

# Triangulation

Monotone Decomposition

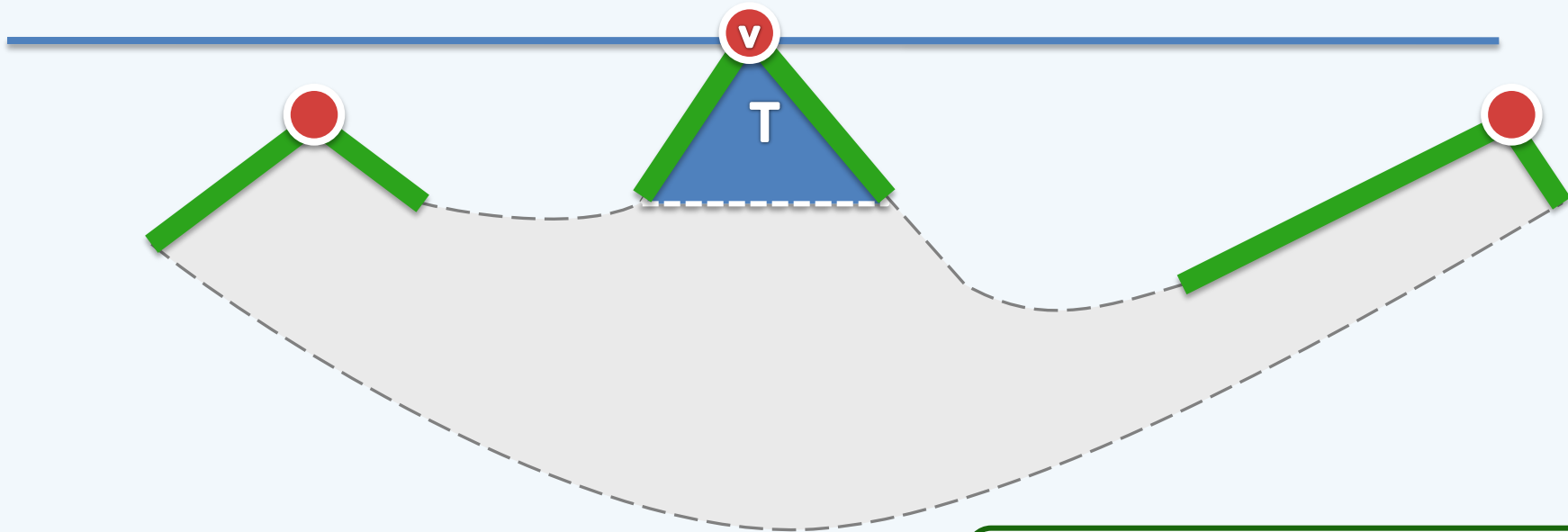
- Possible Cases

Junhui DENG

deng@tsinghua.edu.cn

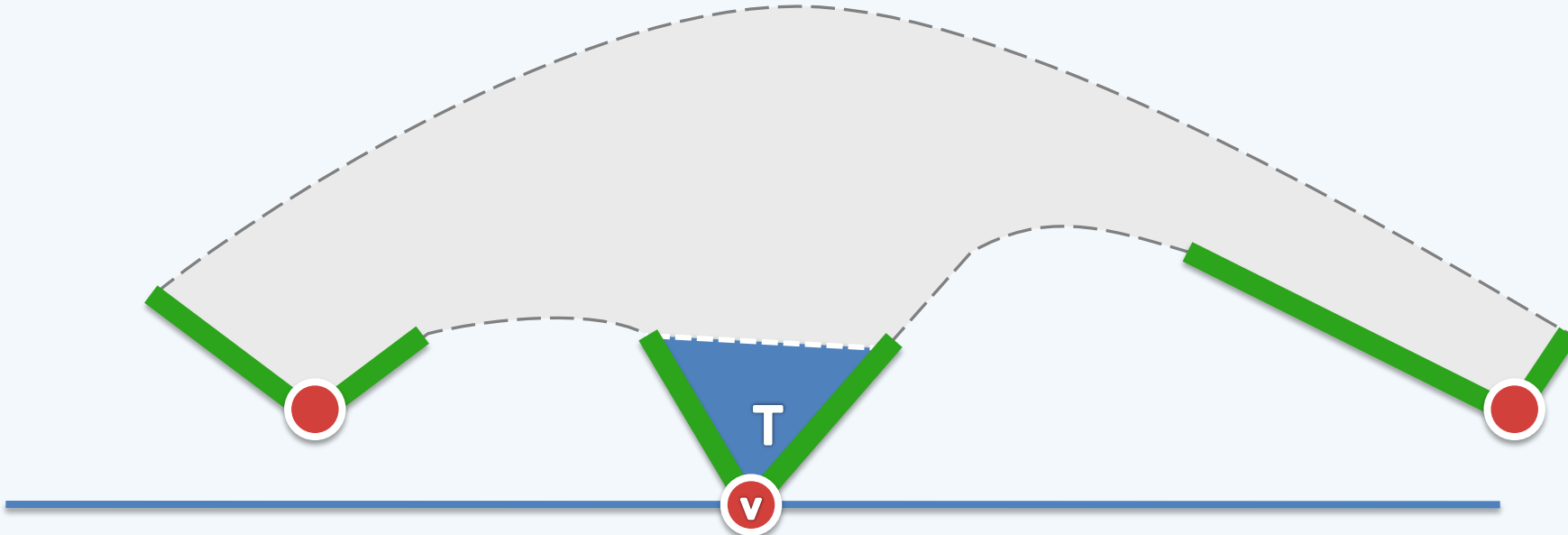
## 1: Start Vertex

- ❖ A start vertex (event)
  - has 2 edges incident from below and
  - defines a convex internal angle
- ❖ At a start vertex  $v$ ,
  - **insert** a new trapezoid  $T$  to  $\mathcal{S}$
  - let  $\text{helper}(T) = \mathbf{v}$



## 2: End Vertex

- ❖ An end vertex (event)
