

→ 16 weeks

mid — 50 → 8

min-1 — 25 → 4

min-2 — 25 → 12

End — 100 → 14

200

S.M

C.S

Q.S

M.B. Statistics



$$\frac{n!}{n_1! n_2! n_3! \dots n_v!}$$



most probable micro state



Zero (or) Integral spin  
0, 1, 2

Bosons  
E.g. - Photons  
B.E.S

F.D.S

BES + PEP





B. E

00

1. indistinguishable

2. 0, 1, 2.

3. Photon

F. D S

00


1. —

2.  $\pm \frac{1}{2}$

3.  $e^{\pm}, \mu$



# $O_A O_B$ M-B Statistics

1. distinguishable  $\Rightarrow$  there is no symmetric restriction
2. There is no restriction on the no. of particles in any eigen state 
3. The total no. of particles in the either system is always constant  $n = n_1 + n_2 + n_3 + \dots + n_r + \dots = \sum_{i=1}^r n_i = \text{const}$
4. The sum of energy of all the particles in different quantum groups taken together constitutes the total energy of the system.





300

large system

$10^{24}$  atoms/m<sup>3</sup>

N,

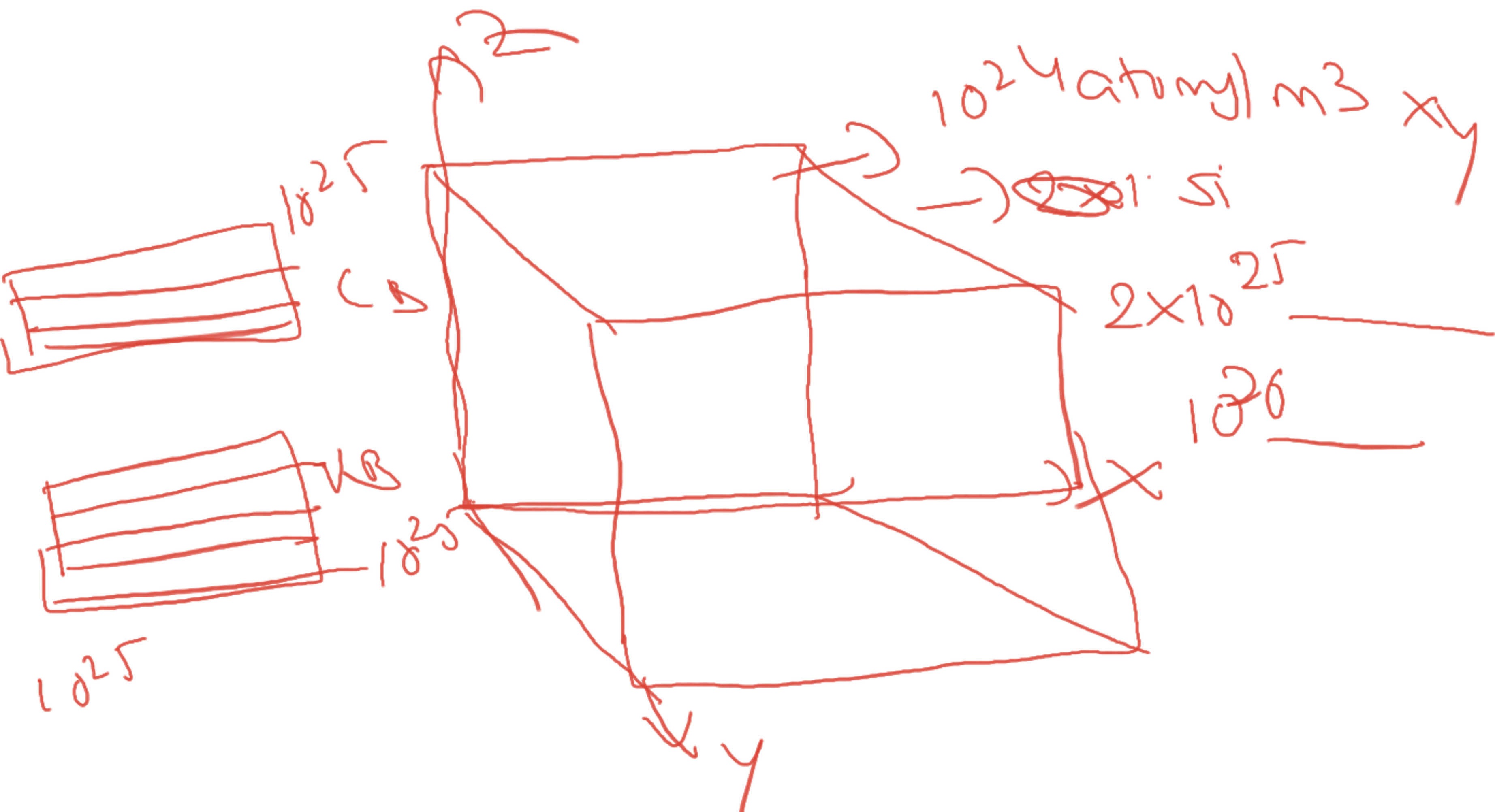
$\Rightarrow 90 =$



Total capacity = 90

Total no. of stu = 90





$$\sum_{i=0}^{\infty} \epsilon_i n_i = U \quad \epsilon_1, \epsilon_2, \epsilon_3, \epsilon_4 \dots$$

