Introduction to spagetti and meatballs



CSC 418/2504: Computer Graphics

Course web site (includes course information sheet):

http://www.dgp.toronto.edu/~karan/courses/418/fall2016

Instructors:

L0101, W 12-2pm L0201, T 12-2pm

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or by appointment. or by appointment.

Textbooks: Fundamentals of Computer Graphics

OpenGL Programming Guide & Reference

Tutorials: (first tutorial next week)

This is a Green Course!



Your instructor has committed to reducing this course's environmental impact.

sustainability.utoronto.ca

#greenerUofT

Today's Topics

- 0. Introduction: What is Computer Graphics?
- 1. Basics of scan conversion (line drawing)
- 2. Representing 2D curves

Topic 0.

Introduction: What Is Computer Graphics?

What is Computer Graphics?

Computers:

accept, process, transform and present information.

Computer Graphics:

accept, process, transform and present information in a visual form.

Ok but... what is the course really about?

The science of turning the rules of geometry, motion and physics into (digital) pictures that mean something to people

What its not about?

Photoshop, AutoCAD, Maya, Renderman, Graphics APIs.

...wow, heavy math and computer science!!

Movies

Movies define directions in CG Set quality standards Driving medium for CG







Games

Games emphasize the interactivity and AI

Push CG hardware to the limits (for real time performance)





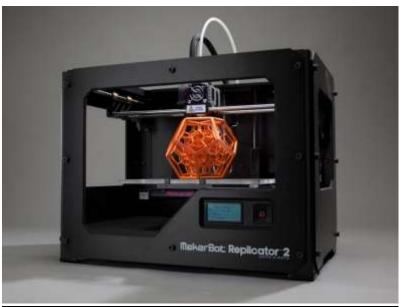


Design

CG for prototyping and fabrication

Requires precision modeling and engineering visualization





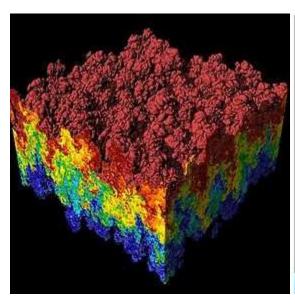


Scientific and Medical Visualization, Operation

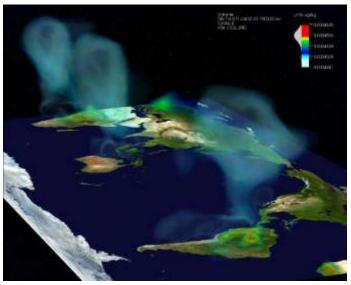
Requires handling large datasets

May need device integration

Real-time interactive modeling & visualization







GUIs, AR/VR, scanners...

Interaction with software & hardware, I/O of 3D data Emphasis on usability



Computer Graphics: Basic Questions

Form (modeling)
 How do we represent (2D or 3D) objects & environments?
 How do we build these representations?

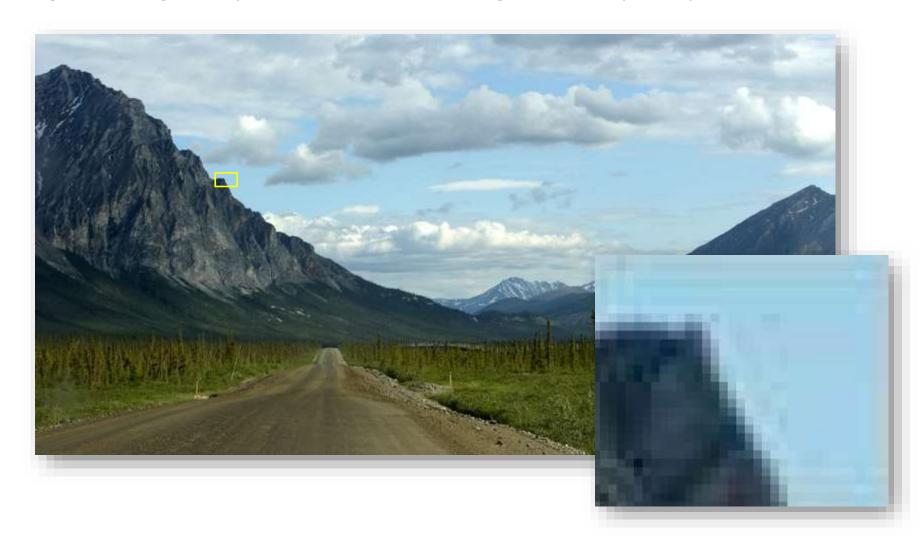
Function, Behavior (animation)
 How do we represent the way objects move?
 How do we define & control their motion?

