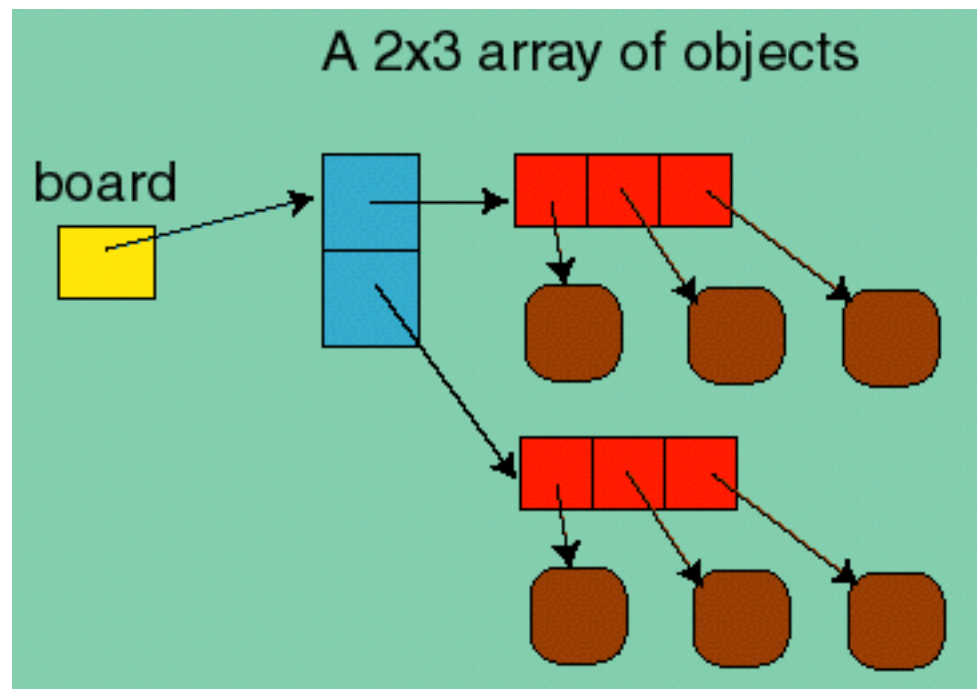


# 15-112

## Fundamentals of Programming

### Week 6 - Lecture 1: “2-dimensional” lists



# “2d lists”

A list can contain any type of object.

```
a = [1, “hello”, False]
```

Can also contain lists.

```
a = [[1, 3, 5], [6], [1, 5]]          # A list of lists
```

`a[0]` is a reference to the first list `[1, 3, 5]`

`a[1]` is a reference to the second list `[6]`

`a[2]` is a reference to the third list `[1, 5]`

`a[0][0]` is a reference to the first element of the first list `[1, 3, 5]`

`a[2][1]` is a reference to the second element of the third list `[1, 5]`

# Example: Print all the elements

```
a = [[1, 3, 5], [6], [1, 5]]
```

```
print(len(a))    3
```

```
a = [ [1, 3, 5],  
      [6],  
      [1, 5]  
    ]
```

Looping through the elements one by one.

```
for i in range(len(a)):  
    for j in range(len(a[i])):  
        print(a[i][j])
```

1  
3  
5  
6  
1  
5

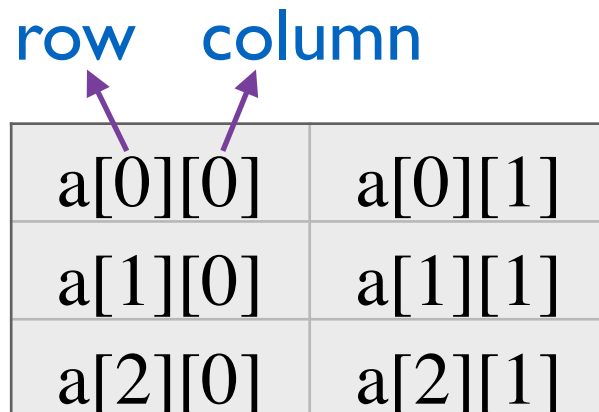
# *rectangular “2d list”*

Most “2d lists” we deal with will have same length sublists.

```
a = [[1, 3], [2, 4], [1, 5]]
```

```
a = [ [1, 3],  
      [2, 4],  
      [1, 5]  
      ]
```

Really like a table (or matrix)



a[0][0]	a[0][1]
a[1][0]	a[1][1]
a[2][0]	a[2][1]

# Example: Pretty printing of 2d lists

## 2d list examples

A chess board: 8 lists of length 8 each (or 8 by 8 table)

Each entry either contains a chess piece or is empty.

An image: a 2d list of points

Each entry contains the color of the point.

A database: e.g. a list of users and various information about the users

	name	age	sex	...
user1				
user2				...
user3				
...		...		

Cool. Seems easy enough. Can we go home?

Unfortunately, no. 

# Tricky thing about 2d lists

1d list: references to **immutable** objects.

Aliases of elements not a problem.

2d list: references to **mutable** objects.

We must be careful about aliases of elements !!



