Assignment 8 MAT 458

Q2: Let  $\{x_n\}$  be an enumeration of the rationals. Define  $E_n = \bigcup_{k=1}^{\infty} \left(x_k - \frac{1}{2^{k-1}n}, x_k + \frac{1}{2^{k-1}n}\right)$ . We have that  $m(E_n) = \frac{1}{n}$ . Set  $E = \bigcap E_n$ . It follows from measure continuity that m(E) = 0. Each  $E_n$  is dense in  $\mathbb{R}$  since  $\mathbb{Q} \subset E_n$ . Thus  $E^c$  is nowhere dense.