Vector

Yector: Object까기 덕화되고, Scalaron 이상 표현 문화 및 아이어

Vectore 33

D Geometric Vector. R, R+y== LR=W

2 Polynomial
3 Signal.
4 Rn = [2]
5 Rnxn

"Closure": Vector 3/2121 Scaling of Addingt the Vector Space Ast.

Systems of linear Equations

Mequation 7 unknown variables

$$\begin{bmatrix} a_{11} & \cdots & a_{1n} \\ \vdots & \vdots & \vdots \\ a_{mn} & \cdots & a_{mn} \end{bmatrix} \begin{bmatrix} x_i \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b_1 \\ \vdots \\ b_m \end{bmatrix} \Rightarrow \text{Solution} \quad \begin{cases} \text{Uhique} \\ \text{No} \end{cases}$$

$$\text{Infinite}$$

Matrix.
• A \in R^{mxn}, B \in R^{mxn} & \arg 24

A+B:= 설계21역할 E pmxn: Element - wise Sum.

· AE RMXN, BERNXK 2 ELH,

 $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$ $C = AB \in \mathbb{R}^{m \times k} \text{ onth set } C_{ij} = \sum_{k=1}^{m} a_{ik}b_{kj}$

· Properties of matrix addition and mulitplication

- Associativity: (AB) C= A(BC)= ABC - Distributivity: (AHB) C= AC+BC

-Multiplication with the identity matrix: HA ERMXN: ImA = AIn=A

Matrix Inverse: AB=In=BA When A∈R^{n×n}, B∈R^{n×n} ⇒ A=B⁻¹, B=A⁻¹

- atologi 224/1: Regular, Invertible, Nonsingular ↔ Noninvertible, Singular

M

latrix.
· Transpose: AGRMON, BERMON Dis=asi is called transpose of A B-AT
Ex (AB)T= BTAT
Symmetric Matrix.
Symmetric Matrix. - AT=A and AE Anon
-when hand B are symmetric, AHB is also symmetric
· Multiplication
- by Scalor.
- by Scalor. AE $\mathbb{R}^{m\times n}$ and $\mathbb{A} \in \mathbb{R}$, $\Rightarrow M = \mathbb{A}$ $\mathbb{K}_{is} = \mathbb{A} \times \mathbb{K}_{is}$
- Compact representation of Systems of linear equations.
$Ax=b \Rightarrow x= x_2 \xrightarrow{\pi} x_2 \xrightarrow{\pi} x_3 \xrightarrow{\pi} x_4 \xrightarrow{\pi} x_4 \xrightarrow{\pi} x_4 \xrightarrow{\pi} x_4 \xrightarrow{\pi} x_5 \xrightarrow{\pi} $
- Compact representation of Systems of linear equations. Ax=b $\Rightarrow x=\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \Rightarrow A \in \mathbb{R}^{m_{MM}}$ B $\in \mathbb{R}^m$ 21 test, How to Solve?
(1) x= A~b when Aep is Non Singular ⇒ 中 产程型 (m of 登表)
2) Make Simpler form (3) - 1. Exchange two equation (You > 21) -2. Multiplicate with costant 1 =0 to an equation (You on) & 4844)
E) - 1. Exchange two equation (Now > 21)
-2. Multiplicate with Costant 150 to an equation (row on 1 / ANH)
-3. Addition of two equations
Row-Echelon Form. Ω Δ((-2)) \ Metrical 3((2) 0)-243
(1) All-Zero Powie Matrixal 21/21/21/2
(2) Pivot 이 앞의 열에서 곱개함수를 가장 위로 배기
e> Pivot: first non zero number from the left
es) # 23 456] : Pivot 00123 00024

SEchelon (Aleta) - Gaussian Elimination 01 404 fow - Echelon Form 383. Ax=b \(\int \left[A/b \right] \top \(\text{R} \left(\text{Row-Echelon Form} \right) \)

Augmented Grussian Elimination

Matrix = Concatenation with A and B

Claussian Elimination.

- example

Whique Solution 2 37, Free Variable of 2241.

Infinite Solution 2 38% Free Variable of 2240,

Back Substitution.

- After Gaussian Elimination, lawest rows tel 78/2 45/1

- 3) Make Another Simpler Form. (Reduced-Echelon Form).
 - Row Echelon Form

- Every Pivot=1
 Pivot=1 =1, 아래 햄의 亞生 是 O (Pivot is the only nonzero entity in its column)
 -> back propagation process=1 4% but Gaussian Etimination 2+ 1241229 4是X.
- Plot Nonsingular (Invertible) show Ad Inverse Matrice Tible 18年12.

 ([A [In] ~> [In [A-1]]

Solving System of Linear Equation. - by using the Inverse.

(I) If A is invertible, 20= A-16 and 20 is Unique Solution. 2 If A has linearly Independent columns, (Assumption) $Ax = b \Leftrightarrow A^{T}Ax = A^{T}b \Leftrightarrow x = (A^{T}A)^{-1}A^{T}b$ (S) (ATA-1) AT: Moore - Pen rose pseudo-inverse of A Why?.

if $A \in A^{dx2}$ (when A > 2), A is singular matrix. (and No square Matrix B)

A^TA is square matrix (Can be Nonsingular) 2= (ATA)-IAT b et 2 Solutione ll Ax-b112号 社会され Approximation Solutionez 대語。(Linear Regression)