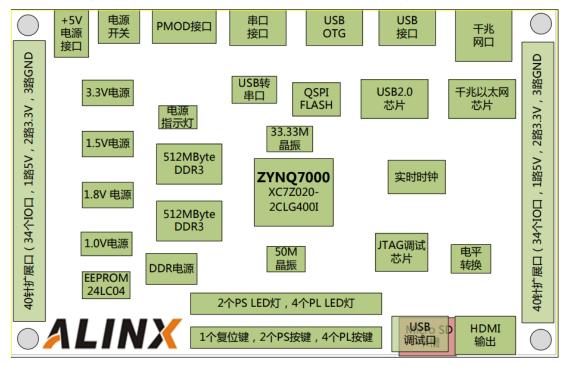
MSD 加法与电子加法计 算时间对比实验



1 实验用具

针对此次试验我们采用 Alinx7020,此款开发板使用的是 Xilinx 公司的 Zynq7000 系列的芯片,型号为 XC7Z020-2CLG400I, 400 个引脚的 FBGA 封装。ZYNQ7000 芯片可分成处理器系统部分 Processor System (PS) 和可编程逻辑部分 Programmable Logic (PL)。在 AX7020 开发板上,ZYNQ7000 的 PS部分和 PL 部分都搭载了丰富的外部接口和设备,方便用户的使用和功能验证。另外开发板上 集成了 Xilinx USB Cable 下载器电路,用户只要用一个 USB 线就可以对开发板进行下载和调 试。图 1 为整个 AX7020 整个系统的结构示意图:



通过这个示意图,我们可以看到,我们这个开发平台所能含有的接口和功能。下面是实物展示:



实验目的

针对两种电子加法器的性能测试以及对比,我们将使用 XC7Z020-2CLG400I型 FPGA 开发板上的资源。首先,我们会利用该板上的双核 ARM Cortex-A9 中的传统加法器,该加法器为 32 位,代表第一种加法器。接着,我们将利用可编程逻辑单元阵列(PL)在同一开发板上构建多个 33 位的最高有效位(MSD)加法器,以代表第二种加法器。

在测试过程中,我们将记录并比较两种加法器的计算用时。对于第一种加法器,我们将测试其处理一个 32 位数据的加法所需的时间。而对于第二种加法器,我们会测试其处理多个 33 位数据的加法所需的时间,并且注意到由于其并行处理的特性,其计算时间可能会显著减少。

通过这些测试,我们将能够直观地评估两种加法器的性能优劣,进而了解到是否值得投资于构建更复杂但性能更优异的 MSD 加法器。

期望的实验结果: 第2种加法器的工作用时短。即: 第2种加法器快。

实验准备

1. **时间计算**:在 Xilinx 提供的库中,xtime_l.h 是与时间管理相关的一个头文件,用于处理时间和延时功能。XTime_GetTime(XTime Xtime) 获取当前时间,结果存储在 Xtime 中。通过计算时间差再乘以时钟周期获取到准确时间。Alinx 的频率为 50Mhz 对应时钟周期是 20ns。

```
XTime_GetTime(&tbegin);
for(int i=0;i<60;i++){
    MSD_33_mWriteReg(deviceAddresses[i], k_reg[0], reg_a[i][0]);
    MSD_33_mWriteReg(deviceAddresses[i], k_reg[1], reg_a[i][1]);
    MSD_33_mWriteReg(deviceAddresses[i], k_reg[2], reg_a[i][2]);
    MSD_33_mWriteReg(deviceAddresses[i], k_reg[3], reg_b[i][0]);
    MSD_33_mWriteReg(deviceAddresses[i], k_reg[4], reg_b[i][1]);
    MSD_33_mWriteReg(deviceAddresses[i], k_reg[5], reg_b[i][2]);
    decresult[i][0] = MSD_33_mReadReg(deviceAddresses[i], k_reg[6]);
    decresult[i][1] = MSD_33_mReadReg(deviceAddresses[i], k_reg[7]);
    decresult[i][2] = MSD_33_mReadReg(deviceAddresses[i], k_reg[8]);
}
XTime_GetTime(&tEnd);
tused = ((tEnd-tbegin)*1000000)/(COUNTS_PER_SECOND);</pre>
```

2. **MSD 加法器并行原理**:在可编程逻辑 (PL)端,我们采用信号机制来协调多个运算单元的操作。具体来说,当 60 个多位数数字 (MSD)加法器完成填充操作后,系统会通过一个同步信号触发所有加法器并行开始计算。这

