



Teleconnection Phenomena in Climate Network via Sea Surface Temperature Datasets

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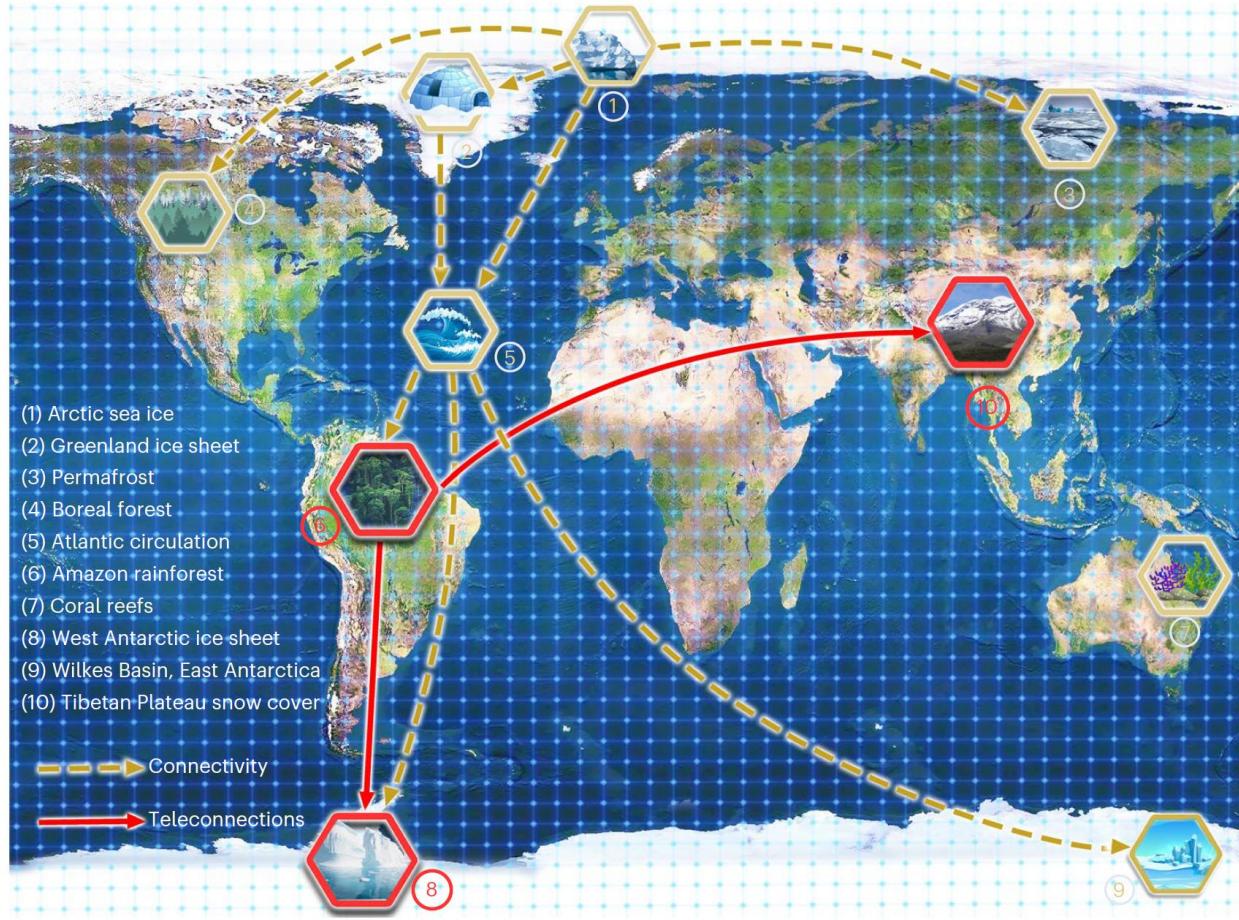
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- Climate phenomena in various regions of the world are connected to each other
- Observing inter-regional climate correlation using data such as air and ocean temperature

Correlation of climate phenomena

Introduction



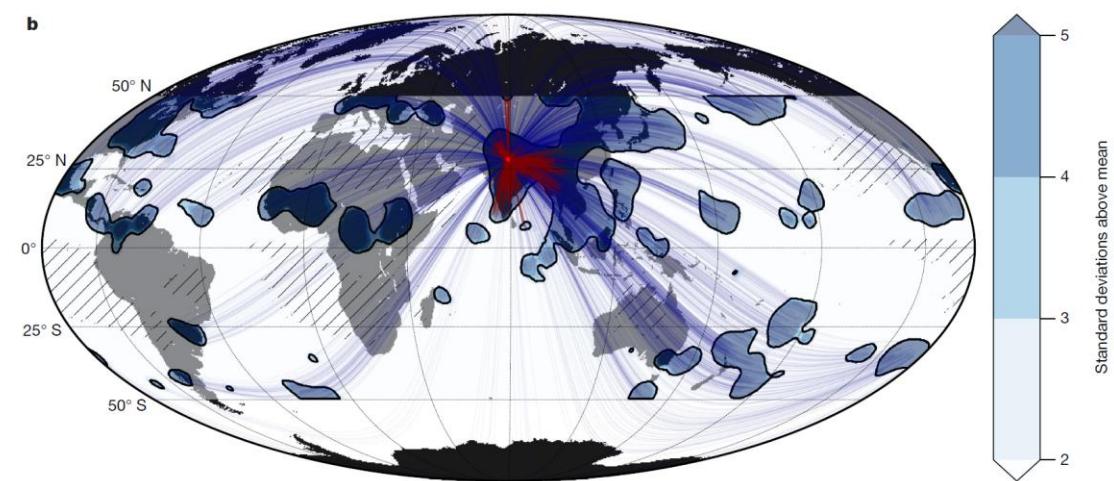
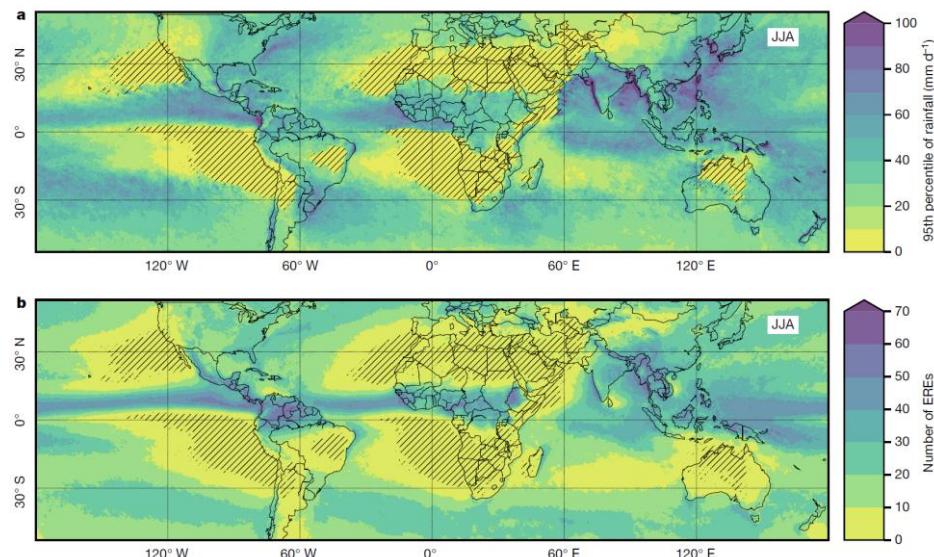
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- Observing inter-regional climate correlation using data such as air and ocean temperature