Appearance (rendering)
 How do we represent the appearance of objects?
 How do we simulate the image-forming process?

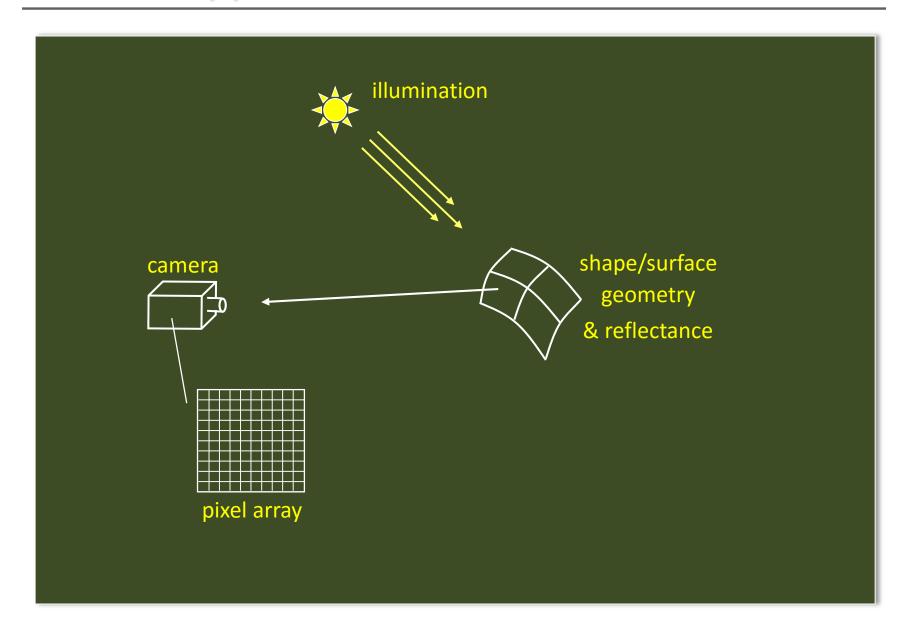
What is an Image?

Image = distribution of light energy on 2D "film"

Digital images represented as rectangular arrays of <u>pixels</u>



Form & Appearance in CG



The Graphics Pipeline

Modeling — Animation — Rendering

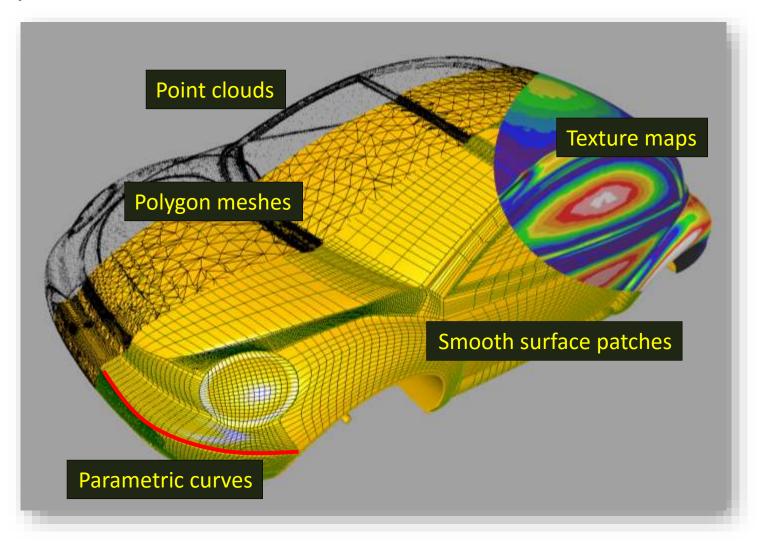
- Geometry: points, curves,
 & surfaces
- Scene Objects: parts, relations, & pose
- Texture and reflectance (e.g., color, diffusivity, opacity, refractions)
- ...