  - has 2 edges incident from above and
  - defines a convex internal angle
- ❖ At an end vertex  $v$ ,
  - find the trapezoid  $T$  supported by  $v$
  - remove  $T$  from  $S$



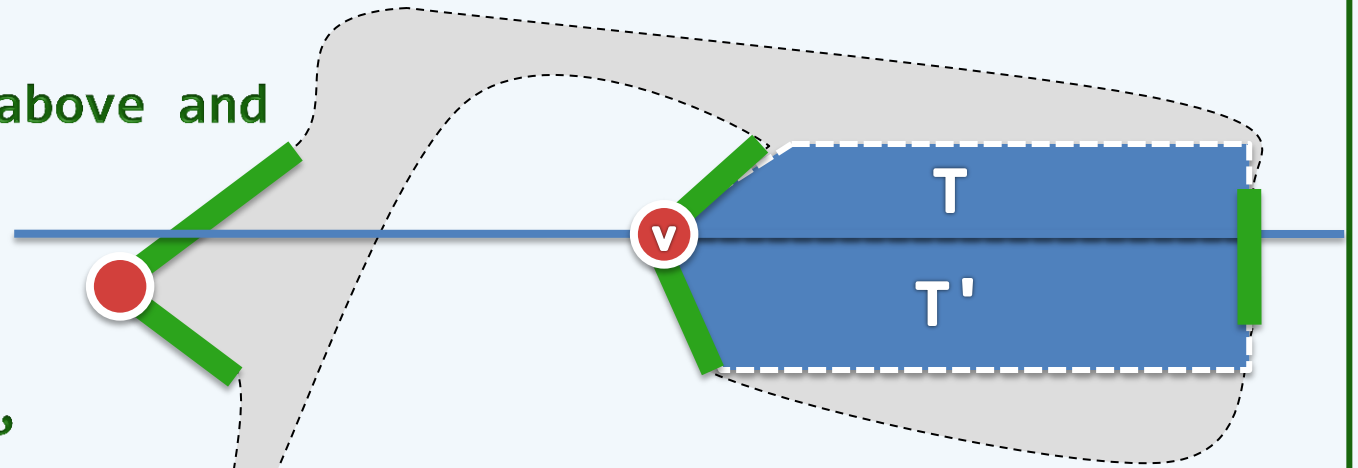
### 3: Left Adjacency

❖ A left adjacency vertex (event) has

- a left edge incident from above and
- another one from below

❖ At a left adjacency vertex  $v$ ,

- find the trapezoid  $T$  supported by  $v$
- replace  $T$  with  $T'$  in  $\mathcal{S}$
- let  $\text{helper}(T') = v$



