

Open CASCADE Technology 7.0.0

BRep Format

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1 Introduction

1 Introduction

BREP format is used to store 3D models and allows to store a model which consists of vertices, edges, wires, faces, shells, solids, compsolids, compounds, edge triangulations, face triangulations, polylines on triangulations, space location and orientation. Any set of such models may be stored as a single model which is a compound of the models.

The format is described in an order which is convenient for understanding rather than in the order the format parts follow each other. BNF-like definitions are used in this document. Most of the chapters contain BREP format descriptions in the following order:

- format file fragment to illustrate the part;
- · BNF-like definition of the part;
- · detailed description of the part.

Note that the format is a part of Open CASCADE Technology (OCCT).

Some data fields of the format have additional values, which are used in OCCT.

Some data fields of the format are specific for OCCT.

2 Format Common Structure

ASCII encoding is used to read/write BREP format from/to file. The format data are stored in a file as text data. BREP format uses the following BNF terms:

- <\n>: It is the operating-system-dependent ASCII character sequence which separates ASCII text strings in the operating system used;
- < \n>: = " "*<\n>;
- <_>: = " "+; It is a not empty sequence of space characters with ASCII code 21h;
- <flag>: = "0" | "1";
- <int>: It is an integer number from -2³¹ to 2³¹ -1which is written in denary system;
- <real>: It is a real from -1.7976931348623158 \cdot 10³⁰⁸ to 1.7976931348623158 \cdot 10³⁰⁸ which is written in decimal or E form with base 10.The point is used as a delimiter of the integer and fractional parts;
- <2D point>: = <real><_><real>;
- <3D point>: = <real>(< ><real)>2:
- <2D direction>: It is a <2D point> x yso that $x^2 + y^2 = 1$;
- <3D direction>: It is a <3D point> x y zso that $x^2 + y^2 + z^2 = 1$;
- <+>: It is an arithmetic operation of addition.

The format consists of the following sections:

- <content type>;
- <version>;
- <locations>;
- <geometry>;
- <shapes>.

<content type> = "DBRep_DrawableShape" <_\n><_\n>; <content type> have other values [1].

<version> = ("CASCADE Topology V1, (c) Matra-Datavision" | "CASCADE Topology V2, (c) Matra-Datavision")<\n>; The difference of the versions is described in the document.

 $Sections < locations>, < geometry> \ and < shapes> \ are \ described \ below \ in \ separate \ chapters \ of \ the \ document.$

3 Locations 5

3 Locations

Example

```
Locations 3

1

0 0 1 0

1 0 0 0

0 1 0 0

1

1 0 0 4

0 1 0 5

0 0 1 6

2 1 1 2 1 0
```

BNF-like Definition

```
<locations> = <location header> <_\n> <location records>;
<location header> = "Locations" <_> <location record count>;
<location record count> = <int>;
<location records> = <location record> ^ <location record count>;
<location record> = <location record 1> | <location record 2>;
<location record 1> = "1" <_\n> <location data 1>;
<location record 2> = "2" <_> <location data 2>;
<location data 1> = ((<_> <real>) ^ 4 <_\n>) ^ 3;
<location data 2> = (<int> <_> <int> <_>) * "0" <_\n>;
```

Description

<location data 1> is interpreted as a 3 x 4 matrix $Q = \begin{pmatrix} q_{1,1} & q_{1,2} & q_{1,3} & q_{1,4} \\ q_{2,1} & q_{2,2} & q_{2,3} & q_{2,4} \\ q_{3,1} & q_{3,2} & q_{3,3} & q_{3,4} \end{pmatrix}$ which describes transformation of 3 dimensional space and satisfies the following constraints:

•
$$d \neq 0$$
 where $d = |Q_2|$ where $Q_2 = \begin{pmatrix} q_{1,1} & q_{1,2} & q_{1,3} & q_{1,4} \\ q_{2,1} & q_{2,2} & q_{2,3} & q_{2,4} \\ q_{3,1} & q_{3,2} & q_{3,3} & q_{3,4} \end{pmatrix}$;

•
$$Q_3^T = Q_3^{-1}$$
 where $Q_3 = Q_2/d^{1/3}$.

The transformation transforms a point (x, y, z) to another point (u, v, w) by the rule:

$$\begin{pmatrix} u \\ v \\ w \end{pmatrix} = Q \cdot (x \ y \ z \ 1)^T = \begin{pmatrix} q_{1,1} \cdot x + q_{1,2} \cdot y + q_{1,3} \cdot z + q_{1,4} \\ q_{2,1} \cdot x + q_{2,2} \cdot y + q_{2,3} \cdot z + q_{2,4} \\ q_{3,1} \cdot x + q_{3,2} \cdot y + q_{3,3} \cdot z + q_{3,4} \end{pmatrix}.$$

Q may be a composition of matrices for the following elementary transformations:

- parallel translation $\begin{pmatrix} 1 & 0 & 0 & q_{1,4} \\ 0 & 1 & 0 & q_{2,4} \\ 0 & 0 & 1 & q_{3,4} \end{pmatrix};$
- rotation around an axis with a direction $\textit{D(D_X , D_Y , D_Z)}$ by an angle $\phi-$

$$\begin{pmatrix} D_x^2 \cdot (1-\cos(\varphi)) + \cos(\varphi) & D_x \cdot D_y \cdot (1-\cos(\varphi)) - D_z \cdot \sin(\varphi) & D_x \cdot D_z \cdot (1-\cos(\varphi)) + D_y \cdot \sin(\varphi) & 0 \\ D_x \cdot D_y \cdot (1-\cos(\varphi)) + D_z \cdot \sin(\varphi) & D_y^2 \cdot (1-\cos(\varphi)) + \cos(\varphi) & D_y \cdot D_z \cdot (1-\cos(\varphi)) - D_x \cdot \sin(\varphi) & 0 \\ D_x \cdot D_z \cdot (1-\cos(\varphi)) - D_y \cdot \sin(\varphi) & D_y \cdot D_z \cdot (1-\cos(\varphi)) + D_x \cdot \sin(\varphi) & D_z^2 \cdot (1-\cos(\varphi)) + \cos(\varphi) & 0 \end{pmatrix};$$

$$\bullet \ \, \mathrm{scaling} - \begin{pmatrix} s & 0 & 0 & 0 \\ 0 & s & 0 & 0 \\ 0 & 0 & s & 0 \end{pmatrix} \mathrm{where} \, S \in (-\infty,\,\infty)/\left\{0\right\};$$

3 Locations 6

- central symmetry $-\begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{pmatrix};$
- axis symmetry $-\begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$; plane symmetry $-\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{pmatrix}$.

<location data 2> is interpreted as a composition of locations raised to a power and placed above this <location data 2> in the section < locations>. < location data 2> is a sequence $l_1p_1...l_np_n$ of $n \ge 0$ integer pairs l_ip_i $(1 \le i \le n)$ n). <flag> 0 is the indicator of the sequence end. The sequence is interpreted as a composition $L_{l_1}^{p_1} \cdot \ldots \cdot L_{l_n}^{p_n}$ where L_{l_i} is a location from l_i -th <location record> in the section locations. <location record> numbering starts from 1.

4 Geometry 7

4 Geometry

```
<geometry> =
<2D curves>
<3D curves>
<3D polygons>
<polygons on triangulations>
<surfaces>
<triangulations>;
```

4.1 3D curves

Example

BNF-like Definition

```
<3D curves> = <3D curve header> <_\n> <3D curve records>;

<3D curve header> = "Curves" <_> <3D curve count>;

<3D curve count> = <int>;

<3D curve records> = <3D curve record> ^ <3D curve count>;

<3D curve record = <3D curve record 1> |

<3D curve record 2> |

<3D curve record 3> |

<3D curve record 4> |

<3D curve record 5> |

<3D curve record 6> |

<3D curve record 7> |

<3D curve record 8> |

<3D curve record 9>;
```

4.1.1 Line - <3D curve record 1>

Example

```
1 1 0 3 0 1 0
```

BNF-like Definition

```
<3D curve record 1> = "1" <_> <3D point> <_> <3D direction> <_\n>;
```

Description

<3D curve record 1> describes a line. The line data consist of a 3D point Pand a 3D direction D. The line passes through the point P, has the direction Dand is defined by the following parametric equation:

$$C(u) = P + u \cdot D, u \in (-\infty, \infty).$$

The example record is interpreted as a line which passes through a point P=(1, 0, 3), has a direction D=(0, 1, 0) and is defined by the following parametric equation: $C(u) = (1,0,3) + u \cdot (0,1,0)$.

4.1.2 Circle - <3D curve record 2>

Example

```
2 1 2 3 0 0 1 1 0 -0 -0 1 0 4
```

BNF-like Definition

Description

<3D curve record 2> describes a circle. The circle data consist of a 3D point P, pairwise orthogonal 3D directions N, D_X and D_Y and a non-negative real r. The circle has a center P and is located in a plane with a normal N. The circle has a radius r and is defined by the following parametric equation:

$$C(u) = P + r \cdot (cos(u) \cdot D_x + sin(u) \cdot D_y), \ u \in [o, 2 \cdot \pi).$$

The example record is interpreted as a circle which has its center P=(1,2,3), is located in plane with a normal N=(0,0,1). Directions for the circle are $D_X=(1,0,0)$ and $D_Y=(0,1,0)$. The circle has a radius r=4 and is defined by the following parametric equation: $C(u)=(1,2,3)+4\cdot(cos(u)\cdot(1,0,0)+sin(u)\cdot(0,1,0))$.

4.1.3 Ellipse - <3D curve record 3>

Example

```
3 1 2 3 0 0 1 1 0 -0 -0 1 0 5 4
```

BNF-like Definition

Description

<3D curve record 3> describes an ellipse. The ellipse data consist of a 3D point P, pairwise orthogonal 3D directions N, D_{maj} and D_{min} and non-negative reals r_{maj} and r_{min} so that $r_{min} \leq r_{maj}$. The ellipse has its center P, is located in plane with the normal N, has major and minor axis directions D_{maj} and D_{min} , major and minor radii D_{maj} and D_{min} and is defined by the following parametric equation:

$$C(u) = P + r_{maj} \cdot cos(u) \cdot D_{maj} + r_{min} \cdot sin(u) \cdot D_{min}, u \in [0, 2 \cdot \pi).$$

The example record is interpreted as an ellipse which has its center P=(1, 2, 3), is located in plane with a normal N=(0, 0, 1), has major and minor axis directions $D_{maj}=(1, 0, 0)$ and $D_{min}=(0, 1, 0)$, major and minor radii $r_{maj}=5$ and $r_{min}=4$ and is defined by the following parametric equation: $C(u)=(1,2,3)+5\cdot cos(u)\cdot (1,0,0)+4\cdot sin(u)\cdot (0,1,0)$.

