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Project Report

Network Based Modelling for the Spread of Scientific Ideas

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1 Abstract

Using simulations, we investigated the changes in networks with nodes that held different ‘scientific ideas’ and influenced each other through a complex contagion mechanism. This was divided into two parts: by varying the network structure and observing features of the distribution of ideas in networks, and by varying the starting idea distributions of the nodes and observing features of the network structures. The update step included a rewiring probability, a complex contagion threshold, and a probability of innovation (producing a new idea). We found that both structures and idea distributions influenced each other’s features. Values of the update parameter also played a role.

2 Individual contributions

This report represents a group effort by all members.

3 Introduction and Motivation

We live in a time in which aspects of our lives and of our world become more and more connected with each other. To understand one aspect, we must understand many other aspects, which all together form a large, complex system, or network. Globalization has changed the meaning of ‘distance’ and communication, allowing seemingly unrelated and unconnected individuals to share more than they ever could before. Fields of studies are overlapping with each other, creating new interdisciplinary domains and building a diverse playground for the sharing of ideas. But how do ideas spread? This question is especially interesting with the increase of technology that allows us to record and visualize the networks that connect individuals and ideas, and in particular the ability to ‘see’ how they change. This can lead to insight about why and when ideas spread and into the complexity of the matter. Research has shown that not only does the nature of information or innovation influence the diffusion of it, but also that the structure of a network influences the diffusion dynamics. Here, we try to simulate the spread of scientific ideas in different networks. The model presented is based on two studies: one that investigated critical parameter values for complex contagion and another that investigated critical values of a rewiring parameter.

3.1 Fundamental Questions

The main goals of this simulation study are to investigate how network structure influences the distribution of ideas, and how the distribution of ideas influences network structure. For a list of the terminology that will be used throughout the paper, please refer to Table 1. By varying three parameters - probability of rewiring, rate of innovation, and complex contagion threshold (ϕ , α , and δ respectively) - and using different network structures and idea distributions, we observed how network structure characteristics changed. Similarly, we observed how the distribution of ideas and the connections between them changed. Below we describe our questions more specifically.

Table 1: List of terminology

	Term
Neighborhood index	The fraction of the holders of the same idea who are neighbor as well averaged over all ideas.
Intra-idea distance	The average distance between holders of the same idea in the network.
Dominant frequency	The frequency of the dominant idea in the network at each time steps of the simulation.
Average dominance time	The average number of time steps in which the dominant idea keeps its dominance.
Novelty index	The fraction of newly generated ideas.
Average shortest path	The average number of steps along the shortest paths for all possible pairs of network nodes.
Clustering coefficient	A measure of degree to which nodes in a graph tend to cluster together.
Degree of connectivity	The number of edges incident to the vertex.
Connected component	A subgraph in which any two vertices are connected to each other by paths, and which is connected to no additional vertices in the supergraph.
Diameter of network	The longest of all the calculated shortest paths in a network.

3.1.1 Effects of Network Structure on Idea Distribution

Given a starting network and a random idea distribution, how do different network structures (see Section ??) affect the distance between nodes that have the same idea (intra-idea distance)? How do they affect the neighbourhood index? How do they change the emergence of dominant ideas and their time of dominance? How do their effects depend on the values of ϕ , α and δ ?

More rigid network structures (those with less ‘randomness’, such as the caveman and the small world networks) may make it more difficult for ‘like-minded’ nodes (that is, nodes with the same idea) to connect and may thus have smaller neighbourhood indexes and larger intra-idea distances than the more random network structures (such as the random and scale-free networks). Their effects may be more sensitive to the values of ϕ (because this affects how likely it is for their structure to change) and to values of δ because being restricted to a more closed group of nodes makes it difficult to reach a threshold necessary to become similar to surrounding nodes. Values of α may decrease the neighbourhood indexes by creating larger diversity

among neighbouring nodes.

If more rigid network structures do make it more difficult for like-minded nodes to connect, then it would be more difficult for a dominant idea to emerge in these networks. These effects may be smaller for larger values of ϕ since these values would allow for the structure to change more. For larger values of ϕ therefore one could expect that the effects of the network structures on the characteristics of the idea distribution are more similar since allowing to change the structure removes their initial influence.

3.1.2 Effects of Idea Distribution on Network Structure

Given a starting idea distribution and a caveman network structure, how do different idea distributions affect the average path length and diameter of the network? Do they change the number of connected components in the network? Do clusters form differently, and how does the clustering coefficient change? What does the distribution of node degree looks like? How do these effects depend on the values of ϕ , α , and δ ?

If the starting idea distribution is parallel to the caveman network structure (see Section 4.1.1 for a description of idea distributions), then like-minded nodes will already be connected and thus rewiring will probably not change much of the average path length, nor will it change the network diameter. Similarly, the clustering coefficient will remain high just like the starting value. The distribution of the node degree will also not change (nodes will have one of two values for their degree). In other words, if the idea distribution is parallel to the network structure, the structure will not change much. Changing ϕ and δ will not change these effects, and perhaps increasing α will decrease the clustering coefficient and will increase the number of connected components because nodes will disconnect from nodes with novel ideas and will rewire to nodes with the same idea.

If the starting idea distribution is random, then the network's caves will disintegrate as nodes will rewire with other nodes outside of their caves. This will change the degree distribution by increasing its variance (because nodes will have a variety of different degree values). Depending on the value of δ this disintegration may be reduced because nodes have a higher chance of forming dominant ideas within caves. Similarly, increasing ϕ will increase the disintegration of caves. Thus, for this idea distribution the parameter values may play a larger role.

If the starting idea distribution is anti-parallel, nodes within each cave will initially be connected with nodes that do not hold the same idea as them. Therefore the threshold δ will not be met in order for nodes to change their ideas, and they will rewire with other nodes outside of their cave. The clustering coefficient, as well as the number of connected components, the network diameter, and the average path length, will likely decrease since the structure will change significantly. The

degree distribution will increase in variance. Increasing ϕ and α and decreasing δ will probably increase the magnitude of these effects. Thus, having an anti-parallel idea distribution will probably display the most changes in the characteristics of the network structure that are in question.

4 Description of the Model

The model used here is based on a study by Holme and Newman [5]. Each simulation begins with a specified network structure as well as a distribution of the ‘idea’ (or state) of the nodes. At each time step a node either changes its idea to that of one of its neighbours’ ideas if its frequency surpasses a defined threshold, rewires to connect with a node that has the same idea, or generates a novel idea (this is the innovation parameter).

Given the network structure and node states, three parameters are introduced: ϕ (probability of rewiring), α (probability of innovation), and δ (complex contagion threshold). As in Holme and Newman [5], ϕ is a value from zero to one, and is the probability that one of the edges of a randomly chosen node i will be changed to connect to another node j that i is unconnected with. We decided to add one more criterion to this definition: node j is a node that has the same idea as node i . This encourages the simulations to reflect a common tendency of individuals to seek out others who think like them. If there is no such node j , then the chosen node will do nothing.

At each time step a node may ‘come up with a new idea’ with a probability of α . This value is small to reflect that novel ideas are not frequently observed.

We introduced a node threshold δ to the general model in order to investigate the behaviour of complex contagion as opposed to simple contagion. This was motivated by a study by Centola and Macy [3]. Simple contagion is well suited for modeling the spread of diseases since they may often be passed on by a single contact with an infected individual. However, as our intuition may suggest, other kinds of innovations raise questions about the legitimacy and credibility of the innovations themselves, and may thus require exposure to multiple sources of the innovation. This is called complex contagion. Models usually represent it in two ways regarding the number of connected sources that must have adopted an innovation in order to influence the agent (or individual) in question: it is either a fixed number (greater than one) or a fraction (between zero and one, inclusive). Our simulation used the second formulation since the degree of individual nodes varied across network structures.

4.1 Networks

For the purposes of our simulations, we used four network structures. These structures can be characterized by properties such as average shortest path lengths, clustering coefficients, and the degree of connectivity (see Table 1 for definitions). Below are short descriptions of each network structure. In order to compare between different structures, the network structure parameters were chosen such that the mean degree of the networks were similar (approximately 25). For further details about parameter

values, see Table 2.

Table 2: Table of parameters used in simulations.

Network	Parameter	Value
	ϕ	0.1 0.3 0.5
	α	0.01 0.05 0.1
	δ	0.001 0.01 0.05
	n	1000
	t_{end}	1000
Caveman	m	40
	p	40
Random (Erdos-Renyi)	$prob$	0.025
Scale free	m_0	24
	m_1	12
Small world	κ	24
	β	0.1

4.1.1 Random Graph

Random graphs have a short average path length. The graph is defined by the total number of nodes, and by the probability of any two nodes to be connected. Thus, all connections are random. They typically have a small clustering coefficient. Here we used a variant of the Erdős-Rényi random graph model [4] as implemented by Brugger and Schwirzer [2].

4.1.2 Caveman Graph

The caveman structure, as defined by Watts [6], has k isolated and fully connected ‘cliques’ from which one link is changed to connect one clique to another, rendering all cliques to be connected. Thus, relative to random graphs, they have a high clustering coefficient and a large average shortest path length.

4.1.3 Small World Graph

Small world graphs have characteristics that lie in between random graphs and highly clustered graphs (such as caveman graphs): they have a high clustering coefficient similar to the latter, but also have a small average shortest path similar to the former. Many real-world networks have been observed to have a small world structure, and

thus we included it in our simulations. Here we used the graph as defined by Watts and Strogatz [7], and implemented by Brugger and Schwirzer [2].

4.1.4 Scale-Free Graph

Scale-free network structures are often found where new nodes are constantly being added, and they are connected to already well-connected nodes. Such a structure displays a scale-free power-law distribution of the degree (connectivity) of nodes. Thus, there are few nodes that are highly connected, and more nodes that are moderately or mildly connected. Compared to random graphs, they have a smaller average shortest path. This graph was implemented by Brugger and Schwirzer [2] as defined by Barabási and Albert [1].

4.2 Ideas

After choosing a starting structure for our model, we then chose a distribution for the starting ideas (states) of nodes. Each node was randomly assigned one of these ideas, thus allowing for multiple nodes to have the same idea. For the caveman structure, however, there were two other options: to either distribute the starting ideas ‘parallel’ to the structure, i.e. such that all nodes in a cave shared the same idea, or ‘anti-parallel’ such that all nodes in a cave had a different idea. This was used for the analysis of the effect of the idea distribution on the network structure. Why was the caveman structure investigated? There were two reasons: firstly, it was straightforward how to define idea distributions that are in accord or disaccord with the caves in the network. Secondly, in the scientific community, research teams may often be made up of closely-connected members that are only weakly connected to other research teams, and within these teams, members may or may not be interested in the same ideas for research.

As previously mentioned, each node had a small probability α of adopting a novel idea from a virtually unlimited number of new ideas.

5 Implementation

Our simulation comprises mainly two parts: the phase 1 corresponding to the study of the effect of network structure on the idea distribution, and phase 2 where we study how the distribution of the ideas affect the topology of the network. These two phases are implemented in the same MATLAB file **mainscript.m**. Implementation of both phases is divided into three steps.

Step 1: Network structure is chosen and we generate the adjacency matrix corresponding to that structure. The initial idea distribution is also generated.

Step 2: The updating process is done onto the chosen network structure.

Step 3: At this step a series of functions are called to get the results.

5.1 Step 1: Generating network structures and initial idea distribution

For the first phase, one of the functions **step1_scalefree**, **step1_caveman**, **step1_smallworld** and **step1_randomgraph** is called, depending on our choice. Each function is found in the MATLAB files **step1_scalefree.m**, **step1_caveman.m**, **step1_randomgraph.m** and **step1_smallworld.m** correspondingly. Each of these functions generates the adjacency matrix corresponding to the chosen network structure. Also in this step, the initial idea distribution - a random distribution for the first phase - is applied onto the nodes.

For the second phase we generated just the adjacency matrix for the caveman structure network, and then we chose among three different initial idea distributions: random, parallel or anti-parallel. After choosing one of them, the initial idea distribution vector is generated.

5.2 Step 2: Update

This step is the same for both phases.

The updating rules in the simulation are implemented in the file **step2.m** and done by function **step2** which requires the following parameters:

- **t_end**: number of iterations
- **phi**: network reorganization rate
- **alpha**: innovation rate
- **mat**: initial connectivity matrix
- **vec**: initial idea vector

- **p**: initial number of opinions

And has as outputs:

- **mat**: connectivity matrix after simulation
- **vec**: idea vector after simulation
- **dominant_freq**: the vector holding the frequency of the dominant idea
- **most_freq**: the vector holding the index of the dominating idea in each time step

The function **step2**, in which the updating process is executed, implements the following algorithm:

Algorithm 1 Update process

```

for each of the iterations do
  choose a node  $x1$  in the network at random
  generate a random number  $a1$ 
  if  $a1 < \phi$  then                                ▷ With probability  $\phi$  we reorganize the network
    eliminate the connection between  $x1$  and one of its neighbours with a different
    idea
    select another node at random among the nodes with the same idea as  $x1$  and
    that are not already neighbours of  $x1$  and create a connection between them
  else change the idea of  $x1$  to one of the ideas of its neighbours which meet the
  threshold
  end if
  choose a node  $y$  in the random to come up with a novel idea
  generate a random number  $a2$ 
  if  $a2 < \alpha$  then  $y$  comes up with a new idea    ▷ With probability  $\alpha$   $y$  comes up
  with a new idea
  end if
end for

```

5.3 Step 3: Getting results

In the phase 1 we want to observe the influence of a certain network structure on the distribution of ideas after the updating process (step 2). For this, it is necessary to search for features that reflect the final distribution of ideas. In this study we observed the following features:

- **n_index**: the average neighbor index of the network
- **intra_idea_distance**: the average of the average shortest distance between agents holding the same idea
- **average_dominance_time**: the average of the dominance time for different dominance periods

All these parameters are obtained in **step3a.m**, **step3b.m** and **step3d.m** which are called in **main_script.m**.

In phase 2 we want to find out how the distribution of ideas changes the network structure. For this reason we look at a fixed network structure: the caveman structure. After step 2 we want to see how the initial structure was modified by the updating process, and in order to do this we observed the following features:

- **clust_coeff**: the clustering coefficient of the network
- **[dgr, frq]**: degree vector and its corresponding frequency vector
- **average_path_length**: the average path length for the graph
- **graph_diameter**: outputs the diameter of the graph

6 Simulation Results and Discussion

For the first section of the results, ideas were assigned randomly onto the nodes of four different network structures (caveman, small world, random, and scale-free). Chapter 4 describes the network structures and idea distributions that are discussed. Simulations were run for each network structure for 27 different parameter combinations (three values for each of ϕ , δ and α). The effects of each network structure on the idea distribution was evaluated on five features: the average dominance time of dominant (i.e., most frequent) ideas, the novelty index, the intra-idea distance, the neighbourhood index, and the frequency of dominance of an idea (see Table 1). We also investigated how these effects varied with the three parameters (ϕ , δ , α).

The second section of the results investigated the opposite direction of effects: how changing the idea distribution affected the resulting network structure. To do this we applied three different idea distributions (random, parallel, and anti-parallel to the structure) to a caveman network (see Table 1) with 40 caves. There were again 27 different parameter combinations for each idea distribution, as in the previous analysis. The five features of the network structure that we evaluated were: the clustering coefficient, the degree distribution of the nodes, the number of connected components, the average path length, and the network diameter.

We found that there were different behaviours for some features of the idea distribution depending on the network structure, and that there were different behaviours for the structure features depending on the idea distribution. Both of these results were at least partly influenced by the values of ϕ , δ , and α .

6.1 Effects of Network Structure on Idea Distribution

The results of the average dominance time and the novelty index were too dependent on the parameter values and were not included; the network structure does not seem to play a strong enough role over all parameter combinations in influencing these two features. It is not surprising, however, that the novelty index was highly dependent on the value of α , but it is not so intuitive why the average dominance time was not correlated with α at all: increasing the number of novel ideas decreases the possible number of ‘followers’ for already-established ideas, which should affect the frequency of dominance and therefore the dominance time. Perhaps the value of α would need to be increased to observe this behaviour.

Furthermore, we observed two different results for the intra-idea distance and the neighbourhood index: those from the caveman and small world structures, and those from the random and scale-free structures. All three parameter values affected these results.

6.1.1 Intra-Idea Distance and Neighbourhood Index

For any parameter combination, the caveman and small world structures resulted in larger intra-idea distances (respectively) than those of the random and scale-free structures, which were very similar to each other (Figure 1). Interestingly, a similar influence was found on the neighbourhood index: the caveman structure held the largest index regardless of parameter combination, followed by the small world, random, and scale-free structures (Figure 1). It seems that the caveman structure encourages nodes to be within the direct neighbourhood of like-minded nodes (nodes with the same idea) and at a farther distance from like-minded nodes that are not in their direct neighbourhood, whereas the random and scale-free structures have a tendency to keep like-minded nodes in each other's direct neighbourhood but to also keep those like-minded nodes not in their direct neighbourhood at a shorter distance. The difference in intra-idea distance between network structures could be a result of the general smaller average path distance that random and scale-free networks have as compared to the caveman and small world graphs.

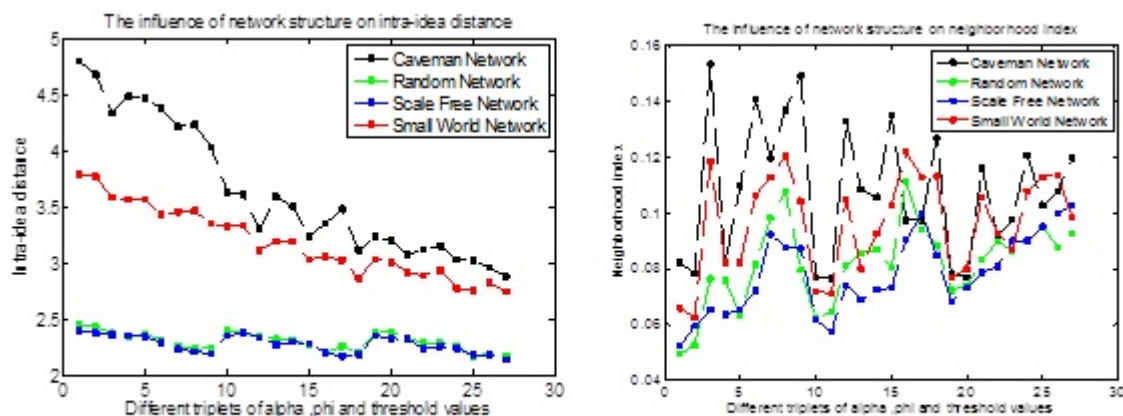


Figure 1: The influence of network structure on intra idea distance (left) and neighborhood index (right) for 27 distinct sets of parameters (triplets of alpha-phi-threshold).

Dependence on α For all network structures, increasing the level of innovation α decreased the intra-idea distance. This effect was more pronounced in the scale-free and random networks (Figure 2). Does innovation bring people together in scientific communities? Perhaps, and perhaps not. It is possible that these results are due to the construction of our model: because the mechanism of influence involves complex

contagion, new ideas would not be able to spread (since they are held only by the originator) and therefore these ideas would technically have an intra-idea distance of zero.

Higher values of α also increased the neighbourhood index for all network structures. This correlation was again most visible for the scale-free network, followed by the random network (Figure 3). One possible explanation for this correlation is that the more novel ideas nodes create, the less likely it is that the contagion threshold is met for other ideas, and thus nodes will only be rewiring instead of also changing their ideas. Thus more like-minded nodes will be connected, and the index increases.

