

1)

Assumptions:

- (i) The sentence  $s$  is made unambiguous by the use of parentheses.
- (ii) For brevity, we only include the symbols  $\wedge$ ,  $\vee$  and  $\neg$
- (iii) We use  $m[a]$  to denote the True/False value of  $a$  in model  $m$ .

Function: PL-True? ( $\wedge, \vee, m$ )

↳ returns True/  
False

a) Let LHS = " , RHS = " , logic  
operator = "

b) Scan  $s$  from left to right,  
looking for a  $\neg$ , left parenthesis  
or symbol.

c) If symbol found, LHS = symbol,  
go to 11

d) If  $\rightarrow$  found, logic - operator =  $\rightarrow$ .  
Go to 2.

c) If left ( found :

Let  $n=1$

while  $n > 0$  :

LHS += next character

if next char =  $)$  :  $n = n - 1$

If next char ==  $($  :  $n = n + 1$

f) If logic operator == " $\rightarrow$ ", logic - operator  
= next character.

g) Repeat lines 3-11, replacing LHS  
and  
RHS

h) If LHS or RHS is not a symbol,  
 $LHS = PL\_TRUE?(LHS, m)$ ,  
 $RHS = PL\_TRUE?(RHS, m)$

(i) If logic - operator ==  $\neg$ :  
Return (True) if LHS is  
False,  
False otherwise.

(j) Else if logic - operator ==  $\wedge$ :  
Return (True) if LHS and RHS  
are both true,  
False otherwise.

(k) Else if logic - operator ==  $\vee$ :  
Return (True) if either LHS/RHS  
are equal to (True),  
False otherwise

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2)

(i) True

(ii) False

(iii) For All  $\forall$  True

Let  $k$  be number of symbols in  $S$  that do not appear in the partial model  $m$ .

Some sentences are always True or always False, no matter the Truth-Table assignment of the symbols in the sentence.

The only way to be sure is to evaluate the  $2^k$  rows of the truth table 1 by 1, waiting to see one true and one False evaluation, to determine if the sentence has Truth value.

However, due to the existence of Always True/False sentences, the worst case is  $O(2^k)$ .