Probability and non-probability sampling

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	Sampling	Interviews	Data environment
1st era	Area probability	Face-to-face	Stand-alone
2nd era	Random digital dial probability	Telephone	Stand-alone
3rd era	Non-probability	Computer-administered	Linked

Probability Samples

$$P(u_i) = \frac{p_i}{(N-1)\cdots(N-n+1)}\binom{N-1}{n-1}(n-1)!$$
$$+\sum_{j\neq i}^{N}\frac{p_j}{(N-1)\cdots(N-n+1)}\binom{N-1}{n-1}(n-1)!\,\frac{n-1}{N-1},$$

which upon simplification becomes

$$(19)\qquad P(u_i) = \frac{N-n}{N-1}p_i + \frac{n-1}{N-1}, \qquad (i = 1, 2, \cdots, N).$$

Similarly, it may be shown that for this case

$$(20)\qquad P(u_iu_j) = \frac{n-1}{N-1}\left[\frac{N-n}{N-2}(p_i+p_j) + \frac{n-2}{N-2}\right],$$
$$(i \neq j\colon i, j = 1, 2, \cdots, N).$$

Non-Probability Samples

http://www.chicagotribune.com/news/nationworld/politics/chi-chicagodays-deweydefeats-story-story.html

Probability Samples

unknown sampling process
weighting based on unverifiable assumptions

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- Not all probability samples look like miniature versions of the population
- But, with appropriate weighting, probability samples can yield unbiased estimates of the frame population

Main insight from probability samples:

- How you collect your data impacts how you make inference
- Focus on properties of estimators not properties samples

$$\hat{\bar{y}} = \frac{\sum_{i \in s} y_i/\pi_i}{N}$$

where π_i is person i's probability of inclusion

Sometimes called:

- Horvitz-Thompson estimator
- π estimator

Inference from probability samples in theory

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$$\hat{\bar{y}} = \frac{\sum_{i \in s} y_i / \hat{\pi}_i}{N}$$

where $\hat{\pi}_i = \frac{n_g}{N_g} \quad \forall \quad i \in g$ (estimated probability of inclusion)

Requires:

- auxiliary information (N_g)
- ability to place respondents in groups
- assumptions

- Key to many adjustment methods is to use external information and make assumptions

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- If external information is incorrect or assumptions are wrong, then you can make things worse (but it usually seems to make things better)

Imagine that you want to estimate the average height of Princeton students.

- Assume 50% are male and 50% are female
- You stand outside Lewis Library and recruit 60 Princeton students
- Males (n= 20): Average height: 180cm
- Females (n=40): Average heigh: 170cm

What is your estimate of the average height? (think-pair-share)

- sample mean $= 173.3\text{cm}$ $\left(\frac{180*20+170*40}{20+40}\right)$

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How could this go wrong?

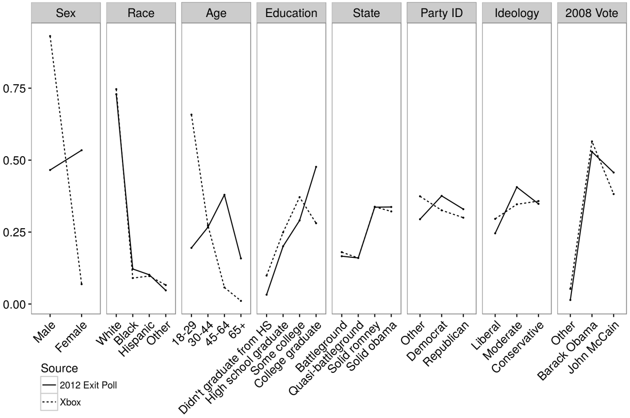
Forecasting elections with non-representative polls

Wei Wang [a,*], David Rothschild [b], Sharad Goel [b], Andrew Gelman [a,c]

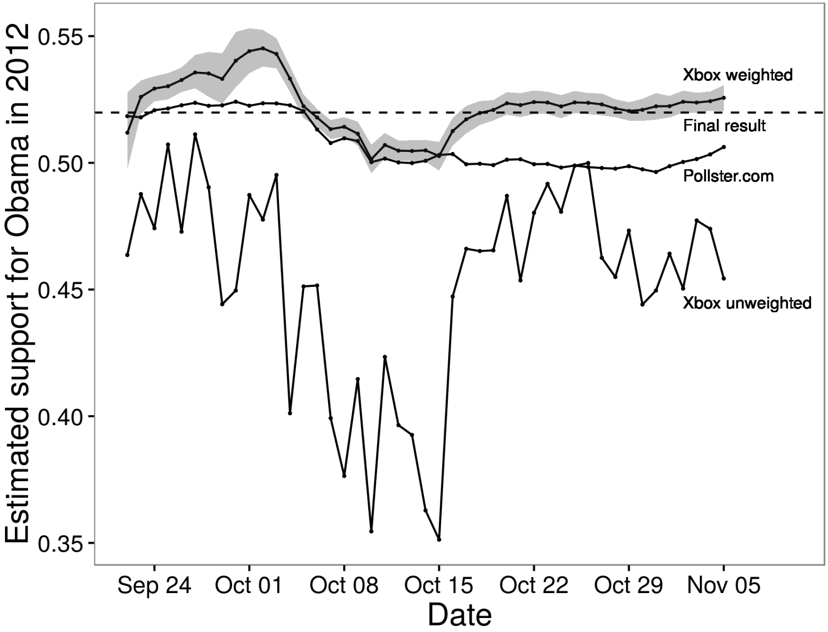
[a] *Department of Statistics, Columbia University, New York, NY, USA*