$\epsilon_i \rightarrow$  Energy level

$$\sum_{i=0}^{\infty} n_i = \text{const} \quad n_1, n_2, n_3, n_4 \dots$$

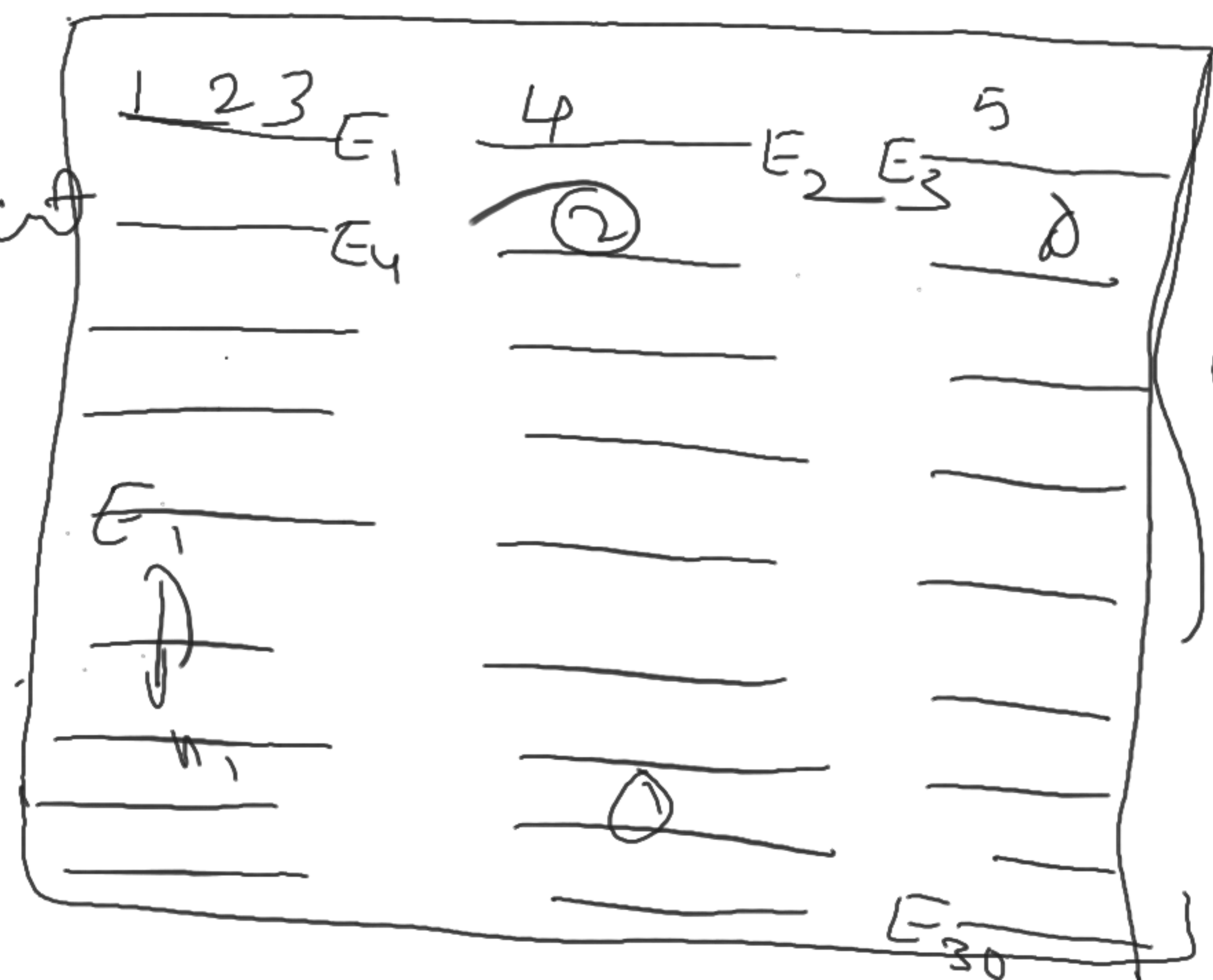
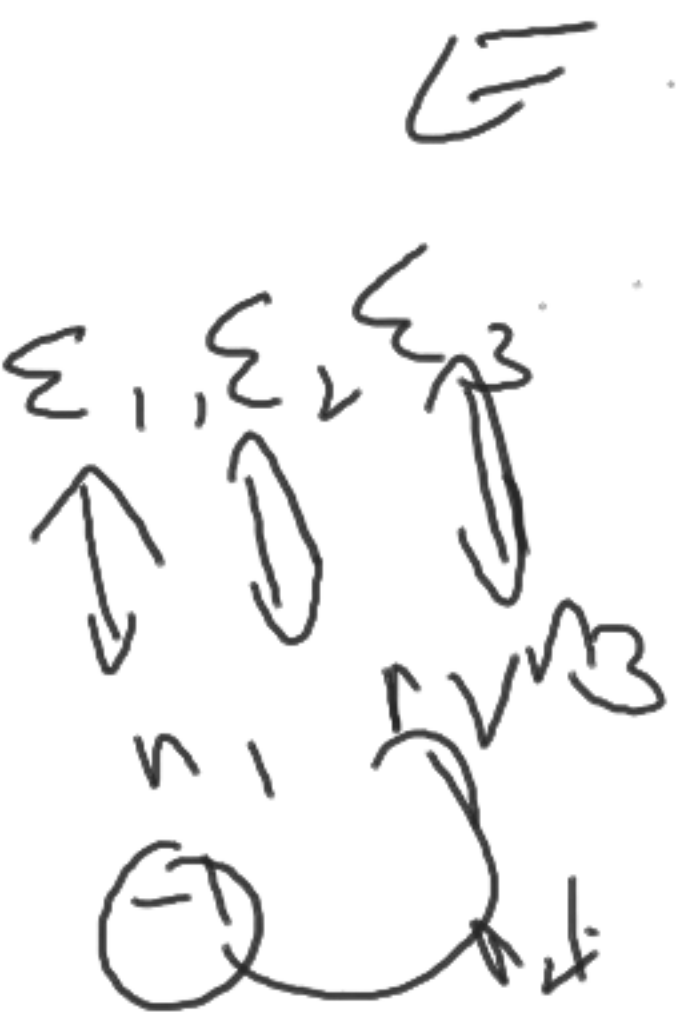
$n_i \rightarrow$  particles

