

Q3: If we let that $\gamma(t) = (\gamma_1(t), \gamma_2(t))$, then we note that since $|\gamma(t)|^2 = 1$, then $\frac{d}{dt}|\gamma(t)|^2 = 0$. For the two vectors in $T_{\gamma(t)} \mathbb{R}^2$, $(\gamma(t), \gamma(t))$ and $(\gamma(t), \gamma'(t))$ we compute their inner product as

$$\begin{aligned}\langle (\gamma(t), \gamma(t)), (\gamma(t), \gamma'(t)) \rangle &= \langle \gamma(t), \gamma'(t) \rangle \\ &= \gamma_1(t) \cdot \gamma'_1(t) + \gamma_2(t) \cdot \gamma'_2(t) \\ &= \frac{1}{2} \frac{d}{dt} |\gamma(t)|^2 \\ &= 0\end{aligned}$$

Therefore, these tangent vectors are perpendicular.