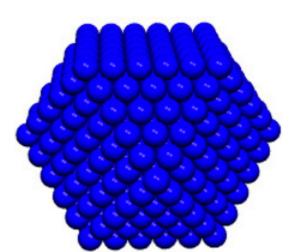
Sphere Packing with Julia

by Kirby Urner



My pedagogy around teaching any computer language is to have the target language e.g. Python on the front burner but then compare and contrast with one or more back burner languages e.g. Julia, Clojure...

Replit makes it easy to walk my talk in this respect.

I'm eager to demonstrate starting a new Jupyter Notebook and having a choice among languages: Ju for Julia, Pyt for Python, Er for R.

The focus is ball packing: triangular and square numbers (figurate on a plain (plane)); tetrahedral and cuboctahedral (= icosahedral) in space.

A student is co-developing a lexical skill (coding language) with a graphical skill (visualizing balls packing in space).

Triangular Numbers

Triangular Numbers 1,3,6,10

```
Integer = 10
```

```
# Triangular Numbers
# https://oeis.org/A000217
tri = n \rightarrow ((n == 0) ? 0 : n + tri(n - 1)) # recursive
println("A000217:", [tri(x) for x in 0:10])
```

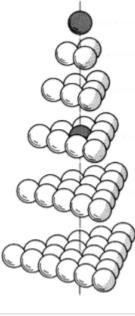
Alternative function syntax, as well as a different algorithm:

A000217:[0, 1, 3, 6, 10, 15, 21, 28, 36, 45, 55]

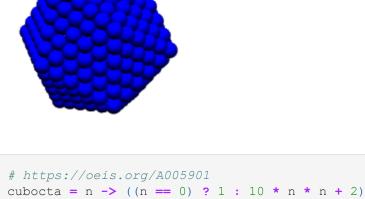
A000217:[0, 1, 3, 6, 10, 15, 21, 28, 36, 45, 55]

```
function tri2(n)
 Int (n * (n + 1) / 2)
end
println("A000217:", [tri2(x) for x in 0:10])
```

Tetrahedral Numbers



```
# https://en.wikipedia.org/wiki/Tetrahedral number
 # https://oeis.org/A000292
 function tetra(n)
    Int ((n * (n + 1) * (n + 2))/6)
 println("A000292:", [tetra(x) for x in 1:10])
A000292:[1, 4, 10, 20, 35, 56, 84, 120, 165, 220]
Cuboctahedral Numbers ( = Icosahedral Numbers)
```



In [4]:

```
println("A005901:",[cubocta(x) for x in 0:10])
A005901:[1, 12, 42, 92, 162, 252, 362, 492, 642, 812, 1002]
Just as tetrahedral numbers may be viewed as cumulative triangular numbers, so may we accumulate
successive layers (1, 12, 42, 92...) in the cuboctahedral packing (1, 13, 55, 147...).
```

```
# https://oeis.org/A005902
accum cubocta(n) = (
  (n == 0) ? 1 :
```

```
cubocta(n) + accum cubocta(n-1)) # recursive
println("A005902:", [accum cubocta(x) for x in 0:10])
A005902:[1, 13, 55, 147, 309, 561, 923, 1415, 2057, 2869, 3871]
 # http://www.4dsolutions.net/ocn/sphpack2.html
{\it \# http://www.4d} solutions.net/synergetica/synergetica2.html
function accum_cubocta2(n)
```

Int(round($(10/3)*n^3 + 5*n^2 + (11/3)*n + 1$, digits=0))

```
println("A005902:",[accum_cubocta2(x) for x in 0:10])
A005902:[1, 13, 55, 147, 309, 561, 923, 1415, 2057, 2869, 3871]
```



Tomb of Ayatollah Khomeini (سید روحالله موسوی خمینی) with an octet truss as a part of its architectural design. Relevant Readings:

- Gnomon by Midhat Gazale The Book of Numbers by Conway and Guy
- Synergetics by Buckminster Fuller