Dependence on ϕ By increasing ϕ , the intra-idea distance decreased for all network structures. This correlation is quite an intuitive result since ϕ is the probability of deleting a connection between two nodes with different ideas and the formation of a new connection between two nodes with the same idea, and thus, by increasing ϕ the distance between like-minded nodes decreases. Unlike the α parameter, the effects of ϕ are more pronounced for the caveman and small world structures rather than for the random and scale-free networks (Figure 4).

On the other hand, the effects of ϕ on the neighborhood index varied between networks. Increasing ϕ increased the neighbourhood indexes of the random and scale-free networks, while it decreased the neighbourhood index of the caveman network and had no correlation with changes in the small world network (Figure 5).

Dependence on δ Increasing values of the complex contagion threshold δ slightly decreased the intra-idea distance for the caveman and small world network structures (Figure 6).

No correlation was found between the neighbourhood index of the small world, scale-free, and random network structures and values of δ . However, the neighbourhood index for the caveman network increased as δ increased (Figure 7). This is an interesting result. On one hand, it is intuitive since requiring more like-minded nodes to be in the direct neighbourhood for a node to adopt their idea automatically increases the number of like-minded nodes in the neighbourhood (if the node adopts their idea). However, increasing δ could have the opposite effect: if the threshold is too high, nodes will not adopt their neighbours' ideas and thus the neighbourhood index would remain small. The influence of δ only on the caveman network could be due to this structure's higher degree per node: almost all nodes have the same degree, whereas the other structures have the same average amount but with greater variance.

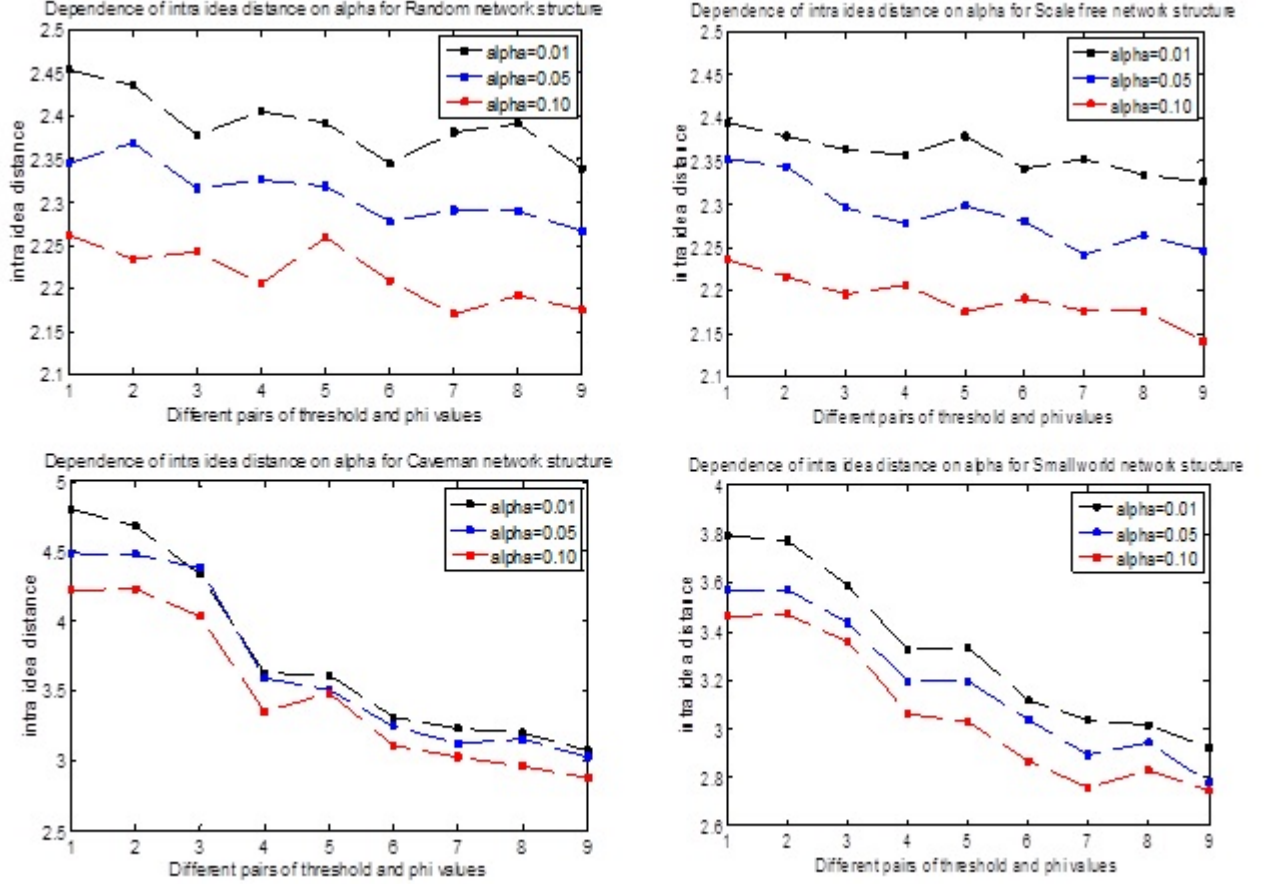


Figure 2: Dependence of intra idea distance on alpha for each network structure. Horizontal axis corresponds to distinct pairs of phi-threshold and vertical axis is the intra idea distance. Each curve corresponds to a different value of alpha. Black curve corresponds to the smallest value of alpha and it always has the highest intra idea distance while the red curve corresponds to the largest value of alpha which always has the lowest value of intra idea distance.

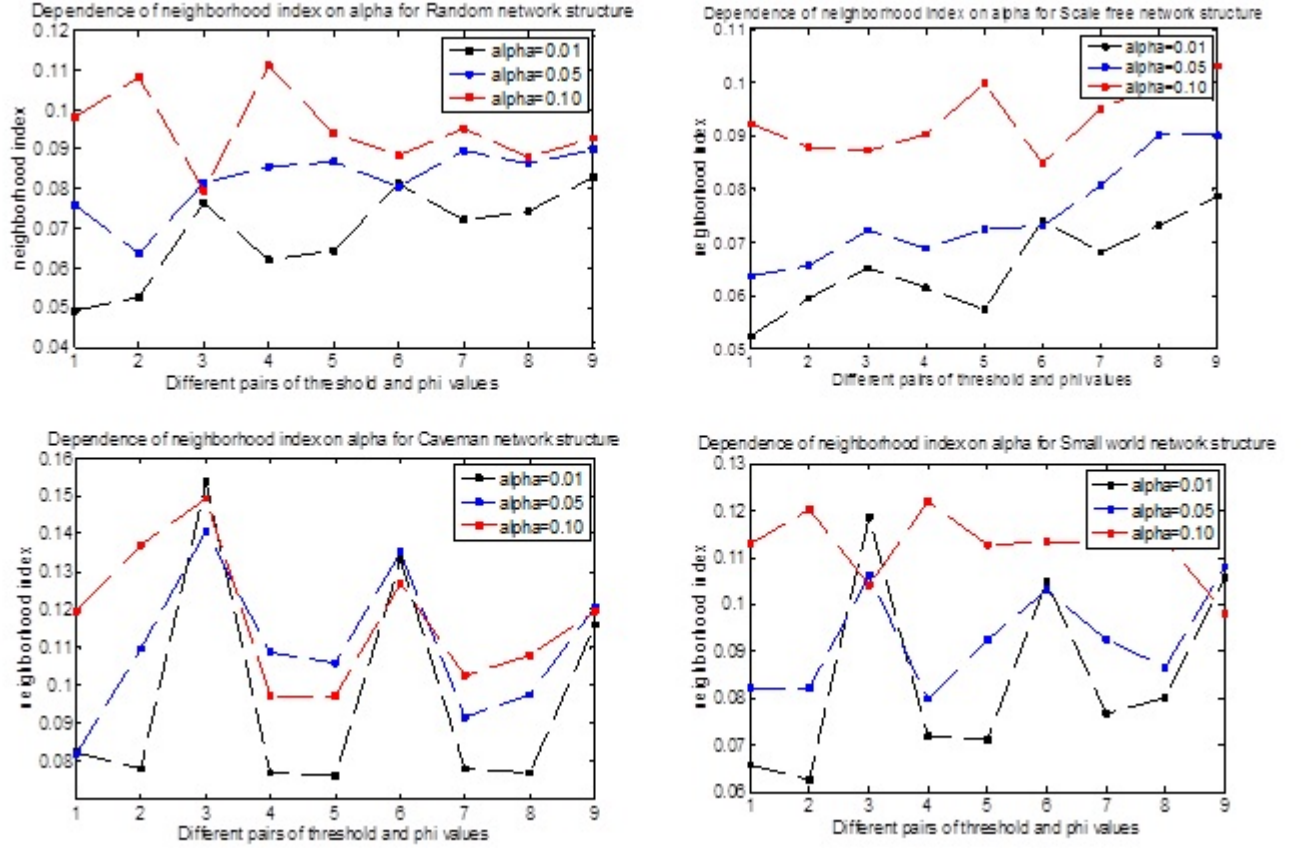


Figure 3: Dependence of neighborhood index on alpha for each network structure. Horizontal axis corresponds to distinct pairs of phi-threshold and vertical axis is the neighborhood index. Each curve corresponds to a different value of alpha. Red curve corresponds to the largest value of alpha and it has the highest neighborhood index while the black curve corresponds to the smallest value of alpha which has the lowest value of intra idea distance.

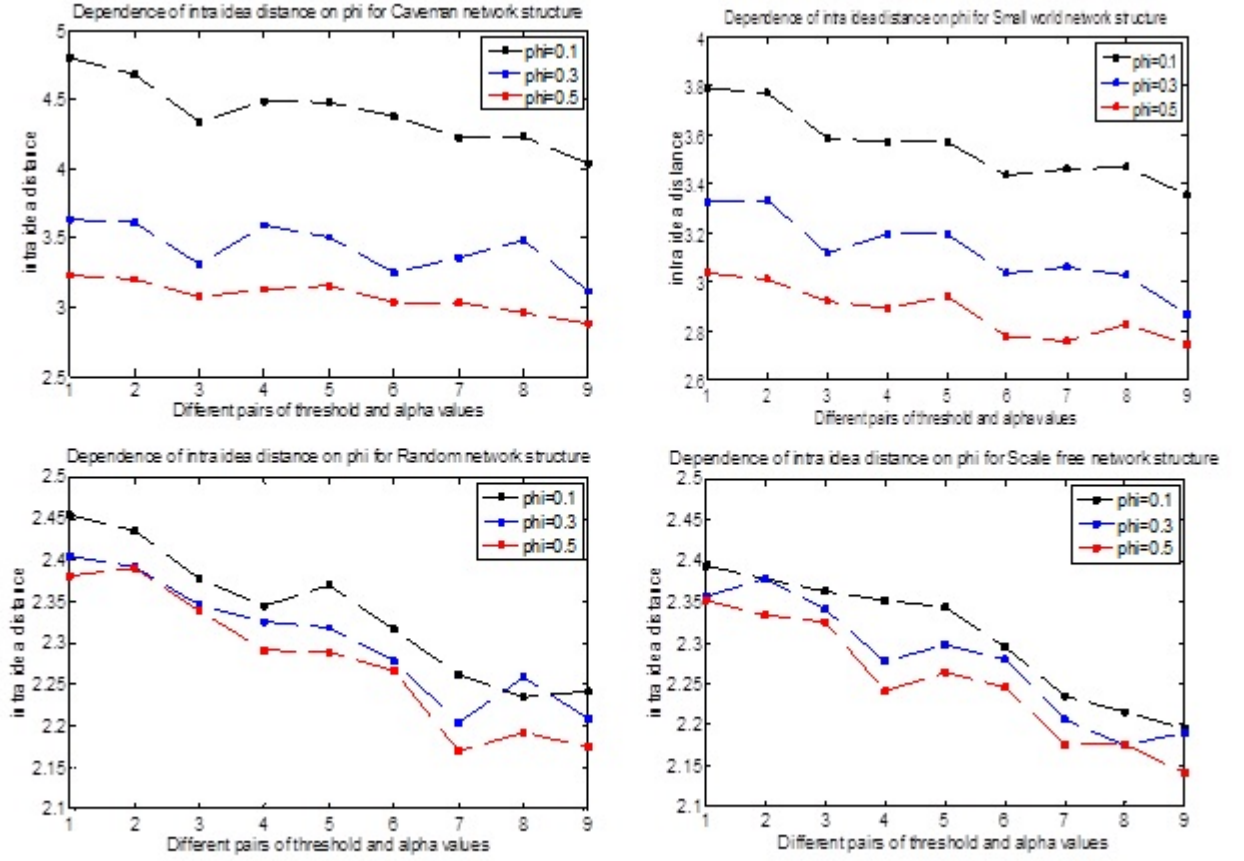


Figure 4: Dependence of intra idea distance on ϕ for each network structure. Horizontal axis corresponds to distinct pairs of alpha-threshold and vertical axis is the intra idea distance. Each curve corresponds to a different value of ϕ . Black curve corresponds to the smallest value of ϕ and it always has the highest intra idea distance while the red curve corresponds to the largest value of ϕ which always has the lowest value of intra idea distance.

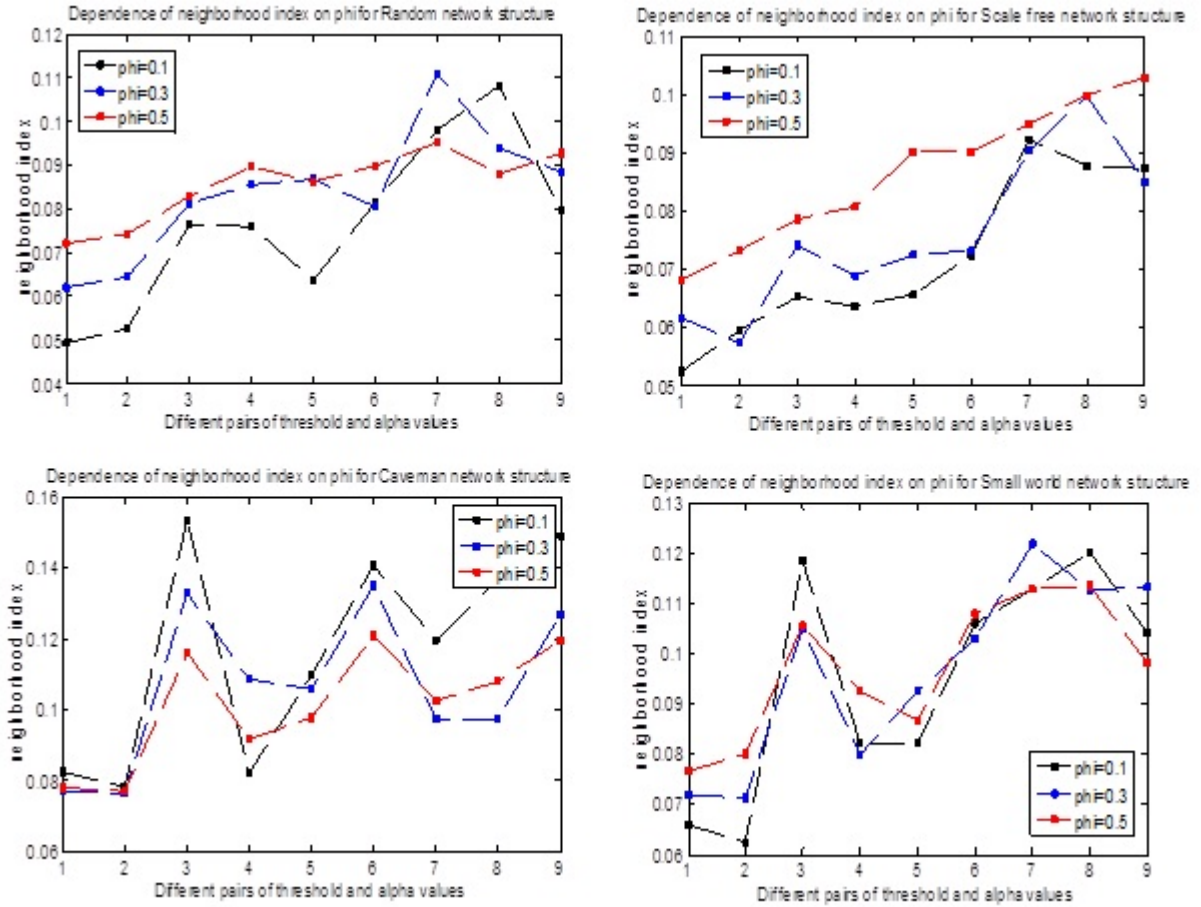


Figure 5: Dependence of neighborhood index on ϕ for each network structure. Horizontal axis corresponds to distinct pairs of alpha-threshold and vertical axis is the neighborhood index. Each curve corresponds to a different value of ϕ . Increasing ϕ leads to increase neighborhood distance for Random and Scale free networks while increasing ϕ causes the neighborhood index to be decreased for Cavemen Network. For Small world network there is no significant dependence of neighborhood index on ϕ .

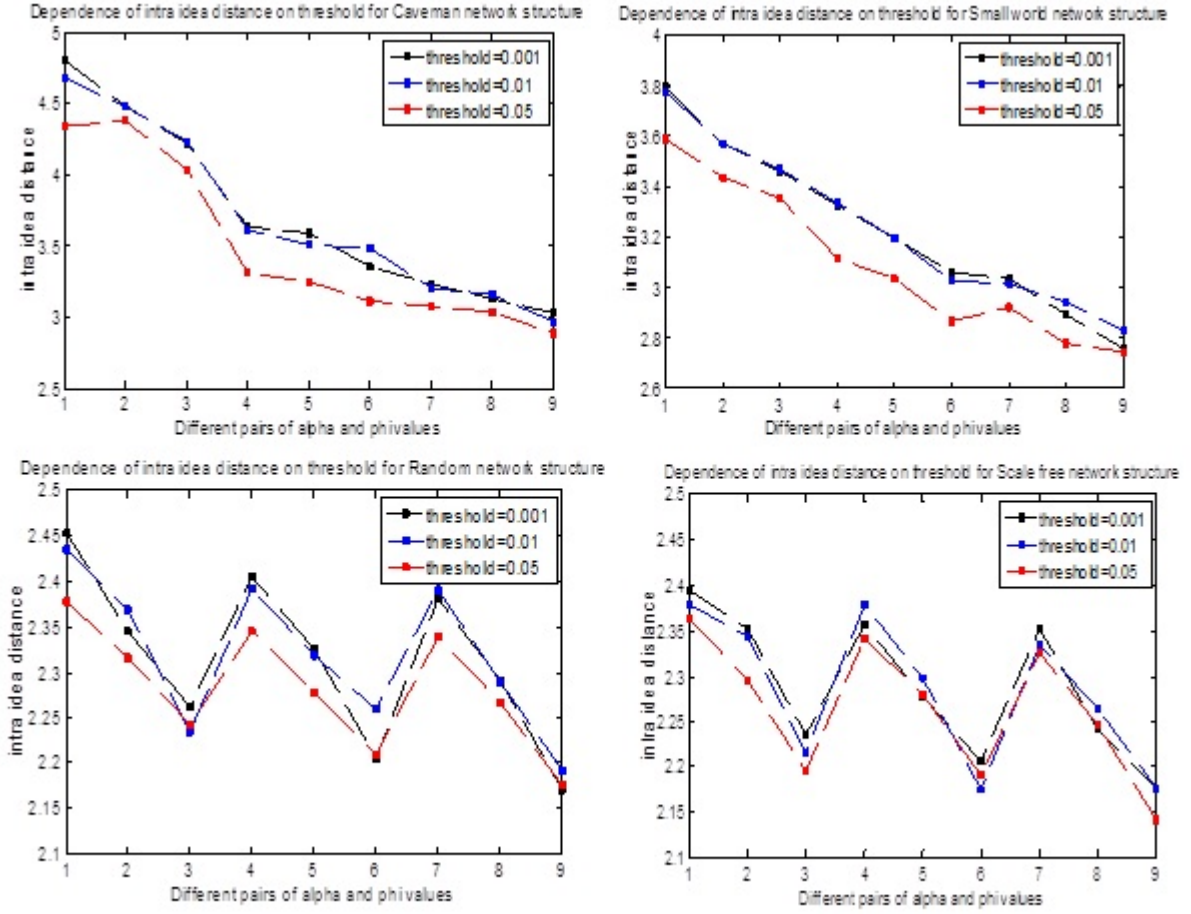


Figure 6: Dependence of intra idea distance on complex contagion threshold for each network structure. Horizontal axis corresponds to distinct pairs of alpha-phi and vertical axis is the intra idea distance. Each curve corresponds to a different value of complex contagion threshold. Black curve corresponds to the smallest value of complex contagion threshold and it has the highest intra idea distance while the red curve corresponds to the largest value of complex contagion threshold which has the lowest value of intra idea distance.