LETTER

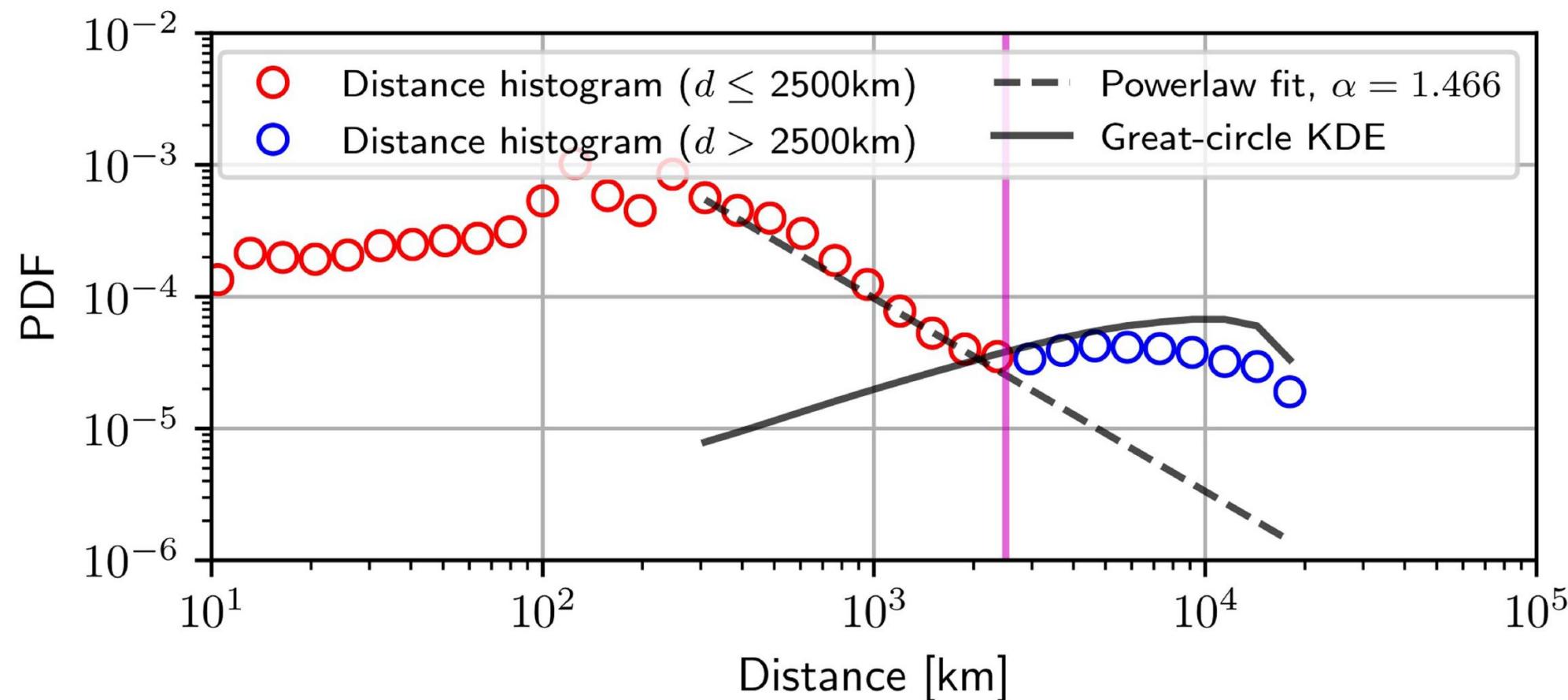
<https://doi.org/10.1038/s41586-018-0872-x>

Complex networks reveal global pattern of extreme-rainfall teleconnections

Niklas Boers^{1,2*}, Bedartha Goswami^{2,7}, Aljoscha Rheinwald^{3,7}, Bodo Bookhagen³, Brian Hoskins^{1,4} & Jürgen Kurths^{2,5,6}



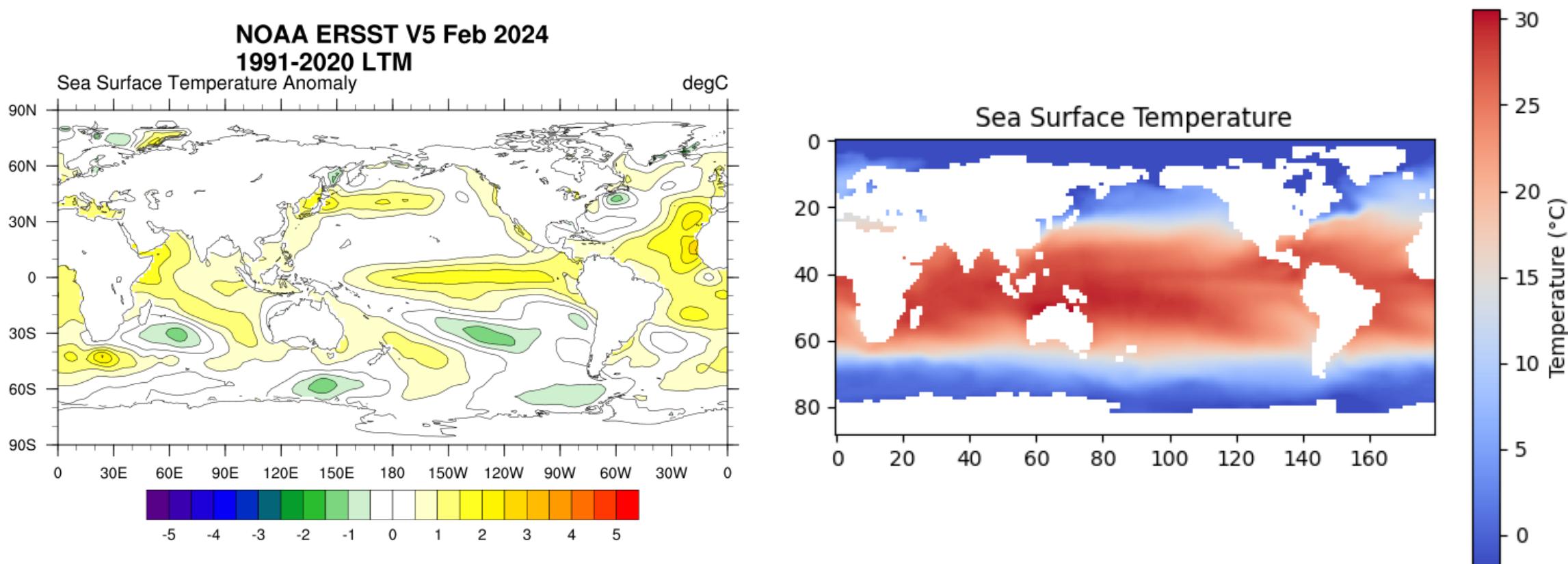
- 2019 Nature paper: Observing teleconnection in global precipitation data
- Synchronization analysis of intense rainfall events (ERE) where high rainfall is observed in a specific region
- Inter-regional correlation is measured through the number of times EREs in two regions occur together
- Many significant correlations are observed even at longer distances → Teleconnection



