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語法

1.1 c++

1 // c++ code

2 #include <bits/stdc++.h>

```
3 lower_bound(a, a + n, k);
                              //最左邊 ≥ k 的位置
4 upper_bound(a, a + n, k);
                              //最左邊 > k 的位置
5 upper_bound(a, a + n, k) - 1; //最右邊 ≤ k 的位置
6 lower_bound(a, a + n, k) - 1; //最右邊 < k 的位置
7 [lower_bound, upper_bound) //等於 k 的範圍
8 equal_range(a, a+n, k);
10 // 從小到大
11 priority_queue<int, vector<int>, greater<int>>pq
12
13 insert(it,x)//向vector的任意迭代器it處插入一個元素x
14 erase(it)//刪除迭代器爲it處的元素, erase(first, last)
15 //刪除一個區間[first,last)內的所有元素,時間複雜度均爲O(N)
16
17 set
18 \mid insert(x) // 將x插入set中 O(log(n))
19 count(x) //回傳x是否存在於 set中() 0(log(n))
20 erase(x) //刪除在set中的x O(log(n))
21 clear() //刪除set中所有元素 O(n)
22 empty() //回傳是否為空 0(1)
23 size() //回傳共有幾個元素 0(1)
24
25 map
26 insert(x) //將 x 這個 pair 插入 map 中 0(log(n))
27 count(x) //回傳x這個key是否在map中 0(log(n))
28 erase(x) //刪除在map中key為x的 O(log(n))
29
30
31 #include <bits/stdc++.h>
32 using namespace std;
33
34 int main(){
35
    set<int>s;
    for(int i = 0; i < 10; i++){
36
37
      s.insert(i);
38
39
    cout << "lower bound: " << *s.lower_bound(5) <<</pre>
        '\n'
            : // 5
    cout << "upper bound: " << *s.upper_bound(5) <<</pre>
40
        '\n';// 6
41
42
    if(s.lower_bound(20) == s.end()){
      cout << "all elements are less than 20\n";</pre>
43
44
45 }
```

1.2 python

```
sorted((4,1,9,6),reverse=True)
    fruits = ['apple', 'watermelon', 'pear', 'banana']
    a = sorted(fruits, key = lambda x : len(x))
  4 print(a)
  5|# 輸出:['pear', 'apple', 'banana', 'watermelon']
  6 divmod(a,b)
    把除數和餘數運算結果結合起來,
  7
    返回一個包含商和餘數的元組(a // b, a % b)
  10 pow(base, exp[, mod])
 11
    >>> pow(38, -1, mod=97)
 12
    23
  13
    >>> 23 * 38 % 97 == 1
3 14
    True
3 15
  16 eof 寫法
  17
    try:
      while True:
  18
  19
       s = input()
    except EOFError:
  20
  21
      pass
  22
  23
    eval(expression, globals=None, locals=None)
  25
  26 list(map(int, input().split()))
  27
    L.append(r)
  28 my_list = ['This' , 'is' , 'a' , 'string' , 'in' ,
         'Python']
  29 my_string = " ".join(my_list)
  30 #This is a string in Python
  31 test = [[0 for j in range(m)] for i in range(n)]
```

1

Graph 2

Bellman-Ford 2.1

```
1 #include < iostream >
 2 using namespace std;
 3 const int INF = 1e9;
  const int MAXN = 1000;
  const int MAXM = 1000;
  struct Edge {
       int u;
 8
       int v;
9
       int w;
10 };
11
12 int n, m;
13 Edge edges[MAXM];
14
  int dis[MAXN];
15
  // s是起點
16
17
  bool bellman(int s) {
18
       for (int i = 0; i < n; i++) {
19
           dis[i] = INF;
20
       dis[s] = 0;
21
22
       bool relax;
23
       // 做 n 輪
24
       for (int i = 0; i < n; i++) {
25
           relax = false;
26
           for (int j = 0; j < m; j++) {
               int u = edges[j].u;
27
28
                int v = edges[j].v;
29
                int w = edges[j].w;
30
               if (dis[u] == INF) {
31
                    continue;
32
                if (dis[v] > dis[u] + w) {
33
                    dis[v] = dis[u] + w;
34
35
                    relax = true;
36
               }
37
           }
```