[b] *Microsoft Research, New York, NY, USA*

[c] *Department of Political Science, Columbia University, New York, NY, USA*



- about 750,000 interviews
- about 350,000 unique respondents


Estimated support for Obama in 2012
0.55
0.50
0.45
0.40
0.35
Xbox weighted
Final result
Pollster.com
Xbox unweighted
Sep 24
Oct 01
Oct 08
Oct 15
Oct 22
Oct 29
Nov 05
Date

Online, Opt-in Surveys: Fast and Cheap, but are they Accurate?

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David Rothschild
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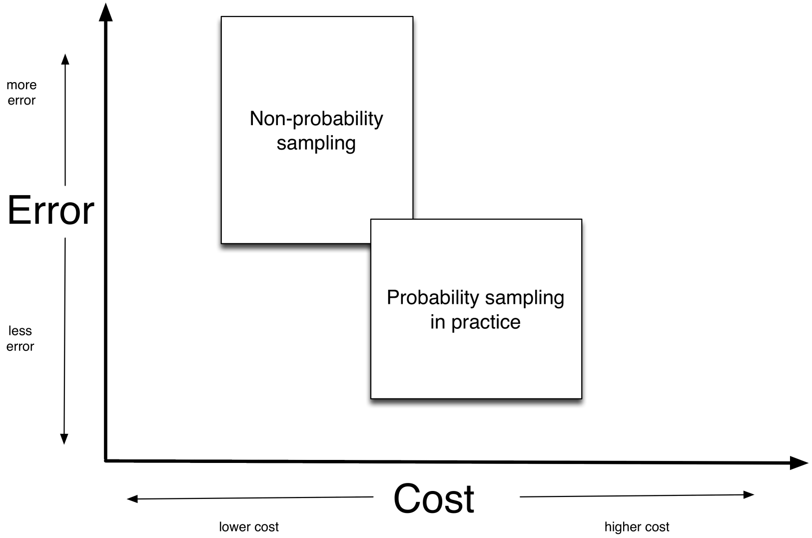
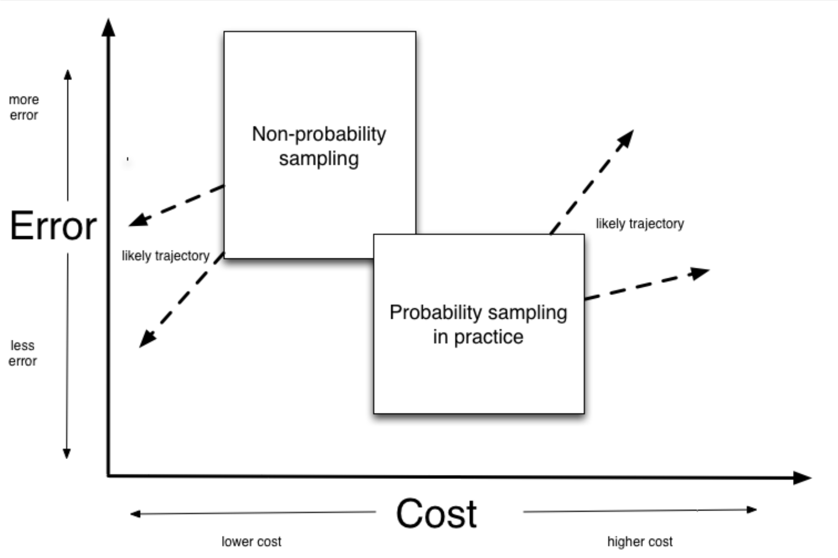

Non-probability sampling
Probability sampling in practice
more error
Error
less error
Cost
lower cost
higher cost



more error
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Non-probability sampling
likely trajectory
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Probability sampling in practice
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- Key to making good estimates is for estimation process to account for the sampling process
- There is not a bright-line difference between probability sampling in practice and non-probability sampling
- To learn more: Lohr (2009) or Sandal et al (2013)