4.1.4 Parabola - <3D curve record 4>

Example

```
4 1 2 3 0 0 1 1 0 -0 -0 1 0 16
```

BNF-like Definition

Description

<3D curve record 4> describes a parabola. The parabola data consist of a 3D point P, pairwise orthogonal 3D directions N, D_X and D_Y and a non-negative real f. The parabola is located in plane which passes through the point P and has the normal N. The parabola has a focus length f and is defined by the following parametric equation:

$$C(u) = P + \frac{u^2}{4 \cdot f} \cdot D_x + u \cdot D_y, u \in (-\infty, \infty) \Leftarrow f \neq 0;$$

$$C(u) = P + u \cdot D_x, u \in (-\infty, \infty) \Leftarrow f = 0 \text{ (degenerated case)}.$$

The example record is interpreted as a parabola in plane which passes through a point P=(1, 2, 3) and has a normal N=(0, 0, 1). Directions for the parabola are $D_X=(1, 0, 0)$ and $D_Y=(0, 1, 0)$. The parabola has a focus length f=16 and is defined by the following parametric equation: $C(u)=(1,2,3)+\frac{u^2}{64}\cdot(1,0,0)+u\cdot(0,1,0)$.

4.1.5 Hyperbola - <3D curve record 5>

Example

```
5 1 2 3 0 0 1 1 0 -0 -0 1 0 5 4
```

```
<3D curve record 5> = "5" <_> <3D hyperbola origin> <_> <3D hyperbola N> <_> <3D hyperbola Dx> <_> <3D
hyperbola Dy> <_> <3D hyperbola Kx> <_> <3D hyperbola Ky> <_\n>;
<3D hyperbola origin> = <3D point>;
```

```
<3D hyperbola N> = <3D direction>;
<3D hyperbola Dx> = <3D direction>;
<3D hyperbola Dy> = <3D direction>;
<3D hyperbola Kx> = <real>;
<3D hyperbola Ky> = <real>;
```

Descripton

<3D curve record 5> describes a hyperbola. The hyperbola data consist of a 3D point P, pairwise orthogonal 3D directions N, D_X and D_Y and non-negative reals k_X and k_Y . The hyperbola is located in plane which passes through the point Pand has the normal N. The hyperbola is defined by the following parametric equation:

$$C(u) = P + k_x \cdot cosh(u) \cdot D_x + k_y \cdot sinh(u) \cdot D_y, u \in (-\infty, \infty).$$

The example record is interpreted as a hyperbola in plane which passes through a point P=(1, 2, 3) and has a normal N=(0, 0, 1). Other hyperbola data are $D_X=(1, 0, 0)$, $D_Y=(0, 1, 0)$, $k_X=5$ and $k_Y=4$. The hyperbola is defined by the following parametric equation: $C(u)=(1,2,3)+5\cdot cosh(u)\cdot (1,0,0)+4\cdot sinh(u)\cdot (0,1,0)$.

4.1.6 Bezier Curve - <3D curve record 6>

Example

```
6 1 2 0 1 0 4 1 -2 0 5 2 3 0 6
```

BNF-like Definition

```
<3D curve record 6> = "6" <_> <3D Bezier rational flag> <_> <3D Bezier degree>
<3D Bezier weight poles> <_\n>;
<3D Bezier rational flag> = <flag>;
<3D Bezier degree> = <int>;
3D Bezier weight poles> = (<_> <3D Bezier weight pole>) ^ (<3D Bezier degree> <+> "1");
<3D Bezier weight pole> = <3D point> [<_> <real>];
```

Description

<3D curve record 6> describes a Bezier curve. The curve data consist of a rational r, a degree $m \le 25$ and weight poles.

The weight poles are m+13D points $B_0 \dots B_m$ if the flag r is 0. The weight poles are m+1 pairs $B_0 h_0 \dots B_m h_m$ if flag r is 1. Here B_i is a 3D point and h_i is a positive real $(0 \le i \le m)$. $h_i = 1$ $(0 \le i \le m)$ if the flag r is 0.

The Bezier curve is defined by the following parametric equation:

$$C(u) = \frac{\sum_{i=0}^{m} B_i \cdot h_i \cdot C_m^i \cdot u^i \cdot (1-u)^{m-i}}{\sum_{i=0}^{m} h_i \cdot C_m^i \cdot u^i \cdot (1-u)^{m-i}}, \ u \in [0, \ 1]$$

where $0^0 \equiv 1$.

The example record is interpreted as a Bezier curve with a rational flag r=1, degree m=2 and weight poles $B_0=(0, 1, 0)$, $h_0=4$, $B_1=(1, -2, 0)$, $h_1=5$ and $B_2=(2, 3, 0)$, $h_2=6$. The Bezier curve is defined by the following parametric equation:

$$C(u) = \frac{(0,1,0) \cdot 4 \cdot (1-u)^2 + (1,-2,0) \cdot 5 \cdot 2 \cdot u \cdot (1-u) + (2,3,0) \cdot 6 \cdot u^2)}{4 \cdot (1-u)^2 + 5 \cdot 2 \cdot u \cdot (1-u) + 6 \cdot u^2}.$$

4.1.7 B-spline Curve - <3D curve record 7>

Example

BNF-like Definition

```
<3D curve record 7> = "7" <_> <3D B-spline rational flag> <_> "0" <_> <3D B-spline degree> <_>
<3D B-spline pole count> <_> <3D B-spline multiplicity knot count> <3D B-spline weight poles>
<_\n> <3D B-spline multiplicity knots> <_\n>;

<3D B-spline rational flag> = <flag>;

<3D B-spline degree> = <int>;

<3D B-spline pole count> = <int>;

<3D B-spline multiplicity knot count> = <int>;

<3D B-spline weight poles> = (<_> <3D B-spline weight pole>) ^ <3D B-spline pole count>;

<3D B-spline weight pole> = <3D point> [<_> <real>];

<3D B-spline multiplicity knots> = (<_> <3D B-spline multiplicity knot>) ^ <3D B-spline multiplicity knot count>;

<3D B-spline multiplicity knots> = (<_> <3D B-spline multiplicity knot>) ^ <3D B-spline multiplicity knot</pre>
```

Description

<3D curve record 7> describes a B-spline curve. The curve data consist of a rational flag r, a degree $m \le 25$, pole count $n \ge 2$, multiplicity knot count k, weight poles and multiplicity knots.

The weight poles are n 3D points B_1 ... B_n if the flag n is 0. The weight poles are n pairs B_1 h_1 ... B_n h_n if the flag n is 1. Here B_i is a 3D point and h_i is a positive real $(1 \le i \le n)$. $h_i = 1$ $(1 \le i \le n)$ if the flag n is 0.

The multiplicity knots are kpairs $u_1 q_1 \dots u_k q_k$. Here u_i is a knot with a multiplicity $q_i \ge 1$ $(1 \le i \le k)$ so that

$$u_i < u_{i+1} (1 \le i \le k-1),$$

$$q_1 \le m+1, \ q_k \le m+1, \ q_i \le m \ (2 \le i \le k-1), \sum_{i=1}^k q_i = m+n+1.$$

The B-spline curve is defined by the following parametric equation:

$$C(u) = \frac{\sum_{i=1}^{n} B_i \cdot h_i \cdot N_{i,m+1}(u)}{\sum_{i=1}^{n} h_i \cdot N_{i,m+1}(u)}, \ u \in [u_1, \ u_k]$$

where functions $N_{i,j}$ have the following recursion definition by j:

$$N_{i,1}(u) = \begin{cases} 1 \Leftarrow \bar{u}_i \leq u \leq \bar{u}_{i+1} \\ 0 \Leftarrow u < \bar{u}_i \vee \bar{u}_{i+1} \leq u \end{cases}, N_{i,j}(u) = \frac{(u - \bar{u}_i) \cdot N_{i,j-1}(u)}{\bar{u}_{i+j-1} - \bar{u}_i} + \frac{(\bar{u}_{i+j} - u) \cdot N_{i+1,j-1}(u)}{\bar{u}_{i+j} - \bar{u}_{i+1}}, \ (2 \leq j \leq m+1) \end{cases}$$

where

$$\bar{u}_i = u_j, \ (1 \le j \le k, \sum_{l=1}^{j-1} q_l + 1 \le i \le \sum_{l=1}^{j} q_l).$$

The example record is interpreted as a B-spline curve with a rational flag r=1, a degree m=1, pole count n=3, multiplicity knot count k=5, weight poles $B_1=(0,1,0)$, $h_1=4$, $B_2=(1,-2,0)$, $h_2=5$ and $B_3=(2,3,0)$, $h_3=6$, multiplicity knots $u_1=0$, $u_1=0$, $u_2=0.25$, $u_2=0.25$, $u_3=0.5$, $u_3=0.5$, $u_4=0.75$

$$C(u) = \frac{(0,1,0) \cdot 4 \cdot N_{1,2}(u) + (1,-2,0) \cdot 5 \cdot N_{2,2}(u) + (2,3,0) \cdot 6 \cdot N_{3,2}(u)}{4 \cdot N_{1,2}(u) + 5 \cdot N_{2,2}(u) + 6 \cdot N_{3,2}(u)}.$$

4.1.8 Trimmed Curve - <3D curve record 8>

Example

```
8 -4 5
1 1 2 3 1 0 0
```

BNF-like Definition

```
<3D curve record 8> = "8" <_> <3D trimmed curve u min> <_> <3D trimmed curve u max> <_\n> <3D curve record>
;
<3D trimmed curve u min> = <real>;
<3D trimmed curve u max> = <real>;
```

Description

<3D curve record 8> describes a trimmed curve. The trimmed curve data consist of reals u_{min} and u_{max} and <3D curve record> so that $u_{min} < u_{max}$. The trimmed curve is a restriction of the base curve Bdescribed in the record to the segment $[u_{min}, u_{max}] \subseteq domain(B)$. The trimmed curve is defined by the following parametric equation:

$$C(u) = B(u), u \in [u_{min}, u_{max}].$$

The example record is interpreted as a trimmed curve with u_{min} =-4and u_{max} =5for the base curve $B(u) = (1,2,3) + u \cdot (1,0,0)$. The trimmed curve is defined by the following parametric equation: $C(u) = (1,2,3) + u \cdot (1,0,0)$, $u \in [-4,5]$.

4.1.9 Offset Curve - <3D curve record 9>

Example

```
9 2
0 1 0
1 1 2 3 1 0 0
```

BNF-like Definition

```
<3D curve record 9> = "9" <_> <3D offset curve distance> <_\n>;
<3D offset curve direction> <_\n>;
<3D curve record>;
<3D offset curve distance> = <real>;
<3D offset curve direction> = <3D direction>;
```

Description

<3D curve record 9> describes an offset curve. The offset curve data consist of a distance d, a 3D direction D and a <3D curve record>. The offset curve is the result of offsetting the base curve B described in the record to the distance d along the vector $[B'(u), D] \neq \vec{0}$. The offset curve is defined by the following parametric equation:

$$C(u) = B(u) + d \cdot \frac{[B'(u), D]}{|[B'(u), D]|}, u \in domain(B).$$

The example record is interpreted as an offset curve with a distance d=2, direction D=(0, 1, 0), base curve $B(u)=(1,2,3)+u\cdot(1,0,0)$ and defined by the following parametric equation: $C(u)=(1,2,3)+u\cdot(1,0,0)+2\cdot(0,0,1)$.

