Assignment 1 MAT 458

Q9: If for all x we had that  $\sup_k \{ \|T_{jk}x\| : j \in \mathbb{N} \} < \infty$  for all x, uniform boundedness would imply that  $\sup_{j,k} \{ \|T_{jk}\| \} < \infty$ . This contradicts the assumption, since we assume that for each k there is x so that  $\sup_k \{ \|T_{jk}x\| : j \in \mathbb{N} \} = \infty$ . Therefore there is an x so that  $\sup_k \{ \|T_{jk}x\| : j \in \mathbb{N} \}$  for all k.