ ,  $C_X = C_Y = C_Z = 0.1\text{ }\mu\text{F}$ , acceleration = 0 g, unless otherwise noted. All minimum and maximum specifications are guaranteed. Typical specifications are not guaranteed.

Table 1.

Parameter	Conditions	Min	Typ	Max	Unit
<b>SENSOR INPUT</b>					
Measurement Range	Each axis	$\pm 3$	$\pm 3.6$		g
Nonlinearity	% of full scale		$\pm 0.3$		%
Package Alignment Error			$\pm 1$		Degrees
Inter-Axis Alignment Error			$\pm 0.1$		Degrees
Cross Axis Sensitivity <sup>1</sup>			$\pm 1$		%
<b>SENSITIVITY (RATIOMETRIC)<sup>2</sup></b>					
Sensitivity at $X_{OUT}$ , $Y_{OUT}$ , $Z_{OUT}$	Each axis $V_S = 3\text{ V}$	270	300	330	mV/g
Sensitivity Change Due to Temperature <sup>3</sup>	$V_S = 3\text{ V}$		$\pm 0.015$		%/ $^\circ\text{C}$
<b>ZERO g BIAS LEVEL (RATIOMETRIC)</b>					
0 g Voltage at $X_{OUT}$ , $Y_{OUT}$ , $Z_{OUT}$	Each axis $V_S = 3\text{ V}$	1.2	1.5	1.8	V
0 g Offset vs. Temperature			$\pm 1$		mg/ $^\circ\text{C}$
<b>NOISE PERFORMANCE</b>					
Noise Density $X_{OUT}$ , $Y_{OUT}$			280		$\mu\text{g}/\sqrt{\text{Hz}}$ rms
Noise Density $Z_{OUT}$			350		$\mu\text{g}/\sqrt{\text{Hz}}$ rms
<b>FREQUENCY RESPONSE<sup>4</sup></b>					
Bandwidth $X_{OUT}$ , $Y_{OUT}$ <sup>5</sup>	No external filter		1600		Hz
Bandwidth $Z_{OUT}$ <sup>5</sup>	No external filter		550		Hz
$R_{FLT}$ Tolerance			$32 \pm 15\%$		k $\Omega$
Sensor Resonant Frequency			5.5		kHz



# Quantization

- An  $n$ -bit digital sensor picks one of  $2^n$  values for a physical quantity.

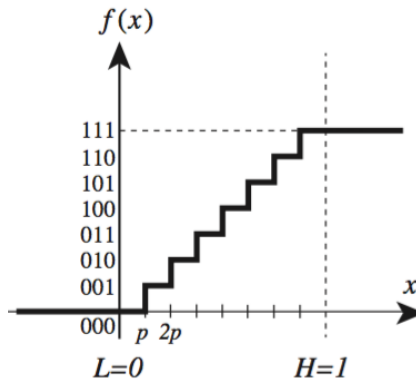
- Precision:

$$p = (H - L) / 2^n$$

- Dynamic range:

$$D_{dB} = 20 \log_{10} \left( \frac{H - L}{p} \right) = 20 \log_{10}(2^n) \\ = 20n \log_{10}(2) \approx 6n \text{ dB}$$

- 6 decibels of dynamic range per bit



f: sensor distortion function

Embedded Real-Time Systems

25

# Noise

- Undesired part of the signal

$$f(x(t)) = x(t) + n(t)$$

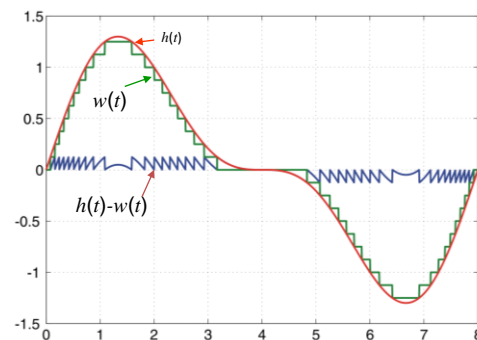
- Root mean square (RMS) of the noise

$$N = \lim_{T \rightarrow \infty} \sqrt{\frac{1}{2T} \int_{-T}^T (n(\tau))^2 d\tau}$$