4.2 Surfaces

Example

```
Surfaces 6
1 0 0 0 1 0 -0 0 0 1 0 -1 0
1 0 0 0 -0 1 0 0 0 1 1 0 -0
1 0 0 3 0 0 1 1 0 -0 -0 1 0
1 0 2 0 -0 1 0 0 0 1 1 0 -0
1 0 0 0 0 0 1 1 0 -0 -0 1 0
1 1 0 0 1 0 -0 0 0 1 0 -1 0
```

BNF-like Definition

4.2.1 Plane - < surface record 1 >

Example

```
1 0 0 3 0 0 1 1 0 -0 -0 1 0
```

BNF-like Definition

```
<surface record 1> = "1" <_> <3D point> (<_> <3D direction>) ^ 3 <_\n>;
```

Description

<surface record 1> describes a plane. The plane data consist of a 3D point Pand pairwise orthogonal 3D directions N, D_U and D_V . The plane passes through the point P, has the normal Nand is defined by the following parametric equation:

$$S(u,v) = P + u \cdot D_u + v \cdot D_v, \ (u,v) \in (-\infty,\infty) \times (-\infty,\infty).$$

The example record is interpreted as a plane which passes through a point P=(0, 0, 3), has a normal N=(0, 0, 1) and is defined by the following parametric equation: $S(u, v) = (0, 0, 3) + u \cdot (1, 0, 0) + v \cdot (0, 1, 0)$.

4.2.2 Cylinder - < surface record 2 >

Example

```
2 1 2 3 0 0 1 1 0 -0 -0 1 0 4
```

```
<surface record 2> = "2" <_> <3D point> (<_> <3D direction>) ^ 3 <_> <real> <_\n>;
```

Description

<surface record 2> describes a cylinder. The cylinder data consist of a 3D point P, pairwise orthogonal 3D directions D_V , D_X and D_Y and a non-negative real r. The cylinder axis passes through the point P and has the direction D_V . The cylinder has the radius r and is defined by the following parametric equation:

$$S(u,v) = P + r \cdot (\cos(u) \cdot D_x + \sin(u) \cdot D_v) + v \cdot D_v, \ (u,v) \in [0, 2 \cdot \pi) \times (-\infty, \infty).$$

The example record is interpreted as a cylinder which axis passes through a point P=(1, 2, 3) and has a direction $D_V=(0, 0, 1)$. Directions for the cylinder are $D_X=(1,0,0)$ and $D_Y=(0,1,0)$. The cylinder has a radius r=4 and is defined by the following parametric equation: $S(u,v)=(1,2,3)+4\cdot(cos(u)\cdot D_X+sin(u)\cdot D_Y)+v\cdot D_V$.

4.2.3 Cone - < surface record 3 >

Example

```
3 1 2 3 0 0 1 1 0 -0 -0 1 0 4 0.75
```

BNF-like Definition

```
<surface record 3> = "3" <_> <3D point> (<_> <3D direction>) ^ 3 (<_> <real>) ^ 2 <_\n>;
```

Description

<surface record 3> describes a cone. The cone data consist of a 3D point P, pairwise orthogonal 3D directions D_Z , D_X and D_Y , a non-negative real rand a real $\varphi \in (-\pi/2, \pi/2)/\{0\}$. The cone axis passes through the point P and has the direction D_Z . The plane which passes through the point P and is parallel to directions D_X and D_Y is the cone referenced plane. The cone section by the plane is a circle with the radius r. The direction from the point P to the cone apex is $-sgn(\varphi) \cdot D_Z$. The cone has a half-angle $|\varphi|$ and is defined by the following parametric equation:

$$S(u,v) = P + (r + v \cdot sin(\varphi)) \cdot (cos(u) \cdot D_X + sin(u) \cdot D_Y) + v \cdot cos(\varphi) \cdot D_Z, (u,v) \in [0, 2 \cdot \pi) \times (-\infty, \infty).$$

The example record is interpreted as a cone with an axis which passes through a point P=(1, 2, 3) and has a direction $D_Z=(0, 0, 1)$. Other cone data are $D_X=(1, 0, 0)$, $D_Y=(0, 1, 0)$, r=4 and $\varphi=0.75$. The cone is defined by the following parametric equation:

$$S(u,v) = (1,2,3) + (4 + v \cdot \sin(0.75)) \cdot (\cos(u) \cdot (1,0,0) + \sin(u) \cdot (0,1,0)) + v \cdot \cos(0.75) \cdot (0,0,1).$$

4.2.4 Sphere - < surface record 4 >

Example

```
4 1 2 3 0 0 1 1 0 -0 -0 1 0 4
```

BNF-like Definition

```
<surface record 4 > = "4" <_> <3D point> (<_> <3D direction>) ^ 3 <_> <real> <_\n>;
```

Description

<surface record 4> describes a sphere. The sphere data consist of a 3D point P, pairwise orthogonal 3D directions D_Z , D_X and D_Y and a non-negative real r. The sphere has the center P, radius r and is defined by the following parametric equation:

$$S(u,v) = P + r \cdot cos(v) \cdot (cos(u) \cdot D_x + sin(u) \cdot D_y) + r \cdot sin(v) \cdot D_Z, (u,v) \in [0, 2 \cdot \pi) \times [-\pi/2, \pi/2].$$

The example record is interpreted as a sphere with its center P=(1, 2, 3). Directions for the sphere are $D_Z=(0, 0, 1)$, $D_X=(1, 0, 0)$ and $D_Y=(0, 1, 0)$. The sphere has a radius r=4 and is defined by the following parametric equation:

$$S(u,v) = (1,2,3) + 4 \cdot \cos(v) \cdot (\cos(u) \cdot (1,0,0) + \sin(u) \cdot (0,1,0)) + 4 \cdot \sin(v) \cdot (0,0,1).$$

4.2.5 Torus - < surface record 5 >

Example

```
5 1 2 3 0 0 1 1 0 -0 -0 1 0 8 4
```

BNF-like Definition

```
<surface record 5> = "5" <_> <3D point> (<_> <3D direction>) ^ 3 (<_> <real>) ^ 2 <_\n>;
```

Description

<surface record 5> describes a torus. The torus data consist of a 3D point P, pairwise orthogonal 3D directions D_Z , D_X and D_Y and non-negative reals r_1 and r_2 . The torus axis passes through the point P and has the direction D_Z . r_1 is the distance from the torus circle center to the axis. The torus circle has the radius r_2 . The torus is defined by the following parametric equation:

$$S(u,v) = P + (r_1 + r_2 \cdot cos(v)) \cdot (cos(u) \cdot D_x + sin(u) \cdot D_y) + r_2 \cdot sin(v) \cdot D_Z, (u,v) \in [0, 2 \cdot \pi) \times [0, 2 \cdot \pi).$$

The example record is interpreted as a torus with an axis which passes through a point P=(1, 2, 3) and has a direction $D_Z=(0, 0, 1)$. $D_X=(1, 0, 0)$, $D_Y=(0, 1, 0)$, $P_Z=(0, 1, 0)$, $P_$

$$S(u,v) = (1,2,3) + (8+4 \cdot cos(v)) \cdot (cos(u) \cdot (1,0,0) + sin(u) \cdot (0,1,0)) + 4 \cdot sin(v) \cdot (0,0,1).$$

4.2.6 Linear Extrusion - < surface record 6 >

Example

```
6 0 0.6 0.8
2 1 2 3 0 0 1 1 0 -0 -0 1 0 4
```

BNF-like Definition

```
<surface record 6> = "6" <_> <3D direction> <_\n> <3D curve record>;
```

Description

<surface record 6> describes a linear extrusion surface. The surface data consist of a 3D direction D_V and a <3D curve record>. The linear extrusion surface has the direction D_V , the base curve C described in the record and is defined by the following parametric equation:

$$S(u,v) = C(u) + v \cdot D_v, (u,v) \in domain(C) \times (-\infty, \infty).$$

The example record is interpreted as a linear extrusion surface with a direction $D_V = (0, 0.6, 0.8)$. The base curve is a circle for the surface. The surface is defined by the following parametric equation:

$$S(u,v) = (1,2,3) + 4 \cdot (\cos(u) \cdot (1,0,0) + \sin(u) \cdot (0,1,0)) + v \cdot (0,0.6,0.8), \ (u,v) \in [0, 2 \cdot \pi) \times (-\infty, \infty).$$

4.2.7 Revolution Surface - < surface record 7 >

Example

```
7 -4 0 3 0 1 0
2 1 2 3 0 0 1 1 0 -0 -0 1 0 4
```

BNF-like Definition

```
<surface record 7 = "7" <_> <3D point> <_> <3D direction> <_\n> <3D curve record>;
```

Description

<surface record 7> describes a revolution surface. The surface data consist of a 3D point P, a 3D direction D and a <3D curve record>. The surface axis passes through the point P and has the direction D. The base curve C described by the record and the axis are coplanar. The surface is defined by the following parametric equation:

$$S(u,v) = P + V_D(v) + cos(u) \cdot (V(v) - V_D(v)) + sin(u) \cdot [D,V(v)], \ (u,v) \in [0,\ 2 \cdot \pi) \times domain(C)$$

where
$$V(v) = C(v) - P, V_D(v) = (D, V(v)) \cdot D$$
.

The example record is interpreted as a revolution surface with an axis which passes through a point P=(-4, 0, 3) and has a direction D=(0, 1, 0). The base curve is a circle for the surface. The surface is defined by the following parametric equation:

$$S(u,v) = (-4,0,3) + V_D(v) + cos(u) \cdot (V(v) - V_D(v)) + sin(u) \cdot [(0,1,0),V(v)], (u,v) \in [0,2 \cdot \pi) \times [0,2 \cdot \pi]$$

where
$$V(v) = (5,2,0) + 4 \cdot (\cos(v) \cdot (1,0,0) + \sin(v) \cdot (0,1,0)), V_D(v) = ((0,1,0),V(v)) \cdot (0,1,0).$$

4.2.8 Bezier Surface - < surface record 8 >

Example

```
8 1 1 2 1 0 0 1 7 1 0 -4 10 0 1 -2 8 1 1 5 11 0 2 3 9 1 2 6 12
```

BNF-like Definition

Description

<surface record 8> describes a Bezier surface. The surface data consist of a u rational flag r_U , v rational flag r_V , u degree $m_u \le 25$, v degree $m_v \le 25$ and weight poles.

The weight poles are $(m_u+1)\cdot (m_v+1)$ 3D points $B_{i,j}$ $((i,j)\in\{0,...,m_u\}\times\{0,...,m_v\})$ if $r_u+r_v=0$. The weight poles are $(m_u+1)\cdot (m_v+1)$ pairs $B_{i,j}h_{i,j}$ $((i,j)\in\{0,...,m_u\}\times\{0,...,m_v\})$ if $r_u+r_v\neq 0$. Here $B_{i,j}$ is a 3D point and $h_{i,j}$ is a positive real $((i,j)\in\{0,...,m_u\}\times\{0,...,m_v\})$. $h_{i,j}=1$ $((i,j)\in\{0,...,m_u\}\times\{0,...,m_v\})$ if $r_u+r_v=0$.