 Key-frame, motion capture, inverse kinematics, dynamics, behaviors, motion planning, ...

- Visibility
- Simulation of light (e.g., illuminants, emissive surfaces, scattering, transmission, diffraction, ...)
- Special effects (e.g., antialiasing, motion blur, nonphotorealism)

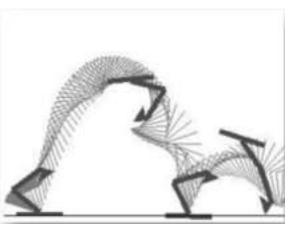
Graphics Pipeline: Modeling

How do we represent an object geometrically on a computer?



Graphics Pipeline: Animation



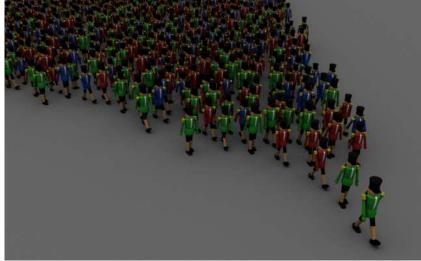




Physical simulation

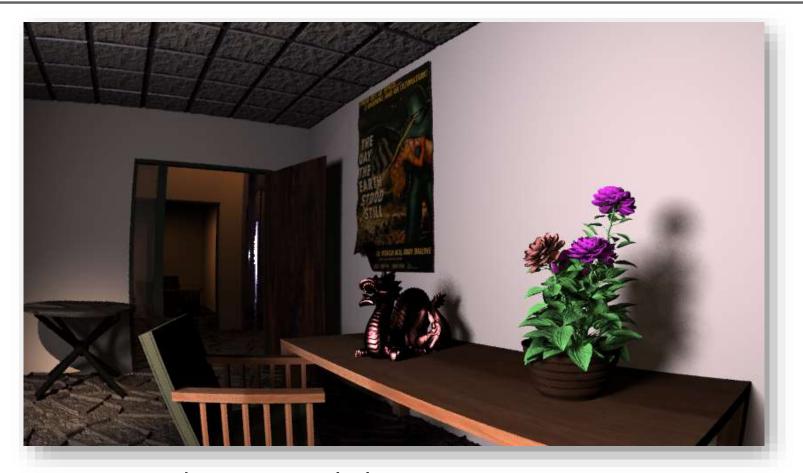


Key-Framing



Behavior rules

Graphics Pipeline: Rendering



Input: Scene description, lighting, camera

Output: Image that the camera will observe...

accounting for visibility, clipping, projection,...

Course Topics

Principles

Theoretical & practical foundations of CG (core mathematics, physics, modeling methods)

CG programming (assignments & tutorials)

- Experience with OpenGL (industry-standard CG library)
- Creating CG scenes

What You Will Take Away ...

#1: yes, math <u>IS</u> useful in CS!!

#2: how to turn math & physics into pictures.

#3: basics of image synthesis

#4: how to code CG tools

Administrivia

Grading:

- 50%: 3 assignments handed out in class (25% 15% 10%).
- 50%: 1 test in class (15%) + 1 final exam (35%).
- First assignment: on web in two weeks.
- Wooden Monkey assignment on web now!
- Check web for schedule, dates, more details & policy on late assignments.

Tutorial sessions:

- Math refreshers, OpenGL tutorials, additional topics.
- Attendance STRONGLY encouraged since I will not be lecturing on these topics in class.

Lecture slides & course notes, already on web.

