

1) a)

RA $\Pi_{\text{Fname, Mname, Lname, Address}} \left(\sigma_{\text{Dname} = \text{"Research"}} (\text{Employee} \bowtie \text{Department}) \right)$

TRC $\{t \mid \exists e \in \text{Employee} (t[\text{Fname}] = e[\text{Fname}] \wedge t[\text{Mname}] = e[\text{Mname}]$
 $\wedge t[\text{Lname}] = e[\text{Lname}] \wedge t[\text{Address}] = e[\text{Address}]$
 $\wedge \exists d \in \text{Department} ($
 $d[\text{Dname}] = \text{"Research"}$
 $\wedge d[\text{Dnumber}] = e[\text{Dnumber}]))\}$

DRC $\{ \langle f, m, l, a \rangle \mid \exists \text{ssn, bd, s, sal, dn} (\langle f, m, l, \text{ssn, bd, a, s, sal, dn} \rangle \in \text{Employee}$
 $\wedge \exists \text{dname, mgrssn, mgrsd} ($
 $\langle \text{dname, mgrssn, mgrsd, dn} \rangle \in \text{Department}$
 $\wedge \text{dname} = \text{"Research"})\}$

1) b) Π

\boxed{RA}

Π

$(Project \bowtie Department \bowtie Employee)$
 $(Plocation = "Delhi") \wedge (MgrSSN = SSN)$
 $Pnumber, Dnumber, Lname, Bdate, Address$

$\boxed{TRC} \{ t \mid \exists p \in Project (t[Pnumber] = p[Pnumber] \wedge$
 $t[Dnumber] = p[Dnumber] \wedge p[Plocation] = "Delhi" \wedge$
 $\exists d \in Department (p[Dnumber] = d[Dnumber] \wedge$
 $\exists e \in Employee (t[Lname] = e[Lname] \wedge t[Bdate] = e[Bdate] \wedge$
 $t[Address] = e[Address] \wedge$
 $e[Dnumber] = d[Dnumber] \wedge e[SSN] = d[MgrSSN])))) \}$

$\boxed{DRC} \{ \langle pn, dn, ln, bd, ad \rangle \mid \exists pN (\langle pN, \underline{pn}, \underline{"Delhi"}, \underline{dn} \rangle \in Project \wedge$
 $\exists DN, mgrssn, mgrsd (\langle DN, \underline{mgrssn}, \underline{mgrsd}, dn \rangle \in Department \wedge$
 $\exists fn, mn, sex, sal (\langle fn, mn, \underline{ln}, \underline{mgrssn}, \underline{bd}, \underline{ad}, sex, sal, dn \rangle \in Employee)) \}$

1) c)

$$\boxed{\text{RA}} \quad \pi_{\text{Fname, Mname, Lname}}(\text{Employee}) - \pi_{\text{Fname, Mname, Lname}}(\sigma_{\text{SSN}=\text{ESSN}}(\text{Employee} \times \text{Dependent}))$$

$$\boxed{\text{TRC}} \quad \{t \mid e \in \text{Employee} (t[\text{Fname}] = e[\text{Fname}] \wedge t[\text{Mname}] = e[\text{Mname}] \\ \wedge t[\text{Lname}] = e[\text{Lname}] \\ \wedge \text{not } \exists d \in \text{Dependent} (\\ d[\text{ESSN}] = e[\text{SSN}]))\}$$

$$\boxed{\text{DRC}} \quad \{ \langle \text{fn, mn, ln} \rangle \mid \exists \text{ssn, bd, a, sex, sal, dn} (\\ \langle \text{fn, mn, ln, ssn, bd, a, sex, sal, dn} \rangle \in \text{Employee} \\ \wedge \text{not } \exists \text{DN, Sex, Bdate, Rel} (\\ \langle \text{ssn, DN, Sex, Bdate, Rel} \rangle \in \text{Dependent})) \}$$

