CEE 111

Engineering Drawing Lecture 4

Scales

Objects around us may vary greatly in size...









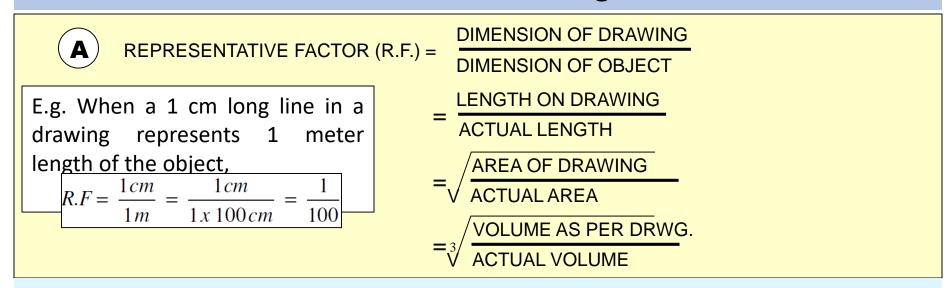
A scale is defined as the ratio of the linear dimensions of the object as represented in a drawing to the actual dimensions of the same. The proportion by which the drawing of a given object is enlarged or reduced is called scale of the drawing.

It is not convenient, always, to draw drawings of the object to its actual size. e.g. Buildings, Heavy machines, Bridges, Watches, Electronic devices etc. Thus, following scales are used

Enlargement scales	Reducing/ Reduction scales	Full scale	
Scales for the drawing of small objects needs to be enlarged	Scales for the drawing of huge objects needs to be reduced	Object is drawn on sheet to its actual size, then its drawn at full scale.	
Format – X:1, X>1, RF>1	Format – 1:Y, Y>1, RF<1	Format – 1:1, RF=1	
E.g. resistors, screws, gears for electronics, Ics, transistors	E.g. buildings, bridges, boilers, ships, aero planes	E.g. spanner, pen, nut bolts etc.	

RF (Representative Fraction)/ Scale factor

Ratio that indicates the scale of a drawing is called RF.



For RF above, both the lengths should have same units. All other dimensions of the object should be drawn to the same RF.

Scale and RF are synonymous, as scale is formatted as X:Y, while RF as X/Y.

Format of scale: SCALE X:Y written in the title block. If different objects are drawn to diff. scales on a sheet, respective scale is mentioned below the drawing of that object.

BIS (SP 46: 2003) recommended scales

Reducing scales	1:2	1:5	1:10
	1:20	1:50	1:100
1:Y (Y>1)	1:200	1:500	1:1000
	1:2000	1:5000	1:10000
Enlarging scales	50:1	20:1	10:1
X:1 (X>1)	5:1	2:1	
Full size scales			1:1

Intermediate scales can be used in exceptional cases where recommended scales can not be applied for functional reasons.

LOS (Length of Scale) (mm)

LENGTH OF SCALE (LOS)= R.F. X MAX. LENGTH TO BE MEASURED.

All the scales (except the scale of chords) are constructed by drawing a line of length equivalent to the actual distance to be represented. This length is called length of scale (LOS).

Types of scale

• Engineers Scale :

The relation between the dimension on the drawing and the actual dimension of the object is mentioned numerically (like 10mm = 15 m).

• Graphical Scale:

Scale is drawn on the drawing itself. This takes care of the shrinkage of the engineer's scale when the drawing becomes old.

Types of scales

- 1. PLAIN SCALES (FOR DIMENSIONS UP TO SINGLE DECIMAL)
- 2. DIAGONAL SCALES (FOR DIMENSIONS UP TO TWO DECIMALS)
- 3. VERNIER SCALES (FOR DIMENSIONS UP TO TWO DECIMALS)
- 4. COMPARATIVE SCALES (FOR COMPARING TWO DIFFERENT UNITS)
- 5. SCALE OF CORDS (FOR MEASURING/CONSTRUCTING ANGLES)





1 KILOMETRE = 10 HECTOMETRES

1 HECTOMETRE = 10 DECAMETRES

1 DECAMETRE = 10 METRES

1 METRE = 10 DECIMETRES

1 DECIMETRE = 10 CENTIMETRES

1 CENTIMETRE = 10 MILIMETRES

Plain scales

- 1. Calculate RF, if not given
- 2. Calculate LOS

If the maximum distance to be represented is not known, it may be taken equal to the maximum measurement (rounded off to the higher whole number) to be made with the help of scale.

