

January Deliverable

1 Progress Made

Overall, progress made has been better than expected with 2 large sections completed and the most important section (The Sentiment Analysis Model) completed as a first draft. I will go back and refine the sections once I have received formal feedback but I am happy with where they are at the moment. Completing so much of the writing is a big step and should hopefully allow me more freedom to build on what I have actually developed closer to the deadline as I won't have to worry about writing so much.

The first proper stage completed was the literature review which was completed around 6 weeks into the first semester. I am happy with the research I was able to find surrounding the topic as I was unsure if such a niche topic would result in some problems in that area. Thankfully there are plenty of similar studies and additional research for the wider field of sentiment analysis which gave me much to write about. It also taught me a lot of useful information that made developing the sentiment analysis model much easier.

The development of the sentiment analysis model took a bit longer than initially expected, but I had not planned to do a write up for it this early so it has balanced out. I was able to fully research, implement and evaluate the sentiment analysis model achieving very good accuracy scores. This success makes me hopeful the approach I am taking can work and result in a prediction model that performs better than those I have seen in my literature review.

As well as this I have written an introduction and a explainer chapter for readers unfamiliar with the FPL game. This should hopefully make the report more readable and enjoyable for people new to the genre. It should also make the report a lot more clear in terms of any jargon or concepts that are not initially obvious.

2 Problems encountered

By far the biggest problem I encountered was the difficulty of obtaining twitter data. As this topic is so niche, it is hard to find good quality public datasets that are relevant and pre-labelled accurately. I was initially hoping to use the

twitter API to retrieve real-time tweets and create an autonomous system, but I found the price to be \$100 a month which is not something I can afford.

I then also realised that this meant I could not use this current season's FPL data as the only twitter data I can find is for previous seasons, so I would not be able to match sentiment analysis scores to this current season. This means it will be harder to go back and find historical player data (like goals scored, minutes played, red cards etc.) that matches the timestamps of my tweets to properly evaluate the final model. However, this should be doable given that data is needed for all things football related (not just FPL) and is very accessible.

I also had the problem of not being able to find hand-labelled data meaning some of the training labels are inaccurate. I stuck with this approach as a tradeoff between either that or having to manually label data which would have required lots of time and a labelling criteria. It would also have reduced the dataset size I would have been able to use, resulting in worse model performance. This is mentioned in the relevant section of my report.

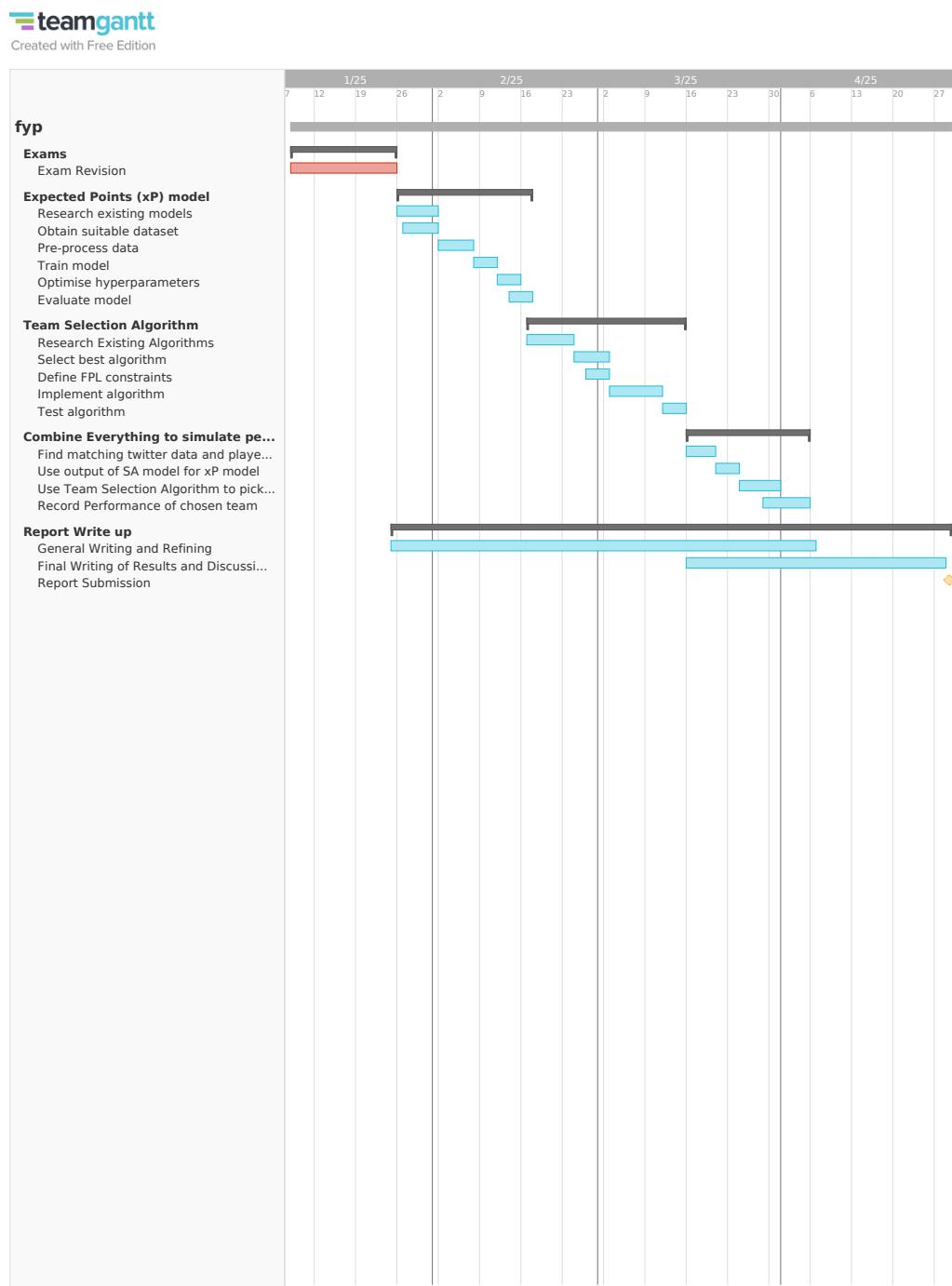
3 Changes of Direction

Given the problems encountered with obtaining twitter data, I have changed the main goal of the project from creating an autonomous system that uses real-time data, to investigating the performance gains that can be achieved when simulating the models I create on the historical data I can obtain. This is not ideal from a user experience point of view as no product is being created, but it will still contribute to the existing research surrounding this topic and the main parts of the system will still be the same. The system will be developed keeping in mind potential to integrate the twitter API and create an autonomous system, if sufficient funding can be secured.

This also means there is no need for an SQL database to keep current season data, as there are no tweets to go with them. Similarly there is no need for integration with the FPL API to automatically manage a team, and there is no need to scrape data from existing AI platforms as their current data will not be used.

To make up for this decrease in workload, I have decided to create my own expected points prediction model that uses the sentiment analysis model's output as an input parameter. I was unsure how to use the output of the sentiment analysis for picking an FPL squad, initially considering just taking an average of the output and adding or subtracting it to an expected points prediction from a third party. However, instead of blindly trialing different values and weights for this method, using my own model should correctly weight the sentiment analysis score in terms of an overall prediction, meaning it will not be too heavily relied on, or ignored too much. It should also allow me to better compare my results to other existing models by using the exact same input parameters and then adding sentiment analysis to see what difference it makes.

4 Updated Work Plan





Sentiment Analysis of Twitter to Optimise Fantasy Premier League Performance

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Chapter 1

Introduction

1.1 Background

Fantasy Premier League (FPL) is a popular online sports game based around the real-life top tier of English Football, the Premier League. Players of the game, often referred to as 'managers', are tasked with selecting a squad of 15 real-life premier league players every week. In game players are assigned a monetary value ranging from £4-15m, and each manager has a budget of £100m to build their team. The real-life performance of players determines how many points they are rewarded each week. Positive actions like scoring goals and providing assists increase points, whilst negative actions like receiving a red card or scoring an own-goal result in a decrease in points. Over the course of a 38-gameweek season, managers aim to score the most amount of points by rotating players in and out of their teams as they see fit.

The first version of FPL was launched in 2002 alongside the launch of the Premier League website, ahead of the 2002/3 season. Around 75,000 players participated in the first season [1], and since then growth has been explosive, with the player count surpassing 10 million in the 2022/23 season [2]. Each season the game has become more competitive, with the Premier League offering incentives such as a 7-night break inclusive of VIP hospitality tickets at two 2025/26 Premier League matches for the winner of the current season [3]. As well as the official prizes, many people participate in 'money leagues' where a small fee is paid for entry, and the winner takes home the prize pot. Alongside this more casual betting, professional gambling companies have started offering fantasy themed games where participants often stake money on day or weekend long periods, choosing a fantasy team to try and win them money by scoring the most points. With the global fantasy sports market valued at over \$27 billion in 2022, and projected to reach \$87 billion in 2031 [4], it is no surprise companies are scrambling to try and capitalise off of the immense popularity of the game.

