

Q3a: By Stoke's Theorem, we know that

$$\int_{S_r^2} \omega = \int_{D_r^3} d\omega$$

Hence we compute that

$$\int_{D_d^3 \setminus \text{int} D_c^3} d\omega = \int_{\partial D_d^3} \omega - \int_{\partial \text{int} D_c^3} \omega = \left(a + \frac{b}{d}\right) - \left(a + \frac{b}{c}\right) = \frac{b}{d} - \frac{b}{c}$$

Q2b: Suppose that  $\omega$  is closed. Then by Stokes' Theorem we see that

$$a + \frac{b}{r} = \int_{S_r^2} \omega = \int_{D_r^3} d\omega = \int_{D_r^3} 0 = 0$$

And we conclude that  $a = b = 0$ .

Q2c: Suppose that  $d\eta = \omega$ . Then by Stokes' Theorem we see that

$$a + \frac{b}{r} = \int_{S_r^2} d\eta = \int_{D_r^3} d^2\eta = \int_{D_r^3} 0 = 0$$

We conclude that  $a = b = 0$ .