

Surprise Test

Ans 1: I have taken the following assumptions for this question.

- $[3]$ is made unambiguous by use of paranthesis
- Only include symbols \wedge, \vee, \sim for simplicity
- Denote truth value as $\underset{\substack{\downarrow \\ \text{model}}}{m[a]}$

fun PL-TRUE?(s, m):

① LHS = " RHS = " logic_op = "

② Scan s from left to right, ~~for~~ :
look for a $\wedge, (, \text{ or } \sim$ symbol.

③ If symbol found, LHS = symbol, goto line 4

④ else if \sim found, logic_op = \sim , goto line 2

else if left parenthesis, ~~(~~ (is found:

set $n = 1$

while ($n > 0$): { LHS += next_char
if next_char = $)$: $n--$;
else if $($: $n++$;

- ④ If $\text{logic_op} = \text{"}$, $\text{logic_op} = \text{not_ch}$.
- ⑤ Repeat ③, ④ & replace LHS with RHS
- ⑥ If LHS or RHS is not symbol,
 $\text{LHS} = \text{PL_TRUE}(\text{LHS}, m)$
 $\text{RHS} = \text{PL_TRUE}(\text{RHS}, m)$
- ⑦ If $\text{logic_op} = \sim$:
return true if LHS is false,
else return false
- ⑧ Else if $\text{logic_op} = \wedge$
return true if LHS & RHS are true
else false
- ⑨ else if $\text{logic_op} = \vee$
return true if LHS or RHS are true
else false

Ans 2:

Examples of sentences:

① true

② $A \vee \text{true}$

③ false

Ans 3: In the partial model \mathcal{M} , assume that \mathcal{K} is the no. of symbols is \mathcal{S} do not appear.

~~to~~ Despite the truth-table of the symbols in the sentence, some sentences will be always true or always false.

So, the only way to be sure is to evaluate ^{all} the rows of the truth table one-by-one, and check

which one is true & false, to determine the sentence's truth value.

But due to the existence of always true & always false sentences, in the worst case $O(2^k)$ operation to determine sentence's truth value

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Last Page