- Signal to noise ratio (SNR, in decibels)

$$SNR_{dB} = 20 \log_{10} \left( \frac{X}{N} \right)$$

- Quantization noise:



Embedded Real-Time Systems

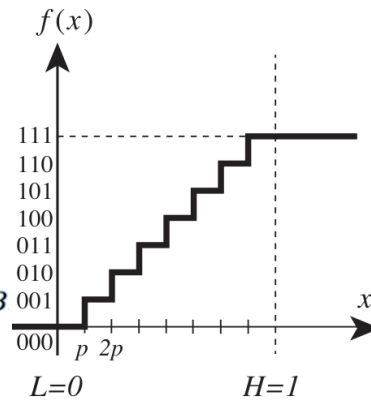
26

## Example: Quantization Noise of a 3-bit Digital Sensor

$$X = \sqrt{\int_0^1 x^2 dx} = \frac{1}{\sqrt{3}}$$

$$N = \sqrt{\int_{-1/8}^0 8n^2 dn} = \sqrt{\frac{1}{3 \cdot 64}} = \frac{1}{8\sqrt{3}}$$

$$SNR_{dB} = 20 \log_{10} \left( \frac{X}{N} \right) = 20 \log_{10} (8) \approx 18dB$$



Embedded Real-Time Systems

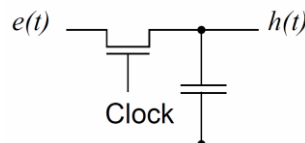
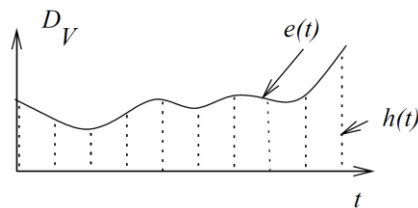
27

## Sampling

- Discretizing a continuous-time physical quantity
- For **uniform** signal sampling with sampling interval  $T$

$$\forall n \in \mathbb{Z}, s(n) = f(x(nT))$$

What is a good  $T$ ?

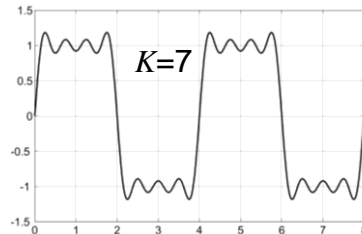
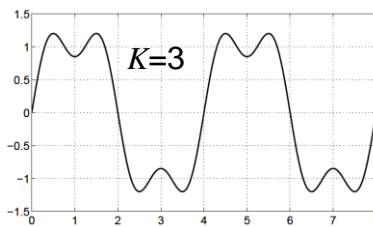
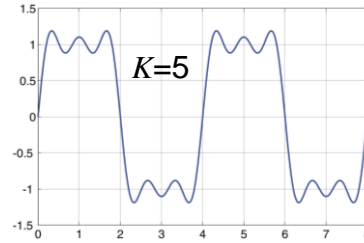
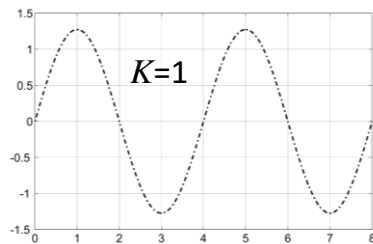


Embedded Real-Time Systems

28

## Approximation of a Square Wave

$$e'_K(t) = \sum_{k=1,3,5,\dots}^K \frac{4}{\pi k} \sin\left(\frac{2\pi t}{p_k}\right) \quad \text{with } \forall k: p_k = p_1/k, p_1=4$$

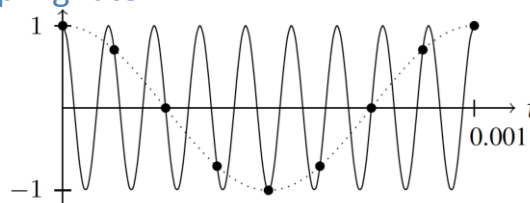


Embedded Real-Time Systems

29

## Aliasing

- A high frequency sinusoid sampled at a low rate looks just like a low frequency sinusoid
- Nyquist criterion (sampling theory)
  - Aliasing can be avoided if we **restrict the frequencies of the incoming signal to less than half of the sampling rate.**



