

# Triangulation

Fisk's Proof

- Pigeon-Hole Principle

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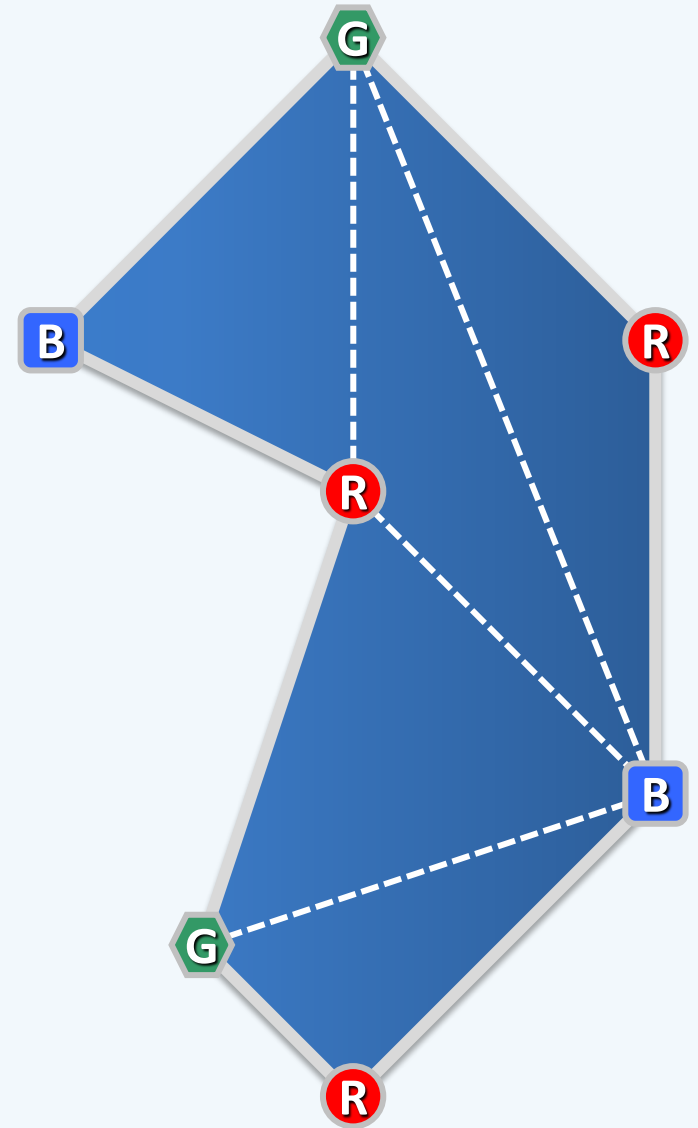
$$\diamond |\mathcal{R}| + |\mathcal{G}| + |\mathcal{B}| = n$$

❖ Here we have

- 3 subsets (holes) and
- $n$  vertices (pigeons)

❖ At least one of the subsets contains

no more than  $\lfloor n/3 \rfloor$  vertices



❖ In this example

$$|\mathcal{R}| + |\mathcal{G}| + |\mathcal{B}|$$

$$= 3 + 2 + 2$$

$$= 7$$

❖ So either  $\mathcal{G}$  or  $\mathcal{B}$  will work

