



Computer vision Cameras

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Cameras

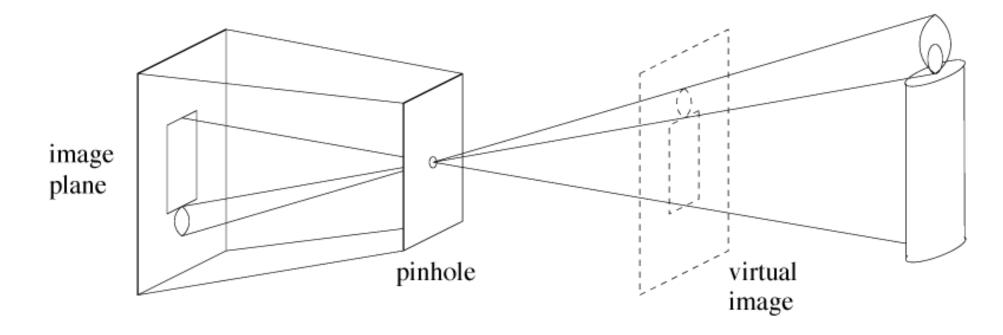
- First photograph due to Niepce
- First on record shown in the book 1822
- Basic abstraction is the pinhole camera
 - lenses required to ensure image is not too dark
 - various other abstractions can be applied



Pinhole cameras

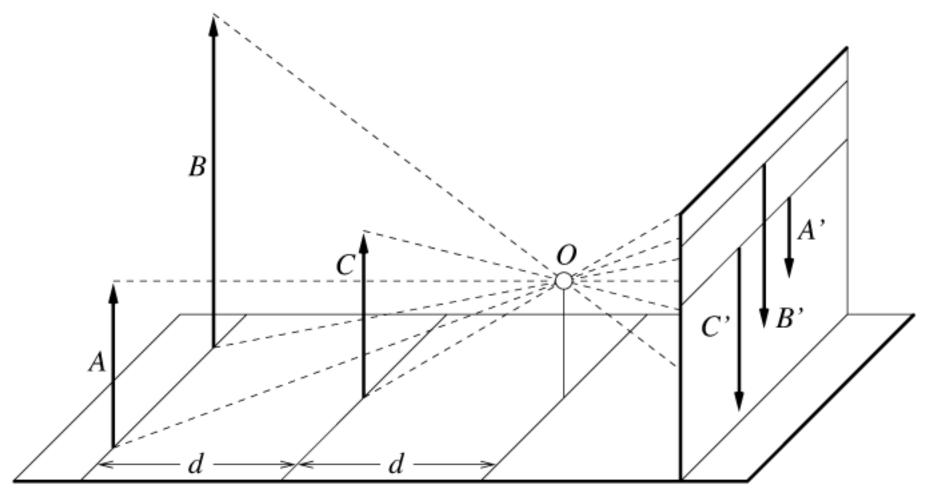
Abstract camera model - box with a small hole in it

Pinhole cameras work in practice



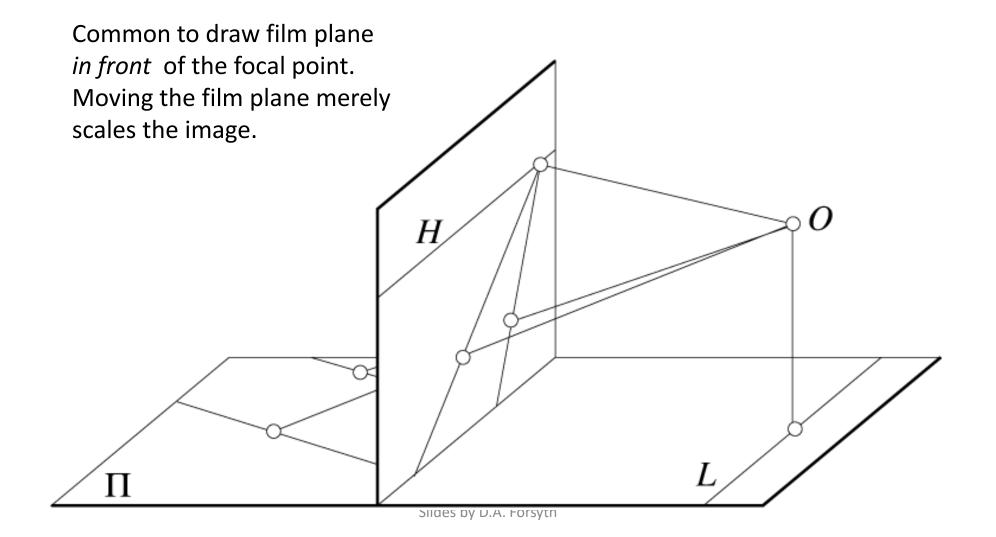
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Distant objects are smaller