The Bezier surface is defined by the following parametric equation:

$$S(u,v) = \frac{\sum_{i=0}^{m_u} \sum_{j=0}^{m_v} B_{i,j} \cdot h_{i,j} \cdot C_{m_u}^i \cdot u^i \cdot (1-u)^{m_u-i} \cdot C_{m_v}^j \cdot v^j \cdot (1-v)^{m_v-j}}{\sum_{i=0}^{m_u} \sum_{j=0}^{m_v} h_{i,j} \cdot C_{m_u}^i \cdot u^i \cdot (1-u)^{m_u-i} \cdot C_{m_v}^j \cdot v^j \cdot (1-v)^{m_v-j}}, (u,v) \in [0,1] \times [0,1]$$

where $0^0 \equiv 1$.

The example record is interpreted as a Bezier surface with a u rational flag r_U =1, v rational flag r_V =1, u degree m_U =2, v degree m_V =1, weight poles $B_{0,0}$ =(0, 0, 1), $h_{0,0}$ =7, $B_{0,1}$ =(1, 0, -4), $h_{0,1}$ =10, $B_{1,0}$ =(0, 1, -2), $h_{1,0}$ =8, $B_{1,1}$ =(1, 1, 5), $h_{1,1}$ =11, $B_{2,0}$ =(0, 2, 3), $h_{2,0}$ =9and $B_{2,1}$ =(1, 2, 6), $h_{2,1}$ =12. The surface is defined by the following parametric equation:

$$S(u,v) = [(0,0,1) \cdot 7 \cdot (1-u)^2 \cdot (1-v) + (1,0,-4) \cdot 10 \cdot (1-u)^2 \cdot v + (0,1,-2) \cdot 8 \cdot 2 \cdot u \cdot (1-u) \cdot (1-v) + (1,1,5) \cdot 11 \cdot 2 \cdot u \cdot (1-u) \cdot v + (0,2,3) \cdot 9 \cdot u^2 \cdot (1-v) + (1,2,6) \cdot 12 \cdot u^2 \cdot v] \\ \div [7 \cdot (1-u)^2 \cdot (1-v) + (1,2,6) \cdot 12 \cdot u^2 \cdot v] \\ + 10 \cdot (1-u)^2 \cdot v + 8 \cdot 2 \cdot u \cdot (1-u) \cdot (1-v) + 11 \cdot 2 \cdot u \cdot (1-u) \cdot v + 9 \cdot u^2 \cdot (1-v) + 12 \cdot u^2 \cdot v]$$

4.2.9 B-spline Surface - < surface record 9 >

Example

```
9  1  1  0  0  1  1  3  2  5  4  0  0  1  7  1  0  -4  10  
0  1  -2  8  1  1  5  11  
0  2  3  9  1  2  6  12  

0  1  0.25  1  
0.5  1  
0.75  1  
1  1  
0  1  
0.3  1  
0.7  1  
1  1
```

```
<surface record 9> = "9" <_> <B-spline surface u rational flag> <_>
<B-spline surface v rational flag> <_> "0" <_> "0" <_> 'B-spline surface u degree> <_>
<B-spline surface v degree> <_> <B-spline surface u pole count> <_>
<B-spline surface v pole count> <_> <B-spline surface u multiplicity knot count> <_>
<B-spline surface v multiplicity knot count> <_> <B-spline surface weight poles> <_\n>
<B-spline surface u multiplicity knots> <_\n> <B-spline surface v multiplicity knots>;
<B-spline surface u rational flag> = <flag>;
<B-spline surface v rational flag> = <flag>;
<B-spline surface v degree> = <int>;
<B-spline surface v pole count> = <int>;
<B-spline surface v pole count> = <int>;
<B-spline surface v multiplicity knot count> = <int>;
<B-spline surface v multiplicity knot count> = <int>;
```

```
<B-spline surface weight poles> =
(<B-spline surface weight pole group> <_\n>) ^ <B-spline surface u pole count>;

<B-spline surface weight pole group> =
(<B-spline surface weight pole> <_>) ^ <B-spline surface v pole count>;

<B-spline surface weight pole> = <3D point> [<_> <real>];

<B-spline surface u multiplicity knots> =
(<B-spline surface u multiplicity knot> <_\n>) ^ <B-spline surface u multiplicity knot>;

<B-spline surface u multiplicity knot> = <real> <_> <int>;

<B-spline surface v multiplicity knot> =
(<B-spline surface v multiplicity knot> <_\n>) ^ <B-spline surface v multiplicity knot> = <real> <_> <int>;
```

Description

<surface record 9> describes a B-spline surface. The surface data consist of a u rational flag r_U , v rational flag r_V , u degree $m_u \le 25$, v degree $m_v \le 25$, u pole count $n_u \ge 2$, v pole count $n_v \ge 2$, u multiplicity knot count k_U , v multiplicity knots, v multiplicity knots.

The weight poles are $n_u \cdot n_v$ 3D points $B_{i,j}$ $((i,j) \in \{1,...,n_u\} \times \{1,...,n_v\})$ if $r_u + r_v = 0$. The weight poles are $n_u \cdot n_v$ pairs $B_{i,j}h_{i,j}$ $((i,j) \in \{1,...,n_u\} \times \{1,...,n_v\})$ if $r_u + r_v \neq 0$. Here $B_{i,j}$ is a 3D point and $h_{i,j}$ is a positive real $((i,j) \in \{1,...,n_u\} \times \{1,...,n_v\})$. $h_{i,j} = 1$ $((i,j) \in \{1,...,n_u\} \times \{1,...,n_v\})$ if $r_u + r_v = 0$.

The u multiplicity knots are k_U pairs $u_1q_1...u_{k_n}q_{k_u}$. Here u_i is a knot with multiplicity $q_i \ge 1$ $(1 \le i \le k_u)$ so that

$$u_i < u_{i+1} \ (1 \le i \le k_u - 1), q_1 \le m_u + 1, \ q_{k_u} \le m_u + 1, \ q_i \le m_u \ (2 \le i \le k_u - 1), \ \sum_{i=1}^{k_u} q_i = m_u + n_u + 1.$$

The v multiplicity knots are k_V pairs $v_1 t_1 \dots v_{k_v} t_k$. Here v_i is a knot with multiplicity $t_i \ge 1$ $(1 \le i \le k_v)$ so that

$$v_j < v_{j+1} \ (1 \le j \le k_v - 1), t_1 \le m_v + 1, \ t_{k_v} \le m_v + 1, \ t_j \le m_v \ (2 \le j \le k_v - 1), \ \sum_{j=1}^{k_v} t_j = m_v + n_v + 1.$$

The B-spline surface is defined by the following parametric equation:

$$S(u,v) = \frac{\sum_{i=1}^{n_u} \sum_{j=1}^{n_v} B_{i,j} \cdot h_{i,j} \cdot N_{i,m_u+1}(u) \cdot M_{j,m_v+1}(v)}{\sum_{i=1}^{n_u} \sum_{j=1}^{n_v} h_{i,j} \cdot N_{i,m_u+1}(u) \cdot M_{j,m_v+1}(v)}, (u,v) \in [u_1, u_{k_u}] \times [v_1, v_{k_v}]$$

where functions $N_{i,j}$ and $M_{i,j}$ have the following recursion definition by j:

$$\begin{split} N_{i,1}(u) &= \left\{1 \Leftarrow \bar{u}_i \leq u \leq \bar{u}_{i+1} 0 \Leftarrow u < \bar{u}_i \vee \bar{u}_{i+1} \leq u \right., \\ N_{i,j}(u) &= \frac{(u - \bar{u}_i) \cdot N_{i,j-1}(u)}{\bar{u}_{i+j-1} - \bar{u}_i} + \frac{(\bar{u}_{i+j} - u) \cdot N_{i+1,j-1}(u)}{\bar{u}_{i+j} - \bar{u}_{i+1}}, \ (2 \leq j \leq m_u + 1), \\ M_{i,1}(v) &= \left\{1 \Leftarrow \bar{v}_i \leq v \leq \bar{v}_{i+1} \\ 0 \Leftarrow v < \bar{v}_i \vee \bar{v}_{i+1} \leq v \right., \\ M_{i,j}(v) &= \frac{(v - \bar{v}_i) \cdot M_{i,j-1}(v)}{\bar{v}_{i+j-1} - \bar{v}_i} + \frac{(\bar{v}_{i+j} - v) \cdot M_{i+1,j-1}(v)}{\bar{v}_{i+j} - \bar{v}_{i+1}}, \ (2 \leq j \leq m_v + 1); \end{split}$$

where

$$\bar{u}_i = u_j \ (1 \le j \le k_u, \sum_{l=1}^{j-1} q_l \le i \le \sum_{l=1}^{j} q_l), \bar{v}_i = v_j \ (1 \le j \le k_v, \sum_{l=1}^{j-1} t_l \le i \le \sum_{l=1}^{j} t_l);$$

The example record is interpreted as a B-spline surface with a u rational flag r_U =1, v rational flag r_V =1, u degree m_U =1, v degree m_V =1, u pole count n_U =3, v pole count n_V =2, u multiplicity knot count k_U =5, v multiplicity knot

count k_V =4, weight poles $B_{1,1}$ =(0, 0, 1), $h_{1,1}$ =7, $B_{1,2}$ =(1, 0, -4), $h_{1,2}$ =10, $B_{2,1}$ =(0, 1, -2), $h_{2,1}$ =8, $B_{2,2}$ =(1, 1, 5), $h_{2,2}$ =11, $B_{3,1}$ =(0, 2, 3), $h_{3,1}$ =9and $B_{3,2}$ =(1, 2, 6), $h_{3,2}$ =12, u multiplicity knots u_1 =0, q_1 =1, u_2 =0.25, q_2 =1, u_3 =0.5, q_3 =1, u_4 =0.75, q_4 =1 and u_5 =1, q_5 =1, v multiplicity knots v_1 =0, r_1 =1, r_2 =0.3, r_2 =1, r_3 =0.7, r_3 =1and r_4 =1. The B-spline surface is defined by the following parametric equation:

```
\begin{split} S(u,v) &= \left[ (0,0,1) \cdot 7 \cdot N_{1,2}(u) \cdot M_{1,2}(v) + (1,0,-4) \cdot 10 \cdot N_{1,2}(u) \cdot M_{2,2}(v) + \right. \\ & \left. (0,1,-2) \cdot 8 \cdot N_{2,2}(u) \cdot M_{1,2}(v) + (1,1,5) \cdot 11 \cdot N_{2,2}(u) \cdot M_{2,2}(v) + \right. \\ & \left. (0,2,3) \cdot 9 \cdot N_{3,2}(u) \cdot M_{1,2}(v) + (1,2,6) \cdot 12 \cdot N_{3,2}(u) \cdot M_{2,2}(v) \right] \vdots \\ & \left. \left[ 7 \cdot N_{1,2}(u) \cdot M_{1,2}(v) + 10 \cdot N_{1,2}(u) \cdot M_{2,2}(v) + 8 \cdot N_{2,2}(u) \cdot M_{1,2}(v) + \right. \\ & \left. 11 \cdot N_{2,2}(u) \cdot M_{2,2}(v) + 9 \cdot N_{3,2}(u) \cdot M_{1,2}(v) + 12 \cdot N_{3,2}(u) \cdot M_{2,2}(v) \right] \end{split}
```