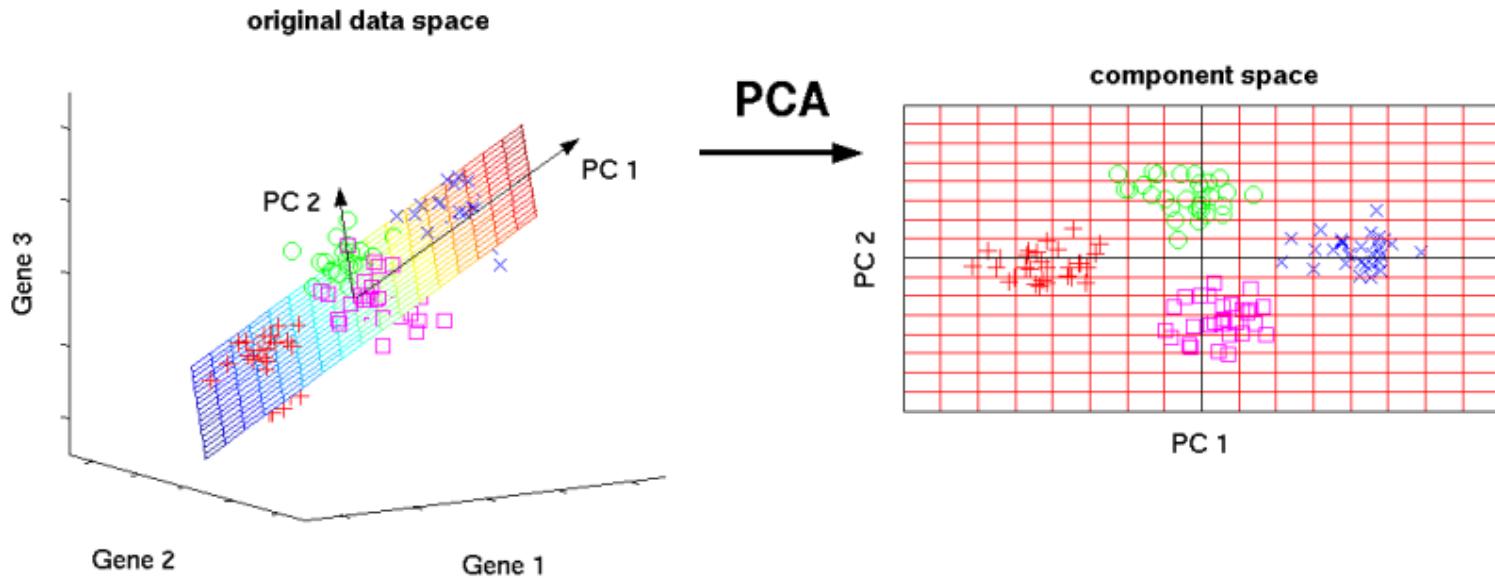
- Synchronization frequency of EREs in distant regions
- The frequency of synchronization decreases as the distance increases
- But increases again at the 2500 km boundary.
- Teleconnection phenomenon that occurs starting at 2500 km

Sea-surface dataset

Dataset



- Observe climate phenomena occurring in the ocean through sea surface temperature data
- Data source: National Oceanic and Atmospheric Administration (NOAA).
- Temperature measurement data at monthly intervals (89x180) (1854-present).
- Cross-verified data based on various data accumulated through buoys, ships, etc.



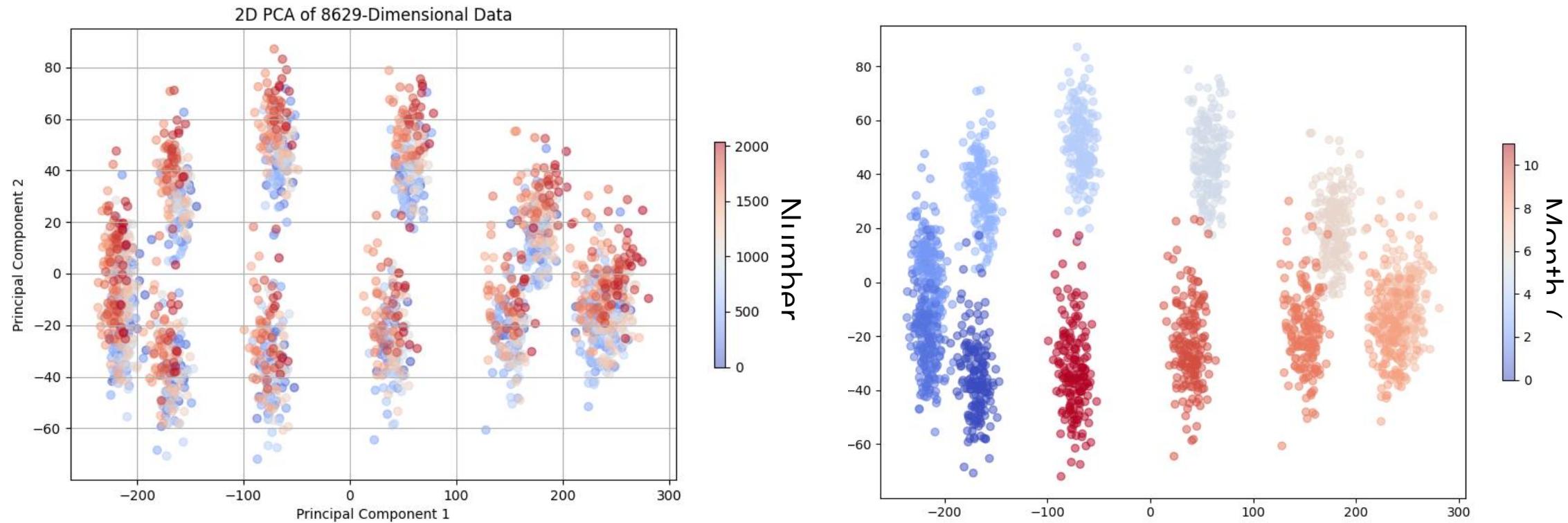
T temperature data for N locations
→ T points in N dimensions

Projection onto the plane where N-dimensional points are best distinguished

- PCA analysis: Observe the distribution of temperature data for each location at each time
- Projection onto the top two principal axes

