

Q6: This is false. Consider $\sigma = (23)(45)$ and $\sigma' = (13)(45)$. They are conjugate by $g = (123)(45)$. In order to conjugate from σ to σ' we must conjugate with a permutation with odd sign to relabel 1 as 2.