

Experiment 9 — Finding the speed of light with microwave optics

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1 Introduction

The aim of this experiment is to find the speed of light in air using three different methods of getting the wavelength λ of the microwave source ($f = 10.525$ GHz). We then compare the three values of the speed of light in air from those methods in terms of the precision and accuracy of those values.

We define the value of the speed of light in air v as:

$$v_a = 3.0 \text{ m s}^{-1} \text{ (to 1 d.p.)}.$$

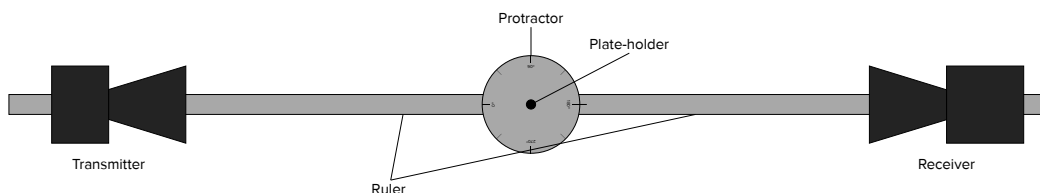


Figure 1.1: A goniometer with the mounted microwave transmitter-receiver pair.

We use a microwave transmitter-receiver pair mounted on a goniometer (Figure ??). The goniometer allows us to change (and measure) the angle of the receiver relative to the transmitter, and both transmitter and receiver's polarization axes are adjustable. The transmitter emits a microwave polarized along the transmitter's axis, and similarly the receiver receives the microwave polarized to its axis.

The plate-holder is an attachment point for the construction of a double-slit plate or a single-slit plate. The plates were stuck together using magnets, which then will be attached to the plate-holder.

Once λ is established using the three experiments, we use the equation

$$v = f\lambda \quad (1.1)$$

to get a value for the speed of light in air (indicated by v) for each experiment.

2 Experiment

2.1 Part I: Finding factors affecting intensity of microwaves

First, we try to figure out what factors affects the intensity of the microwave energy that the receiver detects. We found that the following factors affect the intensity of microwave:

1. Distance between the transmitter and receiver. The further the distance, the lower the intensity of microwave received by the receiver. The opposite is true when the distance is decreased.
2. Relative angle of the polarization axes of the transmitter and receiver. As the receiver turns, the intensity decreases to zero as it approaches 90° and increases to its maximum as it approaches 180° .
3. Presence of water between transmitter and receiver. When we put a dry towel between the pair intensity remains the same. However when we placed a wet towel between the pair the microwave is absorbed by the water present in the towel, so the intensity decreases to zero.

2.2 Part II: Measuring the wavelength λ of microwaves

For each experiment, we adjust the goniometer such that the angle reads 180° for the receiver.

2.2.1 Standing waves method

First, move the receiver and the transmitter on the goniometer such that the receiver is at the intensity maxima. Then, make note of the location of the receiver on the ruler. Afterwards, move the receiver towards the transmitter slowly while counting the number of intensity maxima (Δm). Stop moving the receiver at one of the intensity maxima and make note of the location of the receiver and the number of intensity maxima.

m	$d_m/\pm 0.1 \text{ cm}$
0	93.4
4	87.5

Table 2.1: Initial and final values of the location of the receiver.

The relationship between λ and d is

$$d = \Delta m \left(\frac{\lambda}{2} \right) \quad (2.1)$$

where Δm = number of intensity maxima,

d = difference in location of receiver,

λ = wavelength of microwave.

Now, get the values for Δm and d . The uncertainty for d accumulates as we add/subtract so it'll not be shown as it is trivial enough to do.

$$\begin{aligned} \Delta m &= 4 - 0 \\ &= 4 \\ d &= d_4 - d_0 \\ &= (93.4 \pm 0.1) \text{ cm} - (87.5 \pm 0.1) \text{ cm} \\ &= (5.9 \pm 0.2) \text{ cm} \end{aligned}$$

Using (??), get the value for the wavelength λ .

$$\begin{aligned} 5.9 \text{ cm} &= \frac{(4)\lambda}{2} & \delta\lambda &= |\lambda| \left(\frac{\delta d}{d} \right) \\ \lambda &= \frac{2(5.9 \text{ cm})}{4} & &= 2.95 \text{ cm} \left(\frac{0.2 \text{ cm}}{5.9 \text{ cm}} \right) \\ &= 2.95 \text{ cm} & &= 0.1 \text{ cm} \end{aligned}$$

$$\therefore \lambda = (3.0 \pm 0.1) \text{ cm}$$

Convert λ to metre and find the value for the speed of light in air v .

$$\begin{aligned} v &= f\lambda & \delta v &= |v| \left(\frac{\delta\lambda}{\lambda} \right) \\ &= (10.525 \times 10^9 \text{ Hz})(3.0 \times 10^{-2} \text{ m}) & &= |3.1575 \times 10^8 \text{ m}| \left(\frac{1 \times 10^{-3} \text{ m}}{3.0 \times 10^{-2} \text{ m}} \right) \\ &= 3.1575 \times 10^8 \text{ m s}^{-1} & &= 1.07034 \times 10^7 \text{ m s}^{-1} \\ & & &\approx 1 \times 10^7 \text{ m s}^{-1} \text{ (to 1 s.f.)} \end{aligned}$$

$$\therefore v = (3.2 \pm 0.1) \times 10^8 \text{ m s}^{-1}$$

2.2.2 Double-slit interference method

Setup the apparatus as shown in Figure ???. It is suggested to move the transmitter as close to the plate as possible, while adjusting the receiver such that it is located in one of the intensity maxima. Then, using the available plates construct a double-slit, with the width of the slit each being 2 cm, and a slit spacing (denoted as d) of about 8 cm, measured centre to centre. Make sure the slits are aligned as symmetrical as possible, and the individual slits as