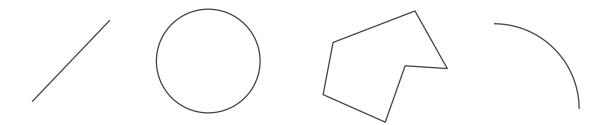
Topic 1.

Basic Raster Operations: Line Drawing

- A simple (but inefficient) line drawing algorithm
- Bresenham's algorithm
- Line anti-aliasing

2D Drawing

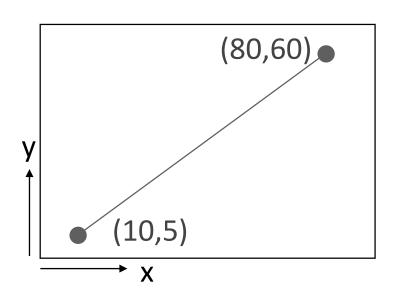
Common geometric primitives:



When drawing a picture, 2D geometric primitives are specified as if they are drawn on a continuous plane

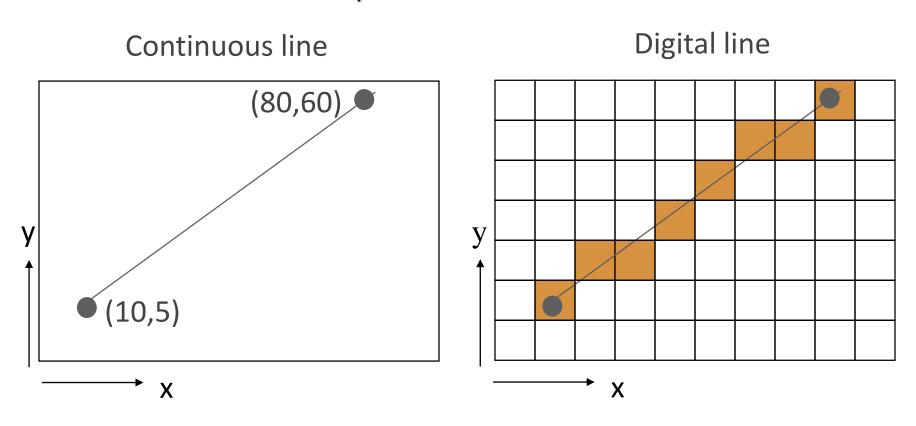
Drawing command:

Draw a line from point (10,5) to point (80,60)



2D Drawing

In reality, computer displays are arrays of <u>pixels</u>, not abstract mathematical continuous planes



In graphics, the conversion from continuous to discrete 2D primitives is called <u>scan conversion</u> or <u>rasterization</u>

Basic Raster Operations (for 2D lines)

- Scan conversion: Given a pair of pixels defining the line's endpoints & a color, paint all pixels that lie on the line.
- Clipping: If one or more endpoints is out of bounds, paint only the line segment that is within bounds.
- Region filling: Fill in all pixels within a given closed connected boundary of pixels.

Line Scan Conversion: Key Objectives

Accuracy:

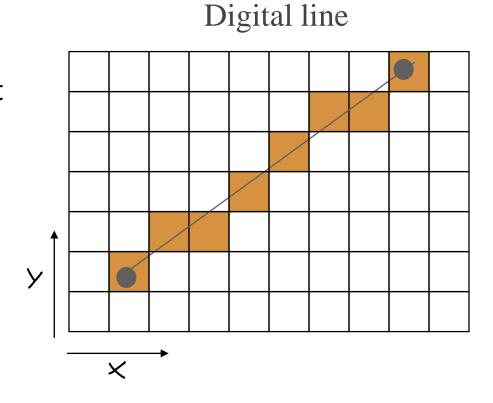
pixels should approximate line closely.

Speed:

line drawing should be efficient

Visual Quality:

No discernable "artifacts".



