

Q9: Any sequence x_n in $M + N$ can be written as $u_n + v_n$ for $u_n \in M, v_n \in N$. By continuity of the inner product, we have that

$$\langle x_n, x_n \rangle = \langle v_n, v_n \rangle + 2\langle u_n, v_n \rangle + \langle u_n, u_n \rangle = |v_n|^2 + |u_n|^2 \rightarrow |u|^2 + |v|^2.$$

Therefore $x_n \rightarrow x = u + v$.