$n_1, n_2, n_3 \dots n_i$  particles lie in groups having approximate energies  $\epsilon_1, \epsilon_2, \epsilon_3, \dots \epsilon_i \dots$

$$\sum_{i=1}^r n_i = \text{const} \quad n_1, n_2, n_3, \dots, n_r$$

$$i=0$$

$$\sum_{i=1}^r \epsilon_i n_i = \text{const}$$



30 desks

↳ 3 seats

90 students

30

$n_1 \rightarrow 3$

$n_2 \rightarrow 3$

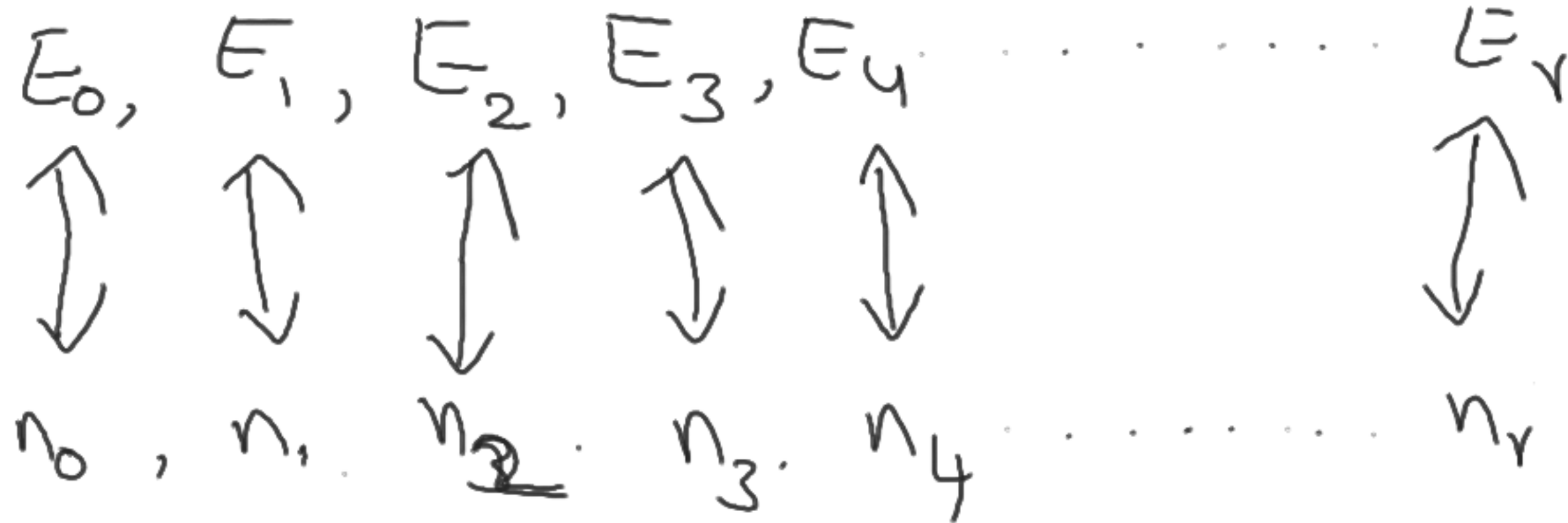
$n_3 \rightarrow$

$n_{30} \rightarrow$

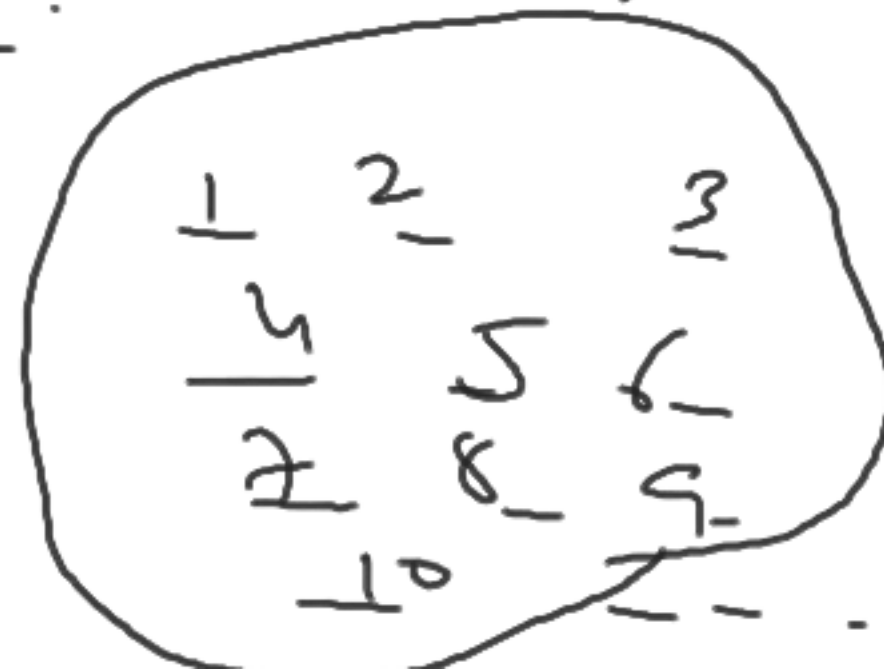
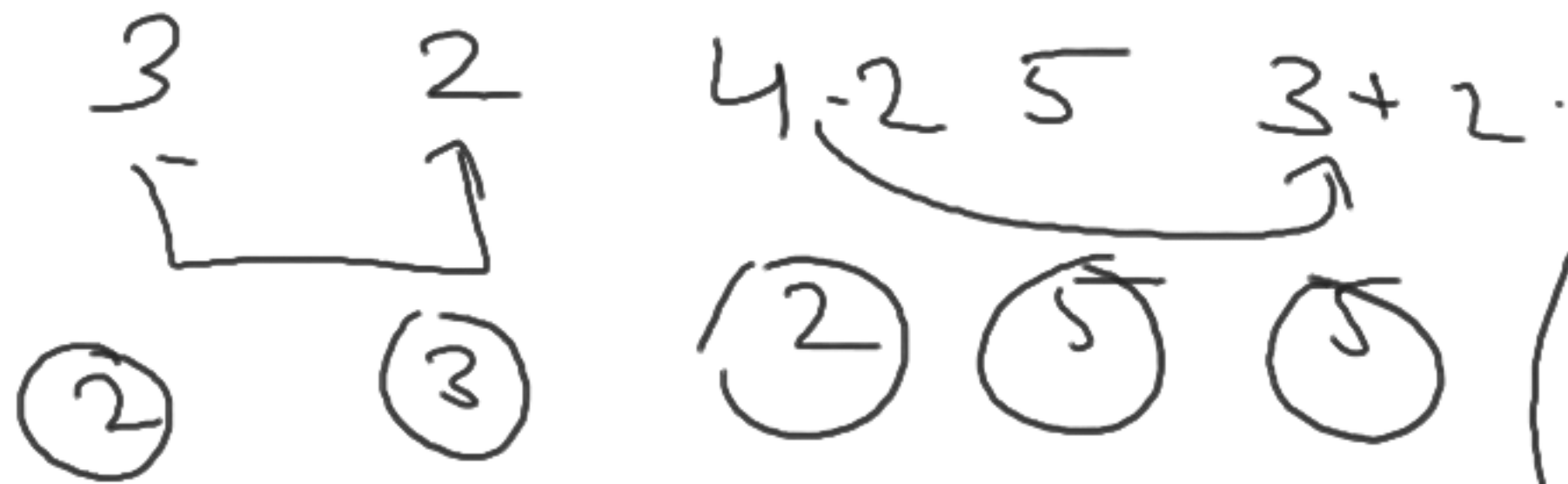


