

# Deviation-based Ranking System

Daekyung Lee<sup>1</sup>, Mi Jin Lee<sup>1</sup>, Seung Ki Baek<sup>2</sup> and Beom Jun Kim<sup>1</sup>

*1)Department of Physics, Sungkyunkwan University*

*2)Department of Physics, Pukyong University*

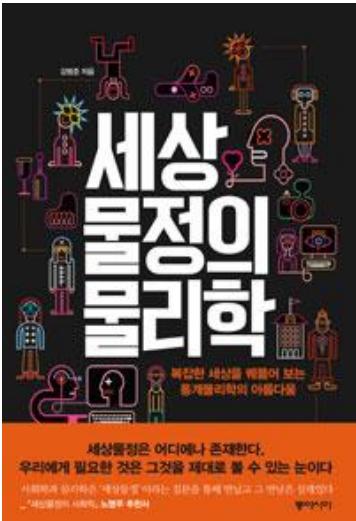
**2017.4.10 workshop in Chonbuk National University**

# Introduction

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## Rating System

How can we know quality of object?



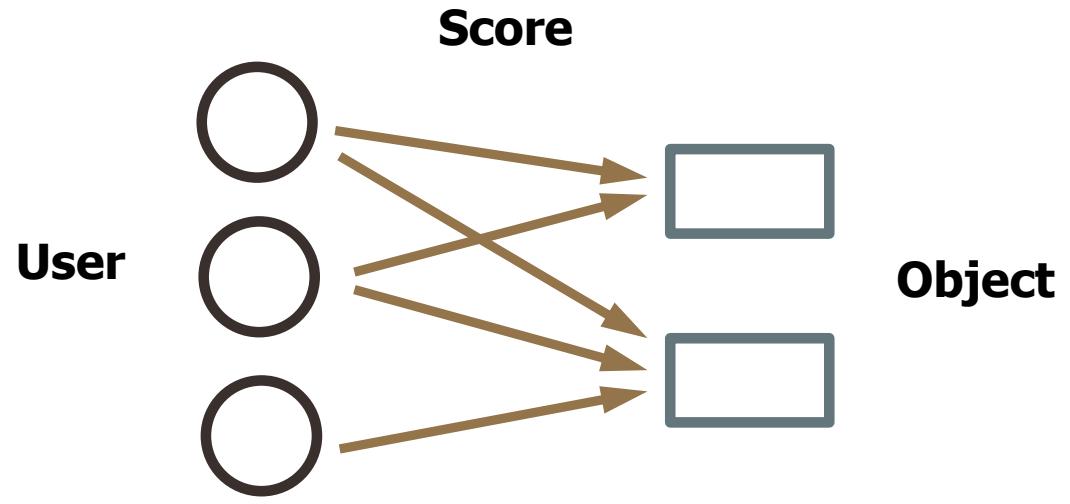
과학 > 과학일반  
**세상물정의 물리학**

복잡한 세상을 페뚫어 보는 통계물리학의 아름다움

김범준 저

★★★★★ 4.3점 (20명)

도서정보 | 동아시아 출판 | 2015년 09월 16일 출간 | EPUB | 13.5 MB  
지원기기 | PAPER | iOS | Android | PC | Mac  
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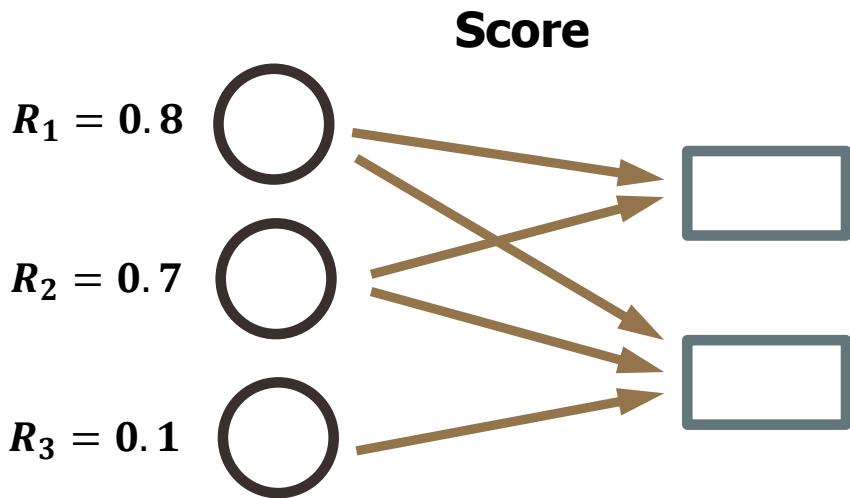


- Users evaluate objects and assign discrete scores
- Quality of object is determined by average score
- Vulnerable to distortion by spammer

# Introduction

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## Reputation System



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**IR, CR, RR, cosRA, ...**

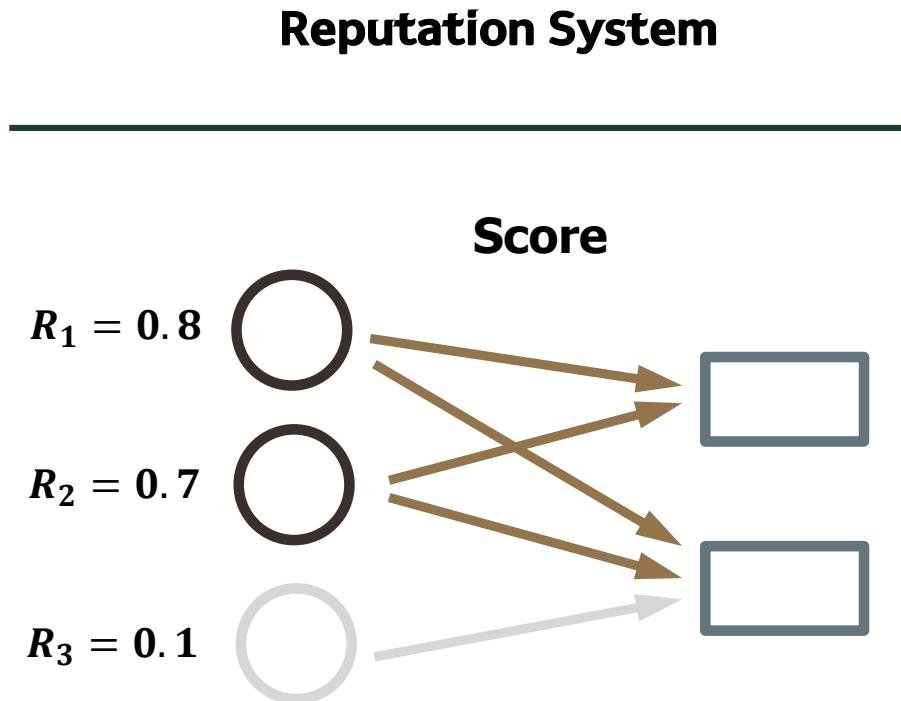
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**GR<sup>1)</sup>**  
**Group-based Ranking System**

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# Introduction

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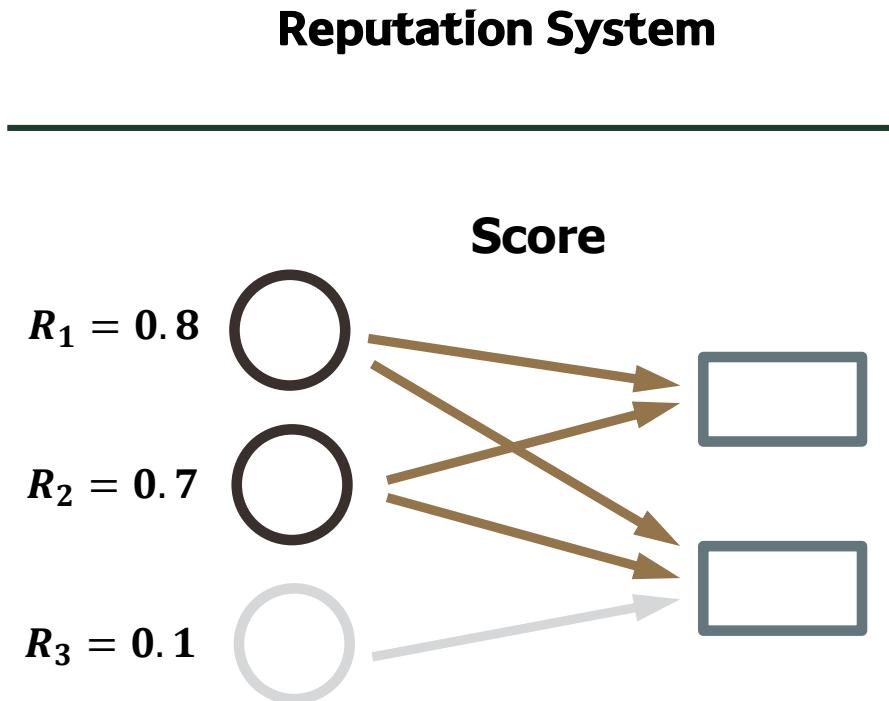
**IR, CR, RR, cosRA, ...**

