



Heuristic Analysis Report

For an Adversarial Game Playing Agent for Isolation

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1. Synopsis

The project aims at developing an adversarial search agent to play the game “Isolation”. This project report focusses on the heuristic to be used in A* Search for minimax and alpha-beta pruning.

Isolation is a deterministic, two player game of perfect information in which the players alternate turns moving a single piece from one cell to another on a board. Whenever either a player occupies a cell, that cell becomes blocked for the remainder of the game. The first player with no remaining legal moves loses, and the opponent is declared the winner.

This project uses a version of Isolation where each agent is restricted to L-shaped movements (like a knight in chess) on a rectangular grid (like a chess/checkerboard). The agent can move to any open cell on the board that is 2-rows and 1-column or 2-columns and 1-row away from their current position on the board. Movements are blocked at the edges of the board (the board does not wrap around), however, the player can “jump” blocked or occupied spaces (just like a knight in chess).

Additionally, agents will have a fixed time limit each turn to search for the best move and respond. If the time limit expires during a player's turn, that player forfeits the match, and the opponent wins. These rules are implemented in the isolation. Board class provided in the repository.

2. Custom heuristic

2.1 Default Heuristic

The heuristic is based on the logic that the difference between the player's moves and opponent's moves. It can be mathematically expressed as:

$$\text{len}(\text{my available moves}) - \text{len}(\text{available opponent moves})$$

2.2 Heuristic 1: Minimizing Opponent's Moves

The heuristic is based on the logic that opponent's moves should be minimized. It can be mathematically expressed as:

$$\text{len}(\text{my available moves}) - \alpha \text{len}(\text{available opponent moves}), \text{ where } \alpha \in (1, \infty)$$

The value of α was empirically chosen as 1.5

2.3 Heuristic 2: Maximizing Player's Moves

The heuristic is based on the logic that player's moves should be maximized. It can be mathematically expressed as:

$$\alpha \text{len}(\text{my available moves}) - \text{len}(\text{available opponent moves}), \text{ where } \alpha \in (1, \infty)$$

The value of α was empirically chosen as 1.5

2.4 Heuristic 3: Maximizing Ratio of Player to Opponent Moves

The heuristic is based on the logic that player should have more moves in comparison to opponent. It can be mathematically expressed as:

$$\frac{\text{len}(\text{my available moves})}{\text{len}(\text{available opponent moves})}$$

2.5 Heuristic 4: Minimizing Ratio of Opponent to Player Moves

The heuristic is based on the logic that opponent should have less moves in comparison to player. It can be mathematically expressed as:

$$-\frac{\text{len}(\text{available opponent moves})}{\text{len}(\text{my available moves})}$$

2.6 Heuristic 5: Combining Heuristic 3 and 4

Can be mathematically expressed as:

$$\frac{\text{len}(\text{my available moves})}{\text{len}(\text{available opponent moves})} - \frac{\text{len}(\text{available opponent moves})}{\text{len}(\text{my available moves})}$$

Maximizing above equation is equivalent to maximizing:

$$[\text{len}(\text{my available moves})]^2 - [\text{len}(\text{available opponent moves})]^2$$

2.7 Heuristic 6: Weighted combination of Heuristic 3 and 4

Can be mathematically expressed as:

$$\frac{\text{len}(\text{my available moves})}{\text{len}(\text{available opponent moves})} - \alpha \frac{\text{len}(\text{available opponent moves})}{\text{len}(\text{my available moves})}, \text{ where } \alpha \in (1, \infty)$$

Maximizing above equation is equivalent to maximizing:

$$[\text{len}(\text{my available moves})]^2 - \beta [\text{len}(\text{available opponent moves})]^2, \text{ where } \beta \in (1, \infty)$$

2.8 Heuristic 7: Weighted combination of Heuristic 3 and 4

Can be mathematically expressed as:

$$\alpha \frac{\text{len}(\text{my available moves})}{\text{len}(\text{available opponent moves})} - \frac{\text{len}(\text{available opponent moves})}{\text{len}(\text{my available moves})}, \text{ where } \alpha \in (1, \infty)$$

Maximizing above equation is equivalent to maximizing:

$$\beta [\text{len}(\text{my available moves})]^2 - [\text{len}(\text{available opponent moves})]^2, \text{ where } \beta \in (1, \infty)$$

2.9 Custom Heuristic

The heuristic is based on the logic that for each player and opponent's moves are considered. First, we will iterate for each move for player and make it move and increment the initial value of the player's moves. The action is then repeated for the opponent. At the end, the logic used can be mathematically expressed as:

$$\text{len}(\text{my total available moves}) - \alpha \text{len}(\text{total available opponent moves}), \text{ where } \alpha \in (1, \infty)$$

The value of α was empirically chosen as 3.

