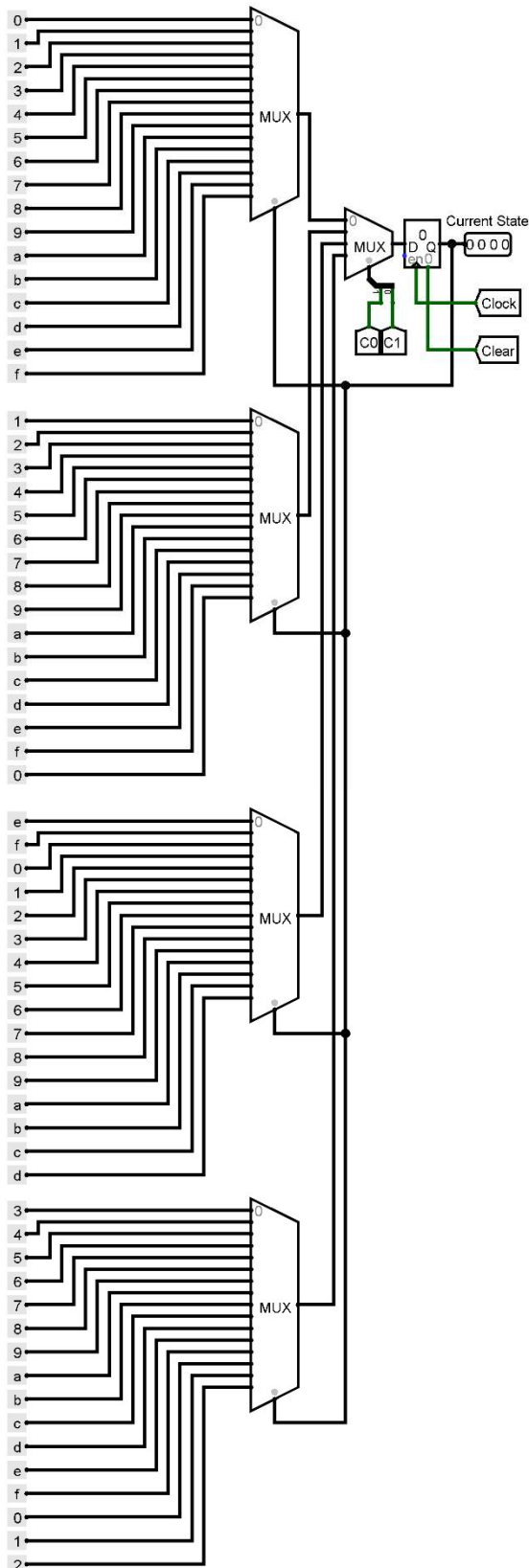


# CS226 - Switching Theory Lab - 11

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Roll No.: 1801CS31

## Ans 1: Circuit Diagram

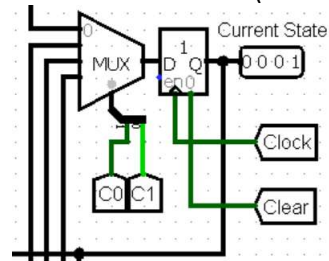


## Test Run

Initially, Counter reads 0

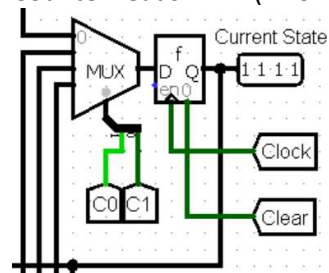
**Step 1:** Set C1 = 0, C0 = 1, and toggle the clock.

- Value stored is incremented by 1
- Counter reads 0001 (DEC 1)



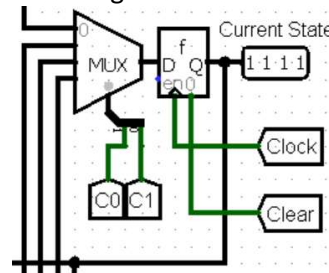
**Step 2:** Set C1 = 1, C0 = 0, and toggle the clock.

