

DM ASSIGNMENT

Q1. Check the relations whether it is Reflexive, Irreflexive, Symmetric, Asymmetric, AntiSymmetric and Transitive Relation and justify your answer.

$$A = \{1, 2, 3, 4\}$$

Relations	Reflexive	Irreflexive	Symmetric	AntiSymmetric	Asymmetric	Transitive
$R_1 = \emptyset$						
$R_2 = A \times A$						
$R_3 = \{(1,1), (1,2), (2,1), (2,2), (3,4), (4,1), (4,4)\}$						
$R_4 = \{(1,1), (1,2), (2,1)\}$						
$R_5 = \{(2,1), (3,1), (3,2), (4,1), (4,2), (4,3)\}$						

Q2. Show whether the relation $(x,y) \in R$, if $x \geq y$ defined on the set of +ve integers is a partial order relation.

Q3. Which of the followings are partial order relation.

- (a) $R = \{(a,b) \mid a,b \in \mathbb{Z}, a < b\}$
- (b) $R = \{(a,b) \mid a,b \in \mathbb{Z}, a \leq b\}$
- (c) $R = \{(a,a), (b,b)\}, A = \{a,b\}$
- (d) $R = \{(1,1), (1,2), (2,1)\}, A = \{1,2,3\}$

Q4. Which of the followings are Equivalence relation on given set A.

$$A = \{1, 2, 3, 4, 5\}$$

- (a) $R = \{\}$
- (b) $R = A \times A$
- (c) $R = \{(1,1), (3,5), (5,4), (1,5), (5,1)\}$
- (d) $R = \{(1,1), (2,2), (3,3), (4,4), (5,5), \}$

Q5. Given relation is Equivalence relation or not.

$$R = \{(a,b) \mid |a-b| \text{ is even} \} \quad a,b \in A$$

$$A = \{1, 2, 3, 4, 5\}$$

Q6. Draw the Hasse diagram and calculate the number of lines

- (a) $A = \{1, 2, 3, 4, 5, 6\}$
 $< A, / >$
- (b) $< D_{60}, / >$
- (c) $< P(A), \subseteq > \quad A = \{1, 2, 3\}$
- (d) $< D_{105}, / >$
- (e) $< P(X), \subseteq > \quad X = \{a, b, c, d\}$
- (f) $< 1, 2, 3, 6, 9, 18, 54 / >$

Find the answer with the explanation for Question no. 7 to Question no 11

7. The number of onto functions (surjective functions) from set $X = \{a, b, c, d, e, f\}$ to set $Y = \{1, 2, 3\}$ is -----
 - a. 540
 - b. 36
 - c. 729
 - d. 192
8. Let $A = \{1, 5, 8, 9\}$ and $B = \{2, 4, 3\}$ And $f = \{(1, 2), (5, 4), (8, 2), (9, 4)\}$. Is f a surjective function?
 - a. Yes
 - b. No
9. Let $A = \{7, 8, 9\}$ and $B = \{7, 8, 9\}$ and f is onto from A to B then which of the following is correct?
 - a. F is one to one

- b. **F if bijective**
- c. F may be one to one or many to one
- d. None of these.

10. If $f : A \rightarrow B$ is an onto function then range of f is:

- a. Subset of B
- b. A
- c. **B**
- d. Cannot be determined

11. Is the given function onto? $g : \mathbb{R} \rightarrow \mathbb{R}$ defined by $g(x) = 1 + x^2$

- a. Yes
- b. **No**
- c. Cannot decide

12. $f(x) = \sqrt{x}$ and $g(x) = x^2$. What will be range of $(g \circ f)(x)$?

13. f and g are both defined on the set of real numbers and c is a constant $f(x) = cx - 3$ $g(x) = cx + 5$ If $(f \circ g)(x) = (g \circ f)(x)$ for all values of x , what is the value of c ?

14. Given $f(x) = \sqrt{x + 2}$ and $g(x) = \ln(1 - x^2)$, find domain of $(g \circ f)(x)$.

15. State whether the following statement is True/False.

"Composite functions are commutative."