cm1[o] = m1[lc] > m1[rc]; cm1[lc] : cm1[rc];

Team Reference Document ECNU ICPC

Geometry

Ŋ

FORE1GNERS March 2019

good buck from

5.1 5.2 5.3 5.5 5.7 5.8 5.9 5.10

Contents

```
RMQ
Segment Tree Beats
Segment Tree
K-D Tree
STL+
Trie
Trie
                                                                                                                                                                                                                                                                                                                                                              CDQ's Divide and Conquer .
                                                                                                                                                                                                                                                                                                                                                                                                                             Persistent Segment Tree
Persistent Union Find
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First Thing First

        Data Structure

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                                 1.2
                                                                                                          2
```

Math ო

#ifdef zerol

Matrix Power
Sieve
Prime Test
Pollard-Rho
Berlekamp-Massey
Extended Euclidean NTT, FFT, FWT
Simpson's Numerical Integration Factor Decomposition Quadratic Residue Gauss Elimination Primitive Root NTT, FFT, FWT

A> void err(T<t> a, A... x) { for (auto v: a) cout << v << ' '; err

(x...); }
template<typename T, typename... A>
void err(T a, A... x) { cout << a << ' '; err(x...); }
#else</pre>

#define dbg(...)

88888666655

#endif

// for CLion

```
Path Intersection on Trees .
```

Minimum Directed Spanning Tree . . Minimum Directed Spanning Tree 2 . Topological Sort Minimum Directed Spanning Tree General Matching CA

Graph Theory 4

Bernoulli Numbers

Centroid Decomposition (Divide-Conquer)
Heavy-light Decomposition
Bipartite Matching
Wirtla Tree
Euler Tour

Bi-connected Components, Block-cut Tree

LCA
Maximum Flow
Maximum Cost Maximum Flow
Minimum Cost Maximum Flow

Global Minimum Cut

55kai 1.2

inline char nc() {
 static char buf[100000], *p1 = buf, *p2 = buf;
 return p1 == p2 && (p2 = (p1 = buf) + fread(buf, 1, 100000,
 stdin), p1 == p2) ? E0F : *p1++; tempcac.
3 bool rn(T& v) {
3 static char ch;
4 if (ch = EOF && !isdigit(ch)) ch = nc();
4 if (ch = EOF) return false;
4 if (ch = EOF) return false;
6 isdigit(ch); ch = nc();
7 isdigit(ch); ch = nc()) template <typename T>

static int stk[70], tp;
if (p == 0) { putchar('0'); return; }
if (p <= 0) { p = -p; putchar('-'); }
while (p) stk(++tp] = p % 10, p /= 10;
while (tp) putchar(stk[tp-] + '0');</pre> template <typename T>
void o(T p) { Half-plane intersection
Circles
Circle Minimum Covering Circle
Circle Inversion
3 Basics
3 Donvex

Data Structure 2

2.1 RMQ

Aho-Corasick Automation
Hash
Manacher
Manacher
Palindrome Automation
Suffix Auromation
Suffix Auromation

6.1 6.3 6.5 6.5 6.5 6.7

String

ဖ

7.1

Miscellaneous

First Thing First

#include <bits/stdc++.h>

1.1 Header

```
ll[p][q]),
max(f[xx - (1 << p) + 1][y][p][q], f[x][yy - (1 << q) +
ll[p][q])
                                                                             max(f[x][y][p][q], f[xx - (1 << p) + 1][yy - (1 << q) +
                   int f[maxn][maxn][10][10];
inline int highbit(int x) { return 31 - __builtin_clz(x); }
inline int calc(int x, int y, int xx, int yy, int p, int q) {
                                                                 return max(
2 2 2 2 2
```

1,], i + (1 << x) - 1, j + (1 << y)max(x - 1, 0), max(y - 1, 0)

}
inline int get_max(int x, int y, int xx, int yy) {
 return calc(x, y, xx, yy, highbit(xx - x + 1), highbit(yy y + 1)); #define dbg(x...) do { cout << "\033[32;1m" << #x << " -> "; err (x); } while (0) wile (0) void err() { cout << "\033[39;0m" << end!; } } template<typename... typename t, typename...

struct RMQ {
 int f[22][M];
 inline int highbit(int x) { return 31 - __builtin_clz(x); } t) + 1]); assert(l <= r);
int t = highbit(r - l + 1);
return min(f[t][l], f[t][r - (1</pre>

Segment Tree Beats 2.2

} rmd;

set(CMAKE_CXX_FLAGS "\${CMAKE_CXX_FLAGS} -02 -Ddebug -Wall

DULTMASTER -DKBlack -Dzerol")