- 3. Draw a line = LOS. Divide this line into the required number of equal parts. The divisions thus obtained are main divisions. Each main division will indicate the main unit of measurement. In case of speed or rate the same scale can be used for both time and distance.
- 4. Mark zero at the end of the first main division. Number the main divisions rightward from zero.
- 5. Divide the first main division into the required number of equal parts. The subdivisions obtained indicates subunits of the main unit. Number the subdivisions leftward from zero. Main unit is written below the right end of the scale and the subunit below the first main division. RF should be mentioned below the scale.



PLAIN SCALE:- This type of scale represents two units or a unit and it's sub-division.

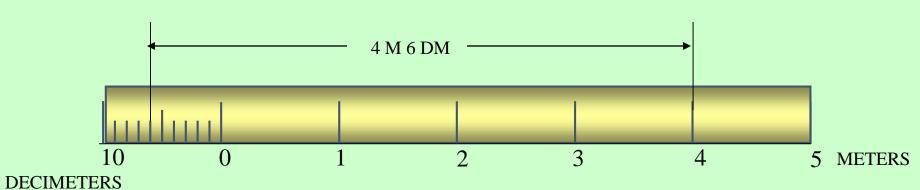
PROBLEM NO.1:- Draw a scale 1 cm = 1m to read decimeters, to measure maximum distance of 6 m. Show on it a distance of 4 m and 6 dm.

a) Calculate R.F.= DIMENSION OF DRAWING DIMENSION OF OBJECT

R.F.= 1cm/ 1m = 1/100 Length of scale = R.F. X max. distance = 1/100 X 600 cm = 6 cms



- b) Draw a line 6 cm long and divide it in 6 equal parts. Each part will represent larger division unit.
- c) Sub divide the first part which will represent second unit or fraction of first unit.
- d) Place (0) at the end of first unit. Number the units on right side of Zero and subdivisions on left-hand side of Zero. Take height of scale 5 to 10 mm for getting a look of scale.
- e) After construction of scale mention it's RF and name of scale as shown.
- f) Show the distance 4 m 6 dm on it as shown.



 $R.F. = 1/100 \\ \label{eq:r.f.}$ PLANE SCALE SHOWING METERS AND DECIMETERS.



PROBLEM NO.2:- In a map a 36 km distance is shown by a line 45 cms long. Calculate the R.F. and construct a plain scale to read kilometers and hectometers, for max. 12 km. Show a distance of 8.3 km on it.

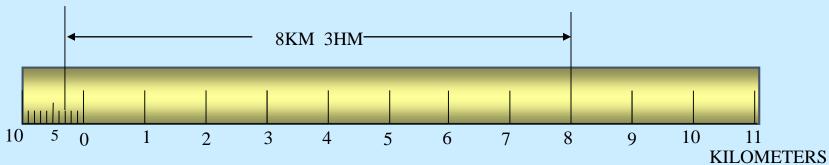
CONSTRUCTION:-

a) Calculate R.F.

R.F.= 45 cm/ 36 km = 45/ 36 . 1000 . 100 = 1/ 80,000 Length of scale = R.F.
$$\times$$
 max. distance = 1/ 80000 \times 12 km = 15 cm



- b) Draw a line 15 cm long and divide it in 12 equal parts. Each part will represent larger division unit.
- c) Sub divide the first part which will represent second unit or fraction of first unit.
- d) Place (0) at the end of first unit. Number the units on right side of Zero and subdivisions on left-hand side of Zero. Take height of scale 5 to 10 mm for getting a look of scale.
- e) After construction of scale mention it's RF and name of scale as shown.
- f) Show the distance 8.3 km on it as shown.



HECTOMETERS

 $R.F. = 1/80,\!000 \\ \label{eq:result}$ PLANE SCALE SHOWING KILOMETERS AND HECTOMETERS

PROBLEM NO.3:- The distance between two stations is 210 km. A passenger train covers this distance in 7 hours. Construct a plain scale to measure time up to a single minute. RF is 1/200,000 Indicate the distance traveled by train in 29 minutes.