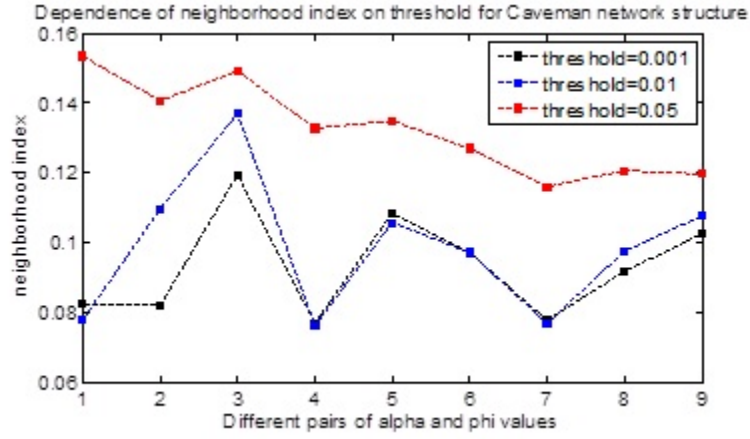


Figure 7: Dependence of neighborhood index on complex contagion threshold. Horizontal axis corresponds to distinct pairs of alpha-phi and vertical axis is neighborhood index. Each curve corresponds to a different value of complex contagion threshold. Red curve corresponds to the largest value of complex contagion threshold which has the largest value of neighborhood index while black curve corresponds to the smallest value of complex contagion threshold and it has the smallest neighborhood index.

6.1.2 Frequency of Dominance

This feature is interesting if one considers scientific society. How dominant are dominant ideas in the scientific community? Does the structure of the community influence this dominance? For all parameter combinations and for all network structures in our simulations, the frequency of dominance of ideas increased with time. This may suggest that none of these structures impede the adoption of new ideas. More surprisingly, however, the increase in dominance frequency progressed more quickly for the caveman network structure (Figure 8). Could it be that this structure encourages nodes to adopt dominant ideas more easily? This may not be generalizable because the results are quite sensitive to parameter values due to the stochasticity of the simulations. For example, Figure 8 shows a different combination of parameters, and here the faster increase in the dominance is not observed for the caveman structure.

6.2 Effects of Idea Distribution on Network Structure

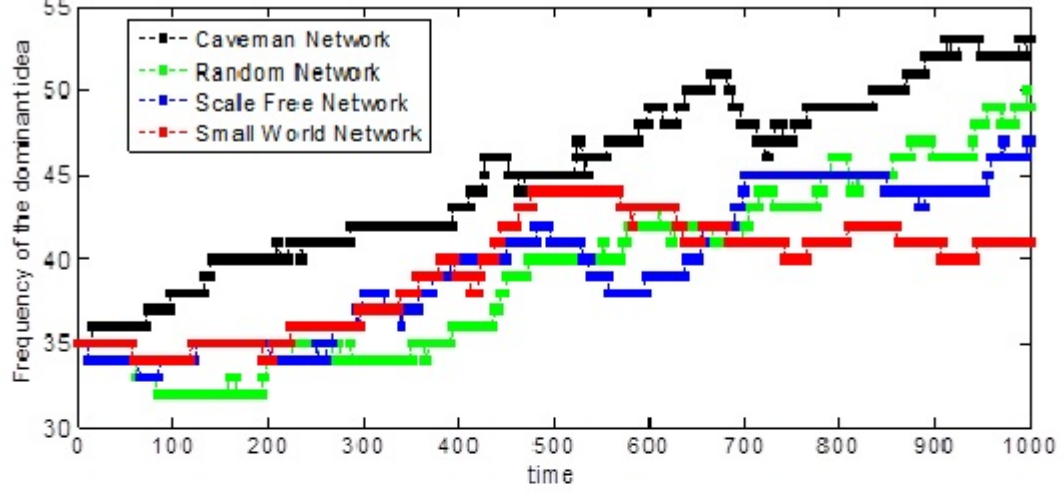
We observed that the results of applying a parallel idea distribution on the features of the network structure were quite different to the results of the random and anti-parallel idea distributions. It is interesting that for all parameter combinations and for each idea distribution, the network always remained fully connected. This could be because of the nature of our model: in order to disconnect with one node, there must be another node with the same idea to connect with. The nodes in a caveman network structure are, in a sense, ‘saturated’ since they are fully connected to their caves, and thus they remain connected to at least one of their original cave members.

While the networks always remained fully connected (Figure 9), the remaining features changed. These effects did not change with the parameter α for any of the idea distributions (see Figure 10, Figure 11 and Figure 12). Given these simulation results, perhaps a caveman-structured scientific community would also manage certain levels of innovativity without changing its fundamental structure.

6.2.1 Clustering Coefficient

The clustering coefficient of resulting networks varied with the type of idea distribution. When nodes in the same cave shared the same idea (parallel distribution), the clustering coefficient was larger (Figure 13). Additionally, the clustering coefficients for both the random and the anti-parallel idea distributions decreased in a similar manner regardless of the parameter combinations. Both of these results are intuitive since less rewiring would have taken place for the parallel distribution case, and the high clustering coefficient of the caveman structure would have been conserved,

The influence of network structure on the frequency of the dominant idea $\phi=0.5$ $\alpha=0.01$ threshold=0.05



The influence of network structure on the frequency of the dominant idea $\phi=0.3$ $\alpha=0.1$ threshold=0.05

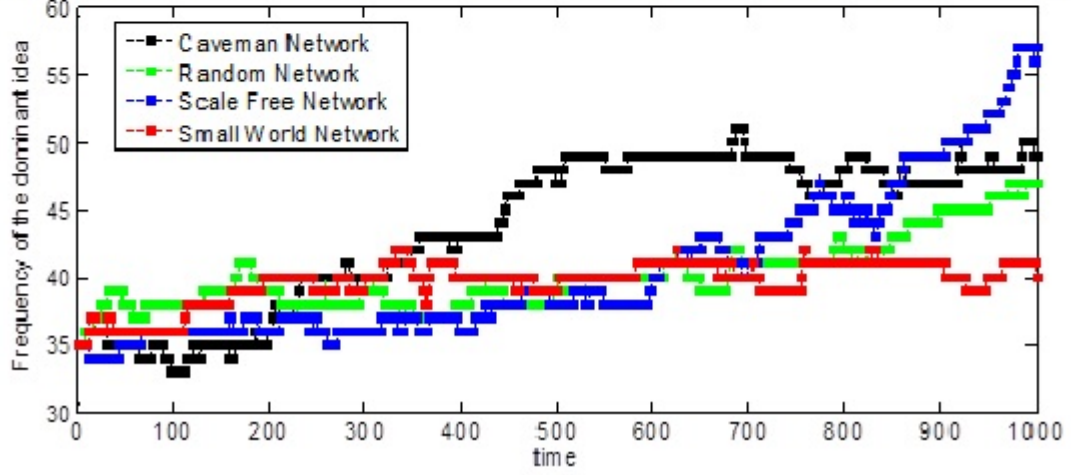


Figure 8: Frequency of the dominant idea at each time for four distinct network structures and two different sets of parameters: $\phi=0.5$, $\alpha=0.01$, threshold=0.05 (top) and $\phi=0.3$, $\alpha=0.1$, threshold=0.05 (bottom).

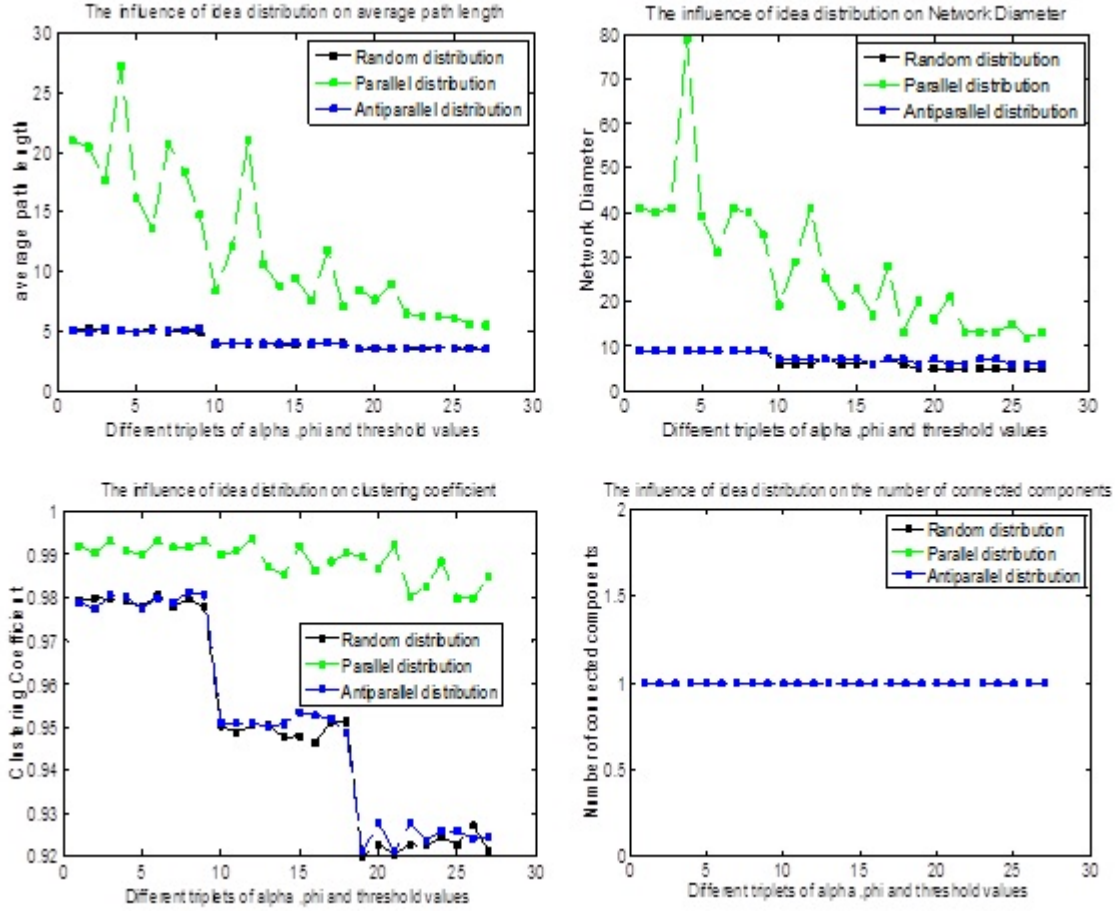


Figure 9: The influence of idea distribution on average path length (upper left), network diameter (upper right), clustering coefficient (bottom left) and number of connected components (bottom right) for 27 distinct sets of parameters (triplets of alpha-phi-threshold).

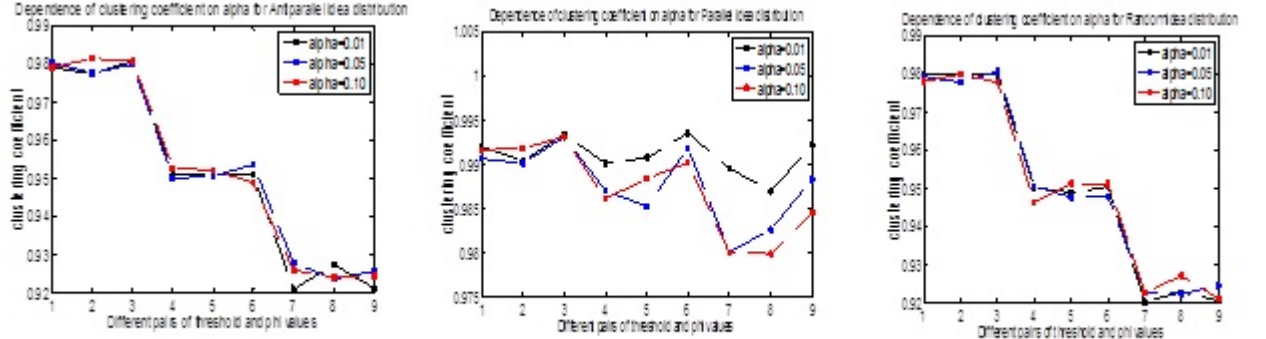


Figure 10: Dependence of clustering coefficient on alpha for each idea distribution. Horizontal axis corresponds to distinct pairs of phi-threshold and vertical axis is the clustering coefficient. Each curve corresponds to a different value of alpha. There is no dependence on alpha for clustering coefficient of the networks with any idea distribution.

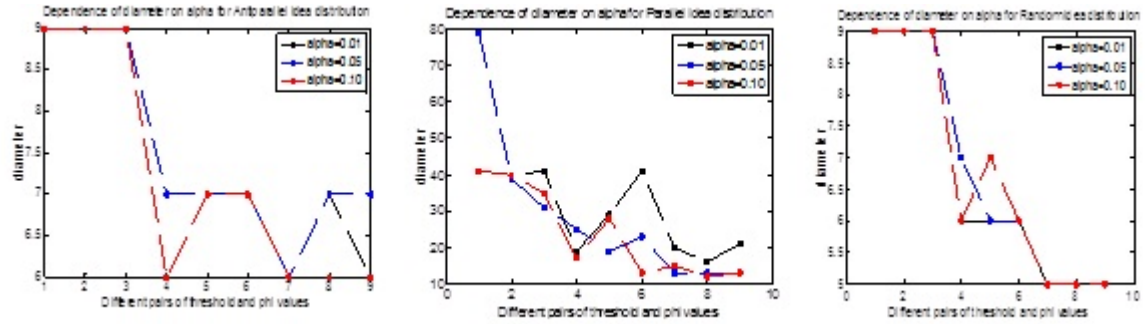


Figure 11: Dependence of network diameter on alpha for each idea distribution. Horizontal axis corresponds to distinct pairs of phi-threshold and vertical axis is the network diameter. Each curve corresponds to a different value of alpha. There is no dependence on alpha for the diameters of the networks with any idea distribution

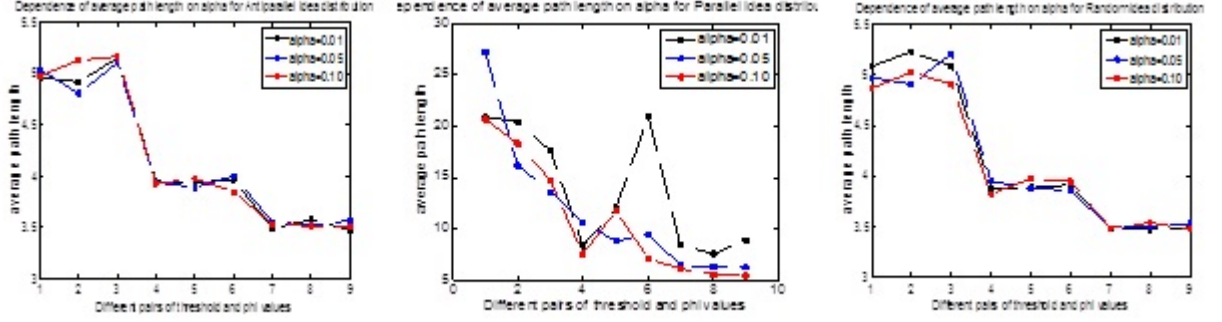


Figure 12: Dependence of average path length on alpha for each idea distribution. Horizontal axis corresponds to distinct pairs of phi-threshold and vertical axis is the average path length. Each curve corresponds to a different value of alpha. There is no dependence on alpha for average path length of the networks with any idea distribution.

whereas more rewiring would have occurred for the two other distributions, thus decreasing the clustering coefficients.

Dependence on parameters Increasing values of the rewiring parameter ϕ decreased the clustering coefficient for all starting distributions, especially for the random and anti-parallel distributions (Figure 14). This again is intuitive since ϕ increases the chances of changing connections in a highly clustered network. Increasing values of δ , however, only slightly increased the clustering coefficient when using a parallel idea distribution (Figure 15).

6.2.2 Average Path Length

The average path length of resulting networks was larger when a parallel idea distribution was used (Figure 9). This is not surprising, since the structure of the caveman network was more preserved (because most nodes were already connected to like-minded nodes and did not need to rewire), and its average path length is larger than that of more randomized networks, such as the ones resulting from a larger amount of rewiring.

Dependence on parameters Increasing ϕ , regardless of the idea distribution, decreased the average path length. This effect was more pronounced for the random and anti-parallel idea distribution cases (Figure 16). This is another intuitive result since more rewiring naturally disturbs the rigid structure of a caveman network,

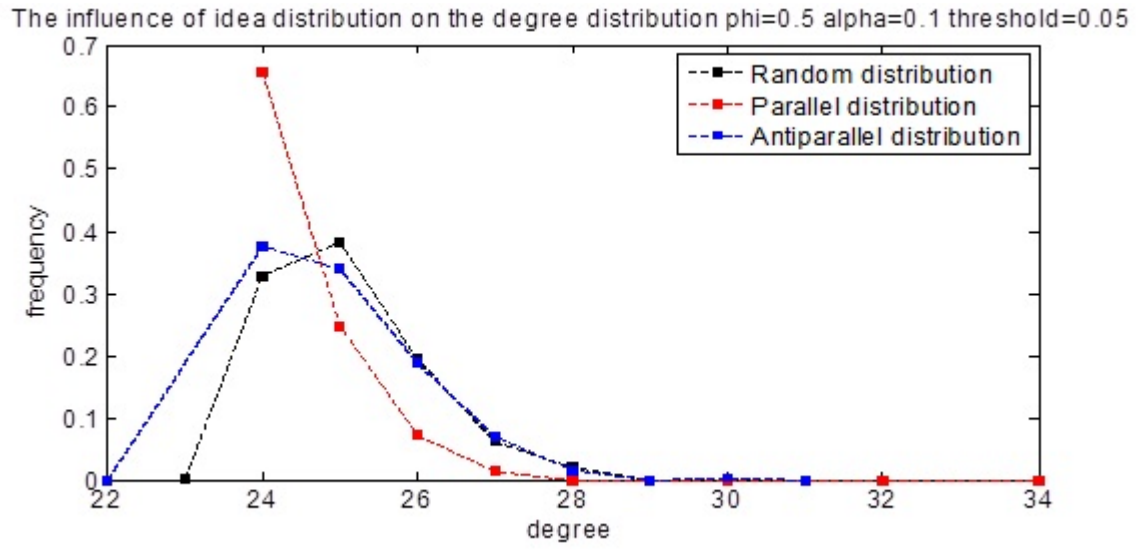


Figure 13: The influence of idea distribution on the degree distribution of the network. Horizontal axis corresponds to the degree of the nodes and vertical axis corresponds to the relative frequency of the nodes with that certain degree.

