$$\lim_{x \to 0^+} \left(\frac{1}{1 - e^{\sqrt{x}}} \right) = \boxed{-\infty}$$