- Value stored is decremented by 2
- Counter reads 1111 (DEC 15)



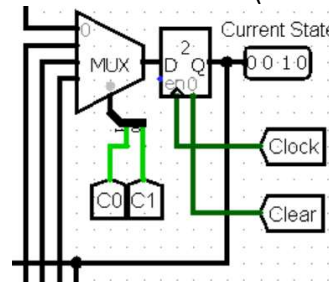
**Step 3:** Set C1 = 0, C0 = 0, and toggle the clock

- No change in stored value



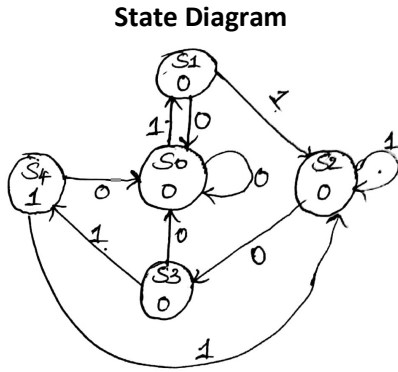
**Step 4:** Set C1 = 1, C0 = 1 and toggle the clock

- Value stored is incremented by 3
- Counter reads 0010 (DEC 2)



**Ans 2:**

**Moore FSM to detect 1101**



**State Encoding**

State	Code
S0	000
S1	001
S2	010
S3	011
S4	100

**Output Table**

Current State			Output
S <sub>2</sub>	S <sub>1</sub>	S <sub>0</sub>	Y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1

**Implementation using JK Flip Flop:**

**State Transition Table**

Current State S <sub>2</sub> S <sub>1</sub> S <sub>0</sub>	Input A	Next State S' <sub>2</sub> S' <sub>1</sub> S' <sub>0</sub>	J <sub>2</sub> K <sub>2</sub>	J <sub>1</sub> K <sub>1</sub>	J <sub>0</sub> K <sub>0</sub>
0 0 0	0	0 0 0	0 X	0 X	0 X
0 0 0	1	0 0 1	0 X	0 X	1 X
0 0 1	0	0 0 0	0 X	0 X	X 1
0 0 1	1	0 1 0	0 X	1 X	X 1
0 1 0	0	0 1 1	0 X	X 0	1 X
0 1 0	1	0 1 0	0 X	X 0	0 X
0 1 1	0	0 0 0	0 X	X 1	X 1
0 1 1	1	1 0 0	1 X	X 1	X 1
1 0 0	0	0 0 0	X 1	0 X	0 X
1 0 0	1	0 1 0	X 1	1 X	0 X
1 0 1	0	0 0 0	X 1	0 X	X 1
1 0 1	1	0 0 0	X 1	0 X	X 1
1 1 0	0	0 0 0	X 1	X 1	0 X
1 1 0	1	0 0 0	X 1	X 1	0 X
1 1 1	0	0 0 0	X 1	X 1	X 1
1 1 1	1	0 0 0	X 1	X 1	X 1

# K-Map Simplification

$S_2 \backslash S_1 A$	00	01	11	10
00	X	X	1	1
01	X	X	1	1
11	X	X	1	1
10	X	X	1	1

$K_0 = 1$

$S_2 \backslash S_1 A$	00	01	11	10
00	X	X	X	X
01			1	1
11	1	1	1	1
10	X	X	X	X

$K_1 = S_2 + S_0$

$S_2 \backslash S_1 A$	00	01	11	10
00	X	X	X	X
01	X	X	X	X
11	1	1	1	1
10	1	1	1	1

$K_2 = 1$

$S_2 \backslash S_1 A$	00	01	11	10
00		1	X	X
01	1		X	X
11			X	X
10			X	X

$J_0 = \bar{S}_2 \bar{S}_1 A + \bar{S}_2 S_1 \bar{A}$   
 $J_0 = \bar{S}_2 (S_1 \oplus A)$

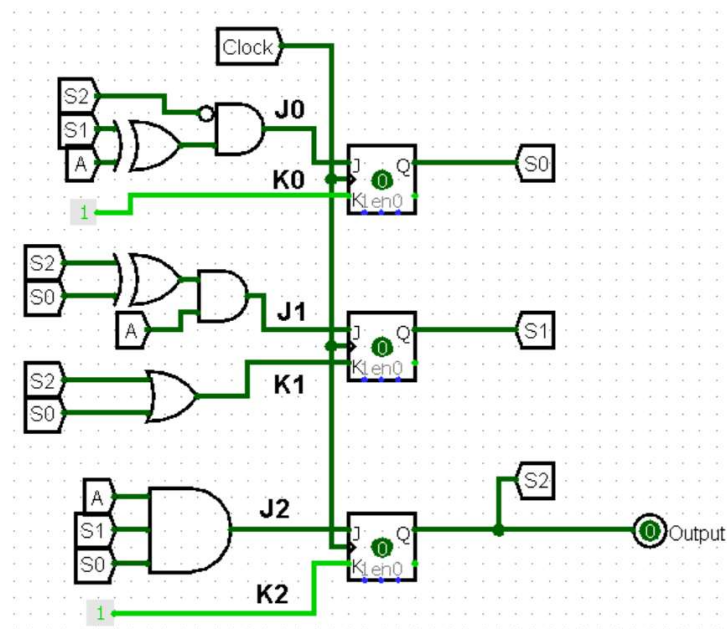
$S_2 \backslash S_1 A$	00	01	11	10
00			1	
01	X	X	X	X
11	X	X	X	X
10		1		