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Parallel lines meet



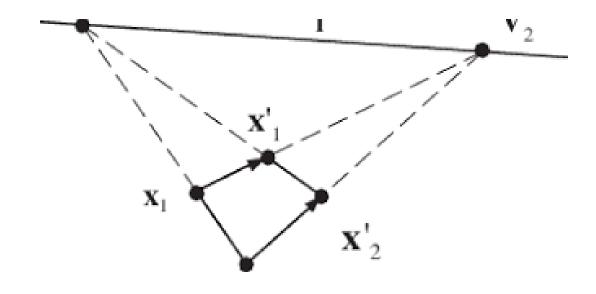


Vanishing points

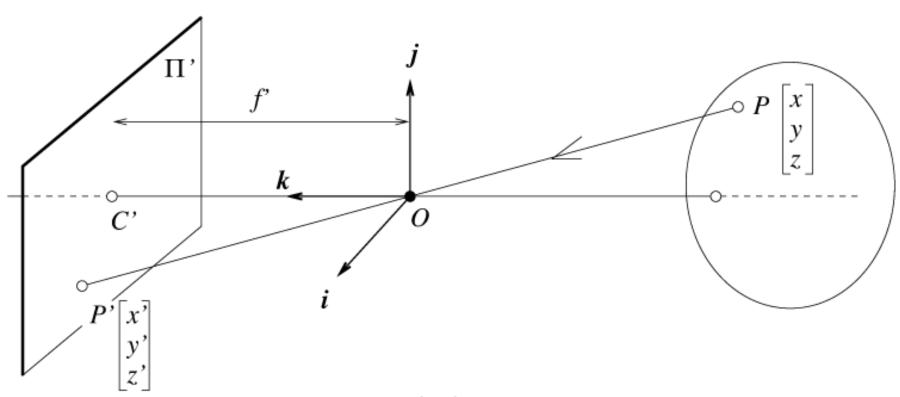
- each set of parallel lines (=direction)
 meets at a different point
 - The vanishing point for this direction
- Sets of parallel lines on the same plane lead to collinear vanishing points.
 - The line is called the *horizon* for that plane

- Good ways to spot faked images
 - scale and perspective don't work
 - vanishing points behave badly
 - supermarket tabloids are a great source.





The equation of projection



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The equation of projection

- Cartesian coordinates:
 - We have, by similar triangles, that $(x, y, z) \rightarrow (f x/z, f y/z, -f)$
 - Ignore the third coordinate, and get

$$(x,y,z) \rightarrow (f\frac{x}{z},f\frac{y}{z})$$
 (x',y')



Homogenous coordinates

- Add an extra coordinate and use an equivalence relation
- for 2D
 - equivalence relationk*(X,Y,Z) is the same as

(X,Y,Z)

- for 3D
 - equivalence relationk*(X,Y,Z,T) is the same as

(X,Y,Z,T)

- Basic notion
 - Possible to represent points "at infinity"
 - Where parallel lines intersect
 - Where parallel planes intersect
 - Possible to write the action of a perspective camera as a matrix