CONSTRUCTION:-

a) 210 km in 7 hours. Means speed of the train is 30 km per hour (60 minutes)

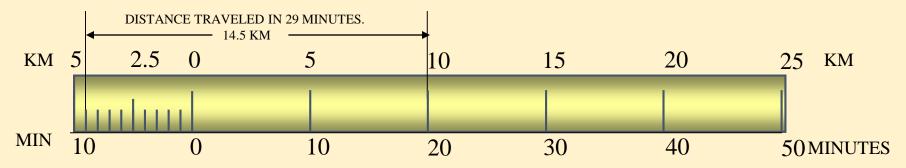


Length of scale = R.F. \times max. distance per hour = 1/2,00,000 \times 30km = 15 cm

- b) 15 cm length will represent 30 km and 1 hour i.e. 60 minutes.

 Draw a line 15 cm long and divide it in 6 equal parts. Each part will represent 5 km and 10 minutes.
- c) Sub divide the first part in 10 equal parts, which will represent second unit or fraction of first unit. Each smaller part will represent distance traveled in one minute.
- d) Place (0) at the end of first unit. Number the units on right side of Zero and subdivisions on left-hand side of Zero. Take height of scale 5 to 10 mm for getting a proper look of scale.
- e) Show km on upper side and time in minutes on lower side of the scale as shown.

 After construction of scale mention it's RF and name of scale as shown.
- f) Show the distance traveled in 29 minutes, which is 14.5 km, on it as shown.



 $R.F. = 1/2,\!00,\!000$ PLANE SCALE SHOWING METERS AND DECIMETERS.

Diagonal scales

- 1. Through Diagonal scale, measurements can be up to second decimal places (e.g. 4.35).
- 2. Are used to measure distances in a unit and its immediate two subdivisions; e.g. *dm*, *cm* & *mm*, or *yard*, *foot* & *inch*.

3. Diagonal scale can measure more accurately than the plain

scale.

Concept (based on similarity of triangles)

- 1. At end B of line AB, draw a perpendicular.
- 2. Step-off ten equal divisions of any length along the perpendicular starting from B and ending at C.
- 3. Number the division points 9,8,7,....1.
- Join A with C.
- 5. Through the points 1, 2, 3, etc., draw lines parallel to AB and cutting AC at 1', 2', 3', etc.

We have seen that the plain scales give only two dimensions, such as a unit and it's subunit or it's fraction.

The diagonal scales give us three successive dimensions that is a unit, a subunit and a subdivision of a subunit.

The principle of construction of a diagonal scale is as follows. Let the XY in figure be a subunit.

From Y draw a perpendicular YZ to a suitable height.

Join XZ. Divide YZ in to 10 equal parts.

Draw parallel lines to XY from all these divisions and number them as shown.

From geometry we know that similar triangles have their like sides proportional.

Consider two similar triangles XYZ and 7' 7Z, we have 7Z / YZ = 7'7 / XY (each part being one unit) Means 7' 7 = 7 / 10. x X Y = 0.7 XY

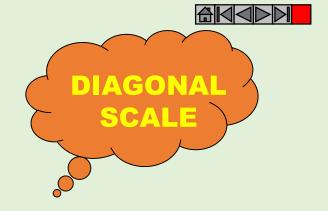
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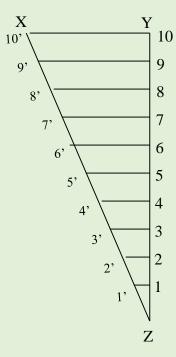
Similarly

$$1' - 1 = 0.1 XY$$

$$2' - 2 = 0.2 XY$$

Thus, it is very clear that, the sides of small triangles, which are parallel to divided lines, become progressively shorter in length by 0.1 XY.





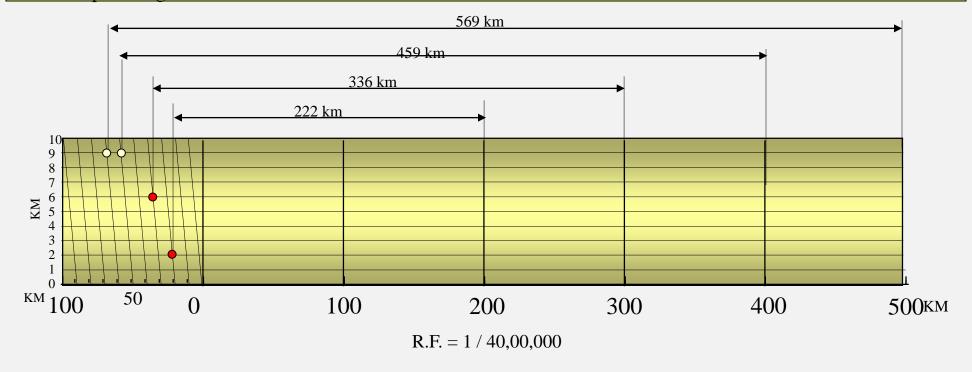
PROBLEM NO. 4: The distance between Delhi and Agra is 200 km. In a railway map it is represented by a line 5 cm long. Find it's R.F. Draw a diagonal scale to show single km. And maximum 600 km. Indicate on it following distances. 1) 222 km 2) 336 km 3) 459 km 4) 569 km



