

# Voronoi Diagram

Divide-And-Conquer

- Intersecting With Cells

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## DCEL

❖ With the DCEL structure

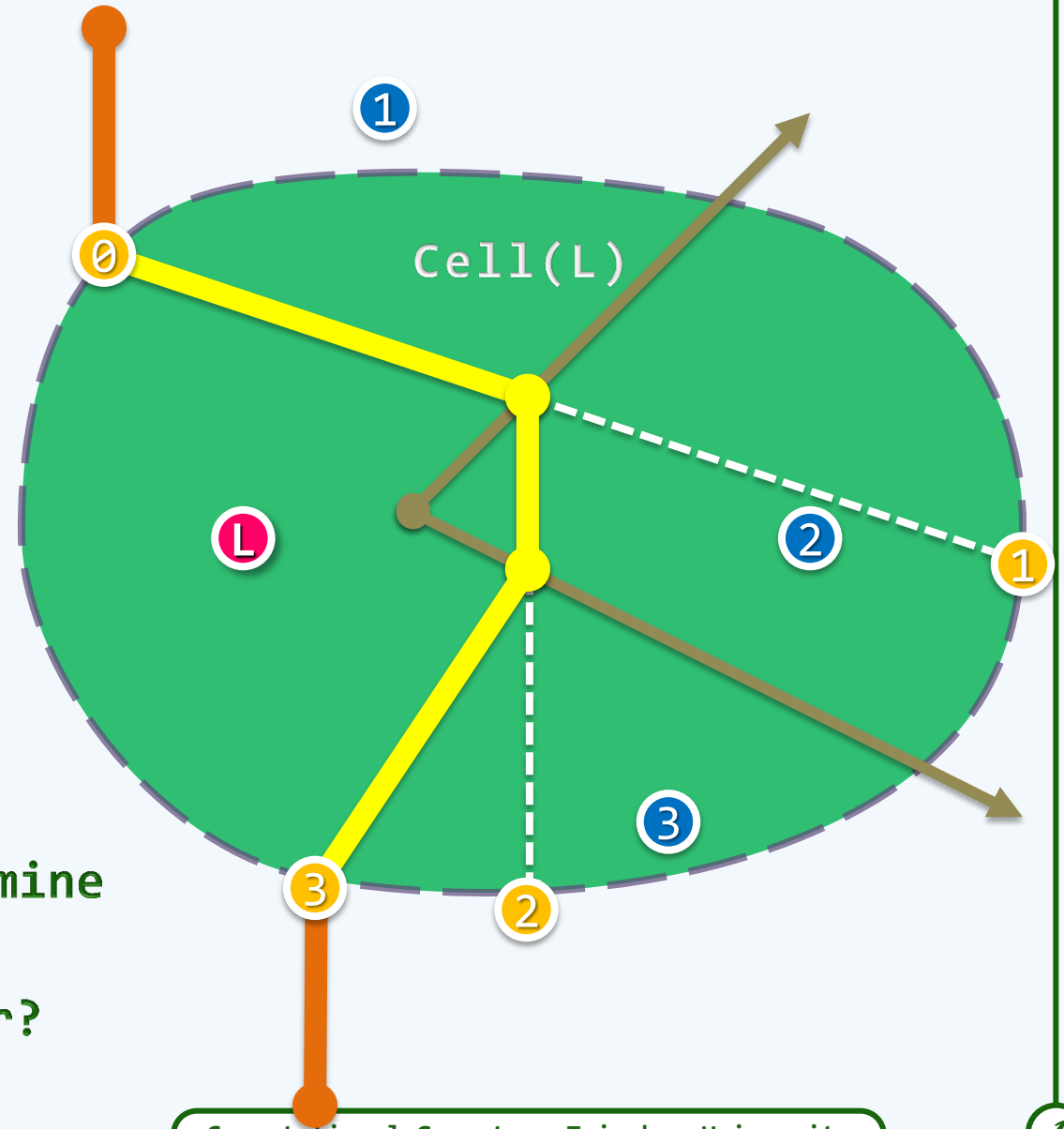
- the upper tangent can be computed

