Q2: From the textbook HSD, the solution to this system must be

$$x(t) = A\sin(t) + B\cos(t)$$

From the initial conditions, we have that $B = 0$, and that $A = 0$. This contradicsts that $x(\pi) = 1$. Hence this system has no solutions.