种方式确保了所有加法器同时进行运算,提高了整体计算效率。最终,所有加法器的计算结果会统一返回,确保数据处理的一致性和同步性。

实验策略

- 1. 利用第二种加法器的"可重构出任意大小加法器"的特性,我们构建了一个33位的最高有效位(MSD)加法器。这样,我们可以直接对33位数据进行加法运算,而第一种加法器则需要两次计算才能完成一个加法运算:首先计算低32位,然后计算高32位(尽管实验数据中仅有一位)。相比之下,第二种加法器只需一次计算就能完成33位数据的加法。
- 2. 利用第二种加法器的"可重构出多个加法器"的优势,我们构建了 60 个 33 位的 MSD 加法器,并使它们能够并行工作。这意味着我们可以一次性 计算 60 个 33 位数的加法,而第一种加法器则只能逐个计算 33 位数的加法(每次加法还需要两次计算)

实验过程

第一步: 数据准备。我们将 60 对原始数据送入内存。数据范围是 2^32-2^33, 范围从 4294967295 到 8589934591

data_a= [

6163550658, 6413109763, 4493162740, 4459676060, 6148214032, 5439006107, 4433876780, 5861763895, 5221972308, 4935524470, 5389687797, 4354296534, 4790236573, 6306732821, 5654945182, 6069373681, 4870013515, 6180308189, 6221500578, 6329734393, 5090246305, 5522595258, 5387336040, 4360315825, 5515023509, 5973410702, 5784501258, 5232857401, 6019818661, 4846029805, 5046807674, 6106273973, 4637160715, 5392211615, 5555725575, 5791996815, 5837229290, 5778789187, 5203953563, 4309582241, 6168520261, 5470611017, 4386111010, 6026674767, 5689423199, 4785091805, 4964832056, 5654890046, 4737018386, 5437568557.

```
6000280530, 6126097812, 5537764560, 6096738408, 5350641731, 5545828808, 6339368421, 6375512686, 6240230742, 5127674579] data_b= [

5670367407, 5412345023, 5914847405, 6128327586, 4587896338, 5026686114, 4935222256, 4760041748, 4614409077, 4377978840, 5175819138, 5634001496, 5947783309, 4908543247, 5960452096, 5591331536, 4727949047, 5955264796, 5970133931, 6321056983, 6073297128, 4455663635, 4521584003, 6273163952, 5632439975, 6265859821, 6278962862, 5399591672, 6238104244, 6005097228, 5727386570, 6035573062, 4814809633, 5901575191, 4373607691, 4403649190, 6153957194, 6109318345, 4673901860, 4906714130, 4635253234, 5761701894, 6103554071, 5135616837, 4835360414, 5610035924, 5553855281, 5663039910, 4390156807, 6134636813, 4409012067, 5272496534, 5612425667, 4960474159, 4752740764, 5935161763, 6080424745, 5902262331, 4863341116, 5603599112]
```

第二步:加法运算。在第一种加法器上,需要重复执行 60 次加法指令。而在第二种加法器上,由于其并行处理能力,我们只需重复执行 1 次加法指令(运算),每次同时计算 60 对位数据。

1. 第一种加法器:

```
for (int i = 0; i < NUM_BINARIES; i++)
{
     binary_add(bin_nums_a, bin_nums_b, bin_result, i);
}</pre>
```

2. 第二种加法器:

```
MSD_33_mWriteReg(deviceAddresses[i], k_reg[0], reg_a[i][0]);
MSD_33_mWriteReg(deviceAddresses[i], k_reg[1], reg_a[i][1]);
MSD_33_mWriteReg(deviceAddresses[i], k_reg[2], reg_a[i][2]);
MSD_33_mWriteReg(deviceAddresses[i], k_reg[3], reg_b[i][0]);
MSD_33_mWriteReg(deviceAddresses[i], k_reg[4], reg_b[i][1]);
MSD_33_mWriteReg(deviceAddresses[i], k_reg[5], reg_b[i][2]);
decresult[i][0] = MSD_33_mReadReg(deviceAddresses[i],
k_reg[6]);
```

```
decresult[i][1] = MSD_33_mReadReg(deviceAddresses[i],
k_reg[7]);
decresult[i][2] = MSD_33_mReadReg(deviceAddresses[i],
k_reg[8]);
```

第三步:显示运算结果。第二步的运算结果会先存储在内存中。当 60 个数据计算完毕后,再执行第三步。屏幕将显示如下信息:

第一种加法器实验结果:

```
6163550658 + 5670367407 = 11833918065
4493162740 + 5914847405 = 10408010145
4493162740 + 5914847405 = 10408010145
4439162740 + 5914847405 = 10408010145
4439676060 + 6128327586 = 10588003646
6148214032 + 4587896338 = 10736110370
5439061007 + 502668611 = 10465692221
4433876780 + 4935222256 = 9369099036
558161638595 + 4760041748 = 10621805643
5221972308 + 4614409077 = 9936381385
439524747 + 4377798404 = 938828030
4790236573 + 5947783309 = 10738019882
6306732821 + 4908543247 = 11215276068
6564945182 + 5960452096 = 11615397279
609937681 + 5591331536 = 11660705217
4870013515 + 4727949047 = 9597962562
6180308189 + 5955264796 = 12135572985
6221500578 + 5970133931 = 12191634509
6329734393 + 6321056983 = 12650791376
5090246305 + 6073297128 = 11163543433
5522595258 + 4455663635 = 9978258893
538733604 + 4521584003 = 9908920043
360315825 + 6278669355 = 10483497777
5515023509 + 5632439975 = 11147463484
5973410702 + 6265859821 = 12239270523
5784501258 + 6278669262 = 12063464120
5232857401 + 53965172 = 10632449073
6019818661 + 6238104244 = 12257922905
619818661 + 6238104244 = 12257922905
648607674 + 5727366570 = 10774194244
6437160715 + 4814809633 = 9451970348
5592211615 + 5901575191 = 11293766806
5555725575 + 373607691 = 992933366
5555725575 + 373607691 = 992933366
5555725575 + 373607691 = 992933366
5568942319 + 483560414 = 10524783613
378508044 + 4030580414 = 10524783613
378508049 + 483580414 = 10524783613
378508049 + 483580414 = 10524783613
378508049 + 483580414 = 10524783613
378508047319 + 483580414 = 10524783613
378508047319 + 483580414 = 10524783613
37850804731 + 43696507 = 121775193
55054647731 + 4752740764 = 10103362495
5537764560 + 5612425667 = 1116190227
5505641731 + 4752740764 = 10103362495
5537764560 + 5612425667 = 11615397188
5127674579 + 5603599112 = 10731273691
600280530 + 4480312067 = 10409292597
5505641731 + 4752740764 = 10103362495
5547666667
```

第二种加法器:

```
PuTTY
                                                                                              X
5090246305 + 6073297128 = 11163543433
                                                    5522595258 + 4455663635 = 9978258893
5387336040 + 4521584003 = 9908920043
                                                   4360315825 + 6273163952 = 10633479777
5515023509 + 5632439975 = 11147463484

5784501258 + 6278962862 = 12063464120

6019818661 + 6238104244 = 12257922905

5046807674 + 5727386570 = 10774194244
                                                    5973410702 + 6265859821 = 12239270523
                                                   5232857401 + 5399591672 = 10632449073
4846029805 + 6005097228 = 10851127033
6106273973 + 6035573062 = 12141847035
                                                  5392211615 + 5901575191 = 11293786806
4637160715 + 4814809633 = 9451970348
                                                  5791996815 + 4403649190 = 10195646005
                                                   5778789187 + 6109318345 = 11888107532
5837229290 + 6153957194 = 11991186484
                                                   4309582241 + 4906714130 = 9216296371
5203953563 + 4673901860 = 9877855423
4386111010 + 6103554071 = 10489665081
                                                    6026674767 +
                                                                    5135616837 = 11162291604
5689423199 + 4835360414 = 10524783613
4964832056 + 5553855281 = 10518687337
                                                   4785091805 + 5610035924 = 10395127729
5654890046 + 5663039910 = 11317929956
                                                  5437568557 + 6134636813 = 11572205370
                                                   6126097812 + 5272496534 = 11398594346
6096738408 + 4960474159 = 11057212567
6000280530 + 4409012067 = 10409292597
5537764560 + 5612425667 = 11150190227
                                                    5545828808 +
6339368421 + 6080424745 = 12419793166
                                                                    5902262331 = 12277775017
6240230742 + 4863341116 = 11103571858
                                                    5127674579
                                                                    5603599112 = 10731273691
60 msd additions ,time elapsed is 119 us
average time per msd addition is 1.983333
```