in  $\mathcal{O}(n + m)$  time

- to switch to a neighbor cell  
w.r.t. a given boundary edge

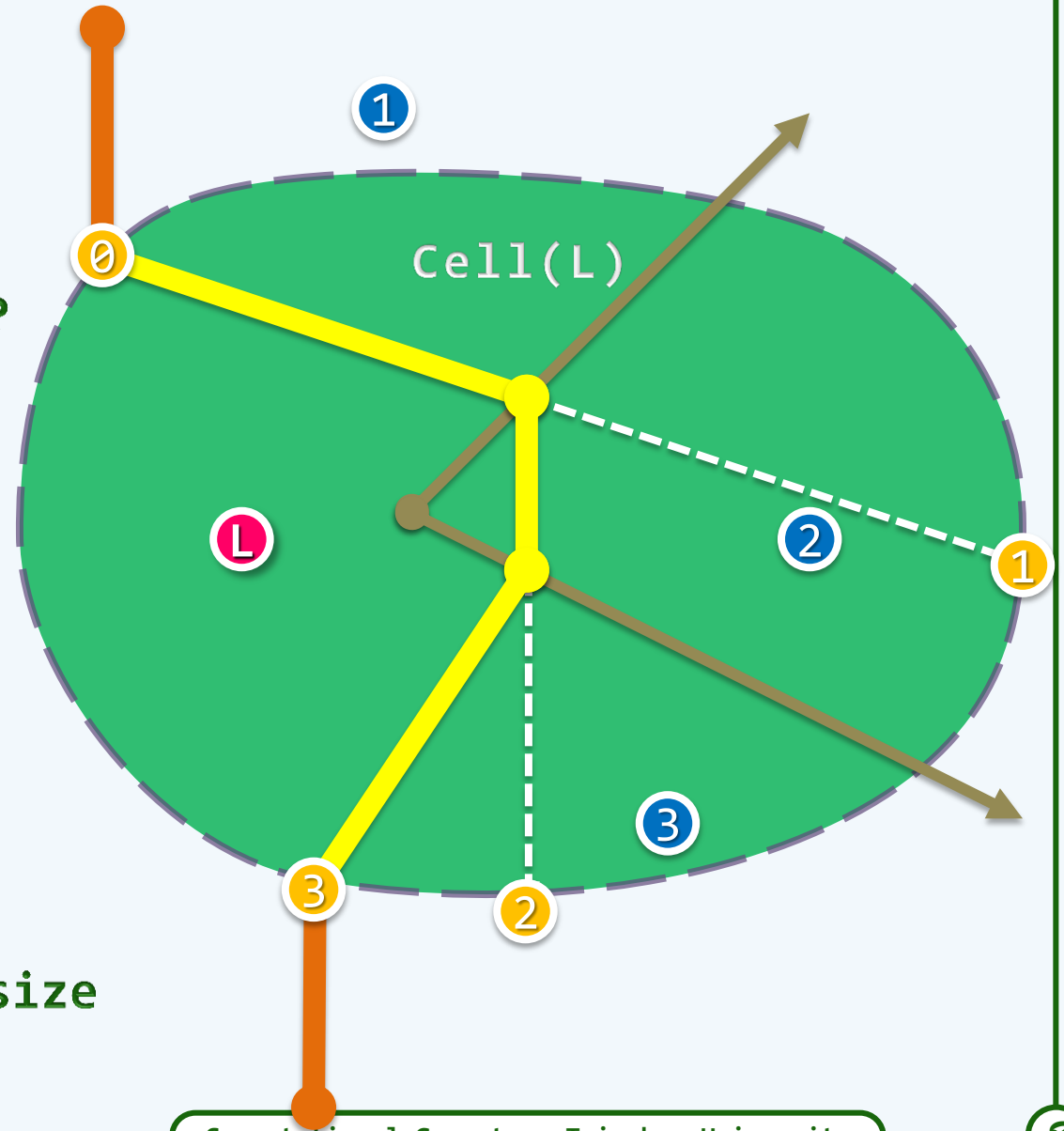
needs  $\mathcal{O}(1)$  time

❖ But how much time is needed to determine  
each turning point of the contour?