$J_1 = \bar{S}_2 A + S_2 \bar{S}_0 A$   
 $J_1 = A (S_0 \oplus S_2)$

$S_2 \backslash S_1 A$	00	01	11	10
00				
01			1	
11	X	X	X	X
10	X	X	X	X

$J_2 = S_1 S_0 A$

## Logic Diagram



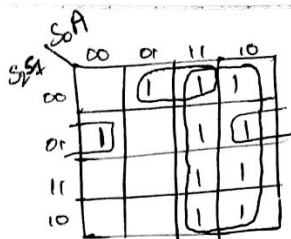
## Implementation using T Flip-Flop

### State Transition Table

Moore FSM State Transition Table

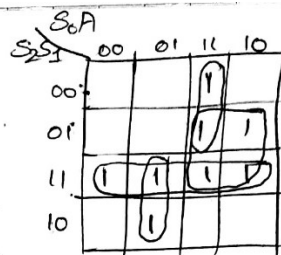
Current State $S_2$ $S_1$ $S_0$			Inputs $A$	Next State $S_2'$ $S_1'$ $S_0'$			$T_2$	$T_1$	$T_0$
0	0	0	0	0	0	0	0	0	0
0	0	0	1	0	0	1	0	0	1
0	0	1	0	0	0	0	0	0	1
0	0	1	1	0	1	0	0	1	1
0	1	0	0	0	1	1	0	0	1
0	1	0	1	0	1	0	0	0	0
0	1	1	0	0	0	0	0	1	1
0	1	1	1	1	1	0	1	1	1
1	0	0	0	0	0	0	1	0	0
1	0	0	1	0	1	0	1	1	0
1	0	1	0	0	0	0	1	0	1
1	0	1	1	0	0	0	1	0	1
1	1	0	0	0	0	0	1	1	0
1	1	0	1	0	0	0	1	1	0
1	1	1	0	0	0	0	1	1	1
1	1	1	1	0	0	0	1	1	1

### K-Map Simplification



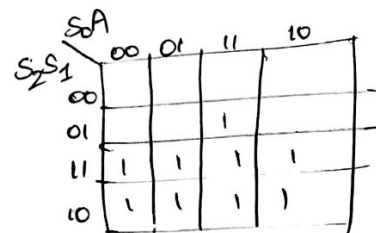
$$T_0 = \bar{S}_2 \bar{S}_1 A + \bar{S}_2 S_1 \bar{A}$$

$$T_0 = \bar{S}_2 (S_1 \oplus A)$$



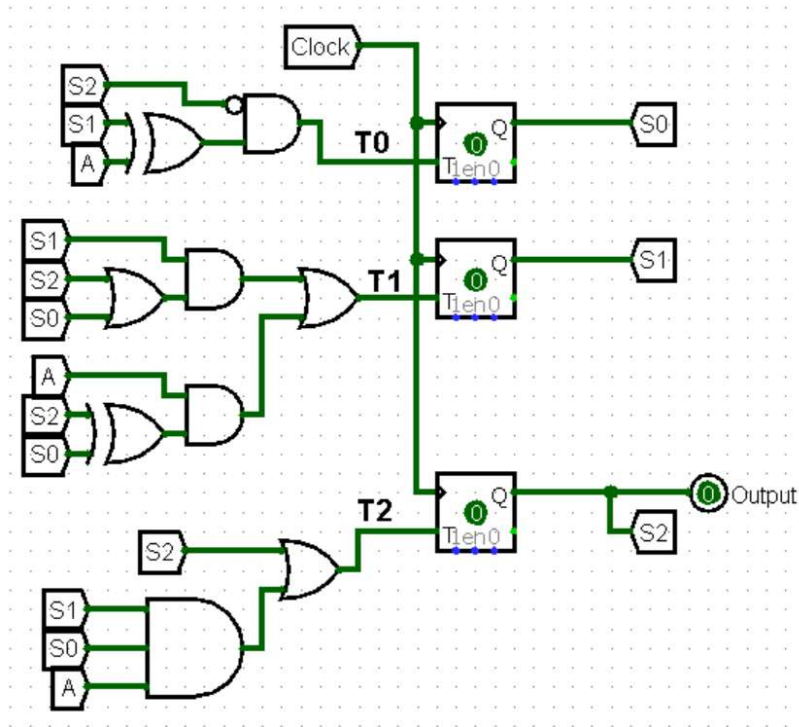
$$T_1 = S_1 S_0 + S_2 S_1 + S_2 \bar{S}_0 A + \bar{S}_2 S_0 A$$

