

Voronoi Diagram

Divide-And-Conquer

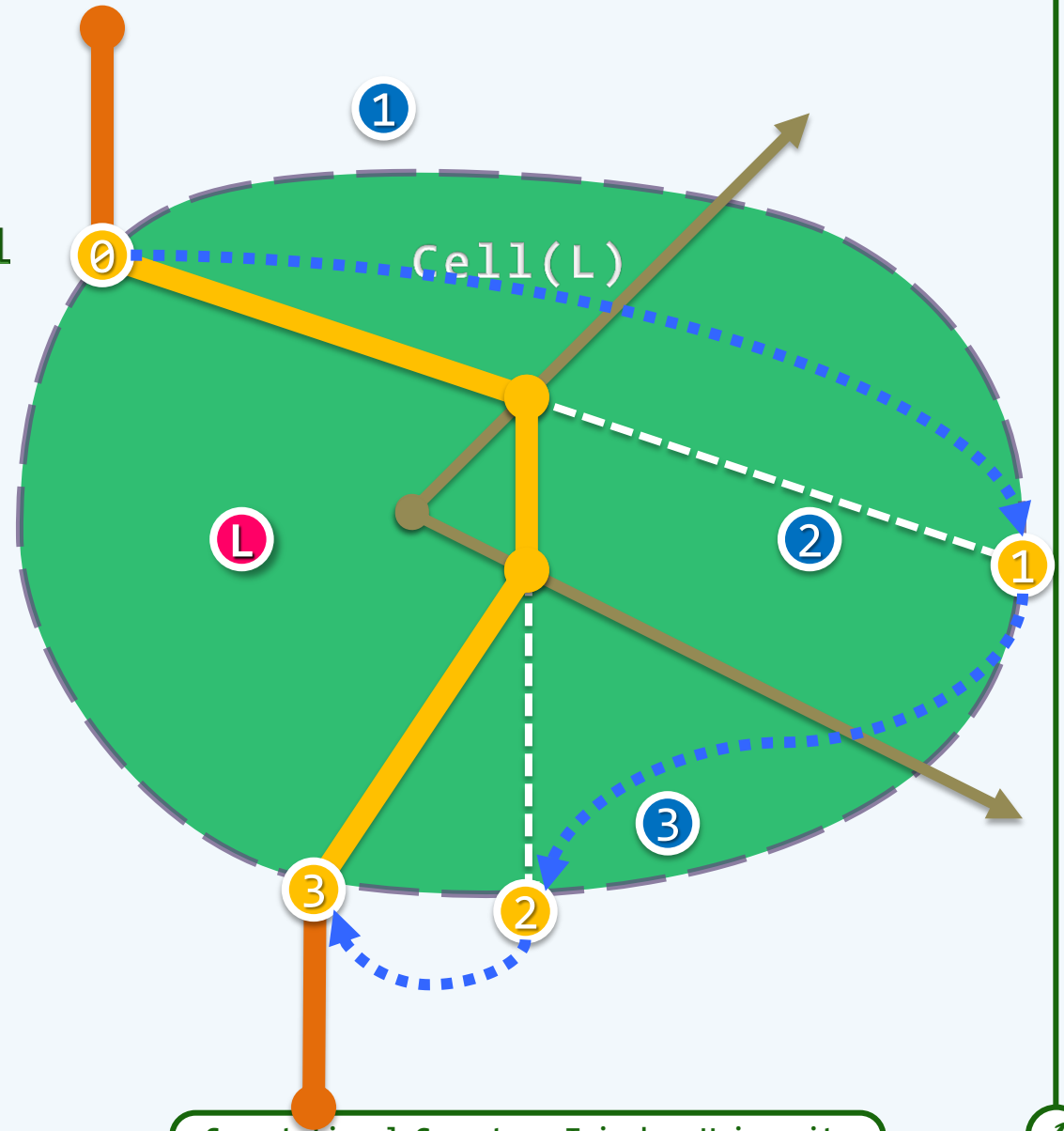
- Avoiding Rescans

Junhui DENG

deng@tsinghua.edu.cn

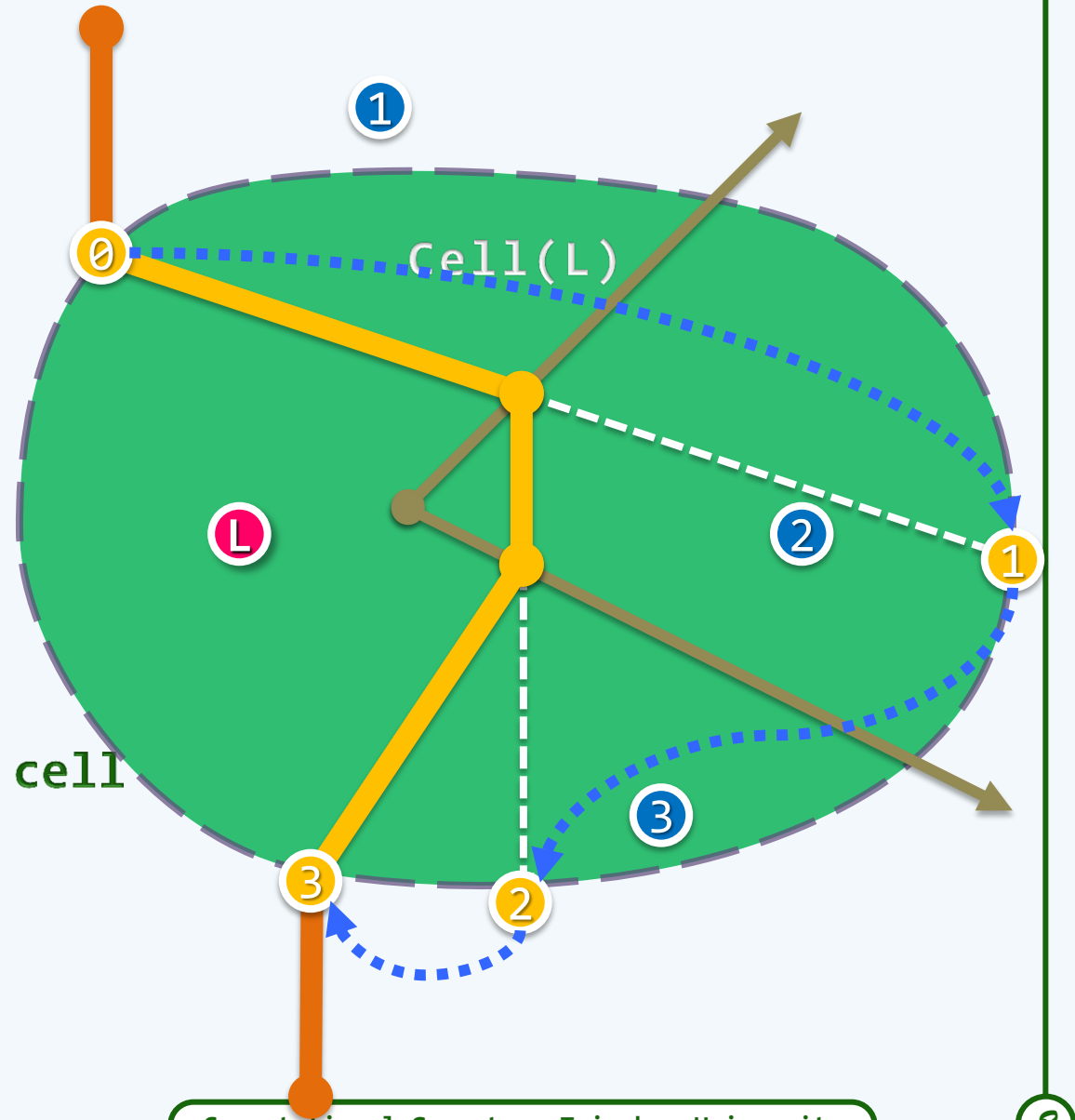
Monotonicity

- ❖ Each time we flip a cell, we add an edge to the un-flipped cell
- ❖ Furthermore, since each cell is itself convex, we know that ...
- ❖ Consecutive edges added to a same cell of the \boxed{L}/\boxed{R} sub-diagram always make an \boxed{R}/\boxed{L} turn



Amortization

- ❖ By keeping track of the last (failure) position, we needn't to start each scan from the right beginning
- ❖ As a result, all the intersection tests with a cell can be done in a total time of $O(n)$



Complexity

❖ Up to now, we know that

- The upper tangent can be computed in $O(n + m)$ time;
- cells will be clipped by the contour in $O(n + m)$ time; and
- we spend $O(n + m)$ time to flip all cells

❖ As a whole,

- two sub-diagrams can be merged in $O(n + m)$ time, and
- the divide-and-conquer algorithm computes the VD in $O(n \log n)$ time