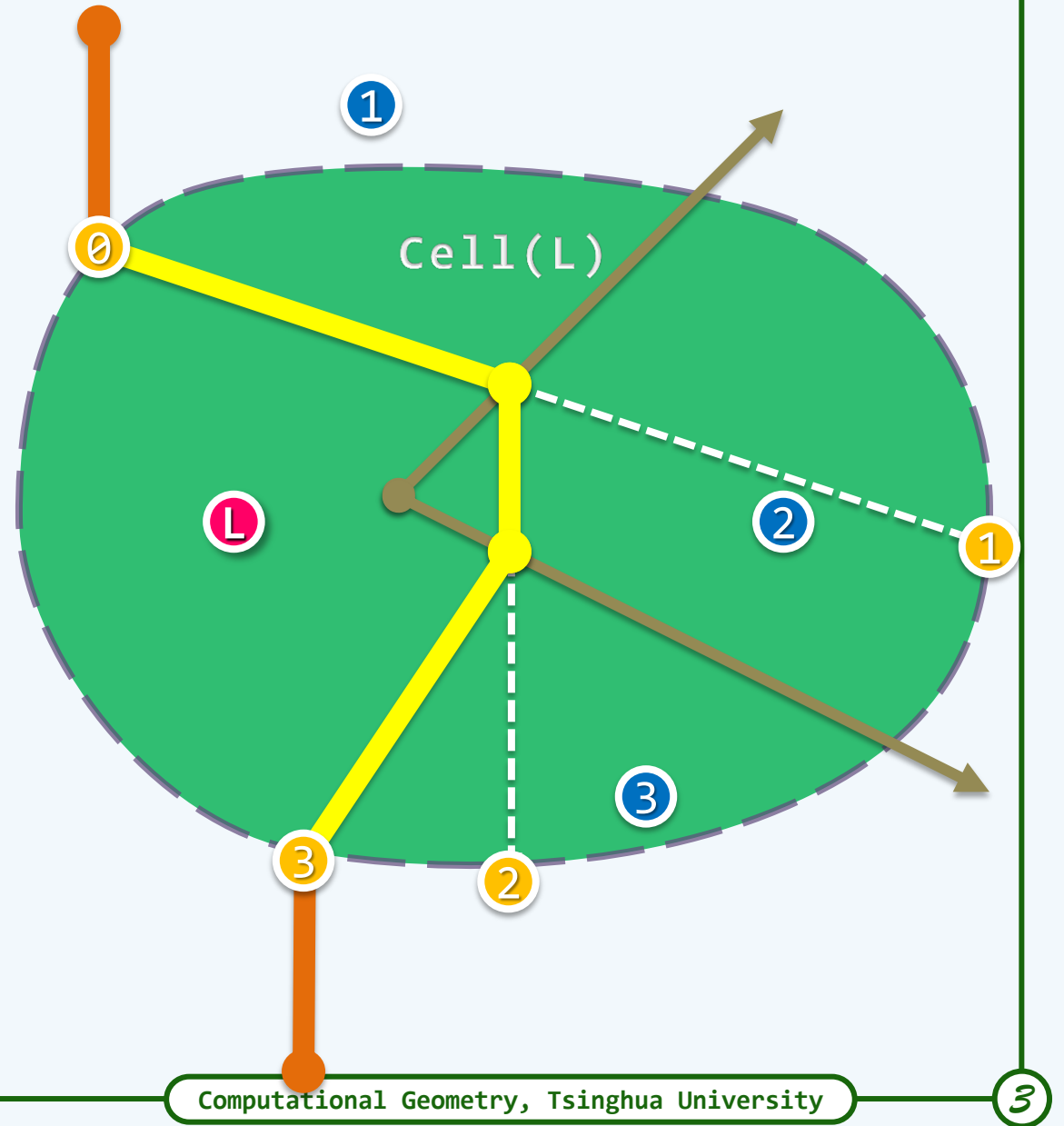
## Brute-Force

- ❖ But how much time does it need to **intersect** a cell with a bisector?
- ❖ A brute-force algorithm
  - tests all the cell edges with the bisector, and hence
  - runs in time **linear** to the cell size



## Worst Cases

- ❖ As we will see later,  
in the worst cases, however,  
every cell edge is **rescanned**  
for each bisector
- ❖ It means that  
the entire process might require  
 **$\Omega(n * m)$  time!**



## Avoiding Rescan

- ❖ A good news is that rescanning edges of a same cell can be **avoided**!
- ❖ Specifically, we need to scan each cell boundary **only once**
- ❖ The trick here is based on the following observations ...