SOLUTION STEPS: RF = 5 cm / 200 km = 1 / 40, 00, 000

Length of scale = 1/40, 00, 000 X 600 X $10^5 = 15$ cm

Draw a line 15 cm long. It will represent 600 km.Divide it in six equal parts.(each will represent 100 km.) Divide first division in ten equal parts. Each will represent 10 km.Draw a line upward from left end and mark 10 parts on it of any distance. Name those parts 0 to 10 as shown. Join 9th sub-division of horizontal scale with 10th division of the vertical divisions. Then draw parallel lines to this line from remaining sub divisions and complete diagonal scale.



DIAGONAL SCALE SHOWING KILOMETERS.

PROBLEM NO.5: A rectangular plot of land measuring 1.28 hectare is represented on a map by a similar rectangle of 8 sq. cm. Calculate RF of the scale. Draw a diagonal scale to read single meter. Show a distance of 438 m on it.

SOLUTION:

1 hectare = 10,000 sq. meters

 $1.28 \text{ hectare} = 1.28 \text{ X} \ 10,000 \text{ sq. meters}$

$$= 1.28 \times 10^4 \times 10^4 \text{ sq. cm}$$

8 sq. cm area on map represents

$$= 1.28 \times 10^4 \times 10^4 \text{ sq. cm}$$
 on land

1 cm sq. on map represents

$$= 1.28 \times 10^4 \times 10^4 / 8 \text{ sq cm on land}$$

1 cm on map represent

$$= \sqrt{1.28 \times 10^4 \times 10^4 / 8} \quad \text{cm}$$

=4,000 cm

1 cm on drawing represent 4, 000 cm, Means RF = 1/4000 Assuming length of scale 15 cm, it will represent 600 m.

Draw a line 15 cm long.

It will represent 600 m.Divide it in six equal parts. (each will represent 100 m.)

Divide first division in ten equal parts. Each will represent 10 m.

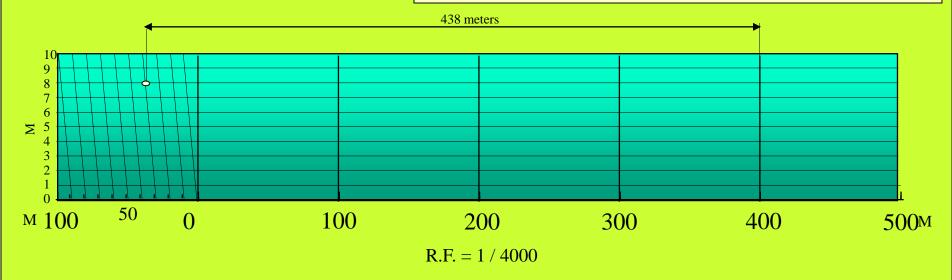
Draw a line upward from left end and mark 10 parts on it of any distance.

Name those parts 0 to 10 as shown. Join 9th sub-division of horizontal scale with 10th division of the vertical divisions.

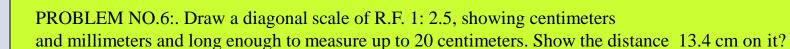
Then draw parallel lines to this line from remaining sub divisions and complete diagonal scale.

DIAGONAL

SCALE



DIAGONAL SCALE SHOWING METERS.





SOLUTION STEPS:

R.F. = 1/2.5

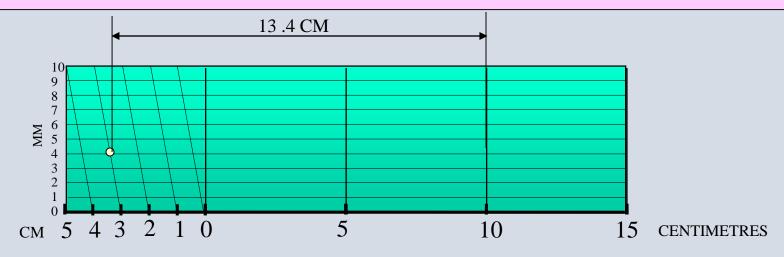
Length of scale = $1/2.5 \times 20 \text{ cm}$.