Embedded Real-Time Systems

30

# Aliasing in Computer Graphics

Sub-sampled, no filtering



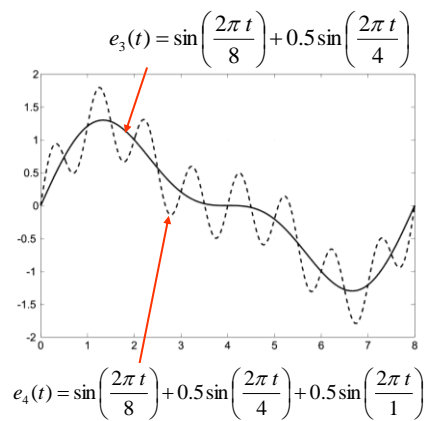
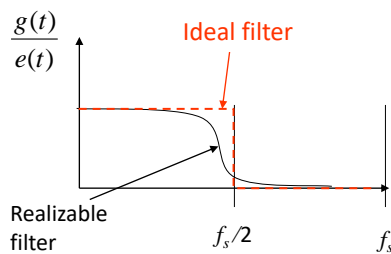
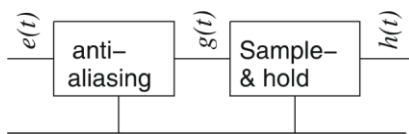
Embedded Real-Time Systems

[http://en.wikipedia.org/wiki/Image:Moiré\\_pattern\\_of\\_bricks\\_small.jpg](http://en.wikipedia.org/wiki/Image:Moiré_pattern_of_bricks_small.jpg)

31

## Anti-Aliasing Filter

- A filter is needed to remove high frequencies



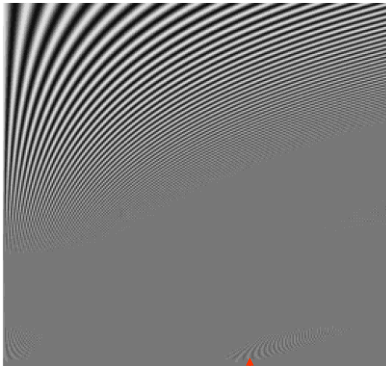
Embedded Real-Time Systems

32



# Aliasing in Computer Graphics

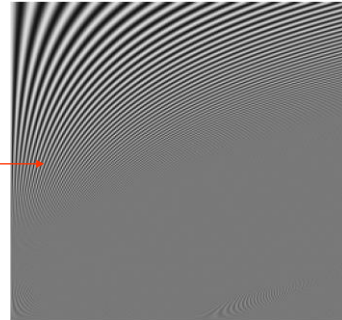
- Original (pdf screen copy)



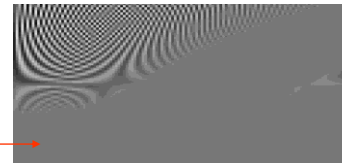
<http://www.niirs10.com/Resources/Reference Documents/Accuracy in Digital Image Processing.pdf>

Impact of rasterization

Filtered & sub-sampled



Sub-sampled, no filtering



## Harmonic Distortion

- A form of **nonlinearity** that occurs even within the operating range of sensors and actuators
    - sensitivity is not constant and depends on the magnitude of the signal
  - Modeled by **powers of the physical quantity**
    - Second harmonic distortion is a dependence on the square of the physical quantity
- $$f(x(t)) = ax(t) + b + d_2(x(t))^2$$
- The importance of harmonic distortion *depends on the application*

