

# Triangulation

## Fisk's Proof - Triangulation

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# Diagonals

❖ S. Fisk gave a **short proof** of AGT in 1978

❖ For any vertices  $x$  and  $y$  of  $P$  a polygon,

the line segment  $xy$  is

called an **internal diagonal** if

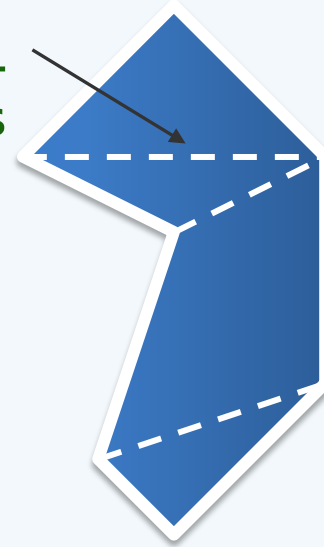
$$xy \setminus \{x, y\} \subset P \setminus \partial P$$

❖ Note that

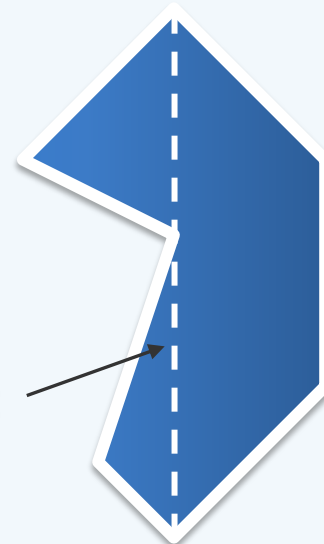
neither any edge nor any tangent

is a diagonal

internal  
diagonals

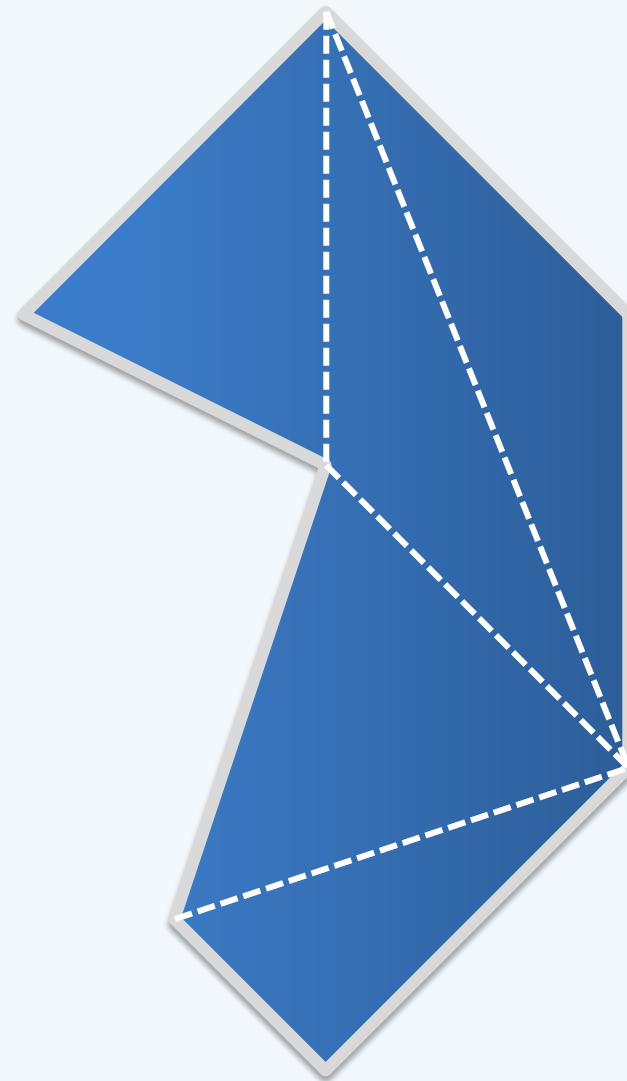


tangent



# Triangulation

- ❖ A set of diagonals  
are called **consistent** if  
no two intersect in their interior
- ❖ A **maximal** consistent diagonal set of  $P$ ,  
 $\text{Tri}(P)$ ,  
is called a **triangulation** of  $P$



## Coloring

❖ The **k-coloring** of  $\text{Tri}(P)$  is a mapping

$$C(k) : \{ \text{vertices of } P \} \rightarrow \{ 1, \dots, k \}$$

s.t. for any vertices  $p$  and  $q$ ,

$$C(k)(p) = C(k)(q) \quad \text{only if } pq \text{ is}$$

neither an **edge** of  $P$

nor a **diagonal** in  $\text{Tri}(P)$