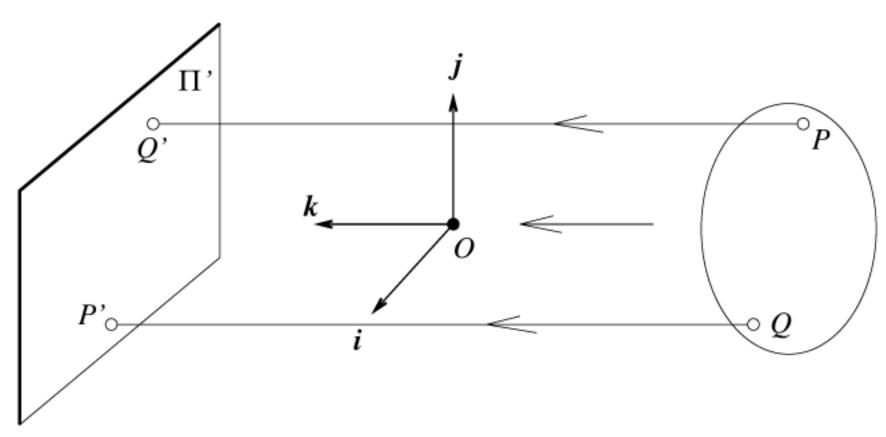


The camera matrix

- Turn previous expression into Homogenous coordinate (HC)'s
 - HC's for 3D point are (X,Y,Z,T)
 - HC's for point in image are (U,V,W)

$$\begin{pmatrix} U \\ V \\ W \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{1}{f} & 0 \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ T \end{pmatrix}$$

Orthographic projection



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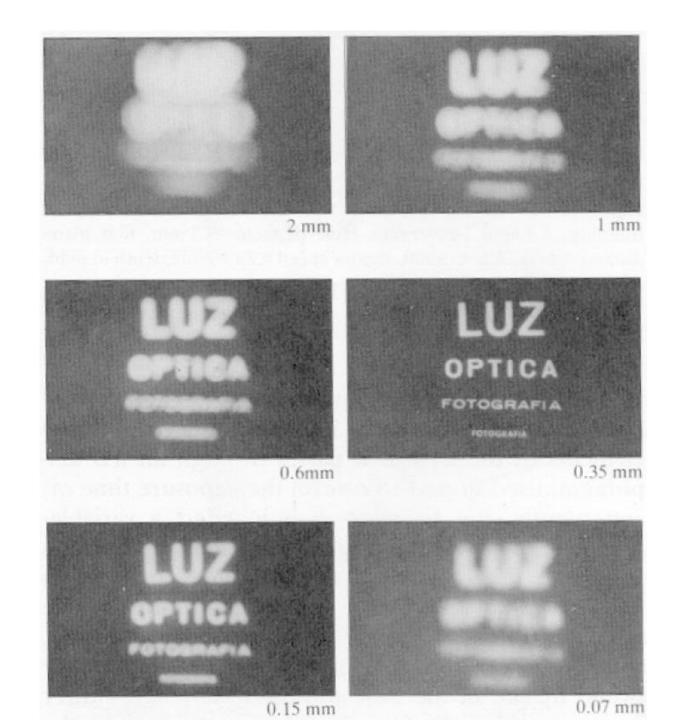
The projection matrix for orthographic projection

$$\begin{pmatrix} U \\ V \\ W \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ T \end{pmatrix}$$

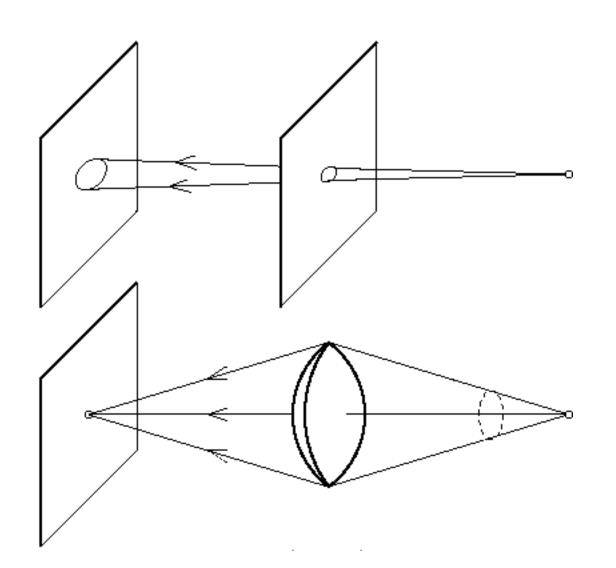
Pinhole too big many directions are averaged, blurring the image

Pinhole too smalldiffraction effects blur the image

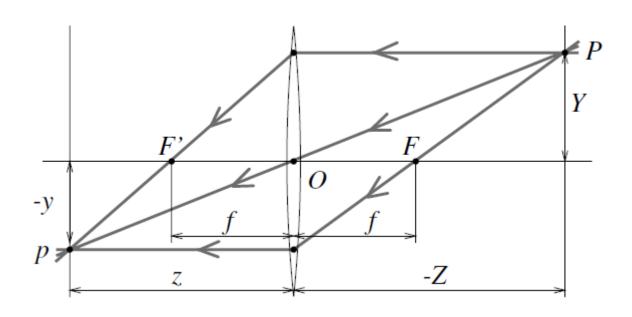
Generally, pinhole cameras are *dark*, because a very small set of rays from a particular point hits the screen.