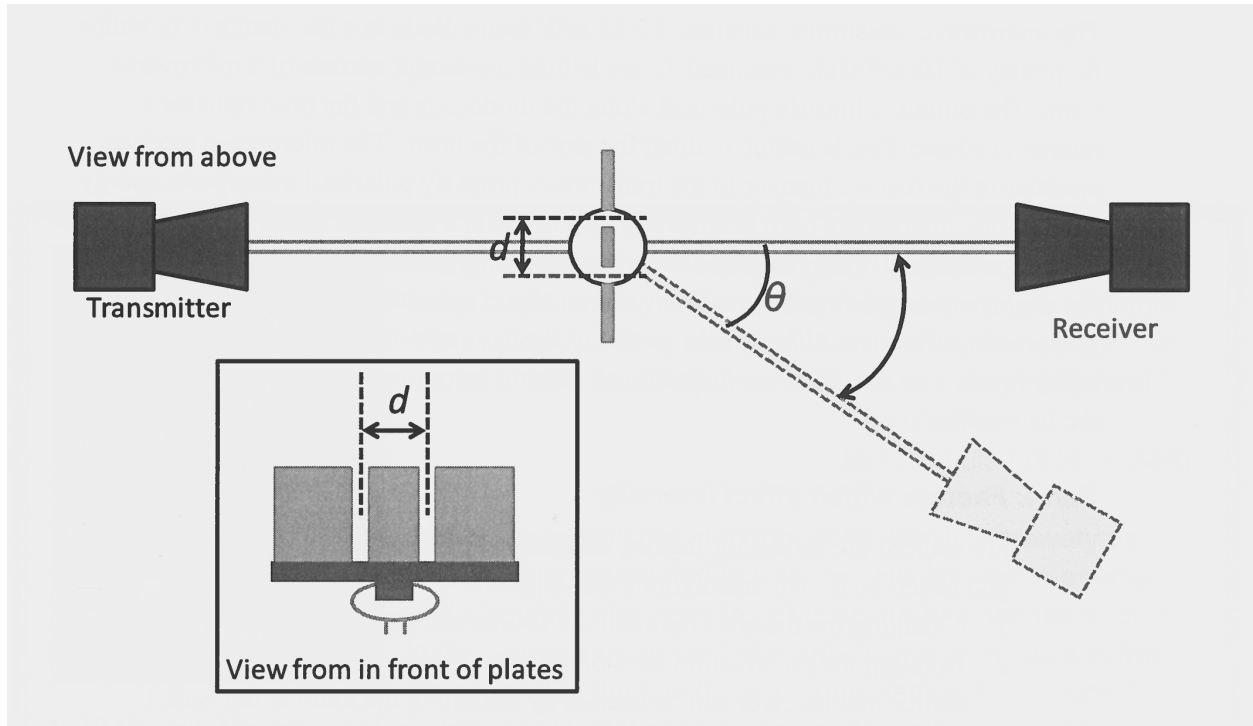


Figure 2.1: Apparatus setup for the double-slit interference experiment.

Variable	Value
θ_0	180°
θ_1	$(159 \pm 2)^\circ$
d	$(8.0 \pm 0.2) \text{ cm}$

Table 2.2: Data gathered from the double-slit experiment.

vertical as possible. Now, rotate the receiver arm slowly to find the first diffraction maximum. If necessary, move the arm the other way around to confirm the angle between the centre and the first diffraction maximum.

Before continuing with the calculation, we need to get the expression for the uncertainty of $\sin \theta$. First, let's define $\sin \theta$ in terms of z .

$$z = \sin \theta$$

$$\frac{d}{d\theta}(z) = \cos \theta$$

Now, for a value of z , the uncertainty of z (and hence $\sin \theta$) is

$$\delta z = \frac{d}{d\theta}(z) \delta \theta$$

$$\delta(\sin \theta) = \cos \theta \delta \theta. \quad (2.2)$$

Get the values for θ and convert $\delta\theta$ to radians.

$$\begin{aligned}\theta &= 180^\circ - (159 \pm 2)^\circ \\ &= (21 \pm 2)^\circ \\ \delta\theta \text{ (radians)} &\approx 0.0349065850398866 \text{ (16 d.p.)}\end{aligned}$$

Find the value for λ using values obtained from the double-slit experiment.

$$\begin{aligned}\lambda &= d \sin \theta \\ &= (8.0 \text{ cm}) \sin 21^\circ \\ &= 2.866\,944 \text{ cm (6 d.p.)}\end{aligned}\quad \begin{aligned}\delta\lambda &= |\lambda| \left(\frac{\delta d}{d} + \frac{\delta(\sin \theta)}{\sin \theta} \right) \\ &= |(8.0 \text{ cm}) \sin 21^\circ| \left(\frac{0.2 \text{ cm}}{8.0 \text{ cm}} + \frac{(\cos 21^\circ)(0.03490658 \dots)}{\sin 21^\circ} \right) \\ &\approx 0.332\,378 \text{ cm (to 6 d.p.)} \\ &\approx 0.3 \text{ cm (1 s.f.)}\end{aligned}$$

$$\therefore \lambda \approx (2.9 \pm 0.3) \text{ cm}$$

Convert λ to metre and find the value for v .

2.2.3 Single-slit interference method

3 Conclusions