

**Arrangement**

**Duality: Preservation**

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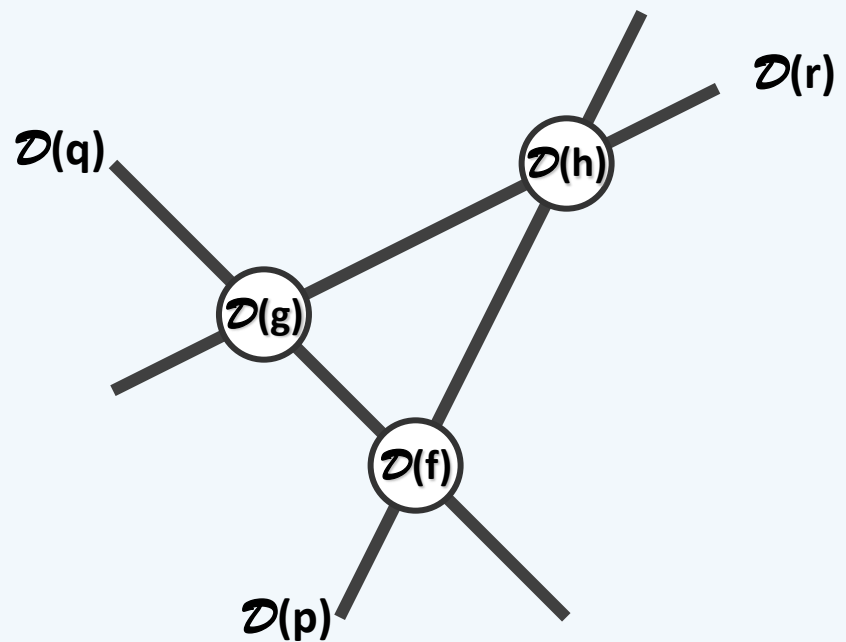
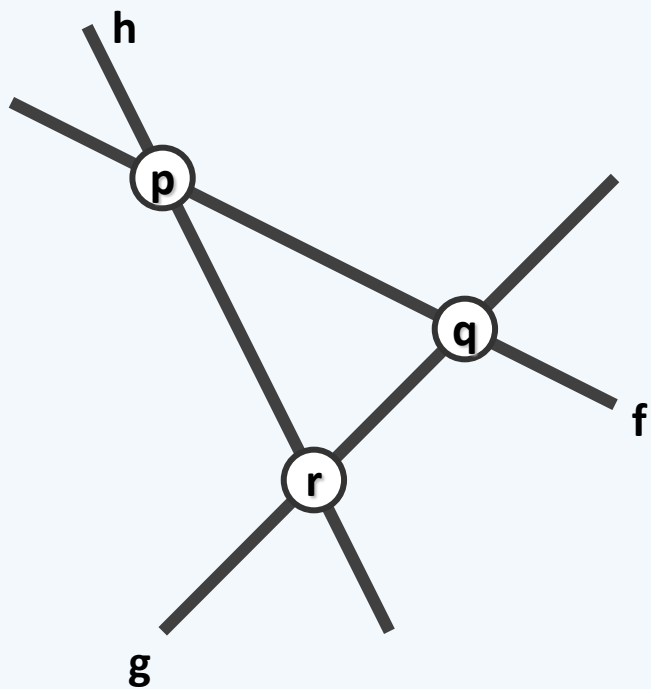
## Incidence & Order Preservation

❖ Let  $p$  be a point and  $h$  be a non-vertical hyperplane in  $\mathcal{E}^d$