**GR<sup>1)</sup>**  
**Group-based Ranking System**

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# Introduction

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**IR, CR, RR, cosRA, ...**

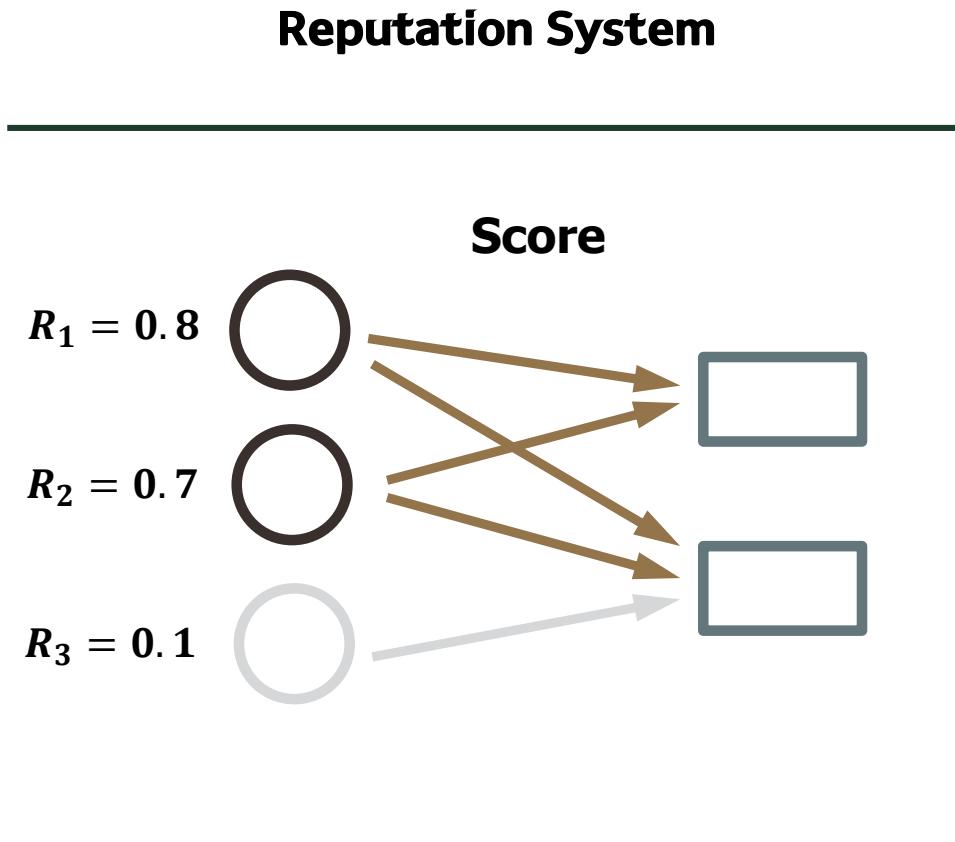
**GR<sup>1)</sup>**  
**Group-based Ranking System**

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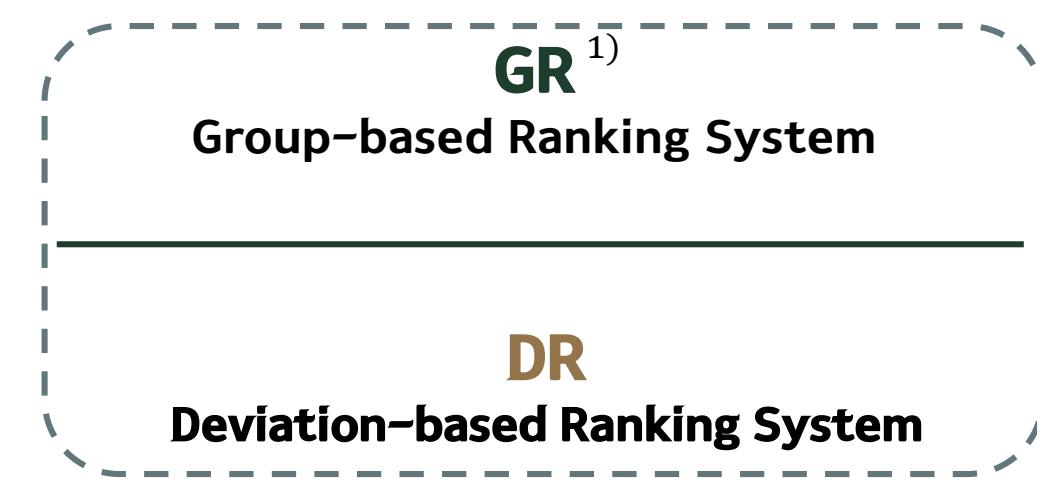
**DR**  
**Deviation-based Ranking System**

# Introduction

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**IR, CR, RR, cosRA, ...**

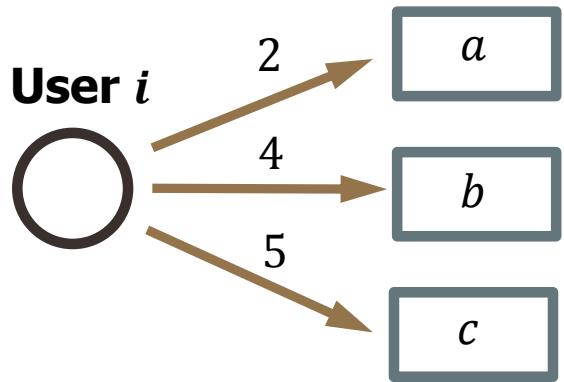


# GR method

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Object  $\in \{a, b, c\}$

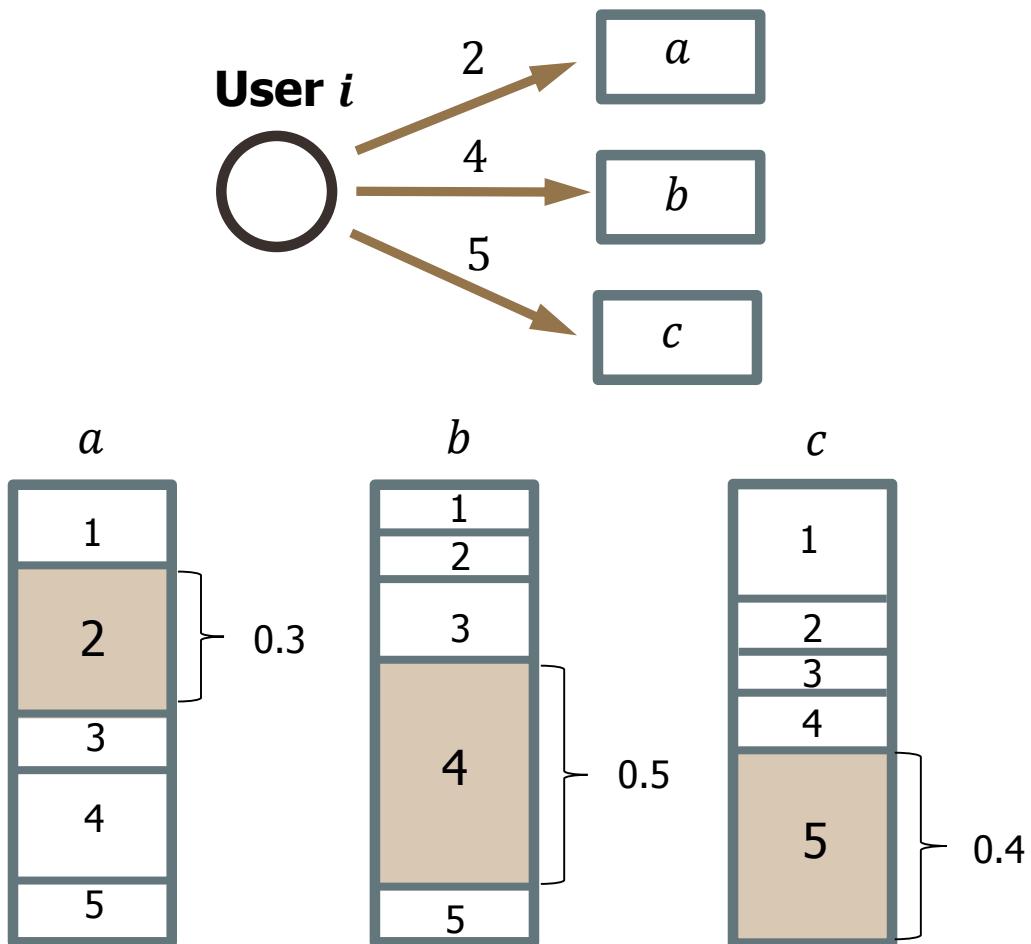
Score  $\in \{1, 2, 3, 4, 5\}$



# GR method

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Object  $\in \{a, b, c\}$   
Score  $\in \{1, 2, 3, 4, 5\}$



$$\vec{x} = (0.3, 0.5, 0.4)$$

Reputation :  $R_i = \frac{\text{mean}(\vec{x})}{\sqrt{\text{var}(\vec{x})}} = \frac{0.4}{0.1} = 4$