# “Weird” Example I

```
a = [1, 2, 3]
```

```
b = copy.copy(a)
```

```
b[0] = 0
```

```
print(a)           [1, 2, 3]
```

```
print(b)           [0, 2, 3]
```

---

```
a = [[1, 2, 3], [4, 5, 6]]
```

```
b = copy.copy(a)
```

```
b[0][0] = 0
```

```
print(a)           [ [0, 2, 3], [4, 5, 6] ]
```

```
print(b)           [ [0, 2, 3], [4, 5, 6] ]
```

## “Weird” Example 2

```
a = [ [0]*2 ]*3
```

```
print(a)           [ [0, 0], [0, 0], [0, 0] ]
```

```
a[0][0] = 9
```

```
print(a)           [ [9, 0], [9, 0], [9, 0] ]
```

# Understanding Example I

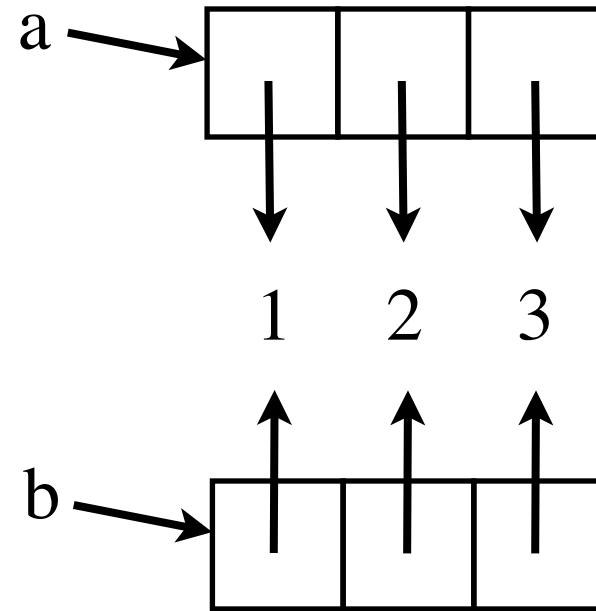
```
a = [1, 2, 3]
```

```
b = copy.copy(a)
```

```
b[0] = 0
```

```
print(a[0])
```

```
print(b[0])
```



Making a copy of the references.

# Understanding Example I

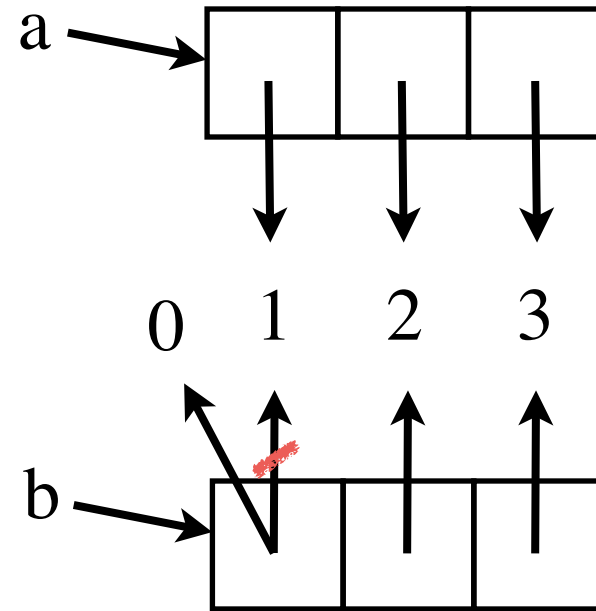
```
a = [1, 2, 3]
```

```
b = copy.copy(a)
```

```
b[0] = 0
```

```
print(a[0])
```

```
print(b[0])
```



Making a copy of the references.