= 8 cm.

1.Draw a line 8 cm long and divide it in to 4 equal parts. (Each part will represent a length of 5 cm.)

- 2.Divide the first part into 5 equal divisions. (Each will show 1 cm.)
- 3.At the left hand end of the line, draw a vertical line and on it step-off 10 equal divisions of any length.
- 4. Complete the scale as explained in previous problems. Show the distance 13.4 cm on it.





R.F. = 1/2.5 DIAGONAL SCALE SHOWING CENTIMETERS.

COMPARATIVE SCALES:

These are the Scales having same R.F. but graduated to read different units.

These scales may be Plain scales or Diagonal scales and may be constructed separately or one above the other.





A distance of 40 miles is represented by a line 8 cm long. Construct a plain scale to read 80 miles. Also construct a comparative scale to read kilometers upto 120 km (1 m = 1.609 km)

SOLUTION STEPS:

Scale of Miles:

40 miles are represented = 8 cm

: 80 miles = 16 cm

R.F. = 8 / 40 X 1609 X 1000 X 100

= 1 / 8, 04, 500

CONSTRUCTION:

Take a line 16 cm long and divide it into 8 parts. Each will represent 10 miles. Subdivide the first part and each sub-division will measure single mile.

Scale of Km.

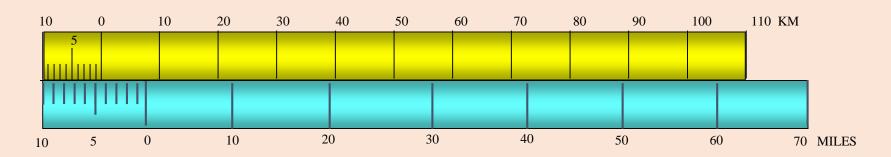
Length of scale = 1 / 8,04,500 X 120 X 1000 X 100

= 14.90 cm

CONSTRUCTION:

On the top line of the scale of miles cut off a distance of 14.90 cm and divide it into 12 equal parts. Each part will represent 10 km.

Subdivide the first part into 10 equal parts. Each subdivision will show single km.



 $R.F. = 1 \ / \ 804500$ COMPARATIVE SCALE SHOWING MILES AND KILOMETERS



COMPARATIVE SCALE:

EXAMPLE NO. 8:

A motor car is running at a speed of 60 kph. On a scale of RF = 1/4,00,000 show the distance traveled by car in 47 minutes.

SOLUTION STEPS:

Scale of km.

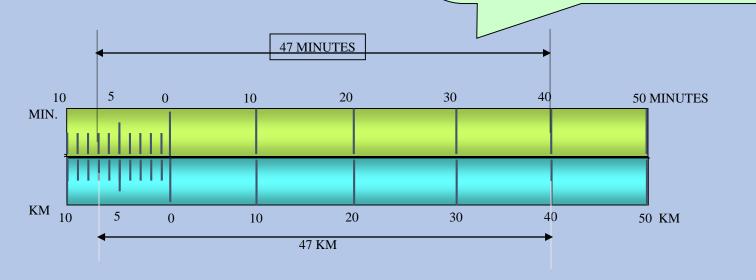
length of scale = RF X 60 km = $1 / 4,00,000 \times 60 \times 10^5$ = 15 cm.

CONSTRUCTION:

Draw a line 15 cm long and divide it in 6 equal parts. (each part will represent 10 km.)
Subdivide 1st part in 0 equal subdivisions. (each will represent 1 km.)

Time Scale:

Same 15 cm line will represent 60 minutes. Construct the scale similar to distance scale. It will show minimum 1 minute & max. 60min.



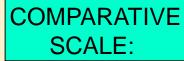
 $R.F. = 1 \ / \ 4,00,000$ COMPARATIVE SCALE SHOWING MINUTES AND KILOMETERS

EXAMPLE NO. 9:

A car is traveling at a speed of 60 km per hour. A 4 cm long line represents the distance traveled by the car in two hours. Construct a suitable comparative scale up to 10 hours. The scale should be able to read the distance traveled in one minute. Show the time required to cover 476 km and also distance in 4 hours and 24 minutes.