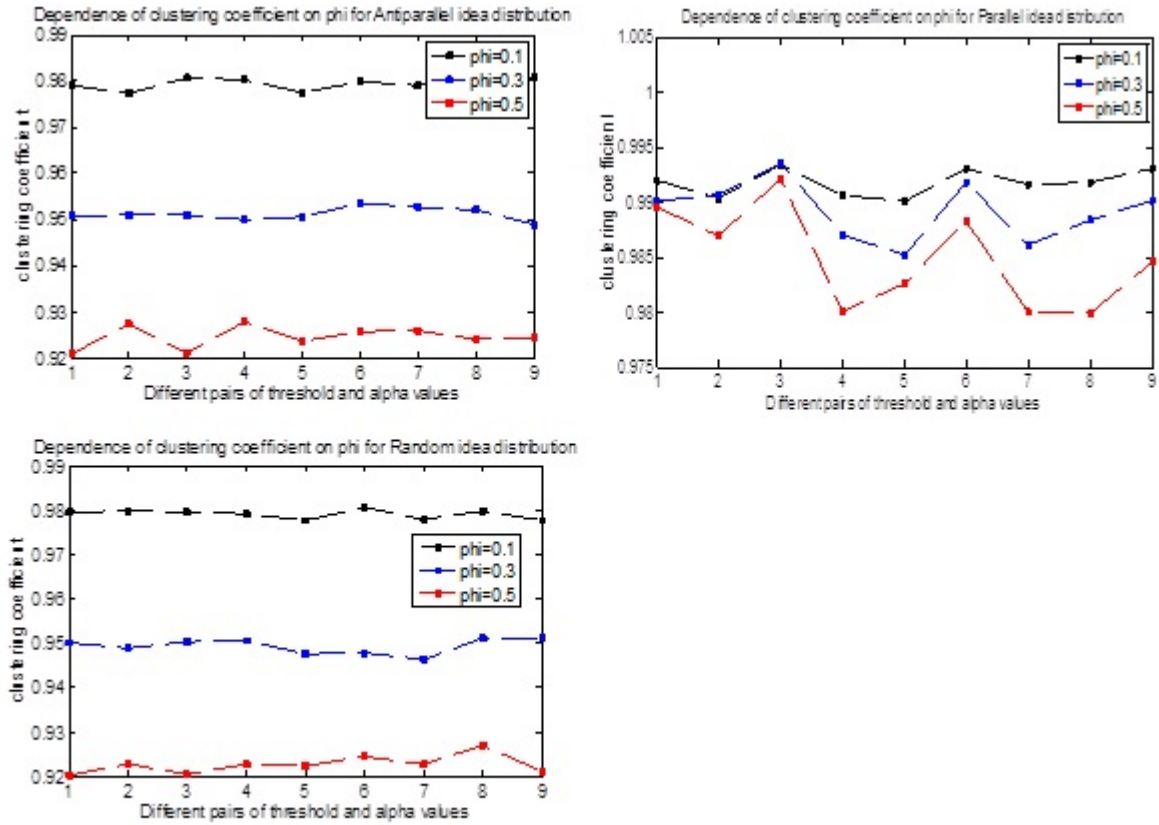


Figure 14: Dependence of clustering coefficient on ϕ for each idea distribution. Horizontal axis corresponds to distinct pairs of α -threshold and vertical axis is the clustering coefficient. Each curve corresponds to a different value of ϕ .

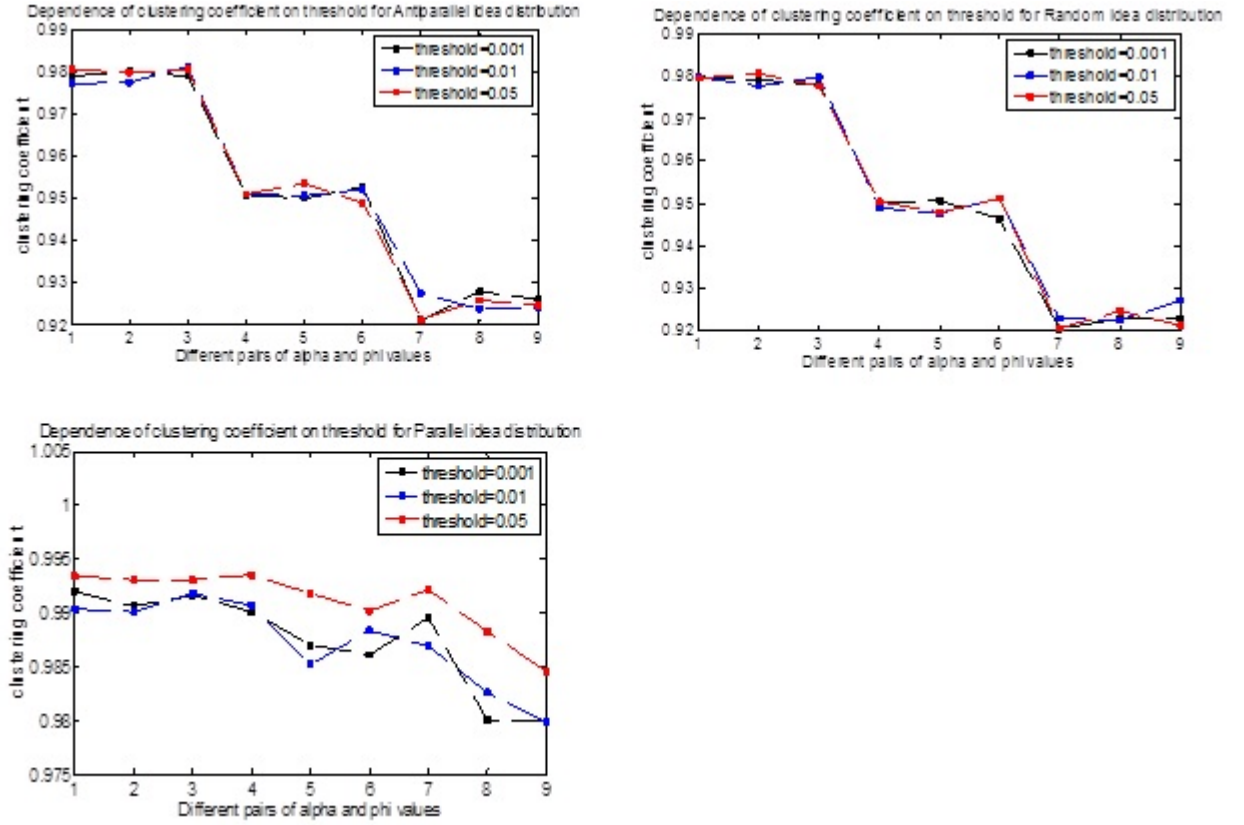


Figure 15: Dependence of clustering coefficient on complex contagion threshold for each idea distribution. Horizontal axis corresponds to distinct pairs of phi-alpha and vertical axis is the clustering coefficient. Each curve corresponds to a different value of complex contagion threshold.

thereby decreasing its large average path length; rewiring also occurs less frequently in the parallel idea distribution case because most nodes are already connected to like-minded nodes. Changing values of δ (which requires more than one neighbouring node to have the same idea in order to influence the chosen node) did not change the effects of idea distributions on the average path length (Figure 17). This is natural, since nodes were either already connected to a significant number of nodes with the same idea (in the case of the parallel distribution), not connected to any other node with the same idea (the anti-parallel case), or connected to nodes with random assignment of ideas. Thus the threshold δ would either already be fulfilled from the start, would definitely not be fulfilled, or would have a very small chance of being fulfilled, respectively.

6.2.3 Network Diameter

Similar to the clustering coefficient and the average path length, the network diameter was larger when the parallel idea distribution was applied (Figure 9). This distribution encouraged the structure of the caveman network to remain mostly unchanged, and thus the farthest distance between two nodes was larger than for the case of random or anti-parallel distributions, where more rewiring occurred.

Dependence on parameters As ϕ increased, the network diameter decreased for all idea distributions, and slightly less for the parallel distribution (Figure 19). Rewiring a caveman network intuitively may decrease the network diameter by connecting more of its caves. Similar to the average path length, values of δ did not change the behaviour of the network diameter given the idea distributions (Figure 18).

6.2.4 Degree Distribution

We observed that the degree distribution of the networks depended on the idea distribution (Figure 13). As scale-free graphs have a degree distribution that follows a scale-free power-law, it seems that the parallel idea distribution resulted in a degree distribution similar to that of a scale-free graph, which is not surprising. Caveman graphs have two or three different degrees for their nodes, and allowing for some rewiring would 'smooth' out this discrete distribution. Similar to previous results, the random and anti-parallel idea distributions behaved similarly: their degree distribution was similar to that of random distribution. It is interesting to see such a visible difference in these distributions over relatively few time steps (1000 steps), regardless of the parameter combinations.

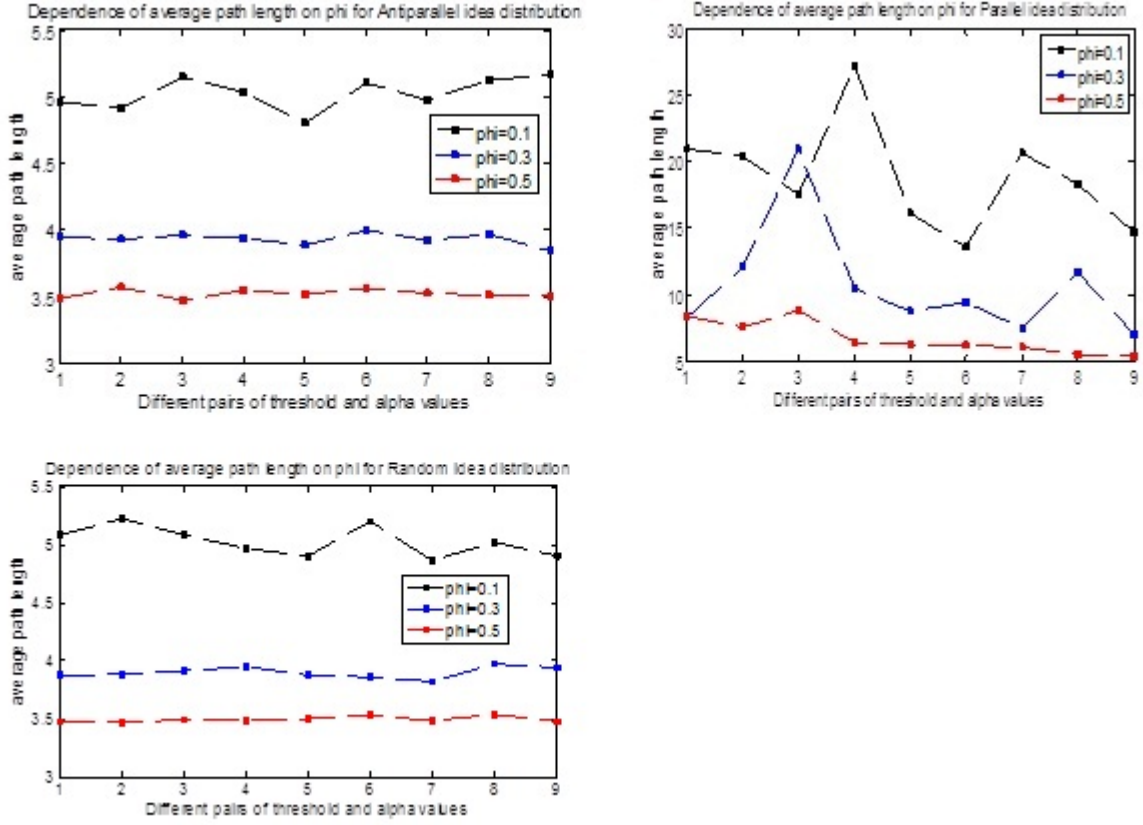


Figure 16: Dependence of average path length on ϕ for each idea distribution. Horizontal axis corresponds to distinct pairs of α -threshold and vertical axis is the average path length. Each curve corresponds to a different value of ϕ .

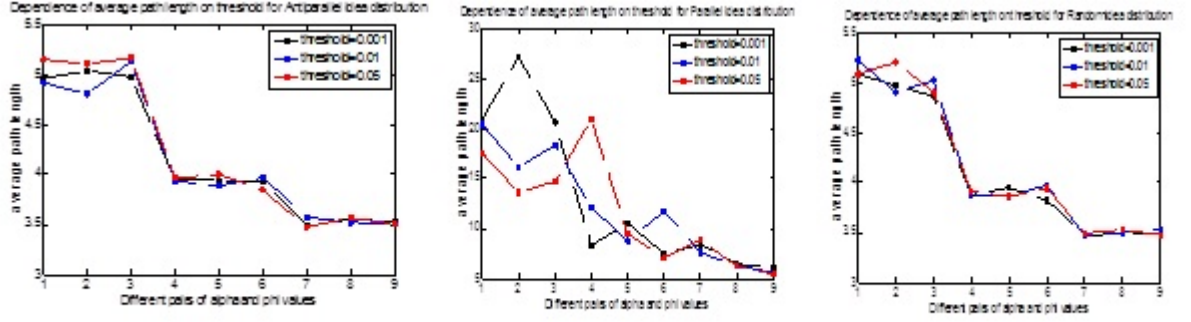


Figure 17: Dependence of average path length on complex contagion threshold for each idea distribution. Horizontal axis corresponds to distinct pairs of alpha-phi and vertical axis is the average path length. Each curve corresponds to a different value of complex contagion threshold. There is no dependence on complex contagion for average path length with any idea distribution.

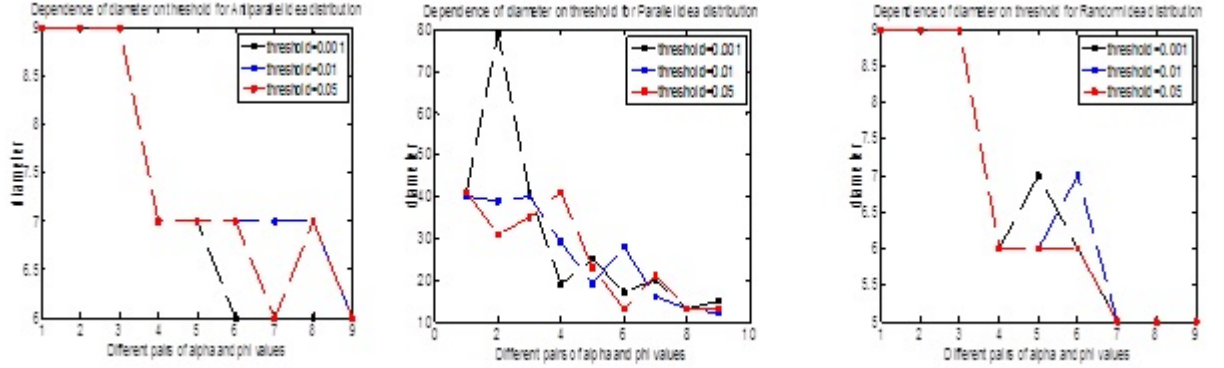


Figure 18: Dependence of network diameter on complex contagion threshold for each idea distribution. Horizontal axis corresponds to distinct pairs of phi-alpha and vertical axis is the network diameter. Each curve corresponds to a different value of complex contagion threshold. There is no dependence on complex contagion for network diameter with any idea distribution.

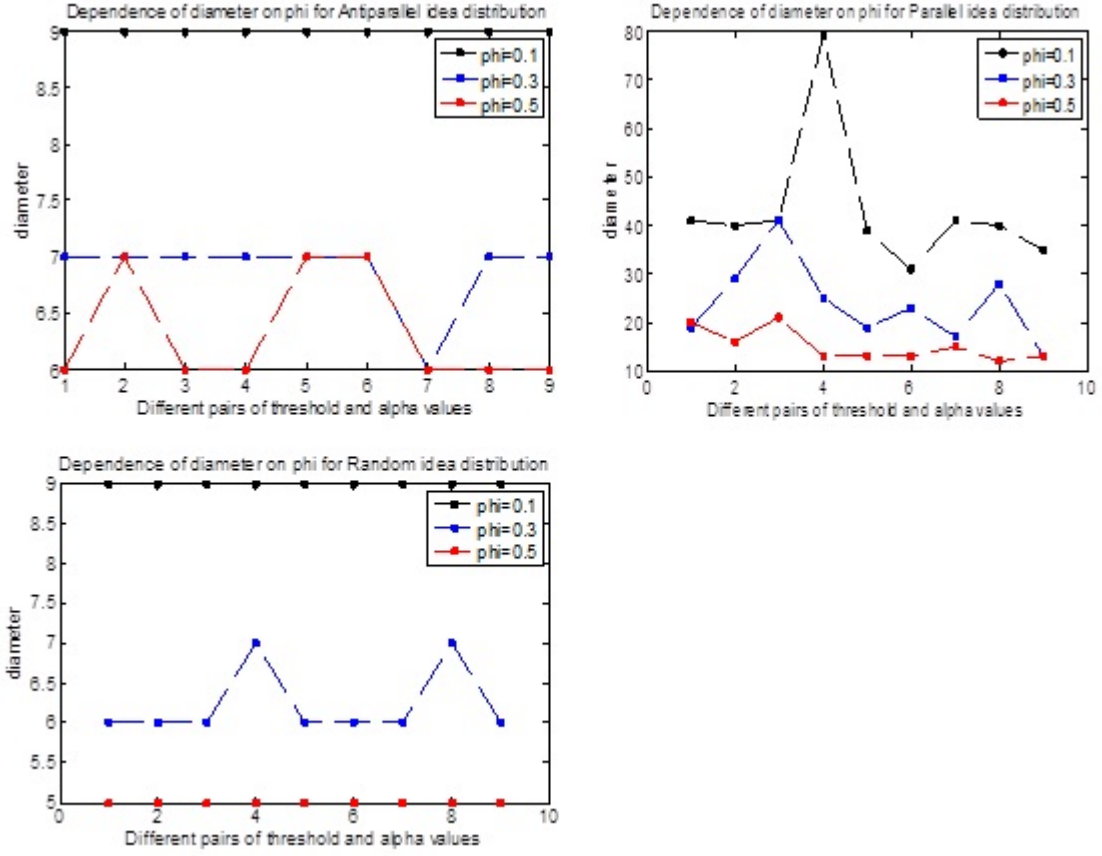


Figure 19: Dependence of network diameter on ϕ for each idea distribution. Horizontal axis corresponds to distinct pairs of alpha-threshold and vertical axis is the network diameter. Each curve corresponds to a different value of ϕ .

6.3 Discussion

As previously mentioned, we observed that some features of the idea distribution varied with the type of network structure. We also observed that some features of the network structure varied with the kind of idea distribution implemented. Some of these results were intuitive and expected, while others were not.

Network structure mainly influenced two features of the idea distribution: the intra-idea distance and the neighbourhood index. The intra-idea distance was larger for the caveman and small world networks, as anticipated. However, contrary to expectations, the neighbourhood index was larger for these two structures, and the caveman structure did not decrease the frequency of dominance (and neither did any other structure). Additionally, the values of ϕ and δ did correlate with changes in the values of the intra-idea distance (by decreasing it) and the neighbourhood index (with different effects depending on the structure), but not always: δ did not vary the results of the intra-idea distance or the neighbourhood index of the random and scale-free networks, and ϕ did not vary the neighbourhood index in the small world network. Lastly, and also contrary to expectations, increasing the α values increased the neighbourhood index of networks.