4.2.10 Rectangular Trim Surface - < surface record 10 >

Example

```
10 -1 2 -3 4
1 1 2 3 0 0 1 1 0 -0 -0 1 0
```

BNF-like Definition

```
<surface record 10> = "10" <_> <trim surface u min> <_> <trim surface u max> <_>
<trim surface v min> <_> <trim surface v max> <_\n> <surface record>;
<trim surface u min> = <real>;
<trim surface u max> = <real>;
<trim surface v min> = <real>;
<trim surface v max> = <real>;
```

Description

<surface record 10> describes a rectangular trim surface. The surface data consist of reals u_{min} , u_{max} , v_{min} and v_{max} and a <surface record> so that $u_{min} < u_{max}$ and $v_{min} < v_{max}$. The rectangular trim surface is a restriction of the base surface Bdescribed in the record to the set $[u_{min}, u_{max}] \times [v_{min}, v_{max}] \subseteq domain(B)$. The rectangular trim surface is defined by the following parametric equation:

$$S(u,v) = B(u,v), (u,v) \in [u_{min}, u_{max}] \times [v_{min}, v_{max}].$$

The example record is interpreted as a rectangular trim surface to the set [-1, 2]x[-3, 4]for the base surface $B(u,v) = (1,2,3) + u \cdot (1,0,0) + v \cdot (0,1,0)$. The rectangular trim surface is defined by the following parametric equation: $B(u,v) = (1,2,3) + u \cdot (1,0,0) + v \cdot (0,1,0), (u,v) \in [-1,2] \times [-3,4].$

4.2.11 Offset Surface - < surface record 11 >

Example

```
11 -2
1 1 2 3 0 0 1 1 0 -0 -0 1 0
```

```
<surface record 11> = "11" <_> <surface record distance> <_\n> <surface record>;<surface record distance> = <real>;
```

Description

<surface record 11> describes an offset surface. The offset surface data consist of a distance dand a <surface record>. The offset surface is the result of offsetting the base surface B described in the record to the distance dalong the normal Nof surface B. The offset surface is defined by the following parametric equation:

$$S(u,v) = B(u,v) + d \cdot N(u,v), \ (u,v) \in domain(B). \\ N(u,v) = [S'_u(u,v), S'_v(u,v)]$$
 if $[S'_u(u,v), S'_v(u,v)] \neq \vec{0}$.

The example record is interpreted as an offset surface with a distance d=-2and base surface $B(u,v)=(1,2,3)+u\cdot(1,0,0)+v\cdot(0,1,0)$. The offset surface is defined by the following parametric equation: $S(u,v)=(1,2,3)+u\cdot(1,0,0)+v\cdot(0,1,0)-2\cdot(0,0,1)$.

4.3 2D curves

Example

```
Curve2ds 24
1 0 0 1 0
1 0 0 1 0
1 3 0 0 -1
1 0 0 0 1
1 0 -2 1 0
1 0 0 1 0
1 0 0 0 -1
1 0 0 0 1
1 0 0 1 0
1 0 1 1 0
1 3 0 0 -1
1 1 0 0 1
1 0 -2 1 0
1 0 1 1 0
1 0 0 0 -1
1 1 0 0 1
1 0 0 0 1
1 0 0 1 0
1 3 0 0 1
1 0 0 1 0
1 0 0 0 1
1 0 2 1 0
1 3 0 0 1
1 0 2 1 0
```

```
<2D curves> = <2D curve header> <_\n> <2D curve records>;
<2D curve header> = "Curve2ds" <_> <2D curve count>;
<2D curve count> = <int>;
<2D curve records> = <2D curve record> ^ <2D curve count>;
<2D curve record = <2D curve record 1> |
<2D curve record 2> |
<2D curve record 3> |
<2D curve record 4> |
<2D curve record 5> |
<2D curve record 5> |
<2D curve record 6> |
<2D curve record 7> |
<2D curve record 8> |
<2D curve record 8> |
<2D curve record 9>;
```

4.3.1 Line - <2D curve record 1>

Example

```
1 3 0 0 -1
```

BNF-like Definition

```
<2D curve record 1> = "1" <_> <2D point> <_> <2D direction> <_\n>;
```

Description

<2D curve record 1> describes a line. The line data consist of a 2D point *P*and a 2D direction *D*. The line passes through the point *P*, has the direction *D*and is defined by the following parametric equation:

$$C(u) = P + u \cdot D, u \in (-\infty, \infty).$$

The example record is interpreted as a line which passes through a point P=(3,0), has a direction D=(0,-1) and is defined by the following parametric equation: $C(u)=(3,0)+u\cdot(0,-1)$.

4.3.2 Circle - <2D curve record 2>

Example

```
2 1 2 1 0 -0 1 3
```

BNF-like Definition

```
<2D curve record 2> = "2" <_> <2D circle center> <_> <2D circle Dx> <_> <2D circle Dy> <_> <2D circle
    radius> <_\n>;

<2D circle center> = <2D point>;

<2D circle Dx> = <2D direction>;

<2D circle Dy> = <2D direction>;

<2D circle radius> = <real>;
```

Description

<2D curve record 2> describes a circle. The circle data consist of a 2D point P, orthogonal 2D directions D_X and D_Y and a non-negative real r. The circle has a center P. The circle plane is parallel to directions D_X and D_Y . The circle has a radius r and is defined by the following parametric equation:

$$C(u) = P + r \cdot (cos(u) \cdot D_x + sin(u) \cdot D_y), u \in [0, 2 \cdot \pi).$$

The example record is interpreted as a circle which has a center P=(1,2). The circle plane is parallel to directions $D_X=(1,0)$ and $D_Y=(0,1)$. The circle has a radius r=3 and is defined by the following parametric equation: $C(u)=(1,2)+3\cdot(cos(u)\cdot(1,0)+sin(u)\cdot(0,1))$.

4.3.3 Ellipse - <2D curve record 3>

Example

```
3 1 2 1 0 -0 1 4 3
```

```
<2D curve record 3> = "3" <_> <2D ellipse center> <_> <2D ellipse Dmaj> <_>
<2D ellipse Dmin> <_> <2D ellipse Rmaj> <_> <2D ellipse Rmin> <_\n>;
<2D ellipse center> = <2D point>;
<2D ellipse Dmaj> = <2D direction>;
<2D ellipse Dmin> = <2D direction>;
<2D ellipse Rmaj> = <real>;
<2D ellipse Rmin> = <real>;
```

Description

<2D curve record 3> describes an ellipse. The ellipse data are 2D point P, orthogonal 2D directions D_{maj} and D_{min} and non-negative reals r_{maj} and r_{min} that $r_{maj} \leq r_{min}$. The ellipse has a center P, major and minor axis directions D_{maj} and D_{min} , major and minor radii P_{maj} and P_{min} and is defined by the following parametric equation:

$$C(u) = P + r_{maj} \cdot cos(u) \cdot D_{maj} + r_{min} \cdot sin(u) \cdot D_{min}, \ u \in [0, 2 \cdot \pi).$$

The example record is interpreted as an ellipse which has a center P=(1,2), major and minor axis directions $D_{maj}=(1,0)$ and $D_{min}=(0,1)$, major and minor radii $r_{maj}=4$ and $r_{min}=3$ and is defined by the following parametric equation: $C(u)=(1,2)+4\cdot cos(u)\cdot (1,0)+3\cdot sin(u)\cdot (0,1)$.

4.3.4 Parabola - <2D curve record 4>

Example

```
4 1 2 1 0 -0 1 16
```

BNF-like Definition

```
<2D curve record 4> = "4" <_> <2D parabola origin> <_> <2D parabola Dx> <_>
<2D parabola Dy> <_> <2D parabola focal length> <_\n>;
<2D parabola origin> = <2D point>;
<2D parabola Dx> = <2D direction>;
<2D parabola Dy> = <2D direction>;
<2D parabola focal length> = <real>;
```

Description

<2D curve record 4> describes a parabola. The parabola data consist of a 2D point P, orthogonal 2D directions D_X and D_Y and a non-negative real f. The parabola coordinate system has its origin P and axis directions D_X and D_Y . The parabola has a focus length f and is defined by the following parametric equation:

$$C(u) = P + \frac{u^2}{4 \cdot f} \cdot D_x + u \cdot D_y, \ u \in (-\infty, \infty) \iff f \neq 0; C(u) = P + u \cdot D_x, \ u \in (-\infty, \infty) \iff f = 0 \ (degenerated \ case).$$

The example record is interpreted as a parabola in plane which passes through a point P=(1,2) and is parallel to directions $D_X=(1,0)$ and $D_Y=(0,1)$. The parabola has a focus length f=16 and is defined by the following parametric equation: $C(u)=(1,2)+\frac{u^2}{64}\cdot(1,0)+u\cdot(0,1)$.

4.3.5 Hyperbola - <2D curve record 5>

Example

51210-0134

BNF-like Definition

```
<2D curve record 5> = "5" <_> <2D hyperbola origin> <_> <2D hyperbola Dx> <_>
<2D hyperbola Dy> <_> <2D hyperbola Kx> <_> <2D hyperbola Ky> <_\n>;
<2D hyperbola origin> = <2D point>;
<2D hyperbola Dx> = <2D direction>;
<2D hyperbola Dy> = <2D direction>;
<2D hyperbola Kx> = <real>;
<2D hyperbola Ky> = <real>;
```

Description

<2D curve record 5> describes a hyperbola. The hyperbola data consist of a 2D point P, orthogonal 2D directions D_X and D_Y and non-negative reals k_X and k_Y . The hyperbola coordinate system has origin P and axis directions D_X and D_Y . The hyperbola is defined by the following parametric equation:

$$C(u) = P + k_x \cdot cosh(u)D_x + k_y \cdot sinh(u) \cdot D_y, \ u \in (-\infty, \infty).$$

The example record is interpreted as a hyperbola with coordinate system which has origin P=(1,2) and axis directions $D_X=(1,0)$ and $D_Y=(0,1)$. Other data for the hyperbola are $k_X=5$ and $k_Y=4$. The hyperbola is defined by the following parametric equation: $C(u)=(1,2)+3\cdot cosh(u)\cdot (1,0)+4\cdot sinh(u)\cdot (0,1)$.

4.3.6 Bezier Curve - <2D curve record 6>

Example

```
6 1 2 0 1 4 1 -2 5 2 3 6
```

BNF-like Definition

```
<2D curve record 6> = "6" <_> <2D Bezier rational flag> <_> <2D Bezier degree>
<2D Bezier weight poles> <_\n>;
<2D Bezier rational flag> = <flag>;
<2D Bezier degree> = <int>;
<2D Bezier weight poles> = (<_> <2D Bezier weight pole>) ^ (<2D Bezier degree> <+> "1");
<2D Bezier weight pole> = <2D point> [<_> <real>];
```

Description

<2D curve record 6> describes a Bezier curve. The curve data consist of a rational flag r, a degree $m \le 25$ and weight poles.