$$T_1 = S_1 (S_2 + S_0) + A (S_2 \oplus S_0)$$



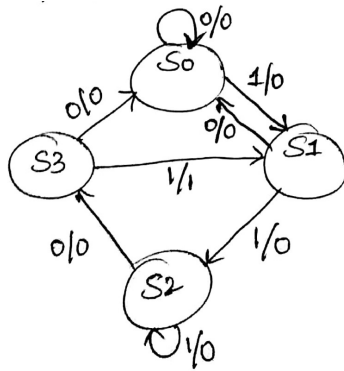
$$T_2 = S_2 + S_1 S_0 A$$

## Logic Diagram



## Mealy FSM to detect 1101

State Diagram



State Encoding

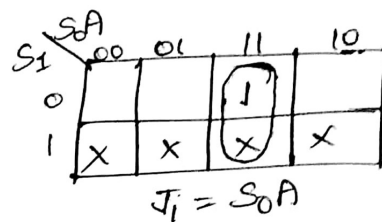
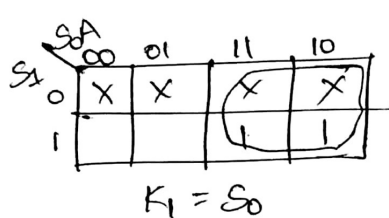
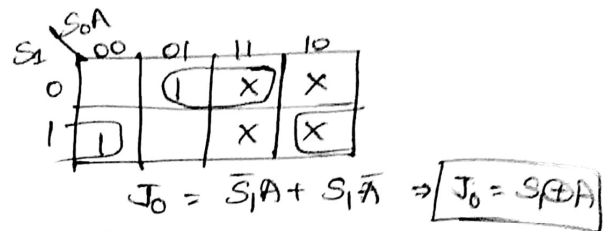
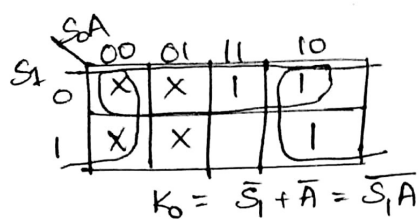
State	Code
S0	00
S1	01
S2	10
S3	11

## Implementation using JK Flip Flop:

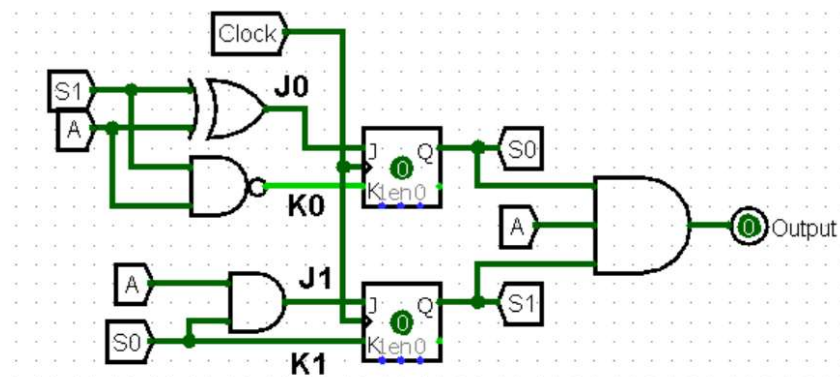
State Transition Table

Current State $S_1 \ S_0$		Input $A$	Next State $S_1' \ S_0'$		Output $Y$	$J_1$	$K_1$	$J_0$	$K_0$
0	0	0	0	0	0	0	X	0	X
0	0	1	0	1	0	0	X	1	X
0	1	0	0	0	0	0	X	X	1
0	1	1	1	0	0	1	X	X	1
1	0	0	1	1	0	X	0	1	X
1	0	1	1	0	0	X	0	0	X
1	1	0	0	0	0	X	1	X	1
1	1	1	0	1	1	X	1	X	0