With the increased popularity of FPL and a rapidly growing market full of potential customers, AI-based platforms aimed at increasing customers' overall ranks for little effort have started to emerge. These tools offer managers a quick and easy way to put together a team that they know will perform at a decent level, taking the effort out of the game for the managers who don't want to spend time diving through data and stats. AI tools also take the bias out of the game, as people tend to just pick their favourite players or players from their favourite teams, regardless of how well they are likely to perform in the game. Whether it be for monetary reasons, or for the simple pleasure of getting bragging rights over friends, the use of these platforms has shot up particularly in the last 2 years. One of the biggest AI platforms is *Fantasy Football Hub* [5], which launched in 2019 and has grown to over 40,000 paying users, with around £2.5m in annual revenue [6]. The platform uses a longitudinal multilevel regression model [7] in combination with the football data platform *Opta* to analyse each player's potential. The model is used to offer users of the platform recommendations for transfers, alongside a spreadsheet of points players are expected to score each week. By using this information to deliver customers clear and precise recommendations, *Fantasy Football Hub* has been successful in capturing a large customer base who can market their platform through word of mouth.

Another tool people consult when making FPL related decisions is social media, where users often share their teams with each other and discuss potential players to buy or sell. It was found that over 70% of FPL players find social media to be at least somewhat influential when it comes to making decisions around their team [8]. The FPL subreddit r/FantasyPL has over 700k members [9], and the official FPL Twitter account has a whopping 6.2m followers [10]. As well as the official accounts run by the Premier League themselves, many so called 'experts' have started to gain a large following on Twitter. Accounts such as @FPLGeneral, @FFScout, @BenCrellin, and @LetsTalk_FPL all have well over 250k followers, where useful tips and insights are often posted to help followers decide who to buy and sell each week.

However, using social media can often be a tedious process, sifting through thousands of posts trying to decide which ones to listen to - a stark contrast to the ease of use AI platforms bring. By leveraging sentiment analysis, this manual process can be automated, enabling AI to sift through vast amounts of data and extract meaningful insights. This study aims to explore how sentiment analysis can be applied to social media data and used in combination with existing AI models to enhance the accuracy of recommendations for FPL managers. In doing so it adds to the ongoing discussion around integrating human feedback into existing AI models used to forecast FPL performance. This study hopes to explore new areas with a particular emphasis on Twitter, a platform previously neglected when it comes to FPL research, due to the complicated jargon found in typical posts.

1.2 Project Aims and Objectives

1.2.1 Goals

The main goal of the project is to create a system that will take twitter data about English Premier League players as an input, and use a fine-tuned sentiment analysis model to analyse the twitter data. The sentiment for each player should be used to create an optimised forecast of a player's expected points (xP) for each *gameweek*. The system will then use a team selection algorithm to pick an optimal squad based on each player's xP and price. The team selection algorithm will also have to abide by the constraints placed on team selection by the official FPL rules.

Users should be able to interact with the system using commands via the console, however the data should be well organised to make it easy to integrate into a web or mobile app with a fully functioning user interface in the future. The system will be modular, meaning the sentiment analysis model, squad selection algorithm, and xP prediction models should be easily upgradable. This should allow the system to keep up with advancements in forecasting technologies that may arise in future.

To the knowledge of the author, no research has been done surrounding sentiment analysis of twitter for player performance forecasting in the FPL domain. This study aims to advance research in this area and further contribute to the existing fantasy sports forecasting research. The results of the system will be tested against existing research done with no sentiment analysis and the most popular AI FPL platform that charges users a subscription fee to use its services. As well as this, models that have used sentiment analysis of other forms of media such as news articles will be compared to test the suitability of using twitter as a data source. The system will be simulated over a range of gameweeks and its overall score will be compared to see where it ranks in the global leaderboard against other prediction methods.

1.2.2 Objectives

1. Analyse the project aims and break them down into key functional and non-functional requirements.
2. Conduct a literature review on fantasy sports forecasting and sentiment analysis techniques, as well as research on existing FPL forecasting platforms.
3. Fine-tune a sentiment analysis model specifically for capturing player sentiment in the FPL context, using labeled data for model training and validation.
4. Develop and validate a predictive model that uses Twitter sentiment, historical player data, and match fixtures to forecast a player's expected points (xP) for each gameweek.

5. Implement a team selection algorithm that optimises squad selection based on player xP, prices, and FPL constraints, ensuring compatibility with official game rules.
6. Test and evaluate the system by simulating its performance over multiple gameweeks against existing FPL forecasting methods, both with and without sentiment analysis.
7. Prepare a comprehensive report documenting the findings, challenges, and recommendations for future work by the end of the project.

1.2.3 Statistical Objectives

- The main goal of the system is to achieve a higher overall rank than existing models over the course of an FPL season.
- Evaluate the effectiveness of Twitter sentiment analysis in improving xP prediction accuracy by comparing the mean squared error (MSE) or root mean squared error (RMSE) of models with and without sentiment analysis.
- Assess the impact of the sentiment analysis model on team performance by comparing the total points scored by squads selected with and without sentiment-informed xP predictions.
- Measure the success of the team selection algorithm by analysing its ability to stay within the top 10% of the global leaderboard during simulations.
- Benchmark the system's results against popular AI-powered FPL platforms by comparing overall ranks, total points, and average weekly points.
- Compare data sources by conducting a statistical comparison against models using sentiment derived from other sources such as news articles.
- Ensure sufficient long-term prediction ability by analysing system performance across multiple gameweeks, accounting for variability in player form, injuries, and match conditions.

Chapter 2

FPL Description

Fantasy Premier League is something that can be quite confusing to someone unfamiliar with the game. With all the constraints and special abilities that are thrown in to add jeopardy, as well as the technical jargon often used in social media settings, it can be difficult to follow without a full understanding of the rules. This chapter will outline the rules in detail, along with the points scoring system, covering some jargon terms frequently used in the context of FPL.

The terms *player* and *manager* can often be confused when it comes to FPL, so please be aware that this study uses the term *manager* to refer to people who participate in the game of FPL, and *players* to refer to real-life premier league footballers.

2.1 Rules of FPL

Fantasy Premier League is a mirror of the real-life English Premier League, meaning that each in game event (referred to as a *gameweek*) represents a set of real-life football matches - typically played out over a weekend. The game takes place over a *season* which usually runs from August until May of the following calendar year, and at the end of the season the winner is crowned. There are 20 teams who play each other twice over the course of the season, resulting in a total of 38 gameweeks (not 40 as they cannot play themselves). Note that sometimes due to unforeseen circumstances like bad weather or domestic cup fixtures, games are postponed resulting in a team not playing in one gameweek (known as a *blank* gameweek), and playing twice in another gameweek (known as a *double* gameweek) to make up.

Upon the start of the season, each manager is tasked with choosing a team of players from a database of around 500. A team must be made up of 15 players, consisting of 2 goalkeepers (GKs), 5 defenders (DEFs), 5 midfielders (MIDs), and 3 strikers (STs). On top of these positional constraints, each

player is assigned a monetary value in £m's roughly according to how well they performed in the previous season, and the manager is given a budget of £100m from which they must select their team. A final constraint on team selection is that you cannot select more than 3 players from the same real-life football team, so it would not be possible to buy the whole Manchester United team, for example. Managers can edit their team as much as they like for no penalty before the first gameweek starts, but after that point changes start to incur penalties.

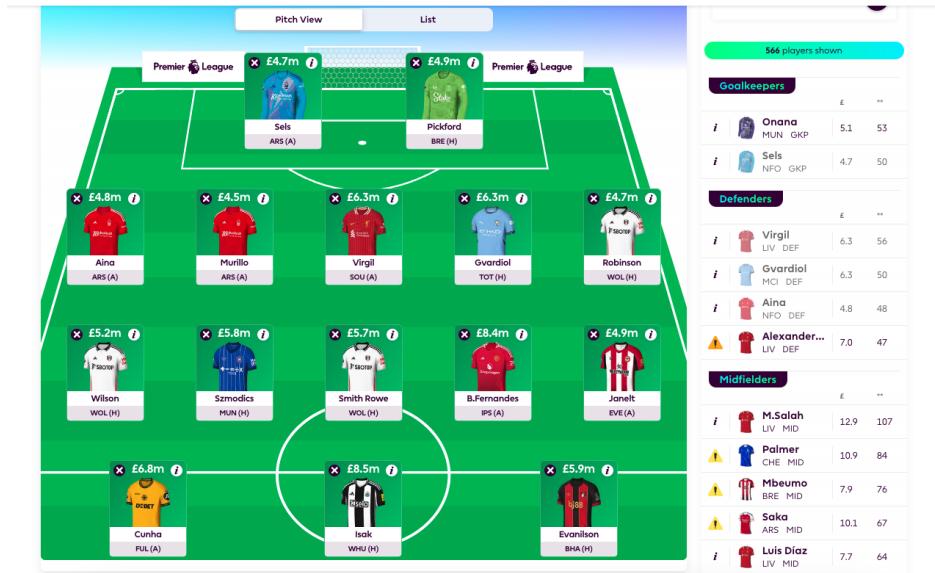


Figure 2.1: Initial Team Selection

Replacing a player in your team with another is known as a *transfer*, and has certain costs that come with it. Each manager is given 1 *free transfer* (also known as an *FT*) every gameweek, which can accumulate up to a maximum of 5. Managers who make a number of transfers that is higher than their free transfer balance have to pay 4 points per additional transfer - referred to as a *hit*. Transfers cannot lead to illegal teams, i.e. teams resulting from transfers must still meet the positional, budgetary, and 3-player per team constraints mentioned above.