# Understanding Example I

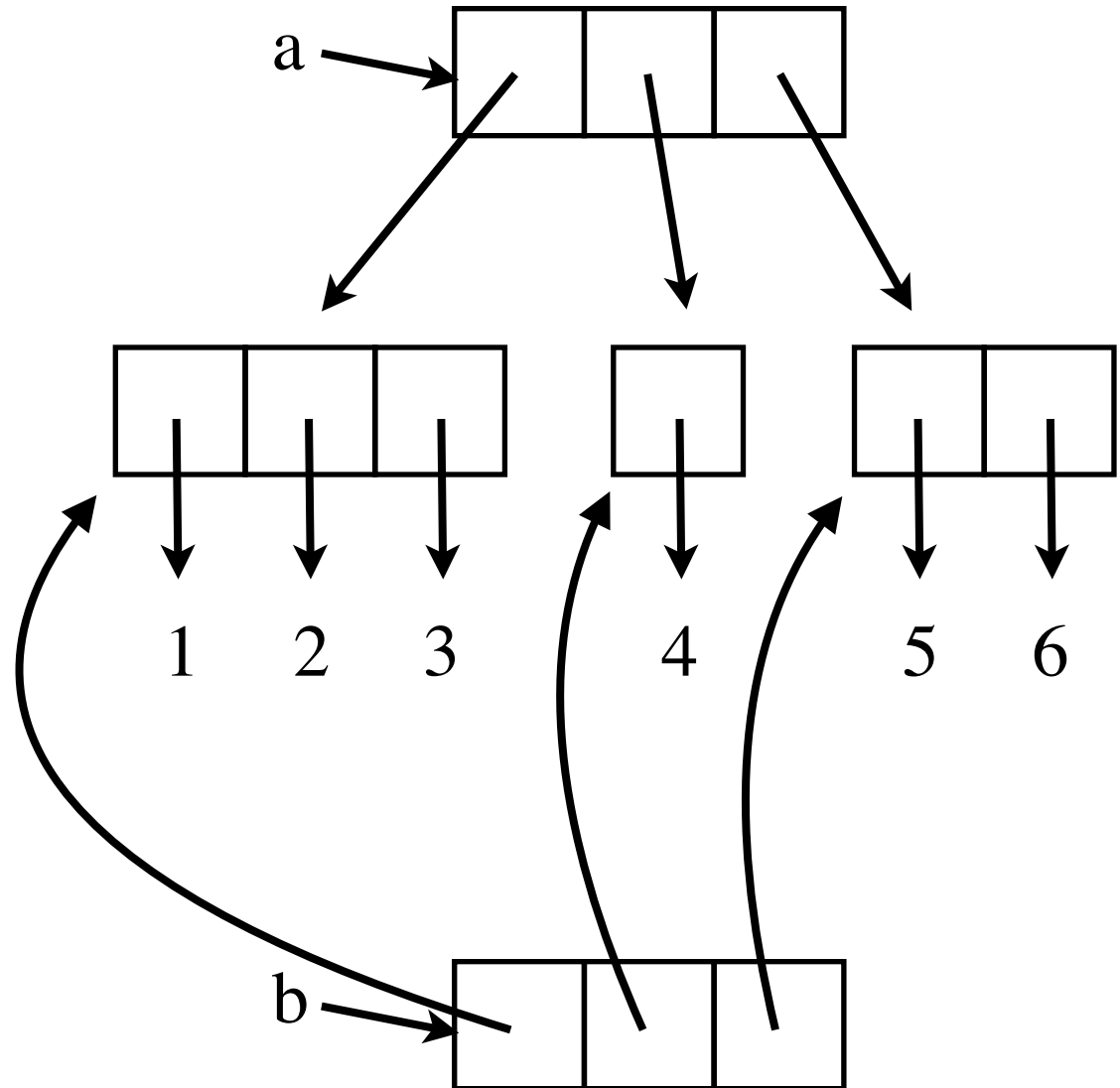
```
a = [[1, 2, 3], [4], [5, 6]]
```

```
b = copy.copy(a)
```

```
b[0][0] = 0
```

```
print(a[0][0])
```

```
print(b[0][0])
```



# Understanding Example I

```
a = [[1, 2, 3], [4], [5, 6]]
```

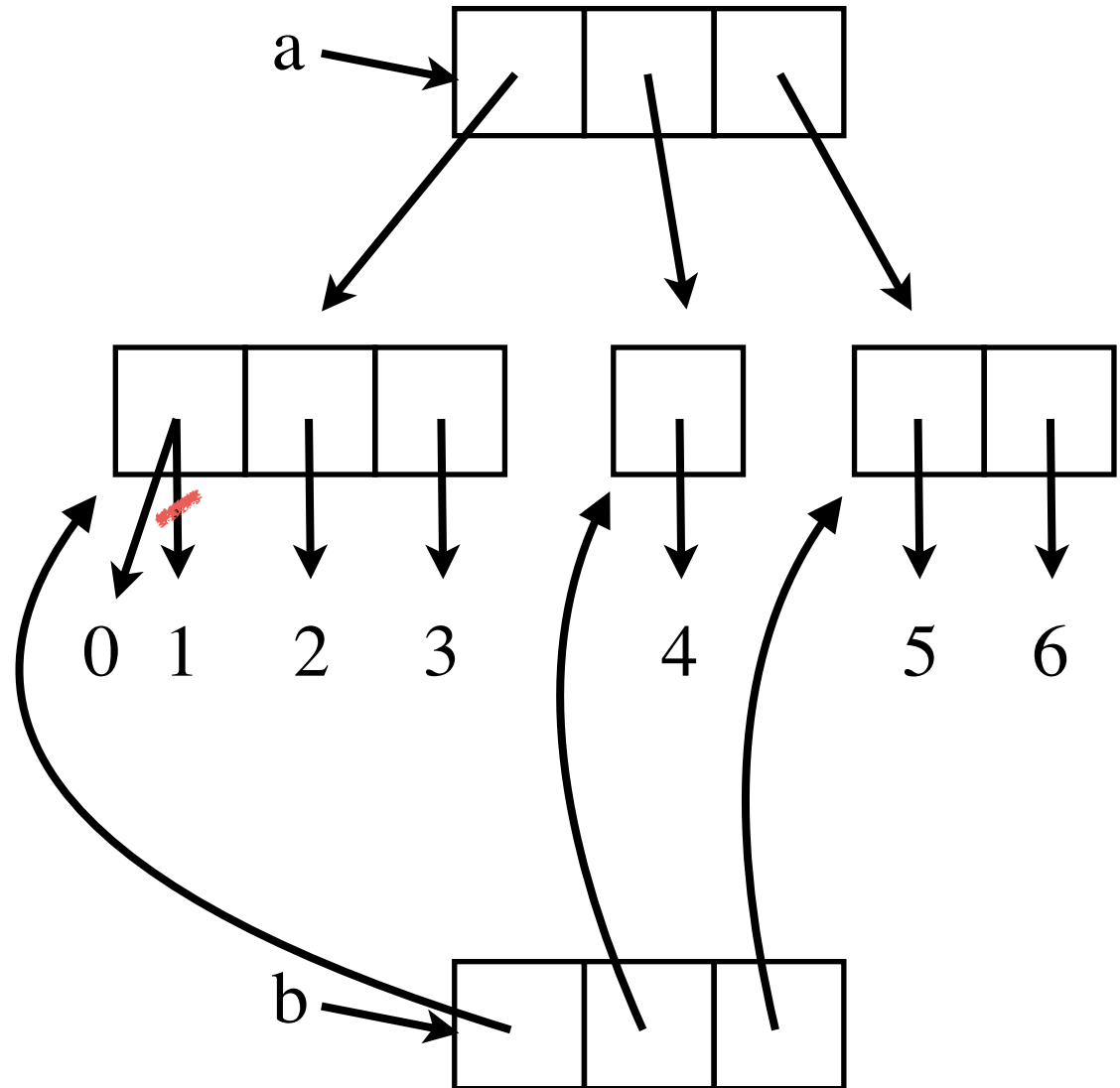
```
b = copy.copy(a)
```

```
b[0][0] = 0
```

```
print(a[0][0])
```

```
print(b[0][0])
```

