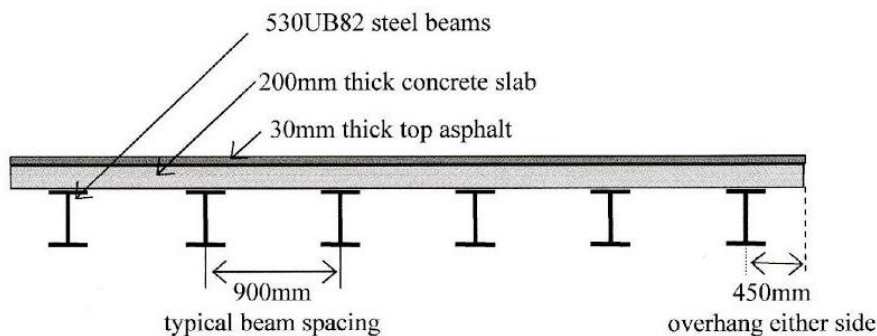


beams span 30m between column supports. The structure cross-section is shown in Figure 1. The bridge carries a traffic live load of 3kPa over its full area.

(a) Calculate the dead and live loads in kN/m for a single 30m spanning beam. Combine dead and live loads to calculate (i) the serviceability limit state load in kN/m for each beam, assuming load factors of 1.0 and 0.7 for the dead and live loads respectively and (ii) the ultimate limit state load in kN/m for each beam, assuming load factors of 1.2 and 1.5 for the dead and live loads respectively. (90%)

(b) Explain the difference between ultimate and serviceability limit state design. (10%)

Density of steel =  $78.5 \text{ kN/m}^3$       Density of concrete =  $24 \text{ kN/m}^3$ .  
Density of asphalt =  $20 \text{ kN/m}^3$       Assume  $1 \text{ kg} \approx 10 \text{ N}$ .



**Figure 1: Bridge Cross-section**

$$\begin{aligned} \text{a) } DL &= \text{conc} + \text{asphalt} + \text{beam} \\ &= 24 \times 0.2 \times 0.9 + 20 \times 0.03 \times 0.9 + 0.82 \text{ kN/m} \\ &= 4.32 \text{ kN/m} + 0.54 \text{ kN/m} + 0.82 \text{ kN/m} \\ &= \underline{5.68 \text{ kN/m}} \end{aligned}$$

$$LL = 3 \text{ kPa} \times 0.9 \text{ m} = \underline{2.7 \text{ kN/m}}$$

$$SLS = DL + 0.7LL = \underline{7.57 \text{ kN/m}}$$

$$ULS = 1.2DL + 1.5LL = \underline{10.87 \text{ kN/m}}$$

ie buckling  
or yield

b) ULS design - is design against Failure, where you carry out a strength check.  
ULS Load =  $1.2DL + 1.5LL$

SLS design is design against excessive deflection where you check the structure does not deflect too much (eg. span/250) SLS Load =  $DL + 0.7LL$

a) A timber plank, 150 mm thick, 3 m wide and 6 m long, is supported by two equally loaded steel beams, each 9 m long. The structure is shown in Figure 1(a). The timber plank supports a uniformly distributed live load of  $3 \text{ kN/m}^2$  as shown in the Figure. The steel beams each directly carry a live load of  $4 \text{ kN/m}$  at one of their ends. Density of timber =  $15 \text{ kN/m}^3$ ; self-weight of the steel beam =  $100 \text{ kg/m}$ . Calculate the Ultimate limit state design loads in  $\text{kN/m}$ , on each beam by applying the appropriate load factors and show this on a beam diagram. (6marks)

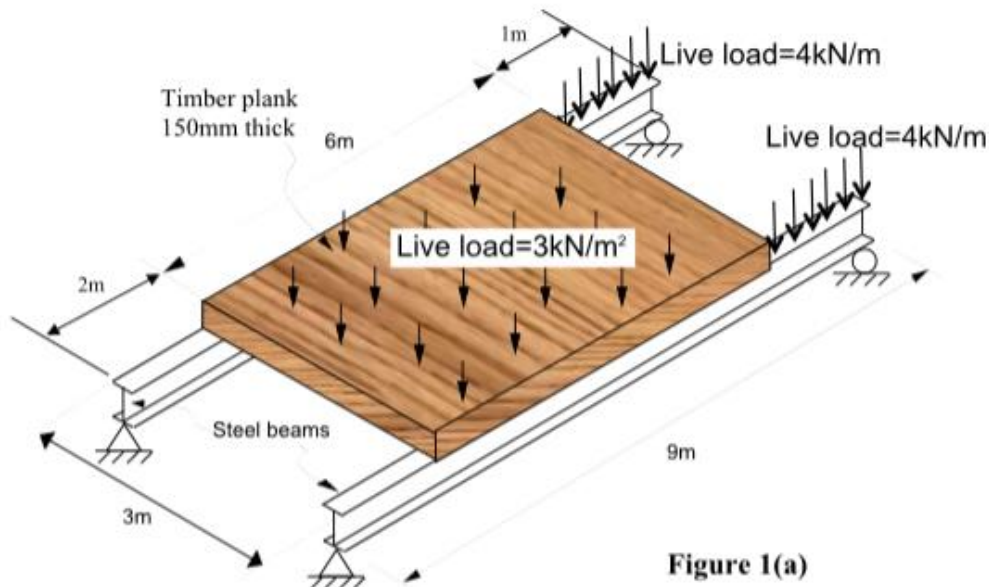
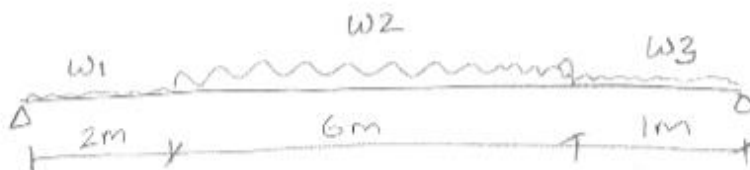


Figure 1(a)

$$a) \begin{cases} \text{timber plank (kN/m)} = 15 \times 1.5 \times 0.15 = 3.375 \text{ kN/m} \\ \text{DL steel beam (kN/m)} = 1 \text{ kN/m} \end{cases}$$

$$LL \begin{cases} 3 \times 1.5 = 4.5 \text{ kN/m} \\ 4 \text{ kN/m} \end{cases}$$



$$w_1 = 1.2(1) + 0 = 1.2 \text{ kN/m}$$

$$w_2 = 1.2(1 + 3.375) + 1.5(4.5) = 12 \text{ kN/m}$$

$$w_3 = 1.2(1) + 1.5(4) = 7.2 \text{ kN/m}$$