Four of the five features of the network structure changed with different idea distributions. The connected component interestingly remained one, regardless of the idea distribution and parameter values. Feature values of the anti-parallel and random idea distributions differed from those of the parallel distribution. Most features changed as expected: the clustering coefficient, average path length, and network diameter were larger when the parallel idea distribution was used as compared to the other two, and their values were similar to those of a caveman network structure. The clustering coefficient of the anti-parallel idea distribution networks did decrease, as expected. The degree distribution did increase in variance (becoming more similar to a normal distribution) for the networks that were initiated with a random or anti-parallel idea distribution, but the degree distribution of the parallel idea distribution networks resembled that of a scale-free power law. Values of ϕ influenced the features of the random and antiparallel distribution networks the most. However, the structure features of the networks with the random idea distribution were not more sensitive to parameter values as would have been expected; they behaved similar to those of the networks with the anti-parallel idea distribution. Values of δ only correlated with changes in the clustering coefficient of the networks with a parallel idea distribution, and only weakly. Values of α did not correlated with any changes of feature values.

7 Summary and Outlook

To conclude our simulation study, our results support the general idea that network structure and qualities of the ideas held in them may mutually influence each other. The more rigid the structure of a network was, the more likely that the intra-idea distance and neighbourhood index of the network was larger. These two features varied more with the innovation rate α for less structured networks, and varied more with the complex contagion threshold δ for the most rigid structure - the caveman network. The average dominance time seemed to vary more with parameter values (ϕ , δ , and α) than with the network structures, whereas the frequency of dominance of ideas did not decrease on average in the long run with any network structure.

A network in which the pattern of ideas held by the nodes are ‘in accord’ within the clusters of the caveman network maintained more of the structure features of a caveman network. These values varied with values of rewiring probabilities ϕ and complex contagion thresholds δ . Networks with a random pattern of ideas or with a pattern with more ‘disaccord’ within the clusters resulted in a structure that began to resemble a random graph more than a caveman network. These networks’ values varied more with the parameter ϕ of rewiring. Nodes given the chance to rewire with nodes that share the same idea had more opportunity to do so in the random and ‘disaccord’ idea patterns than in the pattern which already had much accord.

Thus, in addition to the structure of networks and the pattern of ideas in them, complex contagion thresholds, innovation rates, and the probability of creating new connections (while reflecting ‘preferences’ of being connected with like-minded others) tend to influence features of the network. Several extensions to the proposed model could be investigated to better understand the relationships between network structure and idea distribution.

Rewiring criteria Future simulations may compare the emerging features of idea distributions not just between network structures, but also between different rewiring criteria. It is not clear how much of the features of the idea distribution in this simulation study was a result of the network structure or of the ‘preference’ that nodes had in rewiring to like-minded nodes. Therefore, these results could be compared to (1) random rewiring or, to allow structure to play a larger role, (2) to allow random rewiring to nodes that are at most a distance of three nodes away. This is somewhat more realistic since most people connect with individuals who are somewhat in their vicinity through mutual connections.

Complex contagion and innovation Considering complex contagion, novel ideas in our model were at a disadvantage for spreading in the network. Allowing novel

ideas to have a larger influence weight may be one way to grant the ability of them to spread to other nodes. Alternatively, the complex contagion threshold for novel ideas may be lowered.

Random idea adoption Future simulations may investigate the effects of network structure on idea distributions by comparing to a ‘benchmark’ model. This model would update the ideas of nodes at random, and thus the effects of connections may be better observed within network structures and then compared between network structures.

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A MATLAB code

A.1 Main script

```
1 %% The first phase: Simulation to study the influence of network ...
   structure on the opinion%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2   %% The following parameters will remain constant during this study,
3   %% so we won't play with them %%
4   n=1000; %% the number of agents %%
5   m=40; %% initial number of clusters for caveman matrix%%
6   p=40; %% initial number of opinions%%
7   t_end=1000; %% number of iterations%%
8   %% for the following parameters we'll run different simulations based on
9   %% combinatorial complexity of the parameters%%
10  phi_choices=[0.1,0.3,0.5]; %% network reorganization rate%%
11  alpha_choices=[0.01,0.05,0.10]; %% innovation rate %%
12  threshold_choices=[0.001,0.01,0.05]; %% threshold for complex contagion %%
13
14
15  %% a totally random idea distribution , independent of the connectivity
16  %% matrix, so applicable for every network structure is defined for this
17  %% phase %%
18  vec1=zeros(1,n);
19  for i=1:n
20      vec1(i)=ceil(rand()*p);
21  end
22
23  for choice1=1:4
24  %% Step1: Definition of Different initial matrices ...
      %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
25      %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% For each simulation, we must choose one of the ...
          following connectivity matrices %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
26      switch choice1
27          case 1
28              %% option 1: Caveman Connectivity Matrix
29              mat1=step1_caveman(n,m);
30              s1='Caveman';
31          case 2
32              %% option 2: Random Connectivity Matrix
33              prob=0.025; %% probability of edge formation between any pairs ...
                  of edges
34              mat1=step1_randomgraph(n,prob);
35              s1='Random';
36          case 3
37              %% option 3: Scale Free Connectivity Matrix
38              m0=24; % number of initially placed nodes
39              m1=12; % number of nodes a new added node is connected to,  $1 \leq \dots$ 
                  m1 < m0
```

```

40     mat1=step1.scalefree(n, m0, m1);
41     s1='Scale-free';
42     case 4
43         %% option 4: Small world Connectivity Matrix
44         ka=24; %% mean degree (assumed to be an even integer)
45         beta=0.01; %% rewiring probability
46         mat1= step1.smallworld(n, ka, beta);
47         s1='Small-world';
48     end
49
50     %% Step2: Simulation ...
51     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
52     for choice2=1:3
53         phi=phi_choices(choice2);
54         for choice3=1:3
55             alpha=alpha_choices(choice3);
56             for choice4=1:3
57                 threshold=threshold_choices(choice4);
58
59                 [mat2,vec2,dominant_freq,most_freq]=
60                 step2(t_end,phi,alpha,mat1,vec1,p,threshold);
61                 %% obtaining the final matrix and vector after running ...
62                 simulation.
63
64                 %%% We need step4c here, since it's outputs will be the input
65                 %%% for step 3b
66                 %%% step4c: number of connected components %%%%%%%%%
67                 sp_mat2=sparse(mat2);
68                 [s,c]=graphconncomp(sp_mat2); %% matlab built in function ...
69                 'Bioinformatics Toolbox'
70                 %% s: number of connected components
71                 %% c: vector which assigns each node to a connected component
72
73                 %% Step3: Results for structure to idea ...
74                 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
75
76                 %%% step3a: defining the average intra-idea ...
77                 neighbourhood index %%%
78                 neighbor_index=step3a(mat2,vec2);
79
80                 %%% step3b: defining the average intra-idea distance ...
81                 %%%
82                 intra_idea_distance=step3b(mat2,vec2,s,c);
83
84                 %%% step3c: frequency of dominant idea with respect to ...
85                 time %%%
86                 %% is the third output of the step2 function ...
87                 (dominant_freq)%%
88                 dominant_freq;

```

```

82         % step3d: Fraction of novel ideas (novelity index) %
83         nov_index=(length(find(vec2>p)))/(length(vec2)); % ...
            indicates the fraction of agents holding the newly ...
            generated ideas
84
85         % step3e: defining the average dominance time (the ...
            average amount of time in which the dominating idea ...
            keeps it's dominance over differnt dominance periods)
86         average_dominance_time=step3e(most_freq);
87
88         % naming the file which saves the results
89         s2=int2str(choice2);
90         s3=int2str(choice3);
91         s4=int2str(choice4);
92         name=['phase1_',s1,'_',s2,'_',s3,'_',s4];
93         save(name);
94     end
95 end
96 end
97 end
98
99 clear;
100
101 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
102 % The second phase: Simulation to study the influence of opinion on the ...
    network structure%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
103
104 % The following three parameters will remain constant during this study,
105 % so won't play with them %
106 n=1200; % the number of agents
107 m=40; % initial number of clusters for caveman matrix
108 p=40; % initial number of opinions
109 t_end=1000; % number of iterations%
110 % for the following parameters we'll run different simulations based on
111 % combinatorial complexity of the parameters%
112 phi_choices=[0.1,0.3,0.5]; % network reorganization rate%
113 alpha_choices=[0.01,0.05,0.10]; % innovation rate %
114 threshold_choices=[0.001,0.01,0.05]; % threshold for complex contagion %
115
116
117
118 % in this phase we'll keep connectivity matrix constant, so we only use
119 % Caveman connectivity matrix %
120 mat1=step1_caveman(n,m);
121
122
123 for choice1=1:3
124 % Step1: Definition of Different initial idea vectors ...
    %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
125     switch choice1

```

```

126         case 1
127             %%%%% option1: Random idea vector %%%%%%
128             %%% a totally random idea distribution , independent of the ...
                connectivity
129             %%% matrix, so applicable for every network structure
130             vec1=zeros(1,n);
131             for i=1:n
132                 vec1(i)=ceil(rand()*p);
133             end
134             s1='Random';
135         case 2
136             %%%%% option2: Parallel idea vector %%%%%%
137             %%% This idea vector is applicable only for caveman ...
                connectivity matrix in
138             %%% which every agents inside a cluster have the same idea
139             vec1=zeros(1,n);
140             for i=1:(m-1) %%% for each cluster
141                 for j=1:ceil(n/m)
142                     vec1((i*ceil(n/m))+j)=i; %%% all agents will hold the ...
                        i-th idea
143                 end
144             end
145             s1='Parallel';
146         case 3
147             %%%%% option3: Antiparallel idea vector %%%%%%
148             %%% This idea vector is applicable only for caveman ...
                connectivity matrix in
149             %%% which every agents inside a cluster have different idea
150             vec1=zeros(1,n);
151             for i=1:(m-1) %%% for each cluster
152                 for j=1:ceil(n/m)
153                     vec1((i*ceil(n/m))+j)=j; %%% all agents will hold ...
                        different idea
154                 end
155             end
156             s1='Antiparallel';
157     end
158     %% Step2: Simulation ...
        %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
159     for choice2=1:3
160         phi=phi_choices(choice2);
161
162         for choice3=1:3
163             alpha=alpha_choices(choice3);
164             for choice4=1:3
165                 threshold=threshold_choices(choice4);
166
167                 [mat2,vec2,dominant_freq,most_freq]=
168                 step2(t_end,phi,alpha,mat1,vec1,p,threshold);

```

```

169         %% obtaining the final matrix and vector after running ...
           simulation.
170
171
172         %% Step3: Results for idea to structure ...
           %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
173
174         %%%%%%%%% step4a: clustering coefficient of the final network ...
           %%%%%%%%%
175         clust_coefficient=step4a(mat2);
176
177         %%%%%%%%% step4b: degree distribution of the final network ...
           %%%%%%%%%
178         [dgr, frq]=step4b(mat2);
179         average_degree=sum(dgr.*frq)/sum(frq);
180
181         %%%%%%%%% step4c: number of connected components %%%%%%%%%
182         sp_mat2=sparse(mat2);
183         [s,c]=graphconncomp(sp_mat2); %% matlab built in function ...
           'Bioinformatics Toolbox'
184         %% s: number of connected components
185         %% c: vector which assigns each node to a connected component
186
187         %%%%%%%%% step4d: average path length for the final network ...
           %%%%%%%%%
188         average_path_length = step4d( mat2,s,c );
189
190         %%%%%%%%% step4e: Diameter of the network %%%%%%%%%
191         diam=step4e(mat2,s,c);
192
193         %%naming and saving
194         s2=int2str(choice2);
195         s3=int2str(choice3);
196         s4=int2str(choice4);
197         name=['phase2-',s1,'_',s2,'_',s3,'_',s4];
198         save(name);
199     end
200 end
201 end
202 end
203
204 clear;

```

A.2 Step 1: generation of structure networks

randomgraph.m

```
1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 %%% code adopted from %%%
3 %%% Modeling and Simulating Social Systems with MATLAB %%%
4 %%% http://www.soms.ethz.ch/teaching/MatlabFall2012 %%%
5 %%% Authors: Stefan Brugger and Cristoph Schwirzer, 2011 %%%
6 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
7
8 function final= step1.randomgraph(n, p)
9 % Generates an undirected random graph (without self-loops) of size n (as
10 % described in the Erdoes-Renyi model)
11 %
12 % INPUT
13 % n: [1]: number of nodes
14 % p: [1]: probability that node i and node j, i != j, are connected by ...
    an edge
15 %
16 % OUTPUT
17 % final: [n n] full symmetric adjacency matrix representing the ...
    generated graph
18
19 % Note: A generation based on sprandsym(n, p) failed (for some values of p
20 % sprandsym was far off from the expected number of n*n*p non-zeros), ...
    therefore
21 % this longish implementation instead of just doing the following:
22 %
23 % B = sprandsym(n, p);
24 % A = (B-diag(diag(B))>0);
25 %
26
27 % Idea: first generate the number of non-zero values in every row for a ...
    general
28 % 0-1-adjacency matrix. For every row this number is distributed ...
    binomially with
29 % parameters n and p.
30 %
31 % The following lines calculate "rowsize = binoinv(rand(1, n), n, p)", ...
    just in a
32 % faster way for large values of n.
33
34 % generate a vector of n values chosen u.a.r. from (0,1)
35 v = rand(1, n);
36 % Sort them and calculate the binomial cumulative distribution function with
37 % parameters n and p at values 0 to n. Afterwards match the sorted random
38 % 0-1-values to those cdf-values, i.e. associate a binomial distributed ...
    value
```



```

39 % with each value in r. Each value in v also corresponds to a value in r:
40 % permute the values in rowSize s.t. they correspond to the order given ...
    in v.
41 [r index] = sort(v); % i.e. v(index) == r holds
42 rowSize = zeros(1, n);
43 j = 0;
44 binoCDF = cumsum(binopdf(0:n, n, p));
45 for i = 1:n
46     while j<n && binoCDF(j+1)<r(i)
47         j = j + 1;
48     end
49     rowSize(i) = j;
50 end
51 rowSize(index) = rowSize;
52
53 % for every row choose the non-zero entries in it
54 nNZ = sum(rowSize);
55 I = zeros(1, nNZ);
56 J = zeros(1, nNZ);
57 j = 1;
58 for i = 1:n
59     I(j:j+rowSize(i)-1) = i;
60     J(j:j+rowSize(i)-1) = randsample(n, rowSize(i));
61     j = j + rowSize(i);
62 end
63
64 % restrict I and J to indices that correspond to entries above the main ...
    diagonal
65 % and finally construct a symmetric sparse matrix using I and J
66 upperTriu = find(I<J);
67 I = I(upperTriu);
68 J = J(upperTriu);
69 A = sparse([I;J], [J;I], ones(1, 2*size(I, 2)), n, n);
70 final=full(A);
71 end % random_graph(...)

```

scalefree.m

```
1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 %%% code adopted from %%%
3 %%% Modeling and Simulating Social Systems with MATLAB %%%
4 %%% http://www.soms.ethz.ch/teaching/MatlabFall2012 %%%
5 %%% Authors: Stefan Brugger and Cristoph Schwirzer, 2011 %%%
6 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
7
8 function A = scalefree(n, m0, m)
9 % Use the Barabasi-Albert model to generate a scale free graph of size n (as
10 % described in Albert-Laszlo Barabasi & Reka Albert: "Emergence of scaling
11 % in random networks")
12 %
13 % INPUT
14 % n: [1]: number of nodes
15 % m0: [1]: number of initially placed nodes
16 % m: [1]: number of nodes a new added node is connected to,  $1 \leq m < m_0$ 
17 %
18 % OUPUT
19 % A: [n n] sparse symmetric adjacency matrix representing the generated ...
    graph
20
21 % Start with a graph of size m0 and add edges to this graph. Each of ...
    these m0
22 % nodes is connected to at least m nodes.
23 B = zeros(m0, m0);
24 for i = 1:m0
25     neighbors = randsample(m0-1, m);
26     neighbors = neighbors + (neighbors >= i);
27     B(i,neighbors) = 1;
28     B(neighbors,i) = 1;
29 end
30
31 % Create a vector of edges added so far, i.e. nodes edge(2*i) and ...
    edge(2*i-1),
32 %  $1 \leq i \leq nEdges$ , are connected by an edge.
33 [rows, columns] = find(triu(B));
34 nEdges = size(rows, 1);
35 edges = reshape([rows';columns'], 2*nEdges, 1);
36 edges = [edges; zeros(2*(n-m0)*m,1)];
37
38 % Add nodes m0+1:n, one at a time. Each node is connected to m existing ...
    nodes,
39 % where each of the existing nodes is chosen with a probability that is
40 % proportional to the number of nodes it is already connected to.
41 used = zeros(n, 1); % is a node already used in a timestep?
42 for i = m0+1:n
43     neighbors = zeros(1, m);
```

```

44     for j=1:m
45         k = edges(randi(2*nEdges));
46         while used(k)
47             k = edges(randi(2*nEdges));
48         end
49         used(k) = 1;
50         neighbors(j) = k;
51     end
52     used(neighbors) = 0;
53     edges(2*nEdges+1:2*nEdges+2*m) = reshape([repmat(i, 1, m); ...
54         neighbors], ...
55         1, 2*m);
56     nEdges = nEdges+m;
57 end
58 % finally construct a symmetric adjacency matrix using the vector of edges
59 edges = edges(1:2*nEdges);
60 first = edges(1:2:end);
61 second = edges(2:2:end);
62 A = sparse([first;second], [second;first], ones(2*nEdges, 1), n, n);
63
64 end % scale_free(...)

```

smallworld.m

```

1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %%% code adopted from %%%
3  %%% Modeling and Simulating Social Systems with MATLAB %%%
4  %%% http://www.soms.ethz.ch/teaching/MatlabFall2012 %%%
5  %%% Authors: Stefan Bruggen and Cristoph Schwirzer, 2011 %%%
6  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
7
8  function A = smallworld(n, k, beta)
9  % Generate a small world graph using the "Watts and Strogatz model" as
10 % described in Watts, D.J.; Strogatz, S.H.: "Collective dynamics of
11 % 'small-world' networks."
12 % A graph with n*k/2 edges is constructed, i.e. the nodal degree is n*k for
13 % every node.
14 %
15 % INPUT
16 % n: [1]: number of nodes of the graph to be generated
17 % k: [1]: mean degree (assumed to be an even integer)
18 % beta: [1]: rewiring probability
19 %
20 % OUTPUT
21 % A: [n n] sparse symmetric adjacency matrix representing the generated ...
    graph

```

```

22
23 % Construct a regular lattice: a graph with n nodes, each connected to k
24 % neighbors, k/2 on each side.
25 kHalf = k/2;
26 rows = reshape(repmat([1:n]', 1, k), n*k, 1);
27 columns = rows+reshape(repmat([1:kHalf] [n-kHalf:n-1]), n, 1), n*k, 1);
28 columns = mod(columns-1, n) + 1;
29 B = sparse(rows, columns, ones(n*k, 1));
30 A = sparse([], [], [], n, n);
31
32 % With probability beta rewire an edge avoiding loops and link duplication.
33 % Until step i, only the columns 1:i are generated making implicit use ...
    of A's
34 % symmetry.
35 for i = [1:n]
36     % The i-th column is stored full for fast access inside the ...
        following loop.
37     col= [full(A(i, 1:i-1))'; full(B(i:end, i))];
38     for j = i+find(col(i+1:end))'
39         if (rand()<beta)
40             col(j)=0;
41             k = randi(n);
42             while k==i || col(k)==1
43                 k = randi(n);
44             end
45             col(k) = 1;
46         end
47     end
48     A(:,i) = col;
49 end
50
51 % A is not yet symmetric: to speed things up, an edge connecting i and ...
    j, i < j
52 % implies A(i,j)==1, A(i,j) might be zero.
53 T = triu(A);
54 A = T+T';
55
56 end % small_world(...)