for University of Porto

setxkbmap us

```
int lc = 0 * 2, rc = lc + 1;
m1[o] = max(m1[lc], m1[rc]);
sum[o] = sum[lc] + sum[rc];
if (m1[lc] == m1[rc]) {
    cm1[o] = cm1[rc] + cm1[rc];
    m2[o] = max(m2[lc], m2[rc]);
                #define Ison o * 2, l, (l + r) / 2
#define Ison o * 2 + 1, (l + r) / 2 + 1,
#int ml(N), m2[N], cml[N];
Lt sum[N];
void up(int o) {
                                                                                                                                                                                                                                                                                  } else
namespace R {
```

```
o->ls = build(l, m, d + 1); o->rs = build(m + 1, r, d +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline bool inside(int p[], int q[], int l[], int r[]) {
    For (i, 0, K) if (r[i] < q[i] || p[i] < l[i]) return
    false;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      query(P* o, int l[], int r[]) {
  if (o == null) return 0;
  FOR (i, 0, K) if (o->r[i] < l[i] || r[i] < o->l[i])
  return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         null->is = null->rs = null;
FOR (i, 0, K) null->l[i] = inf, null->r[i] = -inf;
null->sum = null->val = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         build(p** l, p** r, int d = 0) { // [l, r)
if (d == K) d = 0;
if (l >= r) return null;
p** m = l + (r - l) / 2; assert(l <= m && m < r);
nth_element(l, m r, [&] (const p* a, const p* b);
return a->d[d] < b->d[d];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (d == K) d = 0;
if (o == null) return x->up();
P*& oo = x->d[d] <= 0->d[d] ? 0->ls : 0->rs;
if (oo->sz > 0->sz * lim) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                pt = tmp; FOR (it, pool, pit) *pt++ = it;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 sum = ls->sum + rs->sum + val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  } pool[M], *null = new P, *pit = pool;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             *pt++ = o; dfs(o->ls); dfs(o->rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 pt = tmp; dfs(o); *pt++ = x;
                                                                                                                                                                                                                                                                                                                                                                                                              | LL Sum;
| P *ls, *rs;
| P* up() {
| sz = ls->sz + rs->sz + l;
| - ls->sum + rs->sum + v
                                                                                                                                                                                                                                                                                                 const int K=2, inf = 1E9, M=N; const double lim = 0.7;
                                                                                                                                                                                                                                                                                                                                                                                                        val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return build(tmp, pt, d);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } P* ins(P* o, P* x, int d = 0) {
                                                                                                                                                                                                                                                                                                                                                                                                 int d[K], l[K], r[K], sz,
                                                                                                                                                                                                                   // visit L/R with more potential namespace kd {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 oo = ins(oo, x, d + 1);
return o->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return build(tmp, pt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (o == null) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       static P *tmp[M], **pt;
                                                                                                                                                                                                  // global variable pruning
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return o->up();
                                                                                                                                 K-D Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        null->sz = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void dfs(P* o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 0 = *m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               }
P* Build() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1);
                                                                                                                                                                                                                                                                                                                                                                         struct P {
                                                                                                                                 2.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int update(int o, int ql, int qr, int l, int r, LL add) {
   if (ql > r | | l > qr) return o;
   const P& t = tr[0];
   if (ql <= l && r <= qr) return N(add + t.add, l, r, t.ls
   if (ql <= l && r <= qr) return N(add + t.add, l, r, t.ls</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              1]) + t.sum;
return query(t.ls, lson, add + t.add) + query(t.rs, rson
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return N(t.add, l, r, update(t.ls, lson, add), update(t.
rs, rson, add));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int sz = 1;
int N(LL add, int l, int r, int ls, int rs) {
    tr[sz] = {add, tr[ls].sum + tr[rs].sum + add * (len[r]
    len[l - 1]), ls, rs};
    return sz++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (ql \le l \& r \le qr) return add * (len[r] - len[l - len[l] - l

}
void query(LL p, LL q, LL o, LL l, LL r, LL add, LL& ssum,
LL& smin, LL& smax) {
   if (p > r || l | q) return;
   if (setv[o] != RS) {
        LL v = setv[o] + add + addv[o];
        LL v = setv[o] + add + addv[o];
}

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
LL query(int o, int ql, int qr, int l, int r, LL add = 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    LL m = (l + r) / 2;
update(p, q, ls, v, op); update(p, q, rs, v, op);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           LL \tilde{m} = (1 + r) / 2;
query(p, q, ls, add + addv[o], ssum, smin, smax);
query(p, q, rs, add + addv[o], ssum, smin, smax);
                                                                                                                                                                                                                                                                                                                                                                                                                                      (do
                                                                                                                                                                                                                                                                                                                                                                                                 }
void update(LL p, LL q, LL o, LL l, LL r, LL v, LL
if (p <= r && l <= q)
if (p <= 1 && r <= q) {
   if (op == 2) { setv[o] = v; addv[o] = 0; }
   else addv[o] += v;</pre>
                                                                                                                                                                                                                             };
if (addv[o]) {
    addv[lc] += addv[o]; addv[rc] += addv[o];
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ssum += sumv[o] + add \star (r - l + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        smin = min(smin, minv[o] + add);
smax = max(smax, maxv[o] + add);
                                                                                                                              setv[lc] = setv[rc] = setv[o];
addv[lc] = addv[rc] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (ql > r || l > qr) return 0;
const P& t = tr[0];
                                                                LL lc = o * 2, rc = o * 2 + 1;
if (setv[o] != RS) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          } else if (p <= l && r <= q) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             smin = min(smin, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               smax = max(smax, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             #define mid ((l + r) >> 1)
#define lson ql, qr, l, mid
#define rson ql, qr, mid + 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            , add + t.add);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          maintain(o, l, r);
}
void pushdown(LL o) {
                                                                                                                                                                                                     setv[o] = RS;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        pushdown(o);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int ls, rs;
} tr[maxn * 45 * 2];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           , t.rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        LL add, sum;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // persistent
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              } II;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void update(int ql, int qr, int x, int o, int l, int r) {
   if (r < ql || qr < l || m1[o] <= x) return;
   if (ql <= l && r <= qr && m2[o] < x) { mod(o, x); return</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (setv[0] != RS) { minv[0] = maxv[0] = setv[0]; sumv[o
    ] = setv[0] * (r - l + 1); }
if (addv[0]) { minv[0] += addv[0]; maxv[0] += addv[0];
m2[o] = max(min(m1[lc], m1[rc]), max(m2[lc], m2[rc])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 qr, rson));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     update(ql, qr, x, lson); update(ql, qr, x, rson);
up(o);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return qsum(ql, qr, lson) + qsum(ql, qr, rson);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                #define ls o * 2, l, m
#define rs o * 2 + 1, m + 1, r
static const LL M = maxn * 4, RS = 1E18 - 1;
LL addv[M], setv[M], minv[M], maxv[M];
void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          qsum(int ql, int qr, int o, int l, int r) {
if (r < ql || qr < l) return 0;
if (ql <= l && r <= qr) return sum[o];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void maintain(LL 0, LL 1, LL r) {
   if (l < r) {
      LL lc = 0 * 2, rc = 0 * 2 + 1;
      sunv[0] = sunv[lc] + sunv[rc];
      minv[0] = minv[minv[rc], minv[rc]);
   maxv[0] = max(maxv[lc], minv[rc]);
   else sunv[0] = minv[c] = maxv[rc]);
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     qmax(int ql, int qr, int o, int l, int r)
if (r < ql || qr < l) return -INF;
if (ql <= l && r <= qr) return ml[o];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sumv[o] += addv[o] * (r - l + 1);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return max(qmax(ql, qr, lson), qmax(ql,
                                                                                                                                                                                                  assert(x > m2[0]); sum[0] -= 1LL * (m1[0] - x) * cm1[0];
                                                                                                                                                                                                                                                                                                                                void down(int o) {
  int lc = 0 * 2, rc = lc + 1;
  mod(lc, ml[o]); mod(rc, ml[o]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         fill(setv, setv + M, RS);
memset(minv, 0, sizeof minv);
memset(maxv, 0, sizeof maxv);
memset(sumv, 0, sizeof sumv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              memset(addv, 0, sizeof addv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void build(LL o, LL l, LL r) {
   if (l == r) addv[o] = a[l];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       LL m = (l + r) / 2;
build(ls); build(rs);
                                                                                                                                 void mod(int o, int x) {
  if (x >= m1[o]) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Segment Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   maintain(o, l, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct IntervalTree {
                                                                                                                                                                                                                                                                   m1[o] = x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  down(o);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    down(o);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             down (o)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // set + add
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ij,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             2.3
```

```
void split(P* o, int rk, P*& l, P*& r) {
   if (o == null) { l = r = null; return; }
   if (o->ls->sz >= rk) { split(o->ls, rk, l, o->ls); r = o
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else { split(o->rs, rk - o->ls->sz - 1, o->rs, r); l = o
->up(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (l->rd < r->rd) { l->rs = merge(l->rs, r); return l->
                                                                                                                                                                                                        bool u = v & (1 << d);
return _new(o.w + 1, u == 0 ? ins(o.ls, v, d - 1) : o.ls, u</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int lower(int v) {
   if (this == null) return 0;
   return this->v >= v ? ls->lower(v) : rs->lower(v) +
   ls->sz + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 P(int v): ls(null), rs(null), v(v), sz(1), rd(rnd()) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (u == 0) {
   if (rw) { ret += 1 << d; ret += query(p.rs, q.rs, v, d</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            q.ls, v, d
                                                                                        int _new(int w, int ls, int rs) { tr[sz] = {w, ls, rs}; return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (this == null) return 0;
return this->v > v ? ls->upper(v) : rs->upper(v)
ls->sz + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               P* merge(P* l, P* r) {
   if (l == null) return r; if (r == null) return l;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else { r->ls = merge(l, r->ls); return r->up(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 P* up() { sz = ls->sz + rs->sz + 1; return this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (lw) { ret += 1 << d; ret += query(p.ls,</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else ret += query(p.ls, q.ls, v, d - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else ret += query(p.rs, q.rs, v, d - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } *const null = new P, pool[M], *pit = pool;
                                                                                                                                                                                                                                                                                                int query(int pp, int qq, int v, int d = 30) {
   if (d == -1) return 0;
   bool u = v & (1 << d);
   P &p = tr[pp], &q = tr[qq];
   int lw = tr[q.ls].w. + tr[p.ls].w;
   int rw = tr[q.rs].w - tr[p.rs].w;</pre>
                                                                                                                                                                                                                                                          == 1 ? ins(o.rs, v, d - 1) : o.rs);
                                                                                                                                                          P& o = tr[oo];
if (d == -1) return _new(o.w + 1, 0,
                                                                                                                  sz++; }
int ins(int oo, int v, int d = 30) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     namespace treap {
  const int M = maxn * 17;
  extern struct P* const null;
  struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           namespace treap {
   const int M = maxn * 17 * 12;
struct P { int w, ls, rs; };
P tr[M] = {{0, 0, 0}};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int upper(int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ->up(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P(): sz(0) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        up(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         unsigned rd;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int v, sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Treap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      persistent set
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int ret = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } else
                                               int sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // set
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              2
8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void add(int l, int r, int v) { add(l, v); add(r + 1, -v); } int sum(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
void add(LL l, LL r, LL v) { add(l, v); add(r + 1, -v); }
LL sum(LL x) {
    static LL INV2 = (MOD + 1) / 2;
    LL ret = 0;
    for (LL i = x; i > 0; i -= lowbit(i))
    for (LL i = x; i > 0; i -= lowbit(i))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int sum(int l, int r) { return sum(r) - sum(l - 1); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int ch[N * M][2], sz;
void init() { memset(ch, 0, sizeof ch); sz = 2; }
void ins(LL x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    }
LL sum(LL l, LL r) { return sum(r) - sum(l - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               %
                                                                                                                                                                                                                                                                                                                                                                                                                                   int c[maxn], cc[maxn];
inline int lowbit(int x) { return x & -x; }
void add(int x, int v) {
  for (int i = x; i <= n; i += lowbit(i)) {
      c[i] += v; cc[i] += x * v;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ret += (x + 1) * (x + 2) % MOD * c[i]
- (2 * x + 3) * cc[i] % MOD
                                                                                                                                                                                                     int p = 0;
for (int lim = 1 << 20; lim; lim /= 2)
if (p + lim < M && c[p + lim] < k)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int i = x; i > 0; i == lowbit(i))
    ret += (x + 1) * c[i] - cc[i];
return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FORD (i, M, -1) {
    bool b = x & (1LL << i);
    if (!ch[u][b]) ch[u][b] = sz++;
    u = ch[u][b];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          + ccc[i];
return ret % MOD * INV2 % MOD;
                                                                                     for (; x > 0; x -= lowbit(x))
    ret += c[x];
                                                                                                                                                                                                                                                                                                  k -= c[p];
                                                                                                                                                                                                                                                                          p += lim;
  c[x] += v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           namespace trie {
   const int M = 31;
                                                                                                                                                                                                                                                                                                                                             return p + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int ret = 0;
                                             sum(int x) {
LL ret = 0;
                                                                                                                                                                             int kth(LL k) {
                                                                                                                                  return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int u = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                namespace bit {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          namespace bit {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Trie
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // persistent
// !!! sz = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                2.7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          to
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // mapped: null_typeor or null_mapped_type (old) is null
// Node_Update should be tree_order_statistics_node_update:
use flub_yorder & order_of_key
// find_by_order: find the element with order+1 (0-based)
// order_of_key: number of elements lt r_key
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     using namespace __gnu_pbds;
using Tree = tree<int, null_type, less<int>, rb_tree_tag,
                                                                                                                                                                                                                                                            s)
                                                                                                                                                 pairing_heap_tag: support editing
thin_heap_tag: fast when increasing, can't join
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              s.insert(2, s); // equal to s.replace(2, 0, assert(s[2] == s.at(2)); // 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FOR (i, 0, 5) s.push_back(i); // 0 1 2 3 s.replace(l, 2, s); // 0 (0 1 2 3 4) 3 4 auto ss = s.substr(2, 2); // 1 2 s.erase(2, 2); // 0 1 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         LL c[M];
inline int lowbit(int x) { return x & .
void add(int x, LL v) {
  for (; x < M; x += lowbit(x))</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                tree_order_statistics_node_update>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             #include <ext/pb_ds/assoc_container.hpp>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 #include<ext/pb_ds/assoc_container.hpp>
                                                                                                                                                                                         #include<ext/pb_ds/priority_queue.hpp>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         #include<ext/pb_ds/hash_policy.hpp>
                                                                                                                                                                                                                      using namespace __gnu_pbds;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 using namespace __gnu_pbds;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       gp_hash_table<int, int> mp;
cc_hash_table<int, int> mp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                               assert(pq.top() == 3);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    assert(pq.top() == 5);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                using namespace __gnu_cxx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 assert(pq.top() == 4);
                                                                                                                                                                                                                                                                                                                                                                                                                auto it = pq.push(2);
pq.push(3);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                support join & split
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            pq.modify(it, 4);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         #include <ext/rope>
                                                                                                                         // binary_heap_tag
                                                                                   // priority_queue
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // splay_tree_tag
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // Persistent BBT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              pq.join(pq2);
                                   STL+
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         pq2.push(5);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      namespace bit {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // ov_tree_tag
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // Hash Table
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             B
                                                                                                                                                                                                                                                                                                                                                                                               int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rope<int> s;
                                                                                                                                                                                                                                                                                                                                                    PQ pq, pq2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Tree t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // BBT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           2.6
```

```
P* build(int l, int r, int * a) {
   if (l > r) return nutl;
   if (l = r) return new(pit++) P(a[l]);
   if (l = r) return new(pit++) P(a[l]);
   if m = (l + r) / 2;
   return (new(pit++) P(a[m], build(l, m - 1, a), build(m + 1);
}   if the content of the 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return new P{ls, rs, ls->sz + rs->sz + fill, v, ls->sum
+ rs->sum + v, fill, 1};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (a == null) return b;
if (b == null) return a;
if (rand() % (a->sz + b->sz) < a->sz)
    return N(a->ls, merge(a->rs, b), a->v, a->fill);
else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return N(merge(a, b->ls), b->rs, b->v, b->fill);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (p && val[s[p - 1]] > val[x]) last = s[--p];
if (p) G[s[p - 1]][1] = x;
if (last) G[x][0] = last;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void split(int k, P*& l, P*& r) {
   if (this == null) { l = r = null; return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void go(P* o, int x, int y, P*& l, P*& m, P*& r)
o->split(y, l, r);
l->split(x - 1, l, m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rs->split(k - ls->sz - fill, l, r);
l = N(ls, l, v, fill);
      rt = merge(merge(l, new (pit++) P(v)), r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       P* N(P* ls, P* rs, LL v, bool fill) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     P* N(P* ls, P* rs, LL v, bool fill);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   r = N(r, rs, v, fill);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (ls->sz >= k) {
    ls->split(k, l, r);
                                                                                                                                P *l, *r, * , *t;
split(rt, k - 1, l, t);
split(t, 1, _ , r);
rt = merge(l, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           P *const ls, *const rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1, r, a)))->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Cartesian Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ls->cnt++; rs->cnt++;
                                                                                                  inline void erase(int k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        static int s[N], last;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P* merge(P* a, P* b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          namespace treap {
   struct P;
   extern P*const null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          const int sz, v;
const LL sum;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (x, 1, n + 1) {
last = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // persistent sequence
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              s[p++] = x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bool fill;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int cnt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void build() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int p = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rt = s[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2.9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int sz, val, add, sum;
P(int v, P* ls = null, P* rs = null): ls(ls), rs(rs), sz
(1), val(v), add(0), sum(v) {}
P(): sz(0), val(0), add(0), sum(0) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        P* select(int rk) {
   if (rk == ls->sz + 1) return this;
   return ls->sz >= rk ? ls->select(rk) : rs->select(rk
                                                                                                                                                                                                    if (a == null) return b; if (b == null) return a;
if (rand() % (a->sz + b->sz) < a->sz) { a = a->down(); a
                                                                                                                                                                                                                                                                    ->rs = merge(a->rs, b); return a->up(); } { b = b->down(); b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              } pool[M], *pit = pool, *const null = new P, *rt = null;
                                                                                                                                                                                                                                                                                                                                    ->ls = merge(a, b->ls); return b->up(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     split(o->rs, rk - o->ls->sz - 1, o->rs, r);
l = o->up();
      void split(LL p, P*& l, P*& r) { // FIX & MOD
   if (this == null) l = r = null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   sz = ls->sz + rs->sz + 1; sum = ls->sum + rs->sum + val + add * sz;
                                                                                                                                       } pool[M], *pit = pool, *const null = new P;
P* merge(P* a, P* b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (o == null) { l = r = null; return; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (rand() % (a->sz + b->sz) < a->sz)
    a->down()->rs = merge(a->rs, b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     } else {
   b->down()->ls = merge(a, b->ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ls->upd(add); rs->upd(add);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void split(P* o, int rk, P*& l, P*& r)
                                                                else down()->_split(p, l, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (o->ls->sz >= rk) {
    split(o->ls, rk, l, o->ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    P* merge(P* a, P* b) {
  if (a == null) return b->up();
  if (b == null) return a->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline void insert(int k, int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     assert(this != null);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             - ls->sz - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  }
void upd(int v) {
  if (this == null) re
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  extern struct P*const null;
struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P *l, *r;
split(rt, k - 1, l, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        namespace treap {
  const int M = 8E5 + 100;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return a->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return b->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       add += v;
sum += sz * v;
                                                                                                                                                                                                                                                                                                                                                                                                                                      // sequence with add, sum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           r = 0->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   add = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (add) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               P* down() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         o->down();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P* up() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
p+ down() { return check()->_down(); } // FIX & MOD
void _split(LL p, P+& l, P+& r) { // MOD
if (pos >= p) { ls->split(p, l, r); ls = r; r = up()
                                                                                                                                                                                                                                                             + rs
-> sum
+ <)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int lower(int v) { return rk(v, greater_equal<int>()); }
int upper(int v) { return rk(v, greater<int>()); }
} pool[M], *pit = pool, *const null = new P;
P* merge(P* l, P* r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void split(P* o, int rk, P*& l, P*& r) {
   if (o == null) { l = r = null; return; }
   if (o->ls->sz >= rk) { split(o->ls, rk, l, r); r = new P
        {r, o->rs, o->v}; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rs); return this; } // MOD
P*_do_add(LL v) { add += v; pos += v; return this; } //
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else { split(o->rs, rk - o->ls->sz - 1, l, r); l = new P
                                                                                                                                                                                                                                  sum(ls->sum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         P* up() \{ sz = ls -> sz + rs -> sz + 1; sc = ls -> sc + rs -> sc
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   P* _down() { // MOD
if (rev) { ls = ls->do_rev(); rs = rs->do_rev(); rev
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (add) { ls = ls->do_add(add); rs = rs->do_add(add
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      { rs->split(p, l, r); rs = l; l = up()
                                                                                                                                                              P(P* ls, P* rs, int v): ls(ls), rs(rs), v(v), sz(ls->sz + rs->sz + l),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P* do_rev() { if (this == null) return this; return
    check()->do_rev(); } // FIX & MOD
P* do_add(LL v) { if (this == null) return this; return
    check()->_do_add(v); } // FIX & MOD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (this == null) return 0;
return cmp(this->v, v) ? ls->rk(v, cmp) : rs->rk(v,
cmp) + ls->sz + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         _do_rev() { rev ^{\Lambda} = 1; add *= -1; pos *= -1; swap(ls,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (time == now) return this;
P* t = new(pit++) P; *t = *this; t->time = now;
    return t;
                                                                                                                                                                                                                                                                                                                                                                                                                                             void* operator new(size_t _) { return pit++; }
template<typename T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        + cnt; return this; } // MOD
extern struct P* const null, *pit;
struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   extern struct P* const null, *pit;
struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     {o->ls, l, o->v}; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int rk(int v, T&& cmp) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ); add = 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       persistent set with pushdown
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int sz, time;
LL cnt, sc, pos, add;
bool rev;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 namespace Treap {
  const int M = 10000000;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ··
                                                                       P *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P* check()
                                                                                                     int v, sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else
                                                                                                                                       sum;
                                                                                                                                                                                                                                                                                                                                                                                       P()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ∴ <u>*</u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int now;
```

```
cin >> n >> m;
FOR (i, 1, n + 1) p[i] = new (pit++) P{null, null, INF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                second, x.second, clk});
sort(q.begin(), q.end(), [](const Q& a, const Q& b)->bool {
    return a.l < b.l; });</pre>
                                                                                                                                                                                                                                                                                                                                                  void link(P* u, P* v) { make_root(u); u->fa = v; } void cut(P* u, P* v) { split(u, v); u->fa = v->ls = null; v
                                                                                                                                                                                                                                                          void split(P* u, P* v) { make_root(u); access(v); splay(v);
                                                                                                                                                                                                                                                                                                       bool linked(P* u, P* v) { split(u, v); return u == v || u->
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   auto it = mp.find({u, v}); assert(it != mp.end());
q.push_back({1, u, v, it->second, clk});
                                                                                                                                                                                                                                    void make_root(P* o) { access(o); splay(o); o->do_rev(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }
for (auto& x: mp) q.push_back({1, x.first.first, x.first.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P* t = new (pit++) P {null, null, null, cur.r, t, 0};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   map<P*, int> mp2;
FOR (i, 0, q.size()) {
    Q& cur = q[i];
    int u = cur.u, v = cur.v;
    if (u = cur.tp == 0) {
        if (llinked(p[u], p[v])) puts("N");
        else puts(p[v]->minp->v >= cur.r ? "Y" : "N");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                FOR (_, 0, m) {
    int tp, u, v; scanf("%d%d%d", &tp, &u, &v);
    if (u > v) swap(u, v);
    if (tp == 0) mp.insert({{u, v}, clk});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          } else q.push_back({0, u, v, clk, clk});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             cut(p[old.u], t); cut(p[old.v], t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Mo's Algorithm On Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct Q {
  int u, v, idx;
  bool operator < (const Q& b) const {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             P* t = p[v]->minp;
if (t->v > cur.r) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   link(t, p[u]); link(t, p[v]);
                                                                                                                  void access(P* u, P* v = null)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }
if (linked(p[u], p[v])) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        map<pair<int, int>, int> mp;
                                                                                                                                                                                       access(u->up()->fa, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Q& old = q[mp2[t]];
                                                                                                                                            if (u == null) return;
                                                                                                                                                               splay(u); u->rs = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else if (tp == 1) 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                mp.erase(it);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ü
                                                                                                                                                                                                                                                                                                                                 fa != null; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           null->minp = null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         , p[i], 0};
int clk = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int tp, u, v, l,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     using namespace lct;
                       rot(o);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                mp2[t] =
                                                                     () dn<-o
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             vector<Q> q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  P *p[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int n, m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           2.11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           bool d() { return fa->\s == this; }
P*& c(bool x) { return x ? \s : \rs; }
void do_rev() { if (this == null) return; rev ^= 1; swap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bool has_fa() { return fa->ls == this || fa->rs == this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  } *null = new P{0, 0, 0, INF, 0, 0}, pool[maxm], *pit = pool
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                do_rev(); }}
void all_down() { if (has_fa()) fa->all_down(); down();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bool dd = o->d();
p *f = o->fa, *t = o->c(idd);
p *f = o->fa = f = o->c(idd);
if (f ->has_fa()) f ->fa->fa->c(f ->d()) = o; o->fa = f ->fa;
if (t != null) t ->fa = f; f ->c(dd) = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              o->all_down();
while (o->has_fa()) {
   if (o->fa->has_fa()) rot(o->d() ^ o->fa->d() ? o
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void down() { if (rev) { rev = 0; ls->do_rev(); rs->
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (minp->v' > Ls->minp->v) minp = Ls->minp;
if (minp->v > rs->minp->v) minp = rs->minp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             o \rightarrow c(idd) = f \rightarrow up(); f \rightarrow fa = o;
                       split(u, v);
return u == v || u->fa != null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                         P* up() {
    sz = ls->sz + rs->sz + _sz + 1;
                                                                                                                                            0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   splay(u);
u->_sz += u->rs->sz - v->sz;
                                                                                                                                                                                                                                                                        while (u->rs != null) {
    u = u->rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    split(u, v);
u->fa = v; v->_sz += u->sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      l access(P* u, P* v = null)
if (u == null) return;
                                                                                                                  access(o); splay(o);
while (o->ls != null)
bool linked(P* u, P* v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 access(u->up()->fa, u);
                                                                                                                                                                                  }
P* findfa(P* rt, P* u)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       extern struct P* null;
struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       P *fa, *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        minp = this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return this;
                                                                                                                                                                                                                                                                                                                                                                                                                                      // maintain subtree size
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void link(P* u, P* v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     latest spanning tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     () u->down();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               }
P* findrt(P* o) {
                                                                                                                                                                                                                                  split(rt, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void rot(P* o) {
                                                                                                                                                                                                                                                          = u->ls;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         P *minp;
bool rev;
                                                                                                                                                               return o;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                P* up() {
                                                                                                                                                                                                                                                                                                                                                                   return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       namespace lct {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         u->rs = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    v->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void
                                                                                                                                                                                                                                                                                                                                                                        bool has_fa() { return fa->ls == this || fa->rs == this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void all_down() { if (has_fa()) fa->all_down(); down();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P *f = o->fa, *t = o->c(idd);
if (f->has_fa()) f->fa->c(f->d()) = o; o->fa = f->fa;
if (t i= null) t->fa = f; f->c(dd) = t;
if (t i = null) f->fa = f; f->c(dd) = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             } *const null = new P{0, 0, 0, 0, 0, 0}, pool[M], *pit =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           split(u, v);
return v->ls == u && u->ls == null && u->rs == null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      white (o->has_fa()) {
  if (o->fa->has_fa())
    rot(o->d() ^ o->fa->d() ? o : o->fa);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              p* up() {
    maxv = max(v, max(ls->maxv, rs->maxv));
                                                                                                                       do not forget down when findint L/R most son
                                                                                                                                                                                                                                                                                                                                                                                                                   bool d() { return fa->\s == this; }
P*& c(bool x) { return x ? \s : rs; }
void do_rev() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ls->do_rev(); rs->do_rev();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   make_root(o); access(u); splay(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                access(o); splay(o); o->do_rev();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             split(u, v);
u->fa = v->ls = null; v->up();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (this == null) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void access(P* u, P* v = null)
                                                                                                                                                                                     namespace lct {
   extern struct P *const null;
   const int M = N;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           access(u->up()->fa, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (u == null) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      splay(u); u->rs = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void split(P* o, P* u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   n rיnk(P* u, P* v) {
make_root(u); u->fa
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           }
bool adj(P* u, P* v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void cut(P* u, P* v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void make_root(P* o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool dd = o->d();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void link(P* u, P* v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     swap(ls, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (rev) {
    rev = 0;
                                                                                                                                                                                                                                                                                    P *fa, *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return this;
                                                                                                                                                 // make_root if not sure
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void splay(P* o) {
   o->all_down();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } ()uwop piox
                                                                                                                                                                                                                                                                                                            int v, maxv;
bool rev;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void rot(P* 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rot(o);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             o->nb();
                                                                              {\bf c}
                                                                                                                                                                                                                                                               struct P {
```

```
inline void ls(VI& rt) { transform(rt.begin(), rt.end(), rt.
   begin(), [&!(int x)->int{ return tr[X].ls; }); }
inline void rs(VI& rt) { transform(rt.begin(), rt.end(), rt.
   begin(), [&!(int x)->int{ return tr[X].rs; }); }
int query(VI& p, VI& q, int l, int r, int k) {
   if (l = r) return l;
   int w = ls_sum(q) - ls_sum(p);
   if (k = w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sizeof sz); top = 0; } int findset(int x) { while (fa[x] != -1) \times = fa[x]; return x
                                                                                                                                                                                                int add(int tt, int l, int r, int x, int d) {
   if (x < l | | r < x) return tt;
   const P& t = tr[tt],
   if (l = r) return N(t.w + d, 0, 0);
   return N(t.w + d, add(t.ls, lson, x, d), add(t.rs, rson,</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int i = r; i > 0; i -= lowbit(i)) q.push_back(root[
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             v1 p, q;
for (int i = l - 1; i > 0; i -= lowbit(i)) p.push_back(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int fa[maxn], sz[maxn];
int undo[maxn], top;
void init() { memset(fa, -1, sizeof fa); memset(sz, 0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  root[i] = tree.add(root[i], 1, m, x, d);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void init() { memset(root, 0, sizeof root);
inline int lowbit(int x) { return x & -x; }
void update(int p, int x, int d) {
  for (int i = p; i <= m; i = lowbit(i))</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return query(p, q, rson, k - w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Persistent Union Find
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return tree.query(p, q, 1, m, k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return query(p, q, lson, k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    bool join(int x, int y) {
    x = findset(x); y = findset(y);
    if (x == y) return false;
                                                                                                                                                                                                                                                                                                                                                                             int ret = 0;
FOR (i, 0, rt.size())
ret += tr[tr[rt[i]].ls].w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           TREE() { tr[0] = {0, 0, 0}; }
int N(int w, int ls, int rs) {
    tr[sz] = {w, ls, rs};
    return sz++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FOR (i, 1, m + 1)
bit.update(i, a[i], 1);
                                                                                                                                                                                                                                                                                                                                        int w, ls, rs;
} tr[maxn * 20 * 20];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ls(p); ls(q);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rs(p); rs(q);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                root[i]);
                                                                                                                                                                                                                                                                                                                     ×, d));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int root[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void init() {
    m = 10000;
    tree.sz = 1;
                                                                    int sz = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bit.init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               namespace uf {
    struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            } tree;
struct BIT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      2.14
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              } bit;
                                                                                       int mx = -1;
FOR (i, l, r) {
   if (c[i].d1 && c[i].d2) *c[i].f = max(*c[i].f, mx + 1);
   if (!c[i].d1 && !c[i].d2) mx = max(mx, *c[i].f);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return N(t.sum + v, ins(t.ls, x, v, lson), ins(t.rs, x,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ę,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   [66]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           r = ls
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ۹٦,
                                                                                                                                                                                                                                                                                                                                   gol(l, m);
FOR (i, l, m) a[i].dl = 0;
FOR (i, m, r) a[i].dl = 1;
FOR (i, m, r) a[i].dl = 1;
FOR (i, h, r) b + l);
Sort(b + l, b + r, b + l);
if (a.x i = b.x) return a.x < b.x;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (pp,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           }
int ins(int o, int x, int v, int l = 1, int r = ls)
if (x < l || x > r) return o;
const P& t = tr[o];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     query(int o, int ql, int qr, int l = 1, int r =
if (ql > r || | > qr) return 0;
const P& t = tr[0];
if (ql <= 1 && r <= qr) return t.sum;
return query(t.ls, ql, qr, lson) + query(t.rs, q</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int query(int pp, int qq, int l, int r, int k) { //
if (l == r) return l;
const P &p = tr[pp], &q = tr[qq];
int w = tr[q.ls].w;
if (k <= w) return query(p.ls, q.ls, lson, k);
else return query(p.rs, q.rs, rson, k = w);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Persistent Segment Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (l == r) return N(t.sum + v, 0, 0);
const P& b) -> bool {
   if (a.y != b.y) return a.y < b.y;
   return a.d2 > b.d2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (sz == MAGIC) assert(0);
tr[sz] = {sum, ls, rs};
return sz++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int sz = 1;
int N(int sum, int ls, int rs)
                                                                                                                                                                                                                                                                 void gol(int l, int r) { // [l,
   if (l + 1 == r) return;
   int m = (l + r) >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return a.d1 > b.d1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int sum, ls, rs;
} tr[MAGIC] = {{0, 0, 0}};
                                                                                                                                                                                     }
FOR (i, l, r) b[i] = c[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          #define lson l, mid
#define rson mid + 1, r
const int MAGIC = M * 30;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                namespace tree {
#define mid ((l + r) >> 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    struct TREE {
#define mid ((l + r) >> 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    INTITUTE THE TRANSPORT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                v, rson));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           #define rson mid + 1, r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                typedef vector<int> VI;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                #define lson l, mid
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      go2(l, r);
go1(m, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  with bit
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ij
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // kth
  const Q& a = *this;
return blk[a.u] < blk[b.u] || (blk[a.u] == blk[b.u] &&
in[a.v] < in[b.v]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \begin{split} & go2(1,\,m); \; go2(m,\,r); \\ & FOR \; (i,\,l,\,m) \; b[i].d2 = 0; \\ & FOR \; (i,\,m,\,r) \; b[i].d2 = 1; \\ & merge(b + l,\,b + m,\,b + m,\,b + r,\,c + l,\,[] (\textbf{const} \; P\& \; a,\,) \end{split}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (u == 1) while (sz) blk[S[--sz]] = blk_cnt - 1;
                                                                                                                                                            ..
o
                                                                                                                                                                                                                                                                                                               dfs(v, d + 1);
if (sz - btm >= B) {
    while (sz > btm) blk[S[--sz]] = blk_cnt;
                                                                                                                                void dfs(int u = 1, int d = 0) {
    static int S[maxn], sz = 0, blk_cnt = 0, clk
    in[u] = clk++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          2.12 CDQ's Divide and Conquer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (bug == -1) {
  if (vis[k] && !vis[fa[k]]) bug = k;
  if (!vis[k] && vis[fa[k]]) bug = fa[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bug = -1;
if (vis[b]) bug = b;
if (dep[a] < dep[b]) swap(a, b);</pre>
                                                                                                                                                                                                dep[u] = d;
int btm = sz;
for (int v: G[u]) {
   if (v == fa[u]) continue;
   fa[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (vis[b]) bug = b;
if (dep[a] < dep[b]) swap(a, b)
white (dep[a] > dep[b]) go(a);
white (a != b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } a[maxn], b[maxn], c[maxn];
int f[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void go2(int l, int r) {
   if (l + 1 == r) return;
   int m = (l + r) >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      const int maxn = 2E5 + 100;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       mv(u, q.u); u = q.u;
mv(v, q.v); v = q.v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void mv(int a, int b) {
                                                                                                                                                                                                                                                                                                                                                                                        ++blk_cnt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ans[q.idx] = Ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       go(a); go(b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                (Q& q: query) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  go(a); go(bug);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                dbg(k);
if (vis[k]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void flip(int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void go(int& k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                 }
S[sz++] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool d1, d2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vis[k] ^= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   k = fa[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int ×, y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 flip(k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int* f;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for
```

```
}
!! w[M];
LL idl[M], id2[M], h[M], g[M];
LL idl(LL x) { return x <= B ? id1[x] : id2[N / x]; }
LL go(LL x, LL k) {
   if (x <= 1 || (k >= 0 && pr[k] > x)) return 0;
   Lt t = id(x);
   Lt ms = ffh((g[t] - sg[k + 1]), (h[t] - sh[k + 1]));
   FOR (i, k + 1, pc) {
        Lt p = pr[i];
        if (p * k p > x) break;
        ans = fgh(pg(p), ph(p));
   for (LL pp = p, e = 1; pp <= x; ++e, pp = pp * p)
        ans += fpk(p, e, pp) * (1 + go(x / pp, i)) % MOD</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         (k, 0, pc) {
    LL p = pr[k];
    FOR (i, 0, sz) {
    LL v = w[i]; if (p * p > v) break;
    LL t = id(v / p);
    g[i] = (g[i] - (g[t] - sg[k]) * pg(p) % MOD;
    h[i] = (h[i] - (h[t] - sh[k]) * ph(p)) % MOD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             static bool vis[M];
static LL pr[M], p_sz, d;
FOR (i, 2, M) {
   if (!vis[i]) { pr[p_sz++] = i; f[i] = -1; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 get_prime(B);
int sz = 0;
for (LL l = 1, v, r; l <= N; l = r + 1) {
    v = N / l; r = N / v;
    w[sz] = v; g[sz] = psg(v); h[sz] = psh(v);
    if (v <= B) idl[v] = sz; else idz[r] = sz;
    sz++;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return (go(N, -1) % MOD + MOD + 1) % MOD;
FOR (j, 0, pc) {
   if (pr[j] * i > n) break;
   vis[pr[j] * i] = 1;
   if (i % pr[j] == 0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Ξ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (!v15!..,
FOR (j, 0, p.sz) {
    vis(d) = 1;
    if (i % pr[j] * i) >= M)
    vis(d) = 1;
    if (i % pr[j] == 0) {
        f(d) = 0;
    }
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FOR (i, 2, M) f[i] += f[i - 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline LL s_fg(LL n) { return 1; }
inline LL s_g(LL n) { return n; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     } else f[d] = -f[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        LL id = N / n;
if (vis[id]) return rd[id];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // see cheatsheet for instructions
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 LL go(LL n) {
   if (n < M) return f[n];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   }
return ans % MOD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  vis[id] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           namespace dujiao {
   const int M = 5E6;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LL f[M] = {0, 1};
void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        LL N, rd[M];
bool vis[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FOR
                                                                                                                                                                                                                                                                                                                                                                                                           = i * prime[j]) < p_max;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    = i * prime[j]) < p_max;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                % (d / dd -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         LL pr[M], pc, sg[M], sh[M];
void get_prime(LL n) {
    static boot vis[M]; pc = 0;
    FOR (i, 2, n + 1) {
        if (!vis[i]) {
            pr[pc++1 = i;
            sg[pc] = (sg[pc - 1] + pg(i)) % MOD;
        sh[pc] = (sh[pc - 1] + ph(i)) % MOD;

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else phi[d] = phi[i] * (prime[j] - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         static LL inv2 = (MOD + 1) / 2; 
 x = x \% MOD; 
 return x * (x + 1) \% MOD * inv2 % MOD - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline LL fpk(LL p, LL e, LL pp) { return (pp
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              inline LL fgh(LL g, LL h) { return h - g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // min_25
namespace min25 {
    const int M = 1E6 + 100;
    LL B, N;
    // g(x)
    inline LL pg(LL x) { return 1; }
    inline LL pg(LL x) { return 3, MOD; }
    // Sum[g(i), (x, 2, x)]
    inline LL pg(LL x) { return x, MOD - 1; inline LL pg(LL x) { return x, MOD - 1; inline LL pg(LL x) { return x, MOD - 1; inline LL pgh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL psh(LL x) { return x, MOD - 1; inline LL x,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (i % prime[j] == 0) {
   phi[d] = phi[i] * prime[j];
   break;
                                                                                                                                                                                                                                                                                                                                                                                                           <u>0</u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ٣
                                                                                                                                                                                                                                      ö
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ö
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   static bool vis[p_max];
static LL prime[p_max], p_sz, d;
mu[1] = 1;
FOR (i, 2, p_max) {
   if (ivis[i]) {
       prime[p_sz++] = i;
}
                                                                                                                                                                                                                                                                                                                                                                                                        for (LL j = 0; j < p_sz && ++j) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ++j) {
vis[d] = 1;
if (i % prime[j] == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (LL j = 0; j < p_sz &&
                                                                                                                                                                                                                                   static LL prime[p_max], p_sz,
FOR (i, 2, p_max) {
   if (!vis[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else mu[d] = -mu[i];
                                                                                                                                                                                                                                                                                                                    prime[p_sz++] = i;
phi[i] = i - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    = fgh(g(p), h(p))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  const LL p_max = 1E5 + 100;
LL mu[p_max];
void get_mu() {
    mu[1] = 1;
                                                                                                                                                                               phi[1] = 1;
static bool vis[p_max];
                                                                                         const LL p_max = 1E5 + 100;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ..
0
11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 vis[d] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                mu[i] = -1;
                                        Sieve
                                                                                                                         LL phi[p_max];
void get_phi() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // f(pp=p^{\Lambda}k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       MOD; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // mobius
                                     3.3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (i, 0, M)
FOR (j, 0, M)
printf("%lld%c", (*this)[i][j], j == M - 1 ? '\
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ret[i][j] = (ret[i][j] + A[i][k] * B[k][j]) 
% MOD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   LL mul(LL u, LL v, LL p) { return (u * v - LL((long double) u * v / p) * p + p) % p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (i, 0, M)
FOR (j, 0, M)
ret[i][j] = (A[i][j] + B[i][j]) % MOD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           LL mul(LL u, LL v, LL p) { // better constant
LL t = u * v - LL((long double) u * v / p) * p;
return t < 0 ? t + p : t;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (x %= MOD; n; n >>= 1, x = mul(x, x, MOD))
if (n & 1) ret = mul(ret, x, MOD);
return ret;
                                                                                                                                    }
inline int checkpoint() { return top;
void rewind(int t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            3.1 Multiplication, Powers
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FOR (K, 0, M)
FOR (i, 0, M) if (A[i][k])
FOR (i, 0, M)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Mat A = *this, ret; ret.eye();
for (; n; n >>= 1, A = A * A)
   if (n & 1) ret = ret * A;
return ret;
if (sz[x] > sz[y]) swap(x, y);
undo[top++] = x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 B) {
                                                                                                                                                                                                                                                     int x = undo[--top];
sz[fa[x]] -= sz[x] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    }
Mat operator + (const Mat& B)
const Mat& A = *this;
Mat ret;
...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    i( - - - - u
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Matrix Power
                                                         fa[x] = y;
sz[y] += sz[x] + 1;
return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       static const LL M = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }
Mat pow(LL n) const {
                                                                                                                                                                                                                        while (top > t)
                                                                                                                                                                                                                                                                                                              fa[x] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void prt() const {
  FOR (i, 0, M)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Math
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct Mat {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    3.2
```

```
FOR (i, 2, n)
inv[i] = (p - p / i) * inv[p % i] % p;
                                                                                                                                                          LL invf[M], fac[M] = {1};
void fac_inv_init(LL n, LL p) {
   FOR (i, 1, n)
   fac[i] = i * fac[i - 1] % p;
   invf[n - 1] = bin(fac[n - 1], p - 2, p);
   FORD (i, n - 2, -1)
   invf[i] = invf[i + 1] * (i + 1) % p;
                                                                                                                                                                                                                                                                                                                                                                      3.9 Binomial Numbers
                                   void inv_init(LL n, LL p) {
    - m] % MOD;
                                                             inv[1] = 1;
                      inv[N];
                        Ⅎ
                                                                                                                                                                                                                                                               %
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        t.clear(); for (auto\& v: b) t.push_back(d * v % MOD)
                                                                                                                                 int k = (int) m.size() - 1; assert (m[k] == -1 || m[k]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   - 1 - j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             LL d = 0, la = a.size();
FOR (j, 0, la) up(d, a[j] * x[i - la + 1 + j]);
if (d == 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          1b = max(la, lb);
FOR (j, 0, la) up(t[lb - 1 - j], a[la
if (lb > la) {
                                                             for (; n; n >>= 1, x = mul(x, x, m, k))
if (n & 1) r = mul(x, r, m, k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (_, 0, la - lb) t.push_back(0);
                                                                                                                                                                                                                                                                                                V r = pow(n - 1, a);
LL ans = 0;
FOR (i, 0, k) up(ans, r[i] * x[i]);
return (ans + MOD) % MOD;
                        == MOD - 1);
V r(k), x(k); r[0] = x[1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                              return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           static vector<LL> t = \{2, 325, 9375, 28178, 450775, 9780504,
                                                                                                                                                                                                                                                                                                                                       bool checkQ(LL a, LL n) {
   if (n == 2 || a >= n) return 1;
   if (n == 1 || !(n & 1)) return 0;
   if n == 1 || !(n & 1) return 0;
   LL d == n - 1;
   while (!(d & 1)) d >>= 1;
   LL t = bin(a, d, n); // usually needs mul-on-LL
   while (d != n - 1 && t != 1 && t != n - 1) {
        t = mul(t, t, n);
        t = mul(t, t, n);
}
                                                       ret == (s_g(r) - s_g(l - 1)) * go(v);
ret = rd[id] = s_fg(n);
(LL l = 2, v, r; l <= n; l = r + 1)
v = n / l; r = n / v;
                                                                                                                                                                          memset(vis, 0, sizeof vis);
return go(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return t == n - 1 \mid \mid d \& 1;
                                                                                                                                                                                                                                                                                                      Prime Test
                                                                                                                                     solve(LL n) {
N = n;
                                                                                                    return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bool primeQ(LL n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            d <<= 1;
    for
                                                                                                                                                                                                                                                                                                    3.4
```