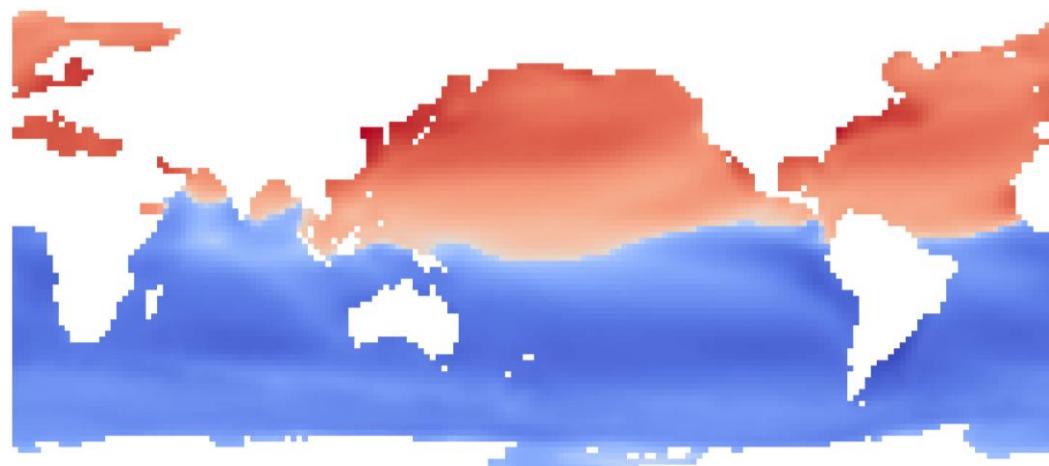
Raw data analysis

Result

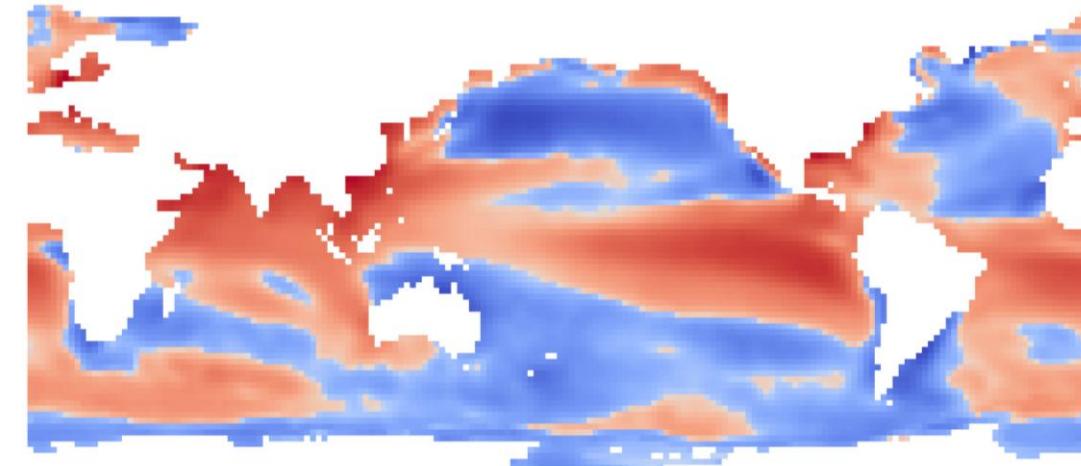


- Distribution on two principal axes obtained by PCA on raw data
- It is divided into 12 chunks representing each month.
- As time passes, the component of the second axis increases → Global warming?

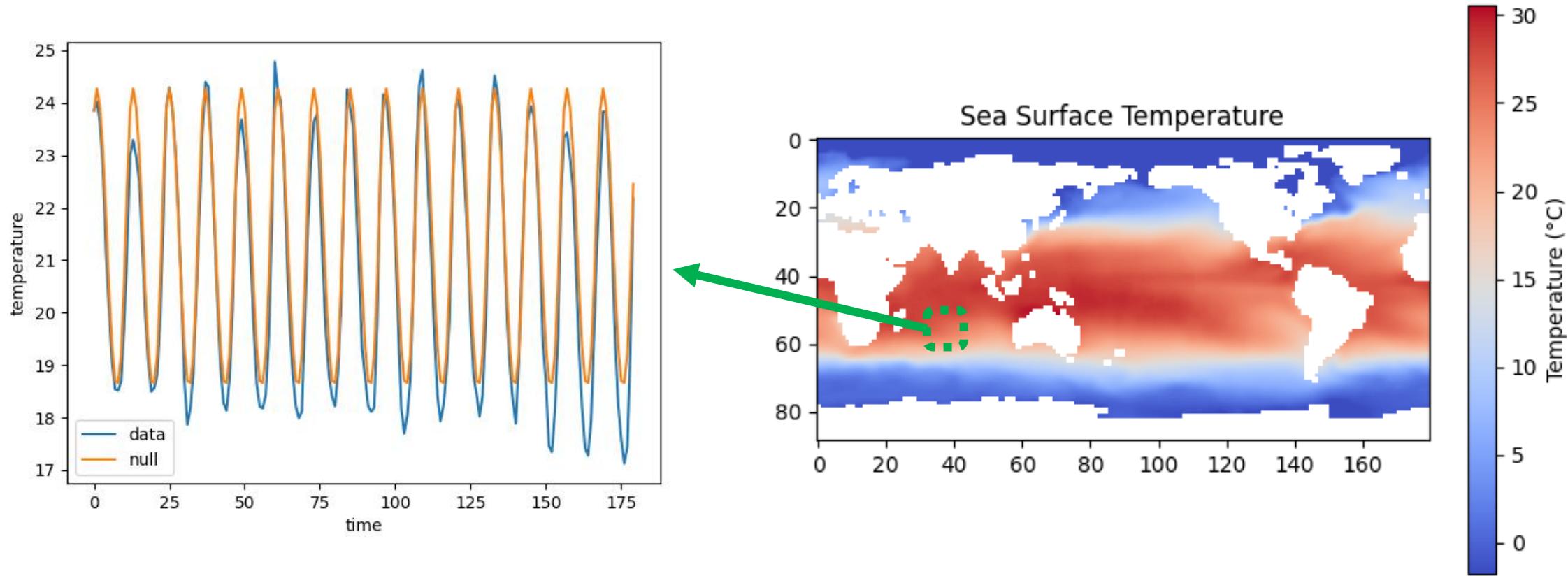
1st axis



2nd axis



- Top two principal component vectors from PCA analysis
- First vector: Temperature patterns that help distinguish between seasons (variance contribution 0.83)
- Second vector: Clusters of temperature change (0.03)



- Eliminates macro trends with monthly averages over the entire period for each location
- Use the difference between the current data and monthly trend over the entire measurement period.
- Focuses on the propagation of fluctuations at each location relative to the overall climate change pattern.