1) d)

$$\boxed{RA} \quad \Pi_{\text{Frame, Mname, Lname}} \left(\left(\text{Employee} \bowtie \rho_{x(\text{SSN})} \left(\Pi_{\text{MgrSSN}}(\text{Department}) \right) \right) \bowtie \rho_{y(\text{SSN})} \left(\Pi_{\text{ESSN}}(\text{Dependent}) \right) \right)$$

$$\boxed{TRC} \quad \{ t \mid \exists e \in \text{Employee} (\exists d \in \text{Department} (\exists D \in \text{Dependent} (\\ t[\text{Frame}] = e[\text{Frame}] \wedge \\ t[\text{Mname}] = e[\text{Mname}] \wedge \\ t[\text{Lname}] = e[\text{Lname}] \wedge \\ e[\text{SSN}] = D[\text{ESSN}] \wedge D[\text{ESSN}] = d[\text{MgrSSN}]))) \}$$

$$\boxed{DRC} \quad \{ \langle fn, mn, ln \rangle \mid \exists ssn, x_1, x_2, x_3, x_4, x_5 (\langle fn, mn, ln, ssn, x_1, x_2, x_3, x_4, x_5 \rangle \\ \in \text{Employee} \\ \wedge \exists y_1, y_3, y_4 (\langle y_1, ssn, y_3, y_4 \rangle \in \text{Department} : \\ \wedge \exists q_2, q_3, q_4, q_5 (\langle ssn, q_2, q_3, q_4, q_5 \rangle \\ \in \text{Dependent}))) \}$$

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2) a) i)

$$\boxed{\text{RA}} \quad \Pi_{\text{Id}} \left(\sigma_{\text{Title} = \text{"Discrete Structures"} \wedge \text{SID} = \text{Id} \wedge \text{Major} = \text{MATH}} (\text{Enroll} \bowtie \text{Course}) \times \text{Student} \right)$$

$$\boxed{\text{TRC}} \quad \{ t \mid \exists s \in \text{Student} (t[\text{Id}] = s[\text{Id}] \wedge s[\text{Major}] = \text{MATH} \\ \wedge \exists e \in \text{Enroll} (e[\text{SID}] = s[\text{Id}] \\ \wedge \exists c \in \text{Course} (c[\text{Title}] = \text{"Discrete Structures"} \\ \wedge c[\text{Dept}] = e[\text{Dept}] \\ \wedge c[\text{Num}] = e[\text{Num}])))) \}$$

2) a) ii)

$$\boxed{\text{RA}} \quad \Pi_{\text{Date}} \left(\sigma_{\text{Title} = \text{"Database Design"}} (\text{Enroll} \bowtie \text{Course}) \right)$$

$$\boxed{\text{TRC}} \quad \{ t \mid \exists e \in \text{Enroll} (t[\text{Date}] = e[\text{Date}] \\ \wedge \exists c \in \text{Course} (c[\text{Dept}] = e[\text{Dept}] \\ \wedge c[\text{Num}] = e[\text{Num}] \\ \wedge c[\text{Title}] = \text{"Database Design"})) \}$$

2) b) i)

$$\boxed{\text{RA}} \quad \Pi_{\text{Title}} \left(\sigma_{\text{Major}=\text{Dept} \wedge \text{Dept}=\text{Abbrev} \wedge \text{DeptName}=\text{"Education"}} (\text{Course} \times \text{Dept} \times \text{Student}) \right)$$

$$\boxed{\text{DRC}} \quad \{ \langle \text{title} \rangle \mid \exists d, n (\langle d, n, \text{title} \rangle \in \text{Course} \wedge \\ \exists \text{office} (\langle d, \text{"Education"}, \text{office} \rangle \in \text{Dept} \wedge \\ \exists \text{id}, \text{sn} (\langle \text{id}, \text{sn}, d \rangle \in \text{Student}))) \}$$

2) b) ii)

$$\boxed{\text{RA}} \quad \Pi_{\text{Office}} \left(\sigma_{\text{Dept}=\text{Abbrev} \wedge \text{Dept}=\text{MATH} \wedge \text{Num}=243} (\text{Course} \times \text{Dept}) \right)$$

$$\boxed{\text{DRC}} \quad \{ \langle \text{office} \rangle \mid \exists t (\langle \text{MATH}, 243, t \rangle \in \text{Course} \wedge \\ \exists n (\langle \text{MATH}, n, \text{office} \rangle \in \text{Dept})) \}$$