Extended Euclidean 3.7

mt19937 mt(time(0));
LL polLand_rho(Ln LL c) {
 LL x = uniform_int_distribution<LL>(1, n - 1)(mt), y = x;
 auto f = [&](LL v) { LL t = mul(v, v, n) + c; return t < n ?</pre>

Pollard-Rho

3.5

x = f(x); y = f(f(y));
if (x == y) return n;
LL d = gcd(abs(x - y), n);
if (d != 1) return d;

t: t - n; };

while (1) {

```
inline int ctz(LL x) { return __builtin_ctzll(x); }
LL gcd(LL a, LL b) {
   if (!a) return b; if (!b) return a;
   int t = ctz(a | b);
LL ex_gcd(LL a, LL b, LL &x, LL &y) {
   if (b == 0) { x = 1; y = 0; return a; }
   LL ret = ex_gcd(b, a % b, y, x);
   y == a / b * x;
   return ret;
                                                                                                                                                                                                                                                                                                                                                    if (a > b) swap(a, b);
                                                                                                                                                                                                                                                                                                                             b >>= ctz(b);
                                                                                                                                                                                                                                                                                                                                                                                                    } while (b);
return a << t;</pre>
                                                                                                                                                                                                                                                                            a >>= ctz(a);
do {
```

void get_fac(LL n, LL cc = 19260817) {
 if (n == 4) { fac[fcnt++] = 2; fac[fcnt++] = 2; return; }
 if (primeQ(n)) { fac[fcnt++] = n; return; }

LL fac[100], fcnt;

LL p = n; while (p == n) p = pollard_rho(n, --cc); get_fac(p); get_fac(n / p);

Berlekamp-Massey

Inverse 3.8

namespace BerlekampMassey {
 inline void up(LL& a, LL b) { (a += b) %= MOD; }
 v widconst V&a, const V& b, const V& m, int k) {
 V r; r.resize(2 * k - 1);
 FOR (i, 0, k) FOR (j, 0, k) up(r[i + j], a[i] * b[j]);
 FOR (i, 0, k) w (r[i + j], r[i + k] * m[j]);
 r.pop_back();

} V pow(LL n, const V& m)

return r;

```
// if p is prime
inline LL get_inv(LL x, LL p) { return bin(x, p = 2, p); }
// if p is not prime
LL get_inv(LL a, LL M) {
                                                                                                               assert(exgcd(a, M, x, y)
return (x % M + M) % M;
                                                                                               static LL x, y;
```

```
inline LL C(LL n, LL m) { // n >= m >= 0 return n < m || m < 0 ? 0 : fac[n] * invf[m] % MOD * invf[n
                                                  }
// The following code reverses n and m
LL C(LL n, LL m) { // m >= n >= 0
Lif (m - n < n) n = m - n;
if (n < 0) return 0;
LL ret = 1;
FOR (i, 1, n + 1)
ret = ret * (m - n + i) % MOD * bin(i, MOD - 2, MOD);

ROD;
                                                                                                                                                                                                                                 FOR (j, 1, i) C[i][j] = (C[i - 1][j] + C[i - 1][j - 1]) % MOD;
                                                                                                                                                                                                                                                                                                                                                                          FOR (\bar{1}, 0, n) {
C[i][0] = C[i][i] = 1;
                                                                                                                                                                                                                                                                                                                                          LL C[M][M];
void init_C(int n) {
                                                                                                                                                                                                                                                                                                                     // precalculations
LL C[M][M];
```

inv %

LL inv = -get_inv(d, MOD);
for (auto& v: b) v = v * ir

b.swap(a);

if (n <= 1) return false; for (LL k: t) if (!checkQ(k, n)) return false;

return true;

for (auto& v: a) up(v, MOD);
return a;

a.swap(t);

NTT, FFT, FWT 3.10

```
for ( ; n < n_.; n <<= 1) ++step; FOR (i, 1, n) rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (step - 1));
                                                                                                                                                                                                                      LL y = a[\dot{1} + \dot{j} + k] * w % MOD;

a[\dot{1} + \dot{j}] = (x + y) % MOD;

a[\dot{1} + \dot{j} + k] = (x - y + MOD) % MOD;
                                                                                                                      int g = bin(G, (MOD - 1) / n, MOD);
wn[0] = 1;
                                                                                                                                                   for (int i = 1; i <= n; ++i)
wn[i] = wn[i - 1] * g % MOD;</pre>
            LL wn[N << 2], rev[N << 2];
int NTT_init(int n_) {
   int step = 0; int n = 1;</pre>
                                                                                                                                                                                           return n;
// NTT
```

```
- 1) >> 1, p); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           res., = (a.x * b.x + a.y * b.y % p * w) % res.y = (a.x * b.y + a.y * b.x) % p; return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             bin(P x, LL n, LL MOD) {
    P ret = {1, 0};
    for (; n; n >>= 1, x = pmul(x, x, MOD))
    if (n & 1) ret = pmul(ret, x, MOD);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }! Legendre(LL a, LL p) { return bin(a, (p :
LL equation_solve(LL b, LL p) {
   if (p == 2) return 1;
   if (p == 2) return 1;
}
                                                                                                                                                                                                                                                              Factor Decomposition
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         pmul(const P& a, const P& b, LL p) {
    P res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if ((Legendre(b, p) + 1) % p == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      3.15 Quadratic Residue
                                                                                                                                                                                                                                                                                                    LL factor[30], f_sz, factor_exp[30];
void get_factor(LL x) {
                                                                                                                                                                                                                                                                                                                                             f_sz = 0;

LL t = sqrt(x + 0.5);

for (LL i = 0; pr[i] <= t; ++i)

if (x % pr[i] == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ++factor_exp[f_sz];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     factor[f_sz++] = pr[i];
                                                                                                                                                                                                                                                                                                                                                                                                                              factor_exp[f_sz] = 0;
while (x % pr[i] == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Primitive Root
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   factor_exp[f_sz] = 1;
factor[f_sz++] = x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             LL q1, q2, w;
struct P { // x + y * sqrt(w)
                                                 FORD (i, m - 1, -1) {
    LD s = a[i[m];
    FOR (j, i+1, m)
    s -= a[i[i]; * x[i];
    x[i] = s / a[i][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (flag) return i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     assert(0); return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             a = rand() % p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while (true) {
}
return m - r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (x > 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     LL x, y;
                                                                                                                                                                             return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             3.14
                                                                                                                                                                                                                                                                                                                                                                                                         LD asr(LD 1, LD r, LD eps, LD S) {
    LD m = (1 + r) / 2;
    LD L = simpson(1, m), R = simpson(m, r);
    if (fabs(L + R - S) < 15 * eps) return L + R + (L + R - S) /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         <u>_</u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       LD asr(LD l, LD r, LD eps) { return asr(l, r, eps, simpson(l,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   LD a[maxn] [maxn], x[maxn];
bool free x[maxn],
intine int sgn(LD x) { return (x > eps) - (x < -eps); }
int gaus.s(LD a[maxn] [maxn], int n, int m) {
    memset(free_x, 1, sizeof free_x); memset(x, 0, sizeof x);
    int r = 0, c = 0;
    while (r < n && c < m) {
        int m.r = r;
    }
</pre>
                                                                                                                                                                                                                                                                    Simpson's Numerical Integration
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return asr(l, m, eps / 2, L) + asr(m, r, eps / 2, R);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // n equations, m variables
// a is an n x (m + 1) augmented matrix
// free is an indicator of free variable
// return the number of free variables, -1 for "404"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FOR (i, r + 1, n)

if (fabs(a[i][c]) > fabs(a[m_r][c])) m_r = i;

if (m_r != r)
                                                                                                                                                                                                                                                                                                       LD simpson(LD 1, LD r) {
    LD c = (1 + r) / 2;
    return (f(l) + 4 * f(c) + f(r)) * (r - l) / 6;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  -= a[r][j] * t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    LD s = a[i][m];

FOR (j, 0, m)

if (j != k) s -= a[i][j] * x[j]];

free_x[k] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (sgn(a[i][j]) && free_x[j]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Gauss Elimination
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (i, r + 1, n)
if (a[i][c]) {
LD t = a[i][c] / a[r][c];
FOR (j, c, m + 1) a[i][j]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
FOR (i, r, n)
if (sgn(a[i][m])) return -1;
                                                                                                                                c[i+j][x] += \tilde{a}[\tilde{i}][x] * b[j][x]

rfwt(c[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(f_cnt > 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         FORD (i, r - 1, -1) {
   int f_cnt = 0, k = -1;
   FOR (j, 0, m)
                                                                                                                                                                               ans[x] = c[popcount(x)][x]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ++f_cnt; k = j;
                                                                      a[popcount(x)][x] = A[x]
b[popcount(x)][x] = B[x]
fwt(a[i]) fwt(b[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FOR (j, c, m + 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ++r; ++c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int n, m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          3.12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (int h = 2; h <= n; h <<= 1) {
    cwn(cos(p * 2 * PI / h), sin(p * 2 * PI / h));
    for (int i = 0; i < n; i += h) {
        Cw(1, 0), u;
    for (int j = i, k = h >> 1; j < i + k; ++j) {
        u = x[j + k] * w;
        x[j + k] = x[j] - u;
        x[j] = x[j] - u;
    w = w * wn;
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return C(a.r * b.r - a.i * b.i, a.r * b.i + a.i * b.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void FFT(C x[], int n, int p) {
  for (int i = 0, t = 0; i < n; ++i) {
    if (i > t) swap(x[1], x[t]);
    for (int j = n >> 1; (t ^= j) < j; j >>= 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void fwt(LL all, int n, T f) {
   for (int d = 1; d < n; d *= 2)
   for (int i = 0, t = d * 2; i < n; i += t)
   FOR (j, 0, d)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  f(a[i + j], a[i + j + d]);
                                                                                                                                                                                                                                                                                 C(LD \ r = 0, \ LD \ i = 0): r(r), \ i(i) \ \{\}
                                                                                                                                                                                                                                                                                                       } C operator * (const C& a, const C& b) {
                                    LL ninv = get_inv(n, MOD);
FOR (i, 0, n)
a[i] = a[i] * ninv % MOD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void AND(LL& a, LL& b) { a += b; }
void OR(LL& a, LL& b) { b += a; }
void XOR (LL& a) LL& b) {
    LL x = a, y = b;
    a = (x + y) % MOD;
    b = (x - y + MOD) % MOD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // C_k = \sum_{{i \oplus j=k} A_i B_j
template<typename T>
                                                                                                                                                                                                                                                                                                                                               return C(a.r + b.r, a.i + b.i);
                                                                                                                                                                                                                                                                                                                                                                                                           return C(a.r - b.r, a.i - b.i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void rAND(LL& a, LL& b) { a -= b; }
void rOR(LL& a, LL& b) { b -= a; }
void rXOR(LL& a, LL& b) {
    static LL INV2 = (MOD + 1) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          LL \times = a, y = b;

a = (x + y) * INV2 % MOD;

b = (x - y + MOD) * INV2 % MOD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void conv(C a[], C b[], int n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FFT(a, n, 1);
FFT(b, n, 1);
FOR (i, 0, n)
a[i] = a[i] * b[i];
FFT(a, n, -1);
                                                                                                                                                                               1/n needs to be power of typedef double LD;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (i, 0, n)
x[i].r /= n;
                                                                                                                                                                                                                     const LD PI = acos(-1);
                 (f == -1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (p == -1)
                                                                                                                                                                                                                                           struct C {
                                                                                                                                                         // FFT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // FWT
```

}
int DFS(int u, int cp) {

return d[t];

static map<LL, LL> mp; mp.clear();
LL m = sqrt(p + 1.5);
LL v = 1;

// x = 0 should satisfy the constraints // initialize v to be 0 // n is dimension of vector, m is number of constraints // min{ b x } / max { c x } // x >= c / A x <= b // x >= 0

Simplex Method

3.18

FOR (i, 1, m + 1) { v = v * a % p;mp[v * b % p] = i;

