

CSE 300

Technical Writing and Presentation Sessional

Report: Maximum Bipartite Matching

Lab Section - A1

Group - 09

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1 Introduction

The concept of maximum bipartite matching, a fundamental problem in graph theory, holds significant relevance across diverse fields due to its ability to model various real-world scenarios. Bipartite graphs serve as the foundational structure for this problem. In essence, a maximum bipartite matching seeks to pair elements from one subset with elements from the other subset in such a way that maximizes the number of paired elements. From applications in network flow optimization, job scheduling, and medical residency programs to its role in solving matching problems in societal contexts like marriage and kidney exchange programs, the utility of maximum bipartite matching extends across numerous domains, making it a subject of continued research and innovation.

1.1 Definitions

1.1.1 Bipartite Graph

A bipartite graph is one whose vertices can be split into two independent groups U, V such that **every edge connects vertices of different groups**.

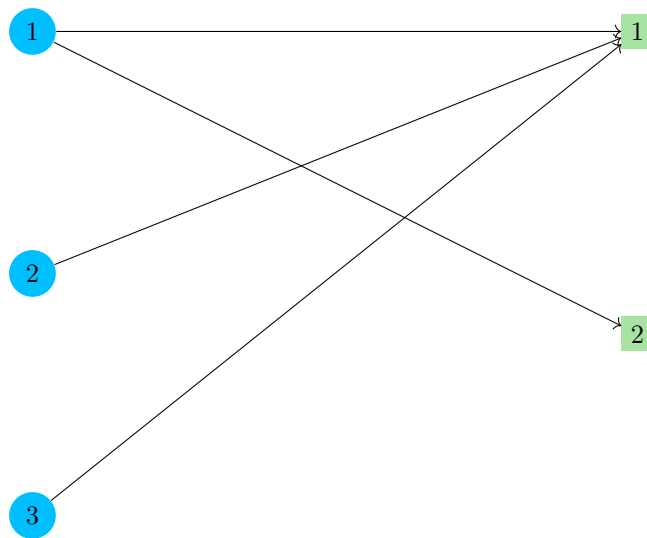


Figure 1: Visualization of bipartite graph

Properties of a Bipartite graph

- There can not be any edge between any two vertices of U or any two vertices of V .
- The graph is **two colourable** and doesn't have **cycles of odd length**.

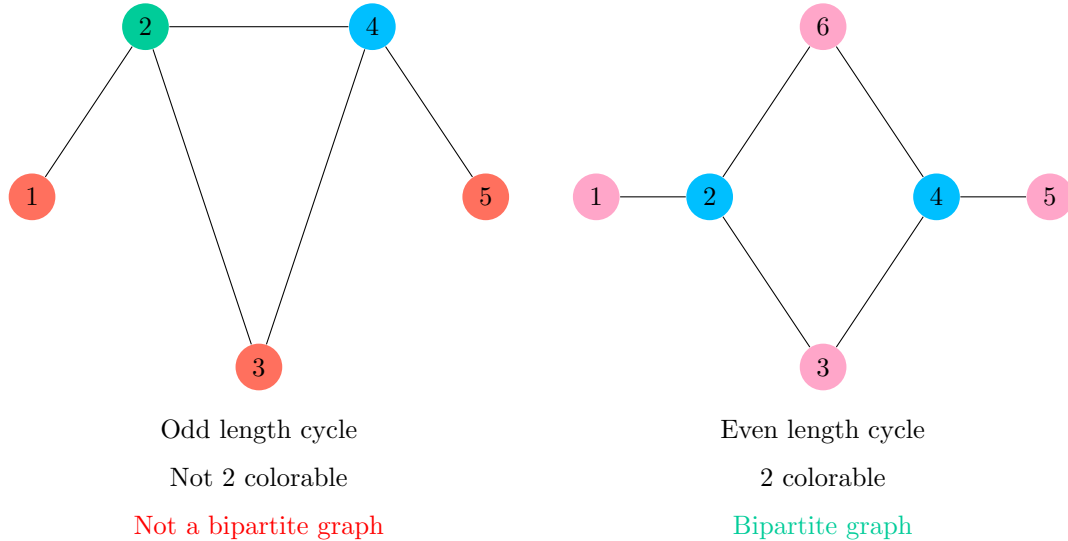


Figure 2: Comparison between Bipartite and Non-bipartite graph

1.1.2 Maximum Matching

Given a bipartite graph, a matching is a subset of the edges for which **every vertex belongs to exactly one of the edges**.