2.2 Dijkstra

```
1 | #include < bits/stdc++.h>
2 using namespace std;
3 #define M 100005
4 #define INF 1e9
5 struct Edge{
       int v, w;
6
7
       Edge(int a, int b):v(a), w(b){};
8 };
9 struct node{
10
       int u, dis;
       node(){};
11
       node(int a, int b):u(a), dis(b){};
12
       bool operator < (const node &r)const{</pre>
13
14
           return dis > r.dis;
15
       }
16 }:
17 int dis[M]; //距離
18 vector < Edge > G[M];
19 void init(){
20
       fill(dis, dis+M, INF);
21
       for(int i = 0; i < M; i++){
           G[i].clear();
22
23
24 }
25
  void dijkstra(int start){
26
       dis[start] = 0;
       priority_queue < node > pq;
27
28
       pq.push(node(start, 0));
       while(!pq.empty()){
29
30
           node now = pq.top();
31
           pq.pop();
32
           if(now.dis > dis[now.u]) continue;
33
           for(Edge i : G[now.u]){
                if(dis[i.v] > now.dis + i.w){
34
                    dis[i.v] = now.dis + i.w;
35
                    pq.push(node(i.v, dis[i.v]));
36
37
                    // printf("push(%d, %d)\n", i.v,
                         dis[i.v]);
                }
38
39
           }
       }
40
41
42
  int main(){
43
44
     int point, side;
45
       cin >> point >> side;
       init();
46
       for(int i = 0; i < side; i++){</pre>
47
48
           int s. t. w:
49
           cin >> s >> t >> w;
           G[s].push_back(Edge(t, w));
50
51
           G[t].push_back(Edge(s, w));
       }
52
53
       dijkstra(1);
       for(int i = 2; i <= point; i++){</pre>
54
55
           cout << dis[i] << '\n';
56
57
58 }
```

2.3 Floyd-Warshall

```
1 #include <bits/stdc++.h>
  using namespace std;
  #define M 1005
  #define INF 1e9
6
  int dis[M][M];
  // int G[M][M];
7
  void init(int n){
       for(int i = 0; i <= n; i++){</pre>
9
            for(int j = 0; j \le n; j++){
10
11
                dis[i][j] = INF;
12
                if(i == j) dis[i][j] = 0;
13
14
       }
  }
15
16
  void Floyd(int n){
       for(int k = 1; k \le n; k++){
17
18
            for(int i = 1; i <= n; i++){</pre>
                for(int j = 1; j <= i; j++){</pre>
19
                     dis[i][j]= dis[j][i] =
20
                          min(dis[i][k]+dis[k][j],
                          dis[i][j]);
21
                }
            }
22
       }
23
24 }
25
  void printarr(int r, int c){
       for(int i = 1; i <= r; i++){</pre>
26
            for(int j = 1; j <= c; j++){</pre>
27
28
                if(dis[i][j] == INF) cout << "INF ";</pre>
29
                else cout << dis[i][j] << ' ';</pre>
30
31
            cout << '\n';
32
       }
33 }
  int main(){
34
35
     int point, side;
       cin >> point >> side;
36
37
       init(point);
       for(int i = 0; i < side; i++){</pre>
38
39
            int s, t, w;
40
            cin >> s >> t >> w;
            dis[s][t] = w;
41
42
            dis[t][s] = w;
43
       }
       Floyd(point);
44
45
       int Cas;
       cin >> Cas;
46
47
       while(Cas--){
            int i, j;
48
            cin >> i >> j;
49
50
            cout << dis[i][j] << '\n';</pre>
51
52
       // printarr(point, point);
53
```

2.4 SPFA

```
1 const int INF = 1e9;
  const int MAXN = 1000;
  struct Edge {
4
      int v;
5
      int w;
6
  };
7 int n, m;
8 vector < Edge > G[MAXN];
                           //向量記圖
  int dis[MAXN];
10 void SPFA(int s) {
      // 記錄目前的點是否在 queue 中
11
12
      bool inq[n];
13
      for (int i = 0; i < n; i++) {
          dis[i] = INF;
14
```

```
inq[i] = false;
15
       }
16
17
       dis[s] = 0;
       inq[s] = true;
18
       queue < int > q;
19
       q.push(s);
20
21
       while (!q.empty()) {
22
           int u = q.front();
23
           q.pop();
24
            inq[u] = false;
25
           for (Edge e : G[u]) {
                if (dis[e.v] > dis[u] + e.w) {
26
27
                    dis[e.v] = dis[u] + e.w;
                    if (!inq[e.v]) {
28
29
                         inq[e.v] = true;
                         q.push(e.v);
30
31
                }
32
33
           }
       }
34
35 }
```

2.5 SPFA

```
1 const int INF = 1e9;
2 const int MAXN = 1000;
3 struct Edge {
4
       int v;
5
       int w;
6 };
7 int n, m;
8 vector < Edge > G[MAXN];
                            //向量記圖
9 int dis[MAXN];
10 void SPFA(int s) {
       // 記錄目前的點是否在 queue 中
11
       bool inq[n];
12
       for (int i = 0; i < n; i++) {</pre>
13
14
           dis[i] = INF;
           inq[i] = false;
15
16
       dis[s] = 0;
17
18
       inq[s] = true;
19
       queue < int > q;
       q.push(s);
20
21
       while (!q.empty()) {
          int u = q.front();
22
23
           q.pop();
           inq[u] = false;
24
           for (Edge e : G[u]) {
25
               if (dis[e.v] > dis[u] + e.w) {
26
                   dis[e.v] = dis[u] + e.w;
27
                   if (!inq[e.v]) {
28
29
                        inq[e.v] = true;
                        q.push(e.v);
30
31
                   }
               }
32
33
           }
34
       }
35 }
```

3 Other

3.1 thm