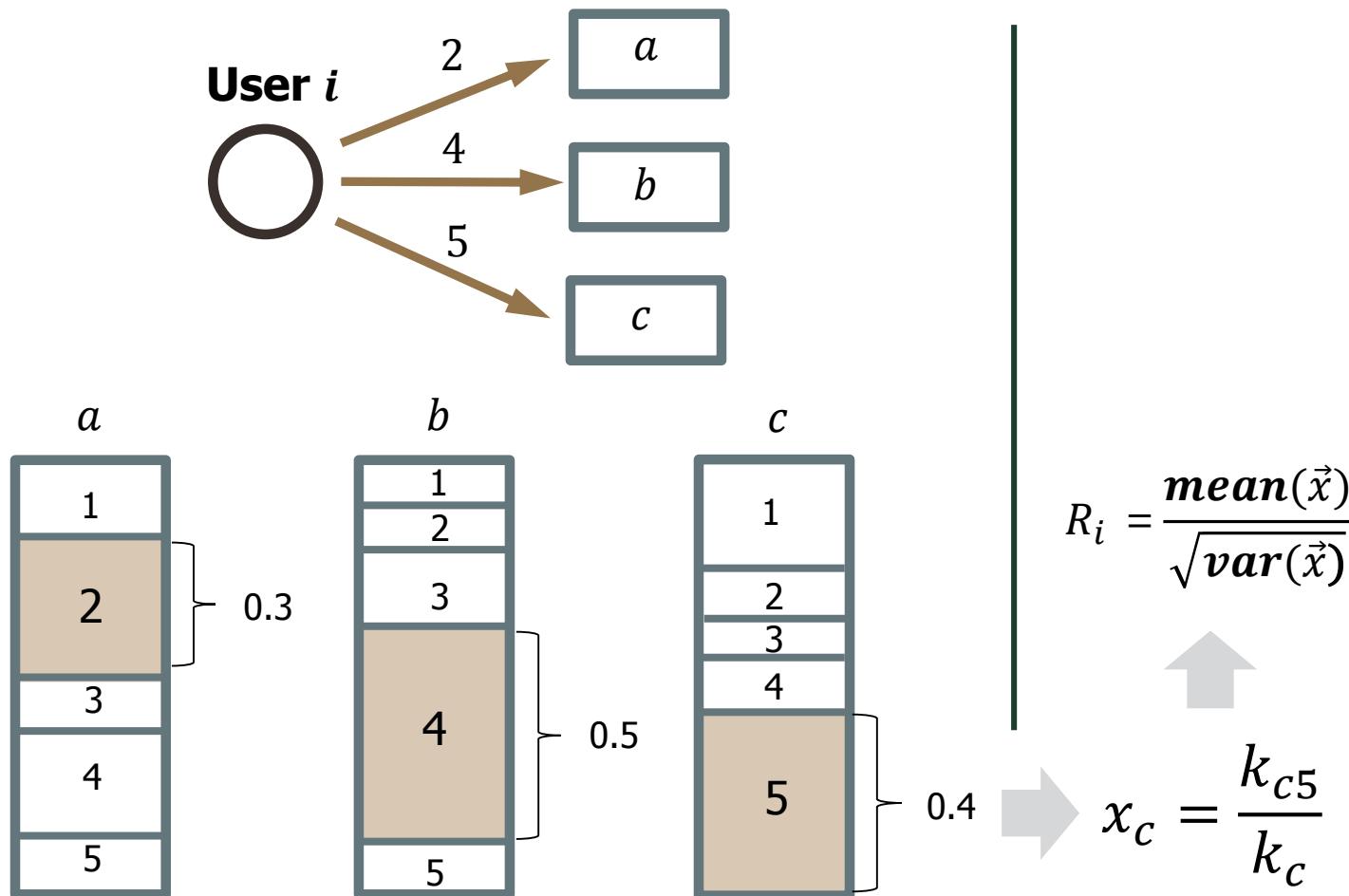
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- User who gives popular score to each object takes high reputation
- Better performance than others
- Fragile to malicious attack

# IGR method

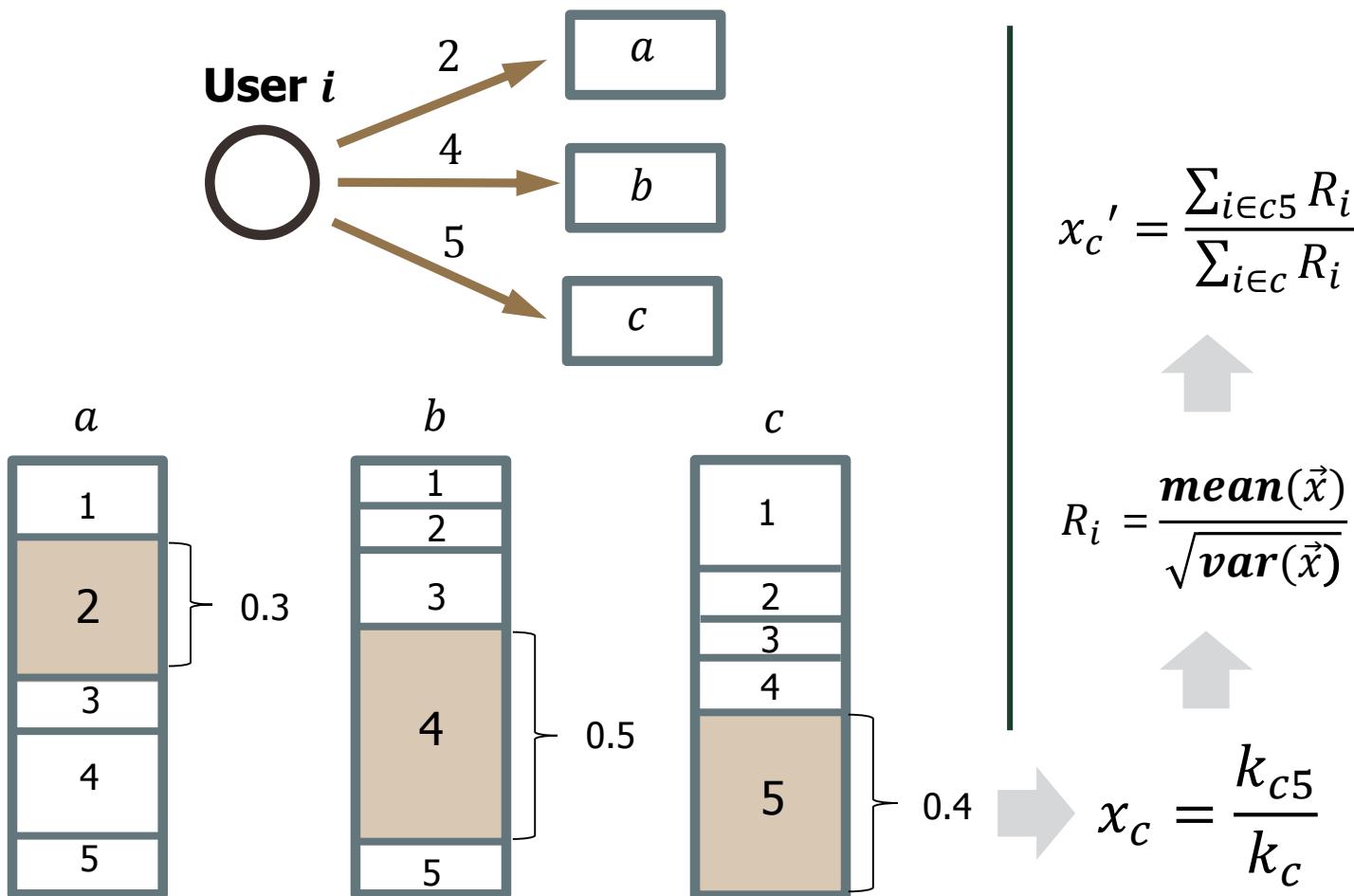
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Object  $\in \{a, b, c\}$   
Score  $\in \{1, 2, 3, 4, 5\}$



