

# Session

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July 2024

## 1st Possible Solution

**Require:** Finding the number of admissible degrees within a given range.

We can do that easily by applying a brute force algorithm.

```
1: for Every-Query do
2:   for Every-Value-In-Query do
3:     for Every-Input-Range do
4:       SUM
5:     end for
6:   end for
7: end for
```

But solving this problem this way is inefficient. The time complexity of the previous solution is:

Time complexity =  $O(n^3)$

There are better ways to solve the same problem in  $O(n^2)$  and  $O(n)$ .

One approach is to optimize the **Brute Force** to achieve  $O(n^2)$  instead of  $O(n^3)$ .

## 2nd Possible Solution

**Require:** To apply the algorithm this way we need to do the following:

```
1: for Every-Input-Range do
2:   Accumulate in the array
3: end for
```

Figure 1: A Simple Array of the first Test-case

91	92	93	94	95	96	97	98	99
1	2	2	2	1	1	2	1	1

Next, we need to change every value in the array to 1 if it is greater than k; otherwise, change it to 0.

```
1: for Every-Value-In-Array do
2:   if  $a[i] > K$  then
3:      $a[i] \leftarrow 1$ 
4:   else
5:      $a[i] \leftarrow 0$ 
6:   end if
7: end for
```

Figure 2: 1st array after the previous operation

91	92	93	94	95	96	97	98	99
0	1	1	1	0	0	1	0	0

After that all we will do is iterate and sum, So the total **Time complexity** =  $O(n^2) + O(n)$ .

**Time complexity** =  $O(n^2)$ .

### 3rd Possible Solution

**Require:** For better **Time complexity** we can solve this problem in  $O(n)$  by using prefix sum algorithm.

- 1: And we will do that by make  $a[l] + 1$  and  $a[r + 1] - 1$  Such : l is the first digit in the query, and r is the second digit in the query.

Figure 3: Array by doing prefix sum this way for example 92:94

91	92	93	94	95	96	97	98	99
0	1	0	0	-1	0	0	0	0
0	1	1	1	0	0	0	0	0

At the end, by doing this little trick we can solve the problem in **Time complexity** =  $O(n)$ .