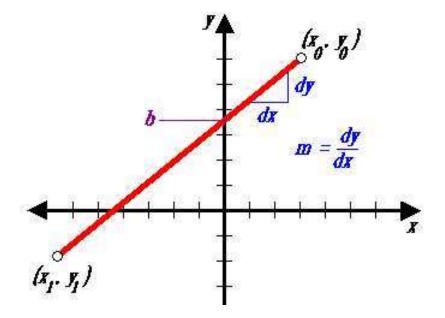
Equation of a Line

Explicit: y = mx + b

Parametric:

$$x(t) = x_0 + (x_1 - x_0)*t$$

 $y(t) = y_0 + (y_1 - y_0)*t$



$$P = P_0 + (P_1-P_0)^*t$$

 $P = P_0^*(1-t) + P_1^*t$ (weighted sum)

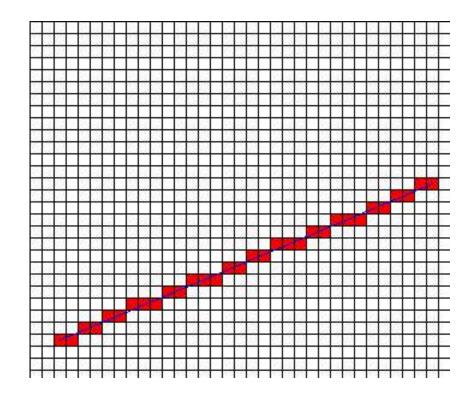
Implicit: $(x-x_0)dy - (y-y_0)dx = 0$

Algorithm I

DDA (Digital Differential Analyzer) **Explicit form:**

```
y = dy/dx * (x-x0) + y0
```

```
float y;
int x;
dx = x1-x0; dy = y1 - y0;
m = dy/dx;
y= y0;
for ( x=x0; x<=x1; x++)
{
    setpixel (x, round(y));
    y= y + m;
}</pre>
```

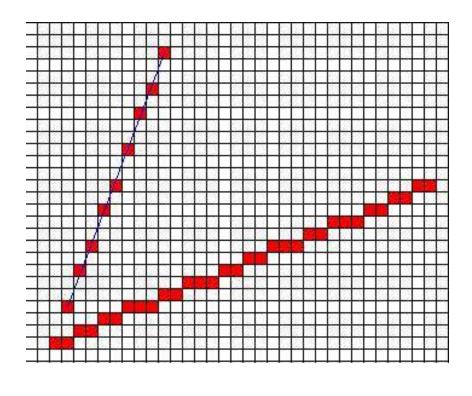


Algorithm I (gaps when m>1)