Another variable affecting team selection is price changes. Throughout the season player's values will go up and down depending on how many managers transfer them in and out of their team. The more people buying a player, the more expensive they become and vice versa. This means managers can grow their budget by selling players who have gone up in value. When a manager sells a player who has gone up in value, the manager only receives 50% of that increase rounded down to the nearest £0.1m. So if a manager bought a player

for £5m and sells them at £5.5m, the manager will only receive £5.2m back. However, when a player goes down in value, the manager suffers the full price loss.

Upon selection of a team, for each gameweek managers must choose 11 *starters* (a *starting 11*) and 4 *substitutes* or '*subs*'. The starting 11 is the set of players who contribute to a manager's overall score (points scored by substitutes do not count towards their total). A starting 11 must consist of at least 3 DEFs, 3 MIDs, 1 ST, and exactly 1 GK. Subs will replace starters in the event that the starting player does not play a single minute in their real-life match. Before the start of the gameweek, the manager must choose a substitution preference, which is the order in which substitutes replace starters. This preference does not supersede the starting 11 constraints - that is, if a defender did not play in real-life and a midfielder was first in the substitute preference, the midfielder would not replace the defender if it resulted in a team with less than 3 defenders.

One of the most important choices a manger must make is who to *captain*. Giving a player captaincy places a 2x multiplier on their points, meaning if they were to score 10 points the manager would receive 20. A vice-captain is also chosen, and in the case that the captain is replaced by a substitute they will become the new captain.

A gameweek *deadline* is the final opportunity for managers to make changes to their teams for that gameweek. This deadline always occurs 90 minutes before the first real-life match of the gameweek. Once the deadline passes, any changes made will apply only to the following gameweek. Points are then awarded based on the outcomes of the matches over the next few days. This process of team selection, deadlines, and scoring continues throughout the season, resulting in a leaderboard ranking that determines the winner.

Finally, managers are given *gamechips* or *chips* to use throughout the season that change the rules of the game for them, for one gameweek only. Currently the gamechips available to managers are as follows:

- Wildcard - allows a manager to make unlimited transfers for no points or free transfer cost
- Triple Captain - increases the captain multiplier to 3x points
- Bench Boost - substitute's points count towards the total
- Free Hit - managers can select a new team from scratch that will play for that gameweek, afterwards the manager's current team will be reinstated

Each manager is given one of each chip, apart from the wildcard which is given once in the first half of the season, and once again in the second half of the season. Gamechips cannot be used simultaneously.

2.2 Points System

Points are awarded to players based on the following criteria which differs depending on the position of the player.

Event	Goalkeeper	Defender	Midfielder	Striker
For playing up to 60 minutes (not including stoppage time)	1	1	1	1
For playing 60 minutes or more	2	2	2	2
For each goal scored	10	6	5	4
For each assist for a goal	3	3	3	3
For a clean sheet	4	4	1	-
For every 3 shots saved	1	-	-	-
For each penalty save	5	-	-	-
For each penalty miss	-2	-2	-2	-2
For every 2 goals conceded	-1	-1	-	-
For each yellow card	-1	-1	-1	-1
For each red card	-3	-3	-3	-3
For each own goal	-2	-2	-2	-2

Table 2.1: Scoring System Based on Events and Positions

An assist is awarded to the player who touched the ball last before the goalscorer, and if a goal is scored from a set piece like a free-kick or penalty, the player who won that set piece is awarded the assist.

Additionally, bonus points are awarded to 3 players each match in the increments of 1, 2, and 3 bonus points. These are awarded based on a bonus points system (BPS) which ranks players on a range of in-game statistics like passes, big chances created and goals scored. The 3 players with the most BPS points are given the bonuses. A full breakdown of the BPS can be found here <https://www.premierleague.com/news/106533>

Chapter 3

Literature Review

Due to the huge popularity of not only Fantasy Premier League, but the multiple games available for different sports under the fantasy sports genre, there exists a wide plethora of research and discussion around the given problem of maximising performance in fantasy sports. This study will look at the existing models that have been created and review how different machine learning methods stack up against each other. The existing research suggests that whilst many different techniques have been applied to varying degrees of success, using Twitter sentiment to predict player performance over the course of a whole season is a novel approach to the fantasy sports optimisation problem. The theory of wisdom of crowds and human-feedback aided models are explored to verify the benefits of using Twitter as a source of information. Finally, existing sentiment analysis methods are analysed to see how natural language is processed and evaluated to gather an overall sentiment value. The combination of all the research gives a good understanding for the necessity and validity of the approach this study focuses on.

3.1 Fantasy Sports Forecasting

The problem of optimising a player's score over the course of a whole fantasy season is an extremely difficult task. The magnitude of this difficulty was illustrated by Kristiansen et al. who developed a mathematical model to describe fantasy premier league, and found that during the 2017/18 season the top manager in the world only managed to achieve a score equivalent to 51.75% of the optimal solution [11]. Furthermore, the mean gap between the optimal solution and the top manager was around 60 points per week, whilst the mean gap between the top manager and the average manager was only 20 points per week. This huge gap highlights the complex intricacies of fantasy sports optimisation, where the sheer number of variables like player mood, injury status, and team rotation make it almost impossible for human strategies to get anywhere close to

an optimal solution. The large discrepancy between optimality and the current peak of human performance shows the potential for advanced machine learning methods to bring new insights and strategies that could help bridge the gap between human strategies and optimal performance.

In terms of existing mathematical and machine learning models, many solutions for predicting performance have already been created by researchers dating back to the early 2000s. These models all largely focus on using historical data with objective, performance-based metrics that describe exactly what a player or team has done in the past few weeks, combined with some sort of score that represents how difficult their upcoming games are going to be. In 2012 Matthews et al. modelled the problem of choosing a team as a belief-state Markov decision process, where player selections were actions that had some reward value [12]. Using a Bayesian Q-learning algorithm actions were chosen to maximise long-term reward, resulting in a team expected to score the most points. This approach retrospectively would have ranked within the top 1% of all managers during the 2010/11 season of FPL.

In 2018 GS created a binary classification model to classify players into groups that are 1 - expected to score at least 4 points in the next gameweek, and 2 - expected to score less than 4 points [13]. He experimented with using different tree models but eventually concluded using a Gradient Boost model was the most accurate, using historical performance data to generate a number between 0 and 1 for each player. A threshold value was then determined to best split the players into the two separate categories. This approach proved successful, with the model achieving a precision of 83% when choosing players expected to score at least 4 points in the next gameweek.

In 2022 Rajesh et al. used random forests and gradient boosting machines to create a system enabling the "average interested person" to make better decisions about who to include in their teams [14]. A key feature found in this study was that training multiple models for each playing position (goalkeeper, striker etc.) drastically increased performance in comparison with using one model for each position. All models used in this study were found to outperform the average player by at least 20%, with Gradient Boosting Machines (GBMs) performing the best.

Also In 2022 Bangdiwala et al. compared three different methods - Linear Regression, Decision Trees, and Random Forests - for predicting the total number of points players would score in their upcoming match [15]. He found that over the course of a whole season, the Linear Regression model performed the best with a smaller root mean square error and mean absolute error than the other two models. The Random Forest model was a close second and the Decision Tree model performed the worst. Another study in 2024 by Papageorgiou et al. compared 14 models for fantasy basketball and found the most effective models to be Random Forests, Bayesian Ridge and AdaBoost [16].

3.2 Wisdom of Crowds

In his 2005 book *The Wisdom of Crowds*, James Surowiecki explains how collective groups are often much better at predicting things than individuals [17]. Aristotle is credited as the first person to write about this theory in his work *Politics*. He stated "it is possible that the many, though not individually good men, yet when they come together may be better, not individually but collectively, than those who are so, just as public dinners to which many contribute are better than those supplied at one man's cost" [18]. This is illustrated in Francis Galton's *Vox Populi* where he describes a country fair in Plymouth in 1906 [19]. During the fair, a contest was being held to guess the weight of an ox. Galton observed that the median guess of a crowd of 800 people was within 1% accuracy of the correct number. Surowiecki uses this example to explain how "a crowd's individual judgement can be modelled as a probability distribution of responses, with the median value being close to the true value of the predicted quantity" [17].

An expansion on this theory is a new technique dubbed "surprisingly popular" [20]. This technique was discovered during a study at MIT's Sloan Neuroeconomics Lab in collaboration with Princeton University. In the study, participants were asked a series of questions for which they had to provide what they thought was the correct answer, alongside what they thought the most popular answer would be. Researchers found that taking the average difference between the two responses as the correct answer, reduced errors by 21.3 in comparison to simple majority results, and 24.2 percent in comparison to confidence weighted results, where participants gave a confidence score alongside their answer to express how confident they were with their answer.