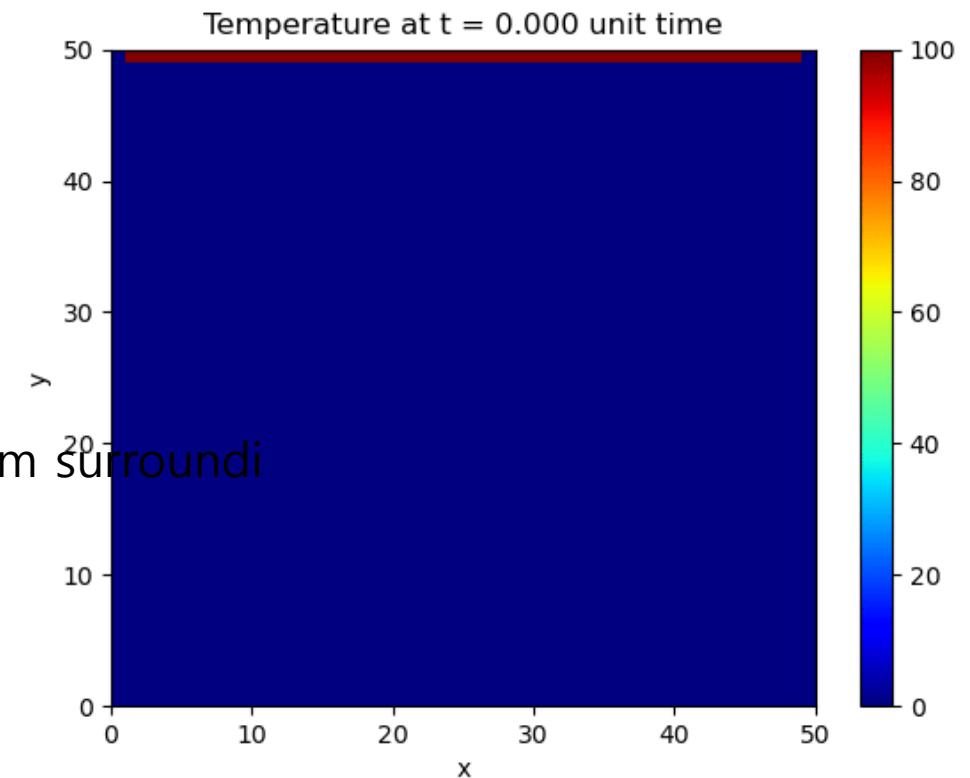
Heat equation

$$\frac{dT}{dt} = D \nabla^2 T$$

therm
al con
ductivi
ty

Temperature difference from surroun
ding area

The temperature in
your area changes



- Approach the relationship between sea surface temperature changes using the heat equation
- The temperature of each point changes depending on the temperature difference from surrounding points.

Heat equation

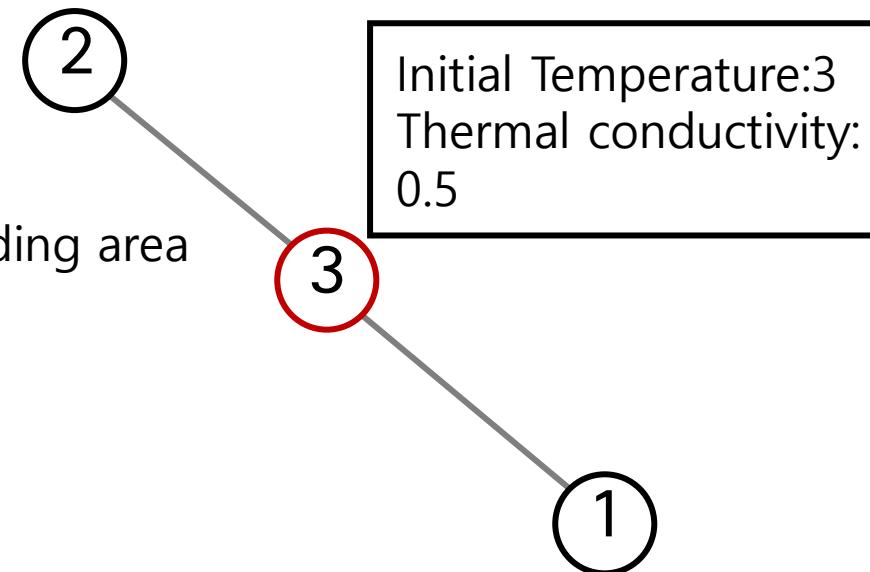
$$\frac{dT}{dt} = D \nabla^2 T$$

The temperature change of target point

Temperature difference from surrounding area

thermal conductivity

Ex) Temperature changes in the network



- Application of heat equation to network structure
- The center follows the temperature of surrounding nodes.

Heat equation

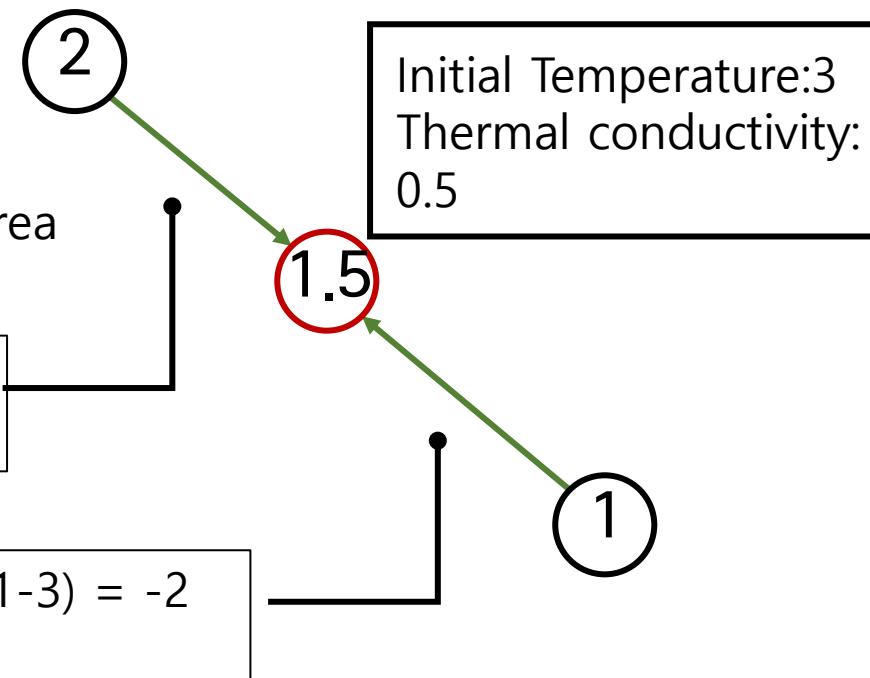
$$\frac{dT}{dt} = D \nabla^2 T$$

thermal conductivity

Temperature difference from surrounding area

The temperature change of target point

Ex) Temperature changes in the network



- Application of heat equation to network structure
- The center follows the temperature of surrounding nodes.
- Total temperature change: -1.5
- The temperature difference is reflected as much as the thermal conductivity of the target node.