Q.push(e.to);

```
}
FOR (i, i, m + 1) {
    q = q * v % p;
    auto it = mp.find(q);
    if (it != mp.end()) return i * m - it->second + c;
                                                                                                                                                                                                                                                                                                                                                                                                                                        void dfs(int u, int fa) {
    pa[u][0] = fa; dep[u] = dep[fa] + 1;
    PCR (i, 1, SP) pa[u][i] = pa[pa[u][i - 1]][i - 1];
    for (int& v: G[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void init(int n, int s, int t) {
    this->s = s; this->t = t;
    for (int i = 0; i <= n; i++) 6[i].clear();</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (!d[e.to] && e.cp > 0)
d[e.to] = d[x] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       \updownarrow
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             cap)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while (!Q.empty()) {
  int x = Q.front(); Q.pop();
  for (int& i: G[x]) {
    E &e = edges[i];
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int to, cp;
E(int to, int cp): to(to), cp(cp)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void addedge(int u, int v, int c
edges.emplace_back(v, cap);
edges.emplace_back(u, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return u == v ? u : pa[u][0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              static const int M = 1E5 \times 5;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool BFS() {
    memset(d, 0, sizeof d);
    queue<int> 0;
    Q.push(s); d[s] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       4.2 Maximum Flow
                                                                                                                                                                                                                                                                                                            Graph Theory
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (v == fa) continue;
dfs(v, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  edges.clear(); m = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  G[u].push_back(m++);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             G[v].push_back(m++);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int m, s, t;
vector<E> edges;
vector<int> G[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int cur[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct Dinic {
                                                                                                                                                                                                                                                                                                                                                                                   4.1 LCA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int d[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               struct E {
                                                                                                                                                                                                                                                                                                               4
                                                                                                                                                                                                                                                 FOR (i, 0, m)
if (i != l && fabs(a[i][e]) > 0) {
    b[i] -= a[i][e] * b[l];
    FOR (j, 0, n)
    if (j != e) a[i][j] -= a[i][e] * a[l][j];
    a[i][e] = -a[i][e] * a[l][e];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int e = -1, l = -1; FOR (i, 0, n) if (c[i] > eps) { e = i; break; } if (e = -1) return v; double t = INF;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FOR (j, 0, n) if (j != e) c[j] -= c[e] * a[l][j]; c[e] = -c[e] * a[l][e];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FOR (i, 0, m)

if (a[i][e] > eps && t > b[i] / a[i][e]) .

t t = b[i] / a[i][e];

l = i;
                                                                                                                void privot(int l, int e) {
    b[1] /= a[1][e];
    FOK (j, 0, n) if (j != e) a[1][j] /= a[1][e];
    a[1][e] = 1 / a[1][e];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // p can be not a prime

LL exBSGS(LL a, LL b, LL p) { // a^x = b (mod p)

a %= p; b %= p;

if (a == 0) return b > 1 ? -1 : b == 0 && p != 1;

LL C = 0 q = 1;

while (1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     LL g = __gcd(a, p);
if (g == 1) break;
if (b == 1) return c;
if (b % g) return -1;
++c; b /= g; p /= g; q = a / g * q % p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // \rho is a prime LL BSGS(LL a, LL b, LL p) { // a^{\Lambda}x = b \pmod{a}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (1a & !b) return 1;
if (1a) return -1;
staric map(LL, LL> mp; mp.clear();
LL m = sqrt(p + 1.5);
LL v = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       == -1) return INF;
                                   int n, m;
double a[M][N], b[M], c[N], v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          mp[v \star b \% p] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                             v += c[e] * b[l];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     pivot(l, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FOR (i, i, m + 1) { v = v * a \% p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                double simplex() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             BSGS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ;;
        namespace lp {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      a %= p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (i, 1, k + 2) ret += C[k + 1][i] * B[k + 1 - i] % MOD * p[i] % MOD
                                                                                                                                                                                                                                                                                                                                                                                               LL y = p - x;
if (x == y) cout << x << endl;
else cout << min(x, y) << " " << max(x, y) << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              init_C(M);
FOR (i, 1, M - 1) {
LL& s = B[i] = 0;
FOR (j, 0, i)
s += C[i + 1][j] * B[j] % MOD;
s = (s % MOD * -inv[i + 1] % MOD + MOD) % MOD;
                                                                                                                                                                           (d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Chinese Remainder Theorem
                                                                                                                                                                        // Given a and prime p, find x such that x*x=a \pmod{\frac{1}{\ln t}} main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LL M = m[0], R = r[0], x, y, d;

FOR (i, 1, n) {

    d = ex.gcd(M, m[i], x, y);

    x = [r[i] - R) % d) return -1;

    x = [r[i] - R) / d * x % (m[i] / d);

    R += x * M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (i, 1, k + 2)

p[i] = p[i - 1] * (n + 1) % MOD;

LL ret = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ret = ret % MOD * inv[k + 1] % MOD;
return ret;
w = ((a * a - b) % p + p) % p;
if ((Legendre(w, p) + 1) % p == 0)
break;
                                                                                                                  return bin({a, 1}, (p + 1) >> 1, p).x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Bernoulli Numbers
                                                                                                                                                                                                                                                                               LL x = equation_solve(a, p);
if (x == -1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return R >= 0 ? R : R + M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (k == 0) return n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LL CRT(LL *m, LL *r, LL n) {
   if (!n) return 0;
                                                                                                                                                                                                                          LL a, p; cin >> a >> p;
a = a % p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           namespace Bernoulli {
   LL inv[M] = {-1, 1};
   LC (M] [M];
   void init();
   LL B[M] = {1};
   void init() {
        void in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 }

LL p[M] = {1};

LL go(LL n, LL k) {

n %= MOD;

'' == 0) retur
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          = M / d * m[i];
%= M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inv_init(M, MOD);
                                                                                                                                                                                                                                                                                                                                                puts("No root");
                                                                                                                                                                                                                                                                                                                                                                             } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          3.16
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         3.17
```

```
return p[r].s - p[l - 1].s + 1LL * (r - l + 1) * d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 get_dep(u, -1, 0);
VP* rt = pit++; tr[u].push_back({rt, nullptr, 0});
for (E& e: G[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool cmp(const P& a, const P& b) { return a.w < b.w; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  r = upper_bound(p.begin(), p.end(), P{r, -1},
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int main() {
    cin >> n >> 0, >> A;
    FOR (i, 1, n + 1) scanf("%d", &w[i]);
    FOR (., 1, n) {
    int u, v, d; scanf("%d%d%d", &u, &v, &d);
    int u, v, d; scanf("%d%d%d", &u, &v, &d);
                                                                                                                                   }
PORD (i, p - 1, -1) {
    u = q[i];
    mx[u] = max(mx[u], p - sz[u]);
    if (mx[u] * 2 <= p) return u;
    sz[fa[u]] * = sz[u];
    mx[fa[u]] = max(mx[fa[u]], sz[u]);
</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                      if (vis[v] || v == fa) continue;
get_dep(v, u, d + e.d);
md[u] = max(md[u], md[v] + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void go(int u, int fa, VP* rt, VP* rt2)
tr[u].push_back({rt, rt2, dep[u]});
for (E& e: 6[u]) {
    int v = e.to;
    if (v = fa || vis[v]) continue;
    go(v, u, rt, rt2);
                                                                                                                                                                                                                                                                                                                                         int dep[maxn], md[maxn];
void get_dep(int u, int fa, int d)
    dep[u] = d; md[u] = 0;
    for (E& e: G[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                };
VP pool[maxn << 1], *pit = pool;
vector<R> tr[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (vis[v]) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                go(v, u, rt, pit++);
dfs(v);
                                                                                                                                                                                                                                                                                                                                                                                                                     int v = e.to;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int v = e.to;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          using VP = vector<P>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              u = get_rt(u);
vis[u] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        struct R {
   VP *rt, *rt2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void dfs(int u) {
                                                                                                                                                                                                                                                                                         assert(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int dep;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int w;
LL s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct P {
                                                                                                                                                                                                                                                                 (Divide-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int get_rt(int u) {
    static int q[N], fa[N], sz[N], mx[N];
    int p = 00, cur = -1;
    q[p+1] = u; fa[u] = -1;
    while (++cur < p) {
        u = q[cur]; mx[u] = 0; sz[u] = 1;
        vi f (cur); mx[u] = 0; sz[u] = 1;
        for (int& v: G[u])
        if (ivis[v] && v != fa[u]) fa[q[p++] = v] = u;</pre>
                                                                                                                                                                                                                                                                                                                                                                                         int tt = lca(t[2], t[3]);
int ret = 1 + dep[t[2]] + dep[t[3]] - dep[tt] * 2;
return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Decomposition
                                                                                                                                                                                                                                  Path Intersection on Trees
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             mx[fa[u]] = max(mx[fa[u]], sz[u]);
                                                                     int go() {
  int flow = 0, cost = 0;
  while (BellmanFord(flow, cost));
  return cost;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               const int maxn = 15E4 + 100, INF = 1E9;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         mx[u] = max(mx[u], p - sz[u]);
if (mx[u] * 2 <= p) return u;
sz[fa[u]] += sz[u];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int v = e.to;
if (vis[v]) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // dynamic divide and conquer
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  }
FORD (i, p - 1, -1) {
    u = q[i];
    ... /mx[i],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       get_dep(u, -1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (E& e: G[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Conquer)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Centroid
     }
return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int get_rt(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           u = get_rt(u);
vis[u] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vector<E> G[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int n, Q, w[maxn];
LL A, ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 dfs(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          bool vis[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          assert(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int to, d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int sz[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                struct E {
                                                                                                                                                                                                                                  4.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       4.5
                                                                                                                                                                , MM .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int n, m, s, t;
vector<E> edges;
vector<int> follown];
bool inq[maxn];
int d[maxn];
int almaxn]; // the last edge id of the path from s to i
int almaxn]; // least remaining capacity from s to i
int almaxn]; // least remaining capacity from s to i
void init(int _n, int _s, int _t) {}
void addedge(int from, int to, int cap, int cap;
edges.emplace_back(from, to, cap, cost);
edges.emplace_back(from, to, cap, cost);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            E(int f, int t, int cp, int v) : from(f), to(t), cp(cp), v(v
for (int& idx: G[u]) {
    E &e = edges[idx];
    if (e.cp && d[e.to] > d[u] + e.v) {
        d[e.to] = d[u] + e.v;
        p[e.to] = idx;
        a[e.to] = min(a[u], e.cp);
    if (linq[e.to]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     4.3 Minimum Cost Maximum Flow
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool BellmanFord(int &flow, int &cost) {
   FOR (i, 0, n + 1) d[i] = INF;
   memset(inq, 0, sizeof inq);
   d[s] = 0, a[s] = INF, inq[s] = true;
   queue<int> Q; Q.push(s);
                                                                                                                                   edges[G[u][i] ^ 1].cp += f;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ing[e.to] = true;
                                                                                                                                                                                                                                                                                                                         memset(cur, 0, sizeof cur);
flow += DFS(s, INF);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int u = Q.front(); Q.pop();
inq[u] = false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while (u i = s) {
    edges[p[u]].cp = a[t];
    edges[p[u] ^ 1].cp += a[t];
    u = edges[p[u]].from;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (d[t] == INF) return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Q.push(e.to);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       [from].push_back(m++);
                                                                                                                                                         cp -= t;
if (!cp) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          G[to].push_back(m++);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    flow += a[t];
cost += a[t] * d[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          while (!Q.empty()) {
                                                                                                                                                                                                                                            return tmp - cp;
                                                                                                                      e.cp -=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int from, to, cp, v;
                                                                                                                                                                                                                                                                                                                                                                                  return flow;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int u = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \(\tau\)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      };
struct MCMF {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         struct E {
                                                                                                                                                                                                                                                                                                                                                                                                                     } DC;
```

```
FOR (j, 0, n) if (visL[j]) L[j] -= d;
FOR (j, 0, m) if (visR[j]) R[j] += d; else slack
                                                                                                            int d = ox3f3f3f3f;
FOR (j, 0, m) if (!visR[j]) d = min(d, slack[j])
                                                                                                                                                                                                                                                               int ret = 0;
FOR (i, 0, m) if (left[i] != -1) ret += w[left[i]][i];
return ret;
                                                        memset(visL, 0, sizeof visL); memset(visR, 0,
    sizeof visR);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline bool cmp(int a, int b) { return in[a] < in[b]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  go(V, ++k);
if (key[to]) f[u] += w[to];
else f[u] += min(f[to], (LL)w[to]);
} else break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            a.erase(unique(a.begin(), a.end()), a.end());
(i, 0, n) {
  memset(slack, 0x3f, sizeof slack);
while (1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             sort(a.begin(), a.end(), cmp);
FOR (i, 1, a.size())
a.push_back(lca(a[i], a[i - 1]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int v = edges[eid].get_other(u);
G[u].erase(eid);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int v = e.to;
if (v == pa[u][0]) continue;
while (k + 1 < V.size()) {
   int to = V[k + 1];
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          static vector<int> a; a.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (in[to] <= out[v]) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int& x: V) a.push_back(x);
                                                                                            if (dfs(i)) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         sort(a.begin(), a.end(), cmp);
                                                                                                                                                                                                                                                                                                                                                                                                                                          void go(vector<int>& V, int& k) {
                                                                                                                                                                                                           -= d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int u = start;
top = 0; path.clear();
S[top++] = u;
while (top) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int tmp; go(a, tmp = 0);
return f[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                             int u = V[k]; f[u] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         LL solve(vector<int>& V) {
                                                                                                                                                                                                                                                                                                                                                                                                         Virtual Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dbg(u, k);
for (auto& e: G[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    S[top++] = u;
for (int eid: G[u]) {
                                                                                                                                                                                                               Ξ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             G[v].erase(eid);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void fleury(int start) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Euler Tour
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         a.push_back(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int S[N << 1], top;
Edge edges[N << 1];
set<int> G[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dbg(u, f[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void DFS(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 DFS(v);
return;
 FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              dbg(a);
                                                                                                                                                                                                                                                                                                                                                                                                         4
8.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      4.9
int finds(int u, int rt) { // find u in which sub-tree of
  while (top[u] != top[rt]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                bool dfs(int u) {
    for (int v: G[u])
    if (vis[v] != clk) {
        vis[v] = clk;
        vis[v] = clk;
    if (left[v] == 1 || dfs(left[v])) {
        left[v] = u;
    return true;
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (left[v] == -1 || dfs(left[v])) {
    left[v] = u;
    return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } else slack[v] = min(slack[v], t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FOR (i, 0, n)
FOR (j, 0, m)
L[1] = max(L[1], w[i][j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vist[u] = true;
FOR (v, 0, m)
if (vist[v]) continue;
int t = L[u] + R[v] - w[u][v];
                                                                                                                                                                                                                                                                                                                                                            this->n = n;
FOR (i, 0, n + 1) G[i].clear();
memset(left, -1, sizeof left);
memset(vis, -1, sizeof vis);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int match() {
  int ret = 0;
  for (clk = 0; clk <= n; ++clk)
   if (dfs(clk)) ++ret;
  return ret;</pre>
                                    u = top[u];
if (fa[u] == rt) return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    memset(left, -1, sizeof left);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int left[maxn], L[maxn], R[maxn];
int w[maxn] [maxn], slack[maxn];
bool visL[maxn], visR[maxn];
                                                                                                                                                                                                           Bipartite Matching
                                                                                                                                                                                                                                                                                                          int vis[maxn], left[maxn], clk;
                                                                                                                return ridx[idx[rt] + 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                visR[v] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       memset(R, 0, sizeof R);
memset(L, 0, sizeof L);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   namespace R {
   const int maxn = 300 + 10;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (t == 0) {
                                                                                                                                                                                                                                                                                      vector<int> G[maxn];
                                                                           u = fa[u];
                                                                                                                                                                                                                                                                                                                                           void init(int n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ининининини
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1111111111
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bool dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return false;
                                                                                                                                                                                                                                                  struct MaxMatch {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // max weight: KM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int go() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int n, m;
                                                                                                                                                                                                                                                                     int n;
                                                                                                                                                                                                             4.7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          , WW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ans += query(*(x.rt), x.dep, l, r);
if (x.rt2) ans -= query(*(x.rt2), x.dep, l, r);
                                                                                                                                                                                                                                                                                 int u; LL a, b; scanf("%d%lld%lld", &u, &a, &b);
a = (a + ans) % A; b = (b + ans) % A;
int l = min(a, b), r = max(a, b);
ans = 0;
for (R& x: tr[u]) {
G[u].push_back({v, d}); G[v].push_back({u, d});
                                                                                                                if (x.rt2) x.rt2->push_back({w[i], x.dep});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
void dfs(int u, int tp) {
    top[u] = tp; idx[u] = ++clk; ridx[clk] = u;
    if (sof[u] != -1) dfs(son[u], tp);
    for (int& v: 6[u])
    if (v != fa[u] && v != son[u]) dfs(v, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Heavy-light Decomposition
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // choose one
// f(idx[v], idx[u]);
// if (u != v) f(idx[v] + 1, idx[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // usage: hld::predf$(1, 1); hld::df$(1, 1); int fa[N], dep[N], idx[N], out[N], ridx[N]; namespace hld {
                                                    FOR (i, 1, n + 1)

for (R& x: tr[i]) {
    x.rt->push_back({W[i], x.dep});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (dep[u] - dep[top[u]] < d) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     u = top[u];
} else return ridx[idx[u] - d];
                                                                                                                                                                                      sort(it->begin(), it->end(), cmp);
FOR (i, 1, it->size())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     d -= dep[u] - dep[top[u]];
                                                                                                                                                                                                         FOR (i, 1, it->size())
(*it)[i].s += (*it)[i - 1].s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               }
if (dep[u] < dep[v]) swap(u, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int sz[N], son[N], top[N], clk;
                                                                                                                                                     (it, pool, pit) {
  it->push_back({-INF, 0});
                                                                                                                                                                                                                                                                                                                                                                                                                                      printf("%lld\n", ans);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        }
int up(int u, int d) {
  while (d) {
    ... / danful = de
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            u = fa[u]; --d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                }
template<typename T>
                                                                                                                                                                                                                                              } while (Q--) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // clear clk
                                      dfs(1);
                                                                                                                                                     FOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    4.6
```

```
Block-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              low[u] = dfn[u] = ++clk;
for (int i = hd[u]; ~i; i = e[i].nxt) {
   if ((feid ^ i) == 1) continue;
   if (ivise[i]) { st[p++] = i; vise[i] = vise[i ^ 1] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  static int st[N], p;
static auto add = [&](int x) {
  if (bno[x] != B) { bno[x] = B; bc[B].push_back(x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int eid = st[--p];
add(e[eid] to); add(e[eid ^ 1].to);
be[B].push_back(eid);
if ((eid ^ i) <= 1) break;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                            Components,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // Single edge also counts as bi-connected comp
// Use |V| <= |E| to filter
struct E { int to, nxt; } e[N];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bc[B].clear(); be[B].clear();
pre[w] = v; pre[v] = u;
q.push_back(w);
} else if (mk[find(v)] == 1) {
int p = get_lca(u, v);
access(u, p, {u, v}, q);
access(v, p, {v, u}, q);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               } else low[u] = min(low[u], dfn[v]);
                                                                                                                                                                                                                                int match() {
    fil(mt + 1, mt + n + 1, 0);
    lca_clk = 0;
    int ans = 0;
    FOR (i, 1, n + 1)
    if (int[i]) ans += aug(i);
    return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int low[N], dfn[N], clk, B, bno[N];
vector<int> bc[N], be[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         memset(vise, 0, sizeof vise);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   memset(bno, -1, sizeof bno);
B = clk = ecnt = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              memset(hd, -1, sizeof hd);
memset(dfn, 0, sizeof dfn);
                                                                                                                                                                                                                                                                                                                                                                                                                                            Bi-connected
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void tarjan(int u, int feid) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // Array size should be 2 * N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int hd[N], ecnt;
void addedge(int u, int v) {
  e[ent] = {v, hd[u]};
  hd[u] = ecnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while (1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 block-cut tree
cactus -> block-cut tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   cut Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ;
+
+ B;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    true;
                                                                                                                                                                  }
return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // N >= |E| \times 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bool vise[N];
void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                            4.13
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int find(int x) { return x == fa[x] ? x : fa[x] = find(fa[x]); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \label{eq:controller} \begin{split} \text{Lea_clk++}; \\ \textbf{for } (u = find(u), \ v = find(v); \ ; \ u = find(pre[u]), \ v = find(v) \end{split}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void access(int u, int p, const pair<int, int>& c, vector<int>&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          (u = find(u); u != p; u = find(pre[u])) {
if (mk[u] == 2) {
    ce[u] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (u && lca_mk[u] == lca_clk) return u;
lca_mk[u] = lca_clk;
if (v && lca_mk[v] == lca_clk) return v;
lca_mk[v] = lca_clk;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int v1 = ce[u].first, v2 = ce[u].second;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int t = 0; t < (int) q.size(); ++t) {
   // q size can be changed</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             } else if (!mk[v]) {
   int w = mt[v];
   mk[v] = 2; mk[w] = 1;
                                                                                                                                              orders.push_back(v);
                                                                                                                                                                                                                                                                                              General Matching
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int u = q[t];
for (int &v: G[u]) {
   if (find(v) == find(u))
   if (imk[v] && imt[v]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 flip(s, pre[mt[u]]);
connect(pre[mt[u]], mt[u]);
                                                       int u = q.front(); q.pop();
for (int v: G[u])
                                                                                                                                                                                                                                                                                                                                                                      int fa[N], mt[N], pre[N], mk[N];
int lca_clk, lca_mk[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bool aug(int s) {
  fill(mk, mk + n + 1, 0);
  fill(pre, pre + n + 1, 0);
  iotaffa, fa + n + 1, 0);
  vector<int> q = {$};
  orders.push_back(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        flip(s, u);
connect(u, v);
return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fa[find(u)] = find(p);
                                                                                                    if (!--deg[v]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                      void connect(int u, int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int get_lca(int u, int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       q.push_back(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void flip(int s, int u) {
   if (s == u) return;
   if (mk[u] == 2) {
                                                                                                                           q.push(v);
                                           while (!q.empty()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         flip(s, v2);
connect(v1, v2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       flip(mt[u], v1);
                                                                                                                                                                                                                                                                                                                                                                                                                   pair<int, int> ce[N]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 pre[v])) {
                                                                                                                                                                                                         return orders;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           mk[s] = 1;
                                                                                                                                                                                                                                                                                                                                                       vector<int> G[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int t = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                        mt[u] = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               mt[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               +
6
                                                                                                                                                                                                                                                                                                                                     // O(n^3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for
                                                                                                                                                                                                                                                                                            4.12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (int i = 0; i < n; i += 2) {
  if (cmp[i] > cmp[i + 1]) printf("%d\n", i + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (int i = (int) vs.size() - 1; i >= 0; --i)
if (!used[vs[i]]) rdfs(vs[i], k++);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int i = 0; i < m; ++i) {
   int a, b; cin >> a >> b;
   add_edge(a - 1, (b - 1) ^ 1);
   add_edge(b - 1, (a - 1) ^ 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (int i = 0; i < n; i += 2) {
  if (cmp[i] == cmp[i + 1]) {
    puts("NIE");
    return 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else printf("%d\n", i + 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int scc() {
   memset(used, 0, sizeof(used));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            memset(used, 0, sizeof(used));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Topological Sort
                                                                                                                                                                                                                                                                                   void add_edge(int from, int to) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (int v = 0; v < n; ++v)
if (!used[v]) dfs(v);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           queue<int> q;
for (int i = 0; i < n; i++)
if (!deg[i]) {</pre>
                                                           else path.push_back(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vector<int> toporder(int n) {
                                                                                                                                                                                                                        vector<int> G[N], rG[N], vs;
int used[N], cmp[N];
                                                                                                                                                                                                                                                                                                          G[from].push_back(to);
rG[to].push_back(from);
                                                                                                                                                                SCC, 2-SAT
    u = S[--top];
if (!G[u].empty())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void rdfs(int v, int k) {
  used[v] = true;
                                                                                                                                                                                                                                                                                                                                                                                void dfs(int v) {
  used[v] = true;
  for (int u: G[v]) {
   if (!used[u])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          vector<int> orders;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rdfs(u, k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (int u: rG[v])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          q.push(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (!used[u])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          vs.push_back(v);
                                           DFS(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  dfs(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       cin >> n >> m;
n *= 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          cmp[v] = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int k = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               scc();
                                                                                                                                                                                                       int n, m;
                                                                                                                                                                  4.10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                4.11
```

```
//out but
dfs(rt);
FORD (1, clk, 1) {
   int x = ridx[i], mn = clk + 1;
   for (int& u: rcf(x)) {
      if (int& u: rcf(x)) {
      if (int\( u \) continue; // reaching all might
      not be possible
   fix(u); mn = min(mn, idx[semi[best[u]]]);
}
                                                                                                                      Lit cycle4() {
   Lit cycle4() {
    Lit cycle4() {
    Lit cycle4() kth + n + 1, 0);
    sort(kth, kth + n , [8](int x, int y) { return deg[x] < deg[y | 1; b];
    FOR (i, 1, n + 1) rk[kth[i]] = i;
    FOR (u, 1, n + 1)
    for (int v: G[u])
    for (int v: G[u])
</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int cycle3() {
   int ans = 0;
   for (E &e: edges) { deg[e.u]++; deg[e.v]++; }
   for (E &e: edges) {
      if (deg[e.u] < deg[e.v] || (deg[e.u] == deg[e.v] && e.u</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void dfs(int u) {
   idx[u] = ++clk; ridx[clk] = u;
   for (int& v: G[u]) if (!idx[v]) { fa[v] = u; dfs(v); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (c[x] == -1) return x;
int &f = c[x], rt = fix(f);
if (idx[semi[best[x]]] > idx[semi[best[f]]]) best[x]
                                                                                                                                                                                                                                                                                            if (rk[v] > rk[u]) key[u].push_back(v);
FOR (u, 1, n + 1) {
   for (int v: G[u])
                                                                                                                                                                                                                                                                                                                                                              for (int w: key[v])
if (rk[w] > rk[u]) ans += cnt[w]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fill(c, c + n + 1, -1);
FOR (i, 1, n + 1) dt[i].clear();
FOR (i, 1, n + 1) semi[i] = best[i] = i;
fill(idx, idx + n + 1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                         for (int w: key[v])
  if (rk[w] > rk[u]) --cnt[w];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int fa[N], idx[N], clk, ridx[N];
int c[N], best[N], semi[N], idom[N];
void init(int n) {
                                                                                                      // refer to cheatsheet for elaboration
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else G[e.v].push_back(e.u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              G[e.u].push_back(e.v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Dominator Tree
                                                                                                                                                                                                                                                                                                                                                                                                       for (int v: G[u])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<int> G[N], rG[N];
vector<int> dt[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return f = rt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                best[f];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void go(int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             < e.v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int fix(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       clk = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    }
return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        namespace tl{
                                                             4.16
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 4.17
                                                                                                                                                                                                                                                                                                                                                                                                                                                              int Fa(int x) { return fa[x] == x? x: (fa[x] = Fa(fa[x])); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(Fa(it->second) == Fa(u)) it = G[u].erase(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(auto pr: G[y]) {
   G[x].emplace(pr.first+shift[y]-shift
                                                                                                                                                                                                                                                       2
                 v = e.v;
e.u = id[e.u]; e.v = id[e.v];
if (e.u != e.v) { e.w == in[v]; i++; }
else { swap(e, edges.back()); edges.pop_back(); }
                                                                                                                                                                                                                                                     Minimum Directed Spanning Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(it == G[u].end()) return { false, -1LL };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                LL lb = it->first; int v = Fa(it->second); G[u].erase(it);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(G[x].size() <G[y].size()) {
  G[x].swap(G[y]);
  swap(shift[x], shift[y]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ans += lb + shift[u];
shift[u] = -lb;
if(vis[v] && Fa(v) != Fa(root)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               [x], pr.second);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int u = i; top = 0;
white(Fa(u) i = Fa(root)) {
    vis[u] = true; stk(top++] = u;
    auto it = G[u].begin();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FOR(i, 1, n+1) if(Fa(i) != Fa(root)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int x = v;
while(stk[top-1] != v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int y = stk[--top];
fa[Fa(y)] = Fa(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while(it != G[u].end()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while(top--) {
  fa[Fa(stk[top])] = root;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void add_edge(int u, int v, int w)
  G[v].emplace(w, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }
G[y].clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            pair<bool, LL> solve(int root)
LL ans = 0;
FOR(i, 1, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fill(vis, vis+n+1, false);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return { false, -1 };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     n = _n;
iota(fa, fa+n+1, 0);
fill(shift, shift+n+1,
fill(shift, shift+n+1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      it);
else break;
auto &e = edges[i];
                                                                                                                                                                                                                                                                                                                                                     int fa[N], stk[N], top, n;
LL shift[N];
bool vis[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return { true, ans };
                                                                                                                                                                                                                                                                                            namespace MDST {
   typedef pair<LL, int> P;
                                                                                                                        n = tn; rt = id[rt];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void init(int _n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ;
= ^;
                                                                                                                                                                                                                                                                                                                                                                                                                      set<P> G[N];
                                                                                                                                                               return ans;
                                                                                                                                                                                                                                                                    }
int idx[N], clk, fa[N];
bool ring[N];
void init() { ecnt = 0; memset(hd, -1, sizeof hd); clk = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        };
if (v != rt && id[v] == -1) {
    for (int u = pre[v]; u != v; u = pre[u]) id[u]
    tn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    G[nn].push_back(v); G[v].push_back(nn); // put
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             FOR (i, 0, n) if (i != rt && in[i] == INF) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Minimum Directed Spanning Tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       G[nn].push_back(x); G[x].push_back(nn);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while (vis[v] != i && id[v] == -1 && v != rt)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   the root of the cycle in the front
for (int x = u; x != v; x = fa[x]) {
    ring[x] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dfs(v, i);
if (!ring[u]) { G[u].push_back(v); G[v].
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FOR (i, 0, n) if (id[i] == -1) id[i] = tn++;
for (int i = 0; i < (int) edges.size(); ) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             fill(id, id + _n, -1); fill(vis, vis + _n,
                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = hd[u]; ~i; i = e[i].nxt) {
  if ((i ^ feid) == 1) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             fill(in, in + n, INF);
for (E &e: edges) {
   if (e.u != e.v && e.w < in[e.v]) {
       pre[e.v] = e.u;
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fa[v] = u; ring[u] = false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             } else if (idx[v] < idx[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      vis[v] = i; v = pre[v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           push_back(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int in[N], id[N], pre[N], vis[N];
// a copy of n is needed
LL zl_tree(int rt, int n) {
    LL ans = 0;
                                                                                                                                                      E e[N * 2];
int hd[N], ecnt;
void addedge(int u, int v) {
    e[ecnt] = {v, hd[u]};
                                                                                                                                                                                                                                                                                                                                                                             void dfs(int u, int feid) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ring[v] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FOR (i, 0, n) {
ans += in[v = i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                            int v = e[i].to;
if (!idx[v]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    in[e.v] = e.w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
if (tn == 0) break;
                                                                                                                   struct E { int to, nxt; };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // edges will be modified
vector<E> edges;
hd[u] = ecnt++;
                                                                                                                                                                                                                                                                                                                                                                                                   idx[u] = ++clk;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int tn = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 in[rt] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int v, _n = n;
while (1) {
                                                        vector<int> G[N];
                                                                                                                                       namespace C
                                                                            int nn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        4.14
```

```
FOR (i, 2, clk + 1) {
    int u = ridx[i];
    if (idom[u] != semi[u]) idom[u] = idom[idom[u]];
                                                                                                           = best[u];
c[x] = fa[x];
dt[seni[x] = ridx[mn]].push_back(x);
x = ridx[i - 1];
for (int& u: dt[x]) {
                                                                                                           (semi[best[u]] != x) idom[u]
                                                                                                                                                                                                                                                                                                      dt[idom[u]].push_back(u);
                                                                                                                                   else idom[u]
                                                                                                                                                                              dt[x].clear();
                                                                                         fix(u);
```