Taking this knowledge back into an FPL context, research exists detailing how the use of crowd-based metrics such as a player's ownership percentage among other managers can benefit overall performance. In the earlier mentioned model built by GS, he states how using the concept of wisdom of crowds by adding features like player ownership%, transfers in, and transfers out to his gradient boost model improved the precision from 75% to 83.33% [13]. Another study in 2019 by Bonello et al. details how expanding on existing models with human feedback such as news articles and betting markets led to a performance increase of over 300 points over the course of a whole season, ranking within the top 0.5% of players in the world [21]. This is compared to a standard statistical model that only placed within the top 13%. The Bonello study also details how they explicitly decided against the use of Twitter posts in their model, as they found it hard to accurately derive sentiment from tweets due to grammatical errors, emoji usage, and football specific jargon. However, this study aims to use proper pre-processing and more accurate sentiment analysis methods that have emerged since 2019 (detailed in subsequent chapters) to eliminate these concerns, as there is a huge amount of data available on Twitter that should not be overlooked and it offers a large crowd of people all sharing opinions.

This is backed up by a 2022 study where Whittaker found that 72% of FPL players found social media to be at least somewhat influential in their decision making when it comes to their FPL team [8]. Twitter was also central to a 2019 study by Bhatt et al. where crowd wisdom was put to the test using Twitter sentiment as a metric for creating diverse crowds [22]. FPL related tweets were collected, and then matched to real people's FPL accounts. User's historical player selection was then collected, focusing specifically on who they chose to captain each week. The Twitter users were then clustered into diverse crowds based on the semantic diversity of their tweets, and further sampled from the clusters to create a final set of diverse crowds. Analysing the captaincy choice from these groups found that on average, the captaincy choice from a random group of 6 outperformed 73% of individuals, and the choice of a diverse group of 6 outperformed 93% of people.

3.3 Sentiment Analysis

The desire to capture and give meaning to public opinions has long been seen throughout history, with democratic voting as a measure of public opinion first appearing in early Greek civilisation in the 5th century BCE [23]. A paper by Droba published in the early 20th century outlines methods for collecting public opinion, explaining how early questionnaires were first deployed [24]. With the emergence of the internet in the last few decades, methods of gathering public opinion have shifted online making it much more efficient for organisations to gather relevant information. Companies have become interested in gathering opinions about their products or services through online reviews. With the explosion in popularity of social media, individual researchers have been able to gather information for tasks like predicting elections, stock market trends, and natural disasters [25].

Liu defines sentiment analysis or opinion mining as the field of study that analyses people's opinions, sentiments, evaluations, attitudes, and emotions from written language [26]. Patel et al. adds to this definition explaining it is a type of classification in which machine learning techniques are used to identify positive and negative words or reviews in text-driven databases [27]. Shah outlines the different methods that can be used for sentiment analysis, explaining their pros and cons [28]. In her article she explains the different machine learning models that are commonly used like the Naive Bayes algorithm that uses probability to determine whether a piece of text should be classified as positive, negative, or neutral. Recurrent Neural Networks (RNNs) and their variants Long Short-term Memory (LSTM) are mentioned due to their ability to handle long term dependencies often found in natural language.

In 2019, a new language representation model called Bidirectional Encoder Representation from Transformers (BERT) was introduced by Devlin et al. with a focus on pre-training deep bidirectional representations by jointly conditioning on both left and right context in all layers [29]. The ability of BERT to un-

derstand language context from both directions (unlike LSTM) more accurately meant it set new benchmarks in the natural language processing community, and has become a cornerstone of modern NLP research. BERT can be fine tuned on a multitude of tasks including sentiment analysis, and a study by Elankath et al. found that when used for sentiment analysis of Malayalam tweets, BERT was the top performing model in terms of accuracy when compared to other models like LSTM [30].

Targeted Aspect-Based Sentiment Analysis (TABSA) aims to determine sentiment toward specific targets, such as individuals or entities [31]. This idea is particularly important in the context of FPL sentiment analysis because tweets often mention multiple players. Identifying sentiment toward specific players is far more valuable than assessing the overall sentiment of a tweet. Sun et al. proposed a methodology using BERT to address TABSA by framing it as a sentence-pair classification task [32]. Their approach involves constructing an auxiliary sentence, such as "What do you think of the safety of location - 1?", and pairing it with the relevant context to identify the sentiment toward the specific target. Building on this idea, Hoang et al. advanced the methodology in 2019, achieving state-of-the-art results across various sentiment analysis benchmarks [33].

3.4 Summary

From the research explored, it is clear that there is a large gap between the points scored by the top performing manager in the world and the ceiling of potential points available. This gap highlights the potentially undiscovered strategies that machine learning models could discover to help bridge that gap and outperform other human managers. The existing models used for optimising FPL performance have been able to perform well with some ranking inside the top 1% of all players in the world. Of these models, some of the best performing include Random Forests, Linear Regression and Gradient Boosting Machines. It is also clear that incorporating human feedback and crowd wisdom into these models helps to improve their performance by a significant margin. Using high-performing deep learning models like BERT can give accurate sentiment analysis of tweets, whilst targeted aspect-based sentiment analysis can further improve this by capturing sentiment towards people and groups.

Chapter 4

Sentiment Analysis Model

This chapter outlines the design decisions taken, their justifications and the implementation methods for the sentiment analysis model. This includes the underlying model architecture, training data used, tools used to fine-tune the model, and the evaluation process.

Whilst it is possible to train a sentiment analysis model from scratch, this study uses a pre-trained BERT model [29] available for free from Google. This approach leverages access to a model that has been trained on billions of texts, giving it an extremely complex understanding of natural language. A model trained from scratch could not hope to replicate such complexity given the timeframe of this project. It would also be unreasonable to expect such a large task to be completed without the use of advanced computing machinery unavailable to individual researchers without the backing of a large corporation. The BERT model has been chosen specifically because it has been proven to outperform other state-of-the-art models like LSTM in sentiment analysis tasks [30, 33].

This study will use fine-tuning to refine BERT for the specific task of sentiment analysis on the FPL tweets. Fine tuning is the process of adapting a pre-trained model for specific tasks or use-cases [34]. This is a much less computationally demanding task that requires only a small to mid sized dataset and computing power available to individual researchers, ideal for a project of this scale. By training the extensive natural language knowledge that BERT already has on a suitable dataset of FPL tweets, a sophisticated and accurate sentiment analysis model that suits the needs of the project will be achievable.

4.1 The BERT Model

Bidirectional Encoder Representation from Transformers or BERT [29], is a pre-trained language representation model based on the transformer architecture proposed in the now infamous 2017 paper "Attention is All You Need" [35]. The transformer is a deep learning architecture that is the backbone of some of the most prominent achievements in AI in recent years, including OpenAI's ChatGPT [36].

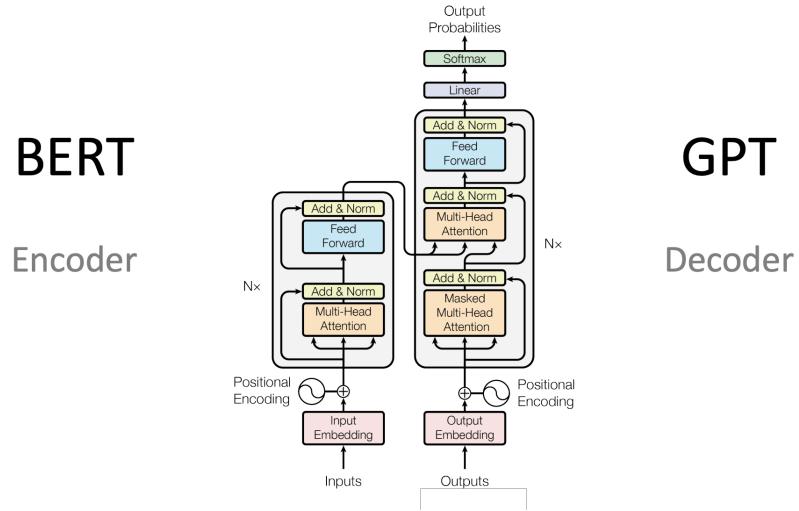


Figure 4.1: Architecture of a Transformer [35]

The original transformer architecture was designed for language translation, but has since been adopted and used for a vast array of other tasks, including for pre-trained systems like BERT and Generative Pre-trained Transformers (GPTs) [37]. The transformer is made up of two parts; the encoder, and the decoder. A few months after the transformer architecture was proposed, researchers started experimenting with the idea of separating the encoder and the decoder resulting in some incredible breakthroughs. The creation of encoder-only and decoder-only transformers is what has resulted in the AI boom that we have seen today with large language models like GPTs [36] and BERT [29]. BERT is made up of deeply bidirectional encoder-only transformers which although have been more understated than their decoder-only siblings (used in ChatGPT), are still extremely powerful for natural language tasks like sentiment analysis.

