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# National Institute of Technology Goa

B.Tech. Minor Examination, April-2021

Department of Humanities and Sciences

Course Name: **MATHEMATICS-I (A & B)**

Course Code: MA100

Date: April 2, 2021

Time: 11:00 AM

Duration: 40 Min.

Max. Marks: 25

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**ANSWER ALL QUESTIONS**

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1. Find the work done in moving a particle once around a circle  $C$  in the  $xy$  plane, if the circle has center at the origin and radius 3 and if the force field is given by  $F = (2x - y + z)i + (x + y - z^2)j + (3x - 2y + 4z)k$ .
2. (a) Show that  $F = (2xy + z^3)i + x^2j + 3xz^2k$  is a conservative force field.  
(b) Find the scalar potential.
3. Find the area of the region cut from the plane  $x + 2y + 2z = 5$  by the cylinder whose walls are  $x = y^2$  and  $x = 2 - y^2$ .
4. Find the flux of the field  $F(x, y, z) = 4xi + 4yj + 2k$  outward (away from the  $z$ -axis) through the surface cut from the bottom of the paraboloid  $z = x^2 + y^2$  by the plane  $z = 1$ .
5. Verify Green's theorem in the plane for  $\int_C (xy + y^2)dx + x^2dy$  where  $C$  is the closed curve of the region bounded by  $y = x$  and  $y = x^2$ .

\* \* \* ALL THE BEST \* \* \*