Heat equation

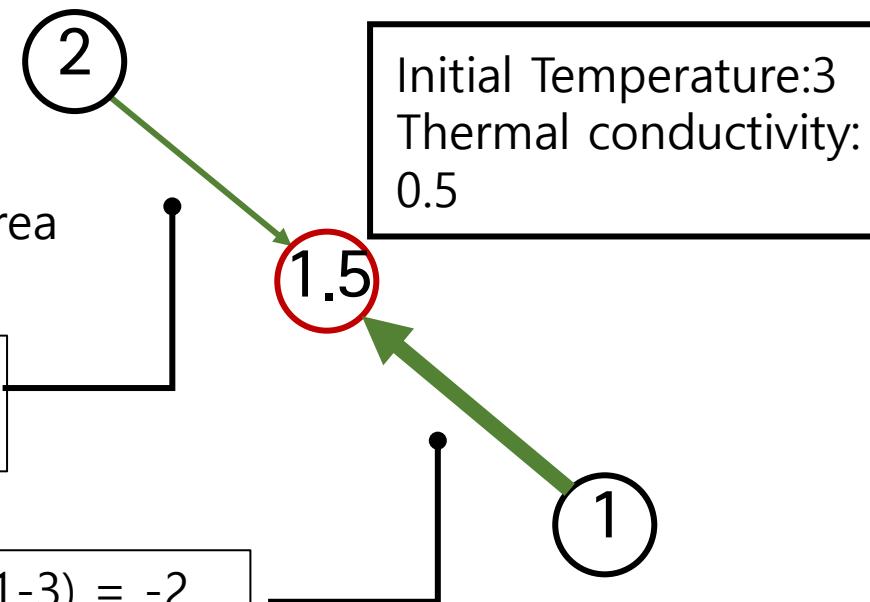
$$\frac{dT}{dt} = D \nabla^2 T$$

thermal conductivity

Temperature difference from surrounding area

The temperature change of target point

Ex) Temperature changes in the network



- However, in sea surface temperature, the conductivity may vary depending on the direction
- Introducing a general heat equation that relaxes symmetry

Heat equation

$$\frac{dT}{dt} = D \nabla^2 T$$

thermal conductivity

The temperature change of target point

Temperature difference from surrounding area



Generalized heat equation

$$T_i(t + \tau) - T_i(t) = \sum_j W_{ij} T_j$$

Generalized interaction matrix
(influence of position j on i)

Temperature at location j at time t

- 불연속적인 데이터에 대한 일반화 열방정식
- 행렬 W_{ij} 는 위치 j와의 온도차가 i의 온도에 미치는 영향을 의미
- 목표: 해수면의 온도 데이터 $T(t)$ 를 입력값으로 이용해 이를 잘 설명하는 W_{ij} 를 탐색

Generalized heat equation

$$E_i = \left(T_i(t + \tau) - T_i(t) - \sum_j W_{ij} T_j \right)^2$$

The diagram shows the error function E_i as the square of the difference between two terms. The first term is highlighted in orange and represents the 'actual temperature change'. The second term is highlighted in light blue and represents the 'predicted value'.

$$T_i(t + \tau) - T_i(t) = \sum_j W_{ij} T_j$$

The diagram shows the generalized heat equation. The right side of the equation, $\sum_j W_{ij} T_j$, is highlighted in light blue and represents the 'Generalized interaction matrix (influence of position j on i)'.

$$W_{ij}(n + 1) = W_{ij}(n) - \frac{dE}{dW_{ij}(n)}$$

The diagram shows the update rule for the weight matrix. The term $dE/dW_{ij}(n)$ is highlighted in light blue and represents the 'Temperature at location j at time t'.

- Take the square of the difference between both sides as the error function
- Searching for W that minimizes this error function.
- Initialize and update the W matrix appropriately to minimize the error.
- Allows correlation between all locations, even if they are not close

$$E_i = \left(T_i(t + \tau) - T_i(t) - \sum_j W_{ij} T_j \right)^2$$

Update W_{ij} such that E decreases

$$W_{ij}(n+1) = W_{ij}(n) - \frac{dE_i}{dW_{ij}(n)}$$

$$= W_{ij}(n) - \left(\frac{\partial E_i}{\partial W_{ij}} + \frac{\partial W_{ii}}{\partial W_{ij}} \frac{\partial E_i}{\partial W_{ii}} \right)$$

$$= W_{ij}(n) - 2\sqrt{E_i} (T_i - T_j)$$

$$\frac{dT_i}{dt} = \sum_j W_{ij} T_j$$

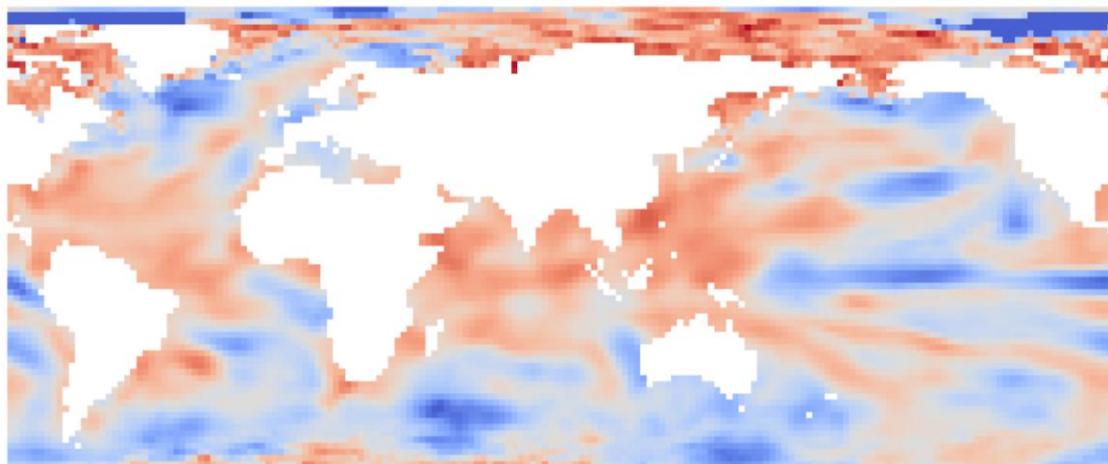
If all $T_j = T$,

$$0 = \sum_j W_{ij} T$$

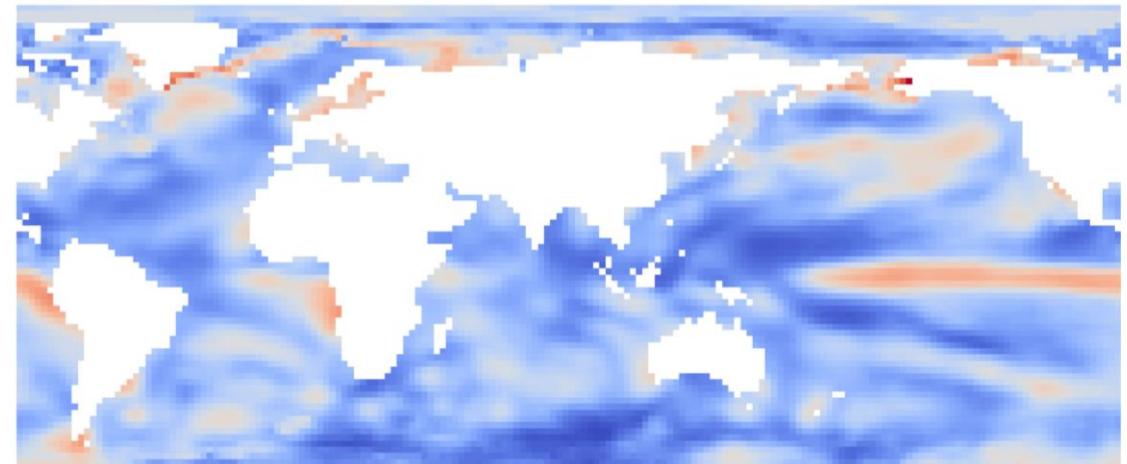
Secondary change ($W_{ij} \rightarrow W_{ii} \rightarrow E$)