3. Evaluating Heuristic

The tournament.py script is used to evaluate the effectiveness of heuristic. The script measures relative performance of player in a round-robin tournament against several other pre-defined agents.

The performance of time-limited iterative deepening search is hardware dependent (faster hardware is expected to search deeper than slower hardware in the same amount of time). The script controls for these effects by also measuring the baseline performance of an agent called "ID_Improved" that uses Iterative Deepening and the improved_score heuristic from sample_players.py.

The tournament opponents are listed below:

- Random: An agent that randomly chooses a move each turn.
- MM_Null: CustomPlayer agent using fixed-depth minimax search and the null_score heuristic
- MM_Open: CustomPlayer agent using fixed-depth minimax search and the open_move_score heuristic
- MM_Improved: CustomPlayer agent using fixed-depth minimax search and the improved_score heuristic
- AB_Null: CustomPlayer agent using fixed-depth alpha-beta search and the null_score heuristic
- AB_Open: CustomPlayer agent using fixed-depth alpha-beta search and the open_move_score heuristic
- AB_Improved: CustomPlayer agent using fixed-depth alpha-beta search and the improved_score heuristic

- ID_Improved: CustomPlayer agent using iterative alpha-beta search and the improved_score heuristic
- Student1: CustomPlayer agent using iterative alpha-beta search and the heuristic 1
- Student2: CustomPlayer agent using iterative alpha-beta search and the heuristic 2
- Student3: CustomPlayer agent using iterative alpha-beta search and the heuristic 3
- Student4: CustomPlayer agent using iterative alpha-beta search and the heuristic 4
- Student5: CustomPlayer agent using iterative alpha-beta search and the heuristic 5
- Student6: CustomPlayer agent using iterative alpha-beta search and the heuristic 6
- Student7: CustomPlayer agent using iterative alpha-beta search and the heuristic 7
- 17080476: CustomPlayer agent using iterative alpha-beta search and the Custom Heuristic

Since, running only a few matches gave different results, the number of matches is set to 10, with all group members agreed to it because faster execution time. Timeout value is 150 which is the default value.

4. Results

Results are compared between the baseline default (ID_Improved), 7 students and 3 of my group members. The results as follow:

Agent	Performance	Rank	Rank (Group members)
ID_Improved	60.36%	9	
Student1	65.71%	4	
Student2	68.57%	1	
Student3	62.86%	8	
Student4	64.64%	5	
Student5	63.57%	7	
Student6	66.07%	3	
Student7	64.29%	6	
17080476	67.86%	2	3
Alif	68.21%		2
Amin	66.79%		4
Fedellic	79.64%		1

The custom heuristic performs better than ID_Improved by a reasonable margin which can be seen in the table. Heuristic 5

5. Appendices

This script evaluates the performance of the custom heuristic function by comparing the strength of an agent using iterative deepening (ID) search with alpha-beta pruning against the strength rating of agents using other heuristic functions. The `ID_Improved` agent provides a baseline by measuring the performance of a basic agent using Iterative Deepening and the "improved" heuristic (from lecture) on your hardware. The `Student` agent then measures the performance of Iterative Deepening and the custom heuristic against the same opponents.

```
*****  
Evaluating: ID_Improved  
*****
```

Playing Matches:

Match 1:	ID_Improved	vs	Random	Result: 35 to 5
Match 2:	ID_Improved	vs	MM_Null	Result: 26 to 14
Match 3:	ID_Improved	vs	MM_Open	Result: 23 to 17
Match 4:	ID_Improved	vs	MM_Improved	Result: 16 to 24
Match 5:	ID_Improved	vs	AB_Null	Result: 23 to 17
Match 6:	ID_Improved	vs	AB_Open	Result: 25 to 15
Match 7:	ID_Improved	vs	AB_Improved	Result: 21 to 19

Results:

ID_Improved 60.36%

```
*****  
Evaluating: Student1  
*****
```

Playing Matches:

Match 1:	Student1	vs	Random	Result: 35 to 5
Match 2:	Student1	vs	MM_Null	Result: 24 to 16
Match 3:	Student1	vs	MM_Open	Result: 22 to 18
Match 4:	Student1	vs	MM_Improved	Result: 25 to 15
Match 5:	Student1	vs	AB_Null	Result: 29 to 11
Match 6:	Student1	vs	AB_Open	Result: 26 to 14
Match 7:	Student1	vs	AB_Improved	Result: 23 to 17

Results:

Student1 65.71%

Evaluating: Student2

Playing Matches:

Match 1:	Student2	vs	Random	Result: 30 to 10
Match 2:	Student2	vs	MM_Null	Result: 31 to 9
Match 3:	Student2	vs	MM_Open	Result: 28 to 12
Match 4:	Student2	vs	MM_Improved	Result: 21 to 19
Match 5:	Student2	vs	AB_Null	Result: 30 to 10
Match 6:	Student2	vs	AB_Open	Result: 26 to 14
Match 7:	Student2	vs	AB_Improved	Result: 26 to 14

Results:

Student2 68.57%

Evaluating: Student3

Playing Matches:

Match 1:	Student3	vs	Random	Result: 37 to 3
Match 2:	Student3	vs	MM_Null	Result: 30 to 10
Match 3:	Student3	vs	MM_Open	Result: 20 to 20
Match 4:	Student3	vs	MM_Improved	Result: 18 to 22
Match 5:	Student3	vs	AB_Null	Result: 24 to 16
Match 6:	Student3	vs	AB_Open	Result: 24 to 16
Match 7:	Student3	vs	AB_Improved	Result: 23 to 17

Results:

Student3 62.86%

Evaluating: Student4

Playing Matches:

Match 1:	Student4	vs	Random	Result: 34 to 6
Match 2:	Student4	vs	MM_Null	Result: 30 to 10
Match 3:	Student4	vs	MM_Open	Result: 21 to 19
Match 4:	Student4	vs	MM_Improved	Result: 21 to 19
Match 5:	Student4	vs	AB_Null	Result: 28 to 12
Match 6:	Student4	vs	AB_Open	Result: 25 to 15
Match 7:	Student4	vs	AB_Improved	Result: 22 to 18

Results:

Student4 64.64%

```
*****
Evaluating: Student5
*****
```

Playing Matches:

Match 1:	Student5	vs	Random	Result: 33 to 7
Match 2:	Student5	vs	MM_Null	Result: 28 to 12
Match 3:	Student5	vs	MM_Open	Result: 23 to 17
Match 4:	Student5	vs	MM_Improved	Result: 20 to 20
Match 5:	Student5	vs	AB_Null	Result: 26 to 14
Match 6:	Student5	vs	AB_Open	Result: 21 to 19
Match 7:	Student5	vs	AB_Improved	Result: 27 to 13

Results:

Student5 63.57%

```
*****
Evaluating: Student6
*****
```

Playing Matches:

Match 1:	Student6	vs	Random	Result: 33 to 7
Match 2:	Student6	vs	MM_Null	Result: 28 to 12
Match 3:	Student6	vs	MM_Open	Result: 27 to 13
Match 4:	Student6	vs	MM_Improved	Result: 21 to 19
Match 5:	Student6	vs	AB_Null	Result: 29 to 11
Match 6:	Student6	vs	AB_Open	Result: 23 to 17
Match 7:	Student6	vs	AB_Improved	Result: 24 to 16

Results:

Student6 66.07%

```
*****
Evaluating: Student7
*****
```

Playing Matches:

Match 1:	Student7	vs	Random	Result: 38 to 2
Match 2:	Student7	vs	MM_Null	Result: 29 to 11
Match 3:	Student7	vs	MM_Open	Result: 17 to 23
Match 4:	Student7	vs	MM_Improved	Result: 18 to 22
Match 5:	Student7	vs	AB_Null	Result: 27 to 13
Match 6:	Student7	vs	AB_Open	Result: 28 to 12
Match 7:	Student7	vs	AB_Improved	Result: 23 to 17

Results:

Student7 64.29%

```
*****
Evaluating: 17080476
*****
```

Playing Matches:

Match 1:	17080476	vs	Random	Result: 37 to 3
Match 2:	17080476	vs	MM_Null	Result: 31 to 9
Match 3:	17080476	vs	MM_Open	Result: 23 to 17
Match 4:	17080476	vs	MM_Improved	Result: 23 to 17
Match 5:	17080476	vs	AB_Null	Result: 32 to 8
Match 6:	17080476	vs	AB_Open	Result: 22 to 18
Match 7:	17080476	vs	AB_Improved	Result: 25 to 15

Results:

17080476 68.93%

```
*****
Evaluating: 17080476
*****
```

Playing Matches:

Match 1:	17080476	vs	Random	Result: 36 to 4
Match 2:	17080476	vs	MM_Null	Result: 33 to 7
Match 3:	17080476	vs	MM_Open	Result: 22 to 18
Match 4:	17080476	vs	MM_Improved	Result: 18 to 22
Match 5:	17080476	vs	AB_Null	Result: 29 to 11
Match 6:	17080476	vs	AB_Open	Result: 27 to 13
Match 7:	17080476	vs	AB_Improved	Result: 25 to 15

Results:

17080476 67.86%