

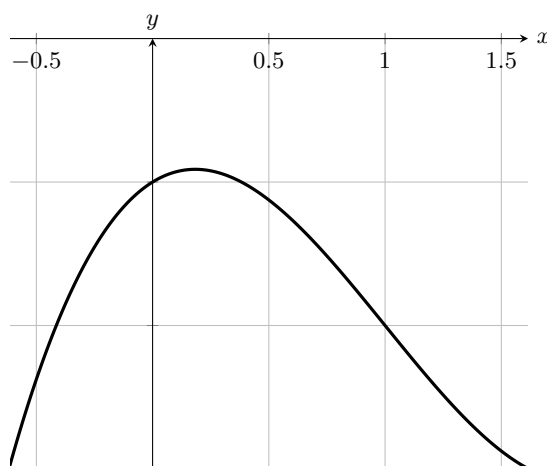
Exercise 1 Find

$$\lim_{x \rightarrow 0} x^3 - 3x^2 + x - 5 = \boxed{-5}$$

Hint: This function is continuous everywhere. Therefore, left-hand and right-hand limits exist at every point and are equal. Use this to your advantage by applying limit laws. Namely, the limit of a sum is the sum of the limits. Hence,

$$\lim_{x \rightarrow 0} (x^3 - 3x^2 + x - 5) = \lim_{x \rightarrow 0} (x^3) + \lim_{x \rightarrow 0} (-3x^2) + \lim_{x \rightarrow 0} (x) + \lim_{x \rightarrow 0} (-5).$$

Hint: Take a look at the graph of the function



Additional limit laws imply that

$$\lim_{x \rightarrow 0} (x^3 - 3x^2 + x - 5) = \left(\lim_{x \rightarrow 0} (x) \right)^3 - 3 \cdot \lim_{x \rightarrow 0} (x^2) + \lim_{x \rightarrow 0} (x) - \lim_{x \rightarrow 0} (5).$$

Hint: Evaluating $\lim_{x \rightarrow 0} (x^3 - 3x^2 + x - 5) = \left(\lim_{x \rightarrow 0} (x) \right)^3 - 3 \cdot \lim_{x \rightarrow 0} (x^2) + \lim_{x \rightarrow 0} (x) - \lim_{x \rightarrow 0} (5)$ we see the answer is 5, since, as we know, $\lim_{x \rightarrow 0} (x) = 0$.