- Take the square of the difference between both sides as the error function
- Searching for W that minimizes this error function.
- Initialize and update the W matrix appropriately to minimize the error.
- Allows correlation between all locations, even if they are not close

$$S_i^{\text{in}} = \sum_j W_{ij} = \text{total inflow}$$



$$S_i^{\text{out}} = \sum_j W_{ji} = \text{total outflow}$$

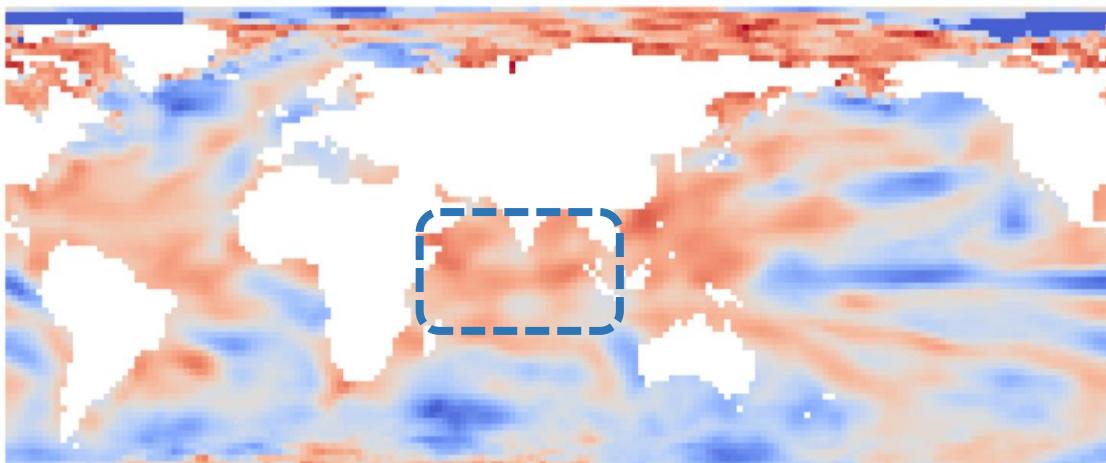


- Influence of each region achieved through optimization
- Left: Total influence (sensitivity) from temperatures in other regions
- Right: Total influence on temperature of different regions

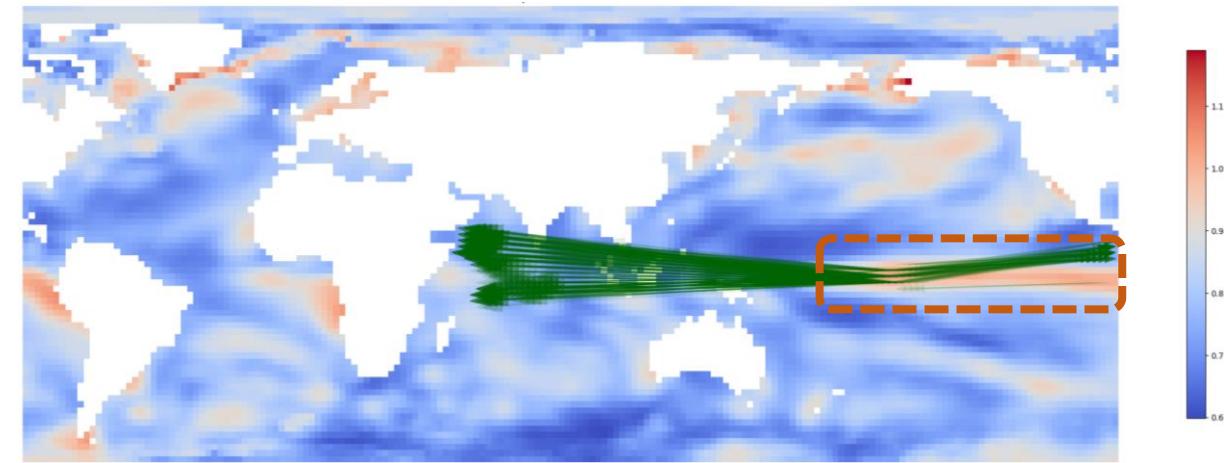
Flow analysis

Result

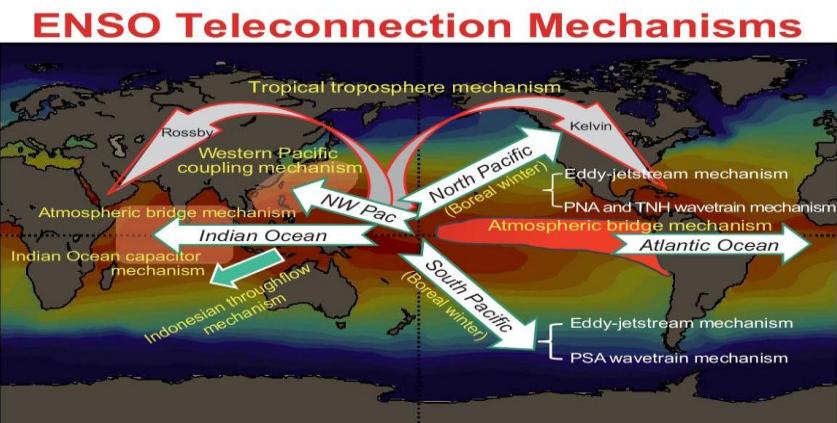
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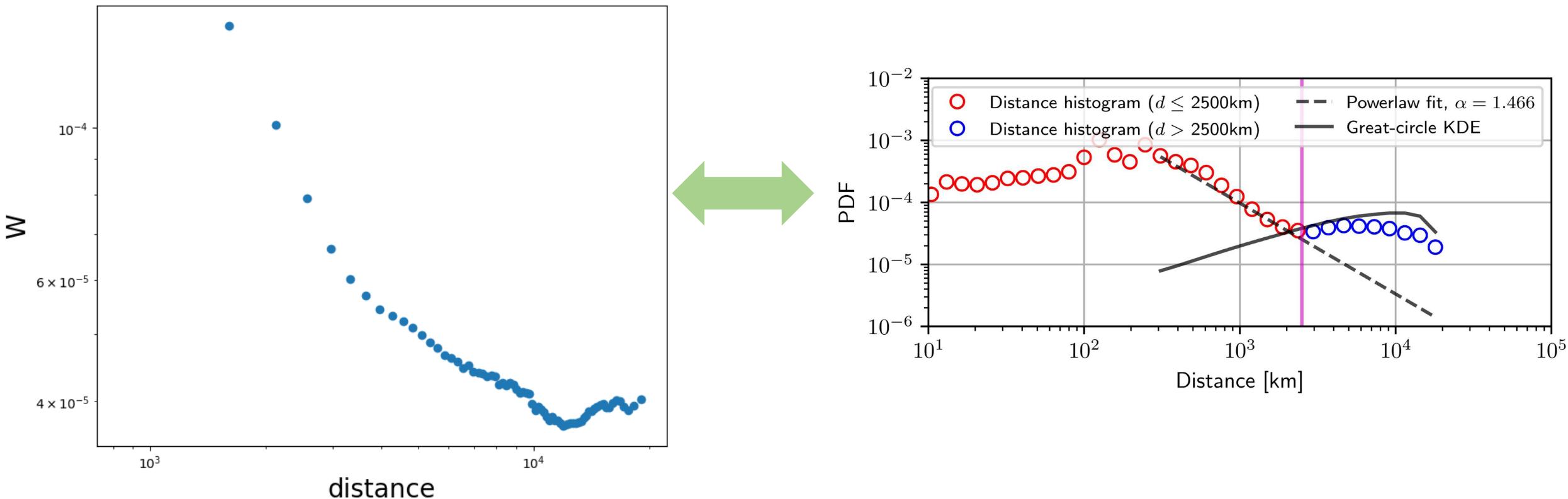


