

# Point Location

Performance Of Trapezoidal Map

- Size Of Search Structure

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$$E[ |SS(S)| ] = \mathcal{O}(n)$$

❖ Claim:

the size of  $SS(S)$  is  $\boxed{\text{expected-}\mathcal{O}(n)}$ , where

the expectation depends  $\boxed{\text{only}}$

on the insertion  $\boxed{\text{order}}$

❖ Observation:

#(new nodes added to  $SS(S)$  with each new segment)

$\propto$

#(newly created trapezoids)

$$E[ |SS(S)| ] = O(n)$$

❖ We have just showed that

with each new insertion,

the expected number of trapezoids that were created

was  $O(1)$

❖ Therefore

-  $O(1)$  new nodes were added to  $SS(S)$

with each insertion, and

- the total size of  $SS(S)$  is  $O(n)$