

Q1a: The matrix  $A = \begin{pmatrix} 0 & 0 & a \\ 0 & b & 0 \\ a & 0 & 0 \end{pmatrix}$  will have eigenvalues of  $\lambda_1 = -a$  corresponding to  $v_1 = \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix}$ ,  $\lambda_2 = b$  corresponding to  $v_2 = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$  and  $\lambda_3 = a$  corresponding to  $v_3 = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ . Therefore this will have a general solution of  $x(t) = \alpha_1 e^{-at} \cdot v_1 + \alpha_2 e^{bt} \cdot v_2 + \alpha_3 e^{at} \cdot v_3$  for some constants  $\alpha_1, \alpha_2, \alpha_3 \in \mathbb{R}$  which will depend on the initial conditions of this system.