```

step1_caveman.m

```
1 function cave_mat = step1_caveman(n,m)
2 %%%%%%%%%%% This function outputs a Caveman Matrix %%%%%%%%%%%
3 %% n: the number of agents
4 %% m: initial number of clusters
5 %% p: initial maximum index of opinions
6 cave_mat=zeros(n,n); %Caveman Matrix
7
8 for i=1:n
9     x=ceil(i/(n/m));
10    for j=1:n
11        y=ceil(j/(n/m));
12        if x==y
13            if i≠j
14                cave_mat(i,j)=1; %definition of intracluster edges
15            end
16        end
17    end
18 end
19 %% x1 and x2 for each cluster represent the two agents who interact with
20 %% nearby clusters%%
21 x1=zeros(1,m);
22 x2=zeros(1,m);
23 for i=1:m
24     x1(i)=ceil(rand()*(n/m)+(n/m)*(i-1));
25     ind=0;
26     while(ind==0) %% This loop is used to prevent x1 and x2 to make the ...
27         same numbers
28         x2(i)=ceil(rand()*(n/m)+(n/m)*(i-1));
29         if x2(i)≠x1(i)
30             ind=1;
31         end
32     end
33 end
34 %% definition of intercluster edges
35 for i=1:(m-1)
36     cave_mat(x2(i),x1(i+1))=1;
37     cave_mat(x1(i+1),x2(i))=1;
38 end
39 cave_mat(x1(1),x2(m))=1;
40 cave_mat(x2(m),x1(1))=1;
41 end
```

step1_randomgraph.m

```
1
2
3 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
4 %%% code adopted from %%%
5 %%% Modeling and Simulating Social Systems with MATLAB %%%
6 %%% http://www.soms.ethz.ch/teaching/MatlabFall2012 %%%
7 %%% Authors: Stefan Brugger and Cristoph Schwirzer, 2011 %%%
8 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
9
10 function final= step1_randomgraph(n, p)
11 % Generates an undirected random graph (without self-loops) of size n (as
12 % described in the Erdoes-Renyi model)
13 %
14 % INPUT
15 % n: [1]: number of nodes
16 % p: [1]: probability that node i and node j, i != j, are connected by ...
    an edge
17 %
18 % OUTPUT
19 % final: [n n] full symmetric adjacency matrix representing the ...
    generated graph
20
21 % Note: A generation based on sprandsym(n, p) failed (for some values of p
22 % sprandsym was far off from the expected number of n*n*p non-zeros), ...
    therefore
23 % this longish implementation instead of just doing the following:
24 %
25 % B = sprandsym(n, p);
26 % A = (B-diag(diag(B))>0);
27 %
28
29 % Idea: first generate the number of non-zero values in every row for a ...
    general
30 % 0-1-adjacency matrix. For every row this number is distributed ...
    binomially with
31 % parameters n and p.
32 %
33 % The following lines calculate "rowsize = binoinv(rand(1, n), n, p)", ...
    just in a
34 % faster way for large values of n.
35
36 % generate a vector of n values chosen u.a.r. from (0,1)
37 v = rand(1, n);
38 % Sort them and calculate the binomial cumulative distribution function with
39 % parameters n and p at values 0 to n. Afterwards match the sorted random
40 % 0-1-values to those cdf-values, i.e. associate a binomial distributed ...
    value
```

```

41 % with each value in r. Each value in v also corresponds to a value in r:
42 % permute the values in rowSize s.t. they correspond to the order given ...
    in v.
43 [r index] = sort(v); % i.e. v(index) == r holds
44 rowSize = zeros(1, n);
45 j = 0;
46 binoCDF = cumsum(binopdf(0:n, n, p));
47 for i = 1:n
48     while j<n && binoCDF(j+1)<r(i)
49         j = j + 1;
50     end
51     rowSize(i) = j;
52 end
53 rowSize(index) = rowSize;
54
55 % for every row choose the non-zero entries in it
56 nNZ = sum(rowSize);
57 I = zeros(1, nNZ);
58 J = zeros(1, nNZ);
59 j = 1;
60 for i = 1:n
61     I(j:j+rowSize(i)-1) = i;
62     J(j:j+rowSize(i)-1) = randsample(n, rowSize(i));
63     j = j + rowSize(i);
64 end
65
66 % restrict I and J to indices that correspond to entries above the main ...
    diagonal
67 % and finally construct a symmetric sparse matrix using I and J
68 upperTriu = find(I<J);
69 I = I(upperTriu);
70 J = J(upperTriu);
71 A = sparse([I;J], [J;I], ones(1, 2*size(I, 2)), n, n);
72 final=full(A);
73 end % random_graph(...)

```

step1_scalefree.m

```
1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 %%% code adopted from %%%
3 %%% Modeling and Simulating Social Systems with MATLAB %%%
4 %%% http://www.soms.ethz.ch/teaching/MatlabFall2012 %%%
5 %%% Authors: Stefan Brugger and Cristoph Schwirzer, 2011 %%%
6 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
7
8 function final = step1_scalefree(n, m0, m)
9 % Use the Barabasi-Albert model to generate a scale free graph of size n (as
10 % described in Albert-Laszlo Barabasi & Reka Albert: "Emergence of scaling
11 % in random networks")
12 %
13 % INPUT
14 % n: [1]: number of nodes
15 % m0: [1]: number of initially placed nodes
16 % m: [1]: number of nodes a new added node is connected to,  $1 \leq m < m0$ 
17 %
18 % OUPUT
19 % final: [n n] full symmetric adjacency matrix representing the ...
    generated graph
20
21 % Start with a graph of size m0 and add edges to this graph. Each of ...
    these m0
22 % nodes is connected to at least m nodes.
23 B = zeros(m0, m0);
24 for i = 1:m0
25     neighbors = randsample(m0-1, m);
26     neighbors = neighbors + (neighbors>=i);
27     B(i,neighbors) = 1;
28     B(neighbors,i) = 1;
29 end
30
31 % Create a vector of edges added so far, i.e. nodes edge(2*i) and ...
    edge(2*i-1),
32 %  $1 \leq i \leq nEdges$ , are connected by an edge.
33 [rows, columns] = find(triu(B));
34 nEdges = size(rows, 1);
35 edges = reshape([rows';columns'], 2*nEdges, 1);
36 edges = [edges; zeros(2*(n-m0)*m,1)];
37
38 % Add nodes m0+1:n, one at a time. Each node is connected to m existing ...
    nodes,
39 % where each of the existing nodes is chosen with a probability that is
40 % proportional to the number of nodes it is already connected to.
41 used = zeros(n, 1); % is a node already used in a timestep?
42 for i = m0+1:n
43     neighbors = zeros(1, m);
```



```

44     for j=1:m
45         k = edges(randi(2*nEdges));
46         while used(k)
47             k = edges(randi(2*nEdges));
48         end
49         used(k) = 1;
50         neighbors(j) = k;
51     end
52     used(neighbors) = 0;
53     edges(2*nEdges+1:2*nEdges+2*m) = reshape([repmat(i, 1, m); ...
54         neighbors], ...
55         1, 2*m);
56     nEdges = nEdges+m;
57 end
58 % finally construct a symmetric adjacency matrix using the vector of edges
59 edges = edges(1:2*nEdges);
60 first = edges(1:2:end);
61 second = edges(2:2:end);
62 A = sparse([first;second], [second;first], ones(2*nEdges, 1), n, n);
63 final=full(A);
64 end % scale_free(...)

```

step1_smallworld.m

```

1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %%% code adopted from %%%
3  %%% Modeling and Simulating Social Systems with MATLAB %%%
4  %%% http://www.soms.ethz.ch/teaching/MatlabFall2012 %%%
5  %%% Authors: Stefan Brugger and Cristoph Schwirzer, 2011 %%%
6  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
7
8  function final = step1_smallworld(n, k, beta)
9  % Generate a small world graph using the "Watts and Strogatz model" as
10 % described in Watts, D.J.; Strogatz, S.H.: "Collective dynamics of
11 % 'small-world' networks."
12 % A graph with  $n*k/2$  edges is constructed, i.e. the nodal degree is  $n*k$  for
13 % every node.
14 %
15 % INPUT
16 % n: [1]: number of nodes of the graph to be generated
17 % k: [1]: mean degree (assumed to be an even integer)
18 % beta: [1]: rewiring probability
19 %
20 % OUTPUT
21 % A: [n n] sparse symmetric adjacency matrix representing the generated ...
    graph

```

```

22
23 % Construct a regular lattice: a graph with n nodes, each connected to k
24 % neighbors, k/2 on each side.
25 kHalf = k/2;
26 rows = reshape(repmat((1:n)', 1, k), n*k, 1);
27 columns = rows+reshape(repmat([(1:kHalf) (n-kHalf:n-1)], n, 1), n*k, 1);
28 columns = mod(columns-1, n) + 1;
29 B = sparse(rows, columns, ones(n*k, 1));
30 A = sparse([], [], [], n, n);
31
32 % With probability beta rewire an edge avoiding loops and link duplication.
33 % Until step i, only the columns 1:i are generated making implicit use ...
    of A's
34 % symmetry.
35 for i = 1:n
36     % The i-th column is stored full for fast access inside the ...
        following loop.
37     col= [full(A(i, 1:i-1))'; full(B(i:end, i))];
38     for j = i+find(col(i+1:end))'
39         if (rand()<beta)
40             col(j)=0;
41             k = randi(n);
42             while k==i || col(k)==1
43                 k = randi(n);
44             end
45             col(k) = 1;
46         end
47     end
48     A(:,i) = col;
49 end
50
51 % A is not yet symmetric: to speed things up, an edge connecting i and ...
    j, i < j
52 % implies A(i,j)==1, A(i,j) might be zero.
53 T = triu(A);
54 A = T+T';
55 final=sparse(A);
56
57 end % small_world(...)

```

A.3 Step 2: Rewiring process

step2.m

```
1 function [mat, vec, dominant_freq, most_freq] = ...
   step2(t_end, phi, alpha, mat, vec, p, threshold)
2 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% step2: Runing the Simulation %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
3 %%% t_end: number of iterations
4 %%% phi: network reorganization rate
5 %%% alpha: innovation rate
6 %%% mat: initial connectivity matrix
7 %%% vec: initial idea vector
8 %%% p: initial number of opinions
9 %%% then it outputs:
10 %%% mat: connectivity matrix after simulation
11 %%% vec: idea vector after simulation
12 %%% dominant_freq: the vector holding the frequency of dominant idea
13 %%% most_freq: the vector holding the index of dominating idea in each time
14
15 most_freq=zeros(1,t_end); %%% Vector for storing the index of the ...
   dominating idea in each time step.
16 dominant_freq=zeros(1,t_end); %%% Vector for storing the frequency of ...
   dominant idea in each time step.
17 a=size(mat);
18 n=a(1); %%% number of agents
19
20 for t=1:t_end
21     x1=ceil(rand()*n); %%% choosing one person randomly for network ...
   reorganization or changing idea
22     a1=rand();
23     b1=phi;
24     if a1<b1 %%% i.e with probability phi to reorganize the network
25         v00=find(mat(x1,:)==1); %%% defining neighbours of x1
26         v=find(vec(v00)~=vec(x1)); %%% define neighbours of x1 that do not ...
   have the same idea as x1
27         if ~isempty(v)
28             x2=v(ceil(rand()*length(v))); %%% choosing one neighbour with ...
   different idea randomly to remove connection with
29             mat(x1,x2)=0; %%% deletion of the edge between x1 and x2
30             mat(x2,x1)=0; %%% deletion of the edge between x2 and x1
31             similar_idea=find(vec==vec(x1)); %%% define the agents with ...
   the same idea as x1
32             non_neighbor_sim_idea=setdiff(similar_idea,v00); %%% the ...
   agents with similar idea as x1 who are not neighbor of x1
33             if ~isempty(non_neighbor_sim_idea)
34                 x3=non_neighbor_sim_idea(ceil(rand()*length(non_neighbor_sim_idea))); ...
   %%% choose x3 randomly among the agents with the same ...
   idea and non-neighbor with x1 as the newly connected ...
   agent to x
```

```

35         mat(x1,x3)=1; %%% formation of new edge between x1 and x3
36         mat(x3,x1)=1; %%% formation of new edge between x3 and x1
37     else %%% we'll forget about network reorganization in this ...
38         time by reforming the deleted edges.
39         mat(x1,x2)=1;
40         mat(x2,x1)=1;
41     end
42 end
43 else %%% otherwise change the idea of x1 to that of one of it's ...
44     randomly chosen neighbours
45     v2=find(mat(x1,:)==1); %%% defining the neighbours of x1
46     if ~isempty(v2)
47         vv=vec(v2); %%% the corresponding ideas of the neighbours
48         vvv=unique(vv); %%% vector of all the distinct ideas
49         freq=zeros(1,length(vvv)); %%% vector for frequencies of the ideas
50         for i=1:length(vvv) %%% to test for all distinct ideas
51             if length(find(vv==vvv(i)))>(threshold*length(v2)) ...
52                 %%%whether the frequency is larger than the threshold ...
53                 [To include complex contagion definition]
54                 freq(i)=1;
55             end
56         end
57         candidates=vvv(find(freq==1)); %%% The ideas meeting the threshold
58         candidates_size=length(candidates); %%% The number of ideas ...
59         meeting the threshold
60         if candidates_size>0
61             chosen=ceil(rand()*candidates_size); %%% Randomly choose one ...
62             of the candidates
63             vec(x1)=candidates(chosen); %%% change the idea of x1 to ...
64             the chosen idea
65         end
66     end
67 end
68 y=ceil(rand()*n); %%%choosing one person randomly for coming up with ...
69 a new idea
70 a2=rand();
71 b2=alpha;
72 if a2<b2 %%% i.e. with probability alpha to generate a novel idea
73     bound=10^6; %%% to limit the index of new ideas to 10^6 which ...
74     simulates nearly boundryless pool of ideas
75     new_idea=ceil(rand()*bound)+p; %%% the index of new idea
76     vec(y)=new_idea; %%% changing the idea of agent y to the novel one
77 end
78 %%%
79 most_freq(t)=mode(vec); %%% the dominant idea at time t
80 dominant_freq(t)=length(find(vec==most_freq(t))); %%% the frequency ...
81 of the dominant idea at time t
82 end

```

A.4 Step 3: Results

step3a.m

```

1 function n_index = step3a(mat,vec)
2 %%%%%%%%% step3a: defining the neighbourhood index between similar ideas ...
   %%%%%%%%%
3 %%% mat: adjacency matrix
4 %%% vec: idea vector
5 %%% it outputs: n_index which is the average neighbour index of the network
6 u=unique(vec); %%% collection of distinct ideas
7 w=zeros(1,length(u)); %%% initializing the vector for storing the ...
   neighbourhood index for each distinct idea
8 s=zeros(1,length(u)); %%% initializing the vector for storing the number ...
   of agents holding each distinct ideas
9 for i=1:length(u)
10     x=find(vec==u(i)); %%% defining the set of agents holding the idea u(i)
11     s(i)=length(x);
12     if s(i)>1
13         sum1=0; %%% number of agents with idea i which are in direct ...
            neighbourhood
14         for k=1:(s(i)-1) %%% These two for loops are used to test the ...
            neighborhoods of all distinct pairs
15             for j=(k+1):s(i)
16                 if mat(x(k),x(j))==1 %%% to check if they are neighbours
17                     sum1=sum1+1;
18                 end
19             end
20         end
21         max_neighbors=(s(i)*(s(i)-1)/2); %%% normalizing factor (i.e., the ...
            maximum number of pairs of distinct agents)
22         w(i)=sum1/max_neighbors; %%% neighborhood index for idea 'i'
23     else
24         w(i)=0;
25     end
26 end
27 norm1=sum(s); %%% Normalizing factor
28 count=sum(w.*s); %%% The weighted sum of neighborhood index
29 n_index=count/norm1; %%% average neighbour index of the whole network
30 end

```

steb3b.m

```

1 function intra_idea_distance = step3b(mat,vec,s,c)
2 %%%%%%%%%%% step3b: Defining the average of the average shortest ...
   distance between agents holding the same idea %%%%%%%%%%%
3 %%% mat: adjacency matrix
4 %%% vec: idea vector
5 %%% s: number of connected components
6 %%% c: vector which assigns each node to a connected component
7 %%% and it outputs the average of average intra_distance between agents
8 %%% holding the same idea %%%%%%%%%%%
9 unq=unique(vec); %%% collection of distinct ideas
10 mean_sum=zeros(1,length(unq)); %%% initializing the vector for storing ...
   the average distance between agents holding a particular idea
11 n=zeros(1,length(unq)); %%% initializing the corresponding vector for ...
   storing the number of agents holding a certain idea
12 mats=sparse(mat);
13
14 for i=1:length(unq)
15     x=find(vec==unq(i)); %%% defining the set of agents holding the ...
       idea unq(i)
16     n(i)=length(x); %%% number of agents holding the idea unq(i)
17     nn=zeros(1,s); %%% initializing the vector which will store the ...
       number of agents holding the idea unq(i) who belong to the m-th ...
       connected component
18     mean_sum0=zeros(1,s); %%% initializing the vector which stores the ...
       mean of the distances between agents holding the idea unq(i) who ...
       belong to each distinct connected component
19     for m=1:s %%% for each connected component
20         y=x(find(c(x)==m)); %%% the set of agents holding the idea ...
           unq(i) who belong to the m-th connected component
21         nn(m)=length(y); %%% number of agents holding the idea unq(i) ...
           who belong to the m-th connected component
22         sum0=0;
23         if nn(m)>1
24             for j=1:(nn(m)-1)
25                 for k=(j+1):nn(m)
26                     dis=graphshortestpath(mats,y(j),y(k)); %%% distance ...
                       of each agent with similar idea from agent j ...
                       inside the group [needs the bioinformatics ...
                       toolbox to be installed]
27                     sum0=sum0+dis; %%% sum of the distances between ...
                       agents holding the idea unq(i) who belong to m-th ...
                       connected component
28                 end
29             end
30             norml0=nn(m)*(nn(m)-1)/2; %%% normalizing factor
31             mean_sum0(m)=sum0/norml0; %%% The average intra-idea distance ...
               between agents holding the idea unq(i) who belong to the ...