4.1.1 Tokenisation

To split large pieces of text into more manageable chunks of data so that natural language models can process and understand them better, a process known as tokenisation is carried out on the training data [38].

In the BERT model, raw text is broken down into tokens using the WordPiece tokenisation algorithm [39]. As opposed to word-level or character-level tokenisation, where whole words or individual characters represent tokens, the WordPiece algorithm is a subword-level tokenisation algorithm. This means words are split into one or more tokens such as '`token`' and '`isation`'.

The algorithm starts by generating an initial vocabulary from the training data, by splitting each word in the data into individual characters. Each character that does not start a word is prefixed with '`##`' to indicate it is a sub-word, so the word '`word`' would be split like this: '`w`', '`##o`', '`##r`', '`##d`'. WordPiece then computes a score for each pair that occurs in the training data using the following formula:

$$\text{score} = \frac{\text{pair_freq}}{\text{first_element_freq} \times \text{second_element_freq}}$$

The pair with the highest score is merged into 1 token and added to the vocabulary, and the same merge is applied to the set of pairs of tokens. This process is then repeated until the vocabulary reaches a desired size. The BERT vocabulary is sized around 30k tokens [29].

Once the vocabulary has been generated, words can be tokenised. This is done by iterating through each word in a piece of text, and looking for the longest available token at the start of a word. If one is found, the algorithm does the same for the next part of the word, and so on until the whole word is tokenised. If the algorithm finds a part of a word that has no matching token in the vocabulary, the **entire word** is given the special token [UNK] or unknown [39]. So if we had a vocabulary of ['hel', 'lo', 'worl'] and the sentence 'hello world', the resulting tokenisation output would be ['hel', 'lo', [UNK]].

The BERT model also uses the special tokens [CLS] (classifier) and [SEP] (separator). The CLS token is placed at the very start of the input, and for sentiment analysis tasks it has a hidden state associated with it that will be passed to a classifier to predict sentiment after the input has been processed [40]. The SEP token is used to separate two sentences for tasks such as question-answering and dual-sentence classification [29].

4.1.2 Input Embeddings

After text has been tokenised, it needs to be converted into numerical values using text encoding. Text encoding allows raw text to be handled by neural networks which only take numerical values as input, not raw text [38]. The raw text is converted into a set of vectors called word embeddings, which can be processed by the encoder’s neural network. Embeddings give meaning to tokens, with similar tokens like ‘great’ and ‘awesome’ closer together in vector space, and opposites like ‘sad’ and ‘happy’ further apart [41].

The embedding layer creates word embeddings (or subword embeddings, in the case of BERT) for each token in the input using 3 different types of embeddings: token embeddings, positional embeddings, and token type embeddings [42].

- **Token embeddings** are vectors that have been learned during the model’s pre-training phase to place similar words close together in vector space, they are stored in an embedding matrix.
- **Positional embeddings** are vectors given to each token that represent their positions in the input sentence.
- **Token type embeddings** are often used for two-sentence NLP tasks like question-answering to tell BERT which tokens belong to each sentence, for one-sentence tasks like typical sentiment analysis, all tokens are assigned the same vector.

The embedding layer then sums these embeddings together, and applies normalisation to their sum. The resulting vector output contains meaningful information about each token and its position in the input. These embeddings are passed into the subsequent transformer layers of the BERT model for processing.

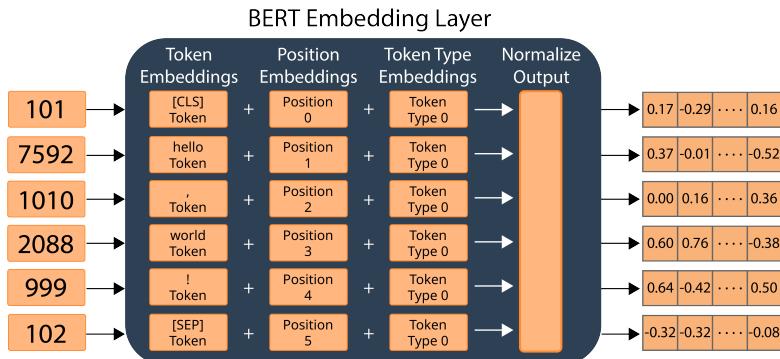


Figure 4.2: BERT Embedding Layer [42]

4.1.3 Multi-Head Attention

A fundamental concept of the transformer architecture is 'self-attention' [35]. Given the sentence: '*I took the pizza out of the oven and then ate it.*' it is apparent to any human that 'it' refers to the pizza and not oven, based on the surrounding context. Neural networks however lack the ability to identify this relationship, and require mechanisms like self-attention in order to resolve such ambiguities.

Self-attention allows neural networks to identify the importance of each token in relation to the other tokens in the input. To calculate attention values, BERT uses multiple attention 'heads' which all focus on different linguistic features of the input. Each head involves 3 components: the query (Q), the key (K), and the value (V) matrices [35]. Each of these matrices are made up of the input embeddings of the previous layer (a vector for each token), and are identical to ensure that every token in the input interacts with every other token, including itself (the idea of self-attention).

Scaled Dot-Product Attention

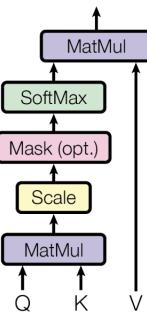


Figure 4.3: Scaled Dot Product Attention [35]

$$\text{Attention}(Q, K, V) = \text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) V$$

Here QK^T computes the similarity between the key and query matrices, scaled by $\sqrt{d_k}$ (the dimension of the embedding vectors), and then the softmax function [43] normalises these values into attention weights. These weights are applied to the value matrix, resulting in an attention net matrix representing the contextual relationship between tokens.

For all attention layer heads (BERT uses $h=12$ attention heads [29]), there is a linear layer that uses learned weights to project the input embeddings into separate Q , K , and V matrices for each head. This way different linguistic features can be explored by the model to improve its learning ability. The outputs (attention nets) from each head are then concatenated to form a unified representation:

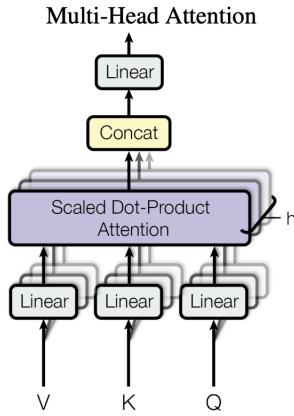


Figure 4.4: Multi-Head Attention [35]

$$\text{MultiHead}(Q, K, V) = \text{Concat}(\text{head}_1, \dots, \text{head}_h) W^O$$

$$\text{where } \text{head}_i = \text{Attention}\left(QW_i^Q, KW_i^K, VW_i^V\right).$$

Here, W_i^Q, W_i^K, W_i^V are the learned projection matrices for the i -th head, and W^O is the projection matrix for the final linear layer. This final layer aggregates the information from all attention heads to produce a final self-attention representation for the input [35].

4.1.4 Feed-Forward Network

The feed-forward neural network (FFNN) is the final stage of the encoder. It is a type of multi-layer perceptron (MLP), used for transforming the output of the self-attention mechanism into a refined representation that can capture deeper relationships within the input sequence [44].

The FFNN processes input embeddings by first projecting them into a higher-dimensional space. Specifically, the 768-dimensional input for each BERT token embedding [29] is transformed into a 3072-dimensional space via a linear projection. This expansion allows the model to explore more complex interactions among the input features. Following this, a ReLU activation function is applied to allow the model to identify more intricate non-linear patterns in the language. Finally, another linear projection reduces the representation back to its original dimensionality, ensuring compatibility with the encoder’s output structure [44].

The FFNN is essential for capturing patterns and interactions that the self-attention mechanism alone cannot model. Its reliance on simple matrix operations makes it computationally efficient and highly parallelisable, leveraging modern hardware accelerators like GPUs and multi-core CPUs to significantly reduce training time. To ensure stable training and enhance convergence, the FFNN’s output undergoes normalisation, producing the final output representation for the encoder.

4.1.5 Final BERT Architecture

The previous sub-sections have explored the components of the encoder, but the BERT model actually makes use of multiple encoders stacked together (12 for BERT_{base} which this study uses) [29]. This is what makes BERT a deep-learning model, as it incorporates many layers into its structure. The stacking of multiple encoders allows the model to progressively learn more high-level representations of the input data as it passes through the layers.

Each encoder layer outputs a 768-dimensional matrix capturing increasingly complex patterns and relationships in the data at every subsequent encoder layer. The output of the final encoder layer represents the most refined and meaningful representations for each token [29], which can then be used for downstream tasks. For sentence classification tasks like sentiment analysis, the special token ([CLS]) is used, and its final vector representation serves as the input to the classification head. The classification head takes the input vector and outputs a score representing the model’s sentiment prediction [40].

The depth of the architecture, combined with the self-attention mechanism, enables BERT to model long-range dependencies effectively. This is a huge benefit for processing natural language, where relationships between words are often spread across entire sentences or paragraphs.

4.1.6 Pre-Training

BERT was pre-trained using two tasks: Next Sentence Prediction (NSP) and Masked Language Modelling (MLM) [29].