DDA (Digital Differential Analyzer) **Explicit form:**

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y = dy/dx * (x-x0) + y0
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y= y0;
for ( x=x0; x<=x1; x++)
{
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}</pre>
```



Algorithm II

Bresenham Algorithm

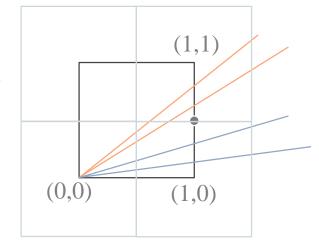
Slope is rational (ratio of two integers). m = (y1 - y0) / (x1 - x0). Assume line slope <1 (first quadrant), implying that either $y_{i+1} = y_i$ or $y_{i+1} = y_i + 1$.

We want to make this decision using only integer math.

Algorithm II

Bresenham Algorithm: Implicit View

$$f(x,y) = x*dy - y*dx = 0$$
 // for points on the line
>0 // below the line
<0 // above the line

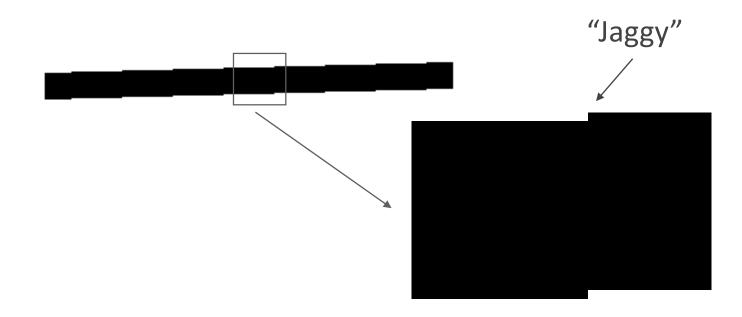


$$f(x+1,y+0.5) = f(x,y) + dy - 0.5*dx$$
-ve , +ve
 $f(1,0.5) = dy - 0.5*dx$
-ve: pick (1,0)
+ve: pick (1,1)

err =
$$2f(x+1,y+0.5) = 2f(x,y) + 2dy - dx$$
 // getting rid of the float

Aliasing

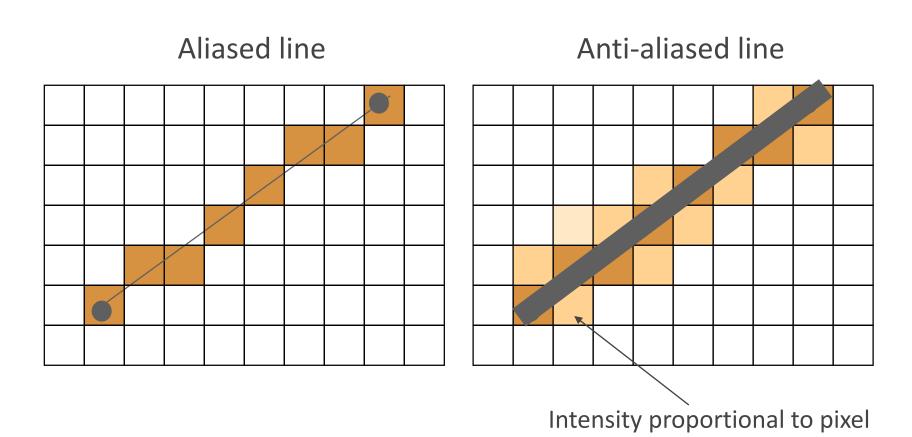
Raster line drawing can produce a "jaggy" appearance.



- Jaggies are an instance of a phenomenon called aliasing.
- Removal of these artifacts is called <u>anti-aliasing</u>.

Anti-Aliasing

How can we make a digital line appear less jaggy?



area covered by "thick" line

Main idea: Rather than just drawing in 0's and 1's, use "inbetween" values in neighborhood of the mathematical line.

Anti-Aliasing: Example



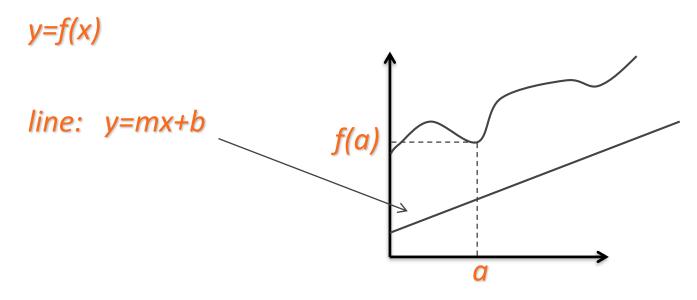
Topic 2.

2D Curve Representations

- Explicit representation
- Parametric representation
- Implicit representation
- Tangent & normal vectors

Explicit Curve Representations: Definition

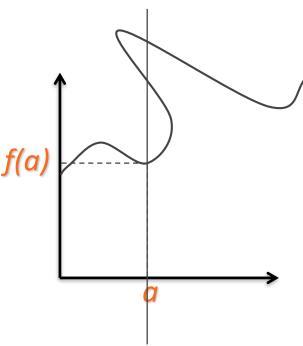
Curve represented by a function *f* such that:



