COMP7990 (Section 1 and Section 2)

Quiz

Write all your answers in your answer books

Question 1 (30 Marks)

1.1 (**10 Marks**) Suppose that we have the following data: [200, 300, 400, 600, 1000], normalize the data by min-max normalization by setting new min to 0 and new max to 1.

Answer: since
$$x_i' = \frac{(x_i - min)}{max - min} (max_{new} - min_{new}) + min_{new} = \frac{(x_i - 200)}{1000 - 200} 1 + 0$$
, the answer is $[0, 1/8, 1/4, 1/2, 1]$ (i.e., $[0, 0.125, 0.25, 0.5, 1]$).

1.2 (**10 Marks**) Suppose we have the following values for prices (already sorted in increasing order): [4, 10, 15, 21, 21, 22, 25, 28, 30, 31, 31, 32]. Use smoothing by bin means to smooth the above data using equal-width binning with 4 bins. Illustrate your steps.

Answer:

1. Compute the width of each bin: (32-4)/4 = 7.

2. Partition data into bins (equal-width):

Bin 1 ([4, 11)): [4, 10]

Bin 2 ([11, 18)): [15]

Bin 3 ([18, 25)): [21, 21, 22]

Bin 4 ([25, 32]): [25, 28, 30, 31, 31, 32]

3. Computing the mean of each bin:

Bin1: 7

Bin2: 15

Bin 3: 21.33

Bin 4: 29.5

4. Smoothing by mean

[7, 7, 15, 21.33, 21.33, 21.33, 29.5, 29.5, 29.5, 29.5, 29.5]

1.3 (10 Marks) In real-world data analytic problems, data with noisy values for some attributes is often occurred. Why noisy values are common in real-world application? Describe various methods for handling noisy data.

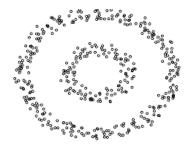
Answer: Noisy data may due to: (1) Errors in data collection devices; (2) Wrong input; and (3) Technology limitation. Methods for handling noisy data: (1) Binning; (2) Regression; and (3) Clustering.

Question 2 (40 Marks)

2.1 (**10 Marks**) Describe the classification process of *K*-nearest neighbor algorithm.

Answer: The classification processes of knn contains the following three steps:

- (1) Compute the distance between a test sample and each training samples
- (2) Sort by distances and get the k nearest neighbor of the test sample
- (3) Use majority vote to predict the class label of the test sample.
- 2.2 (10 Marks) Given the following dataset, will k-means work well on it? Explain your answer in detail.



Answer: k-means will **not work** well on this dataset. K-means works only if the clusters are round shaped. This data contains nonlinear structure that k means algorithm cannot capture.

2.3 (**10 Marks**) Explain the reason why the nonlinear activation function is required in a neural network model.

Answer: Without non linear activation function, the neural network will be reduced to a linear model.

2.4 (10 Marks) Discuss the differences between perceptron algorithm and support vector machines.

Answer: SVM aims to find the separating hyperplane with maximum margin whereas perceptron does not incorporate this maximum margin principle. Perceptron algorithm will not converge on non-separable data where SVM can. SVM can solve nonlinear classification problem whereas the perceptron algorithm can not.

Question 3 (30 Marks)

3.1 Suppose that we want to cluster eight data points as shown in the following table (x_1 and x_2 are the two features) into three clusters.

| ID | x_1 | x_2 |
|----------|-------|-------|
| A1 | 2 | 10 |
| A2 A3 | 2 | 5 |
| A3 | 8 | 4 |
| A4 A5 | 5 | 8 |
| A5 | 7 | 5 |
| A6 | 6 | 4 |
| A7 | 1 | 2 |
| A8 | 4 | 9 |

The distance function is Euclidean distance. Suppose initially we assign A1, A4, A7 as the center of each cluster. Run the *k*-means algorithm for 1 iteration, at the end of the iteration show

(a) (10 marks) The cluster assignments (i.e., which samples belong to which clusters)

<mark>Answer:</mark>

| | Cluster1 center: A1 | Cluster2 center: A4 | Cluster3 center: A1 |
|----|---------------------|---------------------|---------------------|
| A1 | 0 | $\sqrt{13}$ | <mark>√65</mark> |
| A2 | <mark>√25</mark> | $\sqrt{18}$ | $\sqrt{10}$ |
| A3 | <mark>√72</mark> | <mark>√25</mark> | <mark>√53</mark> |
| A4 | $\sqrt{13}$ | 0 | <mark>√52</mark> |
| A5 | $\sqrt{50}$ | <mark>√13</mark> | <mark>√45</mark> |
| A6 | <mark>√52</mark> | <mark>√17</mark> | <mark>√29</mark> |
| A7 | <mark>√65</mark> | $\sqrt{52}$ | 0 |
| A8 | <mark>√5</mark> | $\sqrt{2}$ | <mark>√58</mark> |

cluster 1: {A1}; cluster 2:{A3, A4, A5, A6, A8}; cluster 3: {A2, A7}

(b) (10 marks) The center of the new clusters

Answer: new cluster centers {2, 10}, {6, 6}, {1.5, 3.5}

3.2 (**10 marks**) Describe at least two limitations of *k*-means algorithm. And how to address these two limitations?

Answer: (1) K-means is extremely sensitive to cluster center initialization. We can try multiple initialization and choose the best result to address this limitation; (2) Works only if the cluster are round shaped and of equal size/density cluster. Probabilistic cluster methods can address this limitation; (3) Can not capture non-linear structure. Kernel k-means can address this limitation; (4) Makes hard assignments of points to clusters. Probabilistic cluster methods can address this limitation.