The weight poles are m+12D points B_0 ... B_m if the flag is 0. The weight poles are m+1 pairs B_0 h_0 ... B_m h_m if the flag is 1. Here B_i is a 2D point and h_i is a positive real $(0 \le i \le m)$. $h_i = 1$ $(0 \le i \le m)$ if the flag is 0.

The Bezier curve is defined by the following parametric equation:

$$C(u) = \frac{\sum_{i=0}^{m} B_i \cdot h_i \cdot C_m^i \cdot u^i \cdot (1-u)^{m-i}}{\sum_{i=0}^{m} h_i \cdot C_m^i \cdot u^i \cdot (1-u)^{m-i}}, \ u \in [0,1]$$

where $0^0 \equiv 1$.

The example record is interpreted as a Bezier curve with a rational flag r=1, a degree m=2 and weight poles $B_0 = (0,1)$, $h_0 = 4$, $B_1 = (1,-2)$, $h_1 = 5$ and $B_2 = (2,3)$, $h_2 = 6$. The Bezier curve is defined by the following parametric equation:

$$C(u) = \frac{(0,1) \cdot 4 \cdot (1-u)^2 + (1,-2) \cdot 5 \cdot 2 \cdot u \cdot (1-u) + (2,3) \cdot 6 \cdot u^2}{4 \cdot (1-u)^2 + 5 \cdot 2 \cdot u \cdot (1-u) + 6 \cdot u^2}.$$

4.3.7 B-spline Curve - <2D curve record 7>

Example

```
7 1 0 1 3 5 0 1 4 1 -2 5 2 3 6 0 1 0.25 1 0.5 1 0.75 1 1 1
```

BNF-like Definition

Description

<2D curve record 7> describes a B-spline curve. The curve data consist of a rational flag r, a degree $m \le 25$, a pole count $n \ge 2$, a multiplicity knot count k, weight poles and multiplicity knots.

The weight poles are n2D points $B_1 \dots B_n$ if the flag n is 0. The weight poles are n pairs $B_1 h_1 \dots B_n h_n$ if the flag n is 1. Here B_i is a 2D point and h_i is a positive real $(1 \le i \le n)$. $h_i = 1$ $(1 \le i \le n)$ if the flag n is 0.

The multiplicity knots are kpairs $u_1 q_1 \dots u_k q_k$. Here u_i is a knot with multiplicity $q_i \ge 1 \ (1 \le i \le k)$ so that

$$u_i < u_{i+1} \ (1 \le i \le k-1), q_1 \le m+1, \ q_k \le m+1, \ q_i \le m \ (2 \le i \le k-1), \sum_{i=1}^k q_i = m+n+1.$$

The B-spline curve is defined by the following parametric equation:

$$C(u) = \frac{\sum_{i=1}^{n} B_i \cdot h_i \cdot N_{i,m+1}(u)}{\sum_{i=1}^{n} h_i \cdot N_{i,m+1}(u)}, \ u \in [u_1, \ u_k]$$

where functions $N_{i,j}$ have the following recursion definition by j

$$N_{i,1}(u) = \begin{cases} 1 \Leftarrow \bar{u}_i \leq u \leq \bar{u}_{i+1} \\ 0 \Leftarrow u < \bar{u}_i \vee \bar{u}_{i+1} \leq u \end{cases}, \ N_{i,j}(u) = \frac{(u - \bar{u}_i) \cdot N_{i,j-1}(u)}{\bar{u}_{i+j-1} - \bar{u}_i} + \frac{(\bar{u}_{i+j} - u) \cdot N_{i+1,j-1}(u)}{\bar{u}_{i+j} - \bar{u}_{i+1}}, \ (2 \leq j \leq m+1) \end{cases}$$

where

$$\bar{u}_i = u_j \ (1 \le j \le k, \sum_{l=1}^{j-1} q_l + 1 \le i \le \sum_{l=1}^{j} q_l).$$

The example record is interpreted as a B-spline curve with a rational flag r=1, a degree m=1, a pole count n=3, a multiplicity knot count k=5, weight poles $B_1=(0,1)$, $h_1=4$, $B_2=(1,-2)$, $h_2=5$ and $B_3=(2,3)$, $h_3=6$ and multiplicity knots $u_1=0$, $u_1=0$, $u_2=0.25$, $u_2=0.25$, $u_3=0.5$, $u_3=0.5$, $u_4=0.75$

$$C(u) = \frac{(0,1) \cdot 4 \cdot N_{1,2}(u) + (1,-2) \cdot 5 \cdot N_{2,2}(u) + (2,3) \cdot 6 \cdot N_{3,2}(u)}{4 \cdot N_{1,2}(u) + 5 \cdot N_{2,2}(u) + 6 \cdot N_{3,2}(u)}.$$

4.3.8 Trimmed Curve - <2D curve record 8>

Example

```
8 - 4 5
1 1 2 1 0
```

BNF-like Definition

```
<2D curve record 8> = "8" <_> <2D trimmed curve u min> <_> <2D trimmed curve u max> <_\n>
<2D curve record>;
<2D trimmed curve u min> = <real>;
<2D trimmed curve u max> = <real>;
```

Description

<2D curve record 8> describes a trimmed curve. The trimmed curve data consist of reals u_{min} and u_{max} and a <2D curve record> so that $u_{min} < u_{max}$. The trimmed curve is a restriction of the base curve Bdescribed in the record to the segment $[u_{min}, u_{max}] \subseteq domain(B)$. The trimmed curve is defined by the following parametric equation:

$$C(u) = B(u), u \in [u_{min}, u_{max}].$$

The example record is interpreted as a trimmed curve with u_{min} =-4, u_{max} =5and base curve $B(u) = (1,2) + u \cdot (1,0)$. The trimmed curve is defined by the following parametric equation: $C(u) = (1,2) + u \cdot (1,0)$, $u \in [-4,5]$.

4.3.9 Offset Curve - <2D curve record 9>

Example

```
9 2 1 1 2 1 0
```

BNF-like Definition

```
<2D curve record 9> = "9" <_> <2D offset curve distance> <_\n> <2D curve record>;
<2D offset curve distance> = <real>;
```

Description

<2D curve record 9> describes an offset curve. The offset curve data consist of a distance dand a <2D curve record>. The offset curve is the result of offsetting the base curve Bdescribed in the record to the distance dalong the vector $(B'_Y(u), -B'_X(u)) \neq \vec{0}$ where $B(u) = (B'_X(u), B'_Y(u))$. The offset curve is defined by the following parametric equation:

$$C(u) = B(u) + d \cdot (B'_Y(u), -B'_X(u)), u \in domain(B).$$

The example record is interpreted as an offset curve with a distance d=2and base curve $B(u) = (1,2) + u \cdot (1,0)$ and is defined by the following parametric equation: $C(u) = (1,2) + u \cdot (1,0) + 2 \cdot (0,-1)$.

4.4 3D polygons 26

4.4 3D polygons

Example

```
Polygon3D 1 2 1 0.1 1 0 0 2 0 0 0 0 1
```

BNF-like Definition

```
<3D polygons> = <3D polygon header> <_\n> <3D polygon records>;

<3D polygon header> = "Polygon3D" <_> <3D polygon record count>;

<3D polygon records> = <3D polygon record> ^ <3D polygon record count>;

<3D polygon node count> <_> <3D polygon flag of parameter presence> <_\n> <3D polygon nodes> <_\n> (3D polygon nodes> <_\n> (3D polygon parameters> <_\n);

<3D polygon node count> = <int>;

<3D polygon flag of parameter presence> = <flag>;

<3D polygon deflection> = <real>;

<3D polygon nodes> = (<3D polygon node> <_>) ^ <3D polygon node count>;

<3D polygon node> = <3D point>;

<3D polygon u parameters> = (<3D polygon u parameter> <_>) ^ <3D polygon u parameter> = <real>;
```

Description

<3D polygons> record describes a 3D polyline Lwhich approximates a 3D curve C. The polyline data consist of a node count $m \geq 2$, a parameter presence flag p, a deflection $d \geq 0$, nodes N_i $(1 \leq i \leq m)$ and parameters u_i $(1 \leq i \leq m)$. The parameters are present only if p=1. The polyline Lpasses through the nodes. The deflection ddescribes the deflection of polyline Lfrom the curve C:

$$\max_{P \in C} \min_{Q \in L} |Q - P| \le d.$$

The parameter u_i $(1 \le i \le m)$ is the parameter of the node N_i on the curve C:

$$C(u_i) = N_i$$
.

The example record describes a polyline from m=2nodes with a parameter presence flag p=1, a deflection d=0.1, nodes N_1 =(1,0,0)and N_2 =(2,0,0)and parameters u_1 =0and u_2 =1.

4.5 Triangulations

Example

```
Triangulations 6
4 2 1 0
0 0 0 0 0 3 0 2 3 0 2 0 0 0 3 0 3 -2 0 -2 2 4 3 2 1 4
4 2 1 0
0 0 0 1 0 0 1 0 3 0 0 3 0 0 0 1 3 1 3 0 3 2 1 3 1 4
```

4.5 Triangulations 27

```
      4
      2
      1
      0
      0
      0
      0
      0
      0
      0
      0
      0
      0
      0
      0
      0
      0
      0
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      0
      0
```

BNF-like Definition

```
<triangulations> = <triangulation header> <_\n> <triangulation records;
<triangulation header> = "Triangulations" <_> <triangulation count>;
<triangulation records> = <triangulation record> ^ <triangulation count>;
<triangulation record> = <triangulation node count> <_> <triangulation triangle count> <_> <triangulation parameter presence flag> <_> <triangulation deflection> <_\n> <triangulation nodes> [<_> <triangulation u v parameters>] <_> <triangulation triangles> <_\n>;
<triangulation node count> = <int>;
<triangulation triangle count> = <int>;
<triangulation parameter presence flag> = <flag>;
<triangulation deflection> = <real>;
<triangulation node> = <3D point>;
<triangulation u v parameters> = (<triangulation u v parameter pair> <_>) ^ <triangulation node count>;
<triangulation u v parameter pair> = <real> <_> <real>;
<triangulation triangles> = (<triangulation triangle> <_>) ^ <triangulation triangle count>;
<triangulation triangle> = <int> <_> <int> <_> <int> <_>
```

Description

<triangulation record> describes a triangulation Twhich approximates a surface S. The triangulation data consist of a node count $m \geq 3$, a triangle count $k \geq 1$, a parameter presence flag p, a deflection $d \geq 0$, nodes N_i $(1 \leq i \leq m)$, parameter pairs u_i v_i $(1 \leq i \leq m)$, triangles $n_{j,1}$ $n_{j,2}$ $n_{j,3}$ $(1 \leq j \leq k, n_{j,l} \in \{1,...,m\} \ (1 \leq l \leq 3))$. The parameters are present only if p=1. The deflection describes the triangulation deflection from the surface:

$$\max_{P \in S} \min_{Q \in T} |Q - P| \leq d.$$

The parameter pair u_i v_i $(1 \le i \le m)$ describes the parameters of node N_i on the surface:

$$S(u_i, v_i) = N_i$$
.