Global Minimum Cut 4.18

```
| Mist[i] = g[i][i];
| FOR (i, 1, n) {
| x = t; t = 0;
| FOR (j, 1, n + 1) |
| if (vis[j] != clk && (it || dist[j] > dist[t]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            memset(vis, 0, sizeof vis);
for (int i = 1, x, y; n > 1; ++i, --n) {
    ret = min(ret, min_cut_phase(i, x, y));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (j, 1, n + 1) if (vis[j] != clk)
dist[j] += g[t][j];
                                                                                                                                                                                                                                                   min_cut_phase(int clk, int &x, int &y)
                                                                                                                                                                                                                                                                                           vis[t = 1] = clk;
FOR (i, 1, n + 1) if (vis[i] != clk)
                                                                                                                                             FOR (i, 1, n + 1) FOR (j, 1, n + 1)
                                                                                                                                                                 g[i][j] = w[i][j];
memset(dist, 0, sizeof(dist));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (x > y) swap(x, y);
FOR (i, 1, n + 1)
   if (i | x && i = y) {
    g[i][x] += g[i][y];
   g[x][i] += g[i][y];
                                                                                                       void init(int nn, LL w[N][N]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (y == n) return;
FOR (i, 1, n) if (i != y) {
    swap(g[i][y], g[i][n]);
    swap(g[y][i], g[n][i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void merge(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                            vis[t] = clk;
FOR (j, 1, n +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return dist[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          LL ret = INF;
struct StoerWanger {
  LL n, vis[N];
  LL dist[N];
  LL g[N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      go () {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Η
                                                                                                                                                                                                                                                     Η
```

Geometry

2D Basics

```
== 0 && sgn(a.y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           P operator * (const P& a, LD k) { return P(a.x * k, a.y * k); } P operator / (const P& a, LD k) { return P(a.x / k, a.y / k); } inline bool operator < (const P& a, const P& b) { return sgn(a.x - b.x) < 0 || (sgn(a.x - b.x) = 0 && sgn(a.y - b.x) = 0 & const P& b) |
                                                                                                                                                                                                                                                                                                                                                                                                               P operator + (const P& a, const P& b) { return P(a.x + b.x, a.y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (const P& a, const P& b) { return P(a.x - b.x, a.y
int \operatorname{sgn}(\operatorname{LD} \times) { return fabs(x) < eps ? 0 : (x > 0 ? 1 : -1); } struct L;
                                                                                                                                                        \Leftrightarrow
                                                                                                                                LD \times, y; explicit P(LD \times = 0, LD y = 0): \times(\times), y(y) explicit P(const L& l);
                                                                                                                                                                                                                                                                                                                               \Rightarrow
                                                                                                                                                                                                                                                                                                 L() {}
L(P s, P t): s(s), t(t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  b.y) < 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                b.y); }
                                                                                                                                                                                                                                                                                                                                                                                                                                             + b.y);
                                                                       typedef P V;
                                                                                                                                                                                                                                     struct L {
P s, t;
                                                                                                  struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        P operator
                                                  struct P
```

dist(const P& p) { return sqrt(p.x * p.x + p.y * p.y); } dot(const V& a, const V& b) { return $a.x * b.x + a.y * b.y; }$ det(const V& a, const V& b) { return $a.x * b.x + a.y * b.y; }$ cross(const P& s, const P& t, const P& o = P()) { return det(s - 0, t - 0); } istream &operator >> (istream &is, P &p) return (is >> p.x >> p.y); 9999

Polar angle sort 5.2

```
. operator () (const P& a, const P& b) {
  int qa = quad(a - p), qb = quad(b - p);
  if (qa != qb) return qa < qb; // compore e</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                           <u>..</u>
                     int x = sgn(p.x), y = sgn(p.y);
if (x > 0 && y >= 0) return 1;
if (x <= 0 && y >= 0) return 2;
if (x < 0 && y <= 0) return 3;
if (x > 0 && y <= 0) return 4;</pre>
                                                                                                                                                                                                                                                                                                                                                                  int d = sgn(cross(a, b, p));
if (d) return d > 0;
return dist(a - p) < dist(b -</pre>
                                                                                                                                                                                                                                      struct cmp_angle {
int quad(P p) {
                                                                                                                                                             assert(0);
                                                                                                                                                                                                                                                                                      bool
```

Segments, lines

merge(x, y);

return ret;

} sw;

```
bool l_eq(const L& a, const L& b) {
    return parallel(a, b) && parallel(L(a.s, b.t), L(b.s, a.t));
                                                      bool parallel(const L& a, const L& b)
    return !sgn(det(P(a), P(b)));
5.3
```

```
int s_cross(const L& a, const L& b, P& p) { int d1 = sgn(cross(a.t, b.s, a.s)), d2 = sgn(cross(a.t, b.t,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int d3 = sgn(cross(b.t, a.s, b.s)), d4 = sgn(cross(b.t, a.t,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          { p = l_intersection
                              cos(r) - p.
                                                                                                                                                                                                                                                                     ||
|
                                                                                                                                                                                                                                                                 ( q -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // make sure they have unconstant L& b) {
Plintersection(const L& a, const L& b) {
   LD s1 = det(P(a), b.s - a.s.), s2 = det(P(a), b.t - return (b.s * s2 - b.t * s1) / (s2 - s1);
}
                                                                                                                                                                      // inclusive: <=0; exclusive: <0
bool p_on_seg(const P& p, const L& seg) {
    P a = seg.s, b = seg.t;
    return !sgn(det(p - a, b - a)) && sgn(dot(p - a, p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ( p = b.s; return 2; )
( p = b.t; return 2; )
( p = a.s; return 2; )
( p = a.s; return 2; )
( p = a.t; return 2; )
                        protation(const P& p, const LD& r) { return P(p.x * cc
    y * sin(r), p.x * sin(r) + p.y * cos(r)); }
PROTATECCW90(const P& p) { return P(-p.y, p.x); }
PROTATECW90(const P& p) { return P(p.y, -p.x); }
// inclusive: <=0; exclusive: <0</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      }
LD angle(const V& a, const V& b) {
   LD r = asin(fabs(det(a, b)) / dist(a) / dist(b));
   if (sgn(dot(a, b)) < 0) r = PI - r;
   return r;
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                        ir (L.S == l.t) return dist(p - l);
v vs = p - l.s, vt = p - l.t;
if (sgn(dot(l, vs)) < 0) return dist(vs);
else if (sgn(dot(l, vt)) > 0) return dist(vt);
else return dist_to_line(p, l);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               s_l_cross(const L& seg, const L& line) {
int d1 = sgn(cross(line.s, line.t, seg.s));
int d2 = sgn(cross(line.s, line.t, seg.t));
if ((d1 ^ d2) == -2) return 1; // proper
if (d1 == 0 || d2 == 0) return 2;
return 0;
                                                                                                                                                                                                                                                                                                                     }
LD dist_to_line(const P& p, const L& l) {
    return fabs(cross(l.s, l.t, p)) / dist(l);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if ((d_1 \wedge d_2) == -2 \&\& (d_3 \wedge d_4) == -2)
                                                                                                                                                                                                                                                                                                                                                                                                                                        LD dist_to_seg(const P& p, const L& l) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (id1 && p_on_seg(b.s, a)) {
  if (id2 && p_on_seg(b.t, a)) {
   if (id3 && p_on_seg(a.s, b)) {
      if (id4 && p_on_seg(a.s, b)) {
      return 0;
r radius
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (a, b); return 1; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1: proper; 2: improper
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1: proper; 2: improper
   counter-clockwise
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     a.s));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               b.s))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int s_
```

Polygons 5.4

typedef vector<P> S;