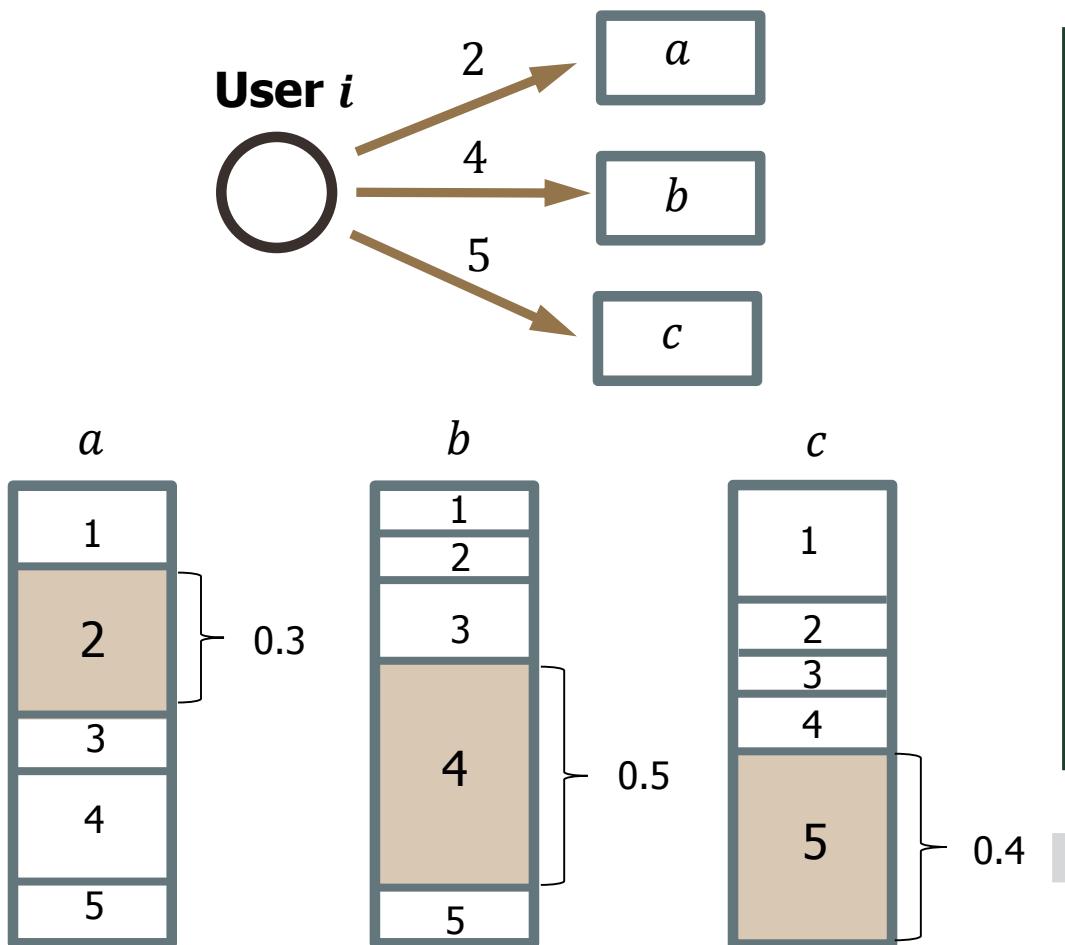
# IGR method

Object  $\in \{a, b, c\}$   
Score  $\in \{1, 2, 3, 4, 5\}$



# IGR method

Object  $\in \{a, b, c\}$   
Score  $\in \{1, 2, 3, 4, 5\}$



$$x_c' = \frac{\sum_{i \in c} R_i}{\sum_{i \in c} R_i}$$

$$R_i' = \frac{\text{mean}(\vec{x})}{\sqrt{\text{var}(\vec{x})}}$$

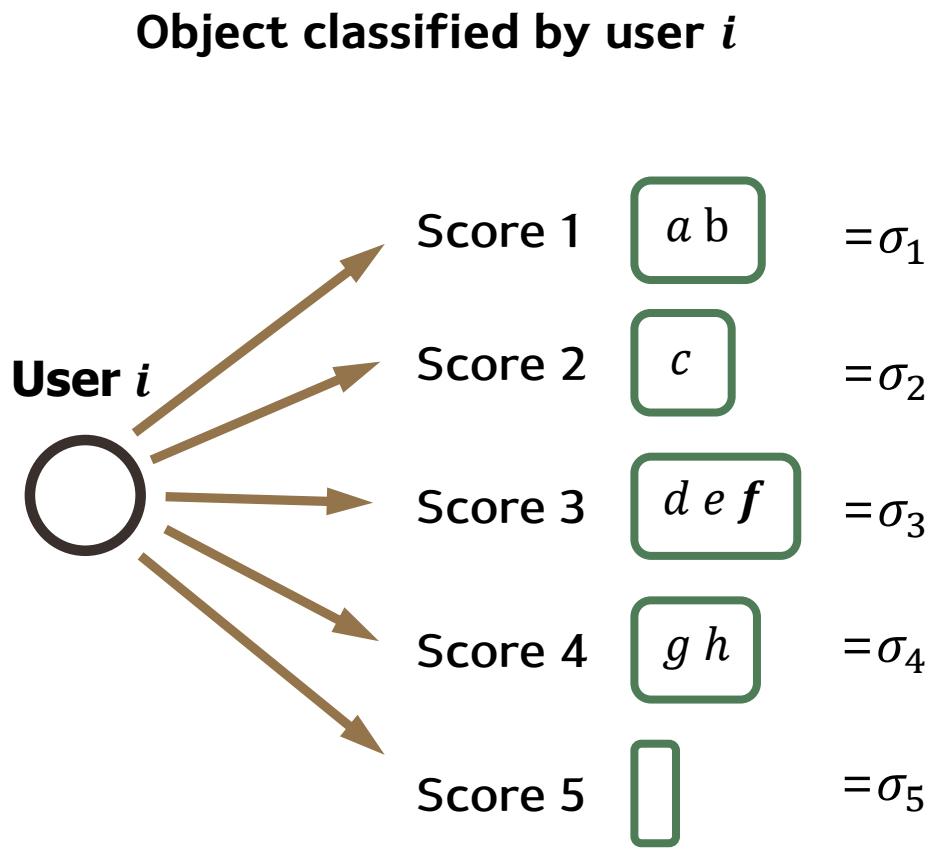
$$x_c = \frac{k_{c5}}{k_c}$$

$$R_i' = \frac{\text{mean}(\vec{x}')}{\sqrt{\text{var}(\vec{x}')}}$$

# DR method

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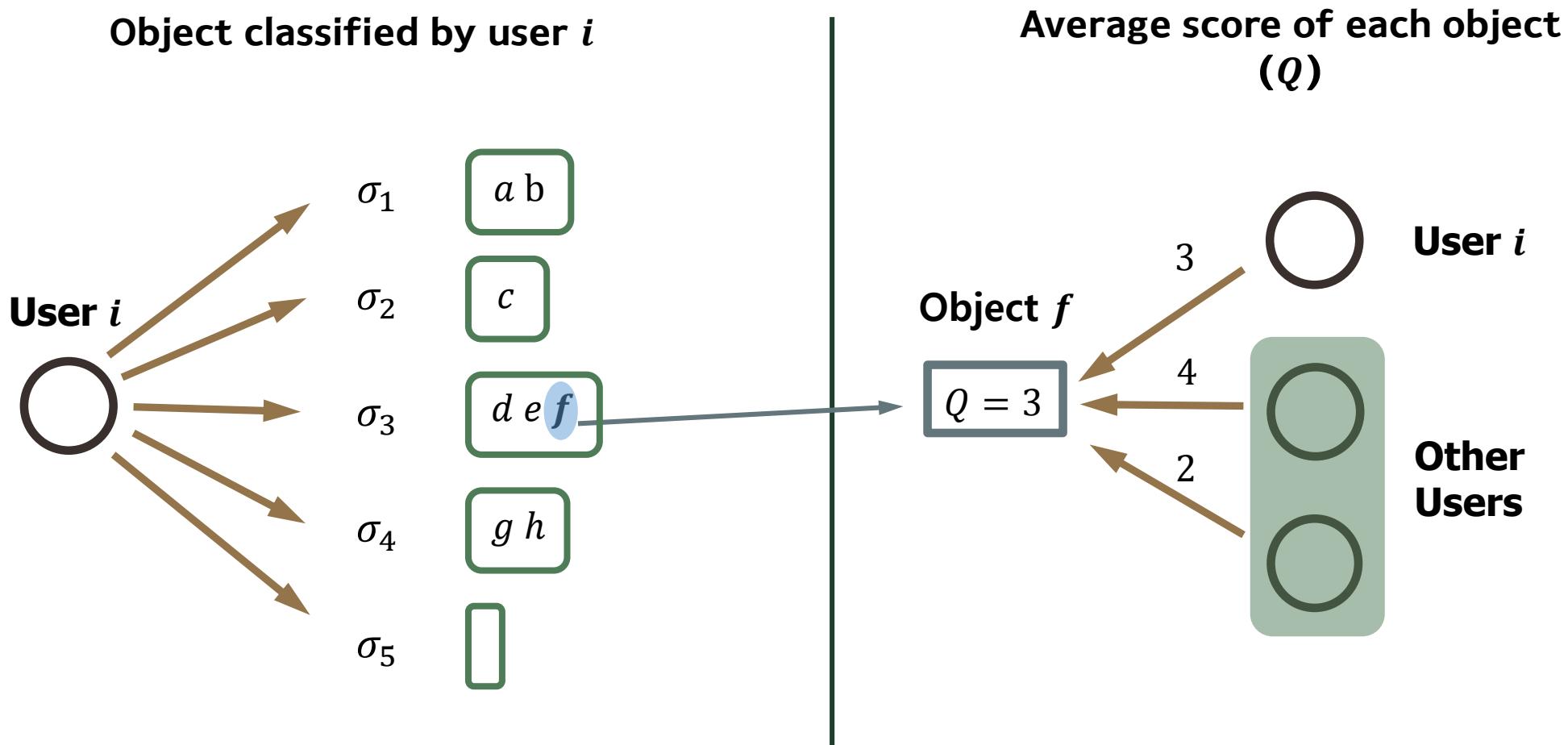
Object  $\in \{a, b, c, d, e, f, g, h\}$   
Score  $\in \{1, 2, 3, 4, 5\}$