The triangle $n_{j,1}$ $n_{j,2}$ $n_{j,3}$ $(1 \le j \le k)$ is interpreted as a triangle of nodes $N_{n_j,1}$ $N_{n_j,2}$ and $N_{n_j,3}$ with circular traversal of the nodes in the order $N_{n_j,1}$ $N_{n_j,2}$ and $N_{n_j,3}$. From any side of the triangulation Tall its triangles have the same direction of the node circular traversal: either clockwise or counterclockwise.

Triangulation record

```
4 2 1 0
0 0 0 0 0 3 0 2 3 0 2 0 0 0 3 0 3 -2 0 -2 2 4 3 2 1 4
```

describes a triangulation with m=4nodes, k=2triangles, parameter presence flag p=1, deflection d=0, nodes N_1 =(0,0,0), N_2 =(0,0,3), N_3 =(0,2,3) and N_4 =(0,2,0), parameters (u_1 , v_1)=(0,0), (u_2 , v_2)=(3,0), (u_3 , v_3)=(3,-2)and (u_4 , v_4)=(0,-2), and triangles ($n_{1,1}$, $n_{1,2}$, $n_{1,3}$)=(2,4,3)and ($n_{2,1}$, $n_{2,2}$, $n_{2,3}$)=(2,1,4). From the point (1,0,0) ((-1,0,0)) the triangles have clockwise (counterclockwise) direction of the node circular traversal.

4.6 Polygons on triangulations

Example

```
PolygonOnTriangulations 24
2 1 2
p 0.1 1 0 3
2 1 4
p 0.1 1 0 3
2 2 3
p 0.1 1 0 2
2 1 2
p 0.1 1 0 2
2 4 3
p 0.1 1 0 3
2 1 4
p 0.1 1 0 3
2 1 4
p 0.1 1 0 2
2 1 2
p 0.1 1 0 2
2 1 2
p 0.1 1 0 3
2 2 3
p 0.1 1 0 3
2 2 3
p 0.1 1 0 2
2 4 3
p 0.1 1 0 2
2 4 3
p 0.1 1 0 3
2 2 3
p 0.1 1 0 3
2 1 4
p 0.1 1 0 2
2 4 3
p 0.1 1 0 2
2 1 2
p 0.1 1 0 1
2 1 4
p 0.1 1 0 1
2 4 3
p 0.1 1 0 1
2 1 4
p 0.1 1 0 1
2 1 2
p 0.1 1 0 1
2 2 3
p 0.1 1 0 1
2 4 3
p 0.1 1 0 1
2 2 3
p 0.1 1 0 1
```

```
<polygons on triangulations> = <polygons on triangulations header> <_\n>
<polygons on triangulations records>;

<polygons on triangulations " <_> <polygons on triangulations record count>;

<polygons on triangulations record count> = <int>;

<polygons on triangulations records> =
    <polygons on triangulations record> ^ <polygons on triangulations record> =
    <polygons on triangulations record> =
    <polygons on triangulations record> =
    <polygons on triangulations node count> <_> <polygons on triangulations node record> =
    <polygons on triangulations node count> <_> <polygons on triangulations node record> <polygons on triangulations parameter presence flag>
```

Description

<polygons on triangulations> describes a polyline L on a triangulation which approximates a curve C. The polyline data consist of a node count $m \geq 2$, node numbers $n_i \geq 1$, deflection $d \geq 0$, a parameter presence flag p and parameters u_i $(1 \leq i \leq m)$. The parameters are present only if p=1. The deflection d describes the deflection of polyline L from the curve C:

$$\max_{P \in C} \min_{Q \in L} \lvert Q - P \rvert \leq d.$$

Parameter u_i $(1 \le i \le m)$ is n_i -th node $C(u_i)$ parameter on curve C.

4.7 Geometric Sense of a Curve

Geometric sense of curve Cdescribed above is determined by the direction of parameter uincreasing.

5 Shapes 30

5 Shapes

An example of section shapes and a whole *.brep file are given in chapter 7 Appendix (p. 35).

BNF-like Definition

```
<shapes> = <shape header> <_\n> <shape records> <_\n> <shape final record>;
<shape header> = "TShapes" <_> <shape count>;
<shape count> = <int>;
<shape records> = <shape record> ^ <shape count>;
<shape record> = <shape subrecord> <_\n> <shape flag word> <_\n> <shape subshapes> <_\n>;
<shape flag word> = <flag> ^ 7;
<shape subshapes> = (<shape subshape> <_>) * "*";
<shape > =
<shape subshape orientation> <shape subshape number> <_> <shape location number>;
<shape subshape orientation> = "+" | "-" | "i" | "e";
<shape subshape number> = <int>;
<shape location number> = <int>;
<shape final record> = <shape subshape>;
<shape subrecord> =
("Ve" <_\n> <vertex data> <_\n>) |
("Ed" <_\n> <edge data> <_\n>) |
("Wi" <_\n> <_\n>) |
("Fa" <_\n> <face data>) |
("Sh" <_\n> <_\n>) |
("So" <_\n> <_\n>)
("CS" <_\n> <_\n>) |
("Co" <_\n> <_\n>);
```

Description

<shape flag word> f_1 f_2 f_3 f_4 f_5 f_6 f_7 <flag>s f_i $(1 \le i \le 7)$ are interpreted as shape flags in the following way:

- f_1 -free;
- f_2 modified;
- f_3 IGNORED(version 1) \ checked (version 2);
- f_4 orientable;
- f_5 -closed;
- f_6 infinite;
- *f*₇- convex.

The flags are used in a special way [1].

<shape subshape orientation> is interpreted in the following way:

- + forward;
- – reversed;
- i internal;

5.1 Common Terms 31

· e - external.

<shape subshape orientation> is used in a special way [1].

<shape subshape number> is the number of a <shape record> which is located in this section above the <shape subshape number>. <shape record> numbering is backward and starts from 1.

<shape subrecord> types are interpreted in the following way:

```
"Ve" – vertex;
```

- "Ed" edge;
- "Wi" wire;
- "Fa" face;
- · "Sh" shell;
- "So" solid;
- · "CS" compsolid;
- "Co" compound.

<shape final record> determines the orientation and location for the whole model.

5.1 Common Terms

The terms below are used by <vertex data>, <edge data> and <face data>.

BNF-like Definition

```
<location number> = <int>;
<3D curve number> = <int>;
<surface number> = <int>;
<2D curve number> = <int>;
<3D polygon number> = <int>;
<triangulation number> = <int>;
<polygon on triangulation number> = <int>;
<curve parameter minimal and maximal values> = <real> <_> <real>;
<curve values for parameter minimal and maximal values> = real> <_> <real> <_> </real>
```

Description

<location number> is the number of <location record> from section locations. <location record> numbering
starts from 1. <location number> 0 is interpreted as the identity location.

<3D curve number> is the number of a <3D curve record> from subsection <3D curves> of section <geometry>. <3D curve record> numbering starts from 1.

<surface number> is the number of a <surface record> from subsection <surfaces> of section <geometry>. <surface record> numbering starts from 1.

<2D curve number> is the number of a <2D curve record> from subsection <2D curves> of section <geometry>. <2D curve record> numbering starts from 1.

5.2 Vertex data 32

<3D polygon number> is the number of a <3D polygon record> from subsection <3D polygons> of section <9eometry>. <3D polygon record> numbering starts from 1.

- <triangulation number> is the number of a <triangulation record> from subsection <triangulations> of section <geometry>. <triangulation record> numbering starts from 1.
- <polygon on triangulation> number is the number of a <polygons on triangulations record> from subsection
 <polygons on triangulations> of section <geometry>. <polygons on triangulations record> numbering starts
 from 1.
- <curve parameter minimal and maximal values> u_{min} and u_{max} are the curve parameter u bounds: $u_{min} \le u \le u_{max}$.
- <curve values for parameter minimal and maximal values> u_{min} and u_{max} are real pairs x_{min} y_{min} and x_{max} y_{max} that $(x_{min}, y_{min}) = C(u_{min})$ and $(x_{max}, y_{max}) = C(u_{max})$ where C is a parametric equation of the curve.

5.2 Vertex data

BNF-like Definition

```
<vertex data> = <vertex data tolerance> <_\n> <vertex data 3D representation> <_\n>
<vertex data representations>;
<vertex data tolerance> = <real>;
<vertex data 3D representation> = <3D point>;
<vertex data representations> = (<vertex data representation> <_\n>) * "0 0";
<vertex data representation> = <vertex data representation u parameter> <_>
<vertex data representation data> <_> <location number>;
<vertex data representation u parameter> = <real>;
<vertex data representation data> =
("1" <_> <vertex data representation data 1>) |
("2" <_> <vertex data representation data 2>) |
("3" <_> <vertex data representation data 3>);
<vertex data representation data 1> = <3D curve number>;
<vertex data representation data 2> = <2D curve number> <_> <surface number>;
<vertex data representation data 3> =
<vertex data representation v parameter> <_> <surface number>;
<vertex data representation v parameter> = <real>;
```

Description

The usage of <vertex data representation u parameter> *U*is described below.

- <vertex data representation data 1> and parameter Udescribe the position of the vertex Von a 3D curve C. Parameter Uis a parameter of the vertex Von the curve C: C(u)=V.
- <vertex data representation data 2> and parameter Udescribe the position of the vertex Von a 2D curve Cwhich is located on a surface. Parameter Uis a parameter of the vertex Von the curve C: C(u)=V.
- <vertex data representation data 3> and parameter udescribe the position of the vertex Von a surface Sthrough < vertex data representation v parameter > v: S(u,v)=V.
- <vertex data tolerance> tdescribes the maximum distance from the vertex Vto the set R of vertex Vrepresentations:

$$\max_{P \in R} |P - V| \le t$$
.

