

Lecture 19: Real-Time Scheduling II

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Based on the Slides by Edward Lee and Rodolfo Pellizzoni

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Review

- Simple RTOS: Microkernel scheduler
- Task model and periodicity
- Preemptive scheduling
- Rate monotonic scheduling
 - Feasibility
 - Optimality

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Outline

- Earliest Due Date (EDD) and Earliest Deadline First (EDF) scheduling
 - Optimality
- Precedence Constraints
 - Latest Deadline First (LDF) scheduling
 - EDF* scheduling

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Deadline Driven Scheduling: Jackson's Algorithm: EDD (1955)

Given n independent *one-time tasks* with deadlines d_1, \dots, d_n , schedule them to minimize the maximum *lateness*, defined as

$$L_{\max} = \max_{1 \leq i \leq n} \{f_i - d_i\}$$

where f_i is the finishing time of task i . Note that this is negative iff all deadlines are met.

Earliest Due Date (EDD) algorithm: Execute them in order of non-decreasing deadlines.

Note that this does not require preemption.

Theorem: EDD is Optimal in the Sense of Minimizing Maximum Lateness

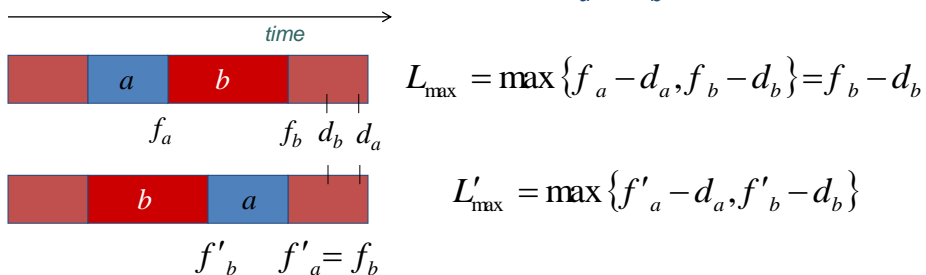
- To prove, use an interchange argument:
 - Given a schedule S that is not EDD, there must be tasks a and b where
 - a immediately precedes b in the schedule but
 - $d_a > d_b$.
 - Why?
- We can prove that this schedule can be improved by interchanging a and b .
 - Thus, no non-EDD schedule achieves smaller max lateness than EDD,
 - so the EDD schedule must be optimal.

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Consider a non-EDD Schedule S

There must be tasks a and b where a immediately precedes b in the schedule but $d_a > d_b$



Theorem: $L'_{\max} \leq L_{\max}$.

Hence, S' is no worse than S .

Case 1: $f'_a - d_a > f'_b - d_b$. ($L'_{\max} = f'_a - d_a$)
 Then: $L'_{\max} \leq f'_a - d_a = f_b - d_a \leq L_{\max}$
 (because: $d_a > d_b$).

Case 2: $f'_a - d_a \leq f'_b - d_b$. ($L'_{\max} = f'_b - d_b$)
 Then: $L'_{\max} \leq f'_b - d_b \leq L_{\max}$
 (because: $f'_b < f_b$).

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Deadline Driven Scheduling: Horn's algorithm: EDF (1974)

- Extend EDD by allowing tasks to “arrive” (become ready) at any time.
- Earliest deadline first (EDF)
 - Given a set of n independent tasks with arbitrary arrival times,
 - any algorithm that at any instant executes the task with the earliest absolute deadline among all arrived tasks
 - is optimal w.r.t. minimizing the maximum lateness.
- Proof uses a similar interchange argument.

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Using EDF for Periodic Tasks

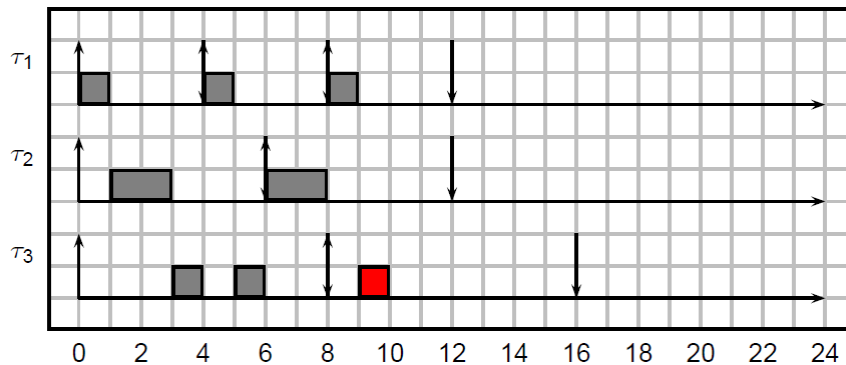
- The EDF algorithm can be applied to periodic tasks as well as aperiodic tasks.
 - Simplest use: Deadline is the *end of the period*.
 - Alternative use: *Separately specify* deadline (relative to the period start time) and period.