数据对比见 MSD 数据对比.xlsx

附录

MSD 加法代码

```
#include "stdio.h"
#include "stdlib.h"
#include "string.h"
#include "xparameters.h"
#include "msd 33.h"
#include "xil_io.h"
#include "sleep.h"
#include "stdlib.h"
#include "stdint.h"
#include "math.h"
#include "xtime 1.h"
#define max(a, b) ((a) > (b) ? (a) : (b))
#define START_ADDRESS 0x43c00000
#define END_ADDRESS 0x43FB0000
#define STEP_SIZE 0x10000 // 假设步长为 0x10000
#define ROWS 60
#define COLS 3
#define ARRAY SIZE 60
long long* generate_random_array(long long* array, int size, int
random seed) {
   long lower_bound = (1LL << 32) - 1; // 2^32 - 1</pre>
   long long upper bound = (1LL << 33) - 1; // 2^33 - 1
   srand(random_seed);
   // 生成随机数并存储在数组中
   for (int i = 0; i < size; ++i) {</pre>
       array[i] = ((long long)rand() % (upper_bound - lower_bound + 1)) +
lower_bound;
   }
   return array;
void decToBin(long long dec, int bin[])
   if (dec < 0)
   {
```

```
dec *= -1;
       bin[0] = 1; // 0代表正, 1代表负
   }
   else
   {
       bin[0] = 0;
   long long num = dec;
   int temp[99];
   int i;
   for (i = 0; num != 0; i++)
       temp[i] = num % 2; // 使用 % 运算符计算余数
       num /= 2;
   }
   for (int j = 1, index = i - 1; j <= i; j++, index--)</pre>
       bin[j] = temp[index];
   bin[i + 1] = -2; // 结束标志
}
void binToMsd(int bin[], int msd[])
   int index_msd = 0;
   if (bin[0] == 1)
       for (int index_bin = 1; bin[index_bin] != -2; index_bin++,
index_msd++)
       {
          msd[index_msd] = 0;
           if (bin[index_bin] == 1)
              msd[index_msd] = -1;
       }
       msd[index_msd] = -2; // 结束标志
   }
   else
   {
       for (int index_bin = 1; bin[index_bin] != -2; index_bin++,
index_msd++)
       {
          msd[index_msd] = bin[index_bin];
```

```
msd[index_msd] = -2; // 结束标志
   }
}
int bin_to_dec(char bin[], int len)
{
   int result = 0, base = 1;
   for (int i = len - 1; i >= 0; i--, base = base * 2)
       result = result + (bin[i] - '0') * base;
   return result;
}
long long msdToDec(int msd[])
   long long result = 0;
   int len = 0;
   for (; msd[len] != -2; len++)
   for (int i = 0, j = len - 1; i < len; i++, j--)</pre>
       long long t = 1;
       for (int k = 0; k < j; k++)
           t *= 2;
       result += msd[i] * t;
   return result;
}
void convertToBinaryString(int *msd, char *result)
{
   int i = 0;
   while (msd[i] != -2)
       if (msd[i] == 0)
       {
           strcat(result, "00");
       else if (msd[i] == 1)
```

```
strcat(result, "01");
       }
       else if (msd[i] == -1)
           strcat(result, "10");
       i++;
   }
}
void binaryStringToMSD(char *binaryString, int *intArray, int length)
   for (int i = 0; i < length; i++)</pre>
   {
       char tmp[3];
       strncpy(tmp, binaryString + i * 2, 2);
       tmp[2] = ' \ 0';
       if (strcmp(tmp, "00") == 0)
           intArray[i] = 0;
       else if (strcmp(tmp, "01") == 0)
           intArray[i] = 1;
       else if (strcmp(tmp, "10") == 0)
           intArray[i] = -1;
       }
       // Add more conditions as needed
   }
}
void cdecToBin(unsigned value, int bits, char *binaryArray)
{
   for (int i = bits - 1; i >= 0; i--)
       binaryArray[bits - 1 - i] = ((value >> i) & 1) + '0';
   binaryArray[bits] = '\0'; // 添加 null 终止符
}
```

```
void write_reg(unsigned int array[][3], long long value,int row) {
   int bin[36];
   int msd[36];
   decToBin(value, bin);
   binToMsd(bin, msd);