SOLUTION:

4 cm line represents distance in two hours, means for 10 hours scale, 20 cm long line is required, as length of scale. This length of scale will also represent 600 kms. (as it is a distance traveled in 10 hours) CONSTRUCTION:



Distance Scale (km)

Draw a line 20 cm long. Divide it in TEN equal parts.(Each will show 60 km)

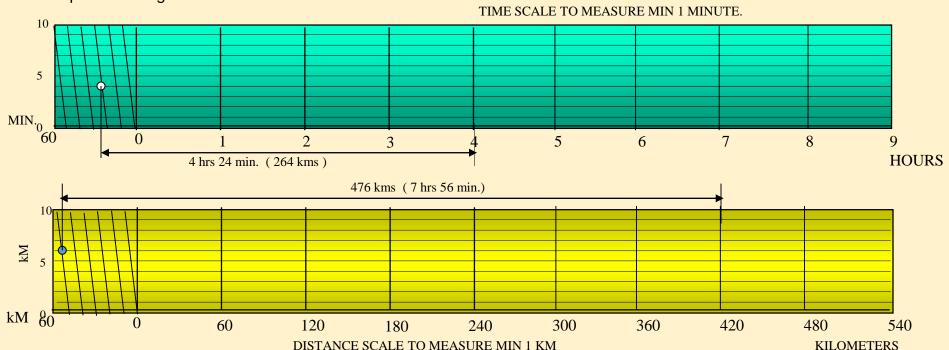
Sub-divide 1st part in SIX subdivisions. (Each will represent 10 km)

At the left hand end of the line, draw a vertical line and on it step-off 10 equal divisions of any length.

And complete the diagonal scale to read minimum ONE km.

Time scale:

Draw a line 20 cm long. Divide it in TEN equal parts. (Each will show 1 hour) Sub-divide 1st part in SIX subdivisions. (Each will represent 10 minutes) At the left hand end of the line, draw a vertical line and on it step-off 10 equal divisions of any length. And complete the diagonal scale to read minimum ONE minute.





Vernier Scales:

These scales, like diagonal scales, are used to read to a very small unit with great accuracy. It consists of two parts – a primary scale and a vernier. The primary scale is a plain scale fully divided into minor divisions.

As it would be difficult to sub-divide the minor divisions in ordinary way, it is done with the help of the vernier. The graduations on vernier are derived from those on the primary scale.

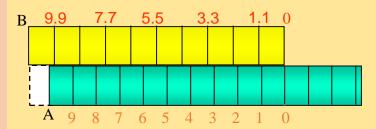
Figure to the right shows a part of a plain scale in which length A-O represents 10 cm. If we divide A-O into ten equal parts, each will be of 1 cm. Now it would not be easy to divide each of these parts into ten equal divisions to get measurements in millimeters.

Now if we take a length BO equal to 10 + 1 = 11 such equal parts, thus representing 11 cm, and divide it into ten equal divisions, each of these divisions will represent 11 / 10 - 1.1 cm.

The difference between one part of AO and one division of BO will be equal 1.1 - 1.0 = 0.1 cm or 1 mm.

This difference is called Least Count of the scale.

Minimum this distance can be measured by this scale. The upper scale BO is the vernier. The combination of plain scale and the vernier is vernier scale.



Example 10:

Draw a vernier scale of RF = 1 / 25 to read centimeters upto 4 meters and on it, show lengths 2.39 m and 0.91 m



SOLUTION:

Length of scale = RF X max. Distance

 $= 1/25 \times 4 \times 100$

= 16 cm

CONSTRUCTION: (Main scale)

Draw a line 16 cm long.

Divide it in 4 equal parts.

(each will represent meter)

Sub-divide each part in 10 equal parts. (each will represent decimeter)

Name those properly.

CONSTRUCTION: (vernier)

Take 11 parts of Dm length and divide it in 10 equal parts. Each will show 0.11 m or 1.1 dm or 11 cm and construct a rectangle Covering these parts of vernier.

