

CSEN 501 – CSEN501 - Databases I

Lecture 6: The Relational Calculus

Prof. Dr. Slim Abdennadher
Dr. Nada Sharaf

German University Cairo, Faculty of Media Engineering and Technology

Relational Data Manipulation Languages

- Variety languages used by relational database management systems
 - **Procedural** languages: The user tells the system how to manipulate the data, e.g. **Relational Algebra**
 - **Declarative** languages: the user states what data is needed but not exactly how it is to be located, e.g. **Relational Calculus** and **SQL**
 - **Graphical** languages: allowing the user to give an example or an illustration of what data should be found, e.g. **QBE**

What is the Relational Calculus?

- **Relational calculus** is a formal query language where we write one declarative expression to specify a retrieval request.
- A calculus expression specifies what is to be retrieved rather than how to retrieve it. Therefore, relational calculus is considered to be a nonprocedural language.
- There are two types of relational calculus:
 - **Tuple relational calculus**
 - Domain relational calculus.

Tuple Relational Calculus

- The tuple relational calculus is based on specifying a number of tuple variables.
- Each tuple variable usually **ranges** over a particular database relation.
- A tuple expression is written as

$$\{t | C(t)\}$$

Where t is a tuple variable and $C(t)$ is a conditional expression involving t .

- Example: Find all employees whose salary is more than 50,000.

$$\{t | \text{employee}(t) \wedge t.\text{salary} > 50000\}$$

Note: The condition $\text{employee}(t)$ specifies that the range relation of tuple variable t is employee.

Tuple Relational Calculus Expressions

- A general expression of a tuple relational calculus is of the form:

$$\{t_1.A_j, t_2.A_k, \dots, t_n.A_m \mid C(t_1, t_2, \dots, t_n, t_{n+1}, \dots, t_{n+m})\}$$

Where:

- t_1, t_2, \dots, t_{n+m} are tuple variables
- A_i is an attribute of the corresponding relation on which t_i ranges.
- C is a condition or a formula of the tuple relational calculus.
- In Relational calculus a **safe expression** is the one guaranteed to yield a finite number of tuples otherwise the expression is unsafe.
- Example:

$$\{t \mid \neg(\text{employee}(t))\}$$

is unsafe expression.

Tuple Relational Calculus - Atoms

- An **atom** is a building block of a relational calculus expression.
- An atom can have one of the following forms:
 - $R(t_i)$: where R is a relation name. This atom specifies the range of tuple variable t_i .
 - $t_i.A \text{ op } t_j.B$: where op is one of the comparison operators.
 - $t_i.A \text{ op } c$ or $c \text{ op } t_j.B$: where op is one of the comparison operators and c is a constant value.
- Each atom evaluates to either true or false for a specific value of tuples, This is called the **truth value** of an atom.

Relational Schema Example

```
employee(fname, lname, ssn, bdate, address, sex,  
         salary, dnr, superssn)  
department(dname, dnr, dMangssn)  
departmentLocation(dnr, dlocation)  
project(pname, pnr, plocation, dnr)  
workson(ssn, pnr, hours)  
dependent(ssn, dependentname, sex, bdate, relationship)
```

Examples (I)

- Retrieve all employees.

$$\{e \mid \text{employee}(e)\}$$

- Retrieve the names of all employees.

$$\{e.\text{fname}, e.\text{lname} \mid \text{employee}(e)\}$$

- Retrieve employees with salary greater than 5000.

$$\{e \mid \text{employee}(e) \wedge e.\text{salary} > 5000\}$$

- Retrieve the names and salary of all employees who work in department 1 and whose salary exceeds 5000

$$\{e.\text{fname}, e.\text{lname}, e.\text{salary} \mid \text{employee}(e) \wedge e.\text{dnr} = 1 \wedge e.\text{salary} > 5000\}$$

Examples (II)

- For each employee, retrieve the employee's first and last name and the first and last name of his/her immediate supervisor.

$$\{e.fname, e.lname, s.fname, s.lname \mid employee(e) \wedge employee(s) \\ \wedge e.superssn = s.ssn\}$$

Tuple Relational Calculus - Formulas

- A formula (condition) is made up of one or more atoms connected via the logical operators: \wedge , \vee , and \neg .
- A **formula** can be recursively defined as:
 - Every atom is a formula
 - If F and G are formulas, then so are the following:
 - $F \wedge G$
 - $F \vee G$
 - $\neg F$

Universal and Existential Quantifiers

- Two quantifiers symbols may appear in a formula:
 - The **existential quantifier**: \exists
 - The **universal quantifier**: \forall
- The truth values of formula with quantifiers is based on the concept of free and bound tuple variables in the formula.

Free and Bound Tuple variables

- An occurrence of a tuple variable t in a formula F that is an atom is **free** in F .
- An occurrence of a tuple variable t is free or bound in a formula made up of logical connectives - $(F \wedge G)$, $(F \vee G)$ and $()$, - depending whether it is free or bound in F or G .
- In the formula of the form $F = (G \wedge H)$ or $F = (G \vee H)$, a tuple variable may be free in G and bound in H , or vice versa. In this case, one occurrence of the tuple variable is bound and the other is free in F .
- All free occurrences of a tuple variable t in F are bound in a formula $F = (\forall t)(G)$ or $F = (\exists t)(G)$. The tuple variable is **bound** to the quantifier specified in F .

Truth Value of a Formula With Quantifier

- If F is a formula then so is $(\exists t)(F)$, where t is a tuple variable.
- The formula $(\exists t)(F)$ is **true** if the formula F evaluates to true for some (at least one) tuple assigned to free occurrence of t in F , otherwise $(\exists t)(F)$ is false.
- If F is a formula then so is $(\forall t)(F)$, where t is a tuple variable.
- The formula $(\forall t)(F)$ is **true** if the formula F evaluates to true for every tuple (in the universe) assigned to free occurrence of t in F , otherwise $(\forall t)(F)$ is *false*.

Free Variables in Expressions

- The **only** free tuple in a relational calculus expression should be those that appear to the left of the bar ($|$).
- A free variable is bound **successively** to each tuple.

Examples with Existential & Universal Quantifiers

- Retrieve the name and address of all employees who work for the research department.
 $\{t.fname, t.lname, t.address | employee(t) \wedge (\exists d)(department(d) \wedge d.dname = 'Research' \wedge d.dnr = t.dnr)\}$
- Find the names of employees who have no dependents.
 $\{e.fname, e.lname | employee(e) \wedge \neg(\exists d)(dependent(d) \wedge e.ssn = d.ssn)\}$
 - Push negation to the atoms:
 $\{e.fname, e.lname | employee(e) \wedge (\forall d)(\neg dependent(d) \vee \neg(e.ssn = d.ssn))\}$
 - Use Implication:
 $\{e.fname, e.lname | employee(e) \wedge (\forall d)(dependent(d) \Rightarrow \neg(e.ssn = d.ssn))\}$
- List the names of managers who have at least one dependent.
 $\{e.fname, e.lname | employee(e) \wedge (\exists d)(\exists p)(department(d) \wedge dependent(p) \wedge e.ssn = d.ssn \wedge p.ssn = e.ssn)\}$