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**NATIONAL INSTITUTE OF TECHNOLOGY GOA**  
**Department of Computer Science and Engineering**  
**B.Tech V Semester-End Examination**

Course Name: **Theory of Computation**

Date: **December 9, 2021**

Duration: **3 Hours**

Course Code: **CS303**

Time: **02:00 PM**

Max. Marks: **100**

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**Note:**

- Be legible. Keep the rough work separate from the space you write the answer.
  - The notations used should be consistent as mentioned in the class.
  - Unnecessary details attracts penalty.
  - The question paper is of *four* pages.
  - Attach the rough work sheets at the end of the answer scripts clearing mentioning it as a rough work. All the necessary calculations to be shown. In multiple choice, write the complete answer with choice.
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**1. State whether True or False. Justify.**

- a) If a CFG  $G$  has three productions, i.e.  $S \rightarrow AA, A \rightarrow aa, A \rightarrow bb$ , then  $L(G)$  is finite. **(2)**
- b) If a CFG  $G$  has productions  $S \rightarrow aS|bS|a$ , then  $L(G)$  is the set of all strings over  $\{a, b\}$  ending in  $a$ . **(2)**
- c) The language  $\{a^n b c^n | n \geq 1\}$  is regular. **(2)**
- d) If the productions of  $G$  are  $S \rightarrow aS|Sb|a|b$ , then  $abab \in L(G)$ . **(2)**
- e) If  $G = (V, T, P, S)$  and  $P \neq \phi$ , then  $L(G) \neq \phi$ . **(2)**

**2. Choose the correct answer for the following.**

- i) The CFG generating  $\{a^n : n \geq 1\}$  is **(2)**
  - a)  $(\{S\}, \{a\}, \{S \rightarrow aS, S \rightarrow a\}, S)$
  - b)  $(\{S\}, \{a\}, \{S \rightarrow aS\}, S)$
  - c)  $(\{S\}, \{a\}, \{S \rightarrow SS, S \rightarrow a\}, S)$
  - d)  $(\{S\}, \{a\}, \{S \rightarrow aSS\}, S)$

ii) Which of the following regular expression represents the set of all binary strings with an odd number of 1's? **(2)**

- a)  $((0 + 1)^*1(0 + 1)^*1)^*10^*$
- b)  $(0^*10^*10^*)^*10^*$
- c)  $10^*(0^*10^*10^*)^*$
- d)  $(0^*10^*10^*)^*0^*1$

iii) Consider the following languages over the alphabet  $\{0, 1\}$ . Note that  $x^R$  is the reverse of the string  $x$ . **(3)**

$$L_1 = \{xx^R | x \in \{0, 1\}^*\}$$

$$L_2 = \{xx | x \in \{0, 1\}^*\}$$

Which of the following is true. **Justify.**

- a) Both  $L_1$  and  $L_2$  are regular.
- b)  $L_1$  is context free but not regular whereas  $L_2$  is regular.
- c) Both  $L_1$  and  $L_2$  are context free and neither is regular.
- d)  $L_1$  is context free but  $L_2$  is not context free.
- e) Both  $L_1$  and  $L_2$  are not context-free.

iv) Let  $a, b, c$  be regular expressions. Which of the following identities is correct? **Justify. (3)**

- a)  $(a + b)^* = a^*b^*$
- b)  $a(b + c) = ab + c$
- c)  $(a + b)^* = a^* + b^*$
- d)  $(ab + a)^*a = a(ba + a)^*$
- e) None of the above

3. Design a CFG to generate the following languages. Also, show by deriving at least one string that is in the language of the designed CFG.

- a)  $L = \{w | w \text{ is a string over } \{0, 1\} \text{ ending in } 0\}$ . **(4)**
- b)  $L = \{w | w \text{ is a string over } \{0, 1\} \text{ beginning with } 0\}$ . **(4)**

4. Write the regular expression for the following languages.

- a) The set of all strings of 0's and 1's ending in 00. **(2)**
- b) The set of all strings of 0's and 1's beginning with 11 and ending with 0. **(2)**
- c)  $L = \{\epsilon, 11, 1111, 111111, \dots\}$  **(2)**

5. a) Convert the following NFA to DFA. (5)

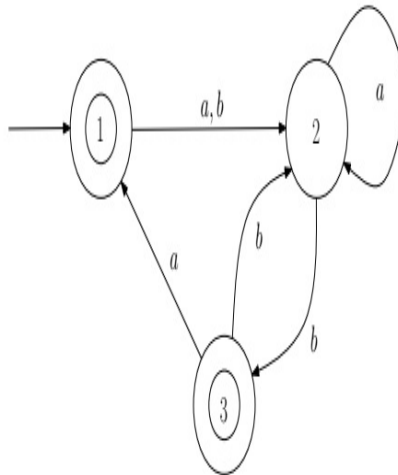
	0	1
$\rightarrow p$	$\{q, s\}$	$\{q\}$
$*q$	$\{r\}$	$\{q, r\}$
$r$	$\{s\}$	$\{p\}$
$*s$	$\phi$	$\{p\}$

b) Convert the following  $\epsilon$ -NFA to DFA. (5)

	$\epsilon$	$a$	$b$	$c$
$\rightarrow p$	$\phi$	$\{p\}$	$\{q\}$	$\{r\}$
$q$	$\{p\}$	$\{q\}$	$\{r\}$	$\phi$
$*r$	$\{q\}$	$\{r\}$	$\phi$	$\{p\}$

c) Convert the Regular expression  $(0 + 1)^*(0 + 1)1$  to  $\epsilon$ -NFA. (5)

d) Convert the DFA to Regular expression. (5)



e) Construct a **DFA with minimum number of states** to accept all strings over  $\{0, 1\}$  ending in 010 or 0010. (5)

6. a) Prove that the language  $L = \{a^n b^{2n} | n > 1\}$  is not regular. (4)
- b) Show that the grammar  $S \rightarrow a|abSb|aAb, A \rightarrow bS|aAAb$  is ambiguous. (4)
- c) Design a PDA to accept the set of all strings of 0's and 1's with an equal number of 0's and 1's. Show for atleast one string in the Language how the designed PDA accepts. In addition, you have to briefly explain the approach in few sentences. (4)

7. a) Consider the following CFG.

$$S \rightarrow AB|CA$$

$$A \rightarrow a$$

$$B \rightarrow BC|AB$$

$$C \rightarrow aB|b$$

Find the equivalent CFG with no useless symbols. (4)

- b) Put the following CFG in Chomsky Normal Form. (10)

$$S \rightarrow ASB|\epsilon$$

$$A \rightarrow aAS|a$$

$$B \rightarrow SbS|A|bb$$

8. a) Prove that the language  $L = \{0^n 1^n 2^n | n \geq 1\}$  is not a context-free language. (5)
- b) Design a Turing machine to recognize the language  $L = \{w | w \text{ is string over } \{0, 1\} \text{ that ends with } 010\}$ . Show how Turing machine processes the input 0101010 using instantaneous descriptions. In addition, you have to briefly explain the approach in few sentences. (10)

\*\*\*\*\*All the Best\*\*\*\*\*