**Shallow copy**



# Understanding Example I

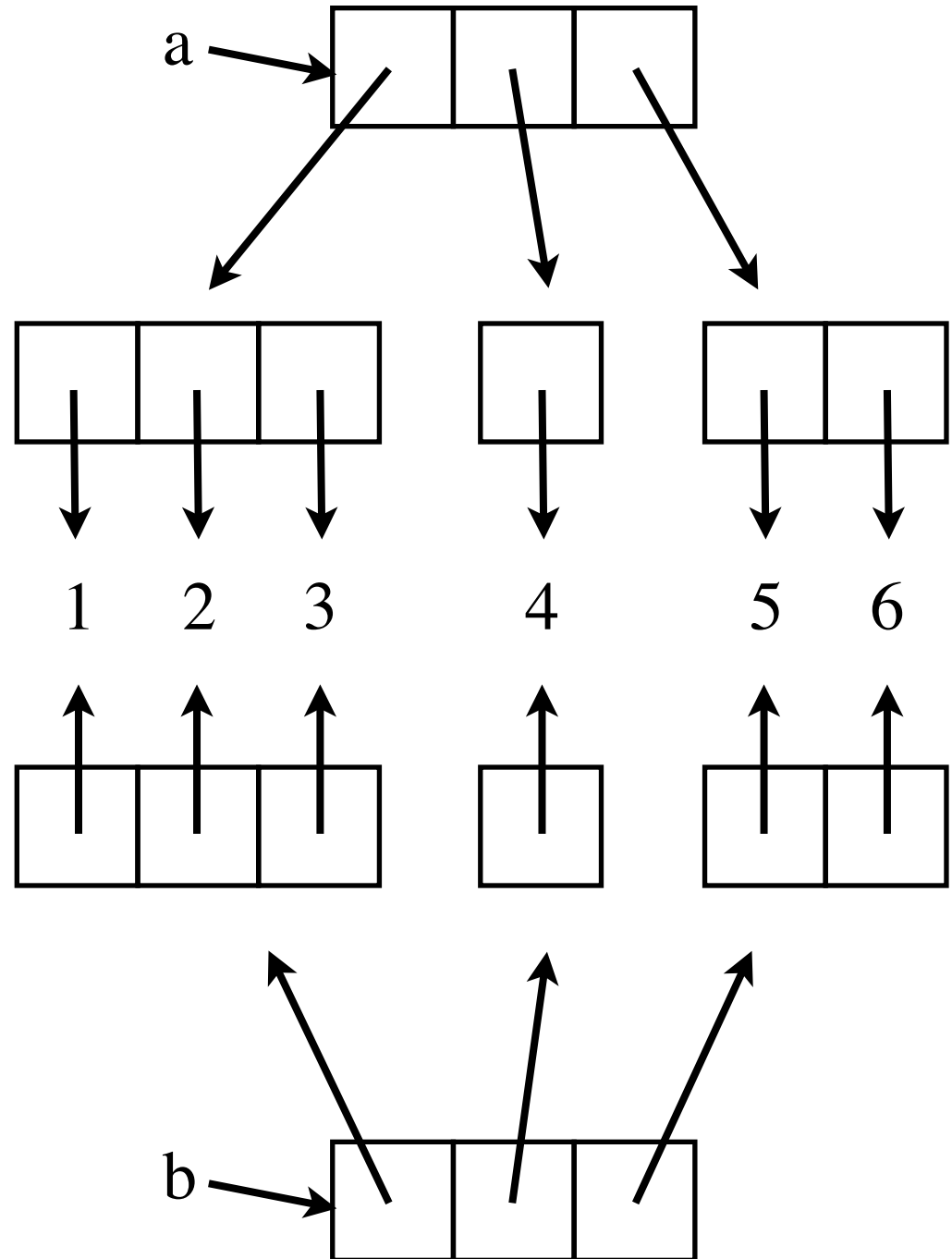
```
a = [[1, 2, 3], [4], [5, 6]]
```

```
b = copy.deepcopy(a)
```

```
b[0][0] = 0
```

```
print(a[0][0])
```

```
print(b[0][0])
```