The first task, MLM, is a technique for training deeply bidirectional models like BERT. Typical language models process tokens sequentially left-to-right, using preceding tokens in a sentence to predict the next. BERT, however, processes all tokens in a sentence simultaneously and can see both preceding and following tokens for each word. To predict a missing token in the middle of a sentence, BERT could "cheat" by leveraging full context, including the token to predict. To address this, word "masks" are applied to randomly hide tokens in a sentence [29], tasking BERT to predict them using only surrounding context. This technique enables BERT to learn bidirectional relationships, resulting in a more robust model than typical left-to-right ones.

The second task, NSP, teaches BERT to understand relationships between two sentences, useful for downstream tasks like Question Answering (QA) and Natural Language Inference (NLI). In this task, BERT is fed two input sentences, A and B, and must guess whether sentence B follows A or is unrelated. BERT is trained on an even split of positive and negative cases. This simple task produces remarkable results, with the final model achieving 97% accuracy on NSP tasks [29].

By leveraging these tasks across millions of sentences and performing millions of optimisation steps, BERT learns complex relationships between words and sentences [29]. The model's weights, including those for input embeddings and self-attention mechanisms, are updated via backpropagation [45] during this process.

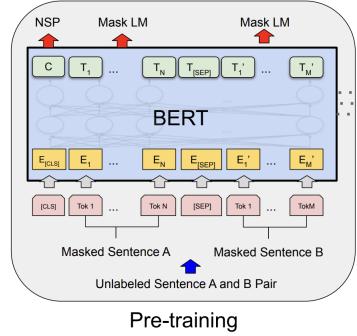


Figure 4.5: BERT Pre-Training [29]

This extensive pre-training enables BERT to capture nuanced patterns and relationships in text, which are then fine-tuned on downstream tasks like sentiment analysis, question answering, and named entity recognition [40].

4.1.7 Fine-Tuning BERT for Sentiment Analysis

Fine-tuning is the process of adapting a pre-trained model to a specific task by training it further on task-specific data [34]. For sentiment analysis, this involves adding a task-specific classification layer on top of the BERT encoder stack [29]. Fine-tuning combines BERT’s pre-trained understanding of language with additional knowledge it needs for the unique challenges of sentiment analysis.

After an input sentence passes through the model, the final hidden state vector \mathbf{h} corresponding to [CLS] acts as a condensed representation of the entire sequence, capturing its sentiment information. A softmax [43] classifier is then applied to predict the probability of each sentiment label c [40]:

$$p(c|\mathbf{h}) = \text{softmax}(W\mathbf{h})$$

Here, W represents the task-specific parameter weights matrix, and the sentiment label with the highest probability is chosen as the final prediction.

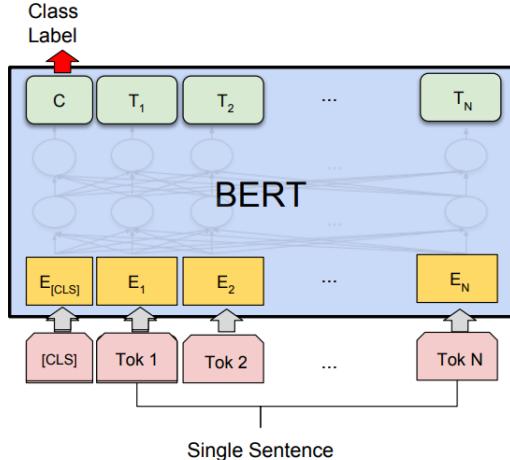


Figure 4.6: Single sentence classification [46]

Using a labeled dataset of texts and their corresponding sentiment labels (e.g., ‘positive,’ ‘negative,’ ‘neutral’), the model is trained to minimise a classification loss, such as cross-entropy. During training, the model’s predictions are compared to their labels, and all weights (including embedding, self-attention, classification etc.) are updated iteratively to improve accuracy. This process is repeated for a set number of epochs (complete passes through the dataset) to improve accuracy whilst preventing overfitting.

For the more complicated task of Targeted Aspect-Based Sentiment Analysis (TABSA), a proven fine-tuning approach involves reframing the problem as a sentence-pair classification task [32]. This method involves constructing an

auxiliary sentence to specify the target and aspect BERT needs to predict. In the context of FPL, the auxiliary sentence could be: "Should *player* be in my FPL team?". Then when given a sentence like "Mo Salah was excellent, but Haaland was awful," an auxiliary sentence is created for each player by replacing the placeholder *player* with the actual player's name; "Should Mo Salah be in my FPL team?" and "Should Haaland be in my FPL team?".

During fine-tuning, BERT processes the auxiliary sentence followed by the [SEP] token and the original sentence for each player. Classification is done in the same way as normal sentiment analysis with the hidden vector h used to predict the label (in this example the labels would be answers to the auxiliary question: 'yes', 'no' or 'unsure'). This approach enables BERT to focus on the sentiment directed toward each specific player, rather than providing a single sentiment value for the entire sentence. A single value would likely be uninformative, as positive and negative sentiments could cancel each other out. By targeting individual players, this method ensures more accurate predictions, with players labeled according to their specific sentiment.

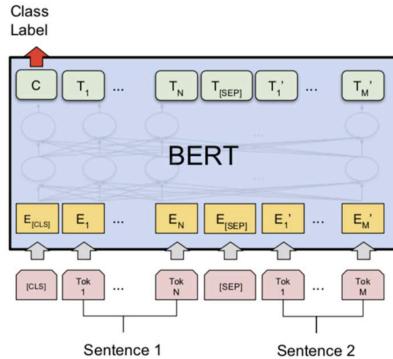


Figure 4.7: Sentence-pair classification [47]

This fine-tuning process not only adapts BERT to specific targets but also allows it to capture domain-specific language features that differ from general usage. For instance, while the word "soft" might generally convey positive sentiment (e.g., a soft blanket), in the FPL context, calling a player "soft" is often a negative sentiment. By fine-tuning BERT on domain-specific tweets, the model can learn such nuanced language patterns, improving its accuracy in the target domain.

Fine-tuning BERT is computationally efficient compared to training a model from scratch and requires a relatively small amount of labeled data. This makes it a practical choice for sentiment analysis tasks across diverse domains.

4.2 Model Implementation

The BERT model used in this study to predict sentiment for FPL players was fine-tuned in Google Colab [48] using Python. Google Colab is a cloud computing platform that was chosen as it allows free GPU and TPU access, much better suited to fine-tuning a deep learning model than a CPU found in a typical laptop, helping reduce training time. Its notebook format also allows for simple and clear separation of functions, allowing for single blocks of code to be independently executed. This allows for easy debugging and troubleshooting of code, improving the development experience.

Python was chosen as the preferred language due to the extensive number of libraries that exist supporting the development of deep learning models. Some of the most popular include Hugging Face’s Transformers library [49] which contains APIs for hundreds of pre-trained transformer models including BERT. The transformers library also includes tokenisers for each model and a PyTorch [50] Trainer class that allows fine-tuning to be done with just a few lines of code. The model’s hyper-parameters can be fine tuned and optimised using the Optuna library [51] to explore the best possible combinations. Use of these libraries ensure correct approaches are taken, and massively reduce development time by simplifying the entire process.

4.2.1 Data Collection

Identifying and collecting suitable data for fine-tuning the model is a critical step in creating a model with optimal performance. The quality of the fine-tuning data directly affects the model’s output quality [52], so it is important to chose a dataset carefully.

The first approach considered was manual data collection directly via Twitter, however exploring this approach led to many dead ends. The first problem was the financial cost of using the official Twitter API, which has seen a price increase from \$3 per month to \$100 per month [53] since the company was sold in 2022. This change has led to many free tools aimed at helping researchers leverage twitter data for their studies being shut down, impacting the entire research field by limiting the options they have when it comes to collecting data. Without being able to use these tools, and with the official API unaffordable, using the API to efficiently collect data was not an option. Whilst other methods of collecting data exist, such as writing code scripts to scrape data from the Twitter website, or using 3rd party browser extensions, these methods are against the Twitter terms of service and could result in a permanent account ban if caught.

Manual collection of data on Twitter is an acceptable approach within the terms of service, however it is an extremely tedious process. When considering a dataset needed to fine tune a BERT model should contain thousands of entries, as well as the time constraints of this project, manually collecting and then labelling thousands of tweets was also not an option.

The chosen approach was an exploration of existing datasets published on popular machine learning forums such as Hugging Face and Kaggle. These sites have thousands of active users contributing to a wide range of research topics. As such, finding a dataset for a similar purpose to this study's was not difficult. 4 potential datasets were identified on Kaggle, and include:

- Fifa World Cup 2022 Tweets with Sentiment Labels - (30k tweets)
- Premier League Teams Tweets with Sentiment Labels - (460k tweets)
- FPL Tweets from 2012 - 2023, unlabelled - (110k tweets)
- Premier League Players Tweets with Sentiment Labels - (167k tweets)

A further inspection of these 4 datasets was carried out to identify the most suitable given the needs of the model being built.