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A Comparative Example

- τ_1 ($e_1 = 1, p_1 = 4$), τ_2 ($e_2 = 2, p_1 = 6$), τ_3 ($e_3 = 3, p_3 = 8$)
- Utilization: $U = 1/4 + 2/6 + 3/8 = 23/24$
- RM: don't know (utilization bound), in reality: not schedulable

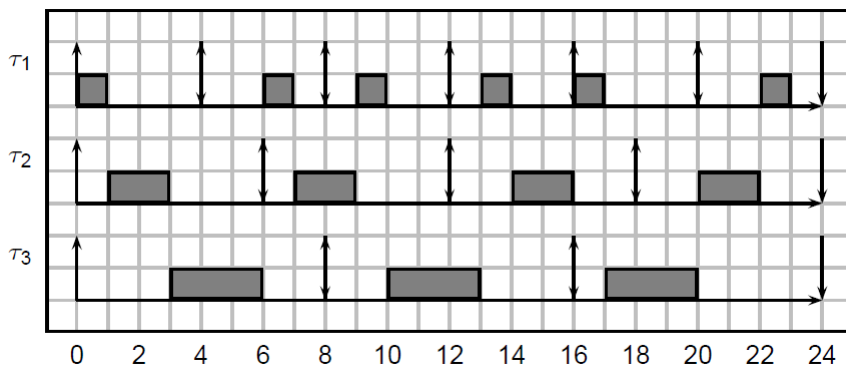


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A Comparative Example

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- Utilization: $U = 1/4 + 2/6 + 3/8 = 23/24$
- EDF: schedulable



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RMS vs. EDF?

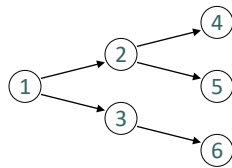
Which one is better?

- Favoring RMS
 - Scheduling decisions are simpler
 - fixed priorities vs. the dynamic priorities required by EDF.
 - EDF scheduler must maintain a list of ready tasks that is sorted by priority.
- Favoring EDF
 - Since EDF is optimal w.r.t. maximum lateness, it is also optimal w.r.t. feasibility.
 - RMS is only optimal w.r.t. feasibility.
 - For infeasible schedules, RMS completely blocks lower priority tasks, resulting in unbounded maximum lateness.
 - EDF can achieve full utilization where RMS fails to do that
 - EDF results in fewer preemptions in practice, and hence less overhead for context switching.
 - Deadlines can be different from the period.

The Simplest Model

- So far we looked at the *simplest possible model*, where
 - All tasks are periodic
 - Single processor
 - Tasks do not share any resource
- Not very realistic, but instructive (we have simple results)!
- Questions happening in reality:
 - What if there are task interdependencies?
 - What happens when you start sharing resources?
 - What happens if you schedule a mix of periodic/apperiodic tasks?
 - What happens if you use a multiprocessor?
 - More complex task models?
- We briefly look at some of these issues.

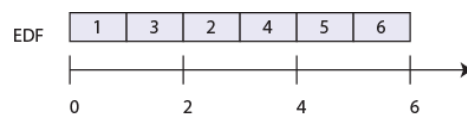
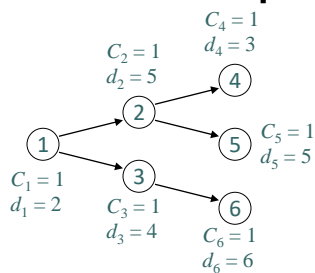
Precedence Constraints



DAG, showing that task 1 must complete before tasks 2 and 3 can be started, etc.

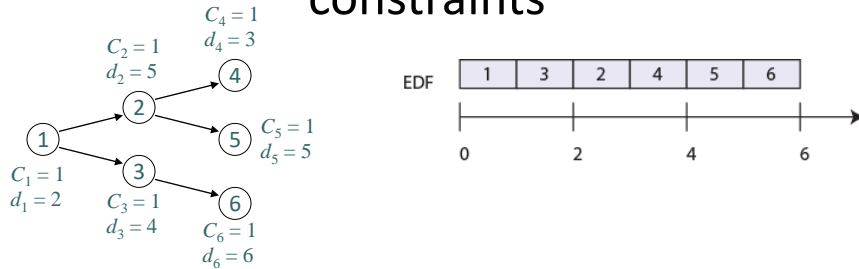
A **directed acyclic graph (DAG)** shows precedences, which indicate which tasks must complete before other tasks start.

Example: EDF Schedule



Is this feasible?

EDF is not optimal under precedence constraints



- The EDF schedule chooses task 3 at time 1 because it has an earlier deadline.
- This choice results in task 4 missing its deadline.