```

```

                                m-th connected component
32         else
33             mean_sum0(m)=0;
34         end
35     end
36
37     if n(i)>1
38         mean_sum(i)=(sum(mean_sum0.*nn))/(sum(nn)); %% The average ...
                                intra_idea distance between agents holding the idea unq(i)
39     else
40         mean_sum(i)=0;
41     end
42 end
43
44 intra_idea_distance=(sum(mean_sum.*n))/(sum(n)); %% The average ...
                                intra_idea distance for the whole network
45 end

```

step3e.m

```

1 function [ average_dominance_time ] = step3e( most_freq )
2 %%%% this function calculates the average of dominance time for the ...
                                dominating idea during the simulation
3 %%%% most_freq: is the vector obtained from simulation which holds the ...
                                index of dominating ideas for each time steps of the simulation
4 %%%% it outputs the average_time which is the average of the dominance ...
                                time for different dominance periods
5 temp=zeros(1,length(most_freq)); %% a temporary array which will hold ...
                                the dominating period for dominating idea
6 count=1; %% is the number of consecutive time steps in which an idea is ...
                                considered as dominating
7 ind=0; %% is the index of domination period
8 for i=2:length(most_freq)
9     if most_freq(i)==most_freq(i-1)
10         count=count+1; %% the number of consecutive steps is conted
11     else
12         ind=ind+1; %% as soon as another domination period gets tarted ...
                                the index of domination period adds by one
13         temp(ind)=count; %% the number of consecutive steps will be ...
                                stored in the ind-th index of tmp
14         count=0; %% and count will be reset to zero to count the ...
                                duration of the new domination period.
15     end
16 end
17
18 if ind==0 %% in case during the simulation, just one special idea ...
                                remains dominating forever

```

```

19     ind=ind+1;
20     temp(ind)=count;
21 end
22
23 %%% from ind-th element till end the temp vector will remain zero we ...
    define a new vector as follows to store the corresponding non-zero ...
    elements of temp
24 final=zeros(1,ind);
25 for j=1:ind
26     final(j)=temp(j);
27 end
28 average_dominance_time=mean(final);
29 end

```

step4a.m

```

1
2 function clust_coeff = step4a( mat )
3 % This function calculates the clustering coefficient of a network with
4 % Corresponding connectivity matrix: mat
5 % The approach used for calculation of clustering coefficient was the one ...
    which was proposed by Watts and Strogatz
6 % in which the clustering coefficient of the whole network equals to the
7 % average of the local clustering coefficient of all nodes:
8 % D. J. Watts and Steven Strogatz (June 1998). "Collective dynamics of ...
    'small-world' networks". Nature 393 (6684): 440 442.
9 a=size(mat);
10 local_clust_coeff=zeros(1,a(1)); %%% the vector to store the local ...
    clustering coefficient of each node of the network
11 for i=1:a(1) %%% for each agent in the network
12     x=find(mat(i,:)==1); %%% find all the neighbours of agent i
13     count=0;
14     l=length(x);
15     if l>1
16         for j=1:(l-1) %%% loop to investigate the neighbour relationship for ...
            all possible pairs among the neighbors of node i
17             for k=(j+1):l
18                 if mat(x(j),x(k))==1
19                     count=count+1; % to count the number of neighbour ...
                        relationships
20                 end
21             end
22         end
23         norml=1*(l-1)/2; % normalizing factor (i.e. the number of distinct ...
            pairs)
24         local_clust_coeff(i)=count/norml; % local clustering coefficient of ...
            node i

```



```

25     else
26         local_clust_coeff(i)=0;
27     end
28 end
29 clust_coeff=sum(local_clust_coeff)/a(1); %% the average clustering ...
        coefficient of entire network
30 end

```

step4b.m

```

1 function [dgr,frq] = step4b(mat)
2 %%% this function outputs the degree vector (dgr) and its corresponding
3 %%% frequency vector (frq) from the connectivity matrix (mat). In other ...
    words,
4 %%% first the degree of all nodes in the network will be calculated and
5 %%% then the set of unique degrees will be stored in the dgr vector and the
6 %%% corresponding frequency will be stored in vector frq. For example,
7 %%% degree x will be stored in the i-th element of the dgr vector, then ...
    the number of nodes whose degree equals x
8 %%% will be calculated and will be stored in the i-th element of vector frq.
9 a=size(mat);
10 degr=zeros(1,a(1)); %% the vector which stores the degree of each node ...
    of the network
11 for i=1:a(1)
12     degr(i)=sum(mat(i,:)); %% degree for each node
13 end
14 degr=unique(degr); %% set of unique degrees of the nodes of the network
15 frq=zeros(1,length(dgr)); %% the corresponding frequency vector
16 for j=1:length(dgr)
17     frq(j)=length(find(degr==dgr(j))); %% frq(j) is the number of nodes ...
        in the network whose degree equals to dgr(j)
18 end
19
20 end

```

step4d.m

```
1 function average_path_length = step4d( mat,s,c )
2 %This function outputs the average path length for the graph
3 %mat: connectivity matrix
4 %s: number of connected components
5 %c: the connected component vector
6 av_p_l=zeros(1,s); %%% the vector which will store the average path ...
    length for each connected component of the 'mat' network
7 n=zeros(1,s); %%% the vector which will store the number of nodes ...
    belonging to each connected component.
8 sp=sparse(mat);
9
10 for i=1:s %%% for each connected component
11     x=find(c==i); %%% characterizing the nodes which belong to the i-th ...
        connected component
12     a=length(x); %%% the number of nodes in the i-th connected component
13     n(i)=a;
14     count=0;
15     if a>1
16         for k=1:(a-1)
17             for j=(k+1):a
18                 count=count+graphshortestpath(sp,x(k),x(j)); %%% sum of the path ...
                    length between all pairs of node
19             end
20         end
21         norml=a*(a-1)/2; %%% normalization factor
22         av_p_l(i)=count/norml; %%% average of path length
23     else
24         av_p_l(i)=0;
25     end
26 end
27 average_path_length=sum(av_p_l.*n)/sum(n); %%% weighted average path length
28 end
```

step4e.m

```
1 function graph.diameter = step4e( mat,s,c )
2 %This function outputs the diameter of the graph 'mat'
3 %mat: connectivity matrix
4 %s: number of connected components
5 %c: the connected component vector
6 sp=sparse(mat);
7 max_path=zeros(1,s); %% vector storing diameter for each connected ...
   components.
8 for i=1:s %% for each connected component
9     x=find(c==i); %% characterizing the nodes which belong to the i-th ...
       connected component
10    a=length(x); %% the number of nodes in the i-th connected component
11    path_length=zeros(1,(a*(a-1)/2)); %% The vector storing the ...
       shortest path between each pairs of nodes belonging to the ...
       connected component i
12    count=0;
13    if a>1
14        for k=1:(a-1)
15            for j=(k+1):a
16                count=count+1;
17                path_length(count)=graphshortestpath(sp,x(k),x(j)); %% the ...
                   vector storing the shortest path between pairs k and j
18            end
19        end
20        max_path(i)=max(path_length); %% the maximum shortest path for ...
           connected component i
21    else
22        max_path(i)=0;
23    end
24 end
25 graph.diameter=max(max_path); %% the maximum shortest path for the hole ...
   network (Diameter of the network)
26 end
```

A.5 Plote codes

plots_phase1.m

```
1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Plots of phase 1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %%%
3  %%% Extracting information from the saved Mat files %%%
4  neighbor_ind=zeros(1,108);
5  int_id_dis=zeros(1,108);
6  nov_ind=zeros(1,108);
7  av_dom_tim=zeros(1,108);
8  dom_freq=zeros(108,1000);
9  alpha=[0.01,0.05,0.1];
10 phi=[0.1,0.3,0.5];
11 threshold=[0.001,0.01,0.05];
12 count=0;
13 f=figure();
14 for i=1:4
15     switch i
16         case 1
17             s1='Caveman';
18         case 2
19             s1='Random';
20         case 3
21             s1='Scale-free';
22         case 4
23             s1='Small-world';
24     end
25     for j=1:3
26         s2=int2str(j);
27         for k=1:3
28             s3=int2str(k);
29             for l=1:3
30                 count=count+1;
31                 s4=int2str(l);
32                 name=['phase1_',s1,'_',s2,'_',s3,'_',s4];
33                 a=load(name);
34                 neighbor_ind(count)=a.neighbor_index;
35                 int_id_dis(count)=a.intra_idea_distance;
36                 nov_ind(count)=a.nov_index;
37                 av_dom_tim(count)=a.average_dominance_time;
38                 dom_freq(count,:)=a.dominant_freq;
39             end
40         end
41     end
42 end
43
44 %%% phase diagrams for each parameter pairs for the results of the effects
45 %%% of network structure on idea distribution.
```

```

46
47 for i=1:4
48     switch i
49         case 1
50             s1='Caveman';
51             val=0;
52         case 2
53             s1='Random';
54             val=27;
55         case 3
56             s1='Scale free';
57             val=54;
58         case 4
59             s1='Small world';
60             val=81;
61     end
62     for j=1:4
63         switch j
64             case 1
65                 s2='neighbor index';
66                 main_vec=neighbor_ind;
67             case 2
68                 s2='intra idea distance';
69                 main_vec=int_id_dis;
70             case 3
71                 s2='nov index';
72                 main_vec=nov_ind;
73             case 4
74                 s2='average dominance time';
75                 main_vec=av_dom_tim;
76         end
77         for k=1:3
78             switch k
79                 case 1
80                     s3='(alpha:phi)';
81                     x=0:0.5:1;
82                     xl='alpha';
83                     y=0:0.5:1;
84                     yl='phi';
85                     for l=1:3
86                         M=[main_vec(val+l),main_vec(val+l+9),main_vec(val+l+18);
87                             main_vec(val+l+3),main_vec(val+l+12),main_vec(val+l+21)
88                             ];main_vec(val+l+6),main_vec(val+l+15),main_vec(val+l+24)];
89                         %
90                         [xlab,ylab]=meshgrid(x,y);
91                         hold on;
92                         view(0,90);
93                         surf(xlab,ylab,M,'EdgeColor','none');
94                         colorbar;
95                         set(gca,'FontSize',14)

```

```

96         xlabel(xl);
97         ylabel(yl);
98         switch l
99             case 1
100                 s5='first';
101             case 2
102                 s5='second';
103             case 3
104                 s5='third';
105         end
106         name2=['phase diagram of ',s2,' for alpha versus phi','
107             and','the', s5,' threshold','obtained for',s1,'network
108             structure'];
109         title(name2);
110         name=['plotting1-', 'Pdiag-',s1,'-',s2,'-',s3,'-',s4,
111             'AND','the', s5,' threshold'];
112         saveas(f,name);
113         hold off
114         %
115     end
116     case 2
117         s3='(alpha:threshold)';
118         x=0:0.5:1;
119         xl='alpha';
120         y=0:0.5:1;
121         yl='threshold';
122         for l=1:3
123             M=[main_vec(val+9*(l-1)+1),main_vec(val+9*(l-1)+2),
124                 main_vec(val+9*(l-1)+3),main_vec(val+9*(l-1)+4),
125                 main_vec(val+9*(l-1)+5),main_vec(val+9*(l-1)+6),
126                 main_vec(val+9*(l-1)+7),main_vec(val+9*(l-1)+8),
127                 main_vec(val+9*(l-1)+9)];
128             %
129             [xlab,ylab]=meshgrid(x,y);
130             hold on;
131             view(0,90);
132             surf(xlab,ylab,M,'EdgeColor','none');
133             colorbar;
134             set(gca,'FontSize',14)
135             xlabel(xl);
136             ylabel(yl);
137             switch l
138                 case 1
139                     s5='first';
140                 case 2
141                     s5='second';
142                 case 3
143                     s5='third';
144             end
145             name2=['phase diagram of ',s2,' for alpha versus threshold

```

```

146         ',' and', 'the', s5, ' phi', 'obtained for', s1, 'network
147         structure'];
148     title(name2);
149     name=['plotting1_', 'Pdiag_', s1, '-', s2, '-', s3, '-', s4, '
150         and', 'the', s5, ' phi'];
151     saveas(f, name);
152     hold off
153     %
154 end
155
156 case 3
157 s3='(phi:threshold)';
158 x=0:0.5:1;
159 xl='phi';
160 y=0:0.5:1;
161 yl='threshold';
162 for l=1:3
163     M=[main_vec(val+3*(l-1)+1), main_vec(val+3*(l-1)+2),
164         main_vec(val+3*(l-1)+3), main_vec(val+3*(l-1)+10),
165         main_vec(val+3*(l-1)+11), main_vec(val+3*(l-1)+12);
166         main_vec(val+3*(l-1)+19), main_vec(val+3*(l-1)+20),
167         main_vec(val+3*(l-1)+21)];
168     %
169     [xlab, ylab]=meshgrid(x, y);
170     hold on;
171     view(0, 90);
172     surf(xlab, ylab, M, 'EdgeColor', 'none');
173     colorbar;
174     set(gca, 'FontSize', 14)
175     xlabel(xl);
176     ylabel(yl);
177     switch l
178     case 1
179         s5='first';
180     case 2
181         s5='second';
182     case 3
183         s5='third';
184     end
185     name2=['phase diagram of ', s2, ' for phi versus threshold'
186         , ' and', 'the', s5, ' threshold', 'obtained for', s1,
187         'network structure'];
188     title(name2);
189     name=['plotting1_', 'Pdiag_', s1, '-', s2, '-', s3, '-', s4,
190         ' and', 'the', s5, ' threshold'];
191     saveas(f, name);
192     hold off
193     %
194 end
195 end

```

```

196         end
197     end
198 end
199
200 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
201 %% Dependence of the property of each network to the parameters
202
203 for i=1:4
204     switch i
205     case 1
206         s1='Caveman';
207         val=0;
208     case 2
209         s1='Random';
210         val=27;
211     case 3
212         s1='Scale free';
213         val=54;
214     case 4
215         s1='Small world';
216         val=81;
217     end
218     for j=1:4
219         switch j
220         case 1
221             s2='neighborhood index';
222             main_vec=neighbor_ind;
223         case 2
224             s2='intra idea distance';
225             main_vec=int_id_dis;
226         case 3
227             s2='novelty index';
228             main_vec=nov_ind;
229         case 4
230             s2='average dominance time';
231             main_vec=av_dom_tim;
232         end
233         for k=1:3
234             switch k
235             case 1
236                 s3='threshold';
237                 f=figure();
238                 for l=1:3
239                     line=main_vec(3*(0:8)+val+1);
240                     set(gca,'FontSize',14)
241                     xlabel('Different pairs of alpha and phi values');
242                     ylabel(s2);
243                     namek=['Dependence of',' ',s2,' ','on',' ',s3,'
244                             ','for',' ',s1,' ','network structure'];
245                     title(namek);

```



```

246
247         switch 1
248             case 1
249                 plot(line, '--ks', 'LineWidth', 2,
250                     'MarkerEdgeColor', 'k', 'MarkerFaceColor',
251                     'k', 'MarkerSize', 5)
252                 hold on
253             case 2
254                 plot(line, '--bs', 'LineWidth', 2,
255                     'MarkerEdgeColor', 'b', 'MarkerFaceColor',
256                     'b', 'MarkerSize', 5)
257                 hold on
258             case 3
259                 plot(line, '--rs', 'LineWidth', 2,
260                     'MarkerEdgeColor', 'r', 'MarkerFaceColor',
261                     'r', 'MarkerSize', 5)
262         end
263         legend('threshold=0.001', 'threshold=0.01',
264             'threshold=0.05')
265         name=['plotting1_', s1, '-', s2, '-',
266             'threshold_sensitivity'];
267         saveas(f, name);
268     end
269
270 case 2
271     s3='alpha';
272     f=figure();
273     for l=1:3
274         line=main_vec([1,2,3,10,11,12,19,20,21]+val+3*(l-1));
275         set(gca, 'FontSize', 14)
276         xlabel('Different pairs of threshold and phi ...
277             values');
278         ylabel(s2);
279         namek=['Dependence of', ' ', s2, ' ', 'on', ' ', s3, ' ',
280             'for', ' ', s1, ' ', 'network structure'];
281         title(namek);
282
283         switch 1
284             case 1
285                 plot(line, '--ks', 'LineWidth', 2,
286                     'MarkerEdgeColor', 'k', 'MarkerFaceColor',
287                     'k', 'MarkerSize', 5)
288                 hold on
289             case 2
290                 plot(line, '--bs', 'LineWidth', 2,
291                     'MarkerEdgeColor', 'b', 'MarkerFaceColor',
292                     'b', 'MarkerSize', 5)
293                 hold on
294             case 3
295                 plot(line, '--rs', 'LineWidth', 2,

```

```

295             'MarkerEdgeColor','r','MarkerFaceColor',
296             'r','MarkerSize',5)
297         end
298         legend('alpha=0.01','alpha=0.05','alpha=0.10')
299         name=['plotting1-',s1,'-',s2,'-',
300             'alpha.sensitivity'];
301         saveas(f,name);
302     end
303
304     case 3
305         s3='phi';
306         f=figure();
307         for l=1:3
308             line=main_vec((1:9)+val+9*(l-1));
309             set(gca,'FontSize',14)
310             xlabel('Different pairs of threshold and alpha ...
311                 values');
312             ylabel(s2);
313             namek=['Dependence of',' ',s2,' ','on',' ',s3,' ',
314                 'for',' ',s1,' ','network structure'];
315             title(namek);
316
317             switch l
318                 case 1
319                     plot(line,'—ks','LineWidth',2,
320                         'MarkerEdgeColor','k',
321                         'MarkerFaceColor','k','MarkerSize',5)
322                     hold on
323                 case 2
324                     plot(line,'—bs','LineWidth',2,
325                         'MarkerEdgeColor','b','MarkerFaceColor',
326                         'b','MarkerSize',5)
327                     hold on
328                 case 3
329                     plot(line,'—rs','LineWidth',2,
330                         'MarkerEdgeColor','r','MarkerFaceColor',
331                         'r','MarkerSize',5)
332             end
333             legend('phi=0.1','phi=0.3','phi=0.5')
334             name=['plotting1-',s1,'-',s2,'-', 'phi.sensitivity'];
335             saveas(f,name);
336         end
337     end
338 end
339 end
340
341 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Plotting each network feature for each set of
342 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% parameters %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
343 for i=1:4

```

```

344     switch i
345         case 1
346             f=figure();
347             line1=neighbor_ind(1:27);
348             line2=neighbor_ind(28:54);
349             line3=neighbor_ind(55:81);
350             line4=neighbor_ind(82:108);
351             plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
352                 'MarkerFaceColor','k','MarkerSize',5)
353             hold on
354             plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
355                 'MarkerFaceColor','g','MarkerSize',5)
356             hold on
357             plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
358                 'MarkerFaceColor','b','MarkerSize',5)
359             hold on
360             plot(line4,'—rs','LineWidth',2,'MarkerEdgeColor','r',
361                 'MarkerFaceColor','r','MarkerSize',5)
362             set(gca,'FontSize',14)
363             xlabel('Different triplets of alpha ,phi and threshold values')
364             ylabel('Neighborhood index')
365             title('The influence of network structure on neighborhood
366                 index');
367             legend('Caveman Network','Random Network','Scale Free Network',
368                 'Small World Network')
369             name=('Plotting1_Network Comparison_Neighborhood_index');
370             saveas(f,name);
371         case 2
372             f=figure();
373             line1=int_id_dis(1:27);
374             line2=int_id_dis(28:54);
375             line3=int_id_dis(55:81);
376             line4=int_id_dis(82:108);
377             plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
378                 'MarkerFaceColor','k','MarkerSize',5)
379             hold on
380             plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
381                 'MarkerFaceColor','g','MarkerSize',5)
382             hold on
383             plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
384                 'MarkerFaceColor','b','MarkerSize',5)
385             hold on
386             plot(line4,'—rs','LineWidth',2,'MarkerEdgeColor','r',
387                 'MarkerFaceColor','r','MarkerSize',5)
388             set(gca,'FontSize',14)
389             xlabel('Different triplets of alpha ,phi and threshold values')
390             ylabel('Intra-idea distance')
391             title('The influence of network structure on intra-idea ...
392                 distance')
392             legend('Caveman Network','Random Network','Scale Free Network',

```

```

393         'Small World Network')
394     name=('Plotting1_Network Comparison_intra_idea_distance');
395     saveas(f,name);
396 case 3
397     f=figure();
398     line1=nov_ind(1:27);
399     line2=nov_ind(28:54);
400     line3=nov_ind(55:81);
401     line4=nov_ind(82:108);
402     plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
403          'MarkerFaceColor','k','MarkerSize',5)
404     hold on
405     plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
406          'MarkerFaceColor','g','MarkerSize',5)
407     hold on
408     plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
409          'MarkerFaceColor','b','MarkerSize',5)
410     hold on
411     plot(line4,'—rs','LineWidth',2,'MarkerEdgeColor','r',
412          'MarkerFaceColor','r','MarkerSize',5)
413     set(gca,'FontSize',14)
414     xlabel('Different triplets of alpha ,phi and threshold values')
415     ylabel('Novelty Index')
416     title('The influence of network structure on Novelty index')
417     legend('Caveman Network','Random Network','Scale Free Network',
418           'Small World Network')
419     name=('Plotting1_Network Comparison_intra_novelty_index');
420     saveas(f,name);
421 case 4
422     f=figure();
423     line1=av_dom_tim(1:27);
424     line2=av_dom_tim(28:54);
425     line3=av_dom_tim(55:81);
426     line4=av_dom_tim(82:108);
427     plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
428          'MarkerFaceColor','k','MarkerSize',5)
429     hold on
430     plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
431          'MarkerFaceColor','g','MarkerSize',5)
432     hold on
433     plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
434          'MarkerFaceColor','b','MarkerSize',5)
435     hold on
436     plot(line4,'—rs','LineWidth',2,'MarkerEdgeColor','r',
437          'MarkerFaceColor','r','MarkerSize',5)
438     set(gca,'FontSize',14)
439     xlabel('Different triplets of alpha ,phi and threshold values')
440     ylabel('Average Dominance Time')
441     title('The influence of network structure on Average Dominance
442           Time')