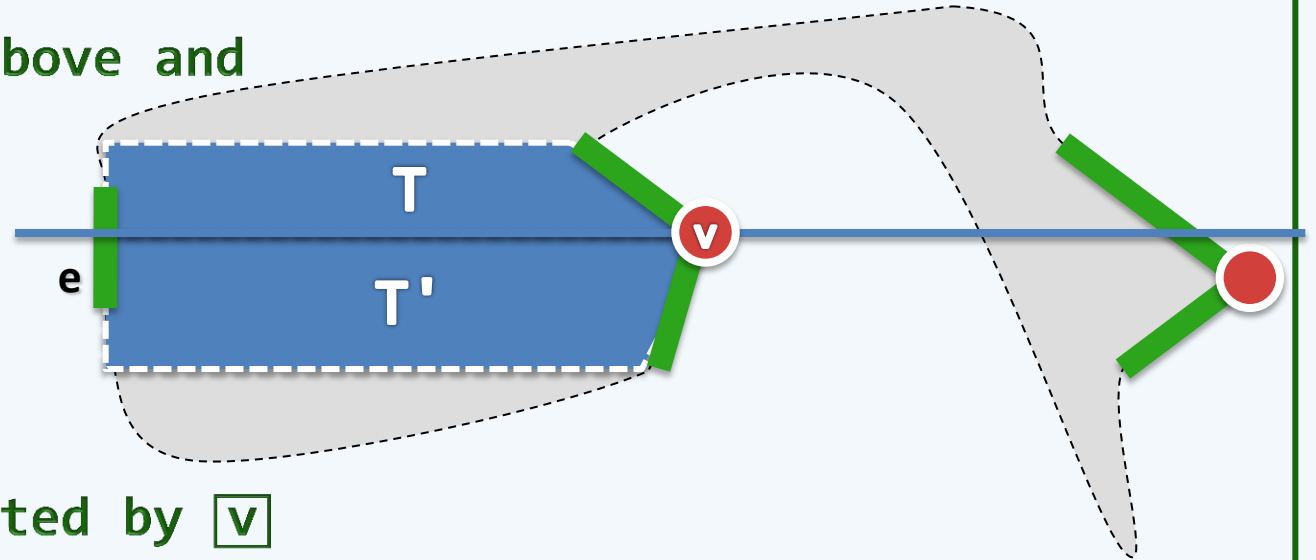
## 4: Right Adjacency

❖ A right adjacency vertex (event) has

- a right edge incident from above and
- another one from below

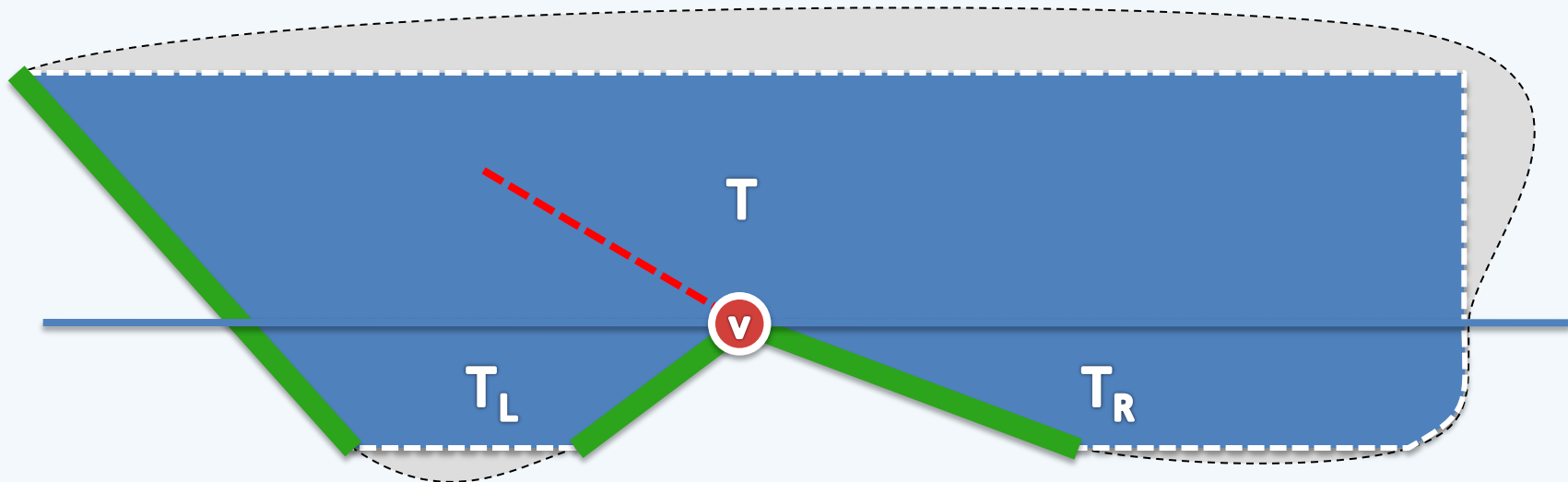
❖ At a right adjacency vertex  $v$ ,

- find the trapezoid  $T$  supported by  $v$
- replace  $T$  with  $T'$  in  $\mathcal{S}$
- let  $\text{helper}(T') = v$



## 5: Stalagmite

- ❖ At a stalagmite vertex  $v$ 
  - find the trapezoid  $T$  supported by  $v$
  - split  $T$  into  $T_L$  and  $T_R$
  - let  $\text{helper}(T_L) = \text{helper}(T_R) = v$



## 6: Stalactite

❖ At a stalactite vertex  $v$

- find the trapezoids  $T_L$  and  $T_R$  supported by  $v$
- merge  $T_L$  and  $T_R$  into  $T$
- let  $\text{helper}(T) = v$