The reason for lenses



The thin lens

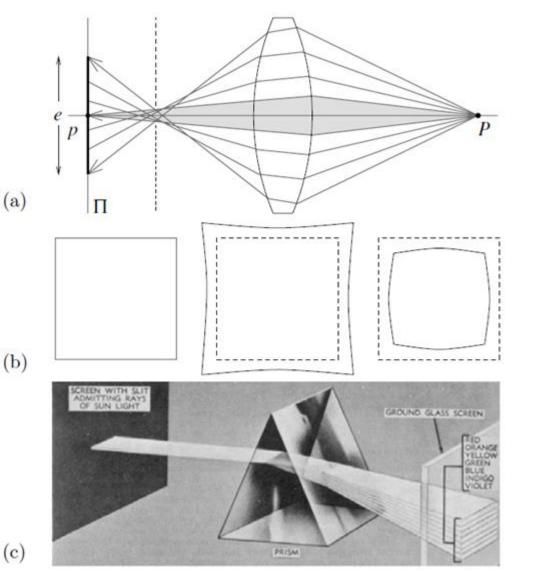


$$\frac{1}{z} - \frac{1}{Z} = \frac{1}{f}$$

 $f = \frac{R}{2(n-1)}$ is the focal length of the lens

radius R and index of refraction n.

Spherical aberration



Spherical aberration: The gray region is the paraxial zone where the rays issued from P intersect at its paraxial image p. If an image plane π were erected in p, the image of p in that plane would form a circle of confusion of diameter e. The focus plane yielding the circle of least confusion is indicated by a dashed line.

Distortion: From left to right, the nominal image of a fronto-parallel square, pincushion distortion, and barrel distortion.

Chromatic aberration: The index of refraction of a transparent medium depends on the wavelength (or color) of the incident light rays. Here, a prism decomposes white light into a palette of colors. Figure from US NAVY MANUAL OF BASIC OPTICS AND OPTICAL INSTRUMENTS, prepared by the Bureau of Naval Perso```nnel, reprinted by Dover Publications, Inc. (1969).

Example of the usual photo of rose without changes and with chromatic aberrations (red-green edging):





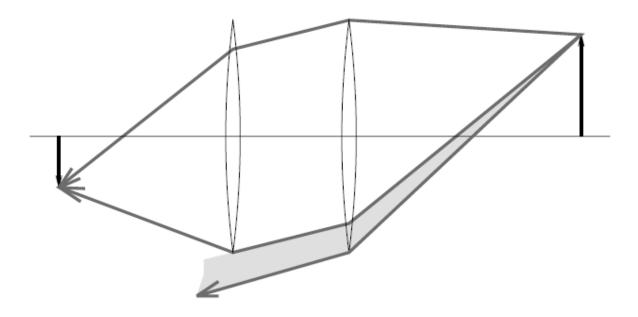


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Barrel distortion Pincushion distortion 17

Vignetting



Vignetting effect in a two-lens system. The shaded part of the beam never reaches the second lens. Additional apertures and stops in a lens further contribute to vignetting.

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Other (possibly annoying) phenomena

- Chromatic aberration
 - Light at different wavelengths follows different paths; hence, some wavelengths are defocussed
 - Machines: coat the lens
 - Humans: live with it
- Scattering at the lens surface
 - Some light entering the lens system is reflected off each surface it encounters (Fresnel's law gives details)
 - Machines: coat the lens, interior
 - Humans: live with it (various scattering phenomena are visible in the human eye)
- Geometric phenomena (Barrel distortion, etc.)