# DR method

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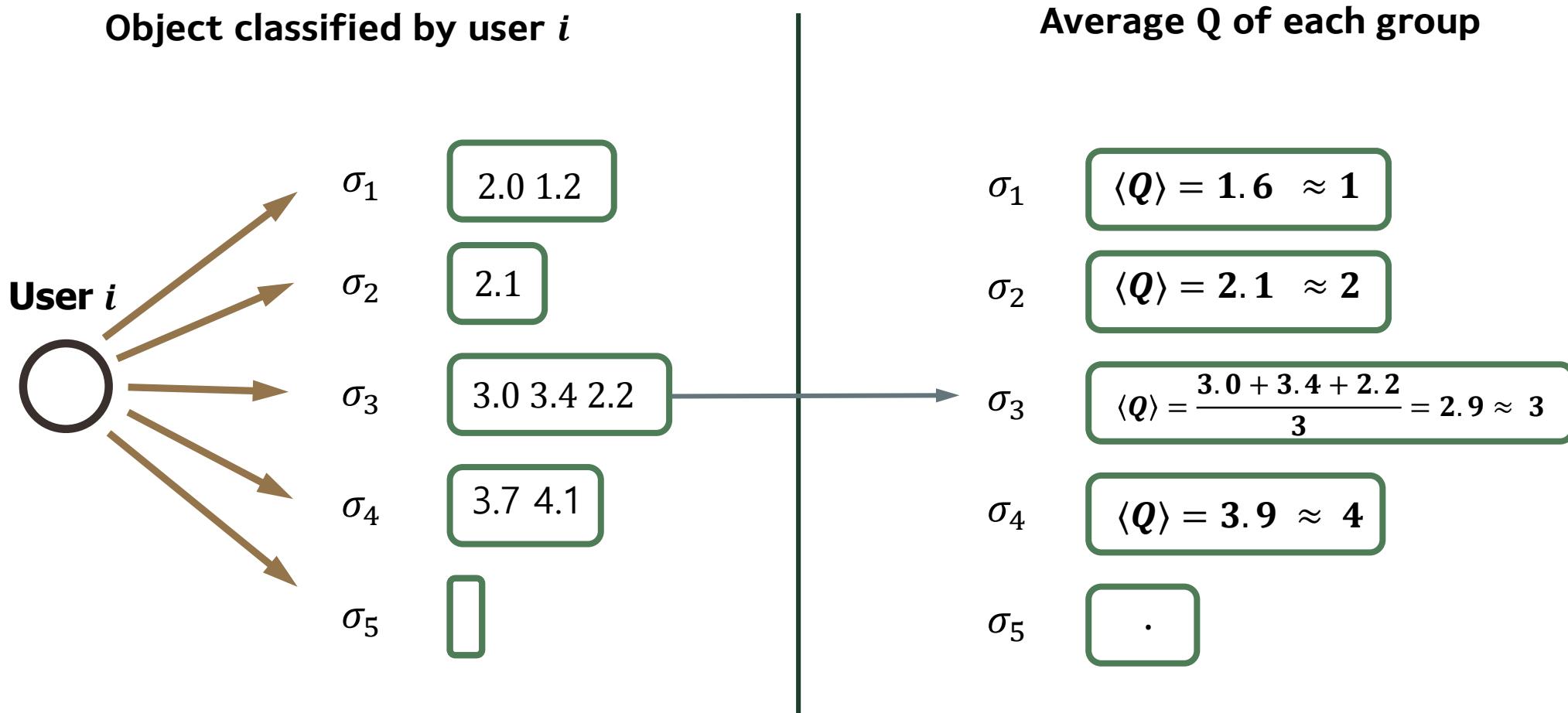
Object  $\in \{a, b, c, d, e, f, g, h\}$   
Score  $\in \{1, 2, 3, 4, 5\}$



# DR method

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Object  $\in \{a, b, c, d, e, f, g, h\}$   
Score  $\in \{1, 2, 3, 4, 5\}$



# DR method

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Average  $Q$  of each group  
(ideal case)

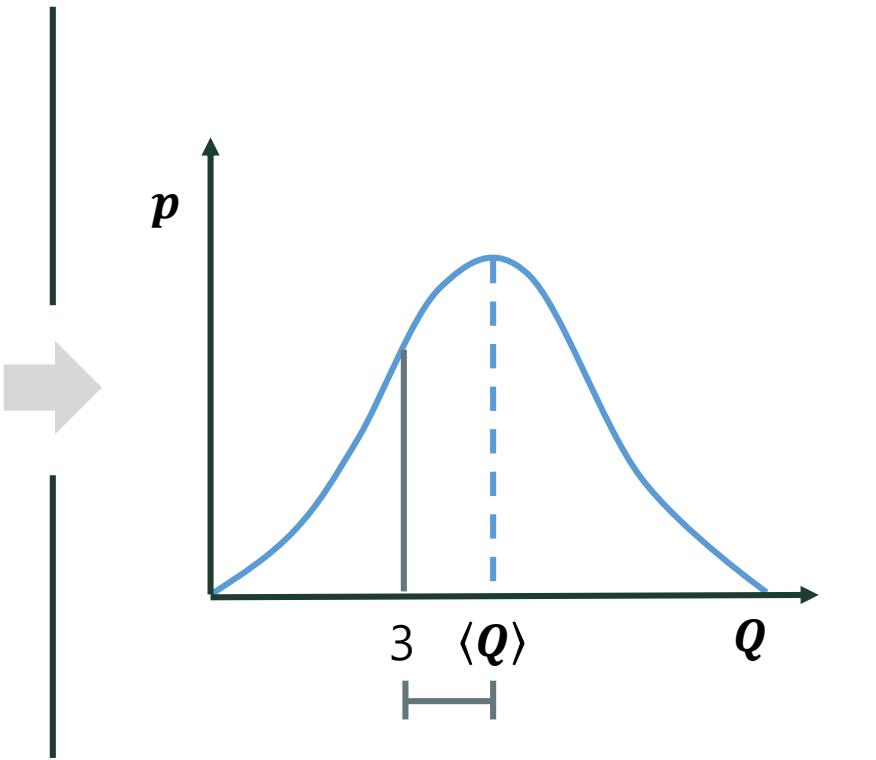
$$\sigma_1 \quad \langle Q \rangle \approx 1$$

$$\sigma_2 \quad \langle Q \rangle \approx 2$$

$$\sigma_3 \quad \langle Q \rangle \approx 3$$

$$\sigma_4 \quad \langle Q \rangle \approx 4$$

$$\sigma_5 \quad \langle Q \rangle \approx 5$$



# DR method

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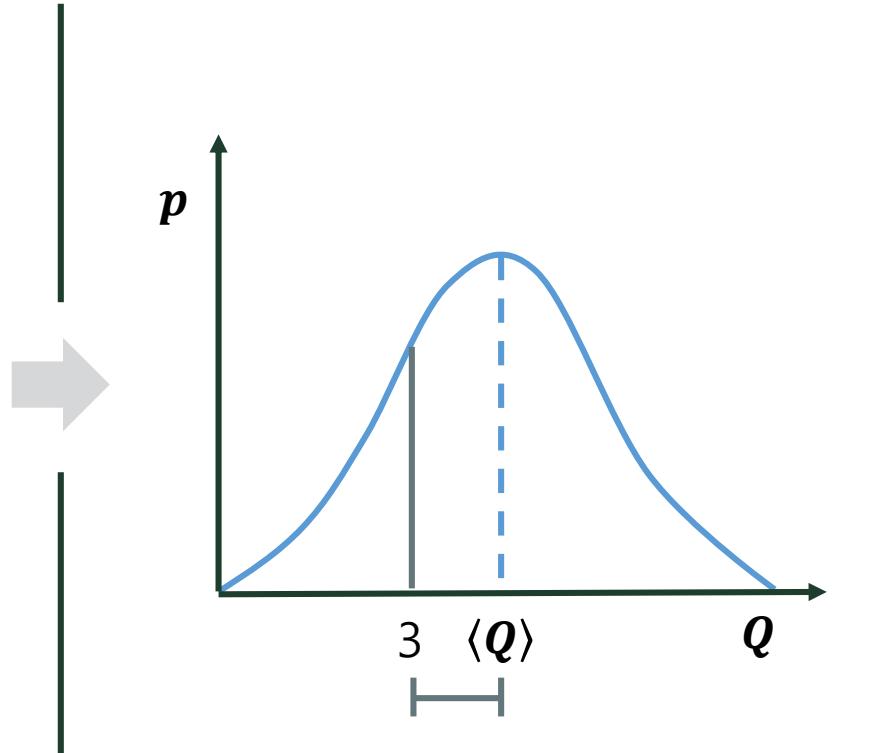
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$$\sigma_5 \quad \langle Q \rangle \approx 5$$



group size =  $w_3$

$$R_i^3 = - \left| \frac{\langle Q \rangle - 3}{\sigma(Q)} \right|$$
$$= -\sqrt{w_3} |\langle Q \rangle - 3|$$