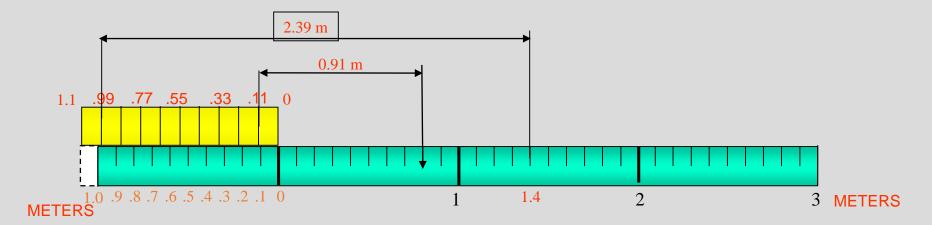
TO MEASURE GIVEN LENGTHS:

(1) For 2.39 m: Subtract 0.99 from 2.39 i.e. 2.39 - .99 = 1.4 m

The distance between 0.99 (left of Zero) and 1.4 (right of Zero) is 2.39 m

(2) For 0.91 m: Subtract 0.11 from 0.91 i.e. 0.91 - 0.11 = 0.80 m

The distance between 0.11 and 0.80 is 0.91 m



Example 11: A map of size 500cm X 50cm wide represents an area of 6250 sq.Kms. Construct a vernier scale to measure kilometers, hectometers and decameters and long enough to measure upto 7 km. Indicate on it a) 5.33 km b) 59 decameters.

Vernier Scale

SOLUTION:

$$RF = \sqrt{\frac{\text{AREA OF DRAWING}}{\text{ACTUAL AREA}}}$$
$$= \sqrt{\frac{500 \times 50 \text{ cm sq.}}{6250 \text{ km sq.}}}$$
$$= 2 / 10^{5}$$

Length of scale = RF X max. Distance = 2 / 10⁵ X 7 kms = 14 cm

CONSTRUCTION: (Main scale)

Draw a line 14 cm long.
Divide it in 7 equal parts.
(each will represent km)
Sub-divide each part in 10 equal parts.
(each will represent hectometer)
Name those properly.

CONSTRUCTION: (vernier)

and divide it in 10 equal parts.

Each will show 1.1 hm m or 11 dm and

Covering in a rectangle complete scale.

Take 11 parts of hectometer part length

TO MEASURE GIVEN LENGTHS:

a) For 5.33 km:

Subtract 0.33 from 5.33

i.e. 5.33 - 0.33 = 5.00

The distance between 33 dm

(left of Zero) and

5.00 (right of Zero) is 5.33 k m

(b) For 59 dm:

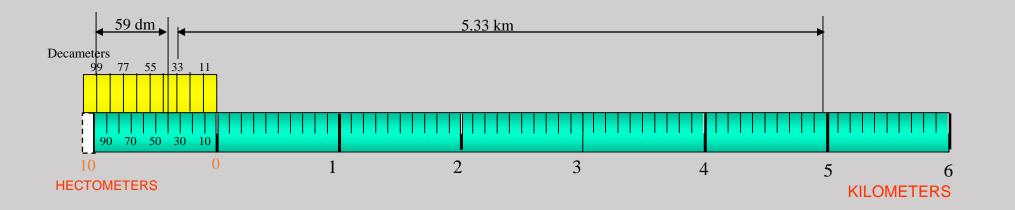
Subtract 0.99 from 0.59

i.e. 0.59 - 0.99 = -0.4 km

(- ve sign means left of Zero)

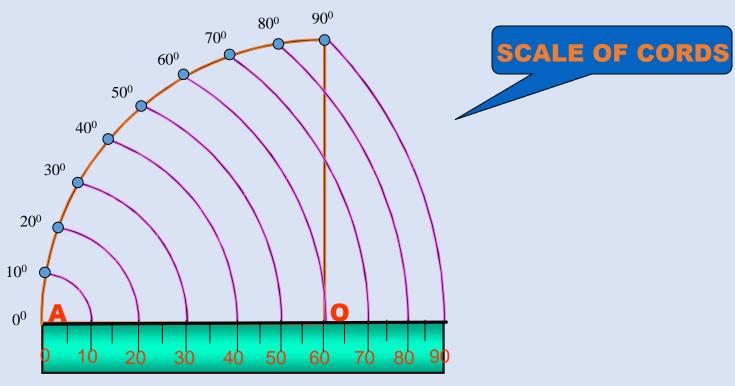
The distance between 99 dm and

- .4 km is 59 dm (both left side of Zero)









CONSTRUCTION:

- 1. DRAW SECTOR OF A CIRCLE OF 90° WITH 'OA' RADIUS. ('OA' ANY CONVINIENT DISTANCE)
- 2. DIVIDE THIS ANGLE IN NINE EQUAL PARTS OF 10 ° EACH.
- 3. NAME AS SHOWN FROM END 'A' UPWARDS.
- 4. FROM 'A' AS CENTER, WITH CORDS OF EACH ANGLE AS RADIUS DRAW ARCS DOWNWARDS UP TO 'AO' LINE OR IT'S EXTENSION AND FORM A SCALE WITH PROPER LABELING AS SHOWN.

