

CS203^y Algorithms Mid-Semester Exam-2014

Note:- Answer according to order & all parts of question be together.

Time: 2hrs Min:40

1. (a) Give an example of comparison-based-sorting having average case time $O(n \log n)$ with stable property. (b) Illustrate with suitable example of Quick-sort of not satisfying stable property. [4]
2. (a) Define a universal hash function. (b) Prove that defined universal class of hash functions is universal. [6]
3. Prove that using Randomized-Partition Algorithm, the randomized-quicksort expected running time is $O(n \log n)$. [6]
4. Prove that the problem of selecting the i^{th} order statistics from a set of n numbers using Randomized-Select is done in $O(n)$ expected running time [6]
5. Prove that Red-Black Tree with n internal nodes has height atmost $2 \log(n+1)$. [5]
6. (a) Briefly describe Skip-lists. (b) What is the running time of search operation on Skip List? [5]
7. Write down short notes on following topics:-
(a) The problem of selecting the i^{th} order statistics from a set of n numbers in $O(n)$ running time in worst case. (b) Perfect hashing [4+4]