

Q4:

Suppose that $\langle x, y \rangle = 0$. It follows that

$$\begin{aligned} & \|x + y\|^2 \\ &= \langle x + y, x + y \rangle \\ &= \langle x, x \rangle + 2\langle x, y \rangle + \langle y, y \rangle \\ &= \langle x, x \rangle + \langle y, y \rangle \\ &= \|x\|^2 + \|y\|^2 \quad \blacksquare \end{aligned}$$