# DR method

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Average  $Q$  of each group  
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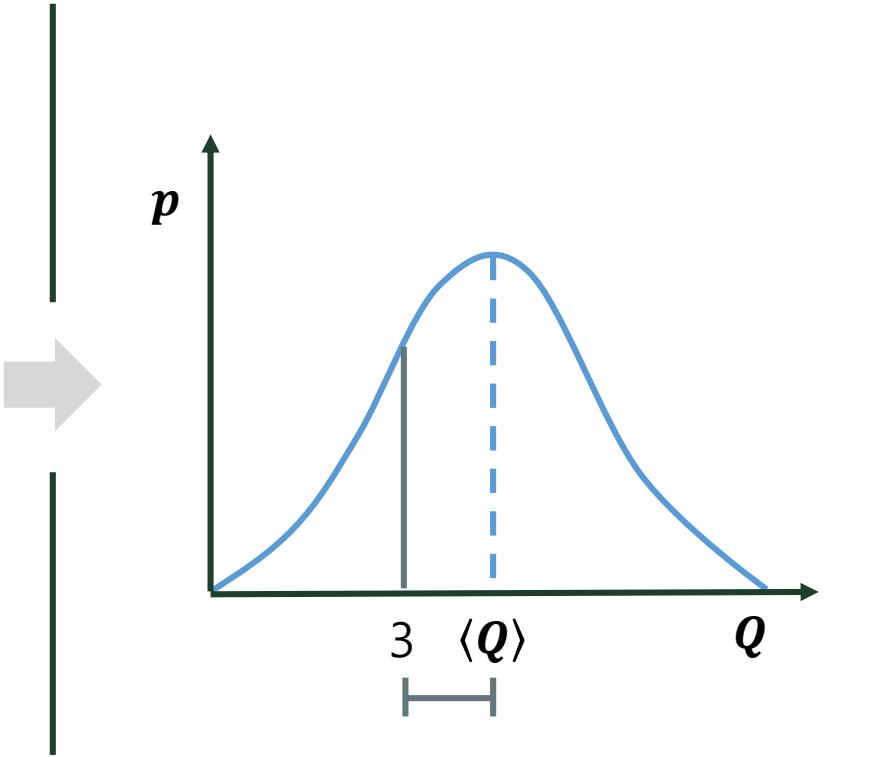
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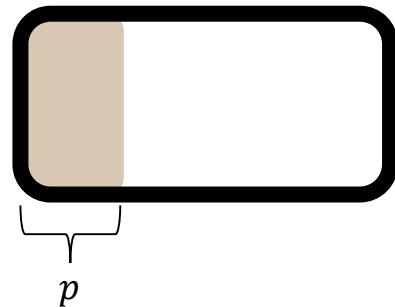
$$= -\sqrt{w_3} |\langle Q \rangle - 3|$$

$$R_i = \sum_{m=1}^5 R_i^m$$

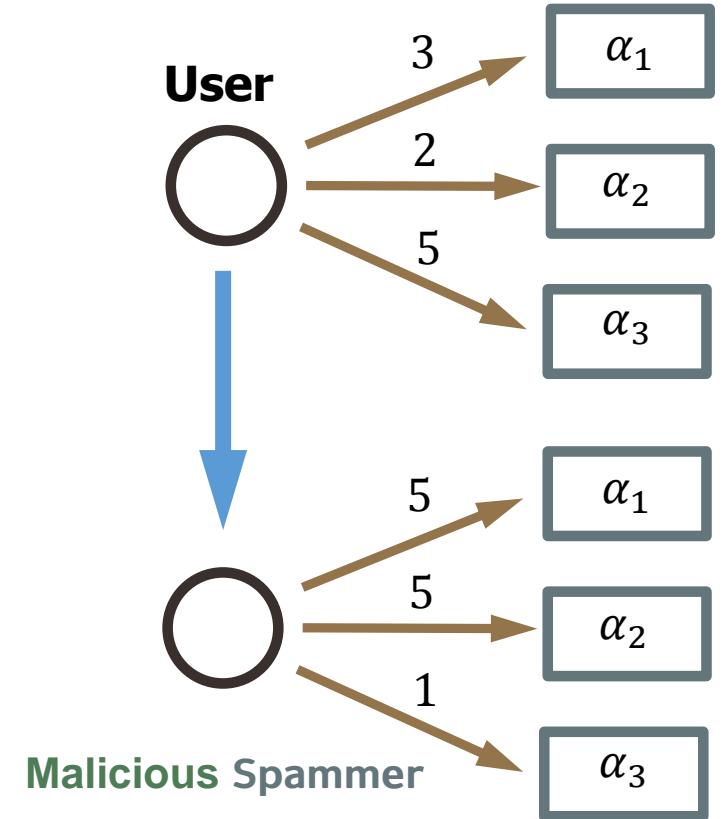
# Measurement

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(MovieLens, Netflix, Amazon)



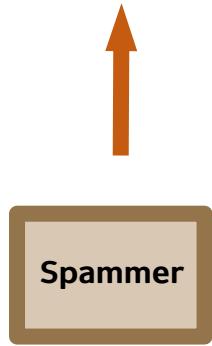
- Converting  $p$  fraction of users in real data to spammer
- ‘**Malicious**’ spammers evaluate with Score $\in \{1,5\}$
- ‘**Random**’ spammer evaluate with Score $\in \{1,2,3,4,5\}$



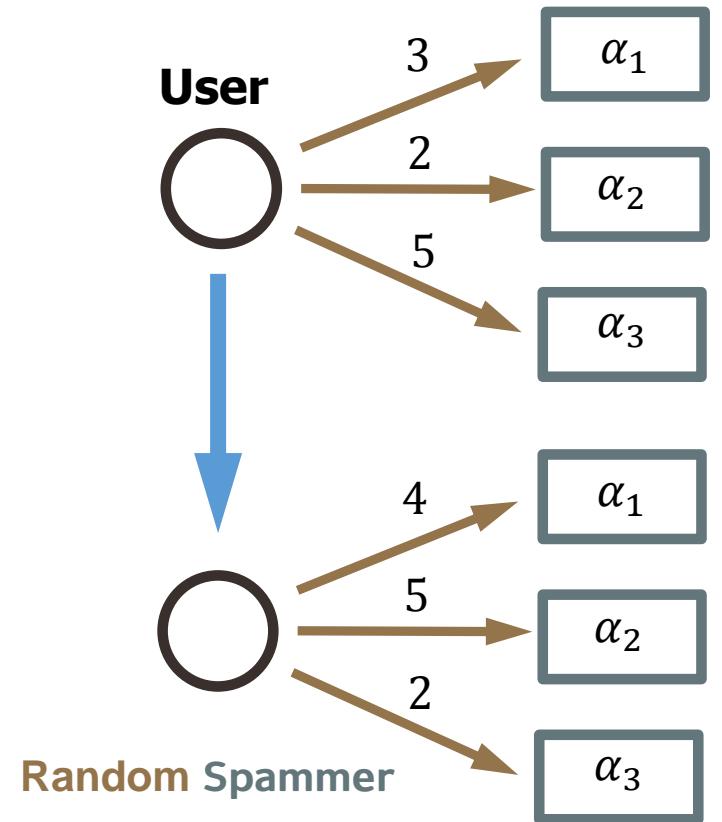
# Measurement

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(MovieLens, Netflix, Amazon)



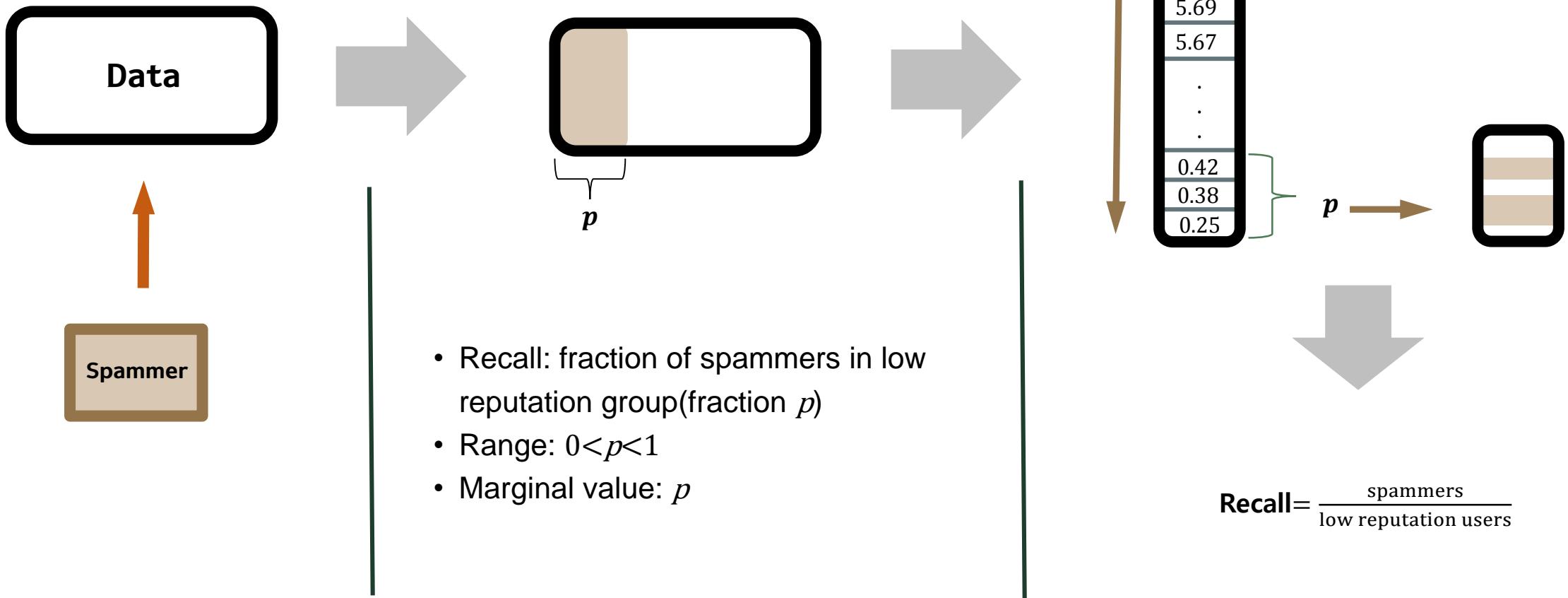
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# Measurement

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(MovieLens, Netflix, Amazon)



