

# Triangulation

Beyond  $\Omega(n \log n)$

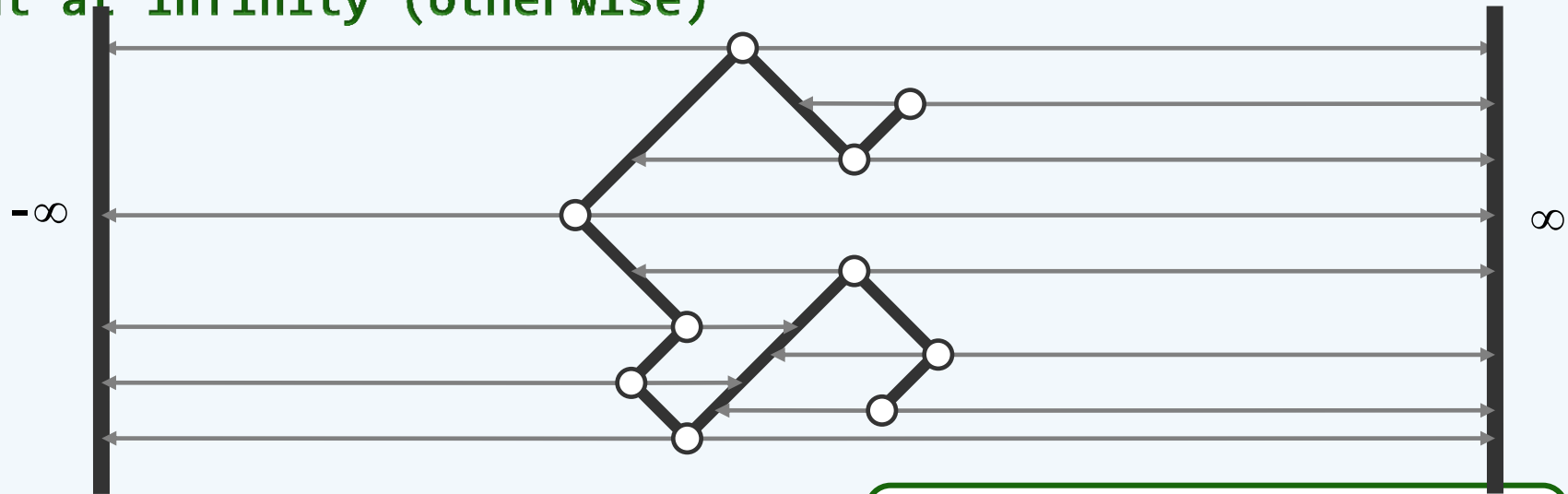
- HVP

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## Horizontal Visibility Partition

- ❖ Trapezoidalization may be extended to **simple polygonal chains**, where the horizontal lines run to infinity if they meet no obstruction
- ❖ The HVP of a simple polygonal chain is the partition of the plane obtained by adding horizontal edges connecting each vertex to
  - the closest point on the chain on both sides (if exists), or
  - a point at infinity (otherwise)



## Merging HVP's

❖ Let  $P_1$  and  $P_2$  be two successively adjacent simple polygonal chains

❖ [Chazelle & Incerpi, 1984]

If  $P_1 \cup P_2$  is also a simple polygonal chain, then

HVP( $P_1 \cup P_2$ ) can be obtained from HVP( $P_1$ ) and HVP( $P_2$ ) in **linear** time

❖ This result indicates a natural divide-and-conquer algorithm  
for computing the HVP of a simple polygonal chain

❖ [Chazelle & Incerpi, 1984]

The HVP of a simple polygonal chain can be computed

in  **$O(n \log n)$**  time, where  **$n$**  is the length of the chain

❖ However, the performance of this algorithm is **not** improved