# Understanding Example I

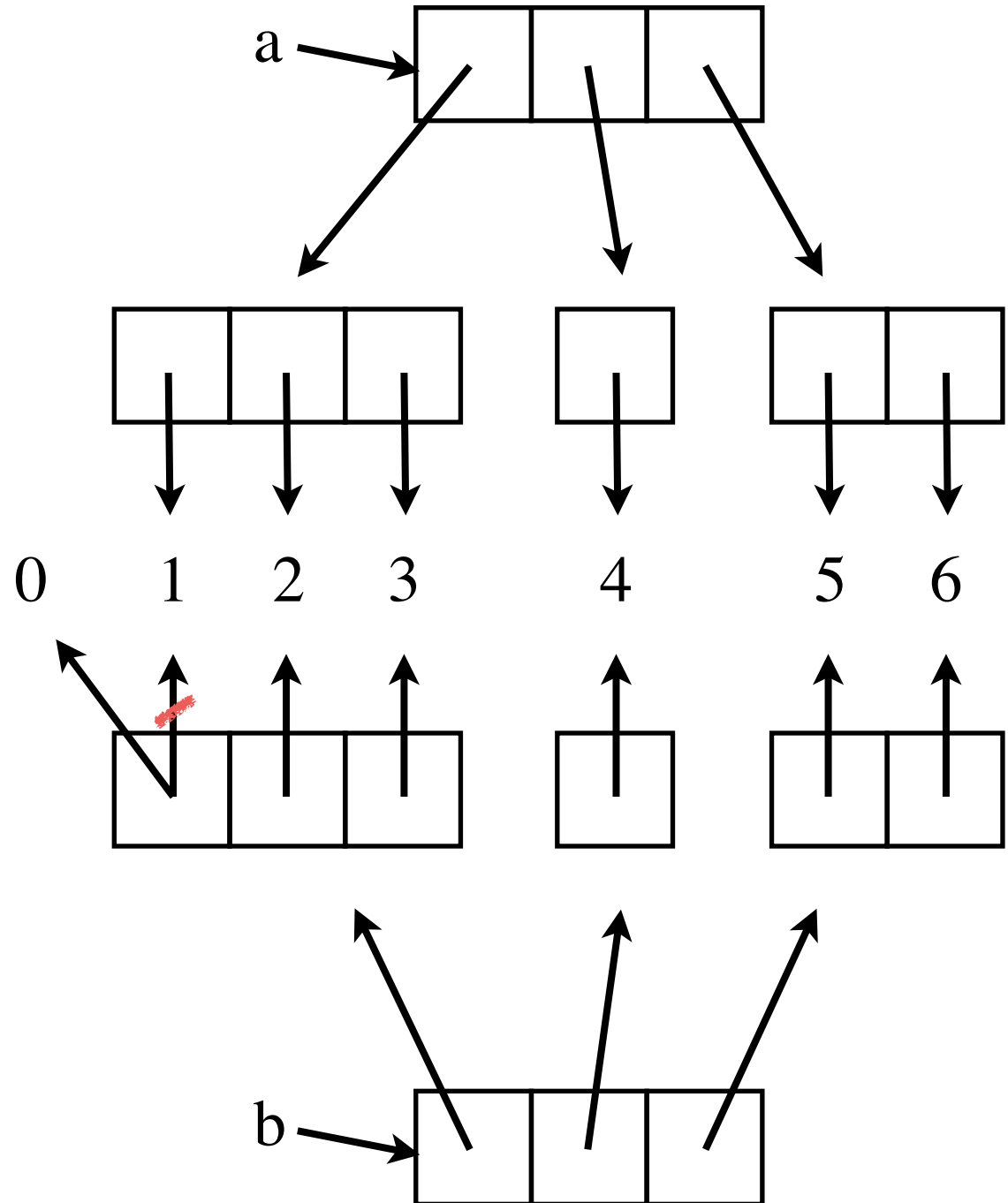
```
a = [[1, 2, 3], [4], [5, 6]]
```

```
b = copy.deepcopy(a)
```

```
b[0][0] = 0
```

```
print(a[0][0])
```