panb

```
FOR (i, 0, S.size()) {
    P a = s[i], b = s[nxt(i)];
    if (p_oo_seg(p, L(a, b))) return -1;
    if (sgn(a.y - b.y) <= 0) swap(a, b);
    if (sgn(p.y - a.y) > 0) continue;
    if (sgn(p.y - b.y) <= 0) continue;
  on border
                                                                                                                                                                                                                                    cnt += sgn(cross(b, a, p)) > 0;
                       int inside(const S& s, const P& p) {
// 0 = outside, 1 = inside, -1 =
                                                                                                                                                                                                                                                                                                                                 LD polygon_area(const S& s)
LD ret = 0;
                                                                                                                                                                                                                                                                                      return bool(cnt & 1);
                                                    int cnt = 0;
```

```
auto cr = p_on_seg(p[0], L(a, b)) ? p[0] : p[1];
if (ina) return sector_area(b, cr, r) + fabs(cross(a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LD c_poly_area(S poly, const C& c) {
    LD ret = 0; int n = poly.size();
    FOR (1, 0, n) {
    int t = sgn(cross(poly[i] - c.p, poly[(i + 1) % n] - c.p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   , cr)) / 2;
else return sector_area(a, cr, r) + fabs(cross(b, cr
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (t) ret += t * c_tri_area(poly[i], poly[(i + 1) % n],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool operator < (const CV& a, const CV& b) { return a.ym < b.ym;
                                                                                                                                                                                                                                                                                                                                                                                     a = a - center; b = b - center;
int ina = sgn(dist(a) - r) < 0, inb = sgn(dist(b) - r) < 0;
// dbg(a, b, ina, inb);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             } else {
   if ((int) p.size() == 2 && p_on_seg(p[0], L(a, b)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return {CV(yl1, yr1, ym1, c, 1), CV(yl2, yr2, ym2, c, -1)};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (dist(p[0] - a) > dist(p[1] - a)) swap(p[0],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return sector_area(a, p[0], r) + sector_area(p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              auto p = c_l_intersection(L(a, b), C(0, 0, r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     pair<CV, CV> pairwise_curves(const C& c, LD xl, LD xr)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              pair<LD, LD> c_point_eval(const C& c, LD x) {
   LD d = fabs(c.p.x - x), h = rt(sq(c.r) - sq(d));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          LD yll, yl2, yr1, yr2, ym1, ym2;
tie(yll, yl2) = c_point_eval(c, xl);
tie(ym1, ym2) = c_point_eval(c, (xl + xr) / 2);
tie(yr1, yr2) = c_point_eval(c, xr);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              + fabs(cross(p[0], p[1])) / 2;
} else return sector_area(a, b, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CV(LD yl, LD yr, LD ym, C c, int t)
: yl(yl), yr(yr), ym(ym), type(t), o(c) {}
                                                                                                                         }
LD c_tri_area(P a, P b, P center, LD r) {
    .--- h - center;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   LD cv_area(const CV& v, LD xl, LD xr) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return fabs(cross(a, b)) / 2;
  - l) > 0) return 3;
- l) == 0) return 2;
- l) < 0) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return {c.p.y - h, c.p.y + h};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               LD yl, yr, ym; C o; int type; CV() {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           [1], b, r)
                                                                                                                                                                                                                                                                                                                                                                                                                                         ina, inb);
nb) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Circle Union
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             )) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         c.p, c.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (ina ^ inb) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // version 1
// union O(n^3 log n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        typedef vector<P> S;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (ina && inb)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      }
return ret;
if (sgn(d -
if (sgn(d -
if (sgn(d -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         struct CV {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     5.7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   p b(l), a = l.s - c.p;
LD x = dot(b, b), y = dot(a, b), z = dot(a, a) - c.r * c.r;
LD = y x y - x * z;
LD = y x y - x * z;
ref. push_back(c.p + a + b * (-y + sqrt(D + eps)) / x);
if (sgn(D) > 0) ret.push_back(c.p + a + b * (-y - sqrt(D)) / x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ret.push_back(a.p + v × x + RotateCCW90(v) × y); if (sgn(y) > 0) ret.push_back(a.p + v × x - RotateCCW90(v) ×
                                                                                                                                                                                                                                                                                                                     q[la
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   convex_intersection(const vector<P> &v1, const vector<P> &v2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                b = (a + b) / 2;
c = (a + c) / 2;
return L_intersection({b, b + RotateCW90(a - b)}, {c , c
RotateCW90(a - c)});
  int n = L.size(), fi, la;
sort(L.begin(), Lend());
sort(L.begin(), Lend());
q[fi = la = 0] = L[0];
FOR (i, 1, n) {
    while (fi < la && ion_left(L[i], p[la - 1])) la--;
    while (fi < la && ion_left(L[i], p[fi])) fi++;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vector<LV> h; int n = v1.size(), m = v2.size();
FOR (' 0, n) h.push_back(LV(v1fi], v1[(i + 1) % n]));
FOR (' 0, m) h.push_back(LV(v2fi], v2[(i + 1) % m]));
return half_plane_intersection(h);
                                                                                                                                                                                                                                                                                                                if (fi < la) p[la - 1] = l_intersection(q[la - 1],</pre>
                                                                                                                                                                                                                                                                                                                                                                                          while (fi < la && ion_left(q[fi], p[la - 1])) la--;
if (la - fi <= 1) return vector<pre>vectorp(;)
if (la - Lintersection(q[la], q[fi]);
return vectorp(p.begin() + fi, p.begin() + la + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         struct C {
    pp; LD r;
    pp; LD r;
    c(LD x = 0, LD y = 0, LD r = 0): p(x, y), r(r) {}
    c(P p, LD r): p(p), r(r) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      LD x = (d * d - b.r * b.r + a.r * a.r) / (2 * d);

LD y = sqrt(a.r * a.r - x * x);

P v = (b.p - a.p) / d;
                                                                                                                                                                                                                                                             if (on_left(q[la], L[i].p)) q[la] = L[i];
                                                                                                                                                                                 q[++la] = L[i];
if (sgn(cross(q[la].v, q[la - 1].v)) == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vector<P> c_l_intersection(const L& l, const C& c) {
   vector<P> ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // intersections are clockwise subject to center
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    LD d = dist(a.p - v.p);

if (sgn(d - a.r - v.r) > 0) return 5;

if (sgn(d - a.r - v.r) == 0) return 4;

LD l = fabs(a.r - v.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int c_c_relation(const C& a, const C& v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       intersect, 4: ext tangent 5: outside
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     compute_circle_center(P a, P b, P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 1: inside, 2: internally tangent
// 3: intersect, 4: ext tangent 5: c
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Circles
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       5.6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              }
int si = 0;
int si = i, sj = j;
while (i = sj || j = si) {
    res = max(res, dist(qs[i] - qs[j]));
if (sgn(cross(qs[(i+1)%n] - qs[i], qs[(j+1)%n] - qs[j]))
    ...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            left(const LV& l, const P& p) { return sgn(cross(l.v, p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (unsigned i = 0; i < p.size(); i++) {
    unsigned j = (i + 1) % p.size();
    c = c + (fi] + p[j]) * (p[i].x * p[j].y - p[j].x * p[i].y);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       FORD (i, (LL)s.size() - 2, -1) {
   while (sz > k && sgn(cross(ret[sz - 1], s[i], ret[sz -
   2])) < 0) --sz;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             bool operator < (const LV &a, const LV& b) { return a.ang < b.
                                                                                                                                                                                                                                                                                int sz = 0;
FOR (i, 0, s.size()) {
while (sz > 1 && sgn(cross(ret[sz - 1], s[i], ret[sz - 2])) < 0) --sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P l_intersection(const LV& a, const LV& b) {
    P u = a.p - b.p; LD t = cross(b.v, u) / cross(a.v, b.v);
    return a.p + a.v * t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             LV(P s, P t): p(s), v(t - s) { ang = atan2(v.y, v.x); }
     FOR (i, 1, (LL)s.size() - 1)
    ret += cross(s[i], s[i + 1], s[0]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Half-plane intersection
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   S half_plane_intersection(vector<LV>& L) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // centroia
P ComputeCentroid(const vector<P> &p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // Rotating Calipers, find convex hull
LD rotatingCalipers(vector<P>& qs) {
   int n = qs.size();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       LD scale = 6.0 * polygon_area(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int i = 0, j = 0;
FOR (k, 0, n) {
  if (!(qs[i] < qs[k])) i = k;
  if (qs[j] < qs[k]) j = k;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ret.resize(sz - (s.size() > 1));
return ret;
                                                                                                    // duplicate points are not allowed
// s is subject to change
const int MAX_N = 1000;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return dist(qs[0] - qs[1]);
                                                                                                                                                                                                                                      sort(s.begin(), s.end());
S ret(MAX_N * 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             3; // åkęäÿÄçğnåŘŚéĞkèqĺçďž
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ret[sz++] = s[i];
                                                                                                                                                                                                                 assert(s.size() >=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return c / scale;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   P p, v; LD ang;
LV() {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       - l.p)) >= 0; }
                                                       return ret / 2;
                                                                                                                                                                                      convex_hull(S& s)
                                                                                                                                                                                                                                                                                                                                                                                                                                            int k = sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (n == 2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  P c(0, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                centroid
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        struct LV
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool on_
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      5.5
```

```
return sgn(a.x - b.x) < 0 \mid | (sgn(a.x - b.x) == 0 \&\& (sgn(a.y - b.y) < 0 \mid |
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      LD mix(const V& a, const V& b, const V& c) { return dot(a, cross
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return P(p.x * cos(r) - p.y * sin(r), p.x * sin(r) + p.y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (sgn(a.y - b.y) == 0 \&\& sgn(a.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   } bool operator == (const P& a, const P& b) { return |sgn(a.x-b.a.max)|
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 << p.z << ")")</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              LD dist2(const P& p) { return p.x * p.x + p.y * p.y + p.z * p.z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            LD dist(const P& p) { return sqrt(dist2(p)); } LD dot(const V& a, const V& b) { return a.x * b.x + a.y * b.y + LD dot(const V& a, const V& b) { return a.x * b.x + a.y * b.y + b.y 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return P(p.x, p.y * cos(r) - p.z * sin(r), p.y * sin(r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               p.x * sin(r), p.y, p.z * sin(r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return P(v.y * w.z - v.z * w.y, v.z * w.x - v.x * w.z, v.x
                                                                                                                                                                                                                                                                                                                                                                                                                                      LD x, y, z; explicit P(LD x = 0, LD y = 0, LD z = 0): x(x), y(y), z(z)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rotation(const P& p, const LD& r, const P& n) { LD c = cos(r), s = sin(r), x = n.x, y = n.y, z = n.z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    z - b.z < 0)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rotation(const P& p, const LD& r, int axis = 0) {
  if (axis == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          x) && isgn(a.y - b.y) && isgn(a.z - b.z); } 
P::p(const L& 1) { *this = \ldot - \ldot - \ldot s; } 
ostream &operator << (ostream &os, const P &p) { return (os << "(" << p.x << "," << p.y << "," << p.y << ","
LD b = 1 / (d + c.r.); c.r = (a - b) / 2 * R2; c.c = -0 + (c.p - 0) * ((a + b) * R2 / 2 / d); return c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 P operator + (const P& a, const P& b) { }
P operator - (const P& a, const P& b) { }
P operator + (const P& a, LD K) { }
P operator / (const P& a, LD K) { }
inline int operator < (const P& a, const P& b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    F() {}
F(P a, P b, P c): a(a), b(b), c(c) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return (is >> p.x >> p.y >> p.z);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   P cross(const P& v, const P& w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            (b, c)); } // counter-clockwise r radius // axis = 0 armond
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             + p.z * cos(r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return P(p.z * cos(r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             + p.x * cos(r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              * cos(r), p.z);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        w.y - v.y * w.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     L(P s, P t): s(s), t(t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       explicit P(const L& l);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // axis = 1 around axis y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // axis = 2 around axis z
P rotation(rone+ n° -
                                                                                                                                                                                                                                                    3D Basics
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else if (axis == 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else if (axis == 2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      n is normal vector
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // this is clockwise Protation(const P& 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       a.z \times b.z; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Pa, b, c;
                                                                                                                                                                                                                                                                                                                                                    struct L;
typedef P V;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      $
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct F {
                                                                                                                                                                                                                                                                                                                 struct P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \Box
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int c = ev[0].t;
FOR(j, 1, ev.size()) {
   int t = cc + belong_to;
   ans[t] + cr crss(ev[j - 1].p + c.p, ev[j].p + c.p) / 2;
   ans[t] + cr_area(c.r, ev[j - 1], ev[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       r = dist(a[j] - c);
FOR (k, 0, j) if (!p_in_circle(a[k], {c, r})) {
c = compute_circle_center(a[i], a[j]), a[k]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                P compute_circle_center(P a, P b) { return (a + b) / 2; } bool p_in_circle(const P& p, const C& c) { return sgn(dist(p - c.p) - c.r) <= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   : (c_c_relation(c, cs[j]) <= 2) {
if (sgn(cs[j].r - c.r) >= 0) // totally covered
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Minimum Covering Circle
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   f (its.size) == 2) {
    P p = its[1] - c.p, q = its[0] - c.p;
    LD a = angle(p), b = angle(q);
if (sgn(a - b) > 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                auto its = c_c_intersection(c, cs[j]);
if (its.size/) -- ^^ (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ev.emplace_back(p, a, 1);
ev.emplace_back(bound, PI, -1);
ev.emplace_back(bound, -PI, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      C min_circle_cover(const vector<P> &in) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vector<P> a(in.begin(), in.end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ev.emplace_back(q, b, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ev.emplace_back(p, a, 1);
ev.emplace_back(q, b, -1);
                                                                                                                                                                                                                                                              ev.emplace_back(bound, -PI, 0);
ev.emplace_back(bound, PI, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              r = dist(a[k] - c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Circle Inversion
                                                                                                                                                                                                                                      P bound = c.p + P(-c.r, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    sort(ev.begin(), ev.end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            C inv(C c, const P& o) {
   LD d = dist(c.p - o);
   assert(sgn(d) != 0);
   LD a = 1 / (d - c.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               belong_to++;
                                                                                                                                                                                                int belong_to = 0;
                                                                                                                                      auto &c = cs[i];
vector<CP> ev;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           += ev[j].t;
                                                                                                                                                                                                                                                                                                                               FOR(j, 0, n) {
if (i == j)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        dbg(a.size());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return {c, r};
                                                                                                                                                                                                                                                                                                                                                                                                       continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                } else {
                                                                                                          continue;
                                                                    if (!ok)
                                                                                                                                                                                                                                                                                                                                                                                                                                      <u>+</u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              5.9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ans += (intv[i].yl - intv[i - 1].yl + intv[i].yr - intv[i - 1].yr) * (xr - xl) / 2;
ans += intv[i - 1].type * areas[i - 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        auto t = pairwise_curves(c, xl, xr);
intv.push_back(t.first); intv.push_back(t.second
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vector<LD> areas(intv.size());
FOR (i, 0, intv.size()) areas[i] = cv_area(intv[i], xl,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bool operator<(const CP &u, const CP &v) { return u.a < v.a; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (sgn(c.p.x = c.r = x1) <= 0 && sgn(c.p.x + c.r
    xr) >= 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (sgn(cs[i].r - cs[j].r) == 0 && cs[i].p == cs[j].p) {
    ok = false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    LD cv_area(LD r, const CP &q1, const CP &q2) {
    return (r * r * (q2.a - q1.a) - cross(q1.p, q2.p)) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inline LD angle(const P &p) { return atan2(p.y, p.x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                   auto pts = c_c_intersection(cs[i], cs[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (auto& p: pts) xs.push_back(p.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ans -= intv[i].type * areas[i];
   - v.yl));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             the first one counts
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CP(P p, LD a, int t) : p(p), a(a), t(t) {}
                                                                                                                                                                                                                                                                                             xs.push_back(cs[i].p.x - cs[i].r);
xs.push_back(cs[i].p.x);
xs.push_back(cs[i].p.x + cs[i].r);
LD l = rt(sq(xr - xl) + sq(v.yr - v.

LD d = rt(sq(v.or) - sq(l / 2));

LD ang = atan(l / d / 2);

return ang * sq(v.o.r) - d * l / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         sort(intv.begin(), intv.end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                LD ans[N];

void circle_union(const vector<C> &cs)
int n = cs.size();
                                                                                                                                      FOR (i, 0, (int) xs.size() - 1) {
   LD xl = xs[i], xr = xs[i + 1];
   vector<CV> intv;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // version 2 (k-cover, O(n^{\Lambda}2 \log n))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     intv.size()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        cc += intv[i].type;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             p is coordinates relative to
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FOR (k, 0, n) {
auto& c = cs[k];
                                                                                                                                                                                                                                                                                                                                                                                                 FOR (j, i + 1, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FOR (i, 0, intv.s<sup>-</sup>
if (cc > 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         same circle, only
                                                                                                                                                                                                   int n = cs.size();
vector<LD> xs;
FOR (i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int cc = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // Points on circle
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool ok = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ×r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FOR(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR(j, 0, i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  LD ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                struct CP {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        CP () d)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int t;
```

```
unsigned int mask32 = ~(00);
ULL left1 = h[left] >> 32, right1 = h[right] >> 32;
ULL left2 = h[left] & mask32, right2 = h[right] & mask32
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (((left2 - right2 * xp2[len] % p2 + p2) % p2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return (((left1 - right1 * xp1[len] % p1 + p1) % p1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ULL get_substring_hash(int left, int right) const {
   int len = right - left;
#ifdef ENABLE_DOUBLE_HASH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return h[left] - h[right] * xp[len];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      res1 = (res1 * \times + s[j]) % p1;
res2 = (res2 * \times + s[j]) % p2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         subsize = length - sublen + 1;
for (int i = 0; i < subsize; ++i)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int j = length - 1; j >= 0;
#ifdef ENABLE_DOUBLE_HASH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // get hash of s[left...right-1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     const int p1 = 1e9 + 7, p2 = 1e9 + 9;
ULL xplNJ, xp2[N];
void init_xp() {
    xp1[o] = xp2[o] = xp[o] = 1;
    for (int i = 1; i < N; ++i) {
        xp1[i] = xp1[i - 1] * x % p1;
        xp2[i] = xp2[i - 1] * x % p2;
    xp2[i] = xp2[i - 1] * x;
    xp[i] = xp2[i - 1] * x;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           h[j] = (res1 << 32) | res2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void get_all_subs_hash(int sublen)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // printf("%llu\n", h[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          length = strlen(s);
ULL res1 = 0, res2 = 0;
h[length] = 0; // ATTENTION!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        res1 = res1 * \times + s[j];
                                                                                                                                                                                                                                                   ac.build();
scanf("%s", s);
int u = 0; n = strlen(s);
FOR (i, 0, n) {
    u = ac.ch[u][mp(s[i])];
    if (ac.danger[u]) {
        puts("YES");
    return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // hash of [left, right)
                                               char s[N];
int main() {
  int n; scanf("%d", &n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int length, subsize;
bool sorted;
ULL h[N], h1[N];
ULL hash() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   h[j] = res1;
                                                                                                                                                 while (n-) {
   scanf("%s", s);
   ac.insert(s, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return h[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  32)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Hash
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 puts("NO"); return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        struct String {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   char s[N];
                                                                                                                                 ac.init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             #endif
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   #else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    #endif
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  #else
       } ac;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           6.2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    }
vector<F> out;
FOR (i, 0, face.size())
out.emplace_back(p[face[i].a], p[face[i].c]
out.emplace_back(p[face[i].a], p[face[i].c]
                                                                                               FOR (i, 0, face.size()) {
    int a = face[i].a, b = face[i].b, c = face[i].c;
    if (sgn(mix(p[a] - p[v], p[b] - p[v]), p[c] - p[v]))
                          FOR (i, 0, tmp.size()) {
    int a = face[i].a, b = face[i].b, c = face[i].c
    if (mk[a][b] == v) face.emplace_back(b, a, v);
    if (mk[b][c] == v) face.emplace_back(c, b, v);
    if (mk[c][a] == v) face.emplace_back(a, c, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }
void insert(const string &s, int m) {
   int n = s.size(); int u = 0, c;
   FOR (i, 0, n) {
      c = mp(s[i]);
   if (!ch[u][c]) {
      memset(ch[sz], 0, sizeof ch[sz]);
   danger[sz] = 0; ch[u][c] = sz++;
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Aho-Corasick Automation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ch[r][c] = ch[fail[r]][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (u) { 0.push(u); fail[u] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int r = 0.front(); 0.pop();
danger[r] |= danger[fail[r]];
for (int c = 0, u; c < M; c++)
u = ch[r][c];</pre>
                                                                                                                                                                                                   mk[a][b] = mk[b][a] = v;
mk[b][c] = mk[c][b] = v;
mk[c][a] = mk[a][c] = v;
} else tmp.push_back(face[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             memset(ch[0], 0, sizeof ch[0]);
memset(danger, 0, sizeof danger);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fail[u] = ch[fail[r]][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fal[0] = 0;
for (int c = 0, u; c < M; c++) {
u = ch[0][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              const int N = 1e6 + 100, M = 26;
int mp(char ch) { return ch - 'a'; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int ch[N][M], danger[N], fail[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while (!Q.empty()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        danger[u] |= 1 << m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Q.push(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      u = ch[u][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (!u)
                                                                                                                                                                                   (o
>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     queue<int> 0;
                                                                                                                                                                                                                                                                                                                                        face = tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  }
void build() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int sz;
void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             sz = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct ACA {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 6.1
       found:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     P norm(const F& f) { return cross(f.a - f.b, f.b - f.c); }
int p_on_plane(const F& f, const P& p) { return sgn(dot(norm(f), p - f.a)) == 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // return 0 if points is on the line
// makes no sense if points and line are not coplanar
int opposite_side(const P& u, const P& v, const L& l) {
    return sgn(dot(cross(P(l), u - l.s), cross(P(l), v - l.s )) > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vectorFFT> face;
FOR (1, 2, p.size()) {
   if (p_on_line(p[1], L(p[0], p[1]))) continue;
   swap(p[1], p[2]);
   FOR (j, j + 1, p.size())
   if (sgn(mix(p[1] - p[0], p[2] - p[1], p[j] - p[0])))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool parallel(const L& a, const L& b) { return !sgn(dist2(cross(P(a), P(b))); } int s_intersect(const L& u, const L& v) {
return P((x * x * (1 - c) + c) * p x + (x * y * (1 - c) + z 
 * s) * p y + (x * z * (1 - c) - y * s) * p z, 
 (x * y * (1 - c) - z * s) * p x + (y * y * (1 - c) 
 + c) * p y + (y * z * (1 - c) + x * s) * p z, 
 (x * z * (1 - c) + y * s) * p x + (y * z * (1 - c) 
 - x * s) * p y + (z * z * (1 - c) + c) * p z, 
 - x * s) * p y + (z * z * (1 - c) + c) * p z, z)
                                                                                                                                                                                                                                                                                                                                                                     P a = seg.s, b = seg.t;
return !sgn(dist2(cross(p - a, b - a))) && sgn(dot(p - a,
                                                                                                                                                                                                                                                                                                                                                                                                                                            }
LD dist_to_line(const P& p, const L& l) {
    return dist(cross(l.s - p, l.t - p)) / dist(l);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // if two points are on the opposite side of a line
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   V vs = p - l.s, vt = p - l.t;
if (sgn(dot(l, vs)) < 0) return dist(vs);
if (sgn(dot(l, vt)) > 0) return dist(vt);
else return dist_to_line(p, l);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FT(int a, int b, int c) : a(a), b(b), c(c) { }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               sort(p.begin(), p.end());
p.erase(unique(p.begin(), p.end()),
random_shuffle(p.begin(), p.end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return p_on_plane(F(u.s, u.t, v.s), v.t) &&
    opposite_side(u.s, u.t, v) &&
    opposite_side(v.s, v.t, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool p_on_line(const P& p, const L& l) {
    return !sgn(dist2(cross(p - l.s, P(l))));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               face.emplace_back(0, 1, 2);
face.emplace_back(0, 2, 1);
                                                                                                                                                                                                                                                                                                                   // <= 0 inproper, < 0 proper
bool p_on_seg(const P& p, const L& seg) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (l.s == l.t) return dist(p - l.s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    LD dist_to_seg(const P& p, const L& l) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 vector<F> convex_hull(vector<P> &p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       swap(p[j], p[3]);
                                                                                                                                                                                                                                                                3D Line, Face
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       goto found;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              3D Convex
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int a, b, c;
FT() { }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct FT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              5.12
```

```
// returns the length of the longest common prefix of s[i...
                                                                                                                                                                                                                                                                                                                                                                                                if (i == j) return L - i; for (int k = (int) P.size() - 1; k >= 0 && i < L && j <
                                                                                                                                                                                                    č
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       minsa = min(minsa, sa[i]);
maxsa = max(maxsa, sa[i]);
if (maxsa > split && minsa < split) return 1;</pre>
                                                                                         // arr has to be 0 based
void rmq_init(int *arr, int length) {
    for (int x = 0; x <= highbit(length); ++x)
    for (int i = 0; i <= length - (1 << x); ++i) {
        if (!x) f[i][x] = arr[i];
        else f[i][x] = min(f[i][x - 1], f[i + (1 << 1))][x - 1]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int checkNonOverlappingSubstring(int K) {
    // Greek if there is two non-overlapping identical
    substring of length K
    int minsa = 0, maxsa = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
int checkBelongToDifferentSubstring(int K, int split)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (S->checkBelongToDifferentSubstring(mid, sp))
        rmq_query(int x, int y) {
  int p = highbit(y - x + 1);
  return min(f[x][p], f[y - (1 << p) + 1][p]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   maxsa = max(maxsa, sa[i]);
if (maxsa - minsa >= K) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      minsa = sa[i]; maxsa = sa[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                minsa = sa[i]; maxsa = sa[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               minsa = min(minsa, sa[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int LongestCommonPrefix(int i, int j)
// getHeight() must be called firs
if (i == j) return L - i;
if (i > j) swap(i, j);
return rmq_query(i + 1, j);
                                                                                                                                                                                                                                                                                                                                                    int LongestCommonPrefix(int i, int j)
  int len = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for (int i = 0; i < L; ++i) {
  if (height[i] < K) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = 0; i < L; ++i) {
   if (height[i] < K) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                         L; k--) {
if (P[k][i] == P[k][j])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            len += 1 << k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int left = 0, right = sp;
while (left < right) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   j += 1 << k;
j += 1 << k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    S = new SuffixArray(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int sp = s.length();
s += "*" + t;
                                                                                                                                                                                                                                                                                                                                   L-1] and s[j
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return len;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              S->getHeight();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return 0;
                                                                                                                                                                                                                                                                   }
#ifdef NEW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   #endif
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  }
#else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        .* × <
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sort(M.begin(), M.end());
for (int i = 0; i < L; i++)
P[level][M[i].second] = (i > 0 && M[i].first ==
M[i - 1].first) ? P[level][M[i - 1].second
] : i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int j = sa[rank[i] - 1];
while (i + k < L && j + k < L && s[i + k] == s[j + k</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int np = _new(len[p] + 2);
num[np] = num[fa[np] = t[get_fa(fa[p])][ch]] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
for (unsigned i = 0; i < P.back().size(); ++i) {
    rank[i] = P.back()[i];</pre>
                                                                                                                                                                                                                 while (rs[n - i - len[x]] != rs[n]) x = fa[x]; return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // This is a traditional way to calculate LCP
        memset(t[sz], 0, sizeof t[0]);
len[sz] = l; cnt[sz] = num[sz] = 0;
return sz++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P.push_back(vector<int>(L, 0));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  memset(height, 0, sizeof height);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }
int f[N][Nlog];
inline int highbit(int x) {
    return 31 - __builtin_clz(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (rank[i] == 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (int i = 0; i < L; ++i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          height[rank[i]] = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                         ++cnt[last = t[p][ch]];
                                                                                                                                                                                                                                                                                                      rs[++n] = ch;
int p = get_fa(last);
if (!t[p][ch]) {
                                                                                                                              last = _new(0);
fa[last] = _new(-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    sa[rank[i]] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rmq_init(height, L);
                                                                                                           rs[n = sz = 0] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                             t[p][ch] = np;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Suffix Array
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      +
+
+
                                                                                                                                                                                                int get_fa(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (k) k--;
                                                                                                                                                                                                                                                             void ins(int ch) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void getHeight() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  struct SuffixArray {
                                                                     }
void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               9.
9.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void get_z(int a[], char s[], int n) {
   int l = 0, r = 0; a[0] = n;
   FOR (i, 1, n) {
        a[i] = i > r ? 0 : min(r - i + 1, a[i - l]);
        while (i + a[i] < n && s[a[i]] == s[i + a[i]]) ++a[i];
   if (i + a[i] - 1 > r) { l = i; r = i + a[i] - 1; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void manacher(int* a, int n) { // "obc" => "#0#b#a#"
int r = 0, p = 0;
FOR (i, 0, n) {
   if (i < r) R[i] = min(RL[2 * p - i], r - i);
   else RL[i] = 1;
   while (i - RL[i] >= 0 && i + RL[i] < n && a[i - RL[i]]</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // num: the number of palindrome suffixes of the prefix
    represented by the node
// cnt: the number of occurrences in string (should update to
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (RL[i] + i - 1 > r) \{ r = RL[i] + i - 1; p = i; \}
                                                                                                                                                                                                                                                                                                                                                      };
int LCP(const String &a, const String &b, int ai, int bi) {
    // Find LCP of a[ai...] and b[bi...]
    int l = 0, r = min(a.length - ai, b.length - bi);
    while (l < r) {
        int mid = (l + r + 1) / 2;
        int mid = (l + r + 1) / 2;
    }
}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hl[i] = get_substring_hash(i, i + sublen);
sorted = 0;
                                                                                                                                                                                                                            return binary_search(hl, hl + subsize, key);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (a.get_substring_hash(ai, ai + mid) == b.
    get_substring_hash(bi, bi + mid))
    l = mid:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int j = a[0] = 0;
FOR (i, 1, n) {
    while (j && s[i] != s[j]) j = a[j - 1];
    a[i] = j += s[i] == s[j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Palindrome Automation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void get_pi(int a[], char s[], int n)
                                                                                                                                                                                if (!sorted) assert (0);
if (!subsize) return false;
                                                                                             sort(hl, hl + subsize);
sorted = 1;
                                                                                                                                                                                                                                                               void init(const char *t) {
  length = strlen(t);
                                                                        void sort_substring_hash()
                                                                                                                                       bool match(ULL key) const
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        == a[i + RL[i]])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }
FOR (i, 0, n) --RL[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         father before using)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else r = mid - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               6.4 Manacher
                                                                                                                                                                                                                                                                                                               strcpy(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              RL[i]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 KMP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return l;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int RL[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                6.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 6.3
```