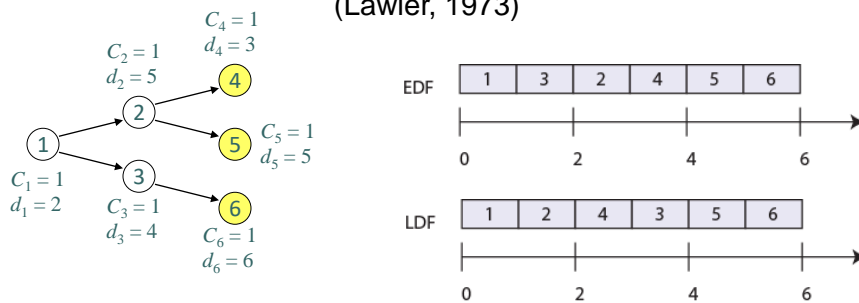
Is there a feasible schedule?

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Latest Deadline First (LDF)

(Lawler, 1973)



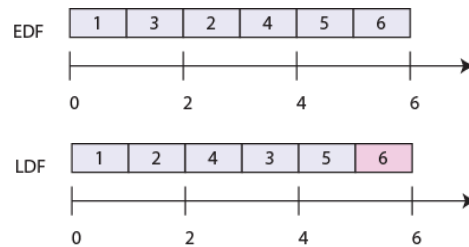
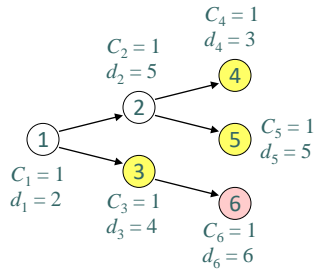
- The LDF scheduling strategy builds a schedule backwards.
- Given a DAG,
 - choose the leaf node with the latest deadline to be scheduled last,
 - and work backwards.

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Latest Deadline First (LDF)

(Lawler, 1973)



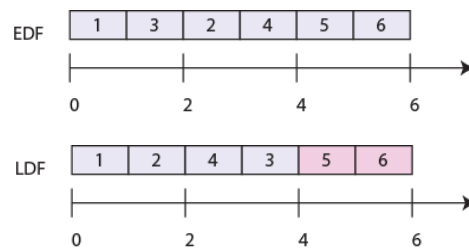
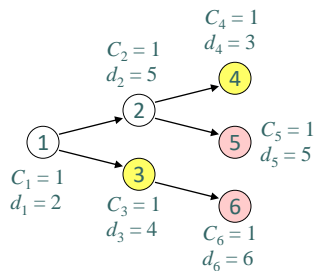
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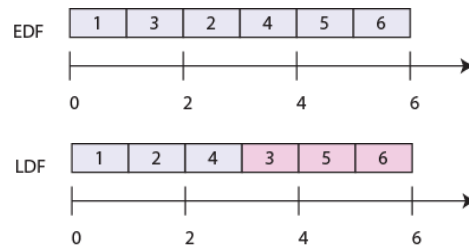
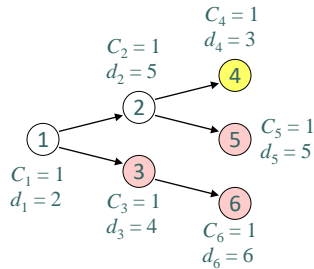
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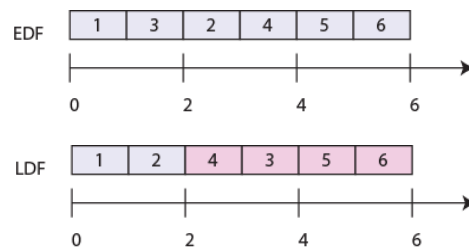
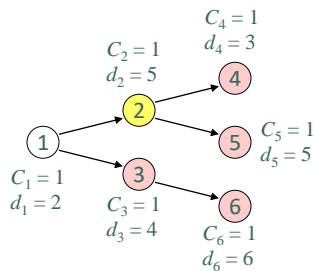
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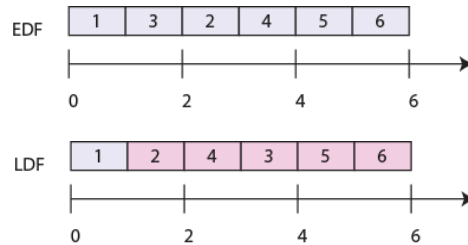
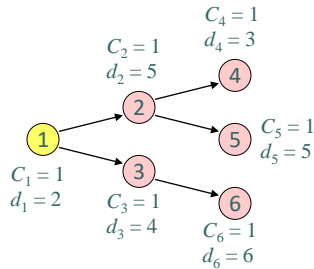
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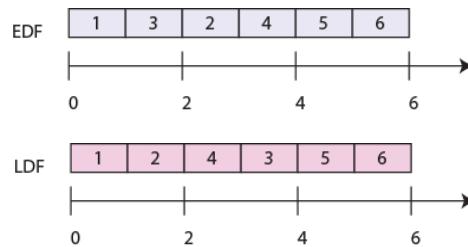
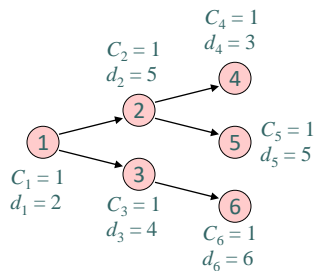
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(Lawler, 1973)