The first dataset, whilst labelled, only contained tweets for the first day of the world cup. This meant a majority of tweets were centred around the event as a whole and the controversy of Qatar hosting, with little mention of players or actions they had carried out during football matches. The second dataset was much more suited to the needs of the model, however had the drawback of being centred around teams rather than individual players. The third dataset was focused specifically on FPL which appeared ideal at first. However it was found that this dataset contained a lot of unrelated tweets from people tweeting about their own performance in FPL, instead of expected performance of actual players.

	into fantasy premier league. Shows how far one good game can get yo...
ddreid88	I scored 61 points in Gameweek 20 on Fantasy Premier League http://t.co/4ys8YkcE
ahmedkungora16	I scored 71 points in Gameweek 20 on Fantasy Premier League http://t.co/6XBH1fVh
murray_rankin	My life's ambition is to one week be the highest scorer on Fantasy Premier League. #fpl #aiminghigh

Figure 4.8: Examples of noisy tweets irrelevant to player performance, such as personal FPL commentary

The fourth and final dataset was identified as the most suitable for this study. This dataset contains a far greater number of relevant tweets, focused on individual Premier League players from the 2022/23 season (it is almost impossible to find more recent data, due to the Twitter API price changes coming into effect from 2023). As well as the relevant focus of the tweets themselves, this dataset contains player labels for each row which is perfect for construction of an auxiliary sentence for target-based sentiment analysis. Instead of manually searching for players in each tweet, the existing *player_name* column in the dataset can be used. Finally, this dataset comes with the advantage of being almost fully cleaned of any noise including emojis, links, images, etc. reducing the amount of pre-processing required.

The sentiment labels provided in the dataset were automatically created by the Vader [54], and TextBlob [55] models. These models are fairly accurate however it is worth noting they do incorrectly label some tweets and therefore this dataset is not perfect. A potential solution to this problem is manually labelling the tweets, however this would require some criteria to match certain labels to tweets, and would also be extremely time consuming. Given the time constraints of this project and the limited human resources available for labelling, the dataset's size would have to decrease significantly to use a manual labelling approach. It is hoped that using the existing labels will be more beneficial due to the much larger dataset size available with this approach, which should result in a more accurate final model.

4.2.2 Data Pre-Processing

The dataset was cut down to a more suitable size of around 20k tweets to keep training time reasonable (the original 167k size would take around 4 hours to train a single epoch). This was done using the Hugging Face Datasets library to randomly pick around 12% of the dataset using the *train_test_split* method. This uses a random sampling approach to reduce biases. Reducing the dataset size will most likely affect the models performance negatively, however given the time constraints of this project the computation time required to train the model on a dataset over 100k rows would have been too large.

Additionally, unseen data was required for evaluation of the model, as well as for testing and implementing the expected points (xP) model described in Chapter 5, so leaving a portion of the dataset for later use was necessary. The sentiment analysis model's output serves as an input parameter for the xP model, so using the same data for both training and testing would compromise the validity of the results. Training on the unseen data ensures accurate and reliable performance evaluation.

Next, the dataset was cleaned which meant removing unnecessary columns, removing any duplicate rows, and cleaning the text values to remove noise. The published dataset had been cleaned of most noise expected from tweets such as emojis and hashtags, however there were still some image links which all

started with the *a href* tag. To remove the noise, a regular expression was used to search for the tag and everything that came after it was removed. Removing noise should help focus the model to learn relationships between meaningful text, rather than irrelevant text that has no effect on sentiment.

Additionally, some rows had a player_name that did not actually appear in the text which is an error and invalidates the auxiliary sentence method to be used for target-based sentiment analysis. To fix this a regular expression search was done in each row to ensure the player_name occurred in the corresponding text.

In terms of the existing sentiment labels in the dataset, the TextBlob labels were ignored and instead the Vader labels were used as this model was designed specifically for social media texts, so it should be more accurate for this dataset. The 'vader_emotion' label was used which specifies whether text has a 'positive', 'negative', or 'neutral' sentiment.

After cleaning the data, the dataset size was around 14k rows. The next step was to create an auxiliary sentence for target-based sentiment analysis, which the model was trained on. The chosen format was: "What do you think of the sentiment towards *placeholder*?". A possible improvement could involve a question more directly related to Fantasy Premier League (FPL), such as: "Should *placeholder* be in my FPL squad?" In this case, sentiment labels like 'positive', 'neutral', and 'negative' could be mapped to 'yes', 'unsure', and 'no', respectively. However, using labels from Vader (a sentiment model) could lead to mismatches in labeling. For instance, the tweet "*Jamie Vardy has great hair!*" might be labeled as 'yes', suggesting a positive FPL outlook, despite the tweet not being relevant to his actual FPL performance.

This mismatch highlights the potential benefit of manual labeling to more accurately answer the focused question. However, given that this study uses pre-labeled sentiment values, a more general question was selected. The rationale behind this choice is that an overall positive sentiment is expected to correlate to anticipation of a good performance in the context of FPL.

```

question \
0 What do you think of the sentiment towards EVAN FERGUSON?
1 What do you think of the sentiment towards RENAN LODI?
2 What do you think of the sentiment towards BEN MEE?
3 What do you think of the sentiment towards RODRIGO BENTANCUR?
4 What do you think of the sentiment towards FABIO VIEIRA?

context \
0 Bring in Evan Ferguson right along with him Hard to think of a more perfect ...
1 Imagine renan lodi at lwb rather than carassco with this cholo supertean
2 Bit no one in the comments is taking you seriously How ironic Has Ake suffer...
3 Since he arrived Rodrigo Bentancur gives verdict on Tottenham s summer signi...
4 Started Fabio Vieira Turner Kiwi vs Sporting looooo keep lying to yourself...

label
0 positive
1 neutral
2 negative
3 positive
4 negative

```

Figure 4.9: Cleaned Dataset with Auxiliary Sentence.

Once the auxiliary sentence was constructed, the dataset was ready to be divided into training and validation subsets. These splits are essential to prevent the model from overfitting. Overfitting occurs when a model learns to recognise specific patterns in the training data too well, to the point where it performs poorly on new, unseen data. To mitigate this, the validation set is used to evaluate the model’s performance on data it hasn’t been trained on, providing a measure of how well it generalises and ensuring that the model does not overfit the training data. The same method and code used to reduce the original dataset down to a smaller size was used to randomly split the data into training and validation subsets. This provided a random split, ensuring that there was no bias involved which could affect the training process.

Finally, the text data needed to be tokenised so it could be fed into the BERT model as input. The reason the dataset was split before tokenisation is to prevent the tokeniser from learning vocabulary that might not end up in the training data. This could unintentionally provide the model with information about the validation dataset, resulting in biased performance. Instead both the training and validation subsets are tokenised separately.

Hugging Face’s transformers library provides a simple *Tokenizer* API which makes tokenising text extremely easy. A pre-trained BERT tokeniser was loaded in from Hugging Face and then passed both the auxiliary sentence and context as input. The labels were also mapped to numerical values so that the BERT model could understand them. Examining the output of the tokeniser (converted back to text from the numerical IDs) for one of the rows shows it has been correctly formatted.

```
→ [CLS] What do you think of the sentiment towards J ##OR ##DA ##N H ##EN ##DE  
##RS ##ON ? [SEP] G ##ini w ##i ##jn ##ald ##um sad ##io man ##e and now Bobby  
firm ##ino 3 players who we should have kept for another few years but instead  
we keep m ##o sa ##lah j ##ord ##an Henderson and James Milne ##r wall ##ahi  
this club deserves to suffer [SEP] [PAD] [PAD] [PAD] [PAD] [PAD] [PAD]
```

Figure 4.10: Human-readable tokeniser output

The [PAD] token is a special padding token used to keep all the inputs the same length regardless of sentence length.

4.2.3 Training the Model

Once the data had been pre-processed, the model could be trained. The first step of training was to configure the `TrainingArguments` from the `transformers` library. This class contains the hyper-parameters for the model such as learning rate, batch size, epochs, and weight decay. These hyper-parameters can be tweaked to improve model performance and prevent overfitting during training. Initially, these were set to default values suggested by the Hugging Face tutorial, with the intention to optimise them properly later (see 4.2.4).

After these arguments were configured, the next step was to set up the `Trainer` object. The pre-trained `BertForSequenceClassification` model was loaded in from the `transformers` library. This model is configured for classification tasks on 2 input sentences with a suitable classification head already implemented, exactly what is needed for target-based sentiment analysis with an auxiliary sentence. The specific model used was 'bert-base-cased' which is just the base variant of the BERT model that is case-sensitive. The `Trainer` was initialised by passing in the model, datasets and training arguments. Once the `Trainer` had been initialised, the training process was started by calling the `train()` method.

Training took around 90 minutes, and the resulting model scored an initial accuracy of around 90.34%. Other performance metrics such as precision and F1 score were configured and will be discussed further during final model evaluation. Focusing on the validation loss, it is clear that the initial model is starting to overfit the training data as the epochs go on, evidenced by the increasing values after epoch 2. This is something that will be refined using hyper-parameter tuning.

