

4. Write a computer program that solves the Lorenz equations:

$$\begin{cases} \frac{dx}{dt} = -3(x(t) - y(t)) \\ \frac{dy}{dt} = 26.5x(t) - y(t) - x(t)z(t), \quad x(0) = z(0) = 0, \quad y(0) = 1 \quad t \in [0, 100] \\ \frac{dz}{dt} = x(t)y(t) - z(t) \end{cases}$$

Implement in the code numerical Runge-Kutta explicit methods of 2nd and 4th order with the grid step that will provide the maximum relative error less than 10^{-8} :

$$\max_{k=1,10} (|x_k(N) - x_k(N/2)| + |y_k(N) - y_k(N/2)| + |z_k(N) - z_k(N/2)|) < 10^{-8}$$

Provide the functionality of printing the array of the relative errors onto the console in the format

-- in the first line print the grid number of the final array (e.g. " $N = N$ "),
-- in the second line print the relative error values for the final array in the time moments: $t_1 = 10, t_2 = 20, \dots, t_{10} = 100$, separated by spaces, without the space after the last item.

Provide the functionality of plotting the phase trajectory of the solution on the 3D plane $\{x(t), y(t), z(t)\}$ at $t \in [0, 100]$.