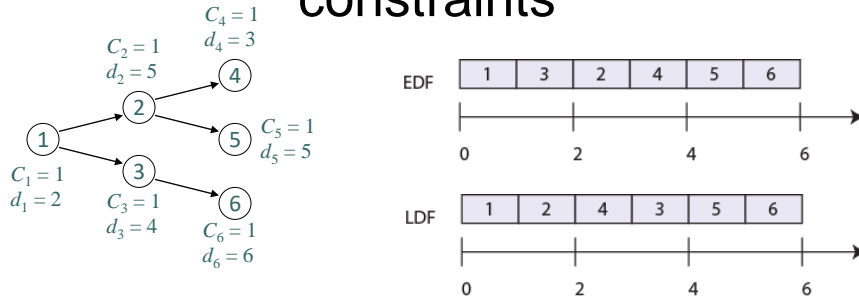


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LDF is optimal under precedence constraints



- The LDF schedule shown at the bottom respects all precedences and meets all deadlines.

✓ Also **minimizes maximum lateness**

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Latest Deadline First (LDF)

(Lawler, 1973)

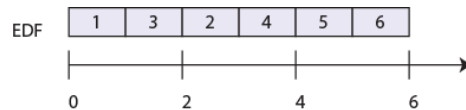
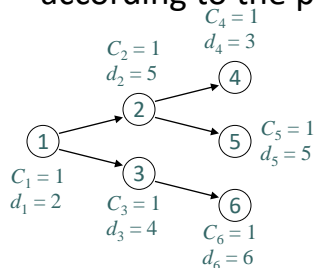
- LDF is optimal in the sense that it **minimizes the maximum lateness**.
- It does **not require preemption**.
 - We'll see that EDF can be made to work with preemption.
- However, it **requires** that
 - all tasks be *available* and
 - their *precedences known* before any task is executed.

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EDF with Precedences (EDF*)

- With a **preemptive scheduler**, EDF can be modified to
 - account for precedences and
 - allow tasks to arrive at arbitrary times.
- Simply *adjust the deadlines and arrival times* according to the precedences.



Recall that for the tasks at the left, EDF yields the schedule above, where task 4 misses its deadline.

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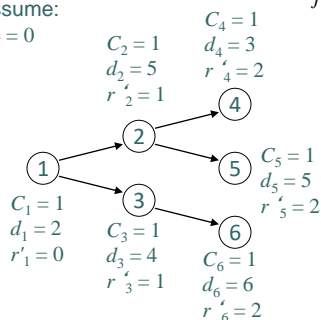
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EDF with Precedences Modifying release times

Given n tasks with precedences and release times r_i , if task i immediately precedes task j , then modify the release times as follows:

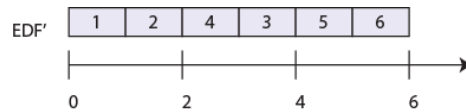
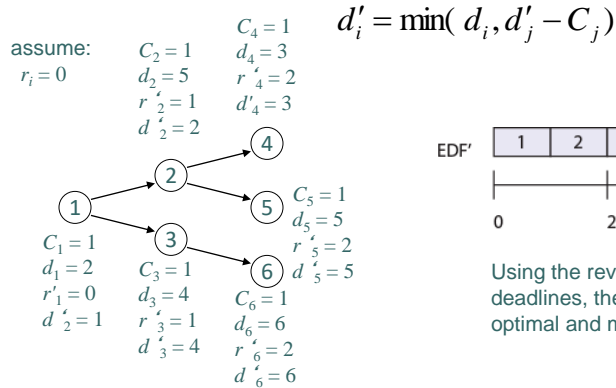
$$r'_j = \max(r_j, r_i + C_i)$$

assume:
 $r_i = 0$



EDF with Precedences Modifying deadlines

Given n tasks with precedences and deadlines d_i , if task i immediately precedes task j , then modify the deadlines as follows:



Using the revised release times and deadlines, the above EDF schedule is optimal and meets all deadlines.

EDF* Optimality

EDF with precedences is **optimal** in the sense of **minimizing the maximum lateness**.