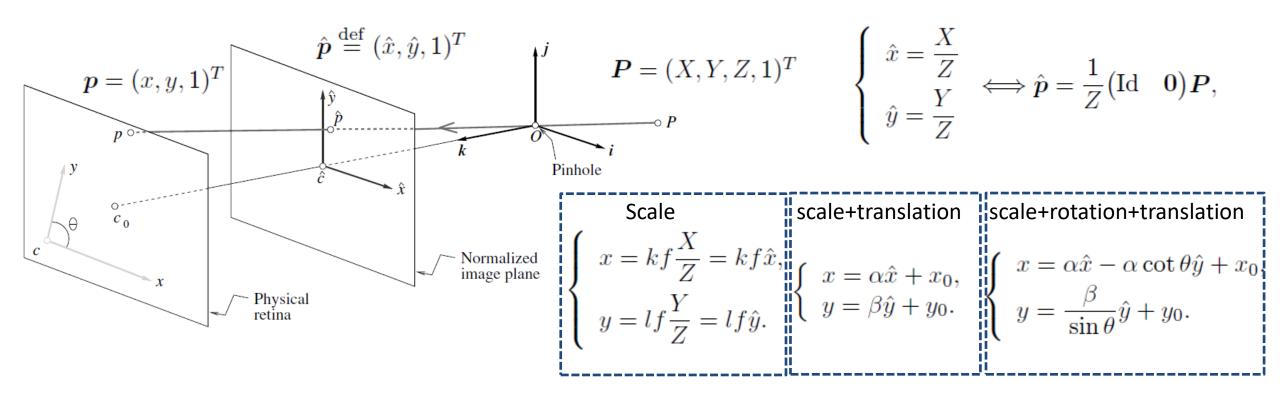
INTRINSIC AND EXTRINSIC PARAMETERS

- The world and camera coordinate systems are related by a set of physical parameters: focal lens, the size of the pixels, the position of the image center, and the position and orientation of the camera.
- Intrinsic parameters, which relate the camera's coordinate system to the idealized coordinate system.
- Extrinsic parameters, which relate the camera's coordinate system to a fixed world coordinate system and specify its position and orientation in space.



Intrinsic parameters

$$p = \frac{1}{Z} \mathcal{M} P.$$

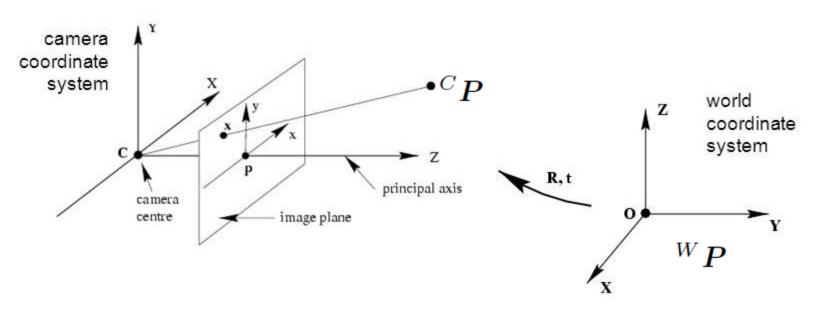


$$p = \frac{1}{Z} \mathcal{K}(\text{Id} \quad \mathbf{0}) P = \frac{1}{Z} \mathcal{M} P$$
, where $\mathcal{M} \stackrel{\text{def}}{=} (\mathcal{K} \quad \mathbf{0})$ $\mathcal{K} \stackrel{\text{def}}{=} \begin{pmatrix} \alpha & \alpha \cos \theta & x_0 \\ 0 & \frac{\beta}{\sin \theta} & y_0 \\ 0 & 0 & 1 \end{pmatrix}$

$$\mathcal{K} \stackrel{\mathrm{def}}{=} egin{pmatrix} lpha & -lpha\cot heta & x_0 \ 0 & \dfrac{eta}{\sin heta} & y_0 \ 0 & 0 & 1 \end{pmatrix}$$
Intrinsic matrix



Extrinsic parameters



Transformation from world coor. to image plane coor.

$$oldsymbol{o} = rac{1}{Z} \mathcal{M}^C oldsymbol{P}, \qquad ^C oldsymbol{P} = egin{pmatrix} \mathcal{R} & t \ 0 & 1 \end{pmatrix} ^W oldsymbol{P},$$

$$p = \frac{1}{Z}\mathcal{M}^{C}P$$
, $^{C}P = \begin{pmatrix} \mathcal{R} & t \\ \mathbf{0}^{T} & 1 \end{pmatrix}^{W}P$, $p = \begin{bmatrix} 1 \\ Z \end{bmatrix}\mathcal{M}P$, where $\mathcal{M} = \mathcal{K}\begin{bmatrix} \mathcal{R} & t \\ \mathcal{R} & t \end{bmatrix}$