Explicit Curve Representations: Limitations

Curve represented by a function *f* such that:

$$y=f(x)$$



Parametric Curve Representation: Definition

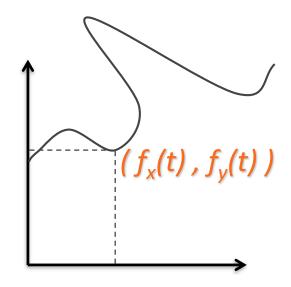
Curve represented by two functions f_{χ} , f_{ν}

And an interval [a,b]

such that:

$$(x,y)=(f_x(t),f_y(t))$$

are points on the curve for tin [a,b]



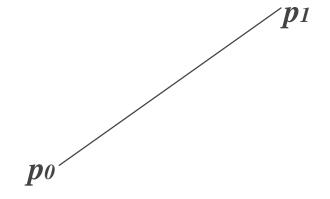
A curve is closed when ??

Parametric Representation of a Line Segment

$$p(t) = p_0 + (p_1 - p_0) *t$$
, $0 \le t \le 1$

 $0 \le t \le \infty$: ray from p_0 through p_1

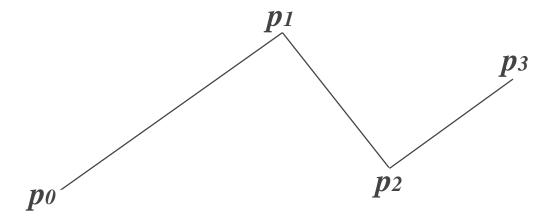
 $-\infty$ ≤ t ≤ ∞ : line through p_{θ} and p_{1}



In general if $p(t) = a_0 + a_1 t$, how do you solve for a_0, a_1 ?

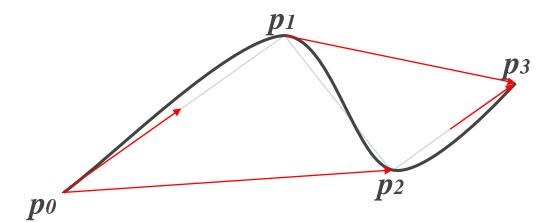
Line Segment as interpolation

$$p(t) = a_0 + a_1 * t$$



Curve as interpolation (Catmull-Romm)

$$p(t) = a_0 + a_1 * t + a_2 * t^2 + a_3 * t^3$$



Polygons

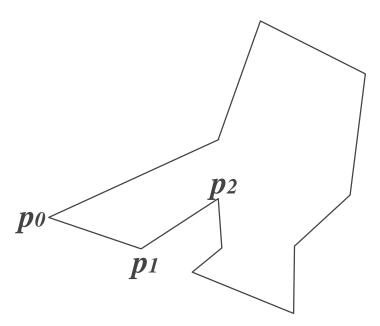
Polygon: A continuous piecewise linear closed curve.

Simple polygon: non-self intersecting.

Convex: all angle less than 180 degrees.

Regular: simple, equilateral, equiangular.

n-gon: $pi = r(cos(2\pi i/n), sin(2\pi i/n))$, $0 \le i < n$



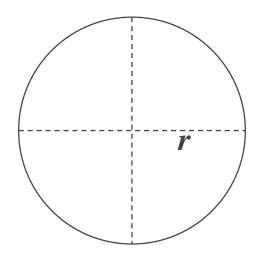
Representations of a Circle

Parametric:

$$p(t) = r(\cos(2\pi t), \sin(2\pi t)), \quad 0 \le t \le 1$$

Implicit:

$$x^2+y^2-r^2=0$$



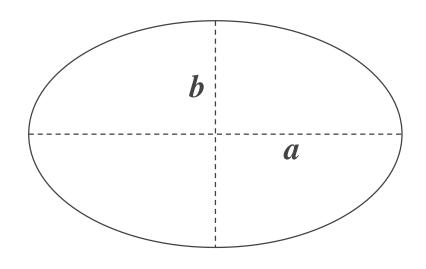
Representations of an Ellipse

Parametric:

$$p(t) = (a*cos(2\pi t), b*sin(2\pi t)), \quad 0 \le t \le 1$$

Implicit:

$$x^2/a^2+y^2/b^2-1=0$$



Curve tangent and normal

Parametric:

$$p(t) = (x(t), y(t)).$$

Tangent: (x'(t),y'(t)).

Implicit:

$$f(x,y) = 0$$
.

Normal: gradient(f(x,y)).

Tangent and normal are orthogonal.