

1.2 Set Representation and Manipulation

Notebook: Discrete Mathematics [CM1020]

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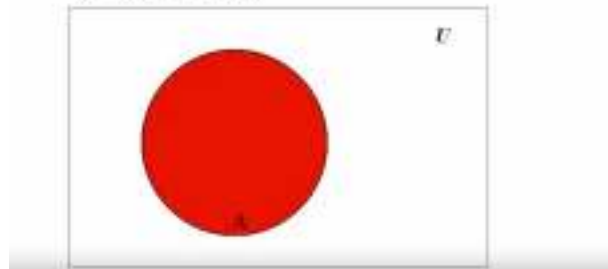
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Tags: Complement, Disjoint, Partition, Universal, Venn

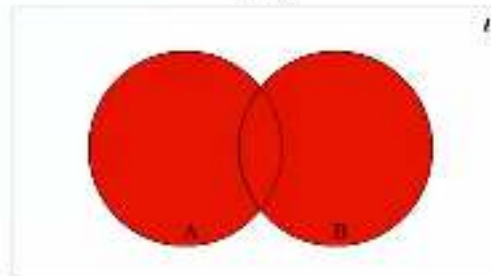
Cornell Notes	Topic: 1.2 Set Representation and Manipulation	Course: BSc Computer Science
		Class: Discrete Mathematics-Lecture
		Date: October 14, 2019
Essential Question:		
What is the visual representation of a set and on the other hand how can the said set be manipulated and partitioned?		
Questions/Cues:		
<ul style="list-style-type: none">• What is the universal set?• What is a Venn Diagram?• What is a compliment of a set?• What is the union of a set and its complement?• What is the Venn Diagram Representation of the union, intersection, set difference and symmetric difference of two sets?• What are De Morgan's Laws?• What is De Morgan's first and second law?• What is the Set identity of Commutativity?• What is the Set identity of Associativity?• What is the set identity of Distributivity?• What is the partition of an object?• What are disjoint sets?• What is the partition of a set?		
Notes		
<ul style="list-style-type: none">• Universal Set = set containing everything, denoted by U• Venn Diagram = to visualize possible relations among collection of sets		

U is called the universal set and it contains everything.
 $A \subset U$ (A is in red).

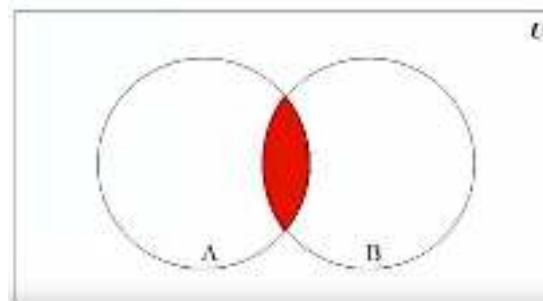


- Given A , Complement of \overline{A} = contains all elem. in U , not in A
 - $\overline{A} = U - A$
- $\overline{A} \cup A = U$