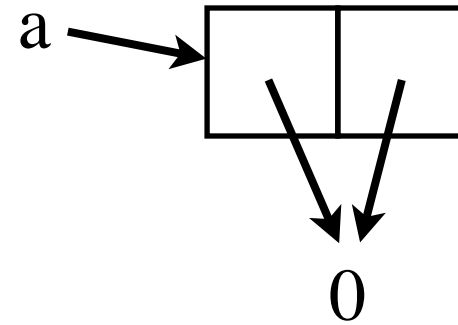
```
print(b[0][0])
```





# Understanding Example 2

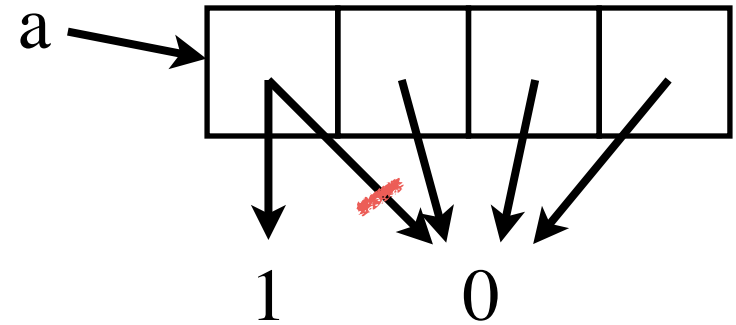
$a = [0]*2$



# Understanding Example 2

$a = [0]^*4$

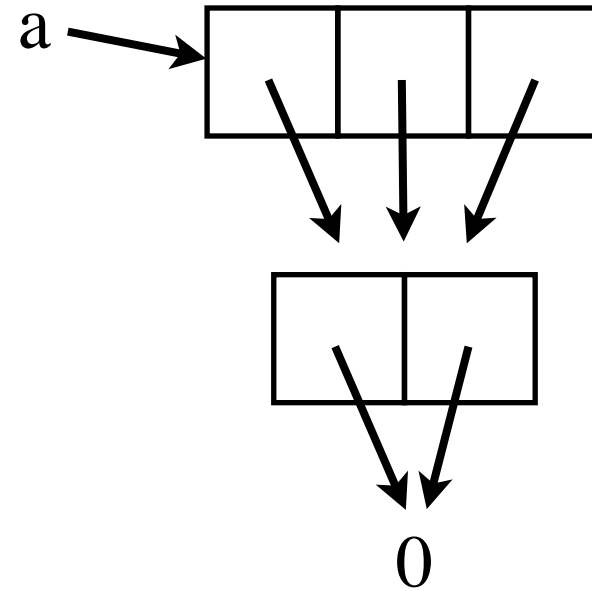
$a[0] = 1$



# Understanding Example 2

# Create a 3 by 2 list

`a = [ [0]*2 ]*3`



# Understanding Example 2

# Create a 3 by 2 list

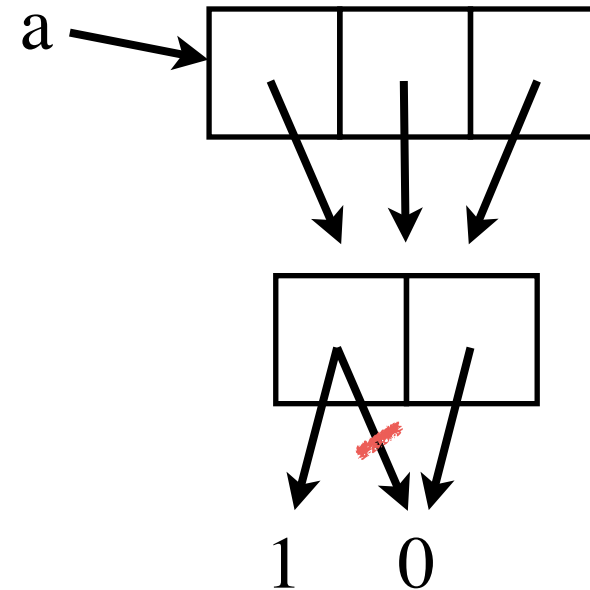
```
a = [ [0]*2 ]*3
```

```
[ [0, 0], [0, 0], [0, 0] ]
```

```
a[0][0] = 1
```

```
print(a)
```

```
[ [1, 0], [1, 0], [1, 0] ]
```



**a[0], a[1], and a[2] are aliases !**

**\* makes a shallow copy !**

# Creating a *rows by cols* 2d list

rows = 2

cols = 3

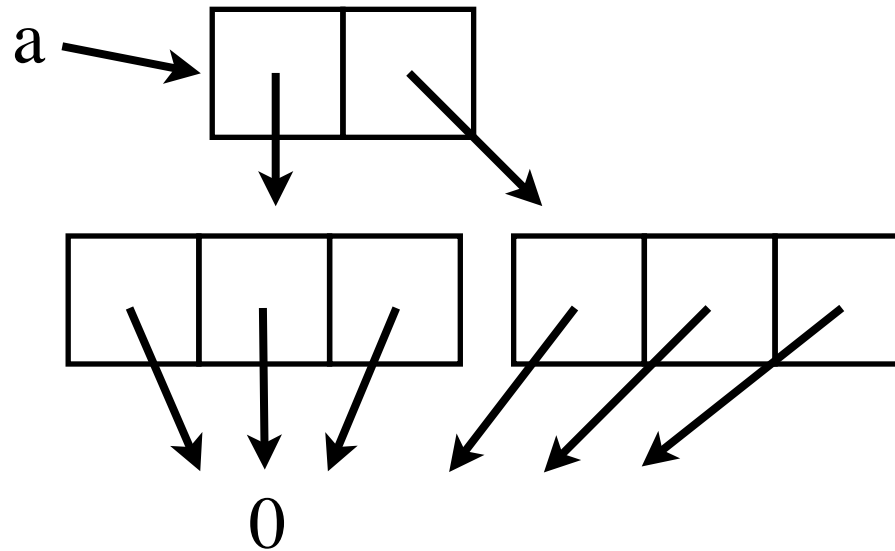
a = [ ]

a += [[0, 0, 0]]

a += [[0, 0, 0]]