$$\textcircled{N} \quad \textcircled{E} = V$$

available  
 $E \in L$  in the  
 system



$\textcircled{N}$



$= \textcircled{90}$

$\textcircled{10}$

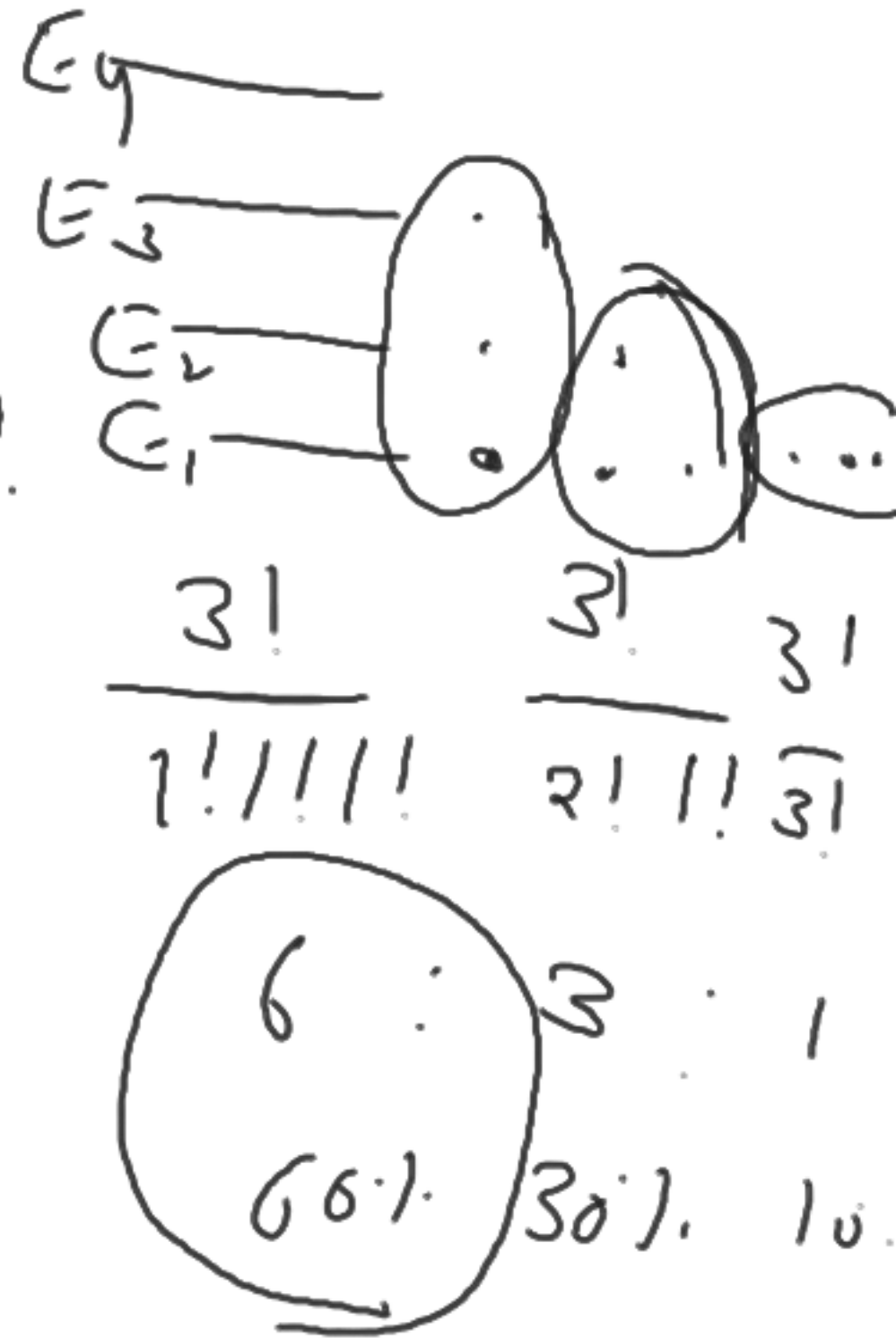
most probable  
 micro

Most Probable micro state =  $\Omega$

$$\Omega = \frac{n!}{n_0! n_1! n_2! n_3! \dots n_r!}$$

$$\Omega = \frac{n!}{\prod_{i=0}^{i=r} n_i!}$$

take log on both sides



$$\ln \Omega = \ln n! - \sum_{i=0}^{k-1} \ln n_i! \quad - (1)$$

$$\sum_{i=0}^{k-1} n_i = n$$

According to Stirling's approximation

$$\ln x! = x \ln x - x \quad (2)$$

$$n_i \approx n_0, n_1, n_2, n_3$$

apply eqn (2) to (1)

$$\ln \Omega = \frac{n \ln n - n}{1} - \sum_{i=0}^{k-1} [n_i \ln n_i - n_i]$$

$$\delta \ln \Omega = \frac{1}{\Omega} \sum_{i=0}^{k-1} \left[ \delta n_i \ln n_i + n_i \frac{1}{n_i} \delta n_i - \delta n_i \right]$$