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Camera parameters

- There are 16 unknowns in intrinsic and extrinsic matrices
- Non-linear
- Estimating these parameters from experiments called camera calibration

$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} f_x & 0 & u_0 \\ 0 & f_y & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r1 & r2 & r3 & t1 \\ r4 & r5 & r6 & t2 \\ r7 & r8 & r9 & t3 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$



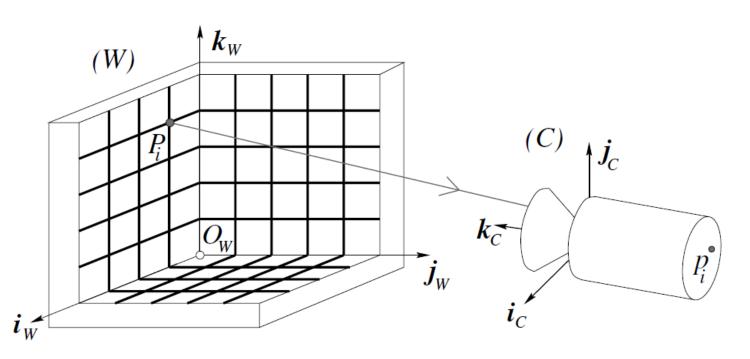
Issues:

- what are intrinsic parameters of the camera?
- what is the camera matrix? (intrinsic+extrinsic)
- General strategy:
 - view calibration object
 - identify image points
 - obtain camera matrix by minimizing error
 - obtain intrinsic parameters from camera matrix

• Error minimization:

- Linear least squares
 - easy problem numerically
 - solution can be rather bad
- Minimize image distance
 - more difficult numerical problem
 - solution usually rather good,
 - start with linear least squares
- Numerical scaling is an issue

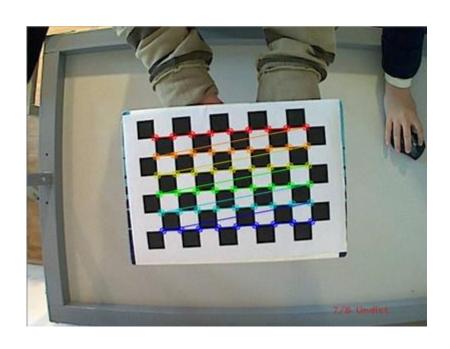


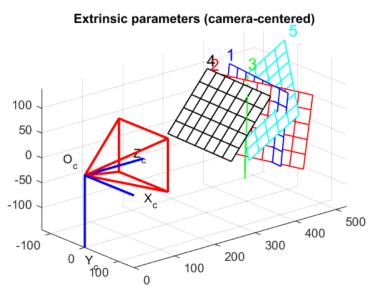


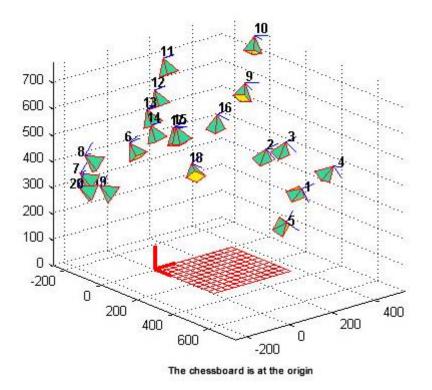
Camera calibration setup: In this example, the calibration rig is formed by three grids drawn in orthogonal planes. Other patterns could be used as well, and they may involve lines or other geometric figures.

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• Bài tập:

- In bảng chess board dành cho camera calibration.
- Dán bảng chess board lên mặt phẳng sàn nhà và sử dụng bảng này để xác
 định hệ tọa độ thực của căn nhà (world coordinate)
- Sử dụng camera điện thoại để chụp chess board ở nhiều góc và kích thước khac nhau
- Viết chương trình camera calibration sử dụng tài liệu tham khảo phía dưới
- Do exercise camera calibration with OpenCV
- https://docs.opencv.org/2.4/doc/tutorials/calib3d/camera_calibration/camera_calibration.html