**for** row **in** range(rows):

    a += [[0]\*cols]



# Creating a *rows by cols* 2d list

```
rows = 3
```

```
cols = 3
```

```
a = [ ]
```

```
for row in range(rows):
```

```
    a += [[0]*cols]
```

---

**Same thing with list comprehension:**

```
rows = 3
```

```
cols = 3
```

```
a = [[([0]*cols) for row in range(rows)]
```

# Creating a *rows by cols* 2d list

Define a function for this task.

```
def make2dList(rows, cols):  
    a = []  
    for row in range(rows):  
        a += [[0]*cols]  
    return a
```

# One more important thing

# Create a 3 by 2 list

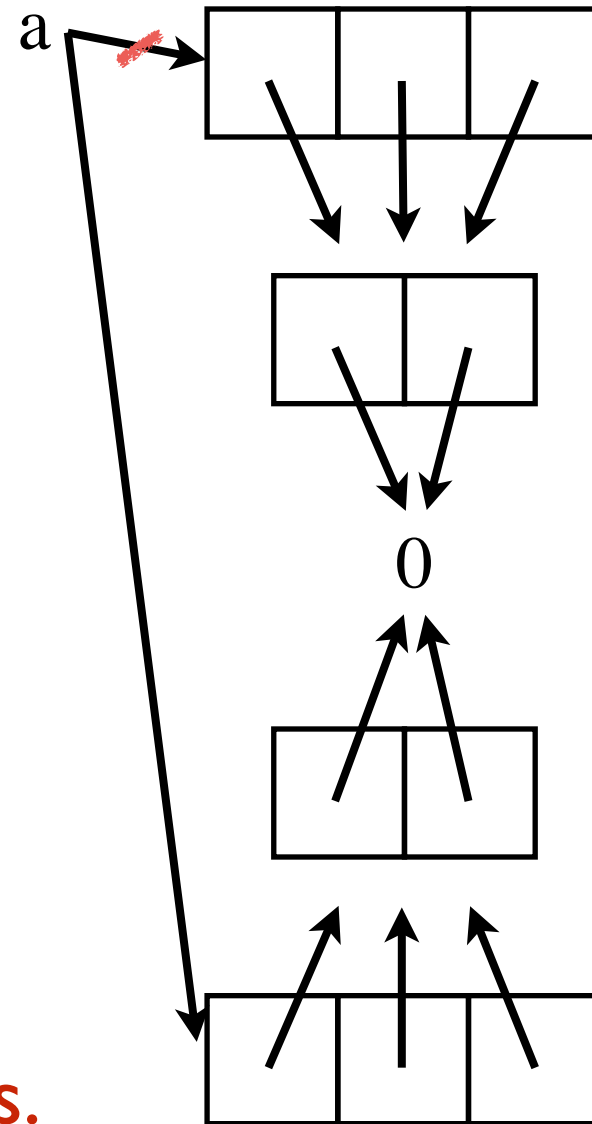
```
a = [ [0]*2 ]*3
```

Trying to break aliasing  
with deepcopy:

```
a = copy.deepcopy(a)
```

deepcopy preserves  
alias structure !!

see myDeepCopy in the notes.





# Rules

Use \* only on the first level (with immutable elements)

- creates aliases

Never use `copy` with 2d lists.

- creates aliases
- ok to use with 1d lists since elements are immutable.

Remember: `deepcopy` does not break alias structure within the list.

# 3d Lists

## 2d list:

```
a = [ [1, 3, 5],  
      [6],  
      [1, 5]  
    ]
```

## Printing elements of 2d lists:

```
for i in range(len(a)):  
    for j in range(len(a[i])):  
        print("a[%d][%d] = %d" % (i, j, a[i][j]))
```

# 3d Lists

```
a1 = [ [ 1, 2 ],  
        [ 3, 4 ] ]
```

```
a2 = [ [ 5, 6, 7 ],  
        [ 8, 9 ] ]
```

```
a3 = [ [ 10 ] ]
```

## 3d list:

```
a = [ a1, a2, a3 ]
```

## 4d list:

```
a = [ a, a ]
```

# 3d Lists

```
a = [ [ [ 1, 2 ],  
        [ 3, 4 ] ],  
       [ [ 5, 6, 7 ],  
         [ 8, 9 ] ],  
       [ [ 10 ] ]  
]
```

## Printing elements of 3d lists:

```
for i in range(len(a)):  
    for j in range(len(a[i])):  
        for k in range(len(a[i][j])):  
            print("a[%d][%d][%d] = %d" % (i, j, k, a[i][j][k]))
```

