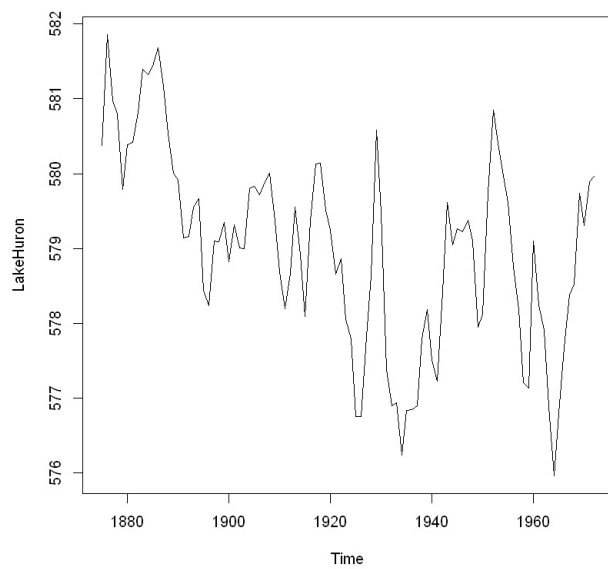
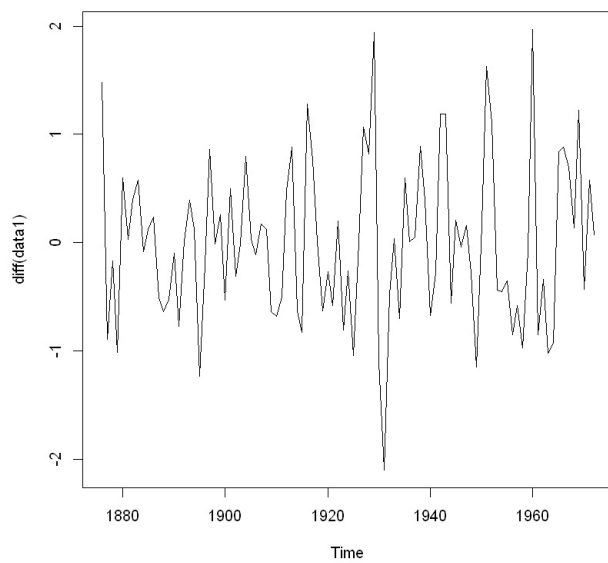


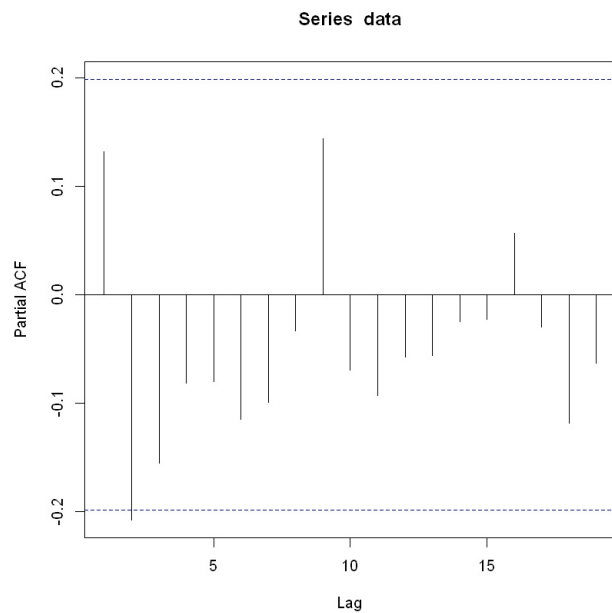
```
In [3]: plot(LakeHuron)
```



```
In [5]: data1<- LakeHuron  
plot(diff(data1))  
data<-diff(data1)
```



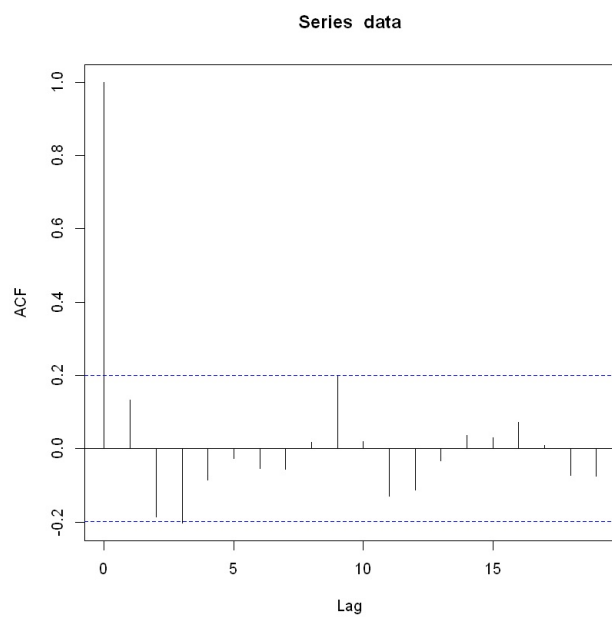
```
In [6]: pacf(data)
```



```
In [8]: (acf(data))
```

Autocorrelations of series 'data', by lag

	0	1	2	3	4	5	6	7	8	9	10
11	1.000	0.132	-0.187	-0.203	-0.087	-0.026	-0.053	-0.055	0.017	0.200	0.019
12		11	12	13	14	15	16	17	18	19	
	-0.130	-0.112	-0.034	0.036	0.030	0.072	0.008	-0.072	-0.075		



Yule walker matrix form

```
In [10]: r=NULL
r[1:2]=acf(diff(LakeHuron), plot=F)$acf[2:3]
r
```

```
0.131924092945853 - 0.187087447396466i
```

```
In [11]: R=matrix(1,2,2)
R[1,2]=r[1]
R[2,1]=r[1]
R
```

```
A matrix: 2 x 2 of type dbl
```

```
1.0000000 0.1319241
0.1319241 1.0000000
```

```
In [12]: b=matrix(r,nrow=2,ncol=1)
b
```

A matrix: 2 ×

1 of type dbl

0.1319241

-0.1870874

Estimating phi

```
In [13]: phi.hat=solve(R,b)
phi.hat
```

A matrix: 2 ×

1 of type dbl

0.1593793

-0.2081134

Calculating gamma 0

```
In [16]: c0=acf(data, type='covariance', plot=F)$acf[1]
c0
```

0.555290530343286

Estimating variance

```
In [17]: var.hat=c0*(1-sum(phi.hat*r))
var.hat
```

0.521994548155539

Let X_t = LakeHuron and $y_t = \text{diff}(\text{LakeHuron})$

$$X_t = 1.1594X_{t-1} - 0.3675X_{t-2} + 0.2081X_{t-3} + Z_t$$

where $Z_t \sim \text{Normal}(0, 0.52)$

$$(1 - 0.1594B + 0.2081B^2)(1-B)X_{t-1} = Z_t$$

$$Y_t = 0.1594Y_{t-1} - 0.2081Y_{t-2} + Z_t$$

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