   char z[67] = "";
   convertToBinaryString(msd, z);
   int len_z = strlen(z);
   if (len_z <= 32)
   {
       array[row][0] = bin_to_dec(z, len_z);
   }
   else if (len_z > 32 && len_z <= 64)</pre>
   {
       array[row][0] = bin_to_dec(z + len_z - 32, 32);
       array[row][1] = bin_to_dec(z, len_z - 32);
   }
   else if (len_z > 64 && len_z <= 96)</pre>
       array[row][0] = bin_to_dec(z + len_z - 32, 32);
       array[row][1] = bin_to_dec(z + len_z - 64, 32);
       array[row][2] = bin_to_dec(z, len_z - 64);
   }
}
void printUnsignedArray(unsigned int array[][3], int rows, int cols) {
   for (int i = 0; i < rows; ++i) {</pre>
       for (int j = 0; j < cols; ++j) {</pre>
           printf("%u ", array[i][j]);
       printf("\n");
   }
}
void regToDec(unsigned int decresult[][3],long long * ansDec,int index){
   char ans_c[70] = "";
   cdecToBin(decresult[index][2], 6, ans_c);
   cdecToBin(decresult[index][1], 32, ans_c + 6);
   cdecToBin(decresult[index][0], 32, ans_c + 38);
   int msd_c[40];
   int length = strlen(ans_c) / 2; // Assuming the length is even
   binaryStringToMSD(ans_c, msd_c, length);
   msd_c[length] = -2;
```

```
ansDec[index] = msdToDec(msd_c);
}
void printLongLongArray(long long array[], int length) {
   for (int i = 0; i < length; ++i) {</pre>
       printf("%11d ", array[i]);
   }
   printf("\n");
}
int main() {
   long long array_a[ARRAY_SIZE];
   long long array_b[ARRAY_SIZE];
   int arrayLength = (END_ADDRESS - START_ADDRESS) / STEP_SIZE + 1;
   int deviceAddresses[arrayLength];
   int currentAddress = START ADDRESS;
   for (int i = 0; i < arrayLength; ++i) {</pre>
       deviceAddresses[i] = currentAddress;
       currentAddress += STEP_SIZE;
   XTime tEnd, tbegin;
   u32 tused;
   long long* data a = generate random array(array a, ARRAY SIZE,123);
   long long* data_b = generate_random_array(array_b, ARRAY_SIZE,456);
   unsigned int reg_a[ROWS][COLS] = { {0} };
   unsigned int reg_b[ROWS][COLS] = { {0} };
   for(int i=0;i<ROWS;i++){</pre>
   write_reg(reg_a,data_a[i],i);
   write_reg(reg_b,data_b[i],i);
   }
   int k_reg[9]={0};
   unsigned int decresult[ROWS][COLS] = { {0} };
   for (int k = 0; k < 9; k++)
       k_reg[k] = k * 4;
   }
   XTime_GetTime(&tbegin);
   for(int i=0;i<60;i++){</pre>
       MSD_33_mWriteReg(deviceAddresses[i], k_reg[0], reg_a[i][0]);
       MSD_33_mWriteReg(deviceAddresses[i], k_reg[1], reg_a[i][1]);
       MSD_33_mWriteReg(deviceAddresses[i], k_reg[2], reg_a[i][2]);
```

```
MSD_33_mWriteReg(deviceAddresses[i], k_reg[3], reg_b[i][0]);
       MSD 33 mWriteReg(deviceAddresses[i], k reg[4], reg b[i][1]);
       MSD_33_mWriteReg(deviceAddresses[i], k_reg[5], reg_b[i][2]);
       decresult[i][0] = MSD_33_mReadReg(deviceAddresses[i], k_reg[6]);
       decresult[i][1] = MSD_33_mReadReg(deviceAddresses[i], k_reg[7]);
       decresult[i][2] = MSD_33_mReadReg(deviceAddresses[i], k_reg[8]);
   XTime_GetTime(&tEnd);
   tused = ((tEnd-tbegin)*1000000)/(COUNTS_PER_SECOND);
   long long ansDec[ROWS] = {0};
   for(int i=0;i<ROWS;i++){</pre>
       regToDec(decresult,ansDec,i);
   }
   for(int i=0;i<60;i++){</pre>
       if((i+1)%2==0){
           printf("\n");
       }
   xil_printf("%d msd additions ,time elapsed is %d us\r\n",ROWS,tused);
   float tused_float = (float)tused / 60.0;
   printf("average time per msd addition is %f\n", tused_float);
   return 0;
}
```