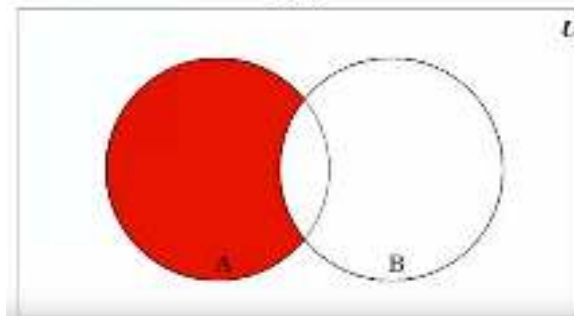
$A \cup B$



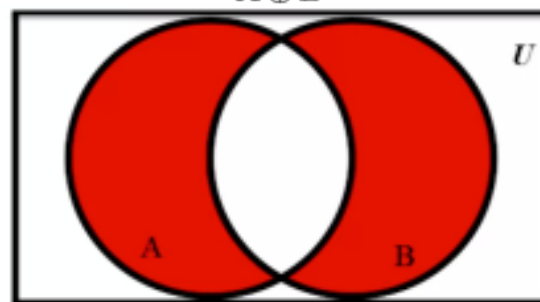
$A \cap B$



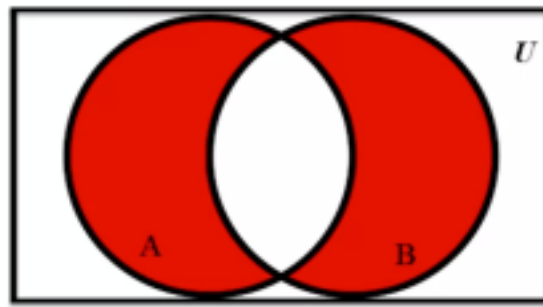
$A - B$



$A \oplus B$



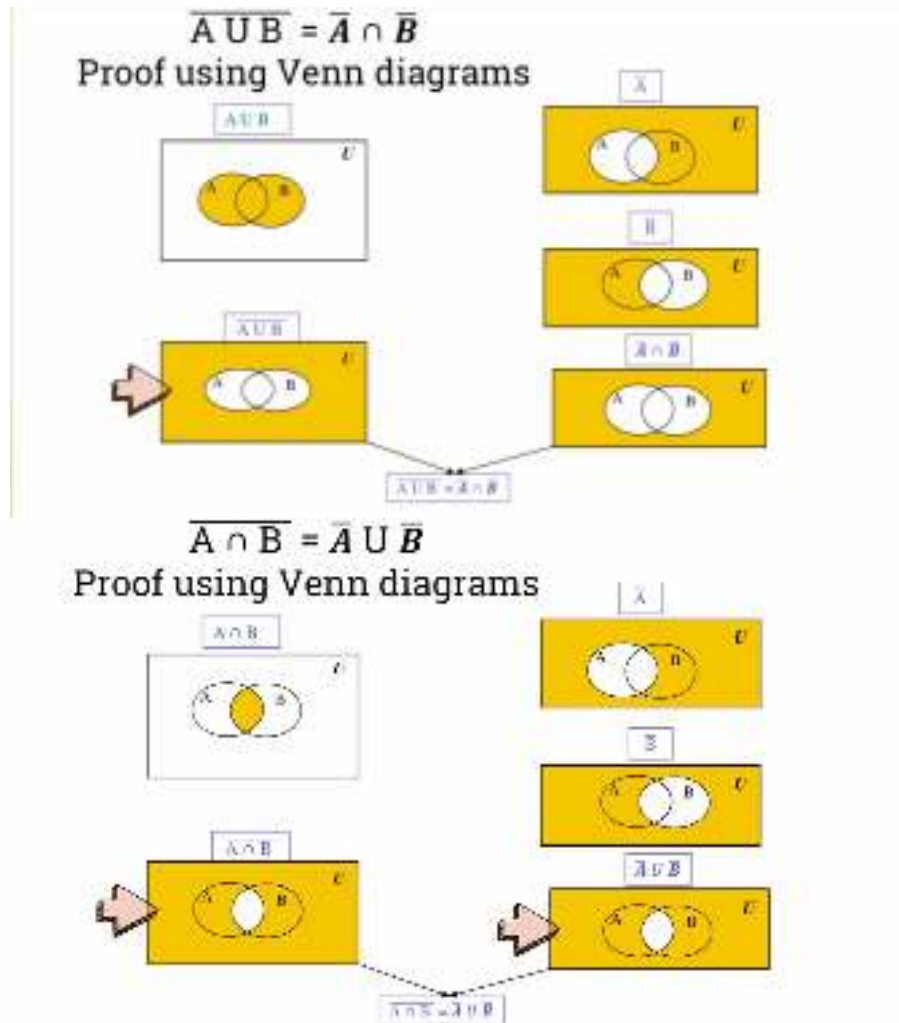
$A \cup B - (A \cap B)$



- De Morgan's Laws = how math statements and concepts related through their opposites
 - In set theory, DMLs relate to intersection and union of set through their complements

$$\overline{A \cup B} = \bar{A} \cap \bar{B}$$

- $\overline{A \cap B} = \bar{A} \cup \bar{B}$



- Commutativity = operation in which order of element doesn't affect result
 - $A \cup B = B \cup A$
 - $A \cap B = B \cap A$
 - $A \oplus B = B \oplus A$
 - Set difference is **NOT** commutative, $A - B \neq B - A$

- Associativity = grouping of elements in operation, where the grouping doesn't effect the result
 - $(A \cup B) \cup C = A \cup (B \cup C)$
 - $(A \cap B) \cap C = A \cap (B \cap C)$
 - $(A \oplus B) \oplus C = A \oplus (B \oplus C)$
 - Set difference is **NOT** associative, $(A - B) - C \neq A - (B - C)$
- Distributivity = multiplying a sum by number gives same result as multiplying each # and adding the products together
 - $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
 - $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

Union	Name	Intersection
$A \cup B = B \cup A$	commutative	$A \cap B = B \cap A$
$(A \cup B) \cup C = A \cup (B \cup C)$	associative	$(A \cap B) \cap C = A \cap (B \cap C)$
$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$	distributive	$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
$\overline{A \cup B} = \overline{A} \cap \overline{B}$	De Morgan's laws	$\overline{A \cap B} = \overline{A} \cup \overline{B}$
$A \cup \emptyset = A$ $A \cup U = U$	identities	$A \cap \emptyset = \emptyset$ $A \cap U = A$
$A \cup \overline{A} = U$ $\overline{\overline{A}} = A$	complement	$A \cap \overline{A} = \emptyset$ $\overline{\emptyset} = U$
$\overline{\overline{A}} = A$	double complement	
$A \cup (A \cap B) = A$	absorption	$A \cap (A \cup B) = A$
$A - B = A \cap \overline{B}$	set difference	

Show that: $(A \cap B) \cup \overline{B} = B \cap \overline{A}$

$$\begin{aligned}
 \overline{(A \cap B) \cup \overline{B}} &= \overline{(A \cap B)} \cap \overline{\overline{B}} && \text{De Morgan's law} \\
 &= \overline{(A \cap B)} \cap B \\
 &= \overline{(A \cup \overline{B})} \cap B && \text{De Morgan's law} \\
 &= B \cap \overline{(A \cup \overline{B})} && \text{commutative} \\
 &= (B \cap \overline{A}) \cup (B \cap \overline{\overline{B}}) && \text{distributive} \\
 &= (B \cap \overline{A}) \cup \emptyset \\
 &= B \cap \overline{A}
 \end{aligned}$$

- Partition of an obj = a subdivision of obj into parts, so that parts are completely separated from each other, yet together they form whole object
- Dis-joint sets = A and B are disjoint $\leftrightarrow A \cap B = \emptyset$
- Partition of Set = Partit. of A is set of subsets A_i of A
 - all subsets A_i are disjointed

- the union of all subsets $A_i = A$

Summary

In this week, we learned that sets can be visually represented by Venn Diagrams, manipulated by set identities to be simplified and subdivided into partitions to represent segments of a whole set.