## Signal Conditioning

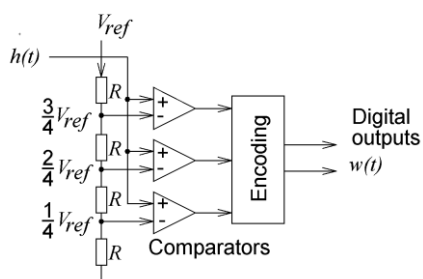
- Use **frequency selective filtering** to remove noise and harmonic distortion
- Relies on Fourier theory to filter-out undesired frequencies
- Example: An accelerometer measures orientation plus vibration of a slowly-rotating object
  - Solution: Filter-out high-frequency vibration

Embedded Real-Time Systems

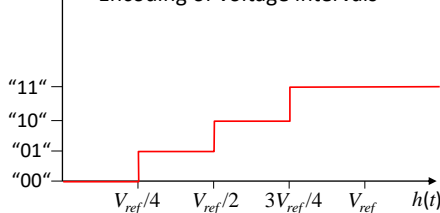
35

## A/D Converters

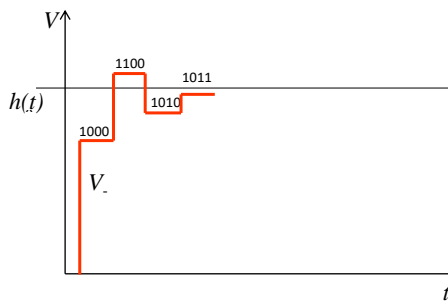
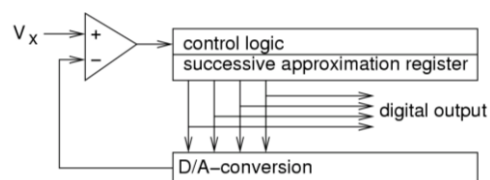
### Flash



Encoding of voltage intervals



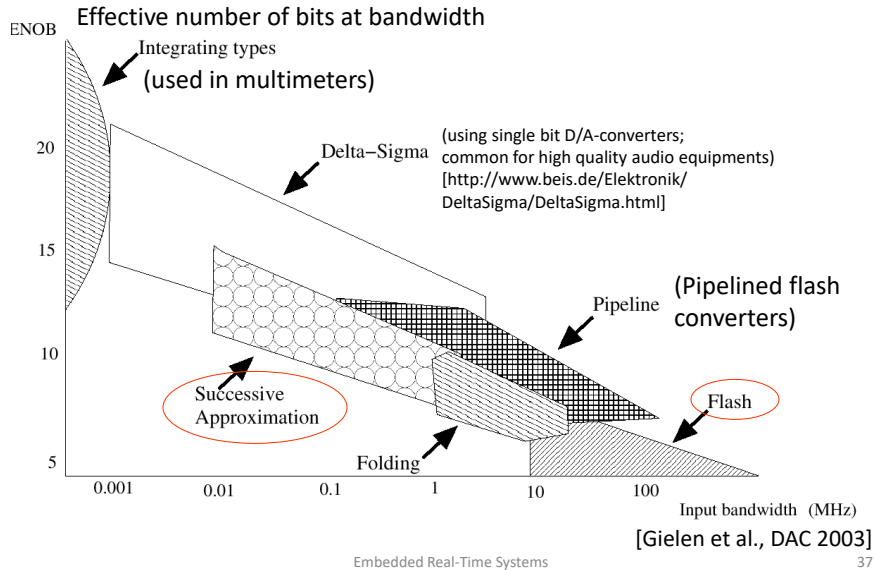
### Successive Approximation



Embedded Real-Time Systems

36

## Application Areas for Different A/D Converters



## Design Issues with Sensors

### Calibration

- Relating measurements to the physical phenomenon
- Can dramatically increase manufacturing costs

### Nonlinearity

- Measurements may not be proportional to physical phenomenon
- Correction may be required
- Feedback can be used to keep operating point in the linear region

### Sampling

- Aliasing
- Missed events

### Noise

- Analog signal conditioning
- Digital filtering
- Introduces latency

### Failures

- Redundancy (sensor fusion problem)
- Attacks (e.g. Stuxnet attack)

Embedded Real-Time Systems

38

## Next Lecture

- Examples of Sensors
- Read chapter 3 of Pan & Zhu