传统计算器加法

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
#include <math.h>
#include "xtime_l.h"

#define NUM_BINARIES 60
#define MAX_BIT_LENGTH 34

// 十进制转二进制 数组低位存二进制低位
void decimal_to_binary(long long decimal_num, int
binary_num[][MAX_BIT_LENGTH], int index)
{
```

```
for (int i = 0; i < MAX_BIT_LENGTH; i++)</pre>
       binary_num[index][i] = decimal_num % 2;
       decimal_num /= 2;
   }
}
void binary_to_decimal(int binary[][MAX_BIT_LENGTH], long long *result, int
index)
{
   long long decimal = 0;
   for (int i = 0; i < MAX_BIT_LENGTH; ++i)</pre>
   {
       long long binary_bit = binary[index][i]; // 获取当前位的二进制值
       if (binary_bit)
       {
           decimal += (1LL << i); // 将当前位的二进制值乘以对应的 2 的次方, 并
累加到十进制数中
       }
   }
   result[index] = decimal;
void binary_add(int binary1[][MAX_BIT_LENGTH], int
binary2[][MAX_BIT_LENGTH], int result_binary[][MAX_BIT_LENGTH], int index)
   int carry = 0;
   for (int i = 0; i < MAX_BIT_LENGTH; i++)</pre>
   {
       int sum = binary1[index][i] + binary2[index][i] + carry;
       result_binary[index][i] = sum % 2;
       carry = sum / 2;
   }
}
long long *generate_random_array(long long *array, int size, int
random_seed)
{
   long long lower_bound = (1LL << 32) - 1; // 2^32 - 1</pre>
   long long upper_bound = (1LL << 33) - 1; // 2^33 - 1</pre>
   srand(random_seed);
   // 生成随机数并存储在数组中
   for (int i = 0; i < size; ++i)</pre>
```

```
{
       array[i] = ((long long)rand() % (upper_bound - lower_bound + 1)) +
lower_bound;
   }
   return array;
}
void printArray(int array[][34], int rows, int cols)
   for (int i = 0; i < rows; ++i)</pre>
       for (int j = 0; j < cols; ++j)</pre>
       {
           printf("%d", array[i][j]);
       printf("\n");
   }
}
int main()
{
   long long array_a[NUM_BINARIES];
   long long array_b[NUM_BINARIES];
   int(*bin_nums_a)[MAX_BIT_LENGTH] = malloc(NUM_BINARIES *
sizeof(*bin_nums_a));
   int bin_nums_b[NUM_BINARIES][MAX_BIT_LENGTH]={{0}};
   int(*bin_result)[MAX_BIT_LENGTH] = malloc(NUM_BINARIES *
sizeof(*bin_result));
   XTime tEnd, tbegin;
   u32 tused;
   for (int i = 0; i < NUM_BINARIES; i++) {</pre>
       for (int j = 0; j < MAX_BIT_LENGTH; j++) {</pre>
           bin_nums_a[i][j] = 0;
           bin_nums_b[i][j] = 0;
           bin_result[i][j] = 0;
       }
   }
   long long dec_result[NUM_BINARIES]={0};
   // 生成60个随机的二进制数
   long long *data_a = generate_random_array(array_a, NUM_BINARIES, 123);
   long long *data_b = generate_random_array(array_b, NUM_BINARIES, 456);
```

```
for (int i = 0; i < NUM_BINARIES; i++)</pre>
   {
       decimal_to_binary(data_a[i], bin_nums_a, i);
       decimal_to_binary(data_b[i], bin_nums_b, i);
   }
   XTime_GetTime(&tbegin);
   for (int i = 0; i < NUM_BINARIES; i++)</pre>
   {
       binary_add(bin_nums_a, bin_nums_b, bin_result, i);
   XTime_GetTime(&tEnd);
   tused = ((tEnd-tbegin)*1000000)/(COUNTS_PER_SECOND);
   for (int i = 0; i < NUM_BINARIES; i++)</pre>
   {
       binary_to_decimal(bin_result, dec_result, i);
   }
   for (int i = 0; i < 60; i++)</pre>
       printf("%11d + %11d = %11d ", data_a[i], data_b[i],
dec_result[i]);
       if ((i + 1) \% 2 == 0)
           printf("\n");
       }
   }
   xil_printf("%d traditional additions ,time elapsed is %d
us\r\n",NUM_BINARIES,tused);
   float tused_float = (float)tused / 60.0;
   printf("average time per traditional addition is %f\n", tused_float);
   free(bin_nums_a);
   free(bin_result);
   return 0;
}
```