

Q5a: We compute  $d\omega$  as follows:

$$\begin{aligned}
 d\omega &= \sum_{i=1}^n dx_i \wedge \frac{\partial \omega}{\partial x_i} \\
 &= \sum_{i=1}^n dx_i \wedge \frac{\partial}{\partial x_i} \sum_{j=1}^n (-1)^{j-1} \frac{x_j}{|x|^p} dx_1 \wedge \cdots \widehat{dx_j} \cdots \wedge dx_n \\
 &= \sum_{i=1}^n dx_i \wedge \frac{\partial}{\partial x_i} (-1)^{i-1} \frac{x_i}{|x|^p} dx_1 \wedge \cdots \widehat{dx_i} \cdots \wedge dx_n \\
 &= \sum_{i=1}^n dx_i \wedge (-1)^{i-1} \frac{|x|^p - px_i^2 |x|^{p-2}}{|x|^{2p}} dx_1 \wedge \cdots \widehat{dx_i} \cdots \wedge dx_n \\
 &= \frac{1}{|x|^{2p}} \left( \sum_{i=1}^n |x|^p - p|x|^{p-2} \sum_{i=1}^n x_i^2 \right) dx_1 \wedge \cdots \wedge dx_n \\
 &= \frac{1}{|x|^{2p}} (n|x|^p - p|x|^{p-2} \cdot |x|^2) dx_1 \wedge \cdots \wedge dx_n \\
 &= \frac{n|x|^p - p|x|^p}{|x|^{2p}} dx_1 \wedge \cdots \wedge dx_n
 \end{aligned}$$

Q5b: We see by taking  $p = n$ ,  $d\omega = 0$