# Example Problem: Word Search

I	X	D	D	R	I	V	E	R	N	E	Y	N	F	R	E	K	N	A	T	O	I	A	P	Q
M	C	P	K	H	P	R	R	A	Z	J	B	B	U	N	D	E	D	T	A	N	K	S	H	T
G	P	B	A	V	E	S	R	L	I	O	S	A	G	I	Y	V	I	P	C	D	T	E	M	J
C	Q	M	M	R	D	G	B	A	R	T	L	U	O	R	E	K	J	K	G	N	T	X	Y	A
U	R	T	V	W	A	E	F	D	E	X	X	Q	F	W	N	G	E	T	A	C	S	B	N	A
C	U	H	N	E	L	F	L	I	C	D	F	R	E	E	D	O	M	C	O	D	E	Y	V	Q
W	Z	B	M	F	C	Y	F	I	D	M	Q	X	Z	F	Q	K	I	A	X	S	B	A	Z	Z
D	T	F	B	A	J	I	K	I	V	I	E	N	E	S	O	R	E	K	A	S	V	L	T	L
H	M	X	R	Z	E	I	V	S	N	E	R	I	E	T	B	H	F	D	W	W	N	T	U	F
R	Y	V	O	J	H	T	D	R	P	G	R	C	O	U	P	I	P	J	I	L	K	K	A	E
O	D	I	T	A	E	U	S	K	E	L	X	Y	L	K	I	H	Y	I	T	B	V	R	A	N
Y	W	J	I	E	A	K	A	E	B	S	F	V	Y	G	E	N	G	I	N	E	O	I	L	J
D	Z	G	N	I	T	A	E	H	L	A	R	T	N	E	C	I	S	G	A	F	C	G	Q	M
B	P	G	O	G	I	A	E	V	P	A	I	E	H	I	V	N	B	R	P	I	D	A	G	Y
O	G	B	M	O	N	G	L	K	X	X	S	N	M	C	D	S	H	E	O	A	C	E	O	K
A	L	S	O	Z	G	F	R	R	U	N	O	U	T	O	E	O	M	A	L	F	C	A	N	X
G	R	E	D	R	O	I	O	O	Q	H	P	M	Q	D	T	R	F	S	L	T	M	Z	L	U
A	F	O	K	T	I	B	N	I	M	U	E	S	L	E	E	S	Y	E	O	V	S	F	F	F
M	Q	W	V	P	L	D	V	M	L	E	S	E	I	D	S	L	U	P	X	B	X	R	G	V
A	G	S	J	J	U	P	G	L	V	T	A	T	E	O	I	L	J	C	X	J	D	T	Q	L
T	M	J	J	S	P	M	I	J	D	L	V	U	Y	D	J	Y	R	A	K	U	I	X	J	I
E	G	E	R	A	R	F	P	L	E	D	I	X	F	G	R	S	T	T	T	E	U	S	Y	T
X	P	G	Z	Z	E	L	X	T	N	E	N	U	B	K	S	O	A	F	R	W	E	A	C	R
V	H	B	L	M	X	G	E	H	X	V	R	S	Z	G	K	N	M	P	Z	G	O	H	U	E
A	C	C	O	U	N	T	Y	B	O	I	L	E	R	A	M	V	J	K	T	E	K	N	U	S

HEATINGOIL
KEROSENE
AGAMATE
KEROULTRA
TANKER
DELIVERY
RUNOUT
TATEOIL
FILLUP
LITRES
DRIVER
FREEDOM
ACCOUNT
ORDER
CENTRALHEATING
CUSTOMERSERVICE
BOILER
PUMP
GASOIL
DIESEL
ADBLUE
ANTIWAX
LUBRICANTS
PARAFFIN
ENGINEOIL
GREASE
BUNDEDTANK
APOLLO
MONITOR
SALESTEAM

# Example Problem: Word Search

```
def testWordSearch():
```

```
    board = [ [ 'd', 'o', 'g' ],  
               [ 't', 'a', 'c' ],  
               [ 'o', 'a', 't' ],  
               [ 'u', 'r', 'k' ],  
             ]
```

```
    print(wordSearch(board, "dog"))  
    print(wordSearch(board, "cat"))  
    print(wordSearch(board, "tad"))  
    print(wordSearch(board, "cow"))
```

```
# ('dog', (0, 0), 'right')
```

```
# ('cat', (1, 2), 'left')
```

```
# ('tad', (2, 2), 'up-left')
```

```
# None
```

# Example Problem: Word Search

```
def wordSearch(board, word):  
    # ...
```

**Algorithm:** wordSearch(board, word)

- go through each **cell** of the board one by one:
  - check if word appears starting at that **cell**

# Example Problem: Word Search

```
def wordSearch(board, word):  
    # ...
```

**Algorithm:** wordSearch(board, word)

- go through each **cell** of the board one by one:
  - check if word appears starting at that **cell**

needs to be broken down further



# Example Problem: Word Search

```
def wordSearchFromCell(board, word, startRow, startCol):  
    # ...
```

**Algorithm:** wordSearchFromCell(board, word, startRow, startCol)

- go through each **direction** one by one:
  - check if word appears in that **direction** starting at the given cell

# Example Problem: Word Search

```
def wordSearchFromCell(board, word, startRow, startCol):  
    # ...
```

**Algorithm:** wordSearchFromCell(board, word, startRow, startCol)

- go through each **direction** one by one:
  - check if word appears in that **direction** starting at the given cell

needs to be broken down further

it is important how you represent **direction**.

let's see an elegant way of doing it...