

Experiment 8 — Focal length of a converging lens

Nero Su, Laurence Amadeus Tristan

25 March 2019

1 Purpose

The purpose of this experiment is to compare the focal length of a lens obtained from the y-intercept of a linear equation and the gradient of another linear equation using measured values of d_o and d_i of a converging lens.

2 Theory

For a thin lens, the distance between an object (or in this case the aperture) with the lens d_o and the distance between the lens and the image d_i is related to the focal length of the lens f by the equation

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \quad \begin{cases} +f & \text{if lens is convex/converging} \\ -f & \text{if lens is concave/diverging} \end{cases} \quad (2.1)$$

where f = focal length of lens

d_i = distance between image and lens

d_o = distance between object and lens.

If the focal length f is positive, it indicates that it is a convex/converging lens. The opposite is true for a concave/diverging lens.

3 Procedure

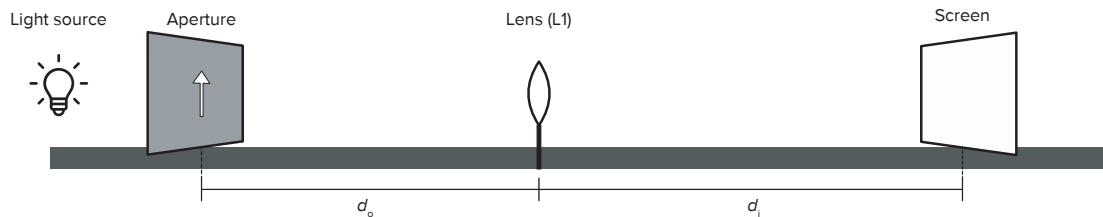


Figure 3.1: A rough diagram of the apparatus. The grey bar is the optical bench.

The experiment was done on a bar called an optical bench. Here, we could place various objects that were able to be secured onto the optical bench, like the aperture (which is arrow-shaped), the lens, and the screen. With this particular optical bench (not shown in the diagram) we could measure the distance between the aperture and other objects on the bench, as there was a built-in ruler on the side of the optical bench.

First, we set up the apparatus as shown roughly in the diagram, with the aperture at the 0 cm mark and the light source being placed right behind the aperture. We then made sure that the apparatus was accurate by checking if the bench is stable enough on the laboratory bench, and if the aperture, convex lens (L1), and screen were parallel to each other and at the same height.

We then turned on the light source. Then, we varied the distance d_o by moving the convex lens L1 along the optical bench. Afterwards, we moved the screen along the optical bench until the image looked as sharp as possible. It is important that a standard for sharpness is established first before starting the experiment.

With the apparatus in place, we recorded the values for d_o and $d_o + d_i$ by looking at the optical bench's built-in ruler. After that, we repeated the experiment, each time increasing the distance d_o by 1 cm

4 Data

$d_o/\pm 0.1 \text{ cm}$	$d_o + d_i/\pm 0.2 \text{ cm}$
15.0	59.0
16.0	54.1
17.0	51.0
18.0	48.9
19.0	47.7
20.0	46.8
21.0	46.4
22.0	46.1

Table 4.1: Experimental result for L1

5 Analysis

First, we need to make two linear equations out of (2.1). Here, we make $\frac{1}{d_o}$ the subject for (5.1) and $d_o d_i$ the subject for (5.2).

$$\begin{aligned}\frac{1}{d_o} + \frac{1}{d_i} &= \frac{1}{f} \\ \frac{1}{d_o} &= -\frac{1}{d_i} + \frac{1}{f}\end{aligned}\tag{5.1}$$

$$\begin{aligned}\frac{1}{d_o} + \frac{1}{d_i} &= \frac{1}{f} \\ \frac{d_i + d_o}{d_o d_i} &= \frac{1}{f} \\ d_o d_i &= f(d_i + d_o)\end{aligned}\tag{5.2}$$

d_o/cm	d_i/cm	$d_o + d_i/\text{cm}$	$\frac{1}{d_o}/\text{cm}^{-1}$	$\frac{1}{d_i}/\text{cm}^{-1}$	$d_o d_i/\text{cm}^2$
15.0 ± 0.1	44.0 ± 0.3	59.0 ± 0.2	0.0667 ± 0.0004	0.0227 ± 0.0002	660 ± 9
16.0 ± 0.1	38.1 ± 0.3	54.1 ± 0.2	0.0625 ± 0.0004	0.0263 ± 0.0002	610 ± 9
17.0 ± 0.1	34.0 ± 0.3	51.0 ± 0.2	0.0588 ± 0.0003	0.0294 ± 0.0003	578 ± 9
18.0 ± 0.1	30.9 ± 0.3	48.9 ± 0.2	0.0556 ± 0.0003	0.0324 ± 0.0003	556 ± 9
19.0 ± 0.1	28.7 ± 0.3	47.7 ± 0.2	0.0526 ± 0.0003	0.0348 ± 0.0004	545 ± 9
20.0 ± 0.1	26.8 ± 0.3	46.8 ± 0.2	0.0500 ± 0.0003	0.0373 ± 0.0004	536 ± 9
21.0 ± 0.1	25.4 ± 0.3	46.4 ± 0.2	0.0476 ± 0.0002	0.0394 ± 0.0005	533 ± 9
22.0 ± 0.1	24.1 ± 0.3	46.1 ± 0.2	0.0456 ± 0.0002	0.0415 ± 0.0005	530 ± 9

Table 5.1: Data from Table 4.1 and calculations done for d_i , $\frac{1}{d_i}$, $\frac{1}{d_o}$, and $d_o d_i$

To get the value for d_i , we subtract d_o from $(d_o + d_i)$, like so:

$$d_i =$$

6 Discussion

From the experiment, we have established two values of f for L1 from two different methods. When we find f as an reciprocal of the y-intercept of a linear equation, the focal length is $(10.89 \pm 0.05) \text{ cm}$, whereas with f as the gradient of another linear equation, we got $(10 \pm 1) \text{ cm}$. With a discrepancy of 7.8%, we consider the difference between the two methods to be significant enough to make a big difference. We can see that the value for the focal length through the y-intercept method to be much more precise than the other method, due to the lower uncertainty. However, this method might not yield an accurate result for the focal length of a lens.

There were many factors that may play into the considerable discrepancy that we observed here. First, the lenses might not be aligned properly to be parallel with the screen and the aperture despite our best efforts, and it might be not high enough for the centre of the arrow to be aligned with the centre of the lens. This might affect the sharpness of the image, however this factor might not even affect the outcome of the experiment.

Another factor might be that we did not properly define what a sharp image looks like. Because we did not have a reference image available during the experiment, the sharpness of the image might vary slightly. Also, due to the presence of a halo around the edges of the image, it adds into the difficulty of determining if the image is at its sharpest. It might be better if the experiment was done with a camera-type equipment as cameras could determine if the image is at its sharpest.