K-Map Simplification (Output  $Y = S_1 S_0 A$ )



Logic Diagram

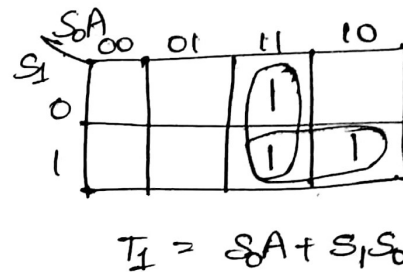
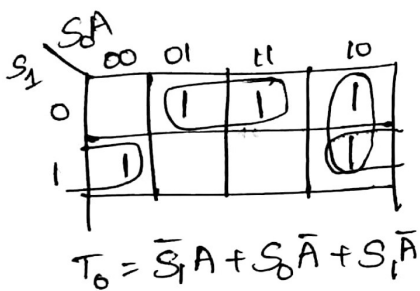


## Implementation using T Flip Flop:

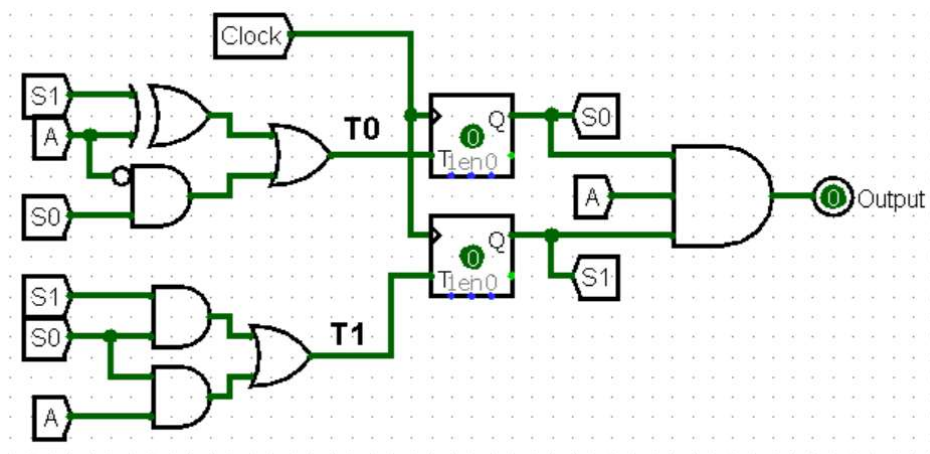
State Transition Table

Current State $S_1 S_0$		Input $A$	Next State $S_1' S_0'$		Output $Y$	$T_1$	$T_0$
0	0	0	0	0	0	0	0
0	0	1	0	1	0	0	1
0	1	0	0	0	0	0	1
0	1	1	1	0	0	1	1
1	0	0	1	1	0	0	1
1	0	1	1	0	0	0	0
1	1	0	0	0	0	1	1
1	1	1	0	1	1	1	0

K-Map Simplification (Output  $Y = S_1 S_0 A$ )



Logic Diagram



### Ans 3:

#### Average of history of temperatures stored in 4 8-bit registers

Method for Division: Shift the bits of the sum twice to the right. This is equivalent to division by 4. We are calculating only quotient but not remainder.

