

Exercise 1 Find

$$\lim_{x \rightarrow 1} f(x) = \boxed{1}.$$

given that $3x - 2 \leq f(x) \leq x^3$.

Hint: Use the Squeeze Theorem on the two bounds for $f(x)$. Observe that $\lim_{x \rightarrow 1} (3x - 2) =$

$$3 \cdot \lim_{x \rightarrow 1} (x) - \lim_{x \rightarrow 1} (2) = 1 \text{ and } \lim_{x \rightarrow 1} (x^3) = \left(\lim_{x \rightarrow 1} (x) \right)^3 = 1.$$

Hint: Since we are given that $3x - 2 \leq f(x) \leq x^3$, and we have seen that $\lim_{x \rightarrow 1} (3x - 2) = \lim_{x \rightarrow 1} (x^3) = 1$, it follows by the Squeeze Theorem that $\lim_{x \rightarrow 1} f(x) = 1$.