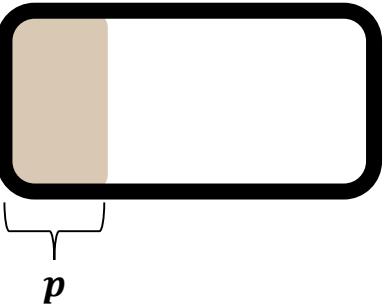
# Measurement

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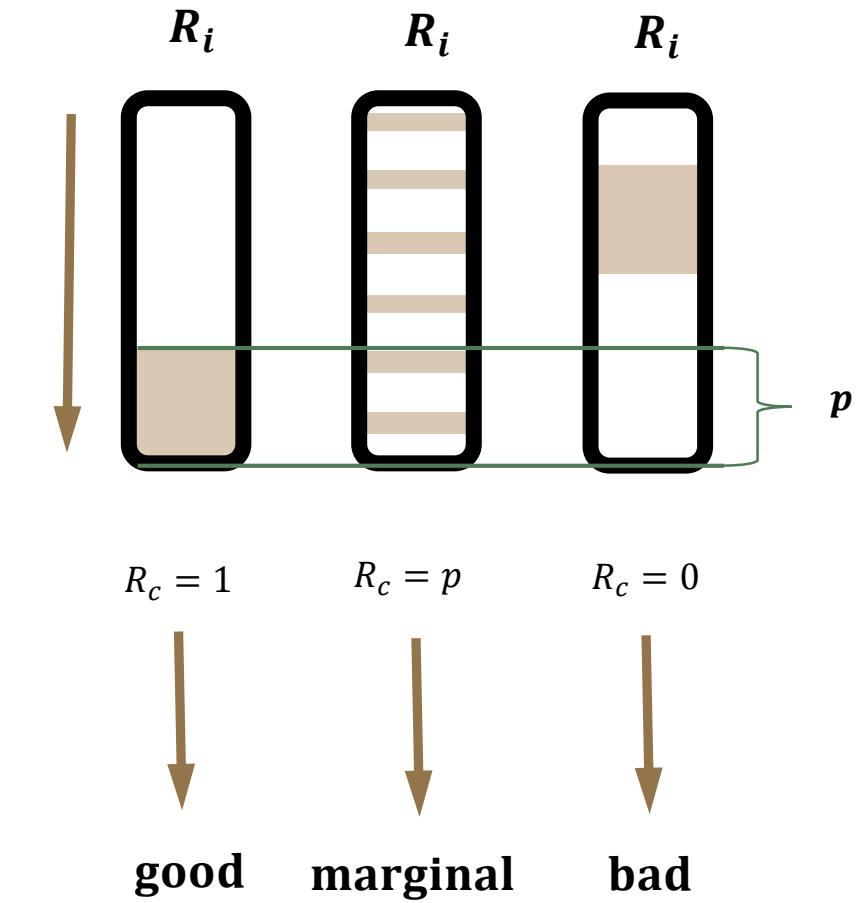
(MovieLens, Netflix, Amazon)



Spammer



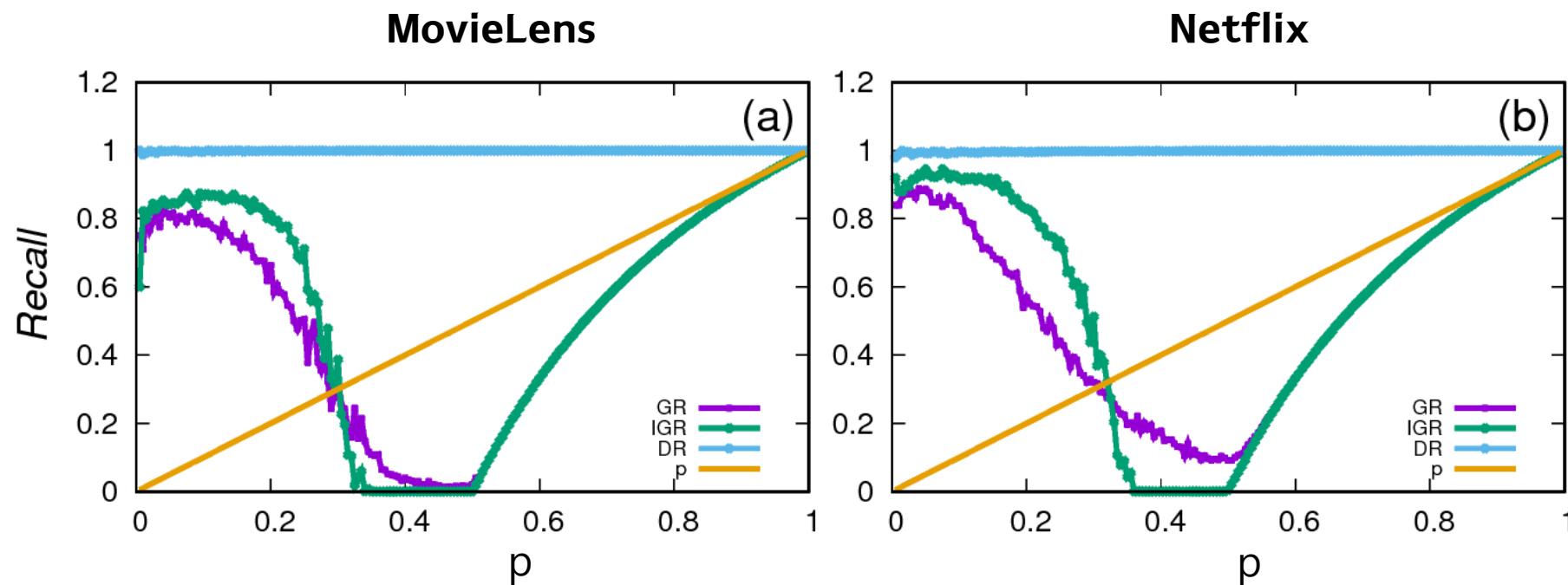
- Recall: fraction of spammers in low reputation group(fraction  $p$ )
- Range:  $0 < p < 1$
- Marginal value:  $p$



# Result

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Malicious spammer



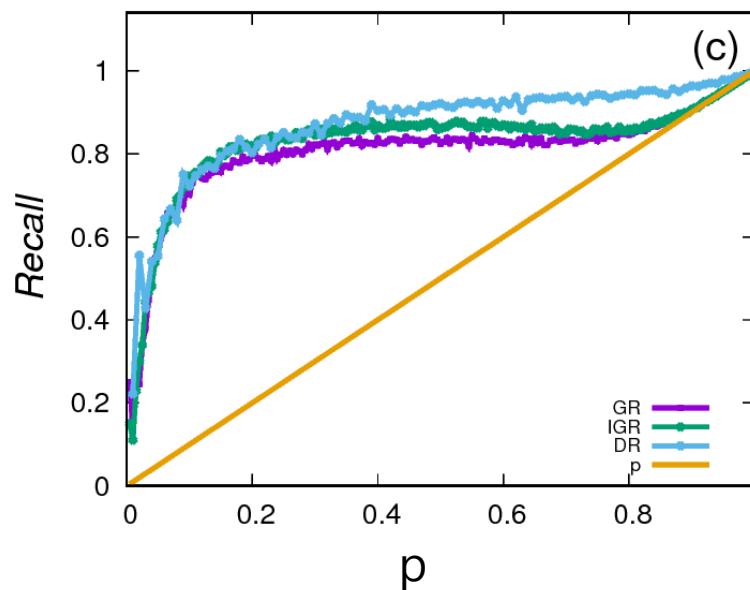
- GR: performing very low value at range  $p>0.3$
  - DR: performing higher than 0.98 in entire range
  - DR method shows higher robustness from malicious attack
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# Result

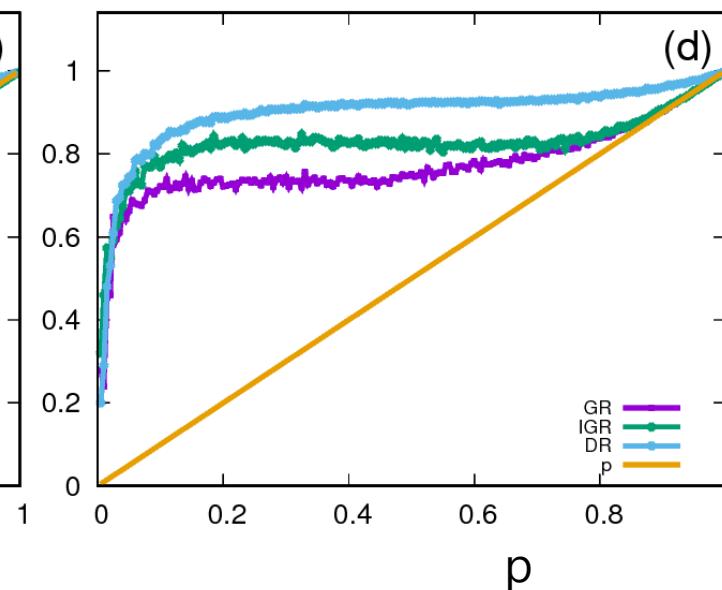
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Random spammer