5.3 Edge data 33

5.3 Edge data

BNF-like Definition

```
<edge data> = <_> <edge data tolerance> <_> <edge data same parameter flag> <_> edge data same range flag>
      <_> <edge data degenerated flag> <_\n> <edge data representations>;
<edge data tolerance> = <real>;
<edge data same parameter flag> = <flag>;
<edge data same range flag> = <flag>;
<edge data degenerated flag> = <flag>;
<edge data representations> = (<edge data representation> <_\n>) * "0";
<edge data representation> =
    <_> <edge data representation data 1>
"2" <_> <edge data representation data 2>
"3" <_> <edge data representation data 3>
"4" <_> <edge data representation data 4>
"5" <_> <edge data representation data 5>
"6" <_> <edge data representation data 6>
"7" <_> <edge data representation data 7>;
<edge data representation data 1> = <3D curve number> <_> <location number> <</pre>
<curve parameter minimal and maximal values>;
<edge data representation data 2> = <2D curve number> < > <surface number> < >
<location number> <_> <curve parameter minimal and maximal values>
[<\_\n> < curve values for parameter minimal and maximal values>];
<edge data representation data 3> = (<2D curve number> <_>) ^ 2 <continuity order> <_> <surface number> <_>
       <location number> <_> <curve parameter minimal and maximal values> <\n> <curve values for parameter minimal</pre>
      and maximal values>1:
<continuity order> = "C0" | "C1" | "C2" | "C3" | "CN" | "G1" | "G2".
<edge data representation data 4> =
<continuity order> (<_> <surface number> <_> <location number>) ^ 2;
<edge data representation data 5> = <3D polygon number> <_> <location number>;
<edge data representation data 6> =
<polygon on triangulation number> <_> <triangulation number> <_> <location number>;
<edge data representation data 7> = (<polygon on triangulation number> <_>) ^ 2
<triangulation number> <_> <location number>;
```

Description

Flags <edge data same parameter flag>, <edge data same range flag> and <edge data degenerated flag> are used in a special way [1].

- <edge data representation data 1> describes a 3D curve.
- <edge data representation data 2> describes a 2D curve on a surface. <curve values for parameter minimal and maximal values> are used only in version 2.
- <edge data representation data 3> describes a 2D curve on a closed surface. <curve values for parameter minimal and maximal values> are used only in version 2.
- <edge data representation data 5> describes a 3D polyline.
- <edge data representation data 6> describes a polyline on a triangulation.
- <edge data tolerance> tdescribes the maximum distance from the edge E to the set Rof edge Erepresentations:

$$\max_{C \in R} \max_{P \in E} \min_{Q \in C} |Q - P| \le t$$

5.4 Face data

5.4 Face data 34

```
<face data = <face data natural restriction flag> <_> <face data tolerance> <_> <surface number> <_> < location number> <\n> ["2" <_> <triangulation number>];

<face data natural restriction flag> = <flag>;

<face data tolerance> = <real>;
```

Description

<face data> describes a surface Sof face F and a triangulation T of face F. The surface Smay be empty: \langle surface number> = 0.

<face data tolerance> tdescribes the maximum distance from the face Fto the surface S:

$$\max_{P \in F} \min_{Q \in S} |Q - P| \leq t$$

Flag < face data natural restriction flag> is used in a special way [1].

6 Appendix

This chapter contains a *.brep file example.

```
DBRep_DrawableShape
CASCADE Topology V1, (c) Matra-Datavision
Locations 3
1 0 0 0
0 1 0 0
1 0 0 4
0 1 0 5
0 0 1 6
2 1 1 2 1 0
Curve2ds 24
1 0 0 1 0
1 0 0 1 0
1 3 0 0 -1
1 0 0 0 1
1 0 -2 1 0
1 0 0 1 0
1 0 0 0 -1
1 0 0 0 1
1 0 0 1 0
1 0 1 1 0
1 3 0 0 -1
1 1 0 0 1
1 0 -2 1 0
1 0 1 1 0
1 0 0 0 -1
1 1 0 0 1
1 0 0 0 1
1 0 0 1 0
1 3 0 0 1
1 0 0 1 0
1 0 0 0 1
1 0 2 1 0
1 3 0 0 1
1 0 2 1 0
Curves 13
1 0 0 0 0 0 1
1 0 0 3 -0 1 0
1 0 2 0 0 0 1
1 0 0 0 -0 1 0
1 1 0 0 0 0 1
1 1 0 3 0 1 0
1 1 2 0 0 0 1
1 1 0 0 -0 1 0
1 0 0 0 1 0 -0
1 0 0 3 1 0 -0
1 0 2 0 1 0 -0
1 0 2 3 1 0 -0
1 1 0 0 1 0 0
Polygon3D 1
2 1
0.1
1 0 0 2 0 0
0 1
PolygonOnTriangulations 24
2 1 2
p 0.1 1 0 3
2 1 4
p 0.1 1 0 3
2 2 3
p 0.1 1 0 2
2 1 2
p 0.1 1 0 2
2 4 3
p 0.1 1 0 3
```

```
2 1 4
p 0.1 1 0 3
2 1 4
p 0.1 1 0 2
2 1 2
p 0.1 1 0 2
2 1 2
p 0.1 1 0 3
2 2 3
p 0.1 1 0 3
2 2 3
p 0.1 1 0 2
2 4 3
p 0.1 1 0 2
2 4 3
p 0.1 1 0 3
2 2 3
p 0.1 1 0 3
2 1 4
p 0.1 1 0 2
2 4 3
p 0.1 1 0 2
2 1 2
p 0.1 1 0 1
2 1 4
p 0.1 1 0 1
2 4 3
p 0.1 1 0 1
2 1 4
p 0.1 1 0 1
2 1 2
p 0.1 1 0 1
2 2 3
p 0.1 1 0 1
2 4 3
p 0.1 1 0 1
2 2 3
p 0.1 1 0 1
Surfaces 6
1 0 0 0 1 0 -0 0 0 1 0 -1 0
1 0 0 0 -0 1 0 0 0 1 1 0 -0
1 0 0 3 0 0 1 1 0 -0 -0 1 0
1 0 2 0 -0 1 0 0 0 1 1 0 -0
1 0 0 0 0 0 1 1 0 -0 -0 1 0
1 1 0 0 1 0 -0 0 0 1 0 -1 0
Triangulations 6
4 2 1 0
0 0 0 0 0 3 0 2 3 0 2 0 0 0 3 0 3 -2 0 -2 2 4 3 2 1 4
4 2 1 0
\begin{smallmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 3 & 0 & 0 & 3 & 0 & 0 & 0 & 1 & 3 & 1 & 3 & 0 & 3 & 2 & 1 & 3 & 1 & 4 \end{smallmatrix}
4 2 1 0
\begin{smallmatrix} 0 & 0 & 3 & 0 & 2 & 3 & 1 & 2 & 3 & 1 & 0 & 3 & 0 & 0 & 0 & 2 & 1 & 2 & 1 & 0 & 3 & 2 & 1 & 3 & 1 & 4 \end{smallmatrix}
4 2 1 0
\begin{smallmatrix} 0 & 2 & 0 & 1 & 2 & 0 & 1 & 2 & 3 & 0 & 2 & 3 & 0 & 0 & 0 & 1 & 3 & 1 & 3 & 0 & 3 & 2 & 1 & 3 & 1 & 4 \end{smallmatrix}
4 2 1 0
0 0 0 0 2 0 1 2 0 1 0 0 0 0 0 2 1 2 1 0 3 2 1 3 1 4
4 2 1 0
1 0 0 1 0 3 1 2 3 1 2 0 0 0 3 0 3 -2 0 -2 2 4 3 2 1 4
TShapes 39
Ve
1e-007
0 0 3
0 0
0101101
Ve
1e-007
0 0 0
0 0
0101101
```

```
Ed
1e-007 1 1 0
1 1 0 0 3
2 1 1 0 0 3
2 2 2 0 0 3
6 1 1 0
6 2 2 0
0101000
-39 0 +38 0 *
Ve
1e-007
0 2 3
0 0
0101101
1e-007 1 1 0
1 2 0 0 2
2 3 1 0 0 2
2 4 3 0 0 2
6 3 1 0
6 4 3 0
0
0101000
-36 0 +39 0 *
Ve
1e-007
0 2 0
0 0
0101101
Ed
1e-007 1 1 0
1 3 0 0 3
2 5 1 0 0 3
2 6 4 0 0 3
6 5 1 0
6 6 4 0
0
0101000
-36 0 +34 0 *
Ed
1e-007 1 1 0
1 4 0 0 2
2 7 1 0 0 2
2 8 5 0 0 2
6 7 1 0
6 8 5 0
0101000
-34 0 +38 0 *
0101000
-37 0 -35 0 +33 0 +32 0 *
Fa
0 1e-007 1 0
2 1
0101000
+31 0 *
Ve
1e-007
1 0 3
0 0
```

```
0101101
Ve
1e-007
1 0 0
0 0
0101101
Ed
1e-007 1 1 0
1 5 0 0 3
2 9 6 0 0 3
2 10 2 0 0 3
6 9 6 0
6 10 2 0
0
0101000
-29 0 +28 0 *
Ve
1e-007
1 2 3
0 0
0101101
1e-007 1 1 0
1 6 0 0 2
2 11 6 0 0 2
2 12 3 0 0 2
6 11 6 0
6 12 3 0
0101000
-26\ 0\ +29\ 0\ \star
Ve
1e-007
1 2 0
0 0
0101101
Ed
1e-007 1 1 0
1 7 0 0 3
2 13 6 0 0 3
2 14 4 0 0 3
6 13 6 0
6 14 4 0
0101000
-26 0 +24 0 *
Ed
1e-007 1 1 0
1 8 0 0 2
2 15 6 0 0 2
2 16 5 0 0 2
6 15 6 0
6 16 5 0
0
0101000
-24 \ 0 \ +28 \ 0 \ \star
Wi
0101000
-27\ 0\ -25\ 0\ +23\ 0\ +22\ 0\ \star
Fa
0 1e-007 6 0
```

```
2 6
0101000
+21 0 *
1e-007 1 1 0
1 9 0 0 1
2 17 2 0 0 1
2 18 5 0 0 1
6 17 2 0
6 18 5 0
0101000
-28 0 +38 0 *
Ed
1e-007 1 1 0
1 10 0 0 1
2 19 2 0 0 1
2 20 3 0 0 1
6 19 2 0
6 20 3 0
0
0101000
-29 0 +39 0 *
Wi
0101000
-19 0 -27 0 +18 0 +37 0 *
0 1e-007 2 0
2 2
0101000
+17 0 *
Ed
1e-007 1 1 0
1 11 0 0 1
2 21 4 0 0 1
2 22 5 0 0 1
6 21 4 0
6 22 5 0
0101000
-24 0 +34 0 *
Ed
1e-007 1 1 0
1 12 0 0 1
2 23 4 0 0 1
2 24 3 0 0 1
6 23 4 0
6 24 3 0
0101000
-26 0 +36 0 *
Wi
0101000
-15 0 -23 0 +14 0 +33 0 \star
Fa
0 1e-007 4 0
2 4
0101000
+13 0 *
Wi
0101000
-32 0 -15 0 +22 0 +19 0 *
Fa
0 1e-007 5 0
2 5
0101000
```

```
+11 0 *
Wi
0101000
-35 0 -14 0 +25 0 +18 0 *
0 1e-007 3 0
2 3
0101000
+9 0 *
Sh
0101100
-30\ 0\ +20\ 0\ -16\ 0\ +12\ 0\ -10\ 0\ +8\ 0\ \star
0100000
+7 0 *
CS
0101000
+6 3 *
Ve
1e-007
1 0 0
0 0
0101101
Ve
1e-007
2 0 0
0 0
0101101
Ed
1e-007 1 1 0
1 13 0 0 1
5 1 0
0101000
+4 0 -3 0 *
Со
1100000
+5 0 +2 0 *
+1 0
0
```