```

```

443         legend('Caveman Network','Random Network','Scale Free Network',
444               'Small World Network')
445         name=('Plotting1_Network Comparison_Average Dominance Time');
446         saveas(f,name);
447     end
448 end
449
450
451 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% plotting frequency of dominant idea over time for each
452 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% parameter sets %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
453 count=0;
454 for choice1=1:3
455     switch choice1
456     case 1
457         s1='phi=0.1';
458         m1='1';
459     case 2
460         s1='phi=0.3';
461         m1='2';
462     case 3
463         s1='phi=0.5';
464         m1='3';
465     end
466
467     for choice2=1:3
468         switch choice2
469         case 1
470             s2='alpha=0.01';
471             m2='1';
472         case 2
473             s2='alpha=0.05';
474             m2='2';
475         case 3
476             s2='alpha=0.1';
477             m2='3';
478         end
479
480         for choice3=1:3
481             switch choice3
482             case 1
483                 s3='threshold=0.001';
484                 m3='1';
485             case 2
486                 s3='threshold=0.01';
487                 m3='2';
488             case 3
489                 s3='threshold=0.05';
490                 m3='3';
491             end
492             count=count+1;

```

```

493     line1=dom_freq(count,:);
494     line2=dom_freq(27+count,:);
495     line3=dom_freq(54+count,:);
496     line4=dom_freq(81+count,:);
497     f=figure();
498     plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
499          'MarkerFaceColor','k','MarkerSize',5)
500     hold on
501     plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
502          'MarkerFaceColor','g','MarkerSize',5)
503     hold on
504     plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
505          'MarkerFaceColor','b','MarkerSize',5)
506     hold on
507     plot(line4,'—rs','LineWidth',2,'MarkerEdgeColor','r',
508          'MarkerFaceColor','r','MarkerSize',5)
509     set(gca,'FontSize',14)
510     xlabel('time')
511     ylabel('Frequency of the dominant idea')
512     title(['The influence of network structure on the frequency
513           of the dominant idea',' ',s1,' ',s2,' ',s3]);
514     legend('Caveman Network','Random Network','Scale Free Network',
515           'Small World Network')
516     name=(['Plotting1_Network_Comparison_frequency_dominant_idea-
517           ',m1,'_',m2,'_',m3]);
518     saveas(f,name);
519     end
520 end
521 end

```

plots_phase2.m

```
1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% Plots of phase 2 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %%
3  %% Extracting information from the saved Mat files %%%%%%%%%
4  %%%
5  clust_coefficient=zeros(1,81);
6  s=zeros(1,81);
7  average_path_length=zeros(1,81);
8  diam=zeros(1,81);
9  dgr=cell(1,81);
10 frq=cell(1,81);
11 alpha=[0.01,0.05,0.1];
12 phi=[0.1,0.3,0.5];
13 threshold=[0.001,0.01,0.05];
14
15 count=0;
16
17 for i=1:3
18     switch i
19         case 1
20             s1='Random';
21         case 2
22             s1='Parallel';
23         case 3
24             s1='Antiparallel';
25     end
26     for j=1:3
27         s2=int2str(j);
28         for k=1:3
29             s3=int2str(k);
30             for l=1:3
31                 count=count+1;
32                 s4=int2str(l);
33                 name=['phase2-',s1,'_',s2,'_',s3,'_',s4];
34                 a=load(name);
35                 clust_coefficient(count)=a.clust_coefficient;
36                 s(count)=a.s;
37                 average_path_length(count)=a.average_path_length;
38                 diam(count)=a.diam;
39                 dgr{1,count}=a.dgr;
40                 frq{1,count}=a.frq;
41             end
42         end
43     end
44 end
45
46 f=figure();
47
```

```

48  %%% phase diagrams for each parameter pairs for the results of the effects
49  %%% of idea distribution on network structure.
50
51  for i=1:3
52      switch i
53          case 1
54              s1='Random';
55              val=0;
56          case 2
57              s1='Parallel';
58              val=27;
59          case 3
60              s1='Antiparallel';
61              val=54;
62      end
63      for j=1:4
64          switch j
65              case 1
66                  s2='Clusteing Coefficient';
67                  main_vec=clust_coefficient;
68              case 2
69                  s2='Number of connected components';
70                  main_vec=s;
71              case 3
72                  s2='Average path length';
73                  main_vec=average_path_length;
74              case 4
75                  s2='Network diameter';
76                  main_vec=diam;
77          end
78          for k=1:3
79              switch k
80                  case 1
81                      s3='(alpha:phi)';
82                      x=0:0.5:1;
83                      xl='alpha';
84                      y=0:0.5:1;
85                      yl='phi';
86                      for l=1:3
87                          M=[main_vec(val+l),main_vec(val+l+9),main_vec(val+l+18)
88                              ;main_vec(val+l+3),main_vec(val+l+12),
89                              main_vec(val+l+21)
90                              ;main_vec(val+l+6),main_vec(val+l+15),
91                              main_vec(val+l+24)];
92                          %
93                          [xlab,ylab]=meshgrid(x,y);
94                          hold on;
95                          view(0,90);
96                          surf(xlab,ylab,M,'EdgeColor','none');
97                          colorbar;

```



```

98         set(gca,'FontSize',14)
99         xlabel(xl);
100        ylabel(yl);
101        switch l
102            case 1
103                s5='first';
104            case 2
105                s5='second';
106            case 3
107                s5='third';
108        end
109        name2=['phase diagram of ',s2,' for alpha versus phi',
110            ' and','the', s5,' threshold','obtained for',s1,
111            'idea distribution'];
112        title(name2);
113        name=['Plotting2_', 'Pdiag_',s1,'_',s2,'_',s3,'_',s4,
114            'AND','the', s5,' threshold'];
115        saveas(f,name);
116        hold off
117        %
118    end
119    case 2
120        s3='(alpha:threshold)';
121        x=0:0.5:1;
122        xl='alpha';
123        y=0:0.5:1;
124        yl='threshold';
125        for l=1:3
126            M=[main_vec(val+9*(l-1)+1),main_vec(val+9*(l-1)+2),
127                main_vec(val+9*(l-1)+3);main_vec(val+9*(l-1)+4),
128                main_vec(val+9*(l-1)+5),main_vec(val+9*(l-1)+6);
129                main_vec(val+9*(l-1)+7),main_vec(val+9*(l-1)+8),
130                main_vec(val+9*(l-1)+9)];
131            %
132            [xlab,ylab]=meshgrid(x,y);
133            hold on;
134            view(0,90);
135            surf(xlab,ylab,M,'EdgeColor','none');
136            colorbar;
137            set(gca,'FontSize',14)
138            xlabel(xl);
139            ylabel(yl);
140            switch l
141                case 1
142                    s5='first';
143                case 2
144                    s5='second';
145                case 3
146                    s5='third';
147            end

```

```

148     name2=['phase diagram of ',s2,' for alpha versus
149           threshold',
150           ' and','the', s5,' phi','obtained for',s1,
151           'idea distribution'];
152     title(name2);
153     name=['Plotting2-','Pdiag-',s1,'-',s2,'-',s3,'-',s4,
154           ' and','the', s5,' phi'];
155     saveas(f,name);
156     hold off
157     %
158 end
159
160 case 3
161     s3='(phi:threshold)';
162     x=0:0.5:1;
163     xl='phi';
164     y=0:0.5:1;
165     yl='threshold';
166     for l=1:3
167         M=[main_vec(val+3*(l-1)+1),main_vec(val+3*(l-1)+2),
168            main_vec(val+3*(l-1)+3);main_vec(val+3*(l-1)+10),
169            main_vec(val+3*(l-1)+11),main_vec(val+3*(l-1)+12);
170            main_vec(val+3*(l-1)+19),main_vec(val+3*(l-1)+20),
171            main_vec(val+3*(l-1)+21)];
172         %
173         [xlab,ylab]=meshgrid(x,y);
174         hold on;
175         view(0,90);
176         surf(xlab,ylab,M,'EdgeColor','none');
177         colorbar;
178         set(gca,'FontSize',14)
179         xlabel(xl);
180         ylabel(yl);
181         switch l
182             case 1
183                 s5='first';
184             case 2
185                 s5='second';
186             case 3
187                 s5='third';
188         end
189     name2=['phase diagram of ',s2,' for phi versus threshold',
190           ' and','the', s5,' threshold','obtained for',s1,
191           'idea distribution'];
192     title(name2);
193     name=['Plotting2-','Pdiag-',s1,'-',s2,'-',s3,'-',s4,
194           ' and','the', s5,' threshold'];
195     saveas(f,name);
196     hold off
197     %

```

```

198         end
199     end
200 end
201 end
202 end
203
204 %%% Dependence of the property of each network to the parameters
205
206 for i=1:3
207
208     switch i
209     case 1
210         s1='Random';
211         val=0;
212     case 2
213         s1='Parallel';
214         val=27;
215     case 3
216         s1='Antiparallel';
217         val=54;
218     end
219
220     for j=1:4
221         switch j
222         case 1
223             s2='clust_coefficient';
224             main_vec=clust_coefficient;
225         case 2
226             s2='s';
227             main_vec=s;
228         case 3
229             s2='average_path_length';
230             main_vec=average_path_length;
231         case 4
232             s2='diam';
233             main_vec=diam;
234         end
235         for k=1:3
236             switch k
237             case 1
238                 s3='threshold';
239                 f=figure();
240                 for l=1:3
241                     line=main_vec(3*(0:8)+val+1);
242                     set(gca,'FontSize',14)
243                     xlabel('Different pairs of alpha and phi values');
244                     ylabel(s2);
245                     namek=['Dependence of',' ',s2,' ','on',' ',s3,' ',
246                             'for',' ',s1,' ','idea distribution'];
247                     title(namek);

```

```

248
249         switch 1
250             case 1
251                 plot(line, '--ks', 'LineWidth', 2,
252                     'MarkerEdgeColor', 'k', 'MarkerFaceColor',
253                     'k', 'MarkerSize', 5)
254                 hold on
255             case 2
256                 plot(line, '--bs', 'LineWidth', 2,
257                     'MarkerEdgeColor', 'b', 'MarkerFaceColor',
258                     'b', 'MarkerSize', 5)
259                 hold on
260             case 3
261                 plot(line, '--rs', 'LineWidth', 2,
262                     'MarkerEdgeColor', 'r', 'MarkerFaceColor',
263                     'r', 'MarkerSize', 5)
264             end
265             legend('threshold=0.001', 'threshold=0.01',
266                   'threshold=0.05')
267             name=['plotting1_', s1, '-', s2, '-',
268                  'threshold_sensitivity'];
269             saveas(f, name);
270         end
271
272     case 2
273         s3='alpha';
274         f=figure();
275         for l=1:3
276             line=main_vec([1,2,3,10,11,12,19,20,21]+val+3*(l-1)
277                           );
278             set(gca, 'FontSize', 14)
279             xlabel('Different pairs of threshold and phi values
280                   ');
281             ylabel(s2);
282             namek=['Dependence of', ' ', s2, ' ', 'on', ' ', ' ', s3, ' ',
283                   'for', ' ', s1, ' ', 'idea distribution'];
284             title(namek);
285
286             switch 1
287                 case 1
288                     plot(line, '--ks', 'LineWidth', 2,
289                         'MarkerEdgeColor', 'k', 'MarkerFaceColor',
290                         'k', 'MarkerSize', 5)
291                     hold on
292                 case 2
293                     plot(line, '--bs', 'LineWidth', 2,
294                         'MarkerEdgeColor', 'b', 'MarkerFaceColor',
295                         'b', 'MarkerSize', 5)
296                     hold on
297                 case 3

```

```

298         plot(line,'--rs','LineWidth',2,
299               'MarkerEdgeColor','r','MarkerFaceColor',
300               'r','MarkerSize',5)
301     end
302     legend('alpha=0.01','alpha=0.05','alpha=0.10')
303     name=['plotting1-',s1,'-',s2,'-', 'alpha.sensitivity
304           '];
305     saveas(f,name);
306 end
307
308 case 3
309     s3='phi';
310     f=figure();
311     for l=1:3
312         line=main_vec((1:9)+val+9*(l-1));
313         set(gca,'FontSize',14)
314         xlabel('Different pairs of threshold and alpha
315               values');
316         ylabel(s2);
317         namek=['Dependence of',' ',s2,' ','on',' ',s3,'
318               ','for',' ',s1,' ','idea distribution'];
319         title(namek);
320
321         switch l
322             case 1
323                 plot(line,'--ks','LineWidth',2,
324                       'MarkerEdgeColor','k','MarkerFaceColor',
325                       'k','MarkerSize',5)
326                 hold on
327             case 2
328                 plot(line,'--bs','LineWidth',2,
329                       'MarkerEdgeColor','b','MarkerFaceColor',
330                       'b','MarkerSize',5)
331                 hold on
332             case 3
333                 plot(line,'--rs','LineWidth',2,
334                       'MarkerEdgeColor','r','MarkerFaceColor',
335                       'r','MarkerSize',5)
336         end
337         legend('phi=0.1','phi=0.3','phi=0.5')
338         name=['plotting1-',s1,'-',s2,'-', 'phi.sensitivity'];
339         saveas(f,name);
340     end
341 end
342 end
343 end
344 end
345
346
347 %%%%%%%%% generating plots for each features of network structure for each

```

```

348 %%%%%%%%% parameter sets %%%%%%%%%
349
350 for i=1:4
351     switch i
352         case 1
353             f=figure();
354             line1=clust_coefficient(1:27);
355             line2=clust_coefficient(28:54);
356             line3=clust_coefficient(55:81);
357             plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
358                 'MarkerFaceColor','k','MarkerSize',5)
359             hold on
360             plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
361                 'MarkerFaceColor','g','MarkerSize',5)
362             hold on
363             plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
364                 'MarkerFaceColor','b','MarkerSize',5)
365             set(gca,'FontSize',14)
366             xlabel('Different triplets of alpha ,phi and threshold values')
367             ylabel('Clustering Coefficient')
368             title('The influence of idea distribution on clustering
369                 coefficient');
370             legend('Random distribution','Parallel distribution',
371                 'Antiparallel distribution')
372             name=('Plotting2.idea.Comparison.clustcoeff');
373             saveas(f,name);
374         case 2
375             f=figure();
376             line1=s(1:27);
377             line2=s(28:54);
378             line3=s(55:81);
379             plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
380                 'MarkerFaceColor','k','MarkerSize',5)
381             hold on
382             plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
383                 'MarkerFaceColor','g','MarkerSize',5)
384             hold on
385             plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
386                 'MarkerFaceColor','b','MarkerSize',5)
387             set(gca,'FontSize',14)
388             xlabel('Different triplets of alpha ,phi and threshold values')
389             ylabel('Number of connected components')
390             title('The influence of idea distribution on the number of
391                 connected components')
392             legend('Random distribution','Parallel distribution',
393                 'Antiparallel distribution')
394             name=('Plotting2.idea.Comparison.conncmp');
395             saveas(f,name);
396         case 3
397             f=figure();

```

```

398         line1=average_path_length(1:27);
399         line2=average_path_length(28:54);
400         line3=average_path_length(55:81);
401         plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
402             'MarkerFaceColor','k','MarkerSize',5)
403         hold on
404         plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
405             'MarkerFaceColor','g','MarkerSize',5)
406         hold on
407         plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
408             'MarkerFaceColor','b','MarkerSize',5)
409         set(gca,'FontSize',14)
410         xlabel('Different triplets of alpha ,phi and threshold values')
411         ylabel('average path length')
412         title('The influence of idea distribution on average path ...
            length')
413         legend('Random distribution','Parallel distribution',
414             'Antiparallel distribution')
415         name=('Plotting2.idea.Comparison.average_path_length');
416         saveas(f,name);
417     case 4
418         f=figure();
419         line1=diam(1:27);
420         line2=diam(28:54);
421         line3=diam(55:81);
422         plot(line1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
423             'MarkerFaceColor','k','MarkerSize',5)
424         hold on
425         plot(line2,'—gs','LineWidth',2,'MarkerEdgeColor','g',
426             'MarkerFaceColor','g','MarkerSize',5)
427         hold on
428         plot(line3,'—bs','LineWidth',2,'MarkerEdgeColor','b',
429             'MarkerFaceColor','b','MarkerSize',5)
430         set(gca,'FontSize',14)
431         xlabel('Different triplets of alpha ,phi and threshold values')
432         ylabel('Network Diameter')
433         title('The influence of idea distribution on Network Diameter')
434         legend('Random distribution','Parallel distribution',
435             'Antiparallel distribution')
436         name=('Plotting2.idea.Comparison.diam');
437         saveas(f,name);
438     end
439 end
440
441 %%%%%%%%% plots for degree distribution resulting from different idea
442 %%%%%%%%% distribution
443 count=0;
444 for choicel=1:3
445     switch choicel
446         case 1

```

```

447         s1='phi=0.1';
448         m1='1';
449     case 2
450         s1='phi=0.3';
451         m1='2';
452     case 3
453         s1='phi=0.5';
454         m1='3';
455 end
456
457 for choice2=1:3
458     switch choice2
459     case 1
460         s2='alpha=0.01';
461         m2='1';
462     case 2
463         s2='alpha=0.05';
464         m2='2';
465     case 3
466         s2='alpha=0.1';
467         m2='3';
468     end
469
470     for choice3=1:3
471         switch choice3
472         case 1
473             s3='threshold=0.001';
474             m3='1';
475         case 2
476             s3='threshold=0.01';
477             m3='2';
478         case 3
479             s3='threshold=0.05';
480             m3='3';
481         end
482         count=count+1;
483         line1=dgr{count};
484         mine1=frq{count}/1000;
485         line2=dgr{27+count};
486         mine2=frq{27+count};
487         line3=dgr{54+count};
488         mine3=frq{54+count};
489         f=figure();
490         loglog(line1,mine1,'—ks','LineWidth',2,'MarkerEdgeColor','k',
491             'MarkerFaceColor','k','MarkerSize',5)
492         hold on
493         plot(line2,mine2,'—rs','LineWidth',2,'MarkerEdgeColor','r',
494             'MarkerFaceColor','r','MarkerSize',5)
495         hold on
496         plot(line3,mine3,'—bs','LineWidth',2,'MarkerEdgeColor','b',

```



```

497         'MarkerFaceColor','b','MarkerSize',5)
498     set(gca,'FontSize',14)
499     xlabel('Log(degree)')
500     ylabel('Log(frequency)')
501     title(['The influence of idea distribution on the degree
502           distribution',' ',s1,' ',s2,' ',s3]);
503     legend('Random distribution','Parallel distribution',
504           'Antiparallel distribution')
505     name=(['Plotting2_idea.comparison_degree_distribution-'
506           ,m1,'-',m2,'-',m3]);
507     saveas(f,name);
508     end
509 end
510 end

```