MovieLens



Netflix

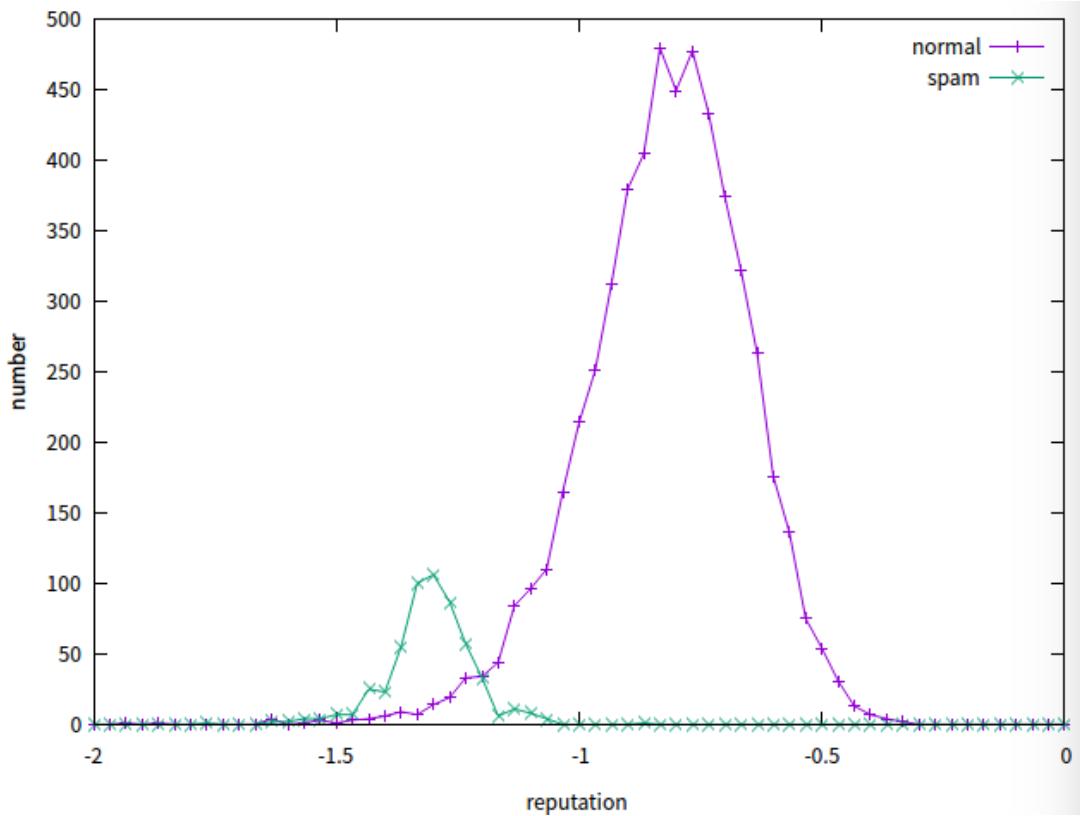


- GR and IGR method show similar curve shape
  - DR method shows higher performance, especially in high  $p$  region
  - 3 curves are similar in low  $p$  region
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# Result

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Distribution of reputation

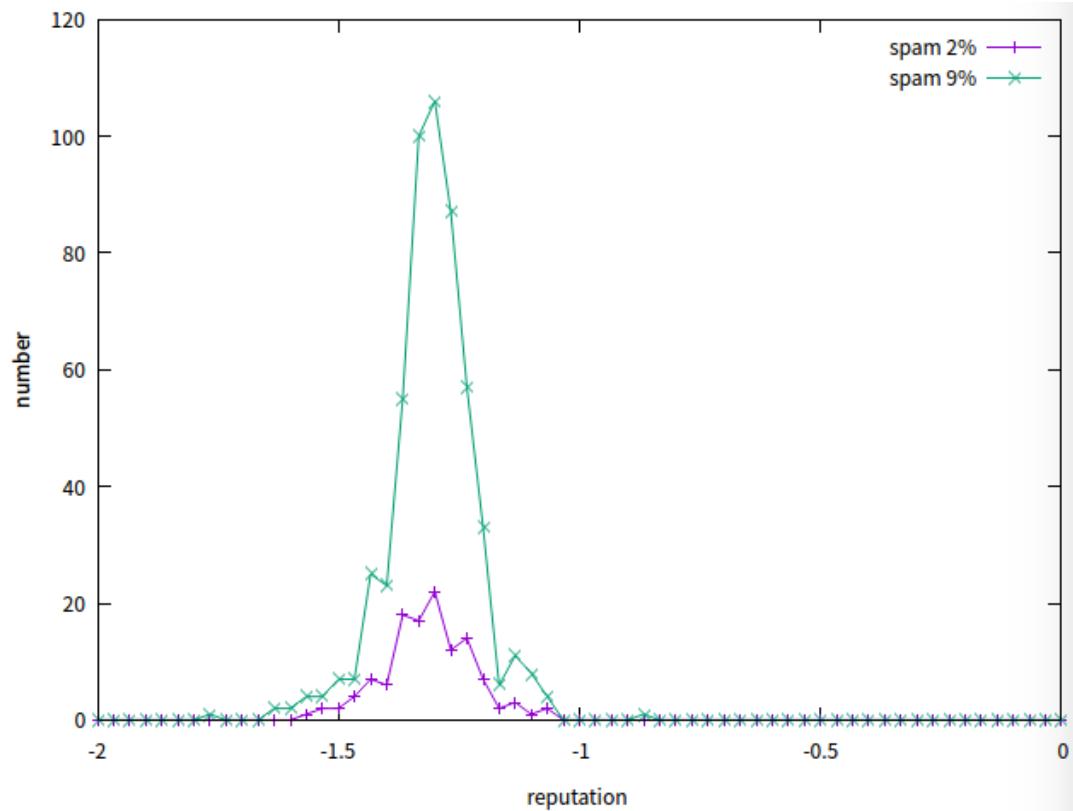


- Overlap between spammer and user

# Result

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Distribution of reputation



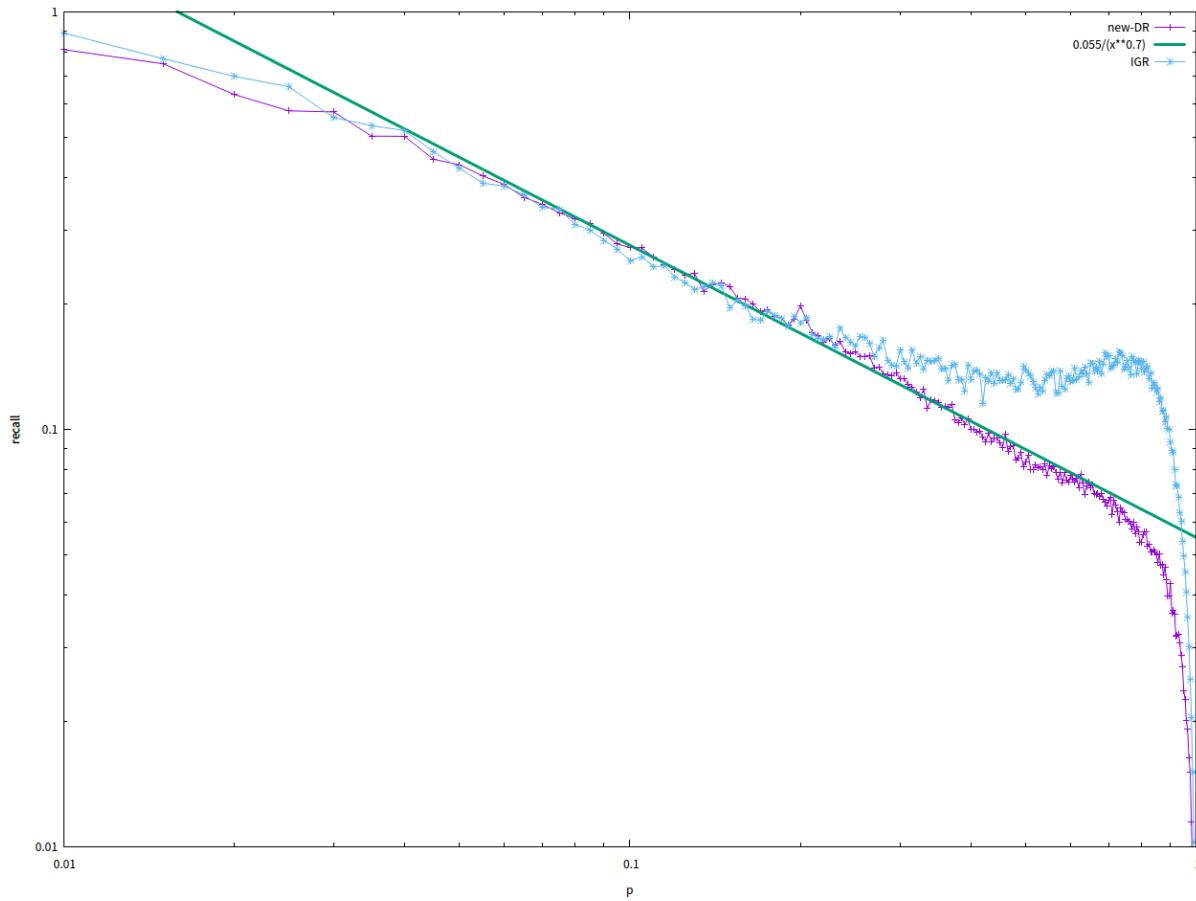
- Overlap between spammer and user
- Spammers' rating distribution is Gaussian(?)
- Overlap = original spammer?

# Result

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Overlap = power function?

1-recall



$$\text{recall} = 1 - 0.055p^{0.7}$$

$$0.055p^{0.7} = \text{original spammer?}$$

# Result

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## Cutting low reputation user