,

```
int get_state(int l, int r) {
   int u = rpos[r], s = r - l + 1;
   FORD (i, SP - 1, -1) if (len[pa[u][i]] >= s) u = pa[u][i];
   Feturn u;
                                                                                                                                                                = one[q];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        = one[q];
                                                                                                                                                                                                                                                         = nd;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        memcpy(t[nq], t[q], sizeof t[0]);
fa[nq] = fa[q];
fa[nq] = fa[q];
fa[nq] = fa[q] = nq;
for (; t[p][ch] == q; p = fa[p]) t[p][ch] = nq;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (; p && !t[p][ch]; p = fa[p]) t[p][ch] = np;
                                                                                                                                                       int nq = sz+; len[nq] = len[p] + 1; one[nq] = nmemcpy(t[nq], t[q], sizeof t[0]); fal[nq] = fal[q]; fal[q] = fal[np] = nq; for (; p && t[p][ch] = q; p = fal[p]) t[p][ch] :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      nq = sz++; len[nq] = len[p] + 1; one[nq]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int t[M][26], len[M] = {0}, fa[M], sz = 2, last = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int u = 1, l = 0;
FOR (i, 0, strlen(s)) {
   int ch = s[i] - 'a';
   while (u && !t[u][ch]) { u = fa[u]; l = len[u];
                                                                                                                                                                                                                                                                                                                                                                                                            FOR (i, 1, 256) c[i] = 0;

FOR (i, 2, sz) up[i] = s[one[i] + len[fa[i]]];

FOR (i, 2, sz) c[up[i]]++;

FOR (i, 1, 256) c[i] + c[i] - 1];

FOR (i, 2, sz) a[-c[up[i]]] = i;

FOR (i, 2, sz) G[fa[a[i]]].push_back(a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           FOR (i, 1, 256) c[i] = 0;

FOR (i, 2, sz) up[i] = *(one[i] + len[fa[i]]);

FOR (i, 2, sz) c[up[i]]++;

FOR (i, 1, 256) c[i] + c[i - 1];

FOR (i, 2, sz) aa[--c[up[i]]] = i;

FOR (i, 2, sz) G[fa[aa[i]]].push_back(aa[i]);
int p = last, np = last = sz++;
len[n] = len[n] + 1; one[np] = pp;
for (; p && it[p][ch]; p = fa[p]) t[p][ch] = if (!p) { fa[np] = 1; return; }
int q = t[p][ch];
int q = t[p][ch];
else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                q = t[p][ch];
if (len[p] + 1 == len[q]) fa[np] = q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    char* one[M];
void ins(int ch, char* pp) {
   int p = last, np = 0, nq = 0, q =
   if (!t[p][ch]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
last = np ? np : nq ? nq : q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           np = sz++; one[np] = pp;
len[np] = len[p] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int up[M], c[256] = {2}, aa[M];
                                                                                                                                                                                                                                                                                                                                                                int up[M], c[256] = {2}, a[M];
void rsort2() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (l) // do something...
                                                                                                                                                                                                                                                                                                 }
// lexicographical order
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (!p) fa[np] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ++l; u = t[u][ch];
if (!u) u = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
// substring state
                                                                                                                                                                                                                                                                                                                                                    generalized sam
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              namespace lct_sam
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vector<int> G[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void rsort() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // LCT-SAM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                }
// match
                                                                                                                                                                                                                                             sa.init(s, n, 128);
FOR (i, 1, n + 1) printf("%d%c", sa.sa[i] + 1, i == _i - 1 ?
FOR (i, 1, n + 1) printf("%d%c", sa.ht[i], i == _i - 1 ? '\n
': ' ');
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int t[M][26], len[M] = {-1}, fa[M], sz = 2, last = 1; void init() { memset(t, 0, (sz + 10) * sizeof t[0]); sz = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int nq = sz++; len[nq] = len[p] + 1;
memcpy(tlnq], t[q], sizeof t[0]);
fa[nq] = fa[q];
fa[np] = fa[q];
for (; t[p][ch] = nq; p = fa[p]) t[p][ch] = nq;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (; t[p][ch] == q; p = fa[p]) t[p][ch] = nq;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 u
d
u
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             n
G
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int p = last, np = last = sz++;
len[n] = len[n] + 1;
for (; p && !t[p][ch]; p = fa[p]) t[p][ch] =
if (!p) { fa[np] = 1; return; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 last = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (; p && !t[p][ch]; p = fa[p]) t[p][ch] =
                                                                                        :
-
-
                                       inline void init(T s, int n, int M) {
    sals(s, sa, ++n, t, b, c, M);
    for (int i = 1; i < n; i++) rk[sa[i]]
    getHeight(s, n, sa);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          q = t[p][ch];
if (len[p] + 1 == len[q]) fa[np] = q;
else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int q = t[p][ch];
if (len[p] + 1 == len[q]) fa[np] = q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  nq = sz+; len[nq] = len[p] + 1;
memcpy(t[nq], t[q], sizeof t[0]);
fa[nq] = fa[q];
fa[np] = fa[q] = nq;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FOR (i, 1, sz) c[i] = 0;
FOR (i, 1, sz) c[len[i]]++;
FOR (i, 1, sz) c[i] += c[i - 1];
FOR (i, 1, sz) a[--c[len[i]]] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Suffix Automation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
last = np ? np : nq ? nq : q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            np = sz++;
len[np] = len[p] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // rsort2 is not topo sort
void ins(int ch, int pp) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             namespace sam {
const int M = N << 1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int c[M] = {1}, a[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // lexicographical order
                                                                                                                                                                                                      int main() {
  int n = s.length();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  }
if (!p) fa[np] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void ins(int ch) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      last = 1; }
    }
template<class T>
                                                                                                                                                            };
SuffixArray<N> sa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        cnt[last][id]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void rsort()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else {
                                                                                                                                                                                                                                                                                                                                                                                                                                             6.7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         fill(b, b + M, 0); fill(sa, sa + n, -1);

FOR (i, 0, n) b[s[i]]++;

FOR (i, 1, M) f[i] = f[i - 1] + b[i];

FOR (i, 1, M) f[i] = f[i - 1] + b[i];

FOR (i, 1, M) f[i] = f[i - 1] + b[i - 1];

FOR (i, 0, n) if (sa[i] > 0 & it[sa[i] - 1];

FOR (i, 1, M) f[i] = f[i - 1] + b[i - 1];

FOR (i, 1, M) f[i] = f[i - 1] + b[i];

FOR (i, 1, M) f[i] = f[i - 1] + b[i];

FOR (i, 1, M) f[i] = sa[i] - 1;

FOR (i, 1, M) f[i] = sa[i] - 1;
                                                                                                                                                                                                                                                                                                     int b[size], c[size],
int sa[size], rk[size],
inline bool isLMS(const int i, const bool *t) { return i > 0
template
template
                                                                                                                                                                                                                                                                                                                                                                                                                               ij
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              cnt
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int j = sa[rk[i] - 1];
while (i + k < n && j + k < n && s[i + k] == s[j
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            FOR (i, bs, n) sa[i] = -1;

FOR (i, 0, bs) {

    x = sa[i];

    for (j = 0; j < n; j++) {

        if (p = -1 || s[x + j] |= s[p + j] || t[x + j] |

        i= t[p + j]) { cnt++, p = x; break; }

    else if (j > 0 && (isLMS(x + j, t) || isLMS(p +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inducedSort(s, sa, n, M, bs, t, b, r, c);
for (i = bs = 0; i < n; i++) if (isLMS(sa[i], t)) sa[bs
++] = sa[i];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bool *t, int *b, int *f, int *p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ij
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               II
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           sa [j
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               cnt);
                                                                                                                                                                                                                                                                                                                                                                                                                               inline void inducedSort(T s, int *sa, const int n, const
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          = (\sim x \& 1 ? x >> 1 : x - 1 >> 1), sa[bs + x] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FORD (1, 1, n) if (t[i] && !t[i - 1]) c[bs++] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline void getHeight(T s, const int n, const int *sa) for (int i = 0, k = 0; i < n; i++) { if (rk[i] == 0) k = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ,
4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (i = j = n - 1; i >= bs; i--) if (sa[i] >= 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ps,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int *s1 = sa + n - bs, *d = c + bs;
if (cnt < bs) sais(s1, sa, bs, t + n, b, c
else FoR (i, 0, bs) sais[s1[i1] = i;
FOR (i, 0, bs) d[i1] = c[sa[i1];
inducedSort(s, sa, n, M, bs, t, b, r, d);</pre>
                                                                                      sa/ht [1..n]
                                                                                                                                                                                                                      template<size_t size>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           j, t))) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           + k]) k++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (k > 0) k--;
                                                                                   // rk [0..n-1] -> [1..n], sc

// si normally as bucket

// c. normally as bucket

// c. normally as bucket

// d. normally as bucket2

// f. normally as cutbuf
                                                                                                                                                                                                                                                                                                                                                                                                                                                    M, const int bs,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ht[rk[i]] = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                --] = sa[i];
  printf("%d\n", left);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
template<typename T>
                                                                                                                                                                                                                                                                     struct SuffixArray {
  bool t[size << 1];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
template<class T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  else {
```

```
LD best_ans = eval(cur_x, cur_y);
LD best_x = cur_x, best_y = cur_y;
FOR (___, 0, 20) {
        LD nxt_x = cur_x + rd() * T, nxt_y = cur_y + rd() * T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FOR (i, 0, n)

r = max(r, sqrt(pow(xx - x[i], 2) + pow(yy - y[i], 2)));
if (!limit && dp[base][pos][len][s] != -1) return dp[base][
    pos][len][s];
    LL ret = 0;
    LL ed = lmit ? a[pos] : base - 1;
    FOR (i, 0, ed + 1) {
        tmp[pos] = i;
    }

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               max(X, Y);
                                                                                                                                                                                                                                                                                                                                       == a[
                                                                                                                                                                               == 0), s, limit
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (eval(cur_x, cur_y) < M) {
    ans = {cur_x, cur_y}; M = eval(cur_x, cur_y);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    printf("(%.1f,%.1f).\n%.1f\n", ans.first, ans.second,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             LD nxt_ans = eval(nxt_x, nxt_y);
if (nxt_ans < best_ans) {
   best_x = nxt_x; best_y = nxt_y;</pre>
                                                                                                                                                                                                                                                                                                                                  ret += dfs(base, pos - 1, len, s, limit &&
                                                                                                                                                  if (len == pos)
    ret += dfs(base, pos - 1, len - (i == 0),
    && i == a[pos]);
else if (s &&pos < (len + 1) / 2)
    ret += dfs(base, pos - 1, len, tmp[len -
    limit && i == a[pos]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             FOR (., 0, 100) {
LD cur_x = x / 2.0, cur_y = Y / 2.0, T = while (T > 1e-3) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             mt19937 mt(time(0));
auto rd = bind(uniform_real_distribution<LD>(-1, 1),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          FOR (i, 0, n) scanf("%d%d", &x[i], &y[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          cur_x = best_x; cur_y = best_y;
T *= .9;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return dfs(base, sz - 1, sz - 1, 1, true);
                                                                                                                                                                                                                                                                                                                                                                                     }
if (!limit) dp[base][pos][len][s] = ret;
return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               best_ans = nxt_ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               eval(ans.first, ans.second));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Simulated Annealing
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int X, Y;
while (cin >> X >> Y >> n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       = x % base;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       LD> ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             const int N = 1E4 + 100;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int x[N], y[N], n;
LD eval(LD xx, LD yy) {
   LD r = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             solve(LL x, LL base)
LL sz = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // Minimum Circle Cover
using LD = double;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  x /= base;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          while (x) {
a[sz++] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       7.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // routines, months are expressed as integers from 1 to 12, days // are expressed as integers from 1 to 31, and // years are expressed as integers from 1 to 31, and
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // converts integer (Julian day number) to Gregorian date: month
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          "Su"};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             string dayOfWeek[] = {"Mo", "Tu", "We", "Th" "Fr", "Sa",
// converts Gregorian date to integer (Julian day number)
int DateToInt (int m, int d, int y) {
    return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       LL dfs(LL base, LL pos, LL len, LL s, bool limit) {
  if (pos == -1) return s ? base : 1;
                                                                                                                                                     FOR (i, 1, N) {
    G[i] = pit++;
    G[i]->ls = G[i]->fa = null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // converts integer (Julian day number) to day of
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void IntToDate (int jd, int &m, int &d, int &y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int s = (S - 1) \& S; s; s = (S - 1) \& S) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1461 * (y + 4800 + (m - 14) / 12) / 4 + 367 * (m - 2 - (m - 14) / 12 * 12) / 12 - 3 * ((y + 4900 + (m - 14) / 12) / 100) / 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // years are expressed as 4-digit integers.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Subset Enumeration
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int x = t & -t, y = t + x;
t = ((t & \simy) / x >> 1) | y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void subset(int k, int n, T&& f) {
  int t = (1 << k) - 1;
  while (t < 1 << n) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               x = (146097 * n + 3) / 4;

i = (4000 * (x + 1)) / 1461001;

x = 1461 * i / 4 - 31;
                                                                                                                                                                                                                                                                                                                                                                                                       Miscellaneous
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     access(pp + 1, G[np]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             string IntToDay (int jd){
    return dayOfWeek[jd % 7];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // subset of length k
template<typename T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     n = 4 \times \times / 146097;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Digit DP
                                                                                                                                                                                                                                                               G[1] = null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // all proper subset
                                                                                                     void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int x, n, i, j;
x = jd + 68569;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Date
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       d - 32075;
                                                                                                                                  ++pit;
                                                                                                                                                       bool has_fa() { return fa->ls == this || fa->rs == this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fa[np] = fa[d] = nq;
G[np]->fa = G[nq];
for (; t[p][ch] == q; p = fa[p]) t[p][ch] = nq;
                                                                                                                                                                                                                                                                                                                                                                                               void all_down() { if (has_fa()) fa->all_down(); down();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (u->last) bit::add(u->last - R + 2, u->last - L + 2,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          bool dd = o->d();
p *f = o->fa, *t = o->c(idd);
p *f = o->fa, *t = o->c(idd);
if (f->has_fa()) f->fa->c(f->d()) = o; o->fa = f->fa;
if (t != null) t->fa = f; f->c(dd) = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               } *const null = new P{0, 0, 0, 0}, pool[M], *pit = pool;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int t[M][26], len[M] = {-1}, fa[M], sz = 2, last = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while (t->ls != null) t = t->ls;
int L = len[fa[t - pool]] + 1, R = len[u - pool];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (o->has_fa()) {
  if (o->fa->has_fa())
    rot(o->d() ^ o->fa->d() ? o : o->fa);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
void insert(P* u, P* v, P* t) {
   if (v != null) { splay(v); v->rs = null; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int p = last, np = last = sz++;
len[np] = len[p] + 1;
for (; p && !t[p][ch]; p = fa[p]) t[p][ch]
if (!p) fa[np] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void access(int last, P* u, P* v = null) {
  if (u == null) { v->last = last; return; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int nq = sz++; len[nq] = len[p] +
memcpy(t[nq], t[q], sizeof t[0]);
insert(G[q], G[fa[q]], G[nq]);
G[nq]->last = G[q]->last;
                                                                                                                                                                                                     bool d() { return fa->ls == this; }
P*& c(bool x) { return x ? ls : rs; }
P* up() { return this; }
void down() { return this; }
if (ls != null) ls->last = last;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     else bit::add(1, 1, R - L + 1);
bit::add(last - R + 2, last - L + 2,
                                                                                                                                                                                                                                                                                                                                             if (rs != null) rs->last = last;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  o \rightarrow c(idd) = f \rightarrow up(); f \rightarrow fa = o;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     access(last, u->up()->fa, u);
  extern struct P *const null;
const int M = N;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fa[nq] = fa[q];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void ins(int ch, int pp) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  u \rightarrow fa = t; t \rightarrow fa = v;
                                                                               *fa, *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void splay(P* o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  o->all_down();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void rot(P* o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rot(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               u \rightarrow rs = v;
                                                                                                             int last;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          o->nb();
                                                       struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else
```

1 数学

1.1 杜教筛

求 $S(n) = \sum_{i=1}^{n} f(i)$, 其中 f 是一个积性函数。

构造一个积性函数 g, 那么由 $(f*g)(n) = \sum_{d|n} f(d)g(\frac{n}{d})$, 得到 $f(n) = (f * g)(n) - \sum_{d|n,d < n} f(d)g(\frac{n}{d})$ 。

$$g(1)S(n) = \sum_{i=1}^{n} (f * g)(i) - \sum_{i=1}^{n} \sum_{d|i,d < i} f(d)g(\frac{n}{d}) \quad (1)$$

$$\stackrel{t=\frac{i}{d}}{=} \sum_{i=1}^{n} (f * g)(i) - \sum_{t=2}^{n} g(t)S(\lfloor \frac{n}{t} \rfloor)$$
 (2)