AS CORD LENGTHS ARE USED TO MEASURE & CONSTRUCT DIFERENT ANGLES IT IS CALLED SCALE OF CORDS.

PROBLEM 12: Construct any triangle and measure it's angles by using scale of cords.

CONSTRUCTION:

First prepare Scale of Cords for the problem.

Then construct a triangle of given sides. (You are supposed to measure angles x, y and z) To measure angle at x:

Take O-A distance in compass from cords scale and mark it on lower side of triangle as shown from corner x. Name O & A as shown. Then O as center, O-A radius draw an arc upto upper adjacent side. Name the point B.

Take A-B cord in compass and place on scale of cords from Zero.

It will give value of angle at x

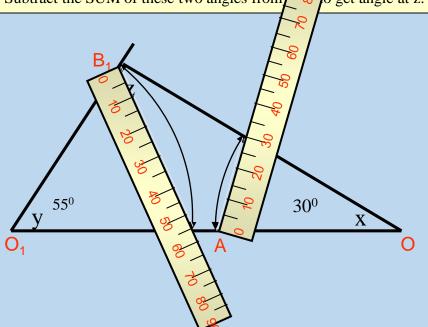
To measure angle at y:

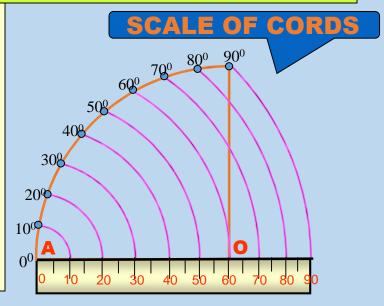
Repeat same process from O₁. Draw arc with radius O₁A₁.

Place Cord A_1B_1 on scale and get angle at y.

To measure angle at z:

Subtract the SUM of these two angles from 6 get angle at z.





PROBLEM 12: Construct 25° and 115° angles with a horizontal line, by using scale of cords.

CONSTRUCTION:

First prepare Scale of Cords for the problem.

Then Draw a horizontal line. Mark point O on it.

To construct 25⁰ angle at O.

Take O-A distance in compass from cords scale and mark it on on the line drawn, from O Name O & A as shown. Then O as center, O-A radius draw an arc upward..

Take cord length of 25⁰ angle from scale of cords in compass and

from A cut the arc at point B.Join B with O. The angle AOB is thus 25⁰

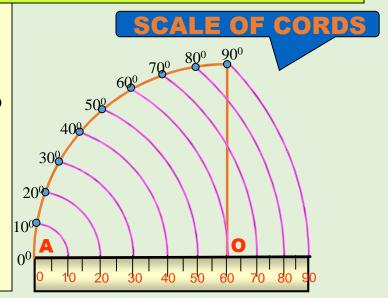
To construct 115⁰ angle at O.

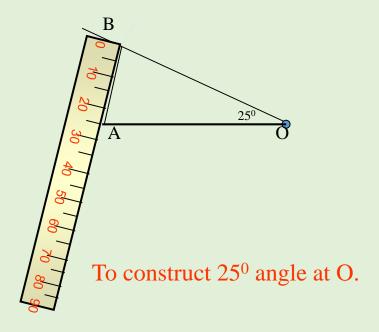
This scale can measure or construct angles upto 90° only directly.

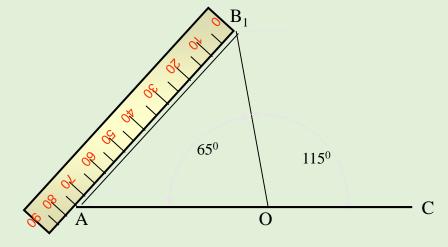
Hence Subtract 115^o from 180^o. We get 75^o angle,

which can be constructed with this scale.

Extend previous arc of OA radius and taking cord length of 75^{0} in compass cut this arc at B₁ with A as center. Join B₁ with O. Now angle AOB₁ is 75^{0} and angle COB₁ is 115^{0} .







To construct 115⁰ angle at O.