For most probable distribution

$$\sum_{i=0}^{i=v} [\delta n_i \ln n_i] = 0$$

- (2)

Total no. of particles in the system remains const

$$\sum_{i=0}^{i=v} n_i = n = \text{const} \Rightarrow \sum_{i=0}^{i=v} \delta n_i = 0$$

- 3

$\bar{\epsilon}$  is const

$$\sum_{i=0}^{i=V} \epsilon_i n_i = \bar{\epsilon} = \text{const}$$

$$\sum_{i=0}^{i=V} \epsilon_i \delta n_i = 0 \quad - \quad (4)$$

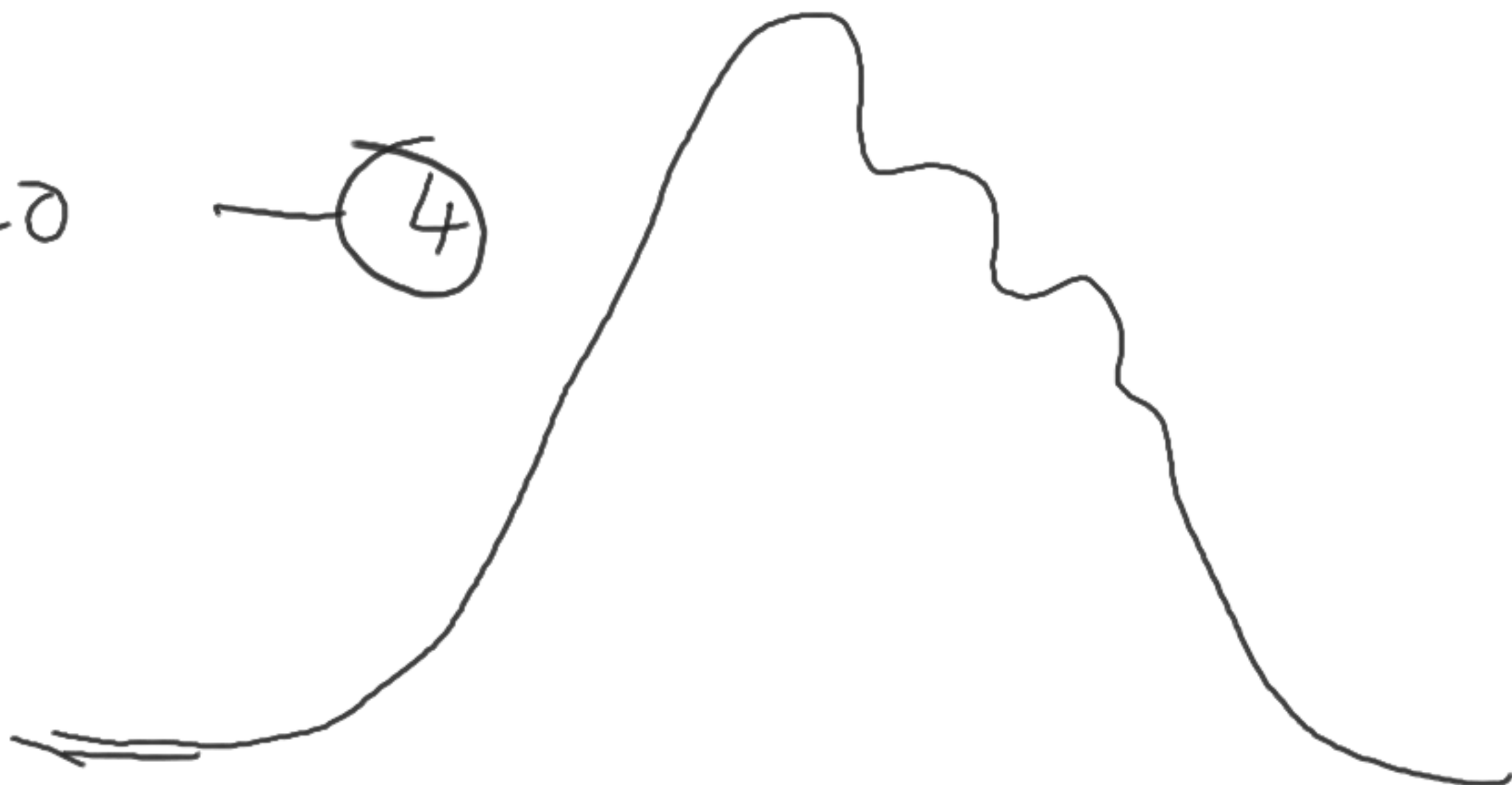
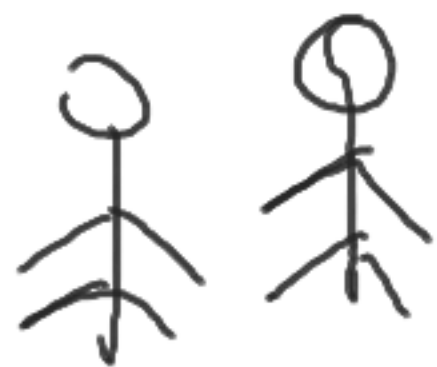