当然,要能够由此计算 S(n),会对 f,g 提出一些要求:

- f * g 要能够快速求前缀和。
- g 要能够快速求分段和(前缀和)。
- 对于正常的积性函数 g(1) = 1,所以不会有什么问题。 在预处理 S(n) 前 $n^{\frac{2}{3}}$ 项的情况下复杂度是 $O(n^{\frac{2}{3}})$ 。

1.2 素性测试

- 前置: 快速乘、快速幂
- int 范围内只需检查 2, 7, 61
- long long 范围 2, 325, 9375, 28178, 450775, 9780504, 1795265022
- 3E15 内 2, 2570940, 880937, 610386380, 4130785767
- 4E13 内 2, 2570940, 211991001, 3749873356
- http://miller-rabin.appspot.com/

1.3 扩展欧几里得

- \bar{x} ax + by = gcd(a, b) 的一组解
- 如果 a 和 b 互素,那么 x 是 a 在模 b 下的逆元
- 注意 x 和 y 可能是负数

1.4 类欧几里得

- $m = \lfloor \frac{an+b}{c} \rfloor$.
- $f(a,b,c,n) = \sum_{i=0}^{n} \lfloor \frac{ai+b}{c} \rfloor$: $\stackrel{\text{def}}{=} a \geq c \text{ or } b \geq c \text{ fl}$, $f(a,b,c,n) = (\frac{a}{c})n(n+1)/2 + (\frac{b}{c})(n+1) + f(a \mod c, b \mod c)$ (c,c,n); 否则 f(a,b,c,n) = nm - f(c,c-b-1,a,m-1)。
- $g(a,b,c,n) = \sum_{i=0}^{n} i \lfloor \frac{ai+b}{c} \rfloor$: $\stackrel{\omega}{=} a \geq c \text{ or } b \geq c \text{ fl},$ $g(a,b,c,n) = (\frac{a}{c})n(n+1)(2n+1)/6 + (\frac{b}{c})n(n+1)/2 +$ $g(a \mod c, b \mod c, c, n)$; 否则 $g(a, b, c, n) = \frac{1}{2}(n(n + c, b \mod c, c))$ 1)m - f(c, c - b - 1, a, m - 1) - h(c, c - b - 1, a, m - 1))
- $h(a,b,c,n) = \sum_{i=0}^{n} \lfloor \frac{ai+b}{c} \rfloor^2$: $\stackrel{\underline{}}{=}$ $a \geq c$ or $b \geq c$ c $\exists f$, $h(a,b,c,n) = (\frac{a}{c})^2 n(n+1)(2n+1)/6 + \dots$ $(\frac{b}{c})^2(n+1) + (\frac{a}{c})(\frac{b}{c})n(n+1) + h(a \bmod c, b \bmod c)$ $(c,c,n) + 2(\frac{a}{c})g(a \bmod c, b \bmod c, c, n) + 2(\frac{b}{c})f(a \bmod c, c, n)$ $c, b \mod c, c, n$); 否则 h(a, b, c, n) = nm(m+1) - 2g(c, c - m)b-1, a, m-1) - 2f(c, c-b-1, a, m-1) - f(a, b, c, n)

1.5 斯特灵数

- 第一类斯特灵数: 绝对值是 n 个元素划分为 k 个环排列 的方案数。s(n,k) = s(n-1,k-1) + (n-1)s(n-1,k)
- 第二类斯特灵数: *n* 个元素划分为 *k* 个等价类的方案数。 S(n,k) = S(n-1,k-1) + kS(n-1,k)

1.6 一些数论公式

- 当 $x \ge \phi(p)$ 时有 $a^x \equiv a^{x \mod \phi(p) + \phi(p)} \pmod{p}$
- $\mu^2(n) = \sum_{d^2|n} \mu(d)$
- $\sum_{d|n} \varphi(d) = n$
- $\sum_{d|n} 2^{\omega(d)} = \sigma_0(n^2)$, 其中 ω 是不同素因子个数 $\sum_{d|n} \mu^2(d) = 2^{\omega(d)}$

1.7 一些数论函数求和的例子

- $\sum_{i=1}^{n} i[gcd(i,n)=1] = \frac{n\varphi(n)+[n=1]}{2}$
- $\sum_{i=1}^{n} \sum_{j=1}^{m} [gcd(i,j) = x] = \sum_{d} \mu(d) \lfloor \frac{n}{dx} \rfloor \lfloor \frac{m}{dx} \rfloor$
- $\sum_{i=1}^{n} \sum_{j=1}^{m} gcd(i,j) = \sum_{i=1}^{n} \sum_{j=1}^{m} \sum_{d|qcd(i,j)} \varphi(d) =$ $\sum_{d} \varphi(d) \left| \frac{n}{d} \right| \left| \frac{m}{d} \right|$
- $S(n) = \sum_{i=1}^{n} \mu(i) = 1 \sum_{i=1}^{n} \sum_{d|i,d < i} \mu(d) \stackrel{t = \frac{i}{d}}{=} 1 \sum_{i=1}^{n} \sum_{d|i,d < i} \mu(d)$ $\sum_{t=2}^{n} S(\lfloor \frac{n}{t} \rfloor) \ (利用 \ [n=1] = \sum_{d|n} \mu(d))$
- $S(n) = \sum_{i=1}^{n} \varphi(i) = \sum_{i=1}^{n} i \sum_{i=1}^{n} \sum_{d|i,d < i} \varphi(i) \stackrel{t = \frac{i}{d}}{=}$ $\frac{i(i+1)}{2} - \sum_{t=2}^{n} S(\frac{n}{t})$ (利用 $n = \sum_{d|n} \varphi(d)$)
- $\sum_{i=1}^n \mu^2(i) = \sum_{i=1}^n \sum_{d^2|n} \mu(d) = \sum_{d=1}^{\lfloor \sqrt{n} \rfloor} \mu(d) \lfloor \frac{n}{d^2} \rfloor$
- $\sum_{i=1}^{n} \sum_{j=1}^{n} gcd^2(i,j) = \sum_{d} d^2 \sum_{t} \mu(t) \lfloor \frac{n}{dt} \rfloor^2$ $\stackrel{x=dt}{=} \sum_x \lfloor \frac{n}{x} \rfloor^2 \sum_{d|x} d^2 \mu(\frac{t}{x})$
- $\sum_{i=1}^{n} \varphi(i) = \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} [i \perp j] 1 = \frac{1}{2} \sum_{i=1}^{n} \mu(i)$ $|\frac{n}{i}|^2 - 1$

1.8 斐波那契数列性质

- $F_{a+b} = F_{a-1} \cdot F_b + F_a \cdot F_{b+1}$
- $F_1+F_3+\cdots+F_{2n-1}=F_{2n}, F_2+F_4+\cdots+F_{2n}=F_{2n+1}-1$
- $\sum_{i=1}^{n} F_i = F_{n+2} 1$
- $\sum_{i=1}^{n} F_i^2 = F_n \cdot F_{n+1}$
- $F_n^2 = (-1)^{n-1} + F_{n-1} \cdot F_{n+1}$
- $gcd(F_a, F_b) = F_{qcd(a,b)}$
- 模 n 周期(皮萨诺周期)
 - $-\pi(p^k) = p^{k-1}\pi(p)$
 - $-\pi(nm) = lcm(\pi(n), \pi(m)), \forall n \perp m$
 - $-\pi(2)=3,\pi(5)=20$
 - $\forall p \equiv \pm 1 \pmod{10}, \pi(p)|p-1$
 - $\forall p \equiv \pm 2 \pmod{5}, \pi(p)|2p+2$

常见生成函数

- $(1+ax)^n = \sum_{k=0}^n \binom{n}{k} a^k x^k$
- $\frac{1 x^{r+1}}{1 x} = \sum_{k=0}^{n} x^k$
- $\bullet \quad \frac{1}{1-ax} = \sum_{k=0}^{\infty} a^k x^k$

- $\frac{1}{(1-x)^2} = \sum_{k=0}^{\infty} (k+1)x^k$
- $\frac{1}{(1-x)^n} = \sum_{k=0}^{\infty} {n+k-1 \choose k} x^k$
- $e^x = \sum_{k=0}^{\infty} \frac{x^k}{k!}$
- $\ln(1+x) = \sum_{k=0}^{\infty} \frac{(-1)^{k+1}}{k} x^k$

1.10 佩尔方程

若一个丢番图方程具有以下的形式: $x^2 - ny^2 = 1$ 。且 n 为 正整数,则称此二元二次不定方程为佩尔方程。

若 n 是完全平方数,则这个方程式只有平凡解($\pm 1,0$)(实 际上对任意的 n, $(\pm 1,0)$ 都是解)。对于其余情况, 拉格朗日证 明了佩尔方程总有非平凡解。而这些解可由 \sqrt{n} 的连分数求出。

$$x = [a_0; a_1, a_2, a_3] = x = a_0 + \cfrac{1}{a_1 + \cfrac{1}{a_2 + \cfrac{1}{a_3 + \cfrac{1}{\ddots}}}}$$

设 $\frac{p_i}{a_i}$ 是 \sqrt{n} 的连分数表示: $[a_0; a_1, a_2, a_3, \ldots]$ 的渐近分 数列,由连分数理论知存在 i 使得 (p_i,q_i) 为佩尔方程的解。取 其中最小的 i, 将对应的 (p_i, q_i) 称为佩尔方程的基本解, 或最 小解,记作 (x_1,y_1) ,则所有的解 (x_i,y_i) 可表示成如下形式: $x_i + y_i \sqrt{n} = (x_1 + y_1 \sqrt{n})^i$ 。或者由以下的递回关系式得到:

$$x_{i+1} = x_1 x_i + n y_1 y_i, y_{i+1} = x_1 y_i + y_1 x_i$$

通常, 佩尔方程结果的形式通常是 $a_n = ka_{n-1} - a_{n-2} (a_{n-2})$ 前的系数通常是-1)。暴力/凑出两个基础解之后加上一个0, **1.18 博弈** 容易解出 k 并验证。

1.11 Burnside & Polya

 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$ 。 $X^g \in G$ 下的不动点数量,也就 是说有多少种东西用 g 作用之后可以保持不变。

 $|Y^X/G| = \frac{1}{|G|} \sum_{g \in G} m^{c(g)}$ 。用 m 种颜色染色,然后对于 某一种置换 g, 有 c(g) 个置换环, 为了保证置换后颜色仍然相 同,每个置换环必须染成同色。

1.12 皮克定理

2S = 2a + b - 2

- S 多边形面积
- a 多边形内部点数
- b 多边形边上点数

1.13 莫比乌斯反演

- $g(n) = \sum_{d|n} f(d) \Leftrightarrow f(n) = \sum_{d|n} \mu(d)g(\frac{n}{d})$
- $f(n) = \sum_{n|d} g(d) \Leftrightarrow g(n) = \sum_{n|d} \mu(\frac{d}{n}) f(d)$

1.14 低阶等幂求和

- $\begin{array}{ll} \bullet & \sum_{i=1}^n i^1 = \frac{n(n+1)}{2} = \frac{1}{2}n^2 + \frac{1}{2}n \\ \bullet & \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{1}{3}n^3 + \frac{1}{2}n^2 + \frac{1}{6}n \end{array}$

- $\sum_{i=1}^{n} i^3 = \left[\frac{n(n+1)}{2}\right]^2 = \frac{1}{4}n^4 + \frac{1}{2}n^3 + \frac{1}{4}n^2$ $\sum_{i=1}^{n} i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{1}{5}n^5 + \frac{1}{2}n^4 + \frac{1}{3}n^3 \frac{1}{30}n^3 + \frac{1}{30}n$
- $\frac{1}{30}n$ $\sum_{i=1}^{n} i^5 = \frac{n^2(n+1)^2(2n^2+2n-1)}{12} = \frac{1}{6}n^6 + \frac{1}{2}n^5 + \frac{5}{12}n^4 \frac{1}{12}n^2$

1.15 一些组合公式

- 错排公式: $D_1 = 0, D_2 = 1, D_n = (n-1)(D_{n-1} + D_{n-2}) =$ $n!(\frac{1}{2!} - \frac{1}{3!} + \dots + (-1)^n \frac{1}{n!}) = \lfloor \frac{n!}{e} + 0.5 \rfloor$
- 卡塔兰数(n 对括号合法方案数, n 个结点二叉树个数, $n \times n$ 方格中对角线下方的单调路径数, 凸 n+2 边形 的三角形划分数,n个元素的合法出栈序列数): C_n = $\frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!}$

1.16 伯努利数与等幂求和

1.17 数论分块

 $f(i) = \lfloor \frac{n}{i} \rfloor = v$ 时 i 的取值范围是 [l, r]。

- Nim 游戏:每轮从若干堆石子中的一堆取走若干颗。先手 必胜条件为石子数量异或和非零。
- 阶梯 Nim 游戏: 可以选择阶梯上某一堆中的若干颗向下 推动一级,直到全部推下去。先手必胜条件是奇数阶梯的 异或和非零 (对于偶数阶梯的操作可以模仿)。
- Anti-SG: 无法操作者胜。先手必胜的条件是:
 - SG 不为 0 且某个单一游戏的 SG 大于 1。
 - SG 为 0 且没有单一游戏的 SG 大于 1。
- Every-SG: 对所有单一游戏都要操作。先手必胜的条件是 单一游戏中的最大 step 为奇数。
 - 对于终止状态 step 为 0
 - 对于 SG 为 0 的状态, step 是最大后继 step +1
 - 对于 SG 非 0 的状态, step 是最小后继 step +1
- 树上删边: 叶子 SG 为 0, 非叶子结点为所有子结点的 SG 值加 1 后的异或和。

尝试:

- 打表找规律
- 寻找一类必胜态(如对称局面)
- 直接博弈 dp

2 图论

2.1 带下界网络流

- 无源汇: $u \to v$ 边容量为 [l,r], 连容量 r-l, 虚拟源点 到 $v \not\in l$, u 到虚拟汇点连 l。
- 有源汇: 为了让流能循环使用, 连 $T \to S$, 容量 ∞ .
- 最大流: 跑完可行流后, 加 $S' \to S$, $T \to T'$, 最大流就 是答案 $(T \to S)$ 的流量自动退回去了, 这一部分就是下界 部分的流量)。
- 最小流: T 到 S 的那条边的实际流量,减去删掉那条边 后 T 到 S 的最大流。
- 网上说可能会减成负的,还要有限地供应 S 之后,再跑一 遍 S 到 T 的。
- 费用流:必要的部分(下界以下的)不要钱,剩下的按照最大流。

2.2 二分图匹配

- 最小覆盖数 = 最大匹配数
- 最大独立集 = 顶点数 二分图匹配数
- DAG 最小路径覆盖数 = 结点数 拆点后二分图最大匹配数

2.3 差分约束

一个系统 n 个变量和 m 个约束条件组成,每个约束条件形如 $x_j - x_i \le b_k$ 。可以发现每个约束条件都形如最短路中的三角不等式 $d_u - d_v \le w_{u,v}$ 。因此连一条边 (i,j,b_k) 建图。

若要使得所有量两两的值最接近,源点到各点的距离初始成 0,跑最远路。

若要使得某一变量与其他变量的差尽可能大,则源点到各 点距离初始化成 ∞ ,跑最短路。

2.4 三元环

将点分成度入小于 \sqrt{m} 和超过 \sqrt{m} 的两类。现求包含第一类点的三元环个数。由于边数较少,直接枚举两条边即可。由于一个点度数不超过 \sqrt{m} ,所以一条边最多被枚举 \sqrt{m} 次,复杂度 $O(m\sqrt{m})$ 。再求不包含第一类点的三元环个数,由于这样的点不超过 \sqrt{m} 个,所以复杂度也是 $O(m\sqrt{m})$ 。

对于每条无向边 (u,v), 如果 $d_u < d_v$, 那么连有向边 (u,v), 否则有向边 (v,u)。度数相等的按第二关键字判断。然后枚举每个点 x, 假设 x 是三元组中度数最小的点,然后暴力往后面枚举两条边找到 y, 判断 (x,y) 是否有边即可。复杂度也是 $O(m\sqrt{m})$ 。

2.5 四元环

考虑这样一个四元环,将答案统计在度数最大的点 b 上。考虑枚举点 u,然后枚举与其相邻的点 v,然后再枚举所有度数比 v 大的与 v 相邻的点,这些点显然都可能作为 b 点,我们维护一个计数器来计算之前 b 被枚举多少次,答案加上计数器的值,然后计数器加一。

枚举完 u 之后,我们用和枚举时一样的方法来清空计数器就好了。

任何一个点,与其直接相连的度数大于等于它的点最多只有 $\sqrt{2m}$ 个。所以复杂度 $O(m\sqrt{m})$ 。

2.6 支配树

- semi[x] 半必经点(就是 x 的祖先 z 中,能不经过 z 和 x 之间的树上的点而到达 x 的点中深度最小的)
- idom[x] 最近必经点(就是深度最大的根到 x 的必经点)

3 计算几何

3.1 k 次圆覆盖

一种是用竖线进行切分,然后对每一个切片分别计算。扫描线部分可以魔改,求各种东西。复杂度 $O(n^3 \log n)$ 。

复杂度 $O(n^2 \log n)$ 。原理是:认为所求部分是一个奇怪的多边形 + 若干弓形。然后对于每个圆分别求贡献的弓形,并累加多边形有向面积。可以魔改扫描线的部分,用于求周长、至少覆盖 k 次等等。内含、内切、同一个圆的情况,通常需要特殊处理。

3.2 三维凸包

增量法。先将所有的点打乱顺序,然后选择四个不共面的 点组成一个四面体,如果找不到说明凸包不存在。然后遍历剩 余的点,不断更新凸包。对遍历到的点做如下处理。

- 1. 如果点在凸包内,则不更新。
- 2. 如果点在凸包外,那么找到所有原凸包上所有分隔了对于 这个点可见面和不可见面的边,以这样的边的两个点和新 的点创建新的面加入凸包中。

4 随机素数表

42737, 46411, 50101, 52627, 54577, 191677, 194869, 210407, 221831, 241337, 578603, 625409, 713569, 788813, 862481, 2174729, 2326673, 2688877, 2779417, 3133583, 4489747, 6697841, 6791471, 6878533, 7883129, 9124553, 10415371, 11134633, 12214801, 15589333, 17148757, 17997457, 20278487, 27256133, 28678757, 38206199, 41337119, 47422547, 48543479, 52834961, 76993291, 85852231, 95217823, 108755593, 132972461, 171863609, 173629837, 176939899, 207808351, 227218703, 306112619, 311809637, 322711981, 330806107, 345593317, 345887293, 362838523, 373523729, 394207349, 409580177, 437359931, 483577261, 490845269, 512059357, 534387017, 698987533, 764016151, 906097321, 914067307, 954169327

适合哈希的素数: 1572869, 3145739, 6291469, 12582917, 25165843, 50331653

NTT 素数表: $p=r2^k+1$, 原根是 g。 3, 1, 1, 2; 5, 1, 2, 2; 17, 1, 4, 3; 97, 3, 5, 5; 193, 3, 6, 5; 257, 1, 8, 3; 7681, 15, 9, 17; 12289, 3, 12, 11; 40961, 5, 13, 3; 65537, 1, 16, 3; 786433, 3, 18, 10; 5767169, 11, 19, 3; 7340033, 7, 20, 3; 23068673, 11, 21, 3; 104857601, 25, 22, 3; 167772161, 5, 25, 3; 469762049, 7, 26, 3; 1004535809, 479, 21, 3; 2013265921, 15, 27, 31; 2281701377, 17, 27, 3; 3221225473, 3, 30, 5; 75161927681, 35, 31, 3; 77309411329, 9, 33, 7; 206158430209, 3, 36, 22; 2061584302081, 15, 37, 7; 2748779069441, 5, 39, 3; 6597069766657, 3, 41, 5; 39582418599937, 9, 42, 5; 79164837199873, 9, 43, 5; 263882790666241, 15, 44, 7; 1231453023109121, 35, 45, 3; 1337006139375617, 19, 46, 3; 3799912185593857, 27, 47, 5.

5 心态崩了

- (int)v.size()
- 1LL << k
- 递归函数用全局或者 static 变量要小心
- 预处理组合数注意上限
- 想清楚到底是要 multiset 还是 set
- 提交之前看一下数据范围,测一下边界

- 数据结构注意数组大小(2倍,4倍)
- 字符串注意字符集
- 如果函数中使用了默认参数的话, 注意调用时的参数个数
- 注意要读完
- 构造参数无法使用自己
- 树链剖分/dfs 序, 初始化或者询问不要忘记 idx, ridx
- 排序时注意结构体的所有属性是不是考虑了
- 不要把 while 写成 if
- 不要把 int 开成 char
- 清零的时候全部用 0 到 n+1。
- 模意义下不要用除法
- 哈希不要自然溢出
- 最短路不要 SPFA, 乖乖写 Dijkstra
- 上取整以及 GCD 小心负数
- mid 用 1 + (r 1) / 2 可以避免溢出和负数的问题
- 小心模板自带的意料之外的隐式类型转换
- 求最优解时不要忘记更新当前最优解
- 图论问题一定要注意图不连通的问题
- 处理强制在线的时候 lastans 负数也要记得矫正
- 不要觉得编译器什么都能优化