#### Circuit Notation

**Clock** stands for Clock

**Hist\_En**, if high, enables entry of a new temperature

**New Value**, to input new temperature reading for storing in registers

**Sum\_En**, if high, calculates sum of temperatures stored in current clock cycle

**Load**, if high loads sum of temperatures of current clock cycle, into the shift register

**Shift**, is the bit that is placed at shift register MSB while shifting bits for division

**Registers 1,2,3,4** store history of temperatures

**Reset\_hist**, erases all data stored in registers 1,2,3,4

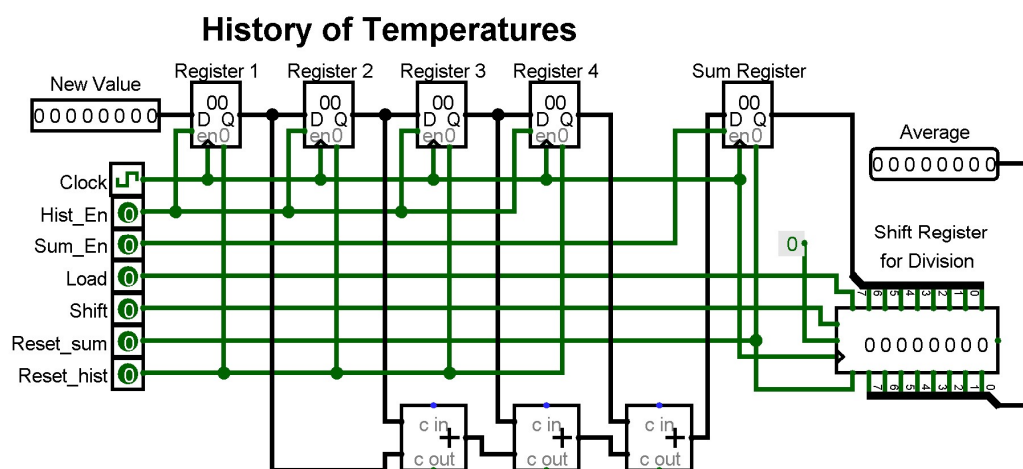
**Reset\_sum**, erases sum for calculating it once again for different temperatures in the next iteration

**Sum Register** stores the sum of temperatures stored in registers 1 to 4

**Shift Register** is used for dividing the sum in Sum Register

**Average** pin shows average of the temperatures in registers 1 to 4

#### Circuit Diagram

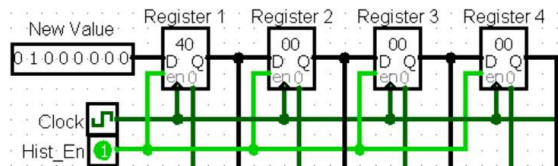


#### Test Run

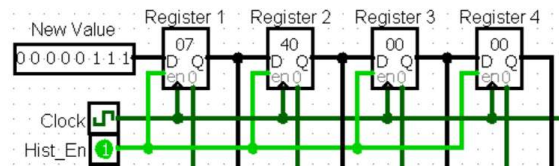
1. Initially, there is nothing stored in the registers.
2. Set **New\_Value** = 0100 0000, **Hist\_En** = 1, and toggle the clock. The value is stored in Register 1.



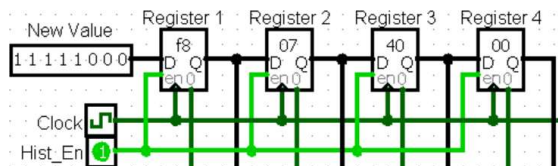
- Set **New\_Value** = 0000 0111 and toggle the clock. The value is stored in Register 1 and previous value is shifted to register 2.
- Set **New\_Value** = 1111 1000, and toggle the clock. The value is stored in Register 1 and previous values are shifted towards right side.
- Set **New\_Value** = 1001 1001, and toggle the clock. The value is stored in Register 1 and previous values are shifted towards right side.