$$\sum_{i=0}^i [\delta n_i, \ln n_i] = 0 \quad - (2)$$

$$\sum_{i=0}^i \delta n_i = 0 \quad - (3)$$

$$\sum_{i=0}^i \epsilon_i \delta n_i = 0 \quad - (4)$$

$$\begin{array}{cccc} \epsilon_1 & \epsilon_2 & \epsilon_3 & \epsilon_4 \\ \downarrow & | & | & | \\ n_1 & n_2 & n_3 & n_4 \end{array}$$



lagrange method of undetermined multipliers

$$\sum_{i=1}^n \delta u_i \ln u_i = 0 \quad (2) \times 1$$

$$\sum_{i=1}^n \delta u_i = 0 \quad - (3) \times \alpha$$

$$\sum_{i=1}^n \varepsilon_i \delta u_i = 0 \quad - (4) \times \beta$$

$$\sum_{i=1}^n \left[ \delta u_i \ln u_i + \delta u_i \times \alpha + \varepsilon_i \delta u_i \times \beta \right] = 0$$

$$\sum_{i=1}^n \left[ \ln u_i + \alpha + \varepsilon_i \beta \right] \delta u_i = 0$$

$$\ln n_i + \alpha + \beta \epsilon_i = 0$$

$$\ln n_i = -[\alpha + \beta \epsilon_i]$$

$$n_i = e^{-\alpha} e^{-\beta \epsilon_i}$$

$$\sum_{i=0}^{\infty} n_i = N \Rightarrow$$

$$\sum_{i=0}^{\infty} e^{-\alpha} e^{-\beta \epsilon_i} = N$$

$$e^{-\alpha} \sum_{i=0}^{\infty} e^{-\beta \epsilon_i} = N$$

$$T \uparrow \quad i=5 \quad e^{-\alpha} = \frac{n}{\sum_{i=0}^5 e^{-\beta E_i}} = \frac{n}{P}$$

$$n_5 = \frac{n}{P} e^{-\frac{E_5}{kT}}$$

P is the Partition function  $i=0$

$$\beta = \frac{1}{kT}$$

$$n_i = \frac{n}{P} e^{-\frac{E_i}{kT}}$$

$$P = \sum_{i=0}^5 e^{-\beta E_i}$$

$$n_i = \frac{n}{P} e^{-\beta E_i}$$

$$n_0 = \frac{n}{P} e^{-\beta E_0}$$

$$i=1 \quad n_1 = \frac{n}{P} e^{-\beta E_1}$$

$$i=2 \quad n_2 = \frac{n}{P} e^{-\beta E_2}$$