Epoch	Training Loss	Validation Loss	Accuracy	Precision	Recall	F1
1	0.563300	0.371035	0.874471	0.873259	0.874471	0.873576
2	0.254500	0.351286	0.894922	0.894328	0.894922	0.894551
3	0.161700	0.411752	0.894217	0.895339	0.894217	0.894556
4	0.095200	0.475788	0.906911	0.906136	0.906911	0.906134
5	0.061300	0.531063	0.903385	0.902512	0.903385	0.902537

Figure 4.11: Performance metrics for the initial model

Once trained, the model was tested to ensure it worked as expected. 5 samples from the unseen data were taken and passed through the model to infer an output. The unseen data was processed by the same tokeniser function used for the training data to ensure the data used for model inference was pre-processed in the exact same way as the training data. This is crucial for achieving an accurate prediction from the model by ensuring the model recognises the inputs and can leverage knowledge learned during training to the fullest extent. Inference was done using the built in `eval()` method that the transformers library provides for every model.

```

Map: 100% [██████████] 5/5 [00:00<00:00, 245.21 examples/s]
Question: What do you think of the sentiment towards TYLER ADAMS?
Context: Tyler Adams and Jonathan David don t exist
Predicted Label: neutral

Question: What do you think of the sentiment towards TAKEHIRO TOMIYASU?
Context: Richardson clashed with Takehiro Tomiyasu on the touchline during Sunday s tense north London derby
Predicted Label: negative

Question: What do you think of the sentiment towards LUKE AYLING?
Context: Patrick Bamford hails Luke Ayling s crucial widespread impact after Leeds United extension
Predicted Label: positive

Question: What do you think of the sentiment towards JHON DURAN?
Context: We love you supe Jhon Duran
Predicted Label: positive

Question: What do you think of the sentiment towards NICK POPE?
Context: it s nick pope s world and everybody is living in it
Predicted Label: neutral

```

Figure 4.12: The model’s predictions on unseen data

Model outputs appear to be mostly correct and are easily retrieved through the built-in methods provided by the transformers library. This allows for a quick and efficient way to generate a list of sentiment predictions for a large set of tweets, necessary for the final system.

4.2.4 Hyper-parameter Optimisation

Selecting a suitable set of hyper-parameters is crucial for model performance. Adjusting these values during training can help the model to avoid overfitting the training data, minimise validation loss, and maximise accuracy [56]. Typically when implementing a machine learning model, researchers manually tweak hyper-parameters and spend significant time exploring configurations that may not improve performance meaningfully. This manual process is inefficient and resource-intensive, so by using an automatic framework, less computational resources and time is spent developing the model.

The framework chosen was Optuna [51], an automatic hyper-parameter optimisation framework for python that finds the most optimal hyper-parameter values via trial and error. It conducts a series of trials and uses the previous trial to identify promising potential tweaks that could be made to improve performance. This process is repeated and a history of trials is kept throughout the process to guide the next changes made to the hyper-parameters. Through enough trial and error, optimal hyper-parameter values are found. Optuna is a well documented library with great Python integration, making it an ideal choice for this project.

The first step in configuring Optuna was to specify the hyper-parameters to be tweaked and the space to be explored. The search space for hyper-parameters was defined based on the values recommended in the original BERT paper [29]. The chosen hyper-parameters along with their respective search space were:

- Learning Rate (2×10^{-5} to 5×10^{-5}) - determines the step size at which the model updates its weights during training. A higher learning rate can speed up training time but risks overshooting the optimal parameters, whilst a lower learning rate ensures stability but may result in slower training.
- Batch Size (16 or 32) - Batch size refers to the number of training samples processed simultaneously before updating the model's weights. A smaller batch size can introduce noise in the gradient updates, which sometimes aids in escaping local minima but can lead to slower convergence. A larger batch size offers smoother gradient updates but may require more computational resources and risks overfitting.
- Number of Epochs (2 to 4) - specifies how many times the entire training dataset will be processed by the model during fine-tuning. Too many epochs can cause the model to focus on specific patterns in the training data, leading to overfitting. Too few epochs can limit the model's ability to learn from the data and lead to poor accuracy.

An objective function was defined to guide the hyper-parameter tuning process. This function evaluates the performance of each 'trial' which is a model trained on a set of hyper-parameters suggested by Optuna. It defines the search space and hyper-parameters available, and then feeds Optuna's suggestions into each model's training arguments. It also specifies which metric to use to evaluate this models - validation loss in this case. The validation loss is a measure of how far away the model's predictions are from the labelled values. To achieve an accurate model, this metric should be as low as possible to indicate the model's guesses are very close to the truth.

The datasets used during this stage were slimmed down to reduce training time. Evaluating models trained with the entire dataset would have taken too long (90 mins per trial) and used too much computing resource, so instead a dataset 25% of the size was used. This approach should give a general view of the best configurations, which can be explored further using the whole dataset.

An Optuna study was created using the *create_study* method, and then run for 10 trials. This amount should allow Optuna to explore a sufficient amount of configurations while keeping resource usage to a minimum. Because Optuna chooses each subsequent configuration based on the previous one, each new configuration should explore meaningful search space and therefore enable a near optimal configuration to be found in 10 trials.

The configurations and resulting validation loss for each trial were:

Trial	Learning Rate	Batch Size	Epochs	Validation Loss
1	3.895×10^{-5}	16	3	0.626
2	3.996×10^{-5}	16	4	0.629
3	3.946×10^{-5}	32	3	0.783
4	2.464×10^{-5}	32	3	0.847
5	4.504×10^{-5}	16	3	0.524
6	2.609×10^{-5}	16	2	0.876
7	3.742×10^{-5}	32	2	0.890
8	2.007×10^{-5}	16	2	0.844
9	3.494×10^{-5}	32	3	0.736
10	3.710×10^{-5}	16	3	0.705

Table 4.1: Hyper-parameter configurations with associated validation loss

4.2.5 Model Evaluation

The three best configurations discovered during hyper-parameter optimisation were used to fully train 3 models. It was initially discovered that these configurations started to overfit due to an increase in data samples, so to compensate for this training was reduced by one epoch. Whilst optimising the hyper-parameters with the full dataset would give the best results, the time taken to do this (around 15 hours for 10 trials) would have been too great, so this approach is chosen as a compromise.

These models were evaluated using the following performance metrics:

- **Accuracy** - The percentage of predictions that the model correctly makes across all classes.
- **Precision** - The combined percentage of predictions that are correct for each class, weighted by the number of instances in each class. E.g. if 30 samples are labelled positive, and the model correctly predicts them all, but also incorrectly predicts 10 more samples as positive the precision for that class will be $30/40 = 75\%$.
- **Recall** - The combined percentage of true instances that were correctly identified by the model, also weighted by the number of instances in each class. For the same example where all 30 positive samples were correctly predicted, the recall would be 100% for the positive class.
- **F1 Score** - The harmonic mean of precision and recall, calculated as:

$$F_1 = 2 \times \frac{\text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$$

Using the F1 score as a performance metric should reward models that are both precise and able to recall relevant rows of data effectively, ensuring a robust model. F1 score is particularly relevant for sentiment analysis with multiple labels, as it ensures a model is not just performing well on the majority class, and can accurately predict less frequent classes of data.

The three models were evaluated on approximately 1000 samples taken randomly from the unseen data, ensuring no prior knowledge from training could influence the evaluation, and providing a fair assessment of the models' performance. The unseen data was processed in the exact same way as the training data to ensure consistency.

The configurations evaluated were the best 3 from hyper-parameter optimisation (see 4.2.4): Trial 5 (Configuration 1), Trial 1 (Configuration 2), and Trial 2 (Configuration 3). The results are as follows:

Class	Precision	Recall	F1-Score	Samples
Positive	0.95	0.75	0.84	483
Negative	0.86	0.62	0.72	190
Neutral	0.71	0.99	0.83	402
Accuracy		0.82		1075
Weighted Avg	0.85	0.82	0.81	1075

Table 4.2: Classification report for Model Configuration 1.

Class	Precision	Recall	F1-Score	Samples
Positive	0.96	0.44	0.61	483
Negative	0.87	0.32	0.46	190
Neutral	0.51	0.99	0.67	402
Accuracy		0.63		1075
Weighted Avg	0.77	0.63	0.61	1075

Table 4.3: Classification report for Model Configuration 2.

Class	Precision	Recall	F1-Score	Samples
Positive	0.94	0.55	0.69	483
Negative	0.81	0.59	0.69	190
Neutral	0.61	0.99	0.76	402
Accuracy		0.72		1075
Weighted Avg	0.79	0.72	0.72	1075

Table 4.4: Classification report for Model Configuration 3.

The models all struggled with the negative class which is likely because the dataset contains far fewer of these samples than neutral or positive samples. They appear to mislabel them as neutral data due to the low precision of the neutral class for all configurations. The first configuration is far better than the other two with a much higher F1 score, and as such was the chosen model. The model weights were saved using the transformers library, for later use.

Chapter 5

Expected Points Model

Chapter 6

Team Selection Algorithm

Chapter 7

Results

Chapter 8

Discussion

Chapter 9

Conclusion

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