❖ Then  $p \in h^+$  iff  $\mathcal{D}(h) \in \mathcal{D}(p)^+$

$p \in h^-$  iff  $\mathcal{D}(h) \in \mathcal{D}(p)^-$ , and

$p \in h$  iff  $\mathcal{D}(h) \in \mathcal{D}(p)$



## Incidence & Order Preservation

❖ Points in a **non-vertical** hyperplane  $h$

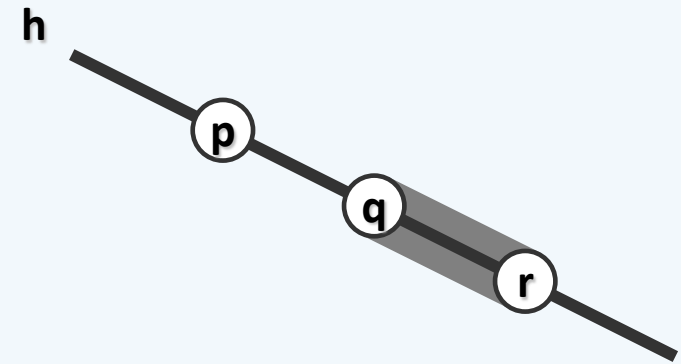
are mapped to

**non-vertical** hyperplanes containing  $\mathcal{D}(h)$

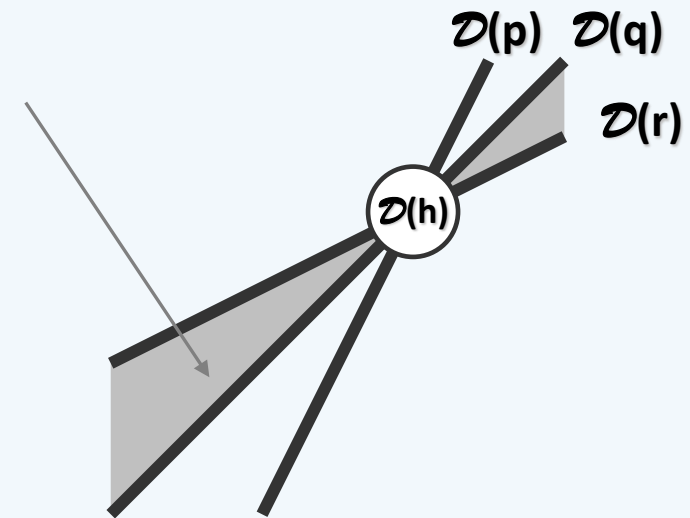
❖ Points in a **vertical** hyperplane

are mapped to

...

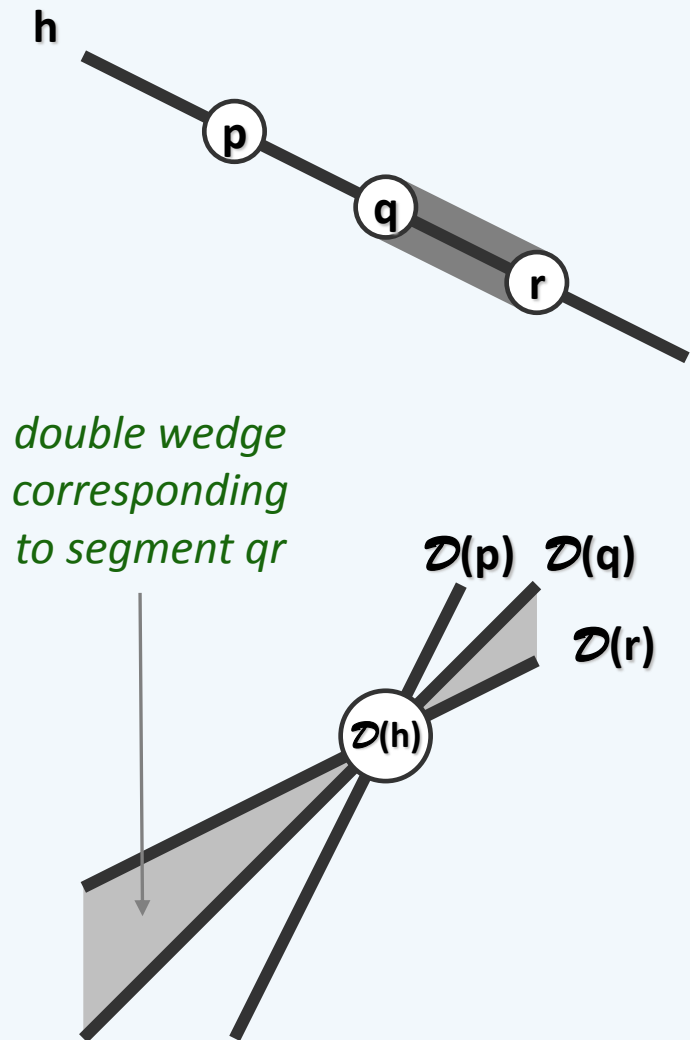


*double wedge  
corresponding  
to segment  $qr$*



## Incidence & Order Preservation

- ❖ Consider the planar arrangements
- ❖ Points in a **non-vertical** line  $h$  are mapped to **non-vertical** lines containing  $\mathcal{D}(h)$   
points in a **vertical** line  $h$  are mapped to lines parallel to each other
- ❖ Points in a **non-vertical** segment are mapped to lines in a **double wedge**  
points in a **vertical** segment are mapped to parallel lines in a **strip**
- ❖ Points in a **triangle** are mapped to ...



# The Magic of Unit Paraboloid