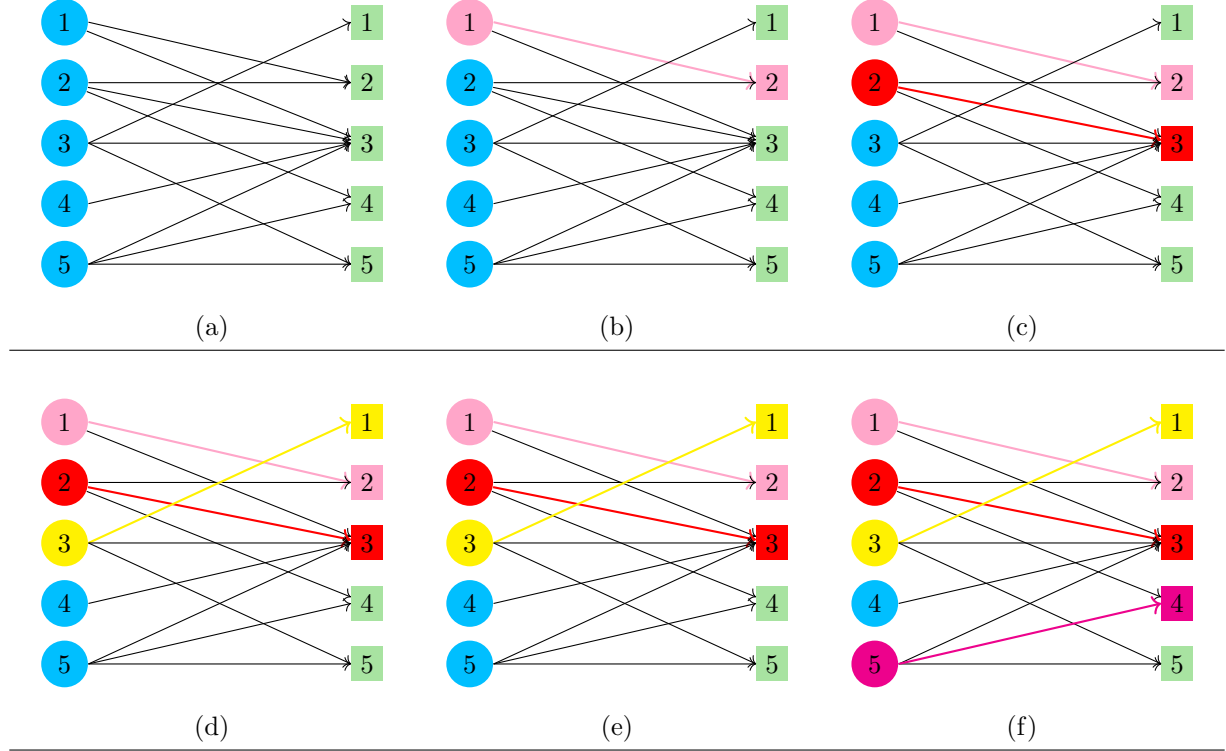
And, a maximum matching is a matching of **maximum number of edges**. In a maximum matching, if any edge is added to it, it is no longer a matching.

2 The Problem

Given a bipartite graph $G = (A \cup B, E)$, find an $\{ S \subseteq A \times B : S \text{ is a matching and is as large as possible.} \}$ [1]

3 Scenario

In a picnic, there are 5 people and 5 food items. Some people express interest in some of the items. How can we satisfy **maximum number of people** while wasting **minimum number of items**?



4 References

References

- [1] Jon Kleinberg and Eva Tardos. *Algorithm design*. Pearson Education India, 2006.