$$S_i^{\text{out}} = \sum_j W_{ji} = \text{total outflow}$$

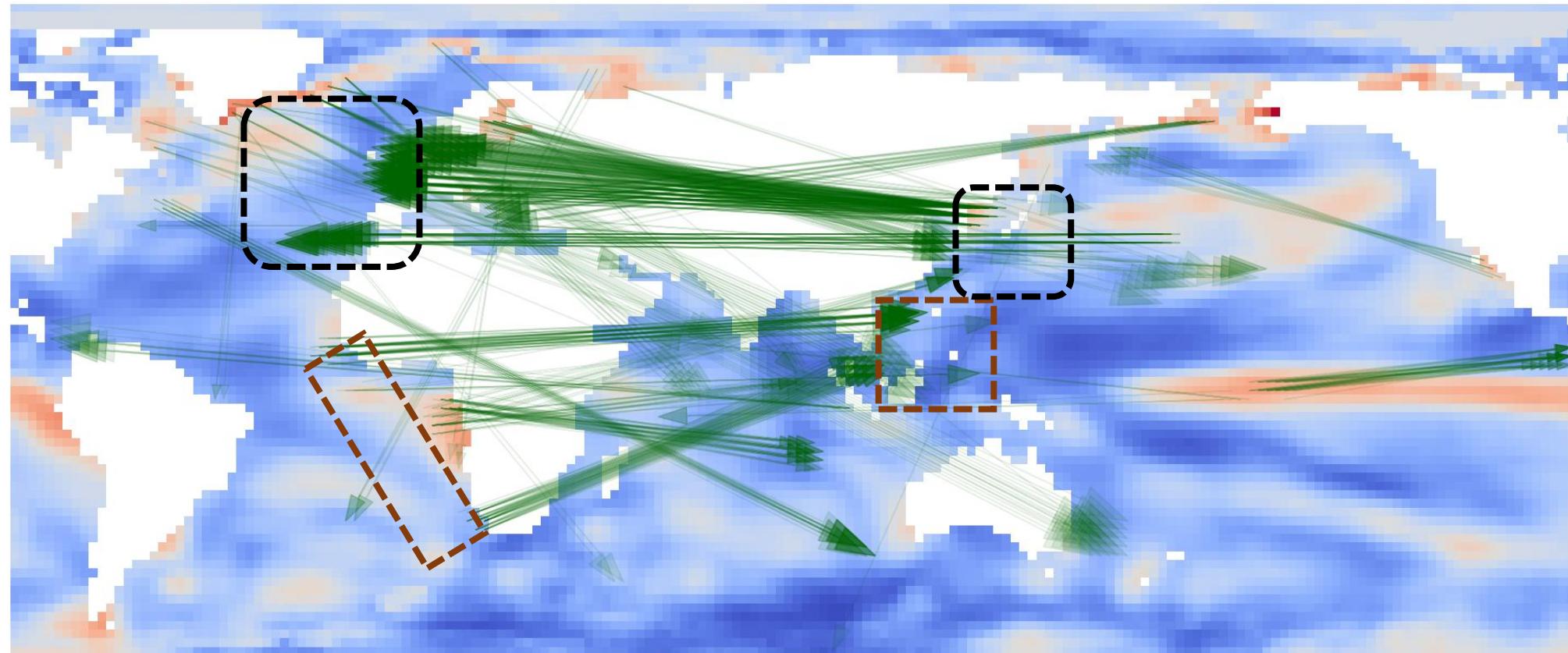


- Influence of each region achieved through optimization
- Left: Total influence (sensitivity) from temperatures in other regions
- Right: Total influence on temperature of different regions
- Similar to the ENSO pattern found in existing climate-related studies





- Change of W as a function of distance
- It changes slightly from around 4,000km and rebounds above 10,000km.
- Consistent with other researches on teleconnection



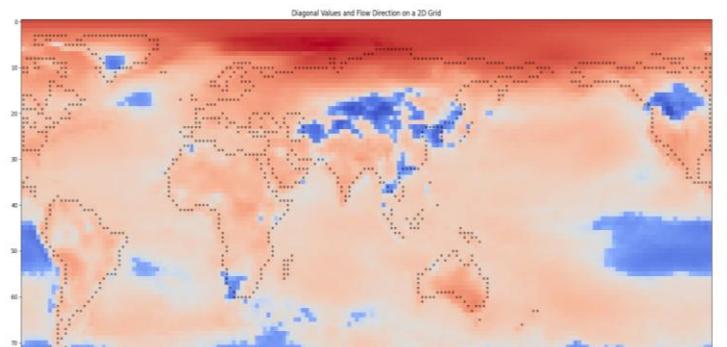
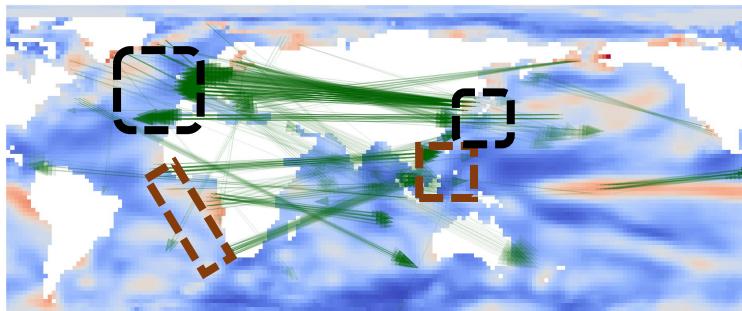
- Top 500 of all connections over 7000km
- Macro flows: West coast of Africa → Southeast Asia, Northeast Asia → Western Europe
- Need for cross-validation with existing context on ocean current circulation

Summary

- Teleconnection observation and analysis using sea surface temperature data
- Extract macroscopic patterns from sea level data through PCA analysis
- Analyzing correlations through generalized heat equations
- Building a network of influence through time series data of temperature
- Observe teleconnection patterns over distance
- Observation of climate correlations through analysis of influence networks

Future Works

- Climate correlation analysis at various time scales (>1 year)
- Applying analytical methodologies to air temperature data
- Comparison and integration of climate phenomena from atmospheric and ocean temperature
- Apply other methodologies such as percolation and eigenvector analysis



This study was conducted with support from the LAMP project of the National Research Foundation of Korea.