

**Exercise 1** Find

$$\lim_{x \rightarrow 3} f(x) = \boxed{9}.$$

given, on the interval  $[0, 5]$ , that  $6x - 9 \leq f(x) \leq x^2$ .

**Hint:** Use the Squeeze Theorem on the two bounds for  $f(x)$ . Observe that  $\lim_{x \rightarrow 3} (6x - 9) =$

$$6 \cdot \lim_{x \rightarrow 3} (x) - \lim_{x \rightarrow 3} (9) = 9 \text{ and } \lim_{x \rightarrow 3} (x^2) = \left( \lim_{x \rightarrow 3} (x) \right)^2 = 9.$$

**Hint:** Since we are given that  $6x - 9 \leq f(x) \leq x^2$  on  $[0, 5]$ , and we have seen that  $\lim_{x \rightarrow 3} (6x - 9) = \lim_{x \rightarrow 3} (x^2) = 9$ , it follows by the Squeeze Theorem that  $\lim_{x \rightarrow 3} f(x) = 9$ .

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