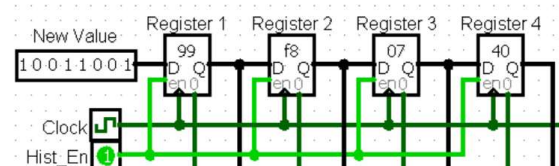
After Step 1



After Step 2



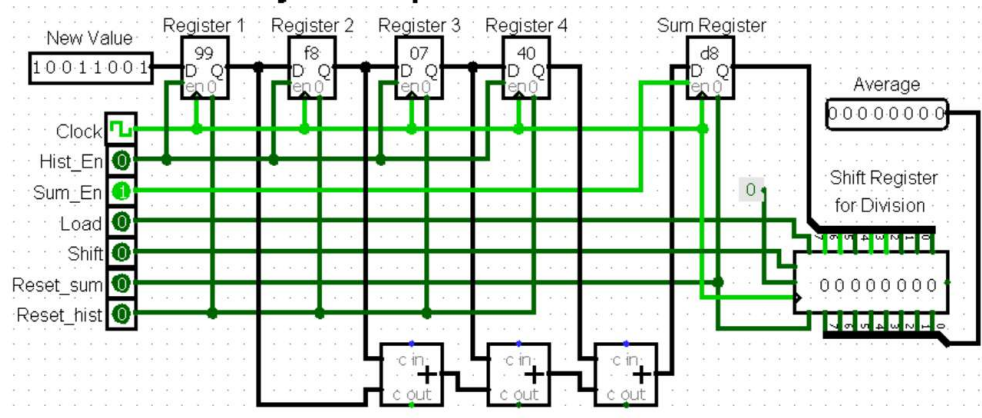
After Step 3



After Step 4

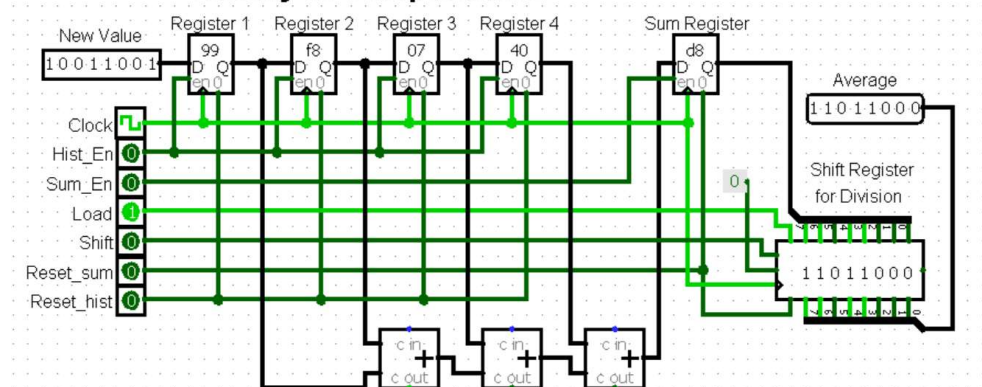
- Now, set **Hist\_En** = 0, **Sum\_En** = 1 and toggle the clock. The sum of all temperatures present in the registers at this moment, is stored in Sum Register.

### History of Temperatures

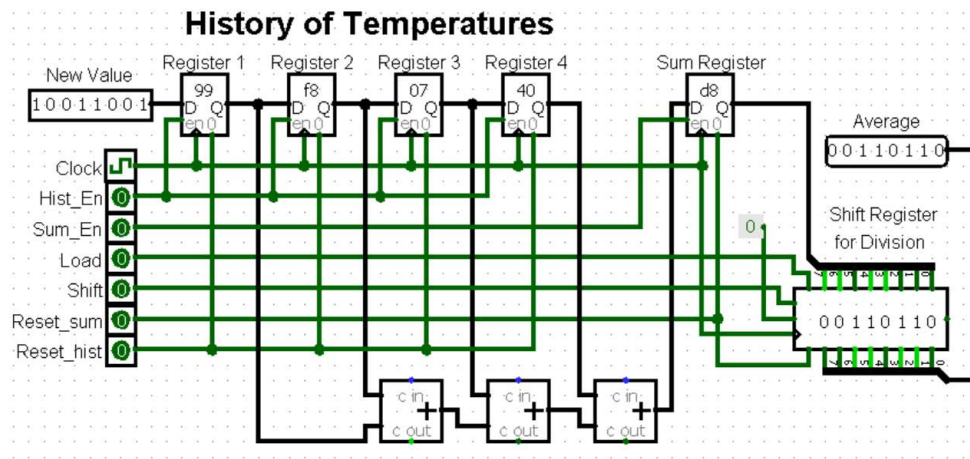


- Set **Sum\_En** = 0, **Load** = 1 and toggle the clock. Sum is loaded into shift register.

### History of Temperatures



- Set **Load** = 0, **Shift** = 1 and toggle the clock twice. The output shows the average values of the temperatures stored in the registers for current clock cycle. Set Shift = 0 before further use.



9. To store a new temperature value, set **New\_Value** to desired value, **Hist\_En** = 1, and toggle the clock.
10. To re-calculate the average, set **Reset\_sum** = 1 to clear previous sum, **Sum\_En** = 1, and toggle the clock. Now load the new sum into shift register and calculate the average as mentioned in steps 7,8,9.
11. To erase all stored values after